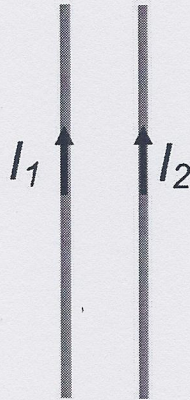


NAME _____

Total :100 (Bonus) Points

1. (25 pts) Consider two parallel current carrying wires. With the currents running in the same direction, the wires are



- ☒ a) attracted (like attract)
- ☐ b) repelled (likes repel)
- ☐ c) pushed in another direction
- ☐ d) not pushed – no net force

2. (25 pts)

Can a charged particle move through a uniform magnetic field without experiencing any force?

Suppose a charged particle is moving under the influence of both electric and magnetic fields. How can the effect of the two fields on the motion of the particle be distinguished?

$$\vec{F}_{\text{magnetic}} = q \vec{v} \times \vec{B}.$$

Yes. when a charged particle moves parallel with the magnetic field.

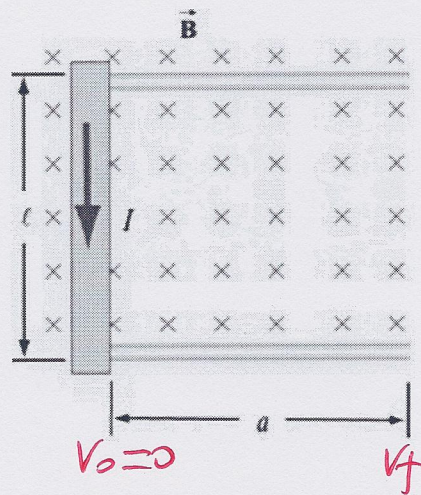
$$\vec{F} = q \vec{E} + q \vec{v} \times \vec{B},$$

If \vec{v} is particle's velocity.

$$m \frac{d\vec{v}}{dt} = q \vec{E} + q \vec{v} \times \vec{B}.$$

So the effect of electric field will be along the velocity direction. and the effect of magnetic field will be perpendicular to the velocity direction.

3. (25 pts) A rod with a mass m and a radius R is mounted on two parallel rails of length a separated by a distance ℓ , as shown in the Figure below. The rod carries a current I and slides in uniform magnetic field



What is the speed of the rod as it leaves the rails?

$$F \cdot a = \frac{1}{2} m V_f^2 - \frac{1}{2} m V_0^2 = \frac{1}{2} m V_f^2$$

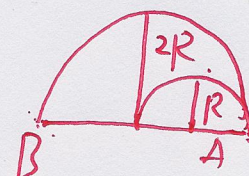
$$F = ILB$$

$$\Rightarrow V_f^2 = \frac{2Fa}{m} = \frac{2ILB \cdot a}{m}$$

$$V_f = \sqrt{\frac{2ILB \cdot a}{m}}$$

4. (25 pts) Particle A with charge q and mass m_A and particle B with charge $2q$ and mass m_B , are accelerated from rest by a potential difference ΔV , and subsequently deflected by a uniform magnetic field into semicircular paths. The radii of the trajectories by particle A and B are R and $2R$, respectively. The direction of the magnetic field is perpendicular to the velocity of the particle. Show that their mass ratio is

$$\frac{m_A}{m_B} = \frac{1}{8}$$



$\frac{1}{2} m v^2 = \Delta V \cdot q$, v is velocity. ΔV is potential difference

$$v = \sqrt{\frac{2\Delta V \cdot q}{m}}$$

$$\Rightarrow v_A = \sqrt{\frac{2\Delta V \cdot q}{m_A}}$$

$$v_B = \sqrt{\frac{2\Delta V \cdot 2q}{m_B}} = \sqrt{\frac{4\Delta V \cdot q}{m_B}}$$

Centripetal force $\frac{m v^2}{r} = q v B$, ($\vec{B} \perp \vec{v}$)

$$v = \frac{r q B}{m}$$

$$\Rightarrow v_A = \frac{R q B}{m_A}$$

$$v_B = \frac{2R \cdot 2q B}{m_B} = \frac{4R q B}{m_B}$$

$$\frac{v_A}{v_B} = \frac{\sqrt{\frac{2\Delta V \cdot q}{m_A}}}{\sqrt{\frac{4\Delta V \cdot q}{m_B}}} = \frac{\frac{R q B}{m_A}}{\frac{4R q B}{m_B}}$$

$$\Rightarrow \sqrt{\frac{2}{\frac{m_A}{4 m_B}}} = \frac{1}{4} \frac{m_B}{m_A}$$

$$\Rightarrow \sqrt{\frac{m_B}{2 m_A}} = \frac{m_B}{4 m_A} \Rightarrow \frac{m_A}{m_B} = \frac{1}{8} \quad \checkmark$$