

COMPUTER SCIENCE AND ENGINEERING Indian Institute of Technology, Palakkad CS5016: Computational Methods and Applications

Assignment 1: Monte Carlo Method

Max points: 100

A few instructions

- Codes should be compatible with *Python3* and should run on Ubuntu.
- Code for each question should be placed in a separate file (Q1.py, Q2.py, Q3.py and Q4.py).
- Codes should be well-commented.
- 1. Stirling's approximation (or Stirling's formula) is an approximation for factorials. It is a good approximation, leading to accurate results even for small values of n^1 . The approximation is as follows

$$n! \approx \sqrt{2\pi n} \left(\frac{n}{e}\right)^n$$

Write a code to visualize the above result for values of n upto 10^6 .

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- 2. Create a class Dice with attributes numSides such that
 - It should be possible to create an object of this type by specifying the number of sides of the dice. If number of sides is not mentioned, create a 6 sided dice.

#The following code should create a 6 faced dice
d = Dice()

#The following code should create a 10 faced dice
d = Dice(10)

• Number of sides should be an integer greater than 4. Otherwise, an **exception** should be thrown.

d = Dice(3)

Expected output:

<class 'Exception'>
Cannot construct the dice

¹https://en.wikipedia.org/wiki/Stirling's_approximation

```
d = Dice(4.5)
```

Expected output:

```
<class 'Exception'>
Cannot construct the dice
```

```
d = Dice('5')
```

Expected output:

```
<class 'Exception'>
Cannot construct the dice
```

• By default, each face of the dice should have equal probability of occurrence. However, by using the function setProb one should be able to set probability of occurrence of each face. This function should take a tuple as its argument

```
#The following code should create a 4 faced dice with probability
#distribution {0.1, 0.2, 0.3, 0.4}
d = Dice(4)
d.setProb((0.1, 0.2, 0.3, 0.4))
```

• If the tuple passed as argument to **setProb** is not a valid probability distribution for the dice, an **exception** should be thrown. A examples are as follows

```
d = Dice(4)
d.setProb((0.1, 0.2, 0.3))
```

Expected output:

```
<class 'Exception'>
Invalid probability distribution
```

```
d = Dice(4)
d.setProb((0.5, 0.2, 0.3, 0.4))
```

Expected output:

```
<class 'Exception'>
Invalid probability distribution
```

• It should be possible to print an object of type Dice.

```
d = Dice(5)
print(d)
```

Expected output:

Dice with 5 faces and probability distribution {0.2, 0.2, 0.2, 0.2}

```
d = Dice(4)
d.setProb((0.1, 0.2, 0.3, 0.4))
print(d)
```

Expected output:

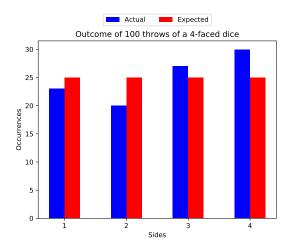
```
Dice with 4 faces and probability distribution {0.1, 0.2, 0.3, 0.4}
```

• It should be possible to simulate n throws of the dice by calling the function roll. This function should take n, the number of throws, as its arguments and displays a bar chart showing the expected and actual number of occurrences of each face when the dice is thrown n times.

NOTE: Only matplotlib and random modules are to be imported. From random module, you are only allowed to use the random function.

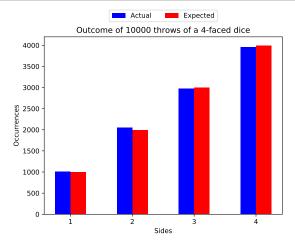
```
d = Dice(4)
d.roll(100)
```

Expected output:



```
d = Dice(4)
d.setProb((0.1, 0.2, 0.3, 0.4))
d.roll(10000)
```

Expected output:

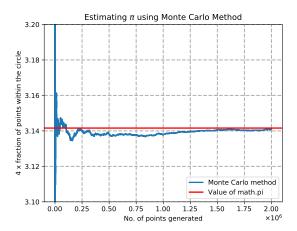


3. Write a function estimatePi that estimates π using the Monte Carlo method. This function should take as argument a positive integer n that denotes the total number of points generated in the simulation.

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estimatePi(2000000)

Expected output:



NOTE: Plot generated by your code should be similar to the above plot.

4. Create a class TextGenerator such that

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• It has a function assimilateText that takes a file name as its argument. It then read all the text in the file and creates a prefix dictionary that maps a pair (2-tuple) of words to a list of words which follow that pair in the text.

```
t = TextGenerator()
t.assimilateText('sherlock,txt')
```

• It has a function generateText that creates random text based on the triplets contained in the prefix dictionary. This function has a mandatory argument that let it know the number of words to be produced in this random manner.

```
t = TextGenerator()
t.assimilateText('sherlock,txt')
t.generateText(100)
```

Expected output:

smelling of iodoform, with a bright, quick face, freckled like a sheep in a single branch office, and the schemer falls into the stable lane. So long was he doing there at all? If his purpose were innocent, why did you first how I employed my morning, or the grace and kindliness with which I beg pardon. As to Miss Turner. On the next evening I would find that all was dark in the air. "May I see it?" But I think that the gas is not so much public attention has now definitely announced his approaching marriage with so

• It should be possible to invoke the function generateText with an additional argument that fixes the first word in the random text it produces.

```
t = TextGenerator()
t.assimilateText('sherlock,txt')
t.generateText(50, 'London')
```

Expected output:

London for the grace and kindliness with which I beg that you have described. You must find your own theory as to come to the altar faced round to his credit at the pool I heard the rush of constables with an inspector, all on fire to the salesman just

• If generateText is not able to produce random text with the specifed start word, it should throw an exception.

```
t = TextGenerator()
t.assimilateText('sherlock,txt')
t.generateText(50, 'Wedge')
```

Expected output:

```
<class 'Exception'>
Unable to produce text with the specified start word.
```

NOTE: Since the text generated by generateText is random in nature, text produced by your code need not match the expected output shown above.