Data Augmentation for Deep Learning

Summary:

- 1. SimpleITK supports a variety of spatial transformations (global or local) that can be used to augment your dataset via resampling directly from the original images (which vary in size).
- 2. Resampling to a uniform size can be done either by specifying the desired sizes resulting in non-isotropic pixel spacings (most often) or by specifying an isotropic pixel spacing and one of the image sizes (width,height,depth).
- 3. SimpleITK supports a variety of intensity transformations (blurring, adding noise etc.) that can be used to augment your dataset after it has been resampled to the size expected by your network.

This notebook illustrates the use of SimpleITK to perform data augmentation for deep learning. Note that the code is written so that the relevant functions work for both 2D and 3D images without modification.

Data augmentation is a model based approach for enlarging your training set. The problem being addressed is that the original dataset is not sufficiently representative of the general population of images. As a consequence, if we only train on the original dataset the resulting network will not generalize well to the population (overfitting).

Using a model of the variations found in the general population and the existing dataset we generate additional images in the hope of capturing the population variability. Note that if the model you use is incorrect you can cause harm, you are generating observations that do not occur in the general population and are optimizing a function to fit them.

```
In [1]: import SimpleITK as sitk
   import numpy as np
   import os

import gui
   %matplotlib notebook

from downloaddata import fetch_data as fdata
   from utilities import parameter_space_regular_grid_sampling, similarity3D_paramet
   er_space_regular_sampling, eul2quat

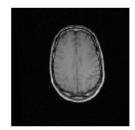
OUTPUT_DIR = 'output'
```

Load data

Load the images. You can work through the notebook using either the original 3D images or 2D slices from the original volumes.

```
In [3]: def disp_images(images, fig_size, wl_list=None):
    if images[0].GetDimension()==2:
        gui.multi_image_display2D(image_list=images, figure_size=fig_size, window_l
    evel_list=wl_list)
    else:
        gui.MultiImageDisplay(image_list=images, figure_size=fig_size, window_level
    _list=wl_list)
    disp_images(data, fig_size=(6,2))
```

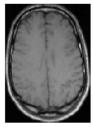




The original data often needs to be modified. In this example we would like to crop the images so that we only keep the informative regions. We can readily separate the foreground and background using an appropriate threshold, in our case we use Otsu's threshold selection method.

```
In [4]: def threshold based crop(image):
            # Set pixels that are in [min_intensity,otsu_threshold] to inside_value, valu
        es above otsu threshold are
            # set to outside_value. The anatomy has higher intensity values than the back
        ground, so it is outside.
            inside value = 0
            outside value = 255
            label_shape_filter = sitk.LabelShapeStatisticsImageFilter()
            label_shape_filter.Execute( sitk.OtsuThreshold(image, inside_value, outside_v
        alue))
            bounding box = label shape filter.GetBoundingBox(outside value)
            # The bounding box's first "dim" entries are the starting index and last "dim
        " entries the size
            return sitk.RegionOfInterest(image, bounding box[int(len(bounding box)/2):],
        bounding box[0:int(len(bounding box)/2)])
        modified data = [threshold based crop(img) for img in data]
        disp_images(modified_data, fig_size=(6,2))
```





At this point we select the images we want to work with, skip the following cell if you want to work with the original data.

```
In [5]: data = modified_data
```

Augmentation using spatial transformations

We next illustrate the generation of images by specifying a list of transformation parameter values representing a sampling of the transformation's parameter space.

The code below is agnostic to the specific transformation and it is up to the user to specify a valid list of transformation parameters (correct number of parameters and correct order).

In most cases we can easily specify a regular grid in parameter space by specifying ranges of values for each of the parameters. In some cases specifying parameter values may be less intuitive (i.e. versor representation of rotation).

Create reference domain

All input images will be resampled onto the reference domain.

This domain is defined by two constraints: the number of pixels per dimension and the physical size we want the reference domain to occupy. The former is associated with the computational constraints of deep learning where using a small number of pixels is desired. The later is associated with the SimpleITK concept of an image, it occupies a region in physical space which should be large enough to encompass the object of interest.

```
In [6]: dimension = data[0].GetDimension()
        \# Physical image size corresponds to the largest physical size in the training se
        t, or any other arbitrary size.
        reference_physical_size = np.zeros(dimension)
        for img in data:
            reference physical size[:] = [(sz-1)*spc if sz*spc>mx else mx for sz,spc,mx
        in zip(img.GetSize(), img.GetSpacing(), reference physical size)]
        # Create the reference image with a zero origin, identity direction cosine matrix
        and dimension
        reference origin = np.zeros(dimension)
        reference direction = np.identity(dimension).flatten()
        # Select arbitrary number of pixels per dimension, smallest size that yields desi
        red results (non-isotropic pixels)
        reference_size = [128]*dimension
        reference_spacing = [ phys_sz/(sz-1) for sz,phys_sz in zip(reference_size, refere
        nce physical size) ]
        # Another possibility is that you want isotropic pixels, uncomment the following
        lines.
        \#reference size x = 128
        #reference spacing = [reference physical size[0]/(reference size x-1)]*dimension
        #reference_size = [int(phys_sz/(spc) + 1) for phys_sz,spc in zip(reference_physic
        al_size, reference_spacing)]
        reference image = sitk.Image(reference size, data[0].GetPixelIDValue())
        reference image.SetOrigin(reference origin)
        reference image.SetSpacing(reference spacing)
        reference image.SetDirection(reference direction)
        # Always use the TransformContinuousIndexToPhysicalPoint to compute an indexed po
        int's physical coordinates as
        # this takes into account size, spacing and direction cosines. For the vast major
        ity of images the direction
        # cosines are the identity matrix, but when this isn't the case simply multiplyin
        g the central index by the
        # spacing will not yield the correct coordinates resulting in a long debugging se
        ssion.
        reference_center = np.array(reference_image.TransformContinuousIndexToPhysicalPoi
        nt(np.array(reference_image.GetSize())/2.0))
```

Data generation

Once we have a reference domain we can augment the data using any of the SimpleITK global domain transformations. In this notebook we use a similarity transformation (the generate_images function is agnostic to this specific choice).

Note that you also need to create the labels for your augmented images. If these are just classes then your processing is minimal. If you are dealing with segmentation you will also need to transform the segmentation labels so that they match the transformed image. The following function easily accommodates for this, just provide the labeled image as input and use the sitk.sitkNearestNeighbor interpolator so that you do not introduce labels that were not in the original segmentation.

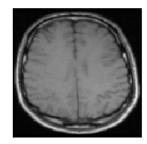
```
In [7]: def augment images spatial(original image, reference image, T0, T aug, transforma
        tion_parameters,
                            output_prefix, output_suffix,
                            interpolator = sitk.sitkLinear, default intensity value = 0.0
        ):
            Generate the resampled images based on the given transformations.
            Args:
                original image (SimpleITK image): The image which we will resample and tr
        ansform.
                reference_image (SimpleITK image): The image onto which we will resample.
                TO (SimpleITK transform): Transformation which maps points from the refer
        ence image coordinate system
                    to the original image coordinate system.
                T aug (SimpleITK transform): Map points from the reference image coordina
        te system back onto itself using the
                       given transformation parameters. The reason we use this transforma
        tion as a parameter
                       is to allow the user to set its center of rotation to something ot
        her than zero.
                transformation parameters (List of lists): parameter values which we use
        T aug.SetParameters().
                output_prefix (string): output file name prefix (file name: output prefix
        p1 p2 ..pn .output suffix).
                output_suffix (string): output file name suffix (file name: output prefix
        _p1_p2...pn_.output_suffix).
                interpolator: One of the SimpleITK interpolators.
                default_intensity_value: The value to return if a point is mapped outside
        the original image domain.
            all_images = [] # Used only for display purposes in this notebook.
            for current parameters in transformation parameters:
                T aug.SetParameters(current parameters)
                # Augmentation is done in the reference image space, so we first map the
        points from the reference image space
                \# back onto itself T aug (e.g. rotate the reference image) and then we ma
        p to the original image space T0.
                T all = sitk.Transform(T0)
                T all.AddTransform(T aug)
                aug image = sitk.Resample(original image, reference image, T all,
                                           interpolator, default_intensity_value)
                sitk.WriteImage(aug_image, output_prefix + ' ' +
                                 _'.join(str(param) for param in current_parameters) +'_.
        ' + output suffix)
                all_images.append(aug_image) # Used only for display purposes in this not
        ebook.
            return all images # Used only for display purposes in this notebook.
```

Before we can use the generate_images function we need to compute the transformation which will map points between the reference image and the current image as shown in the code cell below.

Note that it is very easy to generate large amounts of data, the calls to np.linspace with m parameters each having n values results in n^m images, so don't forget that these images are also saved to disk. If you run the code below for 3D data you will generate 6561 volumes (3^7 parameter combinations times 3 volumes).

```
aug transform = sitk.Similarity2DTransform() if dimension==2 else sitk.Similarity
In [8]:
        3DTransform()
        all images = []
        for index,img in enumerate(data):
            # Transform which maps from the reference_image to the current img with the t
        ranslation mapping the image
            # origins to each other.
            transform = sitk.AffineTransform(dimension)
            transform.SetMatrix(img.GetDirection())
            transform.SetTranslation(np.array(img.GetOrigin()) - reference origin)
            # Modify the transformation to align the centers of the original and referenc
        e image instead of their origins.
            centering transform = sitk.TranslationTransform(dimension)
            img center = np.array(img.TransformContinuousIndexToPhysicalPoint(np.array(im
        g.GetSize())/2.0))
            centering_transform.SetOffset(np.array(transform.GetInverse().TransformPoint(
        img_center) - reference_center))
            centered transform = sitk.Transform(transform)
            centered transform.AddTransform(centering transform)
            # Set the augmenting transform's center so that rotation is around the image
        center.
            aug transform.SetCenter(reference center)
            if dimension == 2:
                # The parameters are scale (+-10%), rotation angle (+-10 degrees), x tran
        slation, y translation
                transformation parameters list = parameter space regular grid sampling(np
        .linspace(0.9, 1.1, 3),
                                                                                         np
        .linspace(-np.pi/18.0,np.pi/18.0,3),
                                                                                         np
        .linspace(-10,10,3),
                                                                                         np
        .linspace(-10,10,3))
                transformation parameters list = similarity3D parameter space regular sam
        pling(np.linspace(-np.pi/18.0,np.pi/18.0,3),
        np.linspace(-np.pi/18.0,np.pi/18.0,3),
        np.linspace(-np.pi/18.0,np.pi/18.0,3),
        np.linspace(-10,10,3),
        np.linspace(-10,10,3),
        np.linspace(-10,10,3),
        np.linspace(0.9,1.1,3))
            generated images = augment images_spatial(img, reference_image, centered_tran
        sform,
                                                aug_transform, transformation_parameters_1
        ist,
                                                os.path.join(OUTPUT DIR, 'spatial aug'+str
        (index)), 'mha')
            if dimension==2: # in 2D we join all of the images into a 3D volume which we
        use for display.
                all images.append(sitk.JoinSeries(generated images))
        # If working in 2D, display the resulting set of images.
        if dimension==2:
             mid wallidam aradaalaaydaa aa 13a, 211 dan aa - Abaada 21daa maaa - Adaada 2
```





What about flipping

Reflection using SimpleITK can be done in one of several ways:

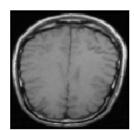
- 1. Use an affine transform with the matrix component set to a reflection matrix. The columns of the matrix correspond to the \mathbf{x} , \mathbf{y} and \mathbf{z} axes. The reflection matrix is constructed using the plane, 3D, or axis, 2D, which we want to reflect through with the standard basis vectors, \mathbf{e}_i , \mathbf{e}_j , and the remaining basis vector set to $-\mathbf{e}_k$.
 - Reflection about xy plane: $[\mathbf{e}_1, \mathbf{e}_2, -\mathbf{e}_3]$.
 - Reflection about xz plane: $[\mathbf{e}_1, -\mathbf{e}_2, \mathbf{e}_3]$.
 - Reflection about yz plane: $[-\mathbf{e}_1, \mathbf{e}_2, \mathbf{e}_3]$.
- 2. Use the native slicing operator(e.g. img[:,::-1,:]), or the FlipImageFilter after the image is resampled onto the reference image grid.

We prefer option 1 as it is computationally more efficient. It combines all transformation prior to resampling, while the other approach performs resampling onto the reference image grid followed by the reflection operation. An additional difference is that using slicing or the FlipImageFilter will also modify the image origin while the resampling approach keeps the spatial location of the reference image origin intact. This minor difference is of no concern in deep learning as the content of the images is the same, but in SimpleITK two images are considered equivalent iff their content and spatial extent are the same.

The following cell corresponds to the preferred option, using an affine transformation:

```
In [9]: flipped images = []
                      for index,img in enumerate(data):
                                # Compute the transformation which maps between the reference and current ima
                      ge (same as done above).
                                transform = sitk.AffineTransform(dimension)
                                transform.SetMatrix(img.GetDirection())
                                transform.SetTranslation(np.array(img.GetOrigin()) - reference_origin)
                                centering transform = sitk.TranslationTransform(dimension)
                                img center = np.array(img.TransformContinuousIndexToPhysicalPoint(np.array(im
                      g.GetSize())/2.0))
                                \verb|centering_transform.SetOffset(np.array(transform.GetInverse().TransformPoint(), or all other contents of the content of th
                      img center) - reference center))
                                centered_transform = sitk.Transform(transform)
                                centered transform.AddTransform(centering transform)
                                flipped transform = sitk.AffineTransform(dimension)
                                flipped transform.SetCenter(reference image.TransformContinuousIndexToPhysica
                      lPoint(np.array(reference image.GetSize())/2.0))
                                if dimension==2: # matrices in SimpleITK specified in row major order
                                           flipped transform.SetMatrix([1,0,0,-1])
                                else:
                                           flipped_transform.SetMatrix([1,0,0,0,-1,0,0,0,1])
                                centered_transform.AddTransform(flipped_transform)
                                # Resample onto the reference image
                                flipped images.append(sitk.Resample(img, reference image, centered transform,
                      sitk.sitkLinear, 0.0))
                      disp_images(flipped_images, fig_size=(6,2))
```





Radial Distortion

Some 2D medical imaging modalities, such as endoscopic video and X-ray images acquired with C-arms using image intensifiers, exhibit radial distortion. The common model for such distortion was described by Brown ["Close-range camera calibration", Photogrammetric Engineering, 37(8):855–866, 1971]:

$$\mathbf{p}_{u} = \mathbf{p}_{d} + (\mathbf{p}_{d} - \mathbf{p}_{c})(k_{1}r^{2} + k_{2}r^{4} + k_{3}r^{6} + ...)$$

where:

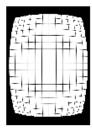
- p_u is a point in the undistorted image
- ullet \mathbf{p}_d is a point in the distorted image
- $oldsymbol{ ext{p}}_c$ is the center of distortion
- $r = \|\mathbf{p}_d \mathbf{p}_c\|$
- k_i are coefficients of the radial distortion

Using SimpleITK operators we represent this transformation using a deformation field as follows:

```
In [10]: def radial distort(image, k1, k2, k3, distortion center=None):
             c = distortion_center
             if not c: # The default distortion center coincides with the image center
                 c = np.array(image.TransformContinuousIndexToPhysicalPoint(np.array(image
         .GetSize())/2.0))
             # Compute the vector image (p_d - p_c)
             delta image = sitk.Image(image.GetSize(), sitk.sitkVectorFloat64)
             delta image.CopyInformation(image)
             index_ranges = [np.arange(0,i) for i in image.GetSize()]
             for indexes in np.nditer(np.meshgrid(*index_ranges)):
                 index = tuple(map(np.asscalar, indexes))
                 delta image[index] = np.array(image.TransformContinuousIndexToPhysicalPoi
         nt(index)) - c
             delta image components = [sitk.VectorIndexSelectionCast(delta image,index) fo
         r index in range(image.GetDimension())]
             # Compute the radial distortion expression
             r2_image = sitk.Image(image.GetSize(), sitk.sitkFloat64)
             r2 image.CopyInformation(image)
             for img in delta_image_components:
                 r2_image+=img**2
             r4_image = r2_image**2
             r6_image = r2_image*r4_image
             disp_image = k1*r2_image + k2*r4_image + k3*r6_image
             displacement image = sitk.Compose([disp image*img for img in delta image comp
         onents])
             displacement field transform = sitk.DisplacementFieldTransform(displacement i
         mage)
             return sitk.Resample(image, image, displacement field transform)
         # We only run the distortion on 2D images (the code will work for 3D but it is sl
         OW)
         if dimension==2:
             k1 = 0.00001
             k2 = 0.0000000000001
             k3 = 0.000000000001
             original image = data[0]
             distorted image = radial distort(original image, k1, k2, k3)
             # Use a grid image to highlight the distortion.
             grid_image = sitk.GridSource(outputPixelType=sitk.sitkUInt16, size=original i
         mage.GetSize(),
                                       sigma=(0.1,0.1), gridSpacing=(20.0,20.0))
             grid image.CopyInformation(original image)
             distorted grid = radial distort(grid image, k1, k2, k3)
             disp_images([original_image, distorted_image, distorted_grid], fig_size=(6,2)
         )
```







Transferring deformations - exercise for the interested reader

Using SimpleITK we can readily transfer deformations from a spatio-temporal data set to another spatial data set to simulate temporal behavior. Case in point, using a 4D (3D+time) CT of the thorax we can estimate the respiratory motion using non-rigid registration and Free Form Deformation or displacement field transformations. We can then register a new spatial data set to the original spatial CT (non-rigidly) followed by application of the temporal deformations.

Note that unlike the arbitrary spatial transformations we used for data-augmentation above this approach is more computationally expensive as it involves multiple non-rigid registrations. Also note that as the goal is to use the estimated transformations to create plausible deformations you may be able to relax the required registration accuracy.

Augmentation using intensity modifications

SimpleITK has many filters that are potentially relevant for data augmentation via modification of intensities. For example:

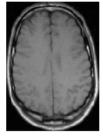
- Image smoothing, always read the documentation carefully, similar filters use use different parametrization σ vs. variance (σ^2):
 - <u>Discrete Gaussian (https://itk.org/SimpleITKDoxygen</u>
 /html/classitk 1 1simple 1 1DiscreteGaussianImageFilter.html)
 - Recursive Gaussian (https://itk.org/SimpleITKDoxygen/html/classitk 1 1simple 1 1RecursiveGaussianImageFilter.html)
 - Smoothing Recursive Gaussian (https://itk.org/SimpleITKDoxygen/html/classitk 1 1simple 1 1SmoothingRecursiveGaussianImageFilter.html)
- Edge preserving image smoothing:
 - Bilateral image filtering (https://itk.org/SimpleITKDoxygen /html/classitk_1_1simple_1_1BilateralImageFilter.html), edge preserving smoothing.
 - Median filtering (https://itk.org/SimpleITKDoxygen/html/classitk 1_1simple_1_1MedianImageFilter.html)
- · Adding noise to your images:
 - Additive Gaussian (https://itk.org/SimpleITKDoxygen /html/classitk 1 1simple 1 1AdditiveGaussianNoiseImageFilter.html)
 - Salt and Pepper / Impulse (https://itk.org/SimpleITKDoxygen/html/classitk 1 1simple 1 1SaltAndPepperNoiseImageFilter.html)
 - Shot/Poisson (https://itk.org/SimpleITKDoxygen/html/classitk 1 1simple 1 1ShotNoiseImageFilter.html)
 - Speckle/multiplicative (https://itk.org/SimplelTKDoxygen /html/classitk_1_1simple_1_1SpeckleNoiseImageFilter.html)
- Adaptive Histogram Equalization (https://itk.org/SimpleITKDoxygen /html/classitk 1 1simple 1 1AdaptiveHistogramEqualizationImageFilter.html)

```
In [11]: def augment images intensity(image list, output prefix, output suffix):
             Generate intensity modified images from the originals.
             Args:
                 image list (iterable containing SimpleITK images): The images which we wh
         ose intensities we modify.
                 output_prefix (string): output file name prefix (file name: output_prefix
         i FilterName.output suffix).
                 output suffix (string): output file name suffix (file name: output prefix
         i FilterName.output suffix).
             # Create a list of intensity modifying filters, which we apply to the given i
         mages
             filter list = []
             # Smoothing filters
             filter list.append(sitk.SmoothingRecursiveGaussianImageFilter())
             filter list[-1].SetSigma(2.0)
             filter list.append(sitk.DiscreteGaussianImageFilter())
             filter_list[-1].SetVariance(4.0)
             filter list.append(sitk.BilateralImageFilter())
             filter list[-1].SetDomainSigma(4.0)
             filter_list[-1].SetRangeSigma(8.0)
             filter list.append(sitk.MedianImageFilter())
             filter list[-1].SetRadius(8)
             # Noise filters using default settings
             # Filter control via SetMean, SetStandardDeviation.
             filter_list.append(sitk.AdditiveGaussianNoiseImageFilter())
             # Filter control via SetProbability
             filter list.append(sitk.SaltAndPepperNoiseImageFilter())
             # Filter control via SetScale
             filter list.append(sitk.ShotNoiseImageFilter())
             # Filter control via SetStandardDeviation
             filter list.append(sitk.SpeckleNoiseImageFilter())
             filter list.append(sitk.AdaptiveHistogramEqualizationImageFilter())
             filter_list[-1].SetAlpha(1.0)
             filter_list[-1].SetBeta(0.0)
             filter list.append(sitk.AdaptiveHistogramEqualizationImageFilter())
             filter list[-1].SetAlpha(0.0)
             filter_list[-1].SetBeta(1.0)
             aug_image_lists = [] # Used only for display purposes in this notebook.
             for i,img in enumerate(image_list):
                 aug_image_lists.append([f.Execute(img) for f in filter_list])
                 for aug image,f in zip(aug image lists[-1], filter list):
                     sitk.WriteImage(aug_image, output_prefix + str(i) + '
                                      f.GetName() + '.' + output suffix)
             return aug image lists
```

Modify the intensities of the original images using the set of SimpleITK filters described above. If we are working with 2D images the results will be displayed inline.

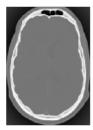
```
In [12]:
         intensity_augmented_images = augment_images_intensity(data, os.path.join(OUTPUT_D
         IR, 'intensity_aug'), 'mha')
                   # in 2D we join all of the images into a 3D volume which we use for dis
         play.
         if dimension==2:
             def list2_float_volume(image_list) :
                 return sitk.JoinSeries([sitk.Cast(img, sitk.sitkFloat32) for img in image
         _list])
             all images = [list2 float volume(imgs) for imgs in intensity augmented images
         ]
             # Compute reasonable window-level values for display (just use the range of i
         ntensity values
             # from the original data).
             original window level = []
             statistics_image_filter = sitk.StatisticsImageFilter()
             for img in data:
                 statistics image filter.Execute(img)
                 max intensity = statistics image filter.GetMaximum()
                 min intensity = statistics image filter.GetMinimum()
                 original_window_level.append((max_intensity-min_intensity, (max_intensity
         +min intensity)/2.0))
             gui.MultiImageDisplay(image_list=all_images, shared_slider=True, figure_size=
         (6,2), window_level_list=original_window_level)
```

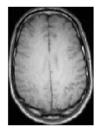




Finally, you can easily create intensity variations that are specific to your domain, such as the spatially varying multiplicative and additive transformation shown below.

```
In [13]: def mult_and_add_intensity_fields(original_image):
             Modify the intensities using multiplicative and additive Gaussian bias fields
             # Gaussian image with same meta-information as original (size, spacing, direc
         tion cosine)
             # Sigma is half the image's physical size and mean is the center of the image
             g_mult = sitk.GaussianSource(original_image.GetPixelIDValue(),
                                      original_image.GetSize(),
                                       [(sz-1)*spc/2.0 for sz, spc in zip(original image.Ge
         tSize(), original image.GetSpacing())],
                                       original image.TransformContinuousIndexToPhysicalPoi
         nt(np.array(original image.GetSize())/2.0),
                                       original image.GetOrigin(),
                                       original_image.GetSpacing(),
                                       original_image.GetDirection())
             # Gaussian image with same meta-information as original (size, spacing, direc
         tion cosine)
             # Sigma is 1/8 the image's physical size and mean is at 1/16 of the size
             g_add = sitk.GaussianSource(original_image.GetPixelIDValue(),
                                      original_image.GetSize(),
                        [(sz-1)*spc/8.0 for sz, spc in zip(original_image.GetSize(), origi
         nal_image.GetSpacing())],
                        original_image.TransformContinuousIndexToPhysicalPoint(np.array(or
         iginal image.GetSize())/16.0),
                        25,
                        original_image.GetOrigin(),
                        original_image.GetSpacing(),
                        original_image.GetDirection())
             return g mult*original image+g add
         disp images([mult and add intensity fields(img) for img in data], fig size=(6,2))
```





(basic_registration.ipynb)

Next » (basic_registration.ipynb)