- 1. 2.3.7.(b)  $((a \cup b)(a \cup b))^*$
- 2. As the hint suggests, by regularity's closure under intersection, it suffices to show  $L\cap a^*bba^*=\{a^nbba^n:n\geq 0\}$  is non-regular. Take arbitrary N>0. Let  $w=a^Nbba^N$ . Take arbitrary xyz=w, with  $|xy|\leq N,\,y\neq\epsilon$ . Note that  $x=a^h,y=a^i,z=a^jbba^N$ , where  $h\geq 0,i>0,j\geq 0$  and h+i+j=N. Let k=2, then  $x(y^k)z=a^ha^{2i}a^jbba^N=a^{N+i}bba^N\notin L$ .

Note: we actually have a stronger conclusion in this case that w can be arbitrary and k>0 is sufficient, since any repetition has to be done both before and after bb, and repetition of y can only appear before or after bb (or containing bb).

3.

$$L = (a \cup b)^*, S = a^n b^n$$