STOR 435 Homework 18

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1.

a)
$$\int_0^1 \int_0^y c(x^2 + y^2) dx dy = 1 \rightarrow \frac{c}{3} = 1 \rightarrow c = 3$$

b)
$$f_X(x) = \begin{cases} \int_x^1 3(x^2 + y^2) dy = -4x^3 + 3x^2 + 1 & \text{if } x \in [0, 1] \\ 0 & \text{otherwise} \end{cases}$$

c)
$$f_Y(y) = \begin{cases} \int_0^y 3(x^2 + y^2) dx = 4y^3 & \text{if } y \in [0, 1] \\ 0 & \text{otherwise} \end{cases}$$

d)
$$\mathbb{E}(X) = \int_0^1 \int_0^y x \times 3(x^2 + y^2) dx dy = \frac{9}{20}$$

2.

a)	x/y	0	1	2	3
	0	0.1	0	0	0
	1	0.08	0.32	0	0
	2	0.016	0.128	0.256	0
	3	0.0008	0.0096	0.0384	0.0512

	\boldsymbol{x}	$p_X(x)$
	0	0.1
b)	1	0.4
	2	0.4
	3	0.1

d)
$$\mathbb{E}(Y) = \sum_{y=0}^{y=3} p_Y(y)y = 1.2$$

3.

a)
$$\frac{23}{32}$$

b)
$$\frac{23}{32}$$

c)
$$\frac{1}{16}(\ln(4) + 13)$$

d)
$$\frac{1}{2}$$