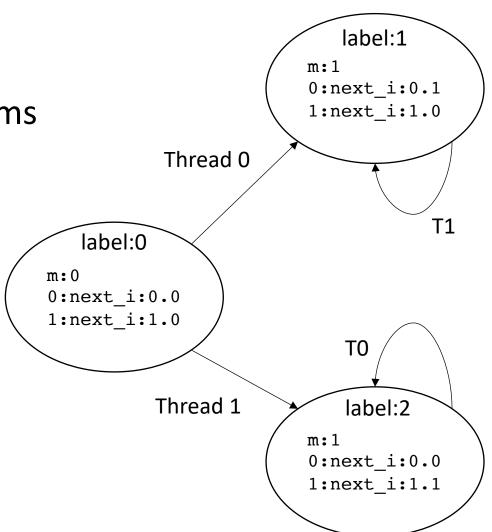
CSE113: Parallel Programming

May 25, 2021

- Topic: Reasoning about concurrent programs
 - Labelled Transition Systems
 - Liveness Properties
 - Schedulers



Announcements

- Homework 4 is posted:
 - Due June 7th
 - PLEASE do not turn this one in late!
 - Already a typo posted in piazza (will fix tonight)
- Behind schedule a bit (grading, HW assigned, etc)
 - HW 5 is canceled
 - Each HW is worth 12.5% of your final grade
 - For those interested in GPGPU programming: The book CUDA by Example is linked on the class resource page
- HW2 grades planning on being released by midnight tomorrow!

Announcements

- SETs are out:
 - Please remember to fill them out! They are very important, especially for new classes and new faculty
 - Any other feedback is welcome! Feel free to email or discuss during office hours

Announcements

Today will finish up Module 4

- Last 3 lectures: heterogeneous and distributed computing:
 - 2 lectures by me about GPGPU programming
 - last lecture by Reese about distributed system programming

Quiz

Quiz

Discuss answers

Schedule

Labeled Transition Systems

Scheduler specifications

• When you write a concurrent program, how do you think about what can happen?

• When you write a concurrent program, how do you think about what can happen?

Interleavings?

• When you write a concurrent program, how do you think about what can happen?

Interleavings?

• RMWs?

• When you write a concurrent program, how do you think about what can happen?

Interleavings?

• RMWs?

Thread Sanitizer?

• When you write a concurrent program, how do you think about what can happen?

Interleavings?

• RMWs?

Thread Sanitizer?

Run the program and pray to the gods of concurrency?

Think about two threads accessing the bank account

getting paid

```
Thread 0:
//lock
while(CAS(&m,0,1) == false);
int tmp = *bank_account;
tmp++;
*bank_account = tmp;
m.store(0); //unlock
```

buying coffee

```
Thread 1:
//lock
while(CAS(&m,0,1) == false);
int tmp = *bank_account;
tmp--;
*bank_account = tmp;
m.store(0); //unlock
```

```
Thread 0:
//lock
while(CAS(&m,0,1) == false);
int tmp = *bank_account;
tmp++;
*bank_account = tmp;
m.store(0); //unlock
```

```
Thread 1:
//lock
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int tmp = *bank_account;
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```
Thread 0:
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while(CAS(&m,0,1) == false);
int tmp = *bank_account;
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```
Thread 1:
//lock
while(CAS(&m,0,1) == false);
int tmp = *bank_account;
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```

step 1 pick a thread

```
Thread 0:
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int tmp = *bank_account;
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```
Thread 1:
//lock
while(CAS(&m,0,1) == false);
int tmp = *bank_account;
tmp--;
*bank_account = tmp;
m.store(0); //unlock
```

```
while(CAS(&m,0,1) == false);
```

step 1 pick a thread

```
Thread 0:
//lock
while(CAS(&m,0,1) == false);
int tmp = *bank_account;
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```
Thread 1:
//lock
while(CAS(&m,0,1) == false);
int tmp = *bank_account;
tmp--;
*bank_account = tmp;
m.store(0); //unlock
```

while(CAS(&m,0,1) == false);

step 1 pick a thread

Keep track of next instruction
to execute

```
Thread 0:
//lock
while(CAS(&m,0,1) == false);
int tmp = *bank_account;
tmp++;
*bank_account = tmp;
m.store(0); //unlock
```

```
Thread 1:
//lock
while(CAS(&m,0,1) == false);
int tmp = *bank_account;
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*bank_account = tmp;
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```

```
while(CAS(\&m,0,1) == false);
```

step 1 pick a thread

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to execute

```
Thread 0:
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Thread 1:
//lock
while(CAS(&m,0,1) == false);
int tmp = *bank_account;
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*bank_account = tmp;
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```

while(CAS(&m,0,1) == false);

step 1 pick a thread

Keep track of next instruction
to execute

pick the next thread to execute

```
Thread 0:
//lock
while(CAS(&m,0,1) == false);
int tmp = *bank_account;
tmp++;
*bank_account = tmp;
m.store(0); //unlock
```

```
Thread 1:
//lock
while(CAS(&m,0,1) == false);
int tmp = *bank_account;
tmp--;
*bank_account = tmp;
m.store(0); //unlock
```

acquired lock while(CAS(&m,0,1) == false);

step 1 pick a thread

Keep track of next instruction
to execute

pick the next thread to execute

```
Thread 0:
//lock
while(CAS(&m,0,1) == false);
int tmp = *bank_account;
tmp++;
*bank_account = tmp;
m.store(0); //unlock
```

```
Thread 1:
//lock
while(CAS(&m,0,1) == false);
int tmp = *bank_account;
tmp--;
*bank_account = tmp;
m.store(0); //unlock
```

while(CAS(&m,0,1) == false); acquired lock Tried and failed while (CAS(&m, 0, 1) == false);

step 1 pick a thread

Keep track of next instruction
to execute

pick the next thread to execute

```
Thread 0:
//lock
while(CAS(&m,0,1) == false);
int tmp = *bank_account;
tmp++;
*bank_account = tmp;
m.store(0); //unlock
```

```
Thread 1:
//lock
while(CAS(&m,0,1) == false);
int tmp = *bank_account;
tmp--;
*bank_account = tmp;
m.store(0); //unlock
```

```
acquired lock
                    while (CAS(&m,0,1) == false);
Tried and failed
                   while (CAS(&m, 0, 1) == false);
```

step 1 pick a thread

Keep track of next instruction
to execute

pick the next thread to execute

Keep track of next instruction to execute

```
Thread 0:
//lock
while(CAS(&m,0,1) == false);
int tmp = *bank_account;
tmp++;
*bank_account = tmp;
m.store(0); //unlock
```

```
Thread 1:
//lock
while(CAS(&m,0,1) == false);
int tmp = *bank_account;
tmp--;
*bank_account = tmp;
m.store(0); //unlock
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acquired lock while (CAS(&m,0,1) == false); Tried and failed while (CAS(&m, 0, 1) == false);

step 1 pick a thread

Keep track of next instruction
to execute

pick the next thread to execute

Keep track of next instruction to execute

which thread to pick next?

```
Thread 0:
//lock
while(CAS(&m,0,1) == false);
int tmp = *bank_account;
tmp++;
*bank_account = tmp;
m.store(0); //unlock
```

```
Thread 1:
//lock
while(CAS(&m,0,1) == false);
int tmp = *bank_account;
tmp--;
*bank_account = tmp;
m.store(0); //unlock
```

acquired lock while (CAS(&m,0,1) == false); Tried and failed while (CAS(&m, 0, 1) == false); while (CAS(&m, 0, 1) == false);

step 1 pick a thread

Keep track of next instruction
to execute

pick the next thread to execute

Keep track of next instruction to execute

which thread to pick next?

```
Thread 0:
//lock
while(CAS(&m,0,1) == false);
int tmp = *bank_account;
tmp++;
*bank_account = tmp;
m.store(0); //unlock
```

```
Thread 1:
//lock
while(CAS(&m,0,1) == false);
int tmp = *bank_account;
tmp--;
*bank_account = tmp;
m.store(0); //unlock
```

acquired lock while (CAS(&m,0,1) == false);Tried and failed while (CAS(&m, 0, 1) == false); while (CAS(&m, 0, 1) == false); What happens if we keep picking thread 1?

step 1 pick a thread

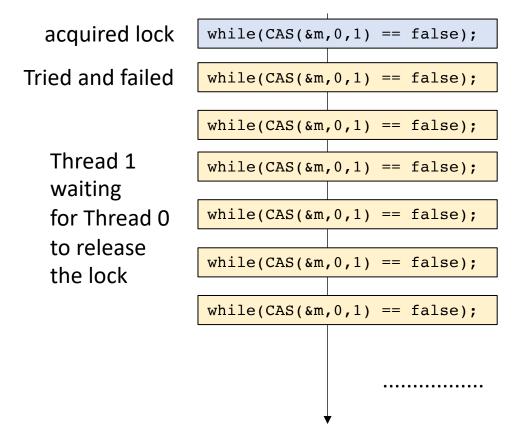
Keep track of next instruction
to execute

pick the next thread to execute

Keep track of next instruction to execute

```
Thread 0:
//lock
while(CAS(&m,0,1) == false);
int tmp = *bank_account;
tmp++;
*bank_account = tmp;
m.store(0); //unlock
```

```
Thread 1:
//lock
while(CAS(&m,0,1) == false);
int tmp = *bank_account;
tmp--;
*bank_account = tmp;
m.store(0); //unlock
```



Can this keep going forever?

Is this program guaranteed to terminate?

Why? Why not?

global timeline

A new way to represent concurrent executions

Global timeline fails to capture the full picture

- Introducing Labelled Transition System (LTS)
 - Concurrent execution in a graph form.

```
Thread 0:
0.0: while(CAS(&m,0,1) == false); //lock
    // critical section
0.1: m.store(0); //unlock
```

Lets only think about the locks and unlocks assume any critical section

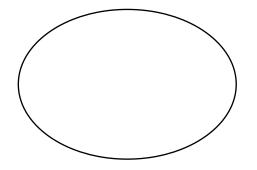
```
Thread 0:
0.0: while(CAS(&m,0,1) == false); //lock
    // critical section
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```

```
Thread 1:
1.0: while(CAS(&m,0,1) == false); //lock
    // critical section
1.1: m.store(0); //unlock
```

program location

Lets only think about the locks and unlocks assume any critical section

Start making our graph, with a starting node:



```
Thread 1:
1.0: while(CAS(&m,0,1) == false); //lock
    // critical section
1.1: m.store(0); //unlock
```

Start making our graph, with a starting node:

```
m:0
0:next_i:0.0
1:next_i:1.0
```

global variable values

```
Thread 1:
1.0: while(CAS(&m,0,1) == false); //lock
    // critical section
1.1: m.store(0); //unlock
```

Start making our graph, with a starting node:

```
m:0
0:next_i:0.0
1:next_i:1.0
```

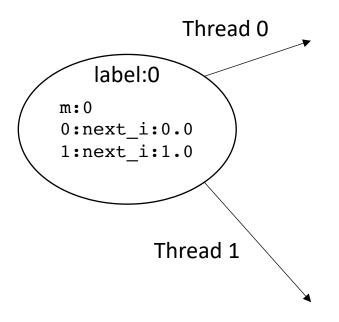
global variable values next instructions to execute

```
Thread 1:
1.0: while(CAS(&m,0,1) == false); //lock
    // critical section
1.1: m.store(0); //unlock
```

```
| label:0
| m:0
| 0:next_i:0.0
| 1:next_i:1.0
```

```
Thread 0:
0.0: while(CAS(&m,0,1) == false); //lock
    // critical section
0.1: m.store(0); //unlock
```

```
Thread 1:
1.0: while(CAS(&m,0,1) == false); //lock
    // critical section
1.1: m.store(0); //unlock
```



two choices: thread 0 executes, or thread 1 executes

```
Thread 0:
0.0: while(CAS(&m,0,1) == false); //lock
    // critical section
0.1: m.store(0); //unlock
```

```
label:1
                        m:??
                        0:next_i:??
                        1:next_i:??
           Thread 0
   label:0
m:0
0:next_i:0.0
1:next_i:1.0
        Thread 1
```

```
Thread 1:
1.0: while(CAS(&m,0,1) == false); //lock
    // critical section
1.1: m.store(0); //unlock
```

```
label:1
                        m:1
                        0:next_i:0.1
                        1:next_i:1.0
           Thread 0
   label:0
m:0
0:next_i:0.0
1:next_i:1.0
        Thread 1
```

```
label:1
                        m:1
                        0:next i:0.1
                        1:next_i:1.0
           Thread 0
   label:0
m:0
0:next_i:0.0
1:next_i:1.0
        Thread 1
                            label:2
                        m:??
                        0:next i:??
                        1:next_i:??
```

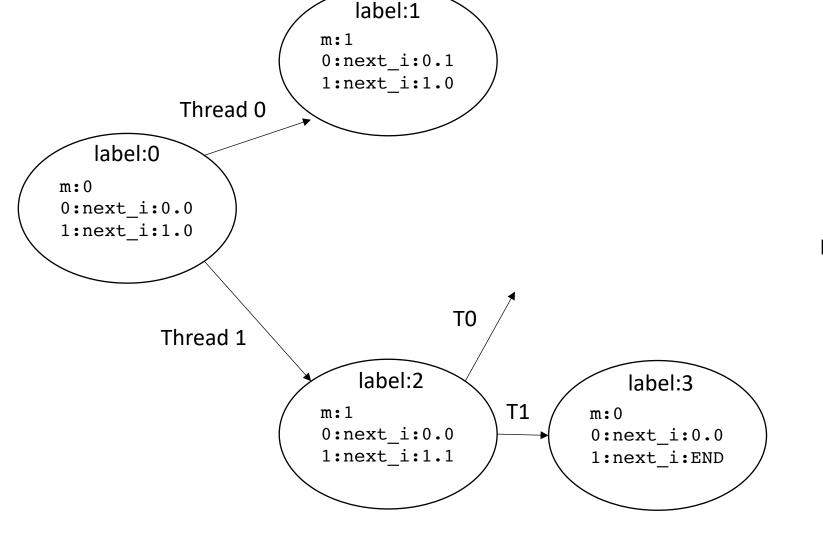
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Thread 1:
1.0: while(CAS(&m,0,1) == false); //lock
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```

```
label:1
                        m:1
                        0:next i:0.1
                        1:next_i:1.0
           Thread 0
   label:0
m:0
0:next_i:0.0
1:next_i:1.0
         Thread 1
                            label:2
                        m:1
                        0:next i:0.0
                        1:next_i:1.1
```

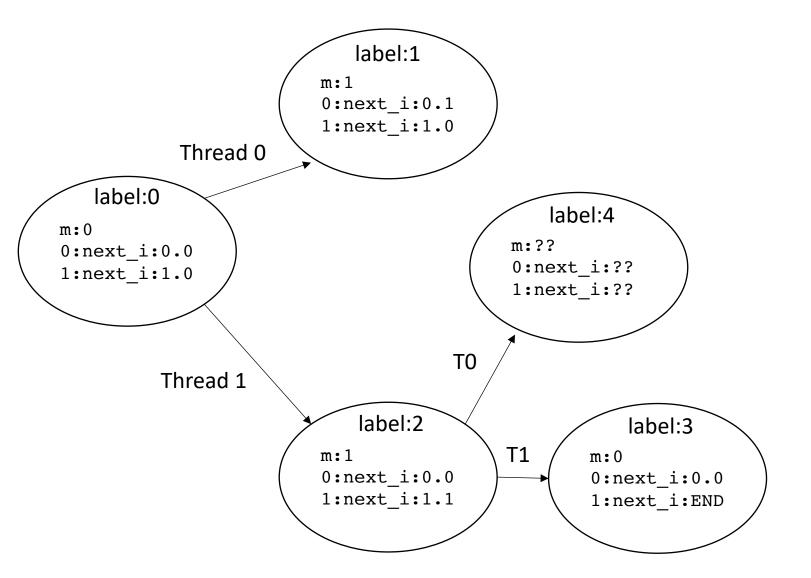
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0.1: m.store(0); //unlock
```

```
label:1
                        m:1
                        0:next i:0.1
                        1:next_i:1.0
           Thread 0
   label:0
m:0
0:next i:0.0
1:next_i:1.0
                                     T0
         Thread 1
                            label:2
                                          T1
                        m:1
                        0:next i:0.0
                        1:next_i:1.1
```

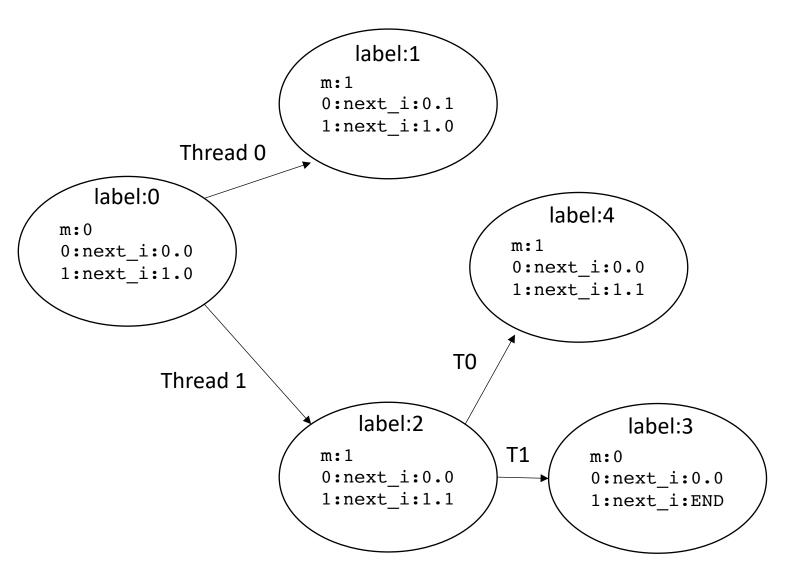
```
Thread 1:
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    // critical section
1.1: m.store(0); //unlock
```



```
Thread 0:
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0.1: m.store(0); //unlock
```

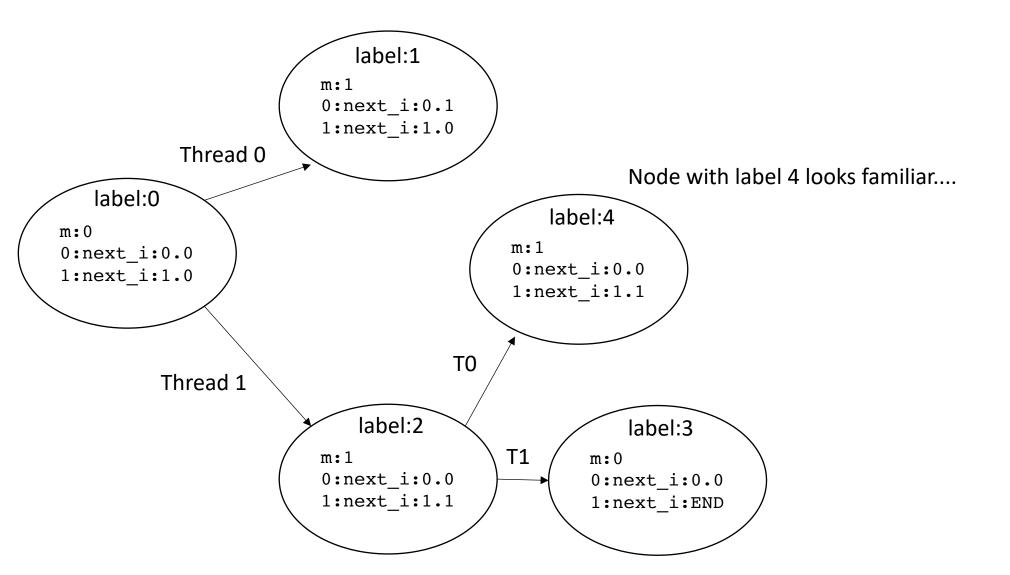


```
Thread 1:
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```



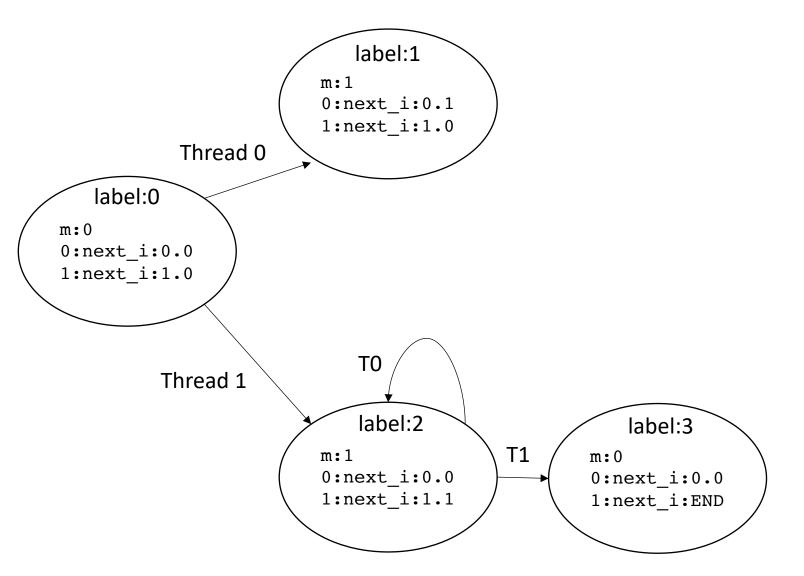
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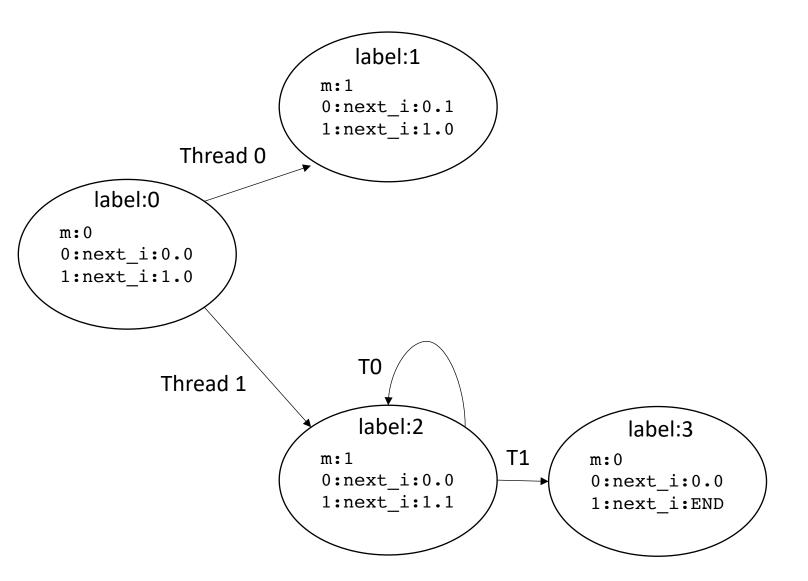


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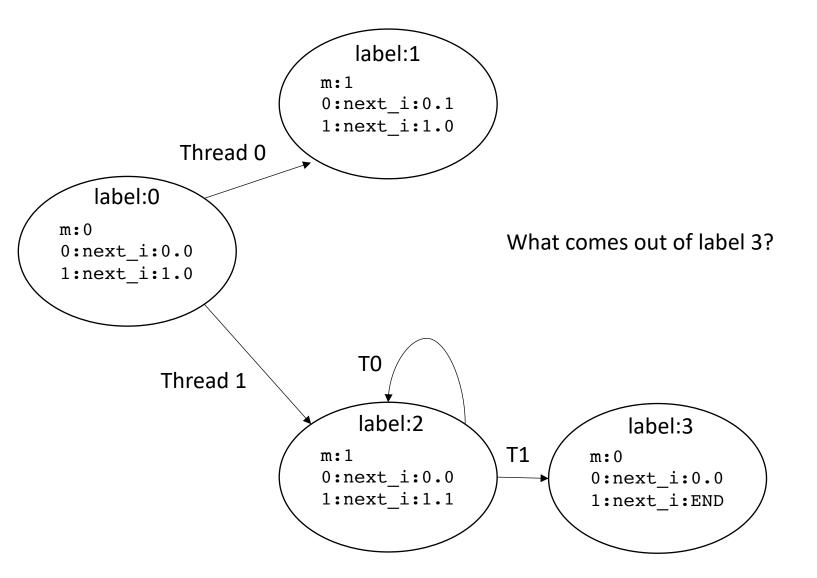


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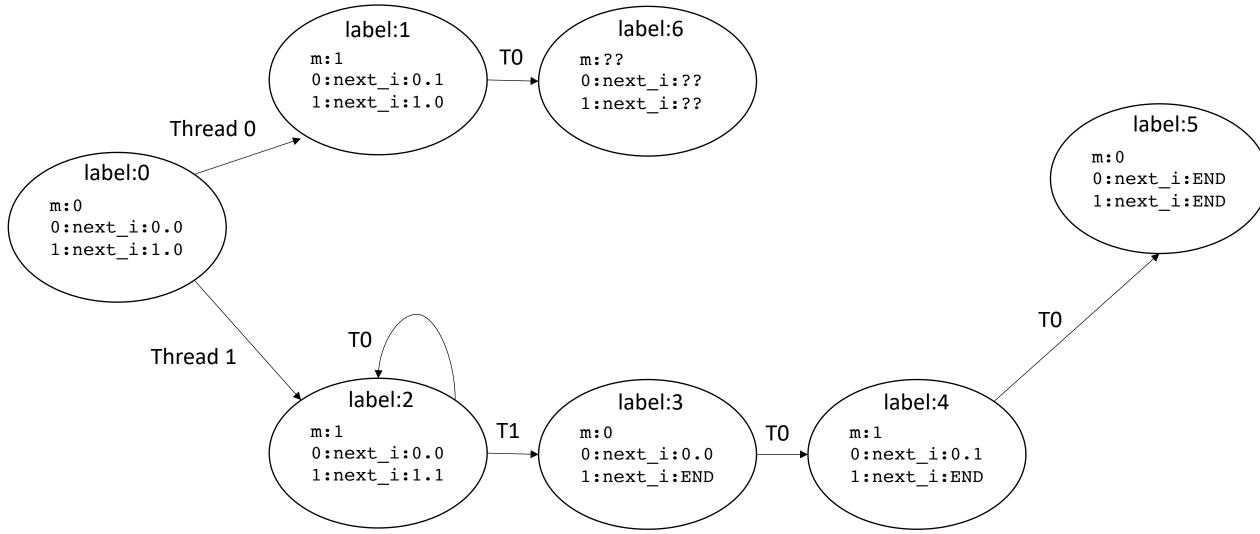
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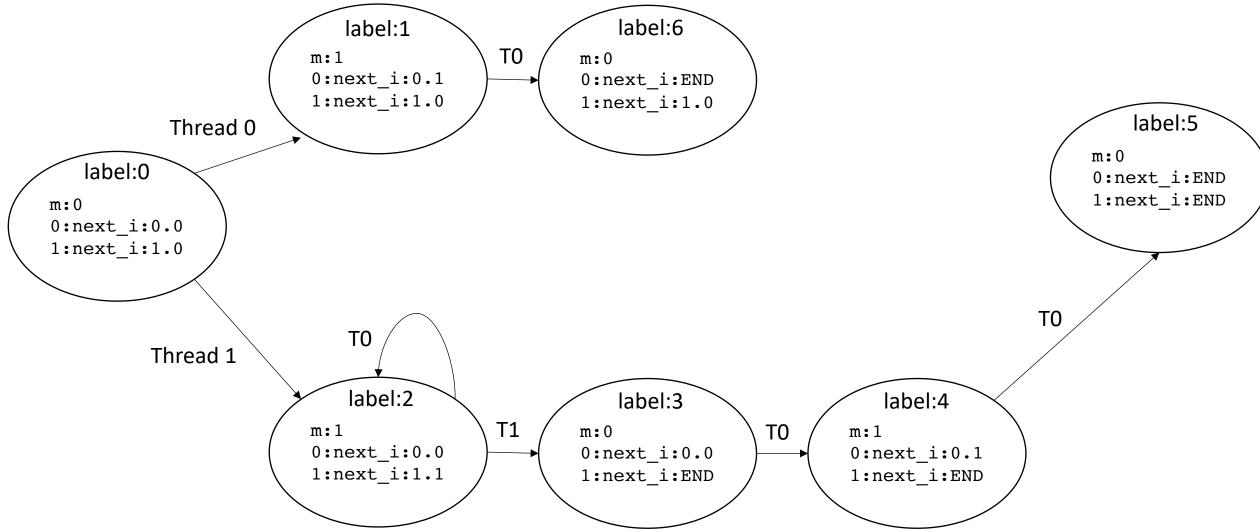
```
Thread 0:
                                                         Thread 1:
                                                         1.0: while (CAS(\&m, 0, 1) == false); //lock
0.0: while (CAS(\&m, 0, 1) == false); //lock
     // critical section
                                                               // critical section
0.1: m.store(0); //unlock
                                                         1.1: m.store(0); //unlock
                             label:1
                          m:1
                          0:next i:0.1
                          1:next_i:1.0
                                                                                                     label:5
             Thread 0
                                                                                                 m:0
      label:0
                                                                                                 0:next i:END
                                                                                                 1:next_i:END
  m:0
  0:next_i:0.0
   1:next i:1.0
                                                                                            TO
                              T0
            Thread 1
                              label:2
                                                      label:3
                                                                              label:4
                                           T1
                                                                   T0
                                                                           m:1
                          m:1
                                                  m:0
                          0:next i:0.0
                                                  0:next i:0.0
                                                                           0:next i:0.1
                          1:next_i:1.1
                                                  1:next i:END
                                                                           1:next i:END
```

```
Thread 0:
                                                          Thread 1:
                                                          1.0: while (CAS(\&m, 0, 1) == false); //lock
0.0: while (CAS(\&m, 0, 1) == false); //lock
     // critical section
                                                               // critical section
0.1: m.store(0); //unlock
                                                          1.1: m.store(0); //unlock
                             label:1
                          m:1
                          0:next i:0.1
                          1:next_i:1.0
                                                                                                     label:5
             Thread 0
                                                                                                 m:0
      label:0
                                                                                                 0:next i:END
                                                                                                 1:next_i:END
  m:0
                                                         Now from label 1
  0:next_i:0.0
   1:next i:1.0
                                                                                            TO
                              T0
            Thread 1
                              label:2
                                                      label:3
                                                                              label:4
                                           T1
                                                                   T0
                                                                           m:1
                          m:1
                                                   m:0
                          0:next i:0.0
                                                   0:next i:0.0
                                                                           0:next i:0.1
                          1:next_i:1.1
                                                   1:next i:END
                                                                           1:next i:END
```

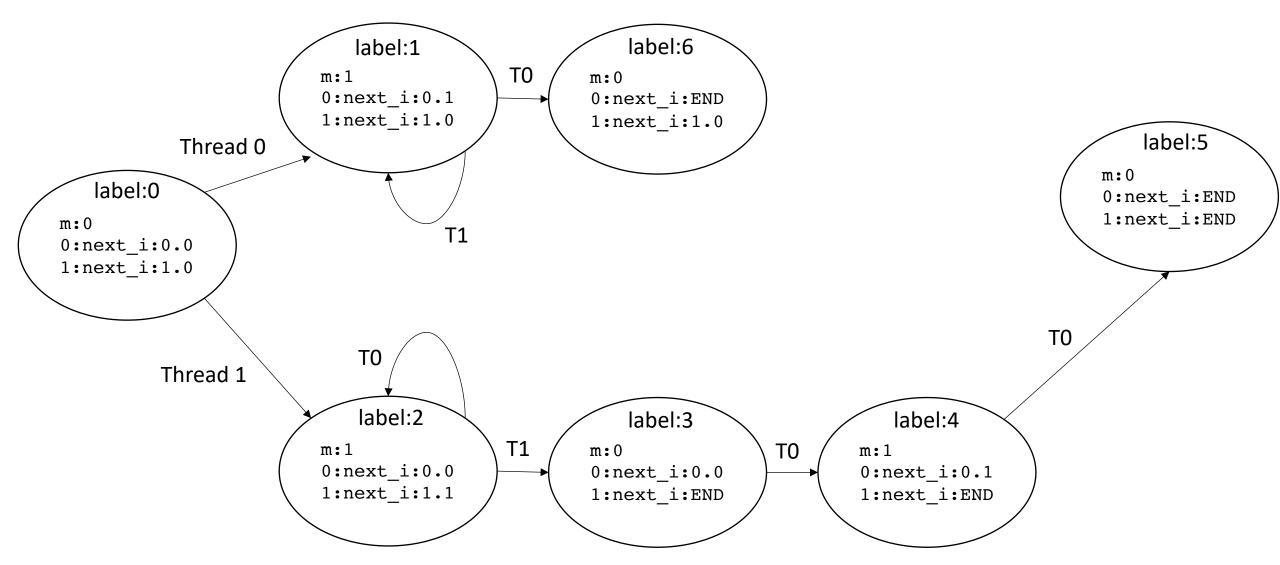
```
Thread 0:
0.0: while(CAS(&m,0,1) == false); //lock
    // critical section
0.1: m.store(0); //unlock
```



```
Thread 0:
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```

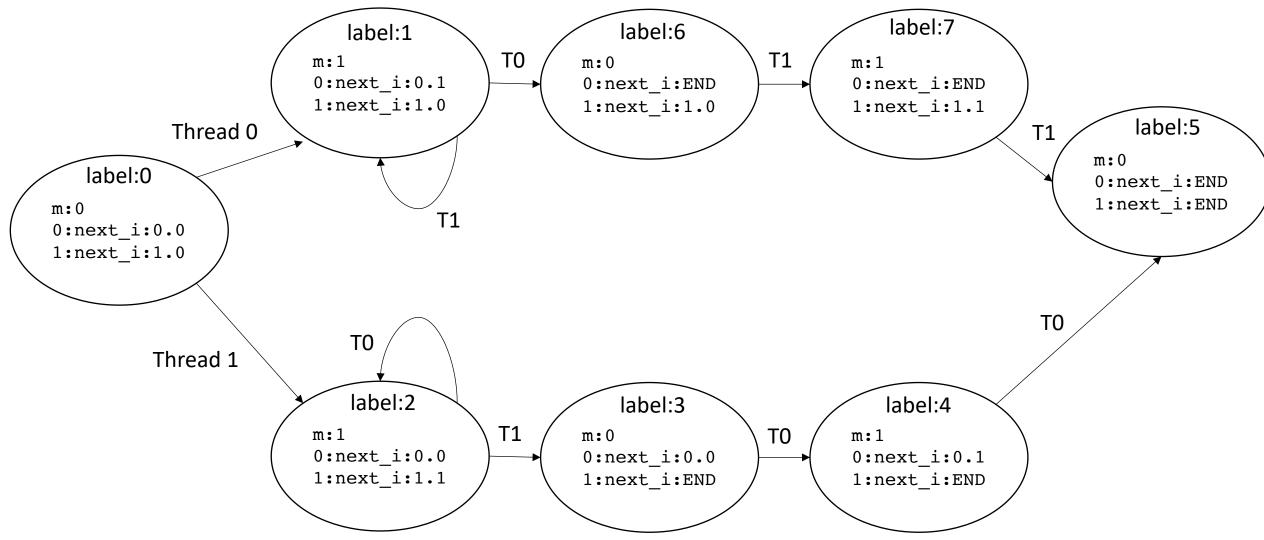


```
Thread 0:
0.0: while(CAS(&m,0,1) == false); //lock
    // critical section
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```



```
Thread 0:
0.0: while(CAS(&m,0,1) == false); //lock
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```

```
Thread 1:
1.0: while(CAS(&m,0,1) == false); //lock
    // critical section
1.1: m.store(0); //unlock
```



This is called an LTS

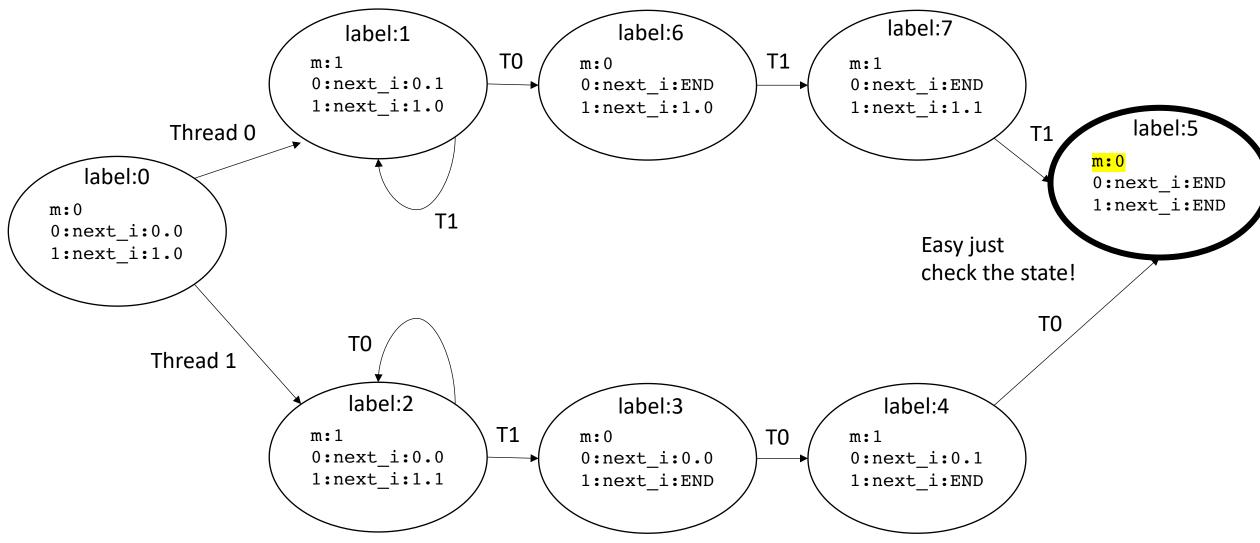
- A graph:
 - Each state encodes all variables/values and what the next instruction to execute is
 - Each edge out of a node is the different threads that can execute
 - A concurrent execution is any path through the LTS

```
Thread 0:
                                                                    Thread 1:
0.0: while (CAS(\&m, 0, 1) == false); //lock
                                                                    1.0: while (CAS(&m,0,1) == false); //lock
       // critical section
                                                                          // critical section
0.1: m.store(0); //unlock
                                                                    1.1: m.store(0); //unlock
                                                                                             label:7
                                                                label:6
                                   label:1
                                                   T0
                                                                                T1
                               m:1
                                                            m:0
                                                                                        m:1
                               0:next i:0.1
                                                            0:next i:END
                                                                                         0:next i:END
                               1:next_i:1.0
                                                            1:next i:1.0
                                                                                        1:next i:1.1
                                                                                                                       label:5
                Thread 0
                                                                                                            T1
                                                                                                                  m:0
       label:0
                                                                                                                  0:next i:END
                                                                                                                  1:next i:END
   m:0
                                                                    Examples:
                                            T1
   0:next i:0.0
                                                                    0 \rightarrow 1 \rightarrow 6 \rightarrow 7 \rightarrow 5
   1:next i:1.0
                                                                    0 \rightarrow 2 \rightarrow 2 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 5
                                                                                                             TO
                                   T0
              Thread 1
                                   label:2
                                                                label:3
                                                                                            label:4
                                                   T1
                                                                               T0
                                                            m:0
                                                                                        m:1
                               m:1
                               0:next i:0.0
                                                            0:next i:0.0
                                                                                        0:next i:0.1
                               1:next i:1.1
                                                            1:next i:END
                                                                                        1:next i:END
```

What is this good for?

• Given this LTS, what kind of questions can we ask?

- Example:
 - At the end of the program, I want to prove that the mutex will not be taken



Safety property

- Something bad will never happen
 - i.e. the program will not exit with the mutex taken
 - can be specified with assert statements in the program
- Easy to check in a LTS: just search the states
 - You have all the values, easy to check if something is wrong!

However...

Safety is only half of the picture

- Self driving car example:
 - Design a car that never crashes (safety property)

However...

Safety is only half of the picture

- Self driving car example:
 - Design a car that never crashes (safety property)
 - Easy! Just design a car that can't move!
 - We need include something else in the specification:

Liveness property

Something good will eventually happen

- Examples:
 - The mutex program will eventually terminate
 - The self driving car will eventually reach its destination
- More difficult to reason about that safety properties

```
Thread 0:
                                                            Thread 1:
0.0: while (CAS(\&m, 0, 1) == false); //lock
                                                            1.0: while (CAS(&m,0,1) == false); //lock
      // critical section
                                                                  // critical section
0.1: m.store(0); //unlock
                                                            1.1: m.store(0); //unlock
Is this program
guaranteed to
                                                                                 label:7
                                                        label:6
                               label:1
terminate?
                                             T0
                                                                      T1
                           m:1
                                                     m:0
                                                                              m:1
What could go
                           0:next i:0.1
                                                     0:next i:END
                                                                              0:next i:END
wrong?
                           1:next_i:1.0
                                                     1:next i:1.0
                                                                              1:next i:1.1
                                                                                                        label:5
              Thread 0
                                                                                               T1
                                                                                                    m:0
      label:0
                                                                                                    0:next i:END
                                                                                                    1:next_i:END
   m:0
                                       T1
   0:next i:0.0
   1:next i:1.0
                                                                                                TO
                               T0
            Thread 1
                               label:2
                                                        label:3
                                                                                 label:4
                                             T1
                                                                      T0
                                                                              m:1
                           m:1
                                                     m:0
                           0:next i:0.0
                                                     0:next i:0.0
                                                                              0:next i:0.1
                           1:next i:1.1
                                                     1:next i:END
                                                                              1:next i:END
```

```
Thread 0:
                                                                         Thread 1:
0.0: while (CAS(\&m, 0, 1) == false); //lock
                                                                         1.0: while (CAS(&m,0,1) == false); //lock
       // critical section
                                                                                // critical section
0.1: m.store(0); //unlock
                                                                         1.1: m.store(0); //unlock
Is this program
guaranteed to
                                                                                                   label:7
                                                                    label:6
                                     label:1
terminate?
                                                       T0
                                                                                     T1
                                 m:1
                                                                m:0
                                                                                               m:1
What could go
                                 0:next i:0.1
                                                                0:next i:END
                                                                                               0:next i:END
wrong?
                                 1:next i:1.0
                                                                1:next i:1.0
                                                                                               1:next i:1.1
                                                                                                                               label:5
                 Thread 0
                                                                                                                   T1
                                                                                                                          m:0
        label:0
                                                                                                                          0:next i:END
                                                                                                                          1:next i:END
    m:0
                                                                         Forever?
                                                T1
    0:next i:0.0
                                                                         0 \rightarrow 1 \dots
    1:next i:1.0
                                                                         0 \rightarrow 2 \dots
                                                                                                                     T0
                                      T0
               Thread 1
                                      label:2
                                                                    label:3
                                                                                                   label:4
                                                       T1
                                                                                     T0
                                                                m:0
                                                                                               m:1
                                 m:1
                                 0:next i:0.0
                                                                0:next i:0.0
                                                                                               0:next i:0.1
                                 1:next i:1.1
                                                                1:next i:END
                                                                                               1:next i:END
```

Liveness

- Starvation cycles
 - There exists a thread that can break the system out of a cycle, but that thread never executes (i.e. it is starved).
- Can starvation cycles happen?

Liveness

- Starvation cycles
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 - Depends on your scheduler!
 - With no scheduler guarantees, they cannot be ruled out!

Liveness

- Starvation cycles
 - There exists a thread that can break the system out of a cycle, but that thread never executes (i.e. it is starved).
- Can starvation cycles happen?
 - Depends on your scheduler!
 - With no scheduler guarantees, they cannot be ruled out!
- Note that we are talking about scheduler specifications, actual implementations are very complicated (take an OS class to learn more)

Schedule

Labeled Transition Systems

Scheduler specifications

5 minute break

The fair scheduler

- every thread that has not terminated will "eventually" get a chance to execute.
 - "concurrent forward progress": defined by C++
 not guaranteed, but encouraged (and likely what you will observe)
 - "weakly fair scheduler": defined by classic concurrency textbooks
- The fair scheduler disallows starvation cycles
 - waiting will always be finite (but no bounds on time)

```
Thread 0:
                                                                        Thread 1:
0.0: while (CAS(&m,0,1) == false); //lock
                                                                        1.0: while (CAS(&m,0,1) == false); //lock
       // critical section
                                                                               // critical section
0.1: m.store(0); //unlock
                                                                        1.1: m.store(0); //unlock
What about a
fair scheduler?
                                                                                                   label:7
                                                                    label:6
                                     label:1
                                                       T0
                                                                                     T1
                                 m:1
                                                                m:0
                                                                                              m:1
                                 0:next i:0.1
                                                                0:next i:END
                                                                                              0:next i:END
                                 1:next i:1.0
                                                                1:next i:1.0
                                                                                              1:next i:1.1
                                                                                                                              label:5
                 Thread 0
                                                                                                                   T1
                                                                                                                         m:0
        label:0
                                                                                                                          0:next i:END
                                                                                                                          1:next i:END
    m:0
                                                                         Forever?
                                               T1
    0:next i:0.0
                                                                        0 \rightarrow 1 \dots
    1:next i:1.0
                                                                        0 \rightarrow 2 \dots
                                                                                                                    T0
                                      T0
               Thread 1
                                      label:2
                                                                    label:3
                                                                                                  label:4
                                                      T1
                                                                                    T0
                                                                                              m:1
                                 m:1
                                                                m:0
                                 0:next i:0.0
                                                                0:next i:0.0
                                                                                              0:next i:0.1
                                 1:next i:1.1
                                                                1:next i:END
                                                                                              1:next i:END
```

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                                                                                                   label:7
                                                                    label:6
                                     label:1
                                                       T0
                                                                                     T1
                                 m:1
                                                                m:0
                                                                                              m:1
                                 0:next i:0.1
                                                                0:next i:END
                                                                                              0:next i:END
                                 1:next i:1.0
                                                                1:next i:1.0
                                                                                              1:next i:1.1
                                                                                                                               label:5
                 Thread 0
                                                                                                                   T1
                                                                                                                          m:0
        label:0
                                                                                                                          0:next i:END
                                                                                                                          1:next i:END
    m:0
                                                                         Forever?
                                               T1
    0:next i:0.0
                                                                         0 \rightarrow 1 \dots
    1:next i:1.0
                                                                         0 \rightarrow 2 \dots
                                                                                                                    T0
                                      T0
               Thread 1
                                      label:2
                                                                    label:3
                                                                                                  label:4
                                                      T1
                                                                                     T0
                                                                                              m:1
                                 m:1
                                                                m:0
                                 0:next i:0.0
                                                                0:next i:0.0
                                                                                              0:next i:0.1
                                 1:next i:1.1
                                                                1:next i:END
                                                                                              1:next i:END
```

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What about a
fair scheduler?
                                                                                                   label:7
                                                                    label:6
                                     label:1
                                                       T0
                                                                                     T1
                                 m:1
                                                                m:0
                                                                                               m:1
                                 0:next i:0.1
                                                                0:next i:END
                                                                                               0:next i:END
                                 1:next i:1.0
                                                                1:next i:1.0
                                                                                               1:next i:1.1
                                                                                                                               label:5
                 Thread 0
                                                                                                                   T1
                                                                                                                          m:0
        label:0
                                                                                                                          0:next i:END
                                                                                                                          1:next i:END
    m:0
                                                                         Forever?
                                                T1
    0:next i:0.0
                                                         disallowed!
                                                                         0 \rightarrow 1 \dots
    1:next i:1.0
                                                                         0 \rightarrow 2 \dots
                                                                                                                    T0
                                      T0
               Thread 1
                                      label:2
                                                                    label:3
                                                                                                   label:4
                                                       T1
                                                                                     T0
                                                                                               m:1
                                 m:1
                                                                m:0
                                 0:next i:0.0
                                                                0:next i:0.0
                                                                                               0:next i:0.1
                                 1:next i:1.1
                                                                1:next i:END
                                                                                               1:next i:END
```

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What about a
fair scheduler?
                                                                                                   label:7
                                                                    label:6
                                     label:1
                                                       T0
                                                                                     T1
                                 m:1
                                                                m:0
                                                                                               m:1
                                 0:next i:0.1
                                                                0:next i:END
                                                                                               0:next i:END
                                 1:next i:1.0
                                                                1:next i:1.0
                                                                                               1:next i:1.1
                                                                                                                               label:5
                 Thread 0
                                                                                                                   T1
                                                                                                                          m:0
        label:0
                                                                                                                          0:next i:END
                                                                                                                          1:next i:END
    m:0
                                                                         Forever?
                                                T1
    0:next i:0.0
                                                         disallowed!
                                                                         0 \rightarrow 1 \dots
    1:next i:1.0
                                                                         0 \rightarrow 2 \dots
                                                                                                                    T0
                                      T0
               Thread 1
                                      label:2
                                                                    label:3
                                                                                                   label:4
                                                       T1
                                                                                     T0
                                                                                               m:1
                                 m:1
                                                                m:0
                                 0:next i:0.0
                                                                0:next i:0.0
                                                                                               0:next i:0.1
                                 1:next i:1.1
                                                                1:next i:END
                                                                                               1:next i:END
```

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                                                                                // critical section
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What about a
fair scheduler?
                                                                                                   label:7
                                                                    label:6
                                     label:1
                                                       T0
                                                                                     T1
                                 m:1
                                                                m:0
                                                                                              m:1
                                 0:next i:0.1
                                                                0:next i:END
                                                                                               0:next i:END
                                 1:next i:1.0
                                                                1:next i:1.0
                                                                                               1:next i:1.1
                                                                                                                               label:5
                 Thread 0
                                                                                                                   T1
                                                                                                                          m:0
        label:0
                                                                                                                          0:next i:END
                                                                                                                          1:next i:END
    m:0
                                                                         Forever?
                                               T1
    0:next i:0.0
                                                         disallowed!
                                                                         0 \rightarrow 1 \dots
    1:next i:1.0
                                                         disallowed!
                                                                        0 \rightarrow 2 \dots
                                                                             Only other paths
                                                                                                                    T0
                                      TO
                                                                             reach the end
               Thread 1
                                      label:2
                                                                    label:3
                                                                                                  label:4
                                                       T1
                                                                                     T0
                                                                                              m:1
                                 m:1
                                                                m:0
                                 0:next i:0.0
                                                                0:next i:0.0
                                                                                              0:next i:0.1
                                 1:next i:1.1
                                                                1:next i:END
                                                                                              1:next i:END
```

A fair scheduler typically requires preemption



Core 0

resources



Operating System

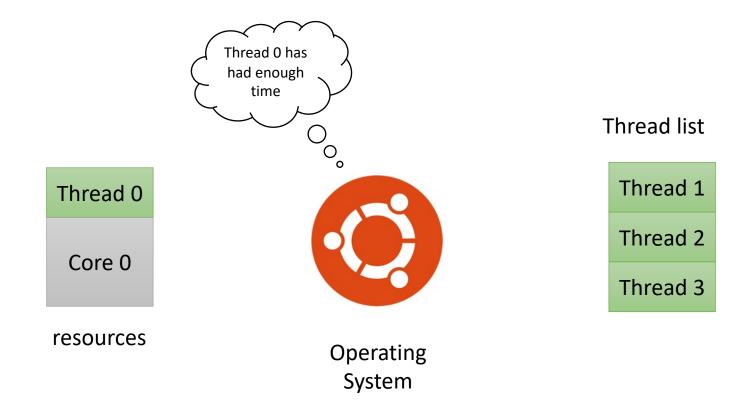
Thread list

Thread 1

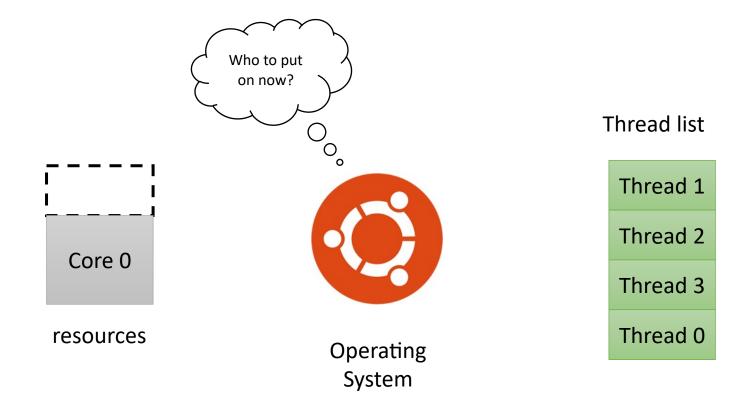
Thread 2

Thread 3

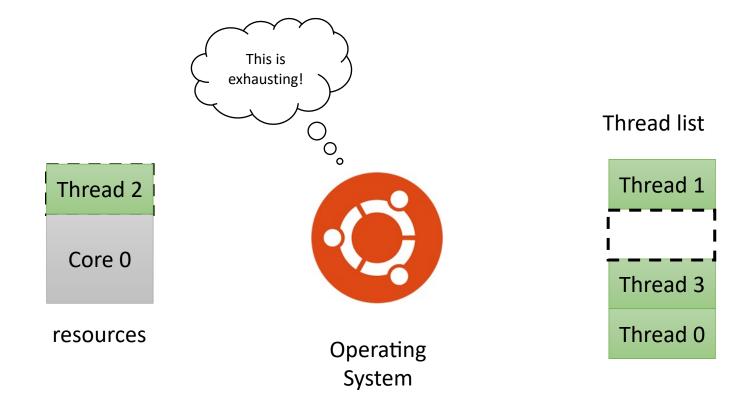
A fair scheduler typically requires preemption



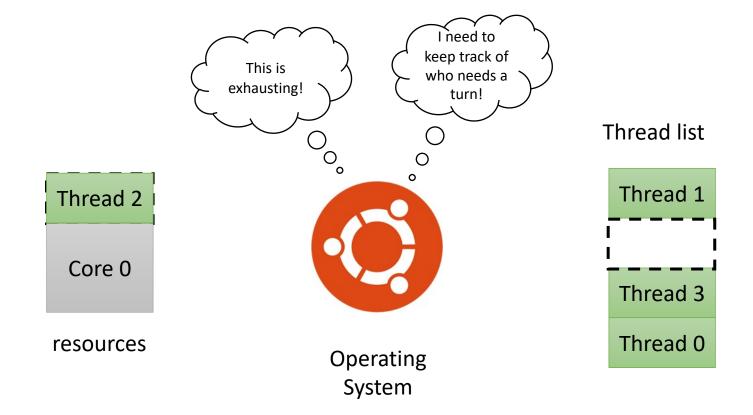
A fair scheduler typically requires preemption



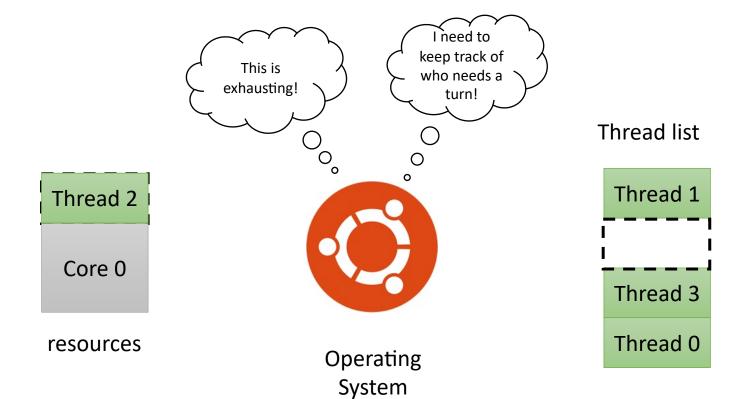
A fair scheduler typically requires preemption



• A fair scheduler typically requires preemption



A fair scheduler typically requires preemption



peak into a thread object:

• A fair scheduler typically requires preemption



peak into a thread object:

Thread 1: program data local variables

Estimated to be ~30K cycles to context switch between threads

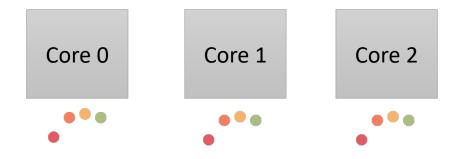
• Systems might not support preemption: e.g. GPUs

simplified execution model

Program with 5 threads



thread pool



Device with 3 Cores

finished threads

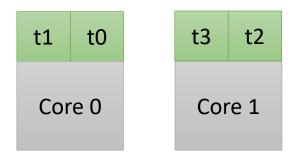
Solutions?

• I have N cores, only run N threads?

Solutions?

• I have N cores, only run N threads?

sometimes concurrency can help hide latency! Don't want to completely disallow it!



Device with 2 cores



Solutions?

• I have N cores, only run N threads?

- GPU examples:
 - Depending on program size Nvidia GPUs support
 - 32 threads per core for small programs
 - 2 threads per core for big programs
- We need a better specification

Parallel Forward Progress

 "Any thread that has executed at least 1 instruction, is guaranteed to continue to be fairly executed"

Also called:

- "Parallel Forward Progress": by C++
- "Persistent Thread Model": by GPU programmers
- "Occupancy Bound Execution Model": in some of my papers

```
Thread 0:
                                                                          Thread 1:
0.0: while (CAS(\&m, 0, 1) == false); //lock
                                                                          1.0: while (CAS(&m,0,1) == false); //lock
        // critical section
                                                                                 // critical section
0.1: m.store(0); //unlock
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Any thread that has
executed at least 1
                                                                                                    label:7
                                                                     label:6
                                      label:1
instruction, is
                                                        T0
                                                                                      T1
                                  m:1
                                                                 m:0
                                                                                                m:1
guaranteed to
                                  0:next i:0.1
                                                                 0:next i:END
                                                                                                0:next i:END
continue to be fairly
                                  1:next i:1.0
                                                                 1:next i:1.0
                                                                                                1:next i:1.1
executed
                                                                                                                                label:5
                                                                                                                     T1
                                                                                                                            m:0
        label:0
                           Thread 0
                                                                                                                            0:next i:END
                                                                                                                            1:next i:END
    m:0
                                                                          Forever?
                                                T1
    0:next i:0.0
                                                                          0 \rightarrow 1 \dots
    1:next i:1.0
                                                                          0 \rightarrow 2 \dots
                                                                                                                      T0
                                      T0
               Thread 1
                                      label:2
                                                                     label:3
                                                                                                    label:4
                                                       T1
                                                                                      T0
                                                                                                m:1
                                  m:1
                                                                 m:0
                                  0:next i:0.0
                                                                 0:next i:0.0
                                                                                                0:next i:0.1
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                                                                 1:next i:END
                                                                                                1:next i:END
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                                                        T0
                                                                                      T1
                                  m:1
                                                                 m:0
                                                                                                m:1
guaranteed to
                                  0:next i:0.1
                                                                 0:next i:END
                                                                                                0:next i:END
continue to be fairly
                                  1:next i:1.0
                                                                 1:next i:1.0
                                                                                                1:next i:1.1
executed
                                                                                                                                 label:5
                                                                                                                     T1
                                                                                                                            m:0
        label:0
                           Thread 0
                                                                                                                            0:next i:END
                                                                                                                            1:next i:END
    m:0
                                                                          Forever?
                                                T1
    0:next i:0.0
                                                                          0 \rightarrow 1 \dots
    1:next i:1.0
                                                                          0 \rightarrow 2 \dots
                                                                                                                      T0
                                      T0
               Thread 1
                                      label:2
                                                                     label:3
                                                                                                    label:4
                                                       T1
                                                                                      T0
                                                                                                m:1
                                  m:1
                                                                 m:0
                                  0:next i:0.0
                                                                 0:next i:0.0
                                                                                                0:next i:0.1
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                                                                 1:next i:END
                                                                                                1:next i:END
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                                                        T0
                                                                                      T1
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                                                                 m:0
                                                                                               m:1
guaranteed to
                                  0:next i:0.1
                                                                 0:next i:END
                                                                                                0:next i:END
continue to be fairly
                                  1:next i:1.0
                                                                 1:next i:1.0
                                                                                                1:next i:1.1
executed
                                                                                                                                label:5
                                                                                                                    T1
                                                                                                                           m:0
        label:0
                           Thread 0
                                                                                                                           0:next i:END
                                                                                                                           1:next i:END
    m:0
                                                                          Forever?
                                                T1
    0:next i:0.0
                                                            disallowed 0 \rightarrow 1 \dots
    1:next i:1.0
                                                                          0 \rightarrow 2 \dots
                                                                                                                      T0
                                      T0
               Thread 1
                                      label:2
                                                                     label:3
                                                                                                    label:4
                                                       T1
                                                                                      T0
                                                                                               m:1
                                  m:1
                                                                 m:0
                                  0:next i:0.0
                                                                 0:next i:0.0
                                                                                                0:next i:0.1
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                                                                                                1:next i:END
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                                                                                      T1
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                                                                m:0
                                                                                               m:1
guaranteed to
                                  0:next i:0.1
                                                                 0:next i:END
                                                                                                0:next i:END
continue to be fairly
                                  1:next i:1.0
                                                                1:next i:1.0
                                                                                                1:next i:1.1
executed
                                                                                                                                label:5
                                                                                                                    T1
                                                                                                                           m:0
        label:0
                           Thread 0
                                                                                                                           0:next i:END
                                                                                                                           1:next i:END
    m:0
                                                                          Forever?
                                                T1
    0:next i:0.0
                                                            disallowed 0 \rightarrow 1 \dots
    1:next i:1.0
                                                                         0 \rightarrow 2 \dots
                                                                                                                     T0
                                      T0
               Thread 1
                                      label:2
                                                                     label:3
                                                                                                   label:4
                                                       T1
                                                                                      T0
                                                                                               m:1
                                  m:1
                                                                m:0
                                  0:next i:0.0
                                                                 0:next i:0.0
                                                                                               0:next i:0.1
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                                                       T0
                                                                                      T1
                                 m:1
                                                                m:0
                                                                                               m:1
guaranteed to
                                  0:next i:0.1
                                                                 0:next i:END
                                                                                               0:next i:END
continue to be fairly
                                  1:next i:1.0
                                                                1:next i:1.0
                                                                                               1:next i:1.1
executed
                                                                                                                                label:5
                                                                                                                    T1
                                                                                                                           m:0
        label:0
                           Thread 0
                                                                                                                           0:next i:END
                                                                                                                           1:next i:END
    m:0
                                                                         Forever?
                                                T1
    0:next i:0.0
                                                            disallowed 0 \rightarrow 1 \dots
    1:next i:1.0
                                                            disallowed 0 \rightarrow 2 \dots
                                                                                                                     T0
                                      T0
               Thread 1
                                      label:2
                                                                     label:3
                                                                                                   label:4
                                                       T1
                                                                                      T0
                                                                                               m:1
                                 m:1
                                                                m:0
                                  0:next i:0.0
                                                                 0:next i:0.0
                                                                                               0:next i:0.1
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                                                                                               1:next i:END
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                                                                m:0
                                                                                              m:1
guaranteed to
                                 0:next i:0.1
                                                                0:next i:END
                                                                                               0:next i:END
continue to be fairly
                                 1:next i:1.0
                                                                1:next i:1.0
                                                                                               1:next i:1.1
executed
                                                                                                                               label:5
                                                                                                                   T1
                                                                                                                          m:0
        label:0
                           Thread 0
                                                                                                                          0:next i:END
                                                                                                                          1:next i:END
    m:0
                                                                         Forever?
                                                T1
    0:next i:0.0
                                                           disallowed 0 \rightarrow 1 \dots
    1:next i:1.0
                                                            disallowed 0 \rightarrow 2 \dots
                                                                        Mutexes will terminate under
                                                                                                                    T0
                                      T0
                                                                        the parallel scheduler
               Thread 1
                                      label:2
                                                                    label:3
                                                                                                   label:4
                                                       T1
                                                                                     T0
                                                                                              m:1
                                 m:1
                                                                m:0
                                 0:next i:0.0
                                                                0:next i:0.0
                                                                                               0:next i:0.1
                                 1:next i:1.1
                                                                1:next i:END
                                                                                               1:next i:END
```

Another example

- Producer consumer
 - Thread 0 waits for Thread 1 to write a flag

```
Thread 0:
```

```
0.0: while(flag.load() == 0);
```

```
Thread 1:
1.0: flag.store(1);
```

```
Thread 0:
```

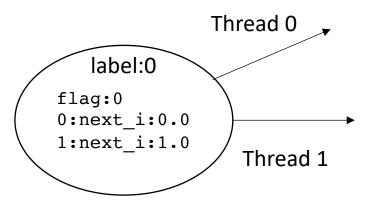
```
0.0: while(flag.load() == 0);
```

start with initial node

```
label:0
flag:0
0:next_i:0.0
1:next_i:1.0
```

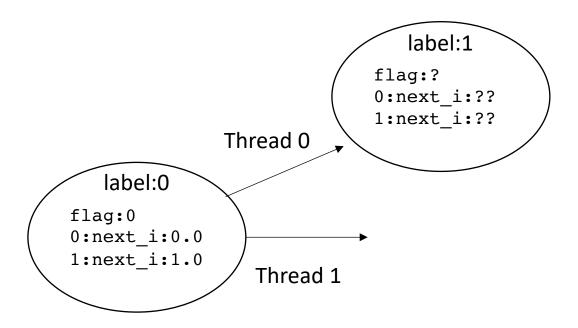
```
Thread 0:
```

```
0.0: while(flag.load() == 0);
```



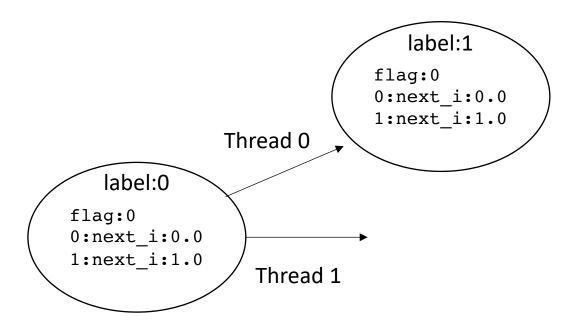
```
Thread 0:
```

```
0.0: while(flag.load() == 0);
```



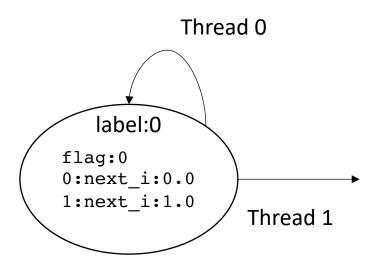
```
Thread 0:
```

```
0.0: while(flag.load() == 0);
```



Thread 0:

0.0: while(flag.load() == 0);

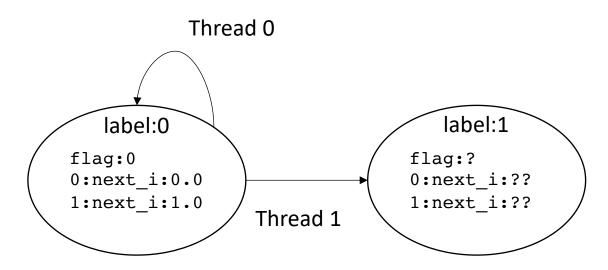


Thread 1:

1.0: flag.store(1);

```
Thread 0:
```

```
0.0: while(flag.load() == 0);
```

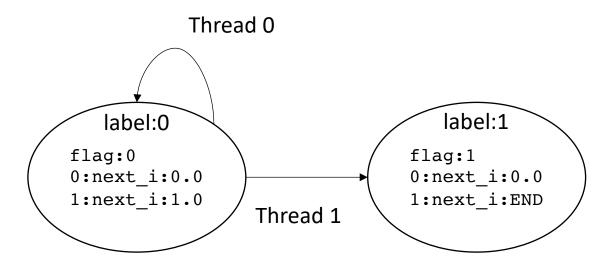


Thread 1:

1.0: flag.store(1);

```
Thread 0:
```

```
0.0: while(flag.load() == 0);
```

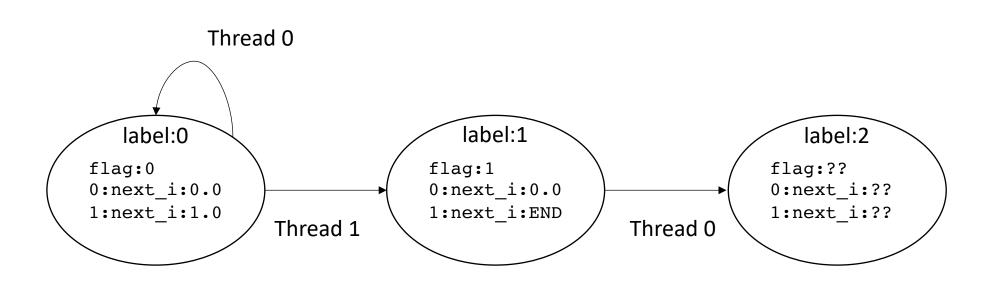


Thread 1:

1.0: flag.store(1);

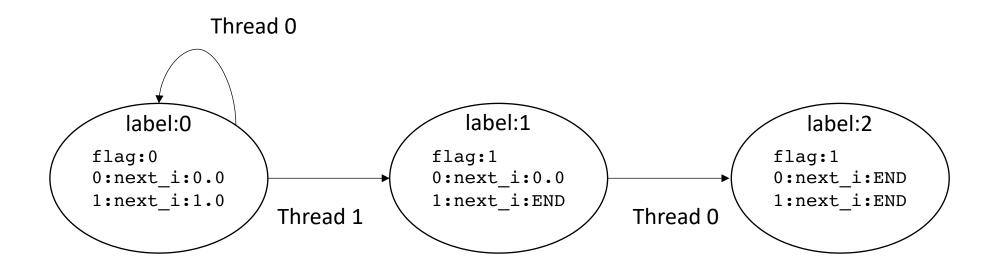
```
Thread 0:
```

```
0.0: while(flag.load() == 0);
```



Thread 0: 0.0: while(flag.load() == 0);

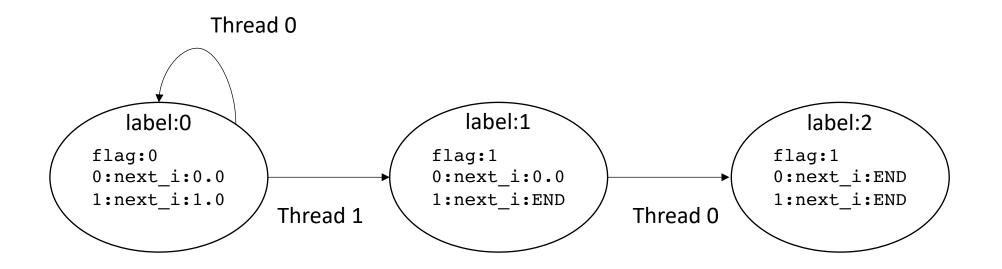
```
Thread 1:
1.0: flag.store(1);
```



```
Thread 0:
0.0: while(flag.load() == 0);
```

```
Thread 1:
1.0: flag.store(1);
```

Is this program guaranteed to terminate under the fair scheduler?

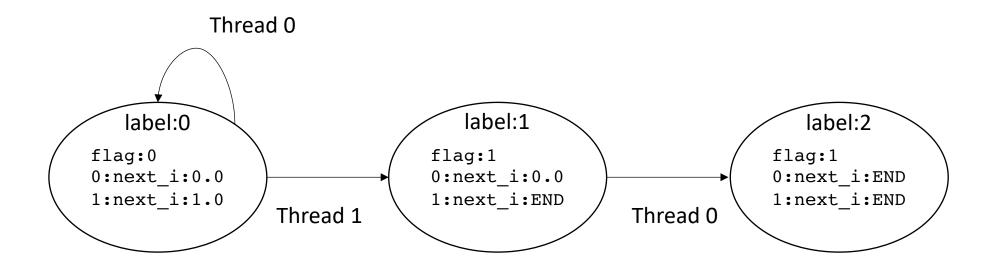


```
\frac{Thread 0:}{0.0: while(flag.load() == 0);}
```

```
Thread 1:
1.0: flag.store(1);
```

Is this program guaranteed to terminate under the fair scheduler?

Is this program guaranteed to terminate under the parallel scheduler?



```
Thread 0:
```

0.0: while(flag.load() == 0);

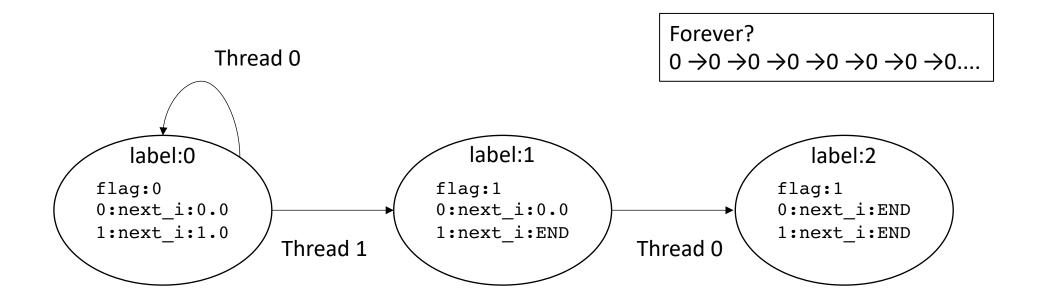
```
Thread 1:
```

1.0: flag.store(1);

Is this program guaranteed to terminate under the fair scheduler?

Is this program guaranteed to terminate under the parallel scheduler?

Any thread that has executed at least 1 instruction, is guaranteed to continue to be fairly executed



Thread 0:

0.0: while(flag.load() == 0);

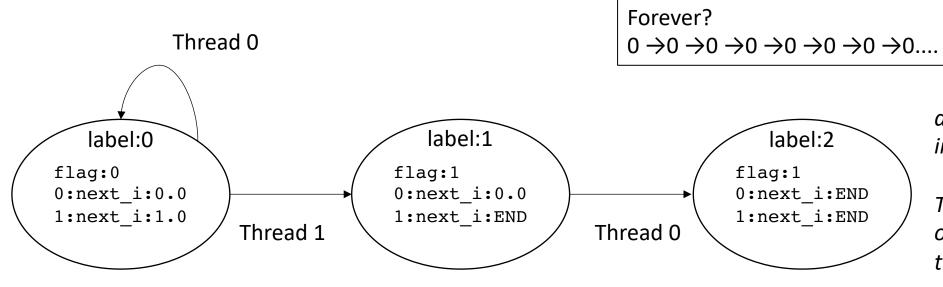
```
Thread 1:
```

1.0: flag.store(1);

Is this program guaranteed to terminate under the fair scheduler?

Is this program guaranteed to terminate under the parallel scheduler?

Any thread that has executed at least 1 instruction, is guaranteed to continue to be fairly executed



allowed to spin forever in the parallel scheduler!

Thread 0 could be scheduled on the only core while thread 1 spins

• In some cases the Parallel scheduler might be too strong

For example dynamic power management on mobile devices

Program with 5 threads



thread pool

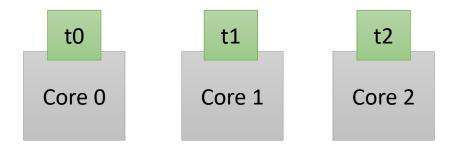
Core 0

Core 1

Core 2

Device with 3 Cores

Program with 5 threads thread pool

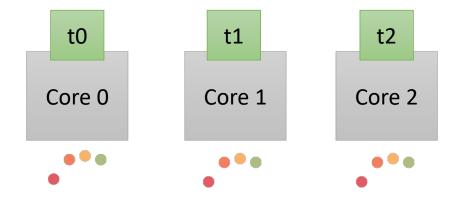


Device with 3 Cores

Program with 5 threads



thread pool



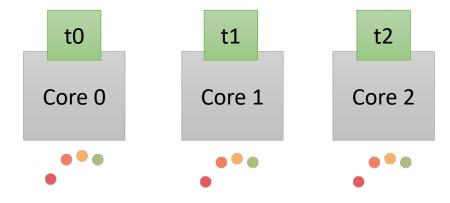
Device with 3 Cores

Program with 5 threads

t4 t3

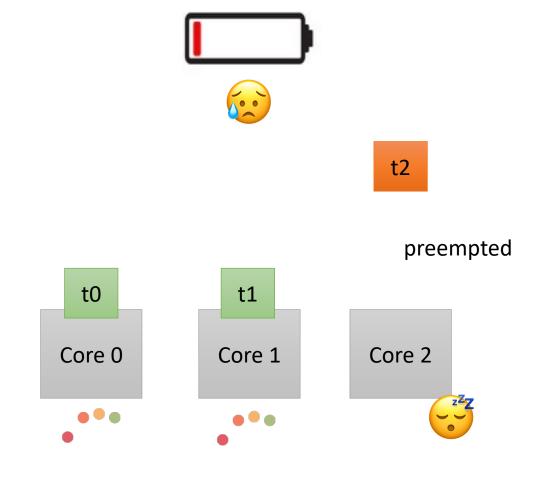
thread pool





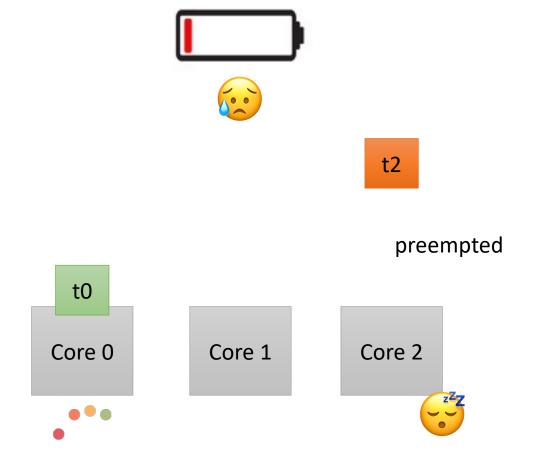
Device with 3 Cores

Program with 5 threads thread pool



Device with 3 Cores

Program with 5 threads thread pool



Device with 3 Cores

t1

Program with 5 threads

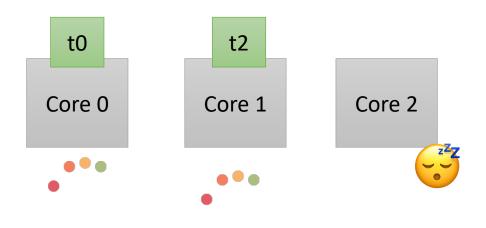
t4 t3

thread pool



t1

finished threads



Device with 3 Cores

Schedulers

 This power-saving optimization messes up the Parallel Scheduler guarantees

Can we do anything interesting with a scheduler like this?

Schedulers

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 The OS can give guarantees about the threads that it preempts for energy savings.

Schedulers

 This power-saving optimization messes up the Parallel Scheduler guarantees

Can we do anything interesting with a scheduler like this?

 The OS can give guarantees about the threads that it preempts for energy savings.

 The OS could target threads with higher ids and give priority with threads with the lower id.

The HSA schduler

• The thread with the lowest ID that hasn't terminated is guaranteed to eventually be executed.

• Called:

- "HSA" Heterogeneous System Architecture, programming language proposed by AMD for new systems.
- The HSA language appears to be defunct now, but the scheduler is a good fit for mobile devices (esp. mobile GPUs).

```
Thread 0:
                                                                         Thread 1:
0.0: while (CAS(\&m, 0, 1) == false); //lock
                                                                         1.0: while (CAS(&m, 0, 1) == false); //lock
        // critical section
                                                                                 // critical section
0.1: m.store(0); //unlock
                                                                         1.1: m.store(0); //unlock
The thread with the
lowest ID that hasn't
                                                                                                    label:7
                                                                     label:6
                                      label:1
terminated is
                                                        T0
                                                                                      T1
                                  m:1
                                                                 m:0
                                                                                                m:1
guaranteed to
                                  0:next i:0.1
                                                                 0:next i:END
                                                                                                0:next i:END
eventually be
                                  1:next i:1.0
                                                                 1:next i:1.0
                                                                                                1:next i:1.1
executed.
                                                                                                                                label:5
                                                                                                                    T1
                                                                                                                           m:0
        label:0
                           Thread 0
                                                                                                                           0:next i:END
                                                                                                                           1:next i:END
    m:0
                                                                          Forever?
                                                T1
    0:next i:0.0
                                                                          0 \rightarrow 1 \dots
    1:next i:1.0
                                                                          0 \rightarrow 2 \dots
                                                                                                                      T0
                                      T0
               Thread 1
                                      label:2
                                                                     label:3
                                                                                                    label:4
                                                       T1
                                                                                      T0
                                                                                                m:1
                                  m:1
                                                                 m:0
                                  0:next i:0.0
                                                                 0:next i:0.0
                                                                                                0:next i:0.1
                                  1:next i:1.1
                                                                 1:next i:END
                                                                                                1:next i:END
```

```
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                                                                                 // critical section
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                                                                          1.1: m.store(0); //unlock
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lowest ID that hasn't
                                                                                                    label:7
                                                                     label:6
                                      label:1
terminated is
                                                        T0
                                                                                      T1
                                  m:1
                                                                 m:0
                                                                                                m:1
guaranteed to
                                  0:next i:0.1
                                                                 0:next i:END
                                                                                                0:next i:END
eventually be
                                  1:next i:1.0
                                                                 1:next i:1.0
                                                                                                1:next i:1.1
executed.
                                                                                                                                label:5
                                                                                                                     T1
                                                                                                                            m:0
        label:0
                           Thread 0
                                                                                                                            0:next i:END
                                                                                                                            1:next i:END
    m:0
                                                                          Forever?
                                                T1
    0:next i:0.0
                                                                          0 \rightarrow 1 \dots
    1:next i:1.0
                                                                          0 \rightarrow 2 \dots
                                                                                                                      T0
                                      T0
               Thread 1
                                      label:2
                                                                     label:3
                                                                                                    label:4
                                                       T1
                                                                                      T0
                                                                                                m:1
                                  m:1
                                                                 m:0
                                  0:next i:0.0
                                                                 0:next i:0.0
                                                                                                0:next i:0.1
                                  1:next i:1.1
                                                                 1:next i:END
                                                                                                1:next i:END
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```
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lowest ID that hasn't
                                                                                                    label:7
                                                                     label:6
                                      label:1
terminated is
                                                       T0
                                                                                      T1
                                 m:1
                                                                m:0
                                                                                               m:1
guaranteed to
                                  0:next i:0.1
                                                                0:next i:END
                                                                                               0:next i:END
eventually be
                                  1:next i:1.0
                                                                1:next i:1.0
                                                                                               1:next i:1.1
executed.
                                                                                                                                label:5
                                                                                                                    T1
                                                                                                                           m:0
        label:0
                           Thread 0
                                                                                                                           0:next i:END
                                                                                                                           1:next i:END
    m:0
                                                                         Forever?
                                                T1
    0:next i:0.0
                                                            disallowed
                                                                         0 \rightarrow 1 \dots
    1:next i:1.0
                                                                         0 \rightarrow 2 \dots
                                                                                                                     T0
                                      T0
               Thread 1
                                      label:2
                                                                     label:3
                                                                                                   label:4
                                                       T1
                                                                                     T0
                                                                                               m:1
                                 m:1
                                                                m:0
                                  0:next i:0.0
                                                                0:next i:0.0
                                                                                               0:next i:0.1
                                  1:next i:1.1
                                                                1:next i:END
                                                                                               1:next i:END
```

```
Thread 0:
                                                                         Thread 1:
0.0: while (CAS(\&m, 0, 1) == false); //lock
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                                                                         1.1: m.store(0); //unlock
The thread with the
lowest ID that hasn't
                                                                                                    label:7
                                                                     label:6
                                      label:1
terminated is
                                                       T0
                                                                                      T1
                                 m:1
                                                                m:0
                                                                                               m:1
guaranteed to
                                  0:next i:0.1
                                                                0:next i:END
                                                                                               0:next i:END
eventually be
                                  1:next i:1.0
                                                                1:next i:1.0
                                                                                               1:next i:1.1
executed.
                                                                                                                                label:5
                                                                                                                    T1
                                                                                                                           m:0
        label:0
                           Thread 0
                                                                                                                           0:next i:END
                                                                                                                           1:next i:END
    m:0
                                                                         Forever?
                                                T1
    0:next i:0.0
                                                            disallowed
                                                                         0 \rightarrow 1 \dots
    1:next i:1.0
                                                                         0 \rightarrow 2 \dots
                                                                                                                     T0
                                      T0
               Thread 1
                                      label:2
                                                                     label:3
                                                                                                   label:4
                                                       T1
                                                                                      T0
                                                                                               m:1
                                 m:1
                                                                m:0
                                  0:next i:0.0
                                                                0:next i:0.0
                                                                                               0:next i:0.1
                                  1:next i:1.1
                                                                1:next i:END
                                                                                               1:next i:END
```

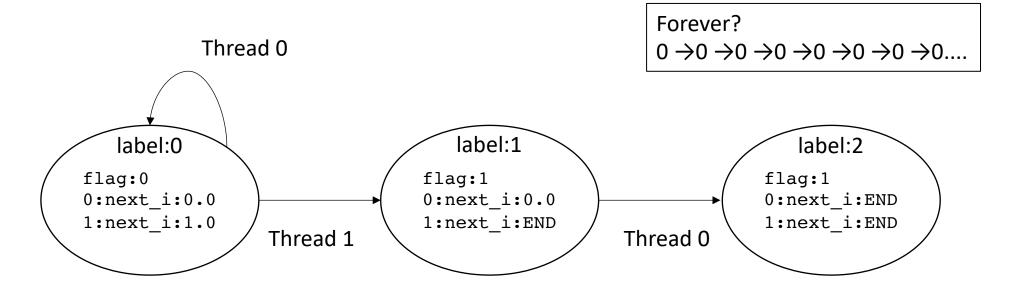
```
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                                                                        Thread 1:
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        // critical section
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The thread with the
lowest ID that hasn't
                                                                                                  label:7
                                                                    label:6
                                     label:1
terminated is
                                                       T0
                                                                                     T1
                                 m:1
                                                                m:0
                                                                                              m:1
guaranteed to
                                 0:next i:0.1
                                                                0:next i:END
                                                                                              0:next i:END
eventually be
                                 1:next i:1.0
                                                                1:next i:1.0
                                                                                              1:next i:1.1
executed.
                                                                                                                              label:5
                                                                                                                   T1
                                                                                                                         m:0
        label:0
                          Thread 0
                                                                                                                         0:next i:END
                                                                                                                         1:next i:END
    m:0
                                                                         Forever?
                                               T1
    0:next i:0.0
                                                           disallowed
                                                                        0 \rightarrow 1 \dots
    1:next i:1.0
                                                                        0 \rightarrow 2 \dots
                                                             allowed
                                                                                                                   T0
                                                                        Mutexes might not terminate under
                                      T0
                                                                        HSA scheduler!
               Thread 1
                                     label:2
                                                                    label:3
                                                                                                  label:4
                                                      T1
                                                                                     T0
                                                                                              m:1
                                 m:1
                                                                m:0
                                 0:next i:0.0
                                                                0:next i:0.0
                                                                                              0:next i:0.1
                                 1:next i:1.1
                                                                1:next i:END
                                                                                              1:next i:END
```

Thread 0: 0.0: while(flag.load() == 0);

```
Thread 1:
1.0: flag.store(1);
```

Is this program guaranteed to terminate under the HSA scheduler

The thread with the lowest ID that hasn't terminated is guaranteed to eventually be executed.

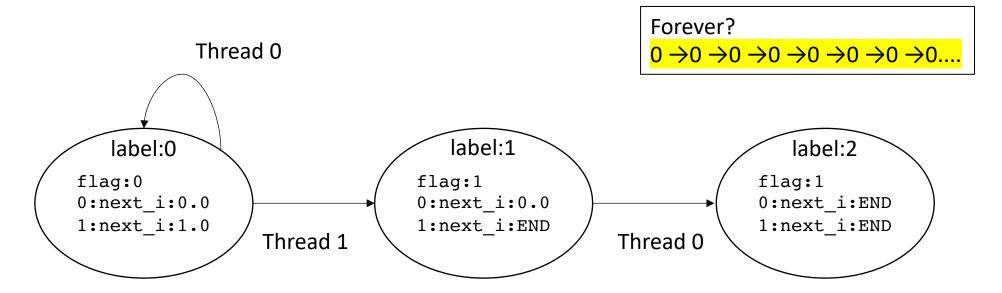


Thread 0: 0.0: while(flag.load() == 0);

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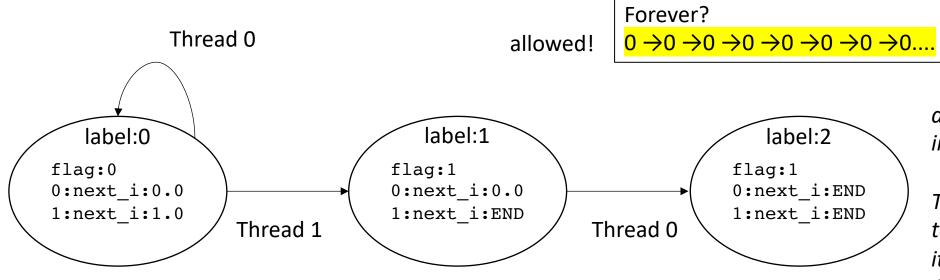


Thread 0: 0.0: while(flag.load() == 0);

```
Thread 1:
1.0: flag.store(1);
```

Is this program guaranteed to terminate under the HSA scheduler

The thread with the lowest ID that hasn't terminated is guaranteed to eventually be executed.



allowed to spin forever in the HSA scheduler!

Thread 0 is guaranteed to be executed because it has the lowest id. Thread 1 is not!

```
Thread 0:
0.0: while(flag.load() == 0);
```

What if we switch the threads? Thread 1 waits for Thread 0?

```
Thread 1:
1.0: flag.store(1);
```

```
Thread 0:
```

```
0.0: flag.store(1);
```

What if we switch the threads? Thread 1 waits for Thread 0?

Thread 1:

```
1.0: while(flag.load() == 0);
```

Thread 0:

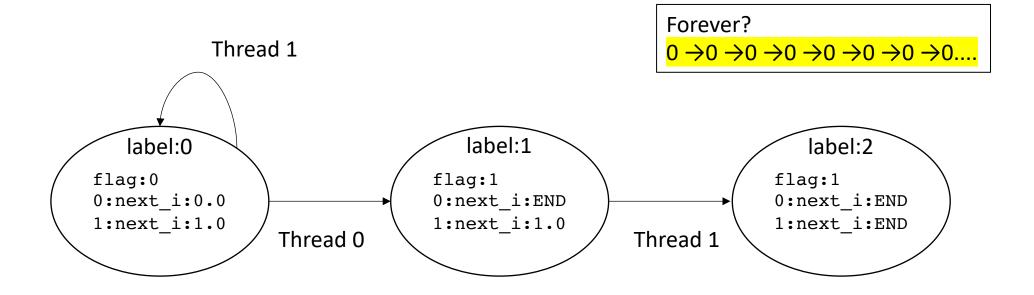
0.0: flag.store(1);

Thread 1:

1.0: while(flag.load() == 0);

What if we switch the threads? Thread 1 waits for Thread 0?

The thread with the lowest ID that hasn't terminated is guaranteed to eventually be executed.



thread 0
has the lowest
id so it is guaranteed
to eventually be
executed

Thread 0:

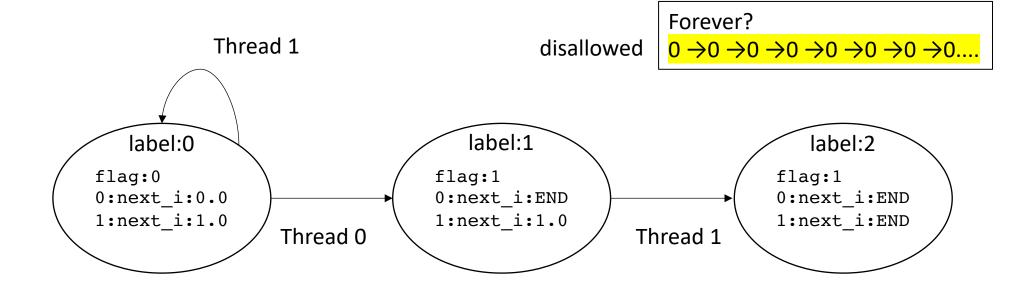
0.0: flag.store(1);

Thread 1:

1.0: while(flag.load() == 0);

What if we switch the threads? Thread 1 waits for Thread 0?

The thread with the lowest ID that hasn't terminated is guaranteed to eventually be executed.



thread 0
has the lowest
id so it is guaranteed
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executed

Liveness

Combining HSA and Parallel Execution?

 Threads are scheduled in the order of their thread IDs and are guaranteed fair execution once they start executing.

- Most modern GPUs seem to support this:
 - With the exception of ARM and Apple GPUs

Liveness

So where are we now?

- C++ gives 3 degrees of progress guarantees:
 - Concurrent scheduler
 - what you will likely see on your machine; fair scheduler!
 - Parallel scheduler
 - Threads that start executing will continue to be fairly executed. Allows mutexes!
 - Weakly parallel scheduler
 - No guarantees. Any cycle in the LTS can potentially execute forever!

Liveness

So where are we now?

- GPU schedulers:
 - Nvidia provides Parallel Forward Progress
 - Allows mutexes, concurrent data structures, etc.
 - OpenCL, Vulkan, and Metal provide no documentation on scheduler behaviors.
 - In practice, many assume parallel forward progress
 - This is not portable (esp. to ARM and Apple)
 - Working with specification groups to try and provide these

Conclusion

- Schedulers are becoming more aggressive
 - Preemption is expensive
 - Power saving shut downs are possible

- Concurrent objects require different amounts of fairness
 - Mutexes require parallel forward progress
 - Producer Consumer requires HSA forward progress
- Be careful that the programs you are writing make the correct assumptions about the underlying scheduler!

Conclusion

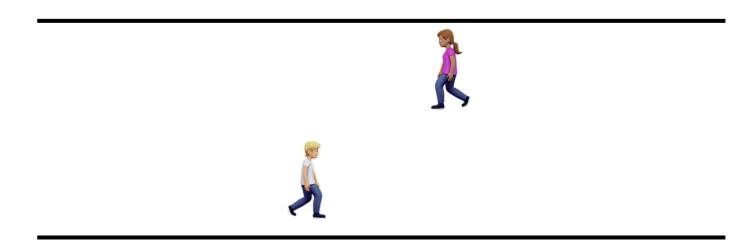
• Demo about how things can go wrong on Ipad.



















Hallway problem





Can they dance around each other forever?

```
Thread 0:
... do {
0.0    x.store(0);
0.1 } while (x.load() != 0)
```

```
Thread 1:
... do {
1.0    x.store(1);
1.1 } while (x.load() != 1)
```

Each thread stores their thread id, and then loads the thread id. It loops while it doesn't see its id

Each thread gets a chance to execute, but they get in each others way.

This is called a livelock

We don't have time to get into it deeply here, but there are lots of interesting research challenges around these types of behaviors!

Thanks!

See you on Thursday!

• We will start a 2 part lecture on GPUs