

1. 1.1.1

- (a) True. Vacuously true.
- (c) True. By definition.
- (e) True.
- (g) False. Elements of  $2^{\{a,b,\{a,b\}\}}$  are sets.

2. 1.1.2

- (a)  $\{3, 5\}$
- (c)  $\{1, 2, 7, 9\}$
- (e)  $\{\emptyset\}$

3. 1.2.2

- $R \circ R = \{(a, a), (a, b), (a, c), (a, d), (b, a), (b, b), (b, c)\}$ , is not a function, since  $a$  is the first component of both  $(a, a)$  and  $(a, b)$
- $R^{-1} = \{(b, a), (c, a), (d, c), (a, a), (a, b)\}$ , is not a function, since  $a$  is the first component of both  $(a, a)$  and  $(a, b)$
- $R$  is not a function, since  $a$  is the first component of both  $(a, a)$  and  $(a, b)$

4. 1.3.2.(a)

- $R$  is
  - (a) Not symmetric,  $(1, 5) \in R$  but  $(5, 1) \notin R$
  - (b) Not reflexive,  $(5, 5) \notin R$
  - (c) Not transitive,  $(3, 1) \in R, (1, 5) \in R$  but  $(3, 5) \notin R$
- $S$  is
  - (a) Symmetric
  - (b) Not reflexive,  $(6, 6) \notin S$
  - (c) Not transitive,  $(3, 1) \in S, (1, 5) \in S$  but  $(3, 5) \notin S$