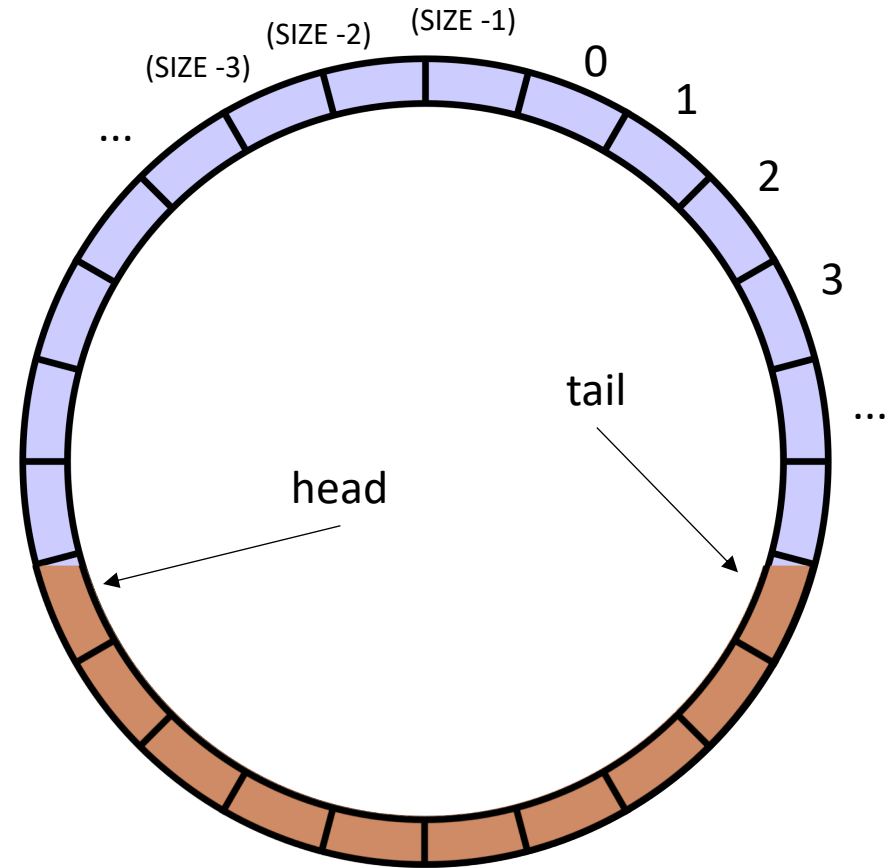


# CSE113: Parallel Programming

May 6, 2021

- **Topic:** Concurrent Objects 4
  - Finishing up linked list
  - Reading/Writing Queues
  - Synchronous Producer Consumer
  - Async Producer Consumer



# Announcements

- Busy Day (at least at midnight)!
  - HW2 due today!
  - Midterm due today!
  - HW3 released today!
  - HW1 Grades released today!
- Gan had office hours this morning
- Reese will have them after class

# Announcements

- Erica is running a study on parallel programming:
  - Sign up if you are interested!
- We won't finish module 3 today:
  - Next week we'll discuss work stealing
  - I will still plan to release the HW today
- May 20 will be guest lecture:
  - Hugues Evrard will discuss message-passing concurrency
  - Alistair Donaldson will discuss testing GPU compilers

# Quiz

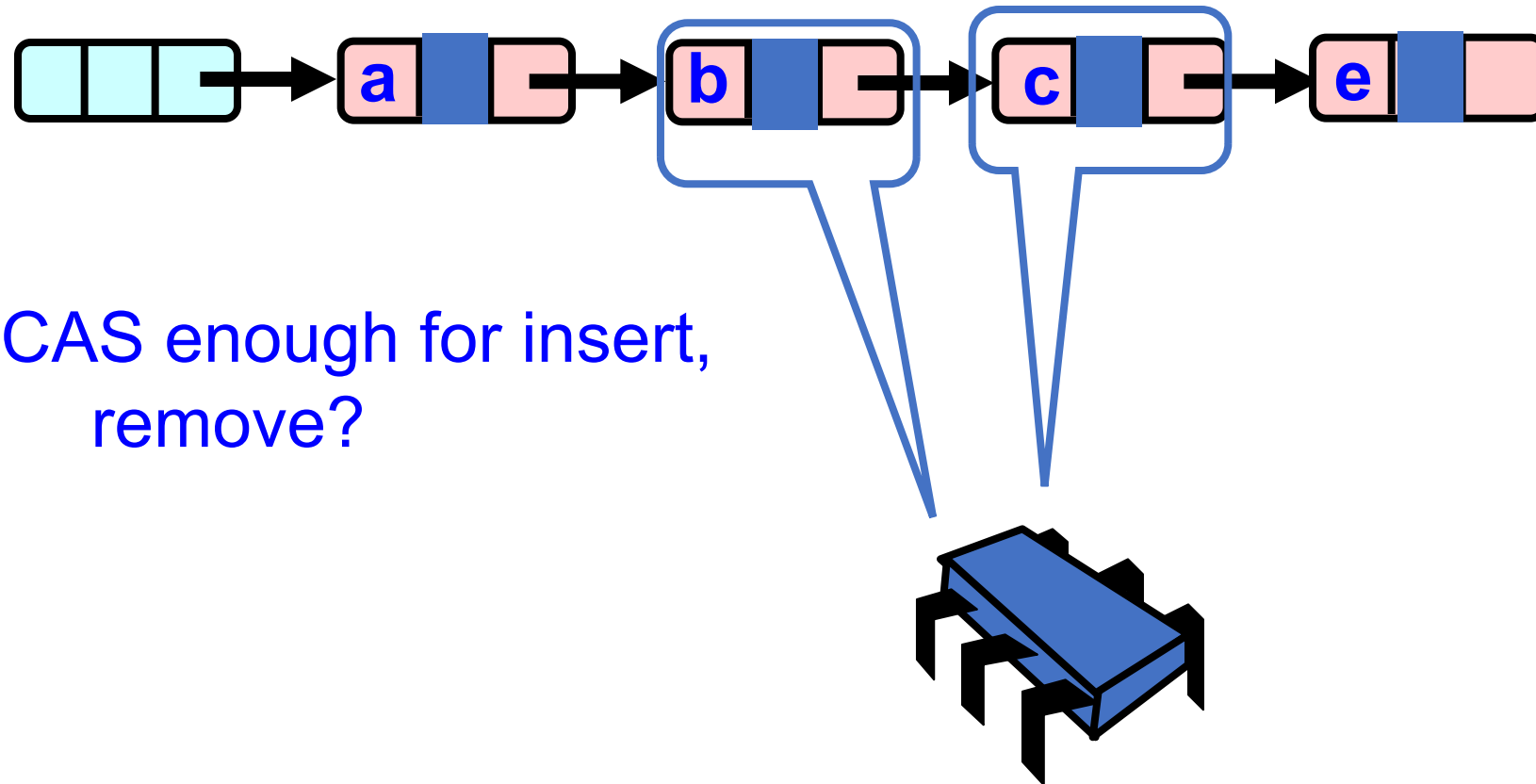
# Quiz

- Discuss Answers

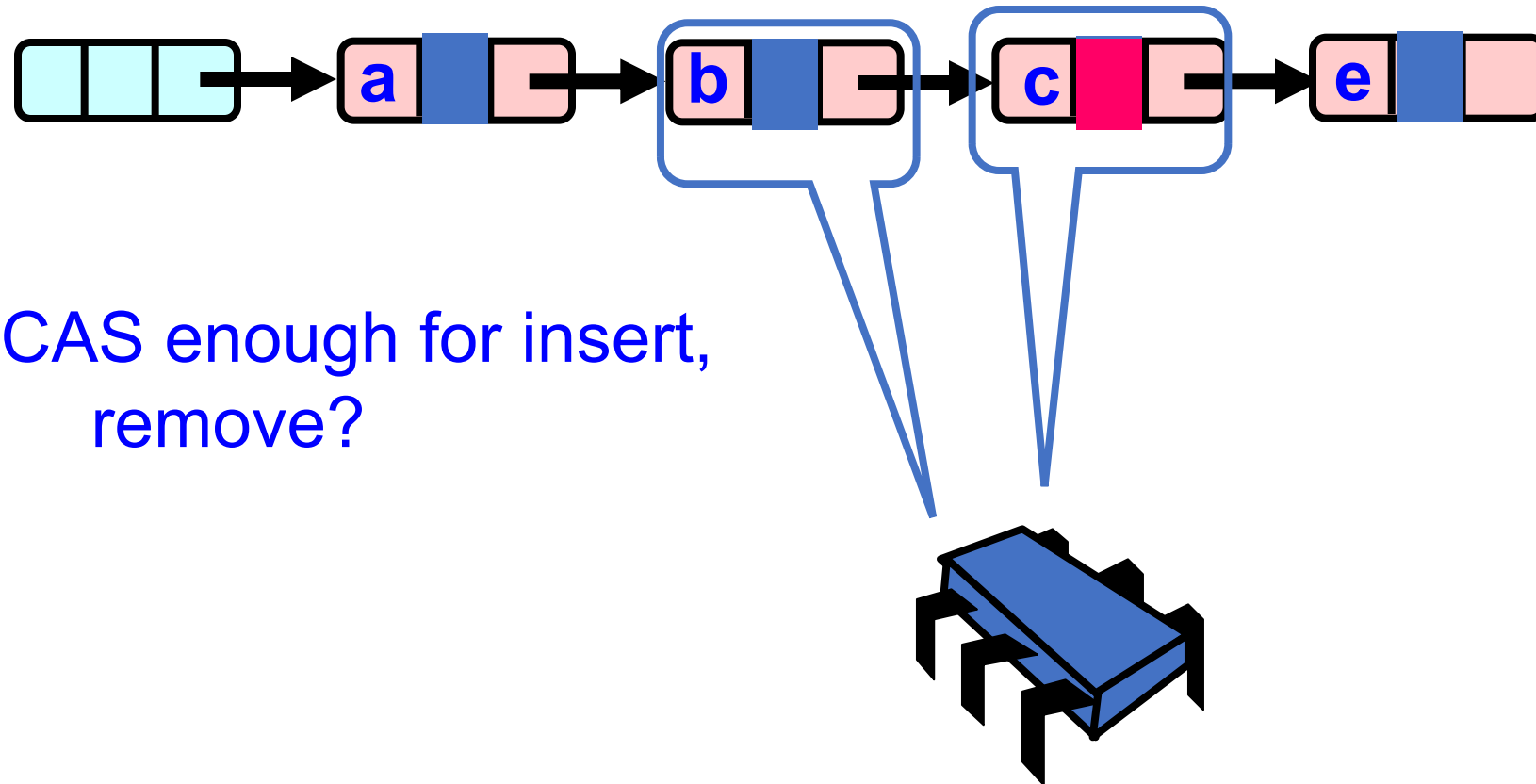
# Schedule

- **Finish up linked-list**
- Concurrent Queues
  - Input/Output Queues
  - Synchronous Producer/Consumer Queue
  - Async Producer/Consumer Queue

# Lock-free Lists

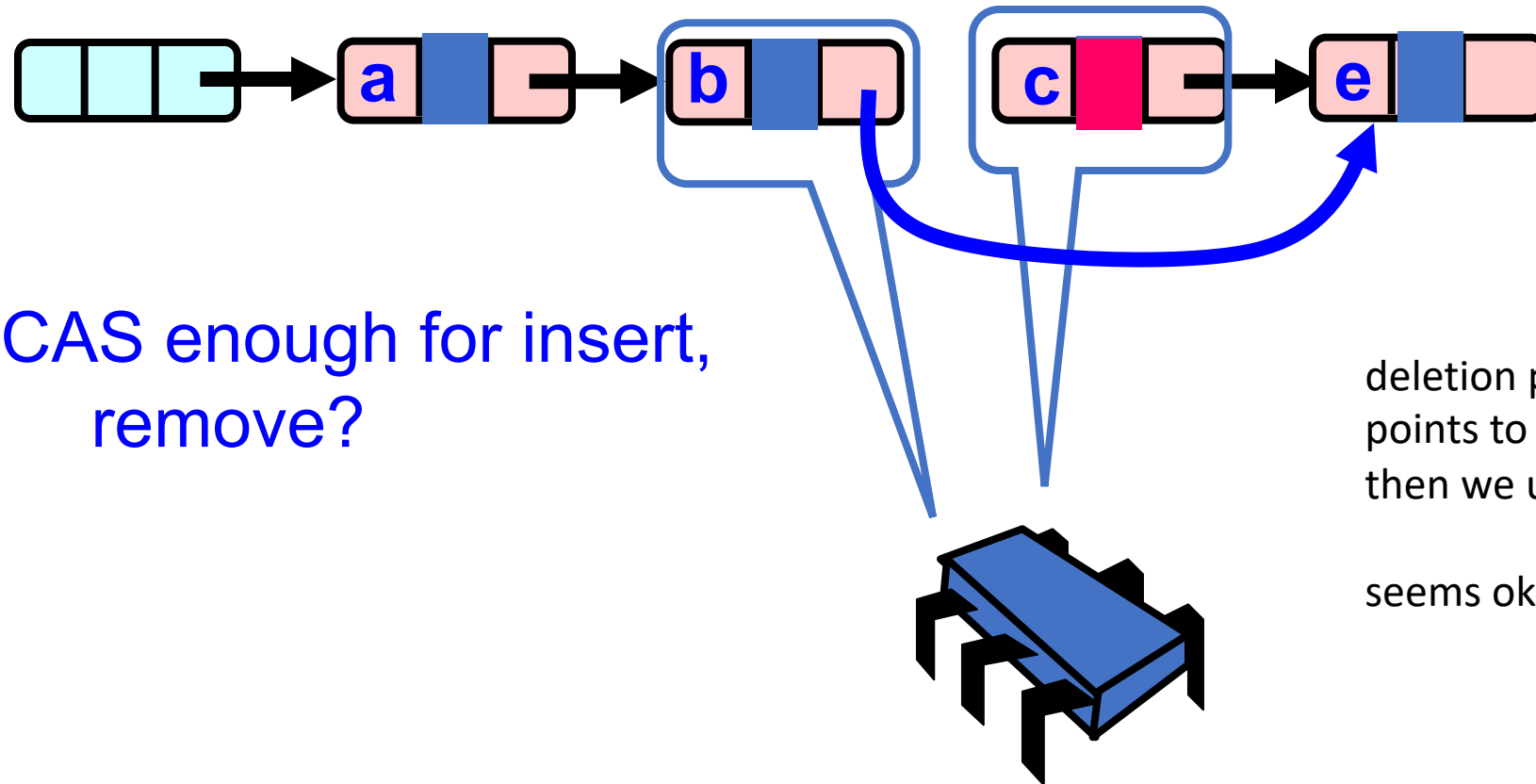


# Lock-free Lists



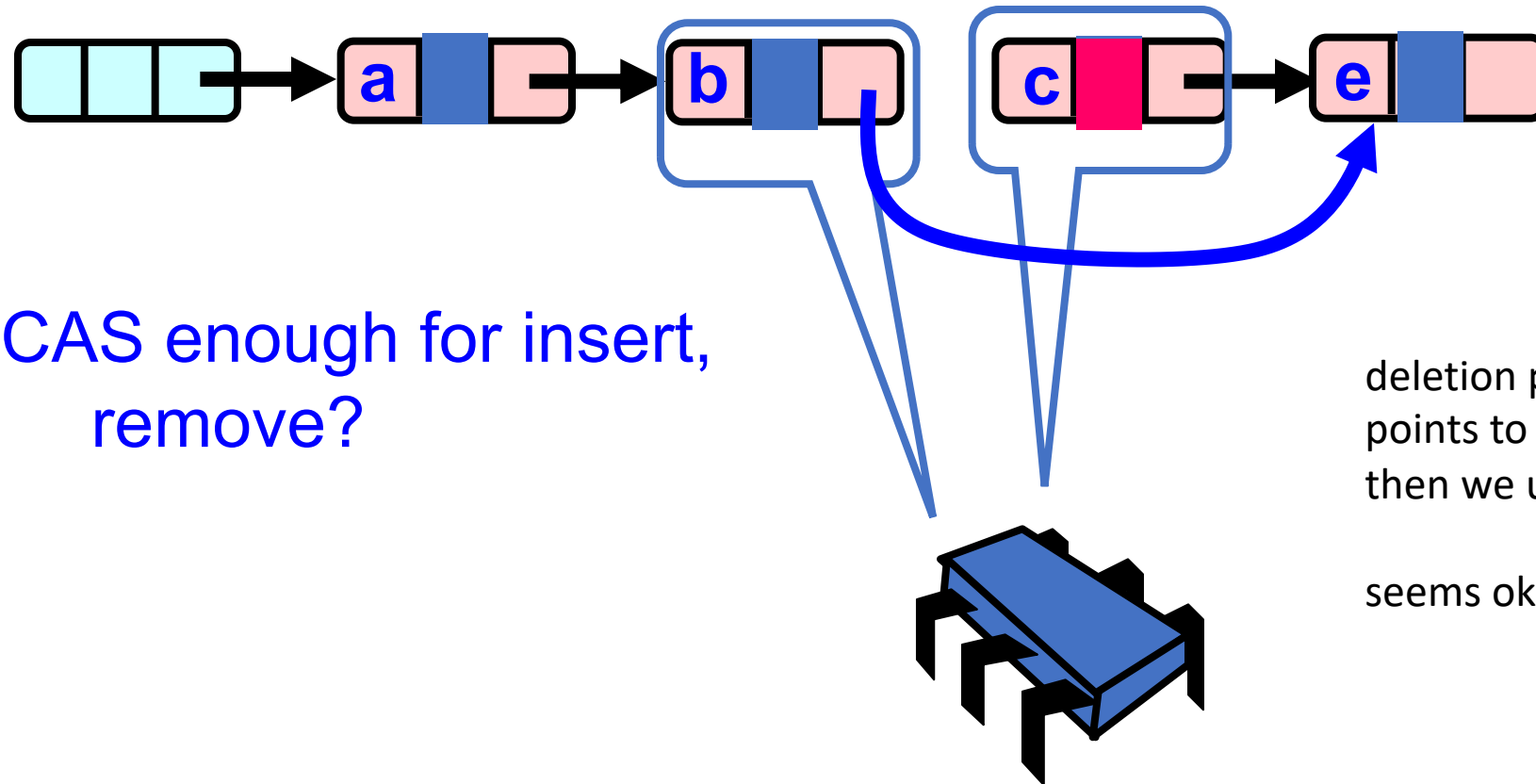


# Lock-free Lists



# Lock-free Lists

*ensures that nobody has inserted a node between b and c*

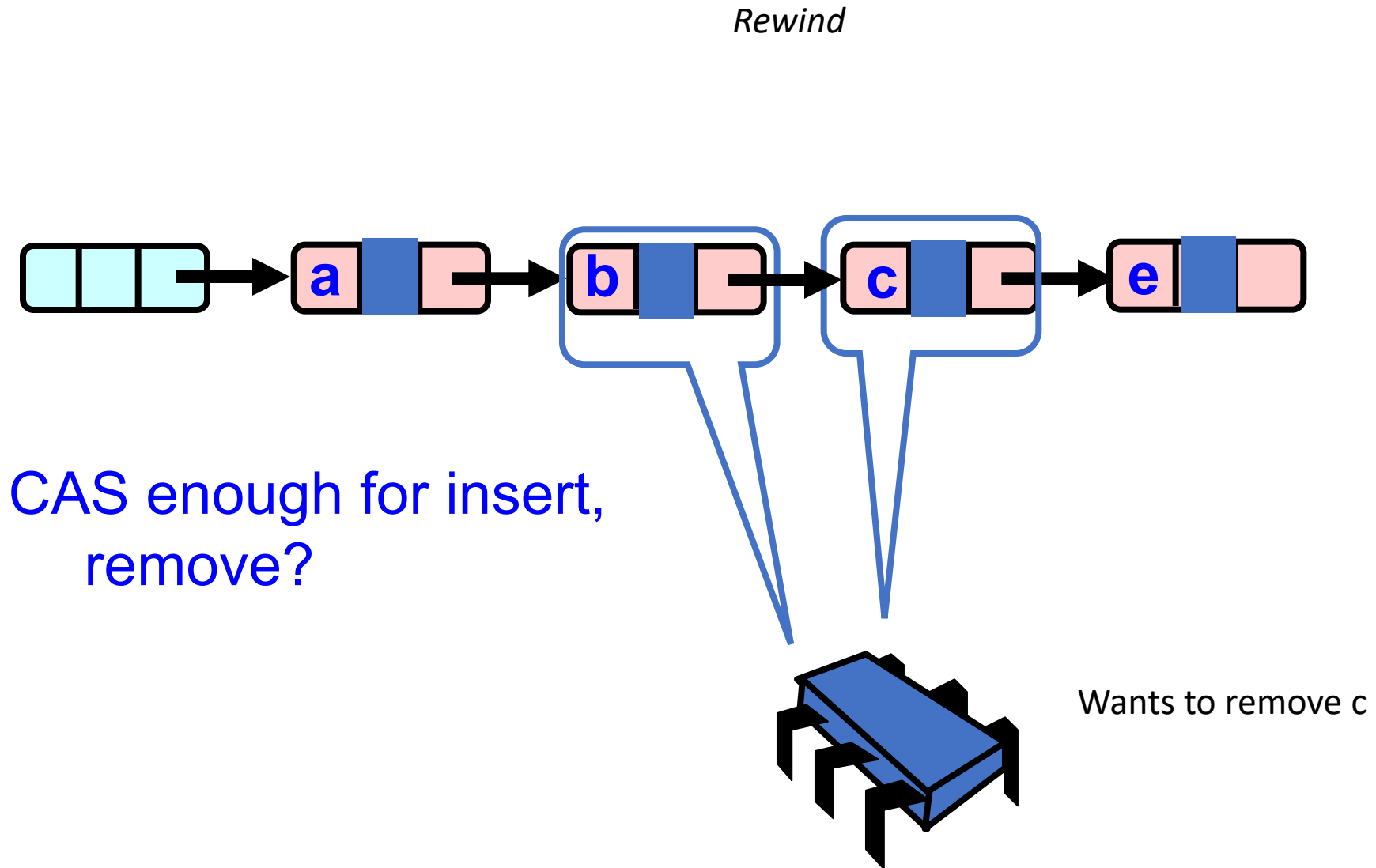


CAS enough for insert,  
remove?

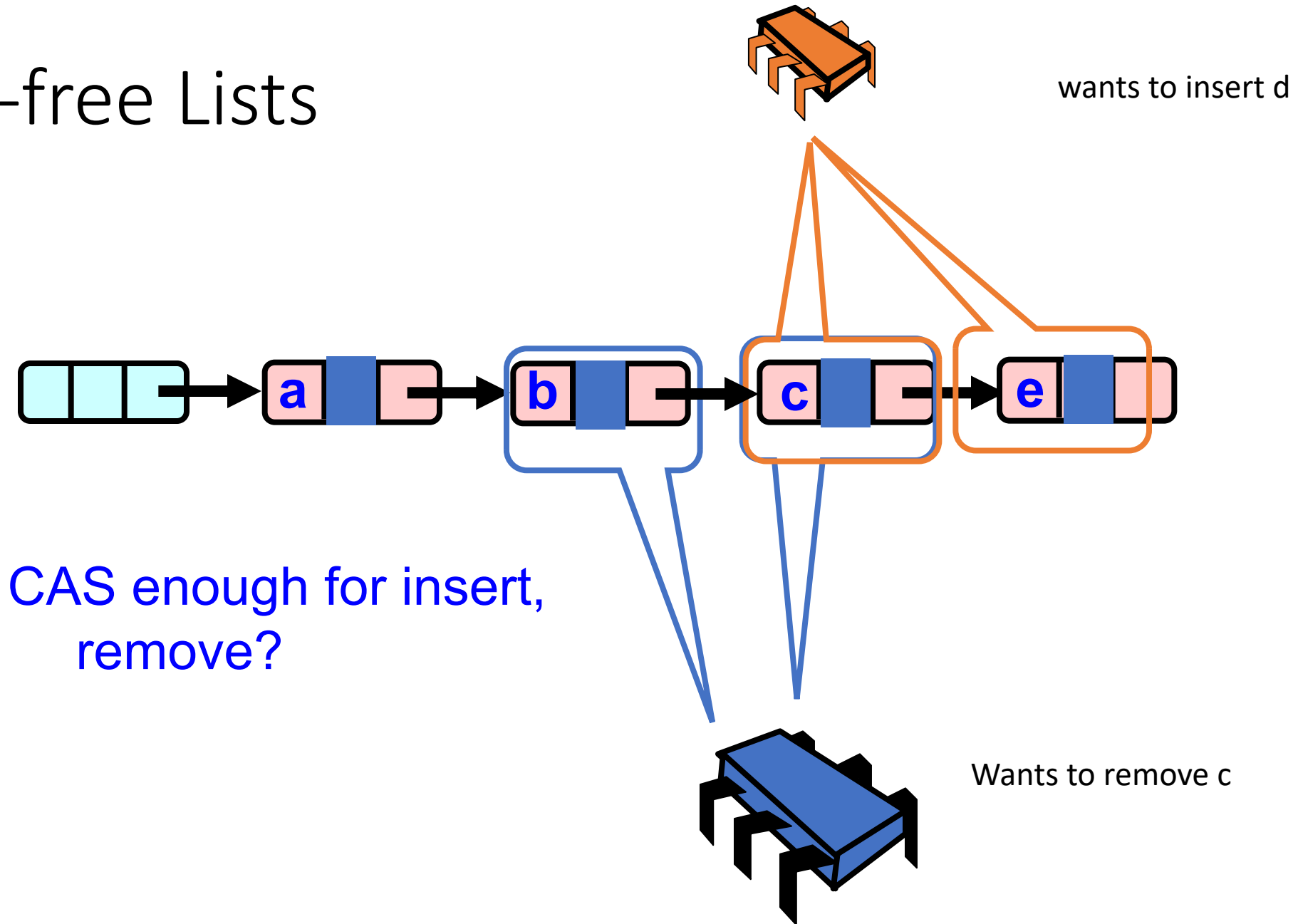
deletion point requires b  
points to c. If that is valid  
then we update to e.

seems okay...

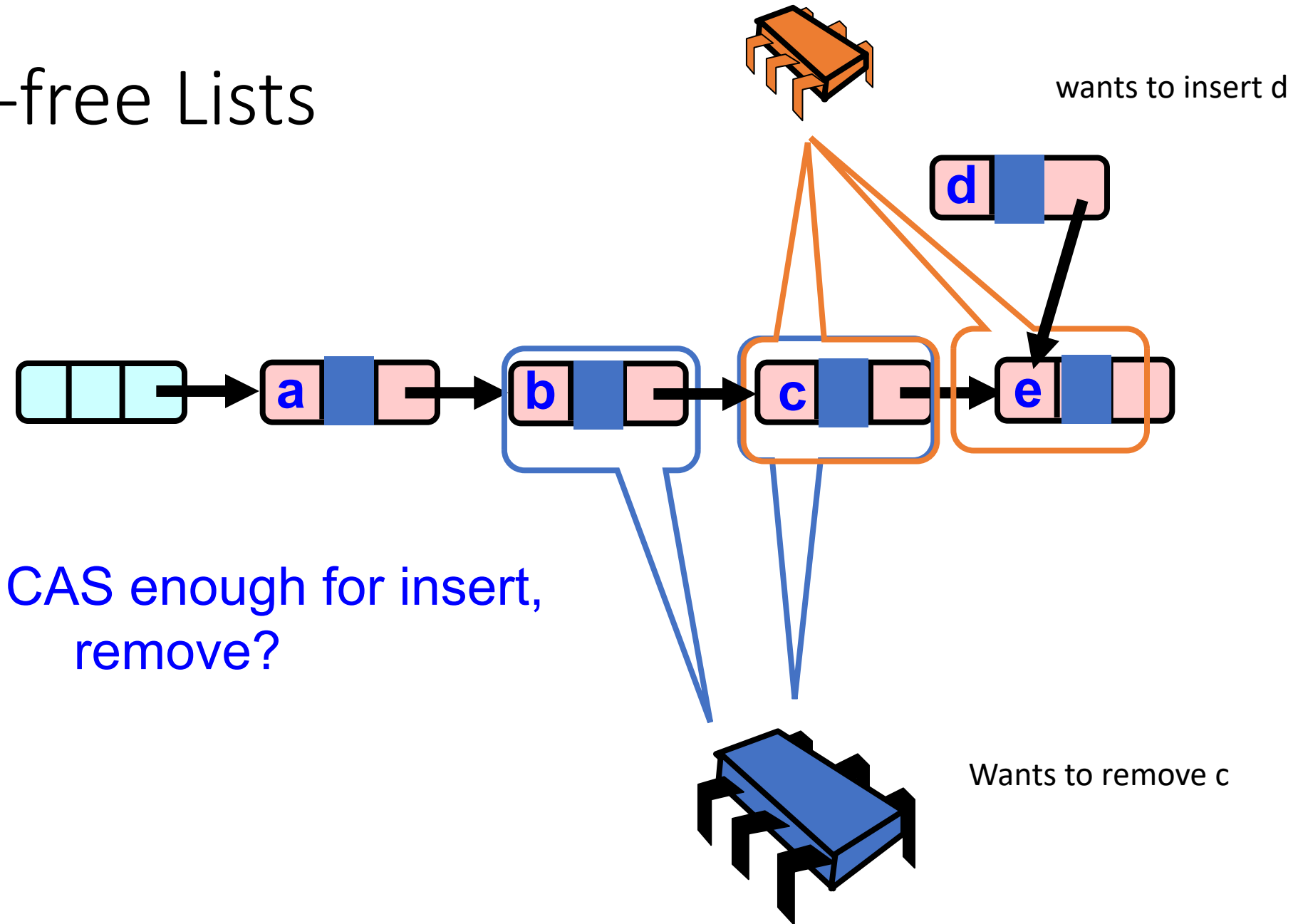
# Lock-free Lists



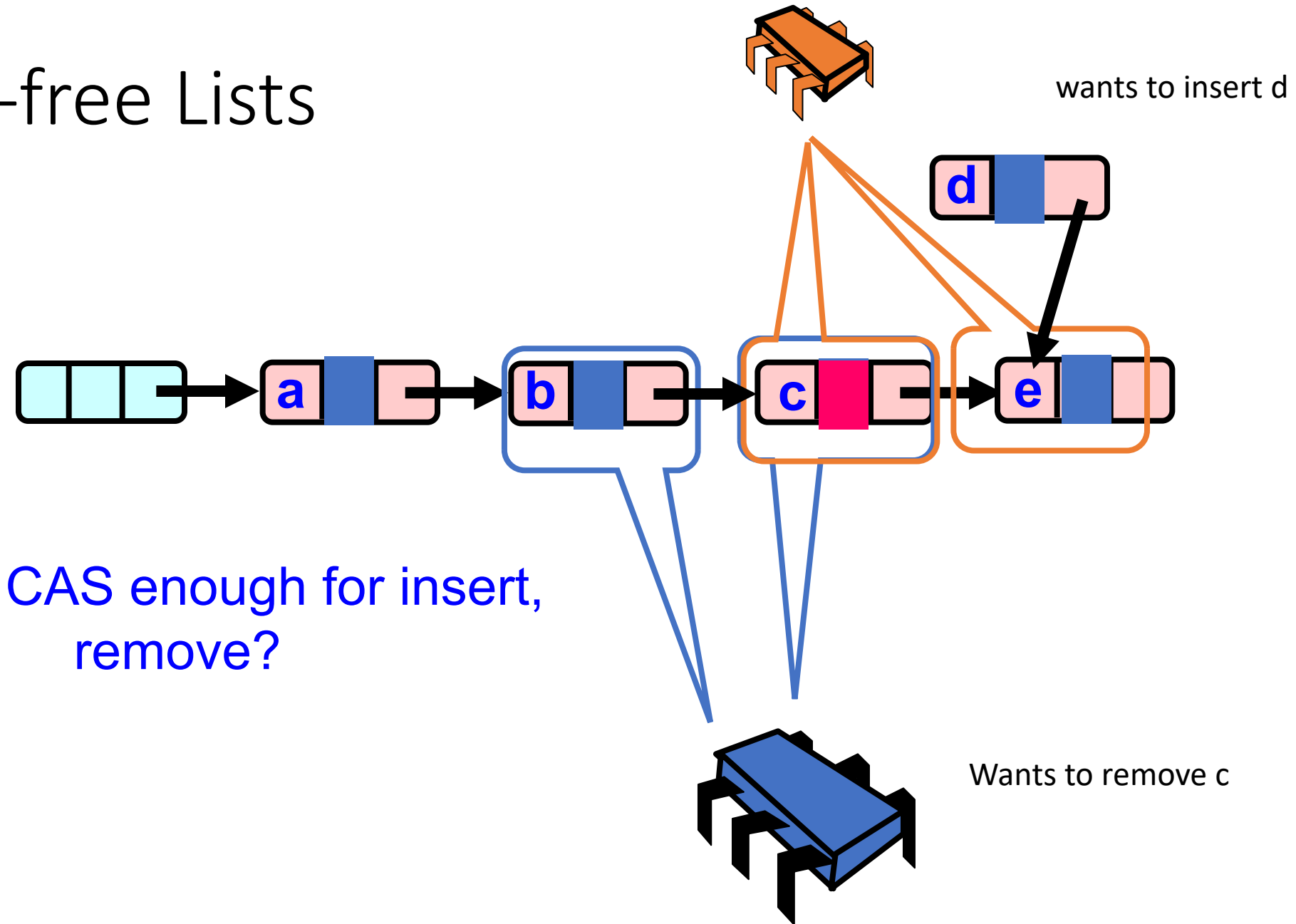
# Lock-free Lists



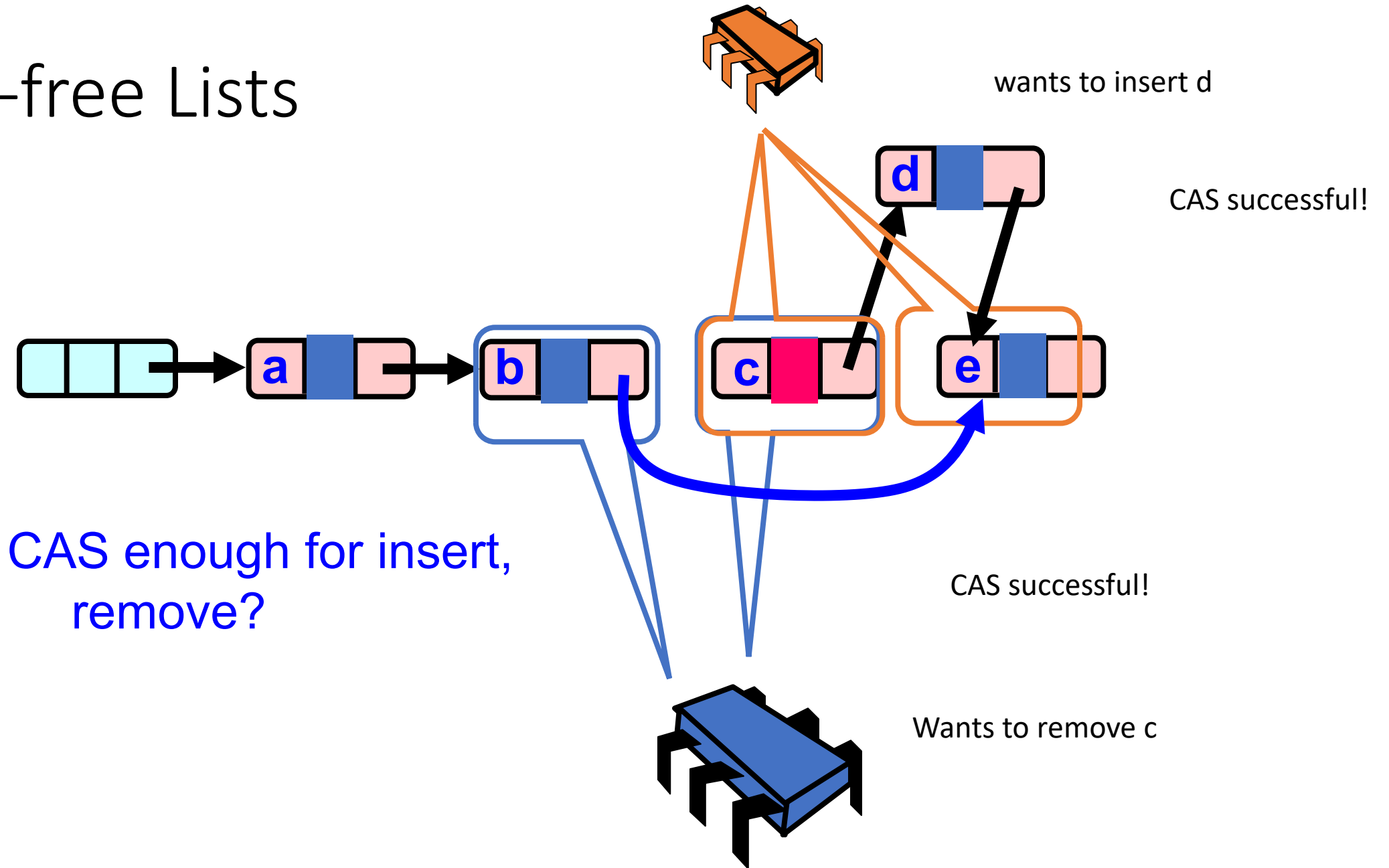
# Lock-free Lists



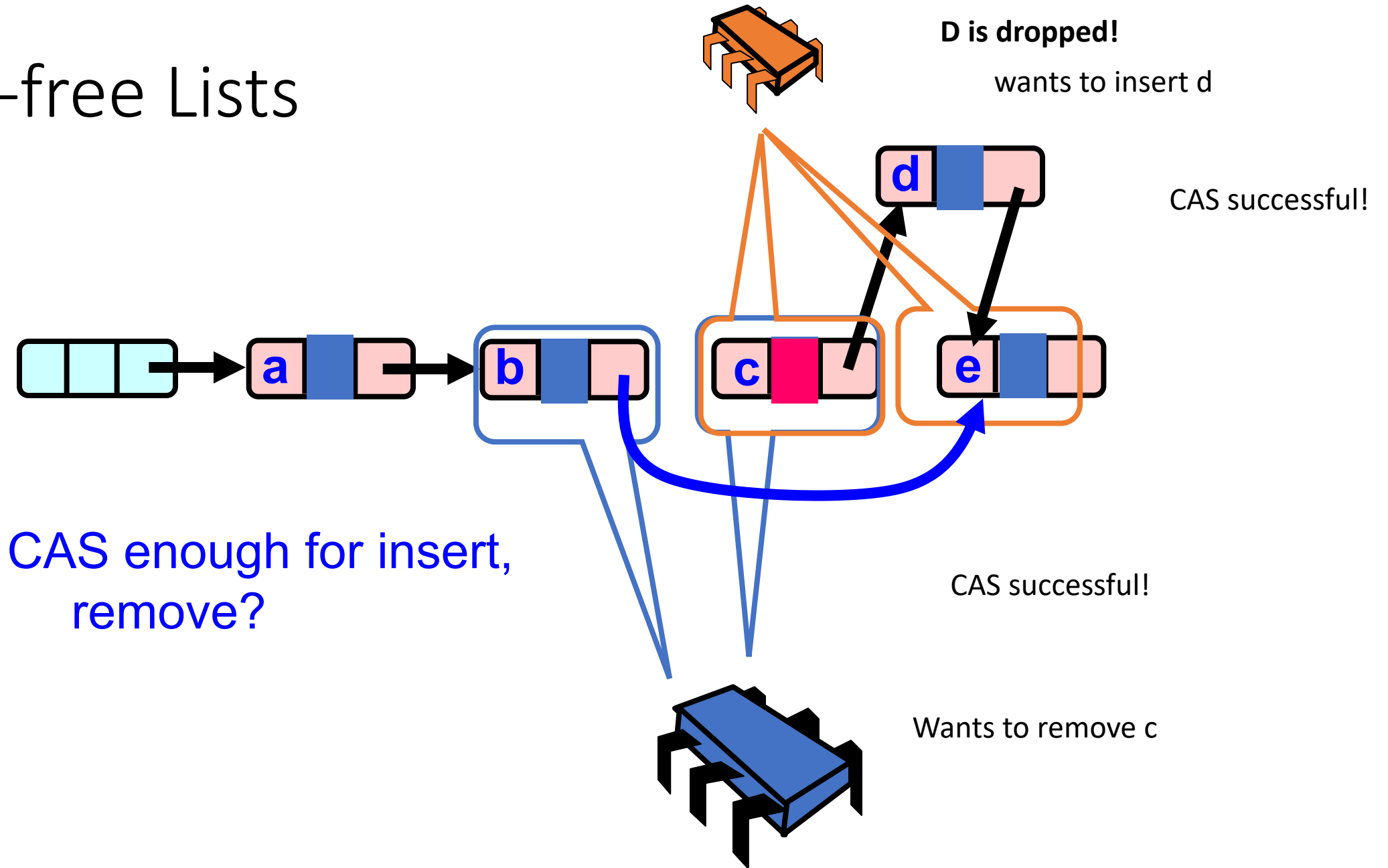
# Lock-free Lists



# Lock-free Lists



# Lock-free Lists

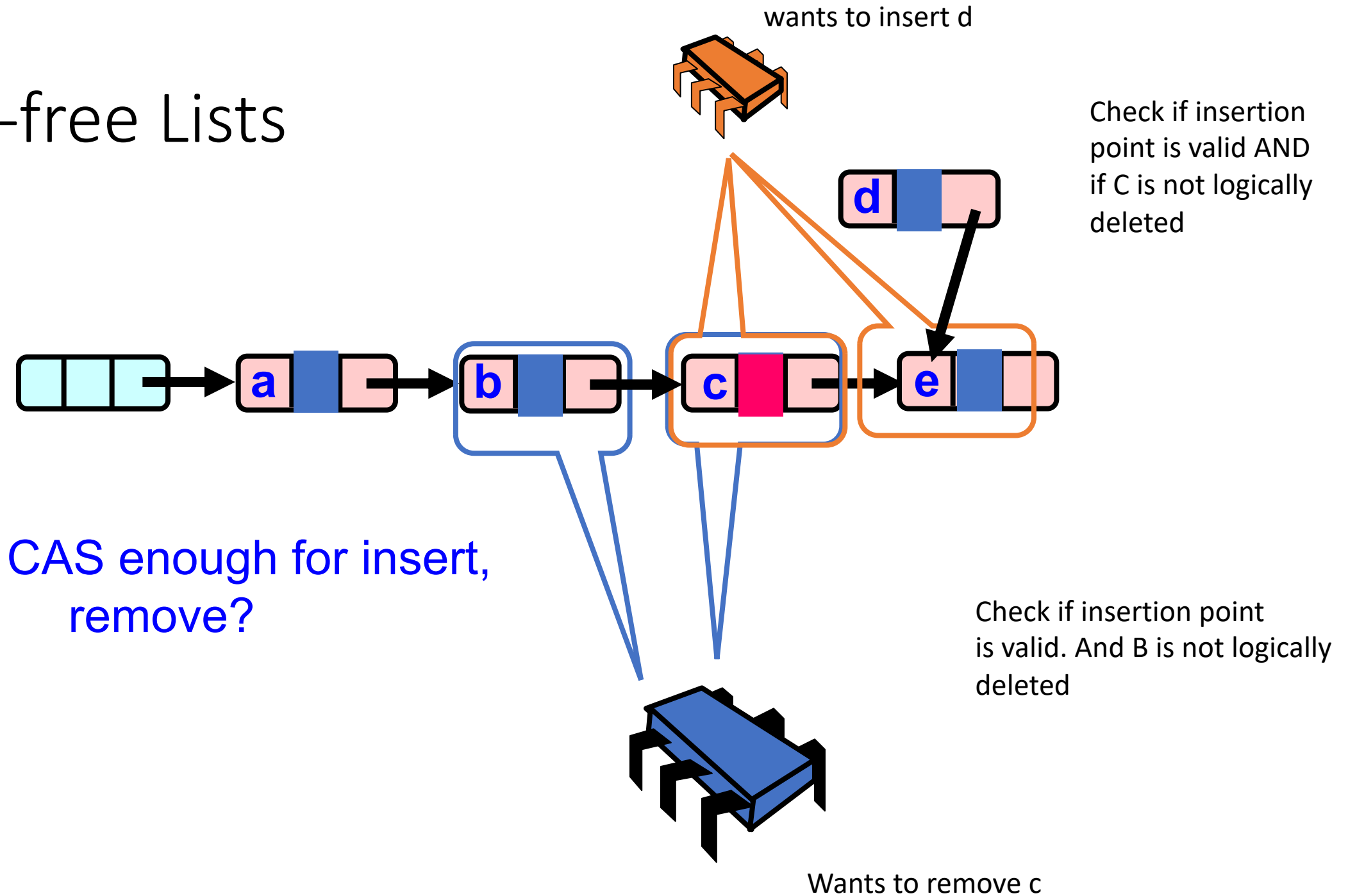




# Solution

- Use AtomicMarkableReference
- Atomic CAS that checks not only the address, but also a bit
- We can say: update pointer if the insertion point is valid AND if the node has not been logically removed.

# Lock-free Lists



# Marking a Node

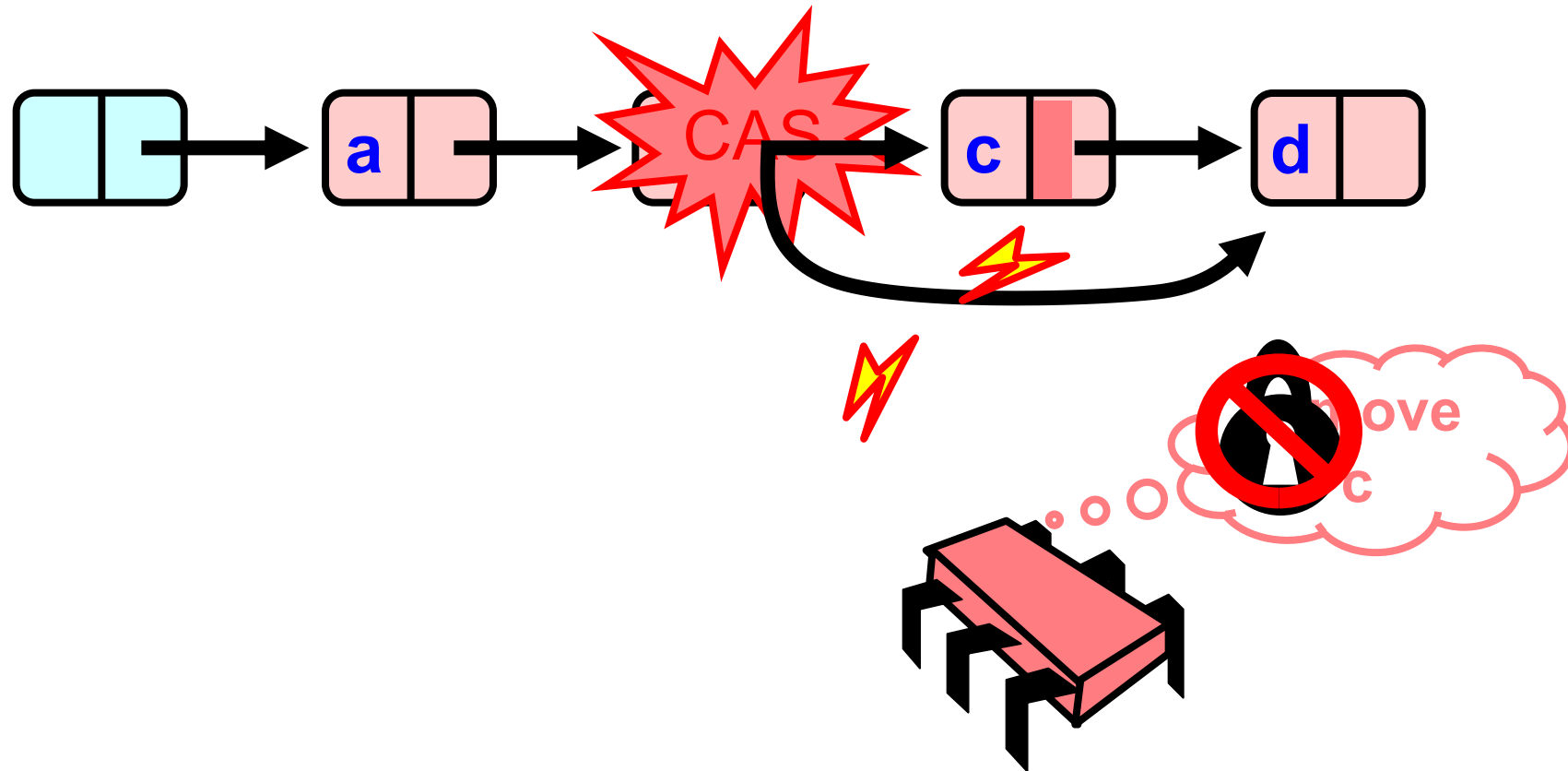
- **AtomicMarkableReference** class
  - Java.util.concurrent.atomic package
  - But we're using a better™ language (C++)



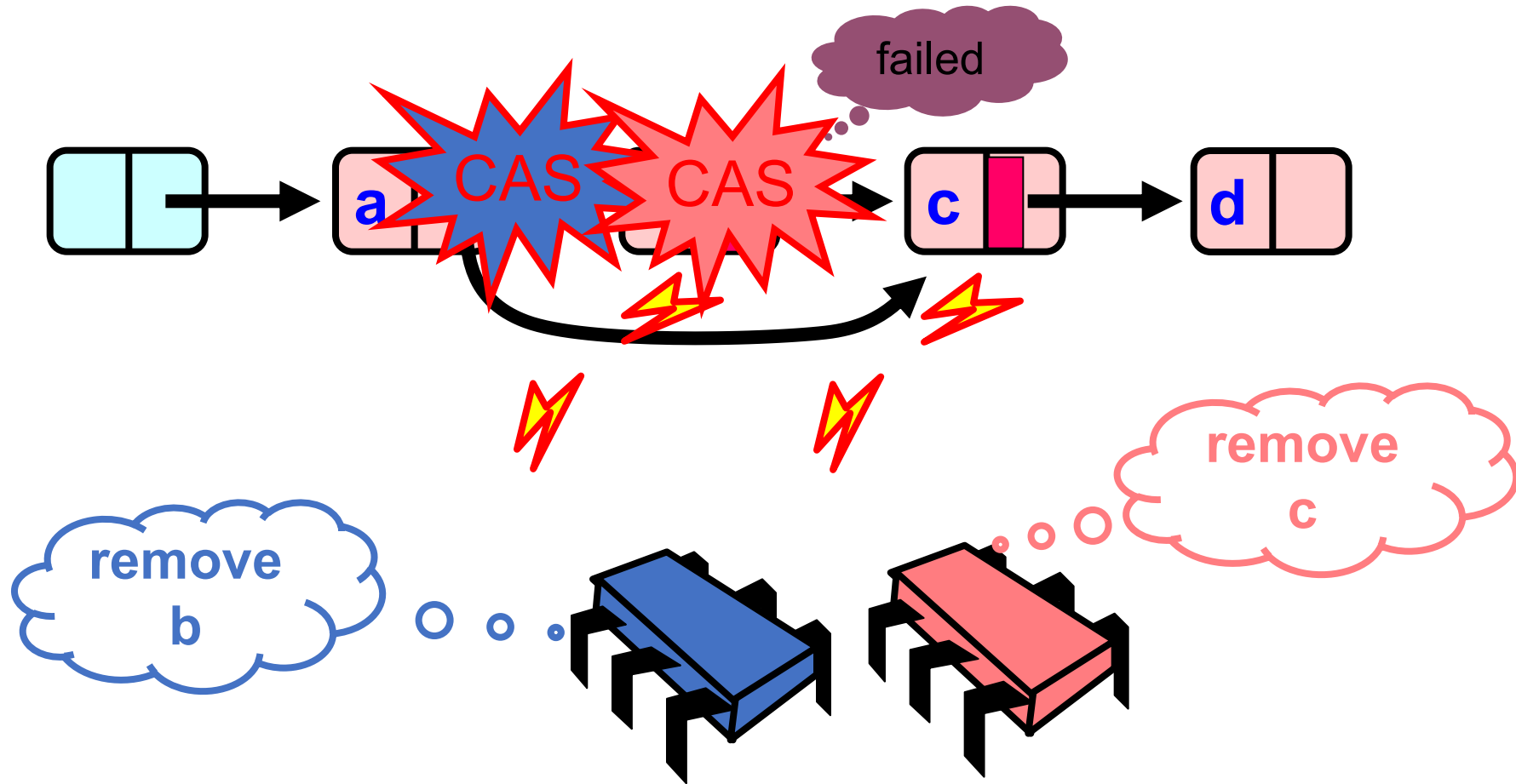
```
class AtomicMarkedNodePtr {  
    private:  
        atomic<node *> ptr;  
    public:  
        AtomicMarkedNodePtr(node *p) {  
            node * marked = p | 1;  
            ptr.store(marked);  
        }  
  
        void logically_delete() {  
            // how to store the marked bit atomically?  
        }  
  
        node * get_ptr() {  
            return ptr.load() & (~1);  
        }  
  
        bool CAS (node *e, node *n) {  
            node * expected = e | 1;  
            node * new_node = n | 1;  
            return atomic_compare_exchange(&ptr, &expected, new_node);  
        }  
}
```

# Lazy node removal

# Removing a Node

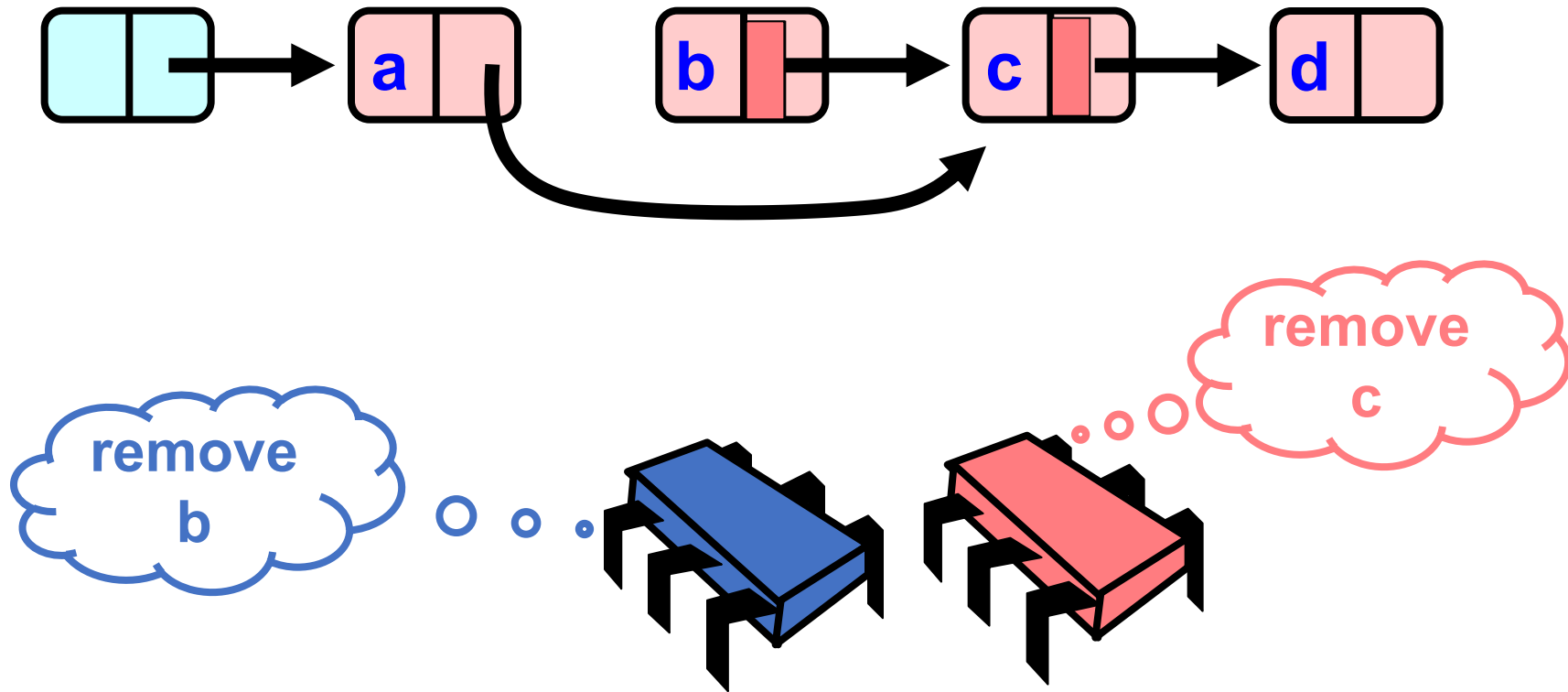


# Removing a Node



# Removing a Node

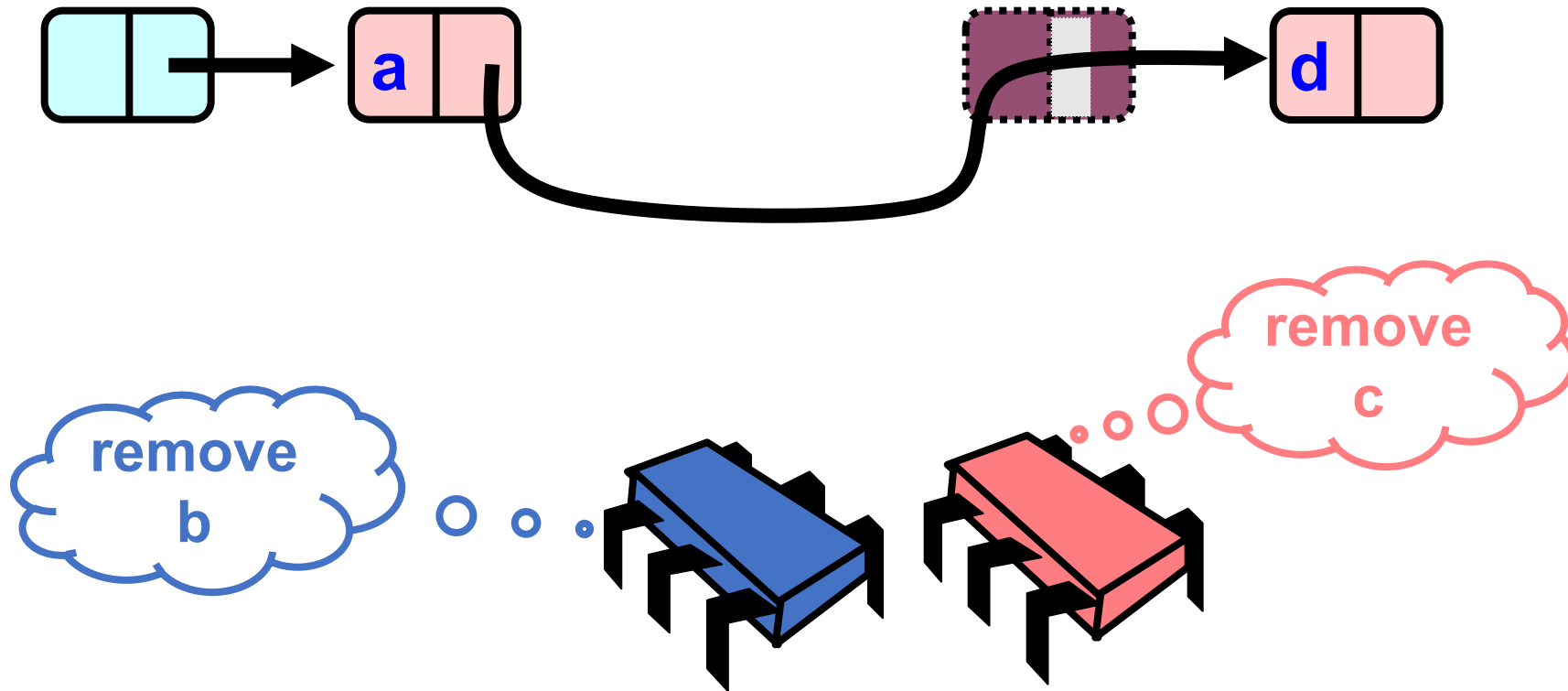
Two options:  
Try removing C again  
or...





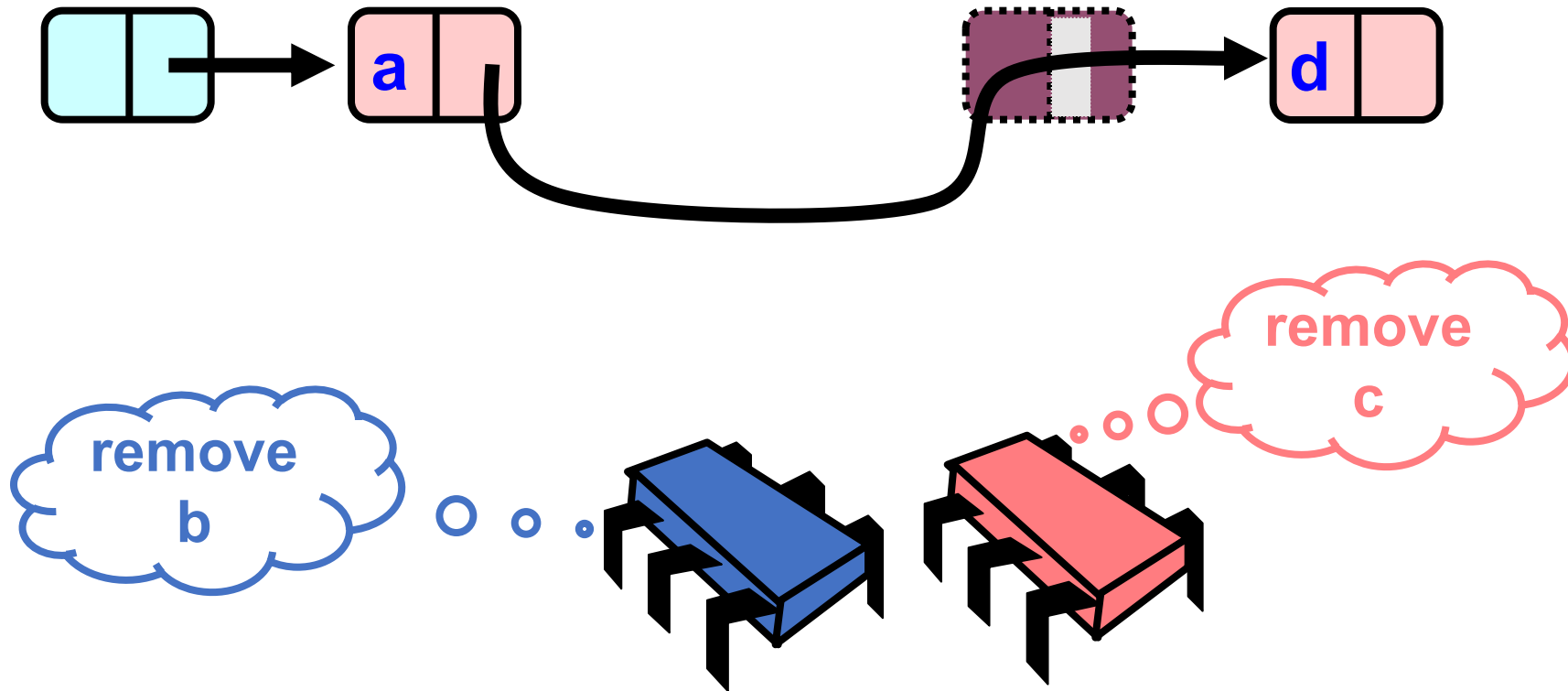
# Removing a Node

c stays in the list as logically deleted



# Removing a Node

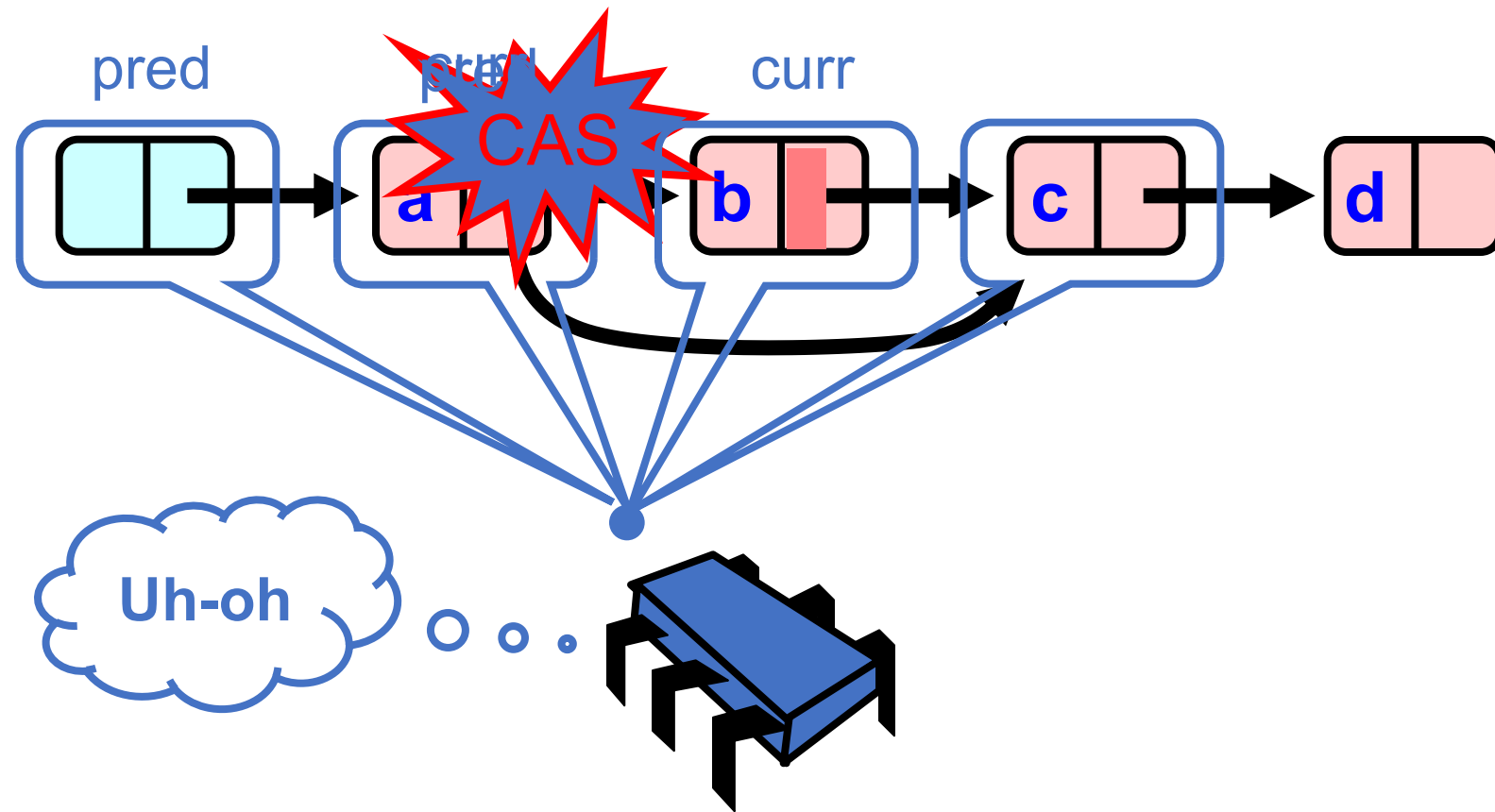
c stays in the list as logically deleted



# Traversing the List

- Q: what do you do when you find a “logically” deleted node in your path?
- A: finish the job.
  - CAS the predecessor’s next field
  - Proceed (repeat as needed)

# Lock-Free Traversal



# Further Reading

- Chapter 9 goes over implementations in detail.
  - This is tricky stuff! Please read to get a different perspective!
- Skip Lists
  - Binary search over linked list ( $\log(n)$  lookup time)
  - Chapter 14 of the book

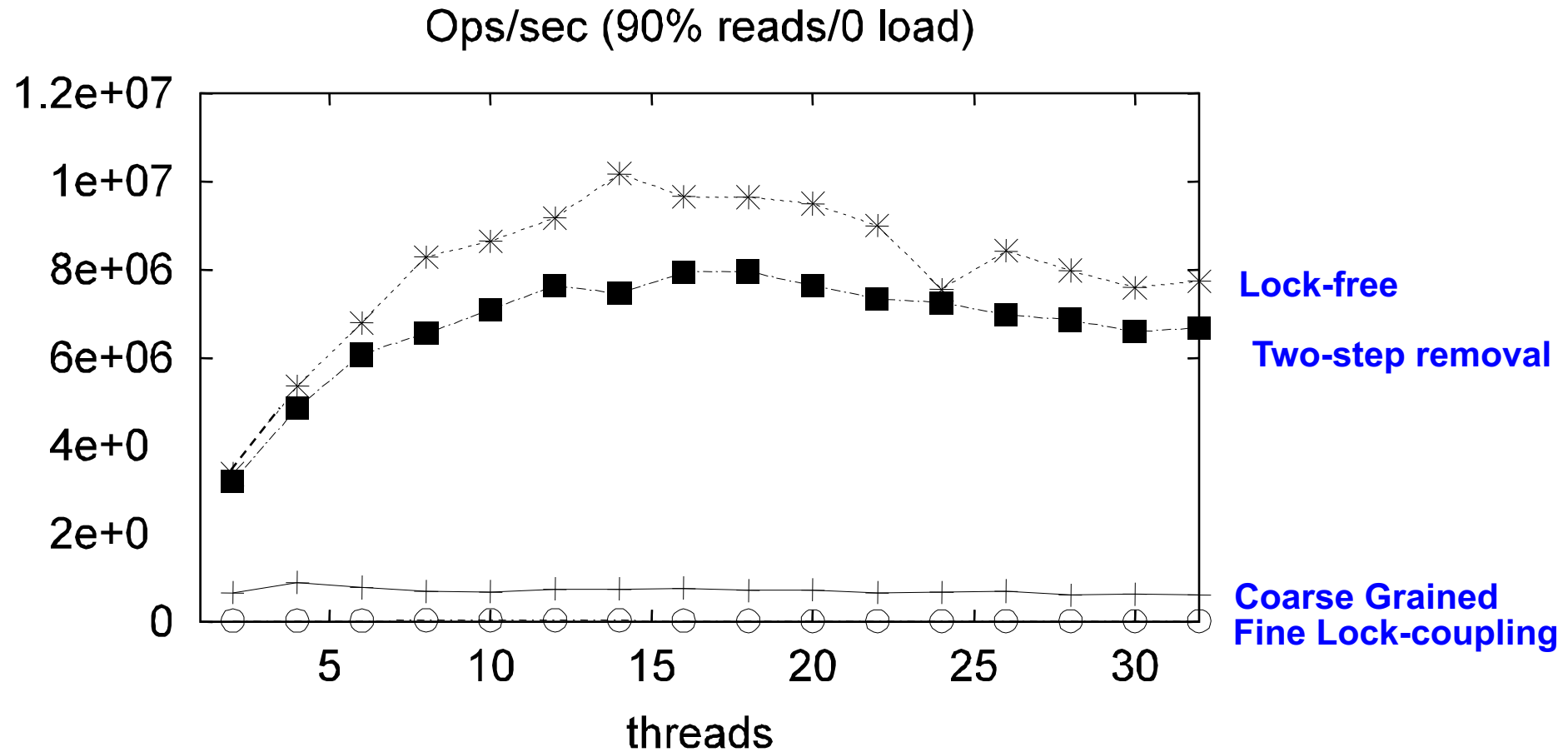
# Performance

- Issues:
  - Lazy removal makes benchmarking traversals very tricky
  - Garbage collection makes benchmarking very tricky

# Some performance results

From: A Lazy Concurrent List-Based Set Algorithm: 2005  
publication from the textbook authors research group

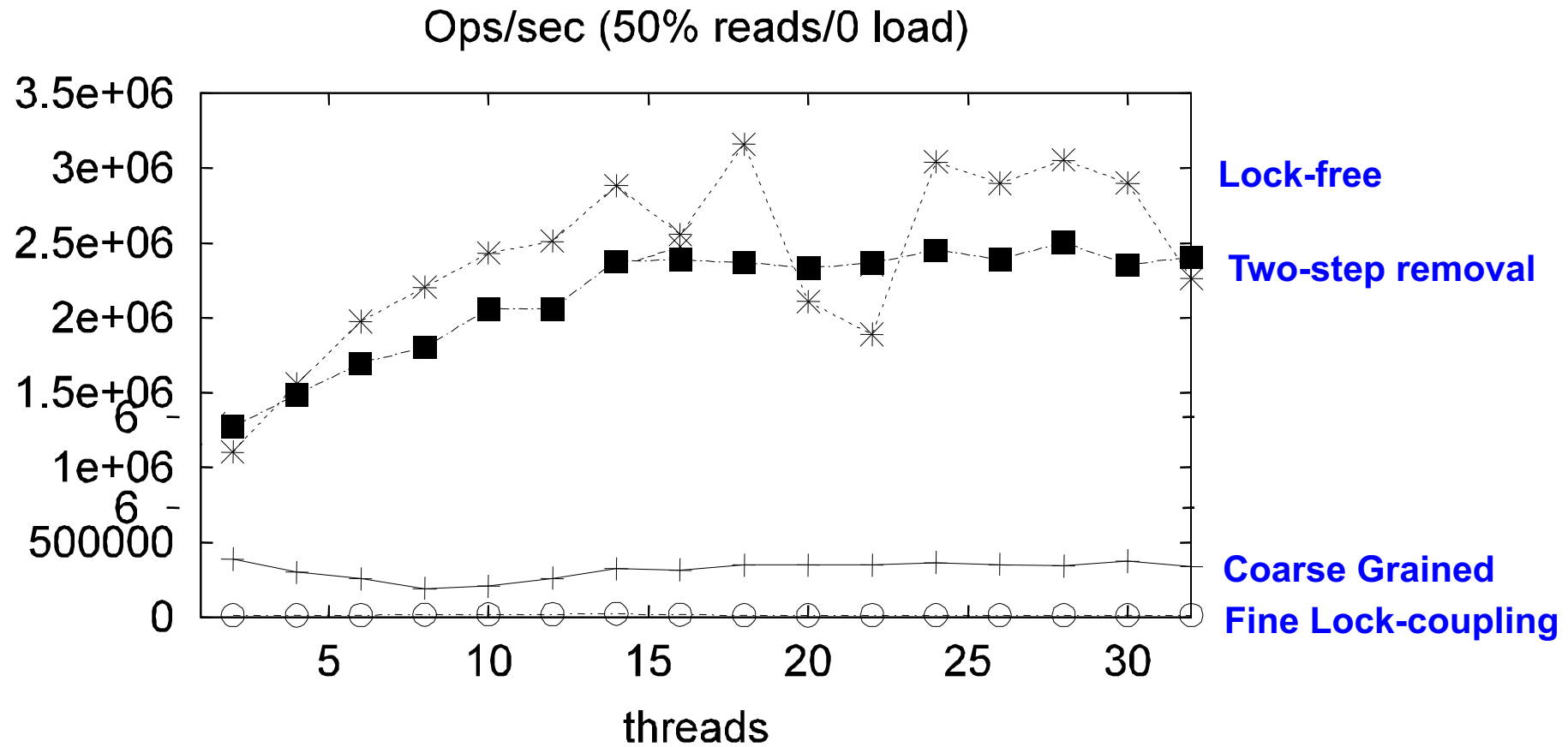
# High Contains Ratio





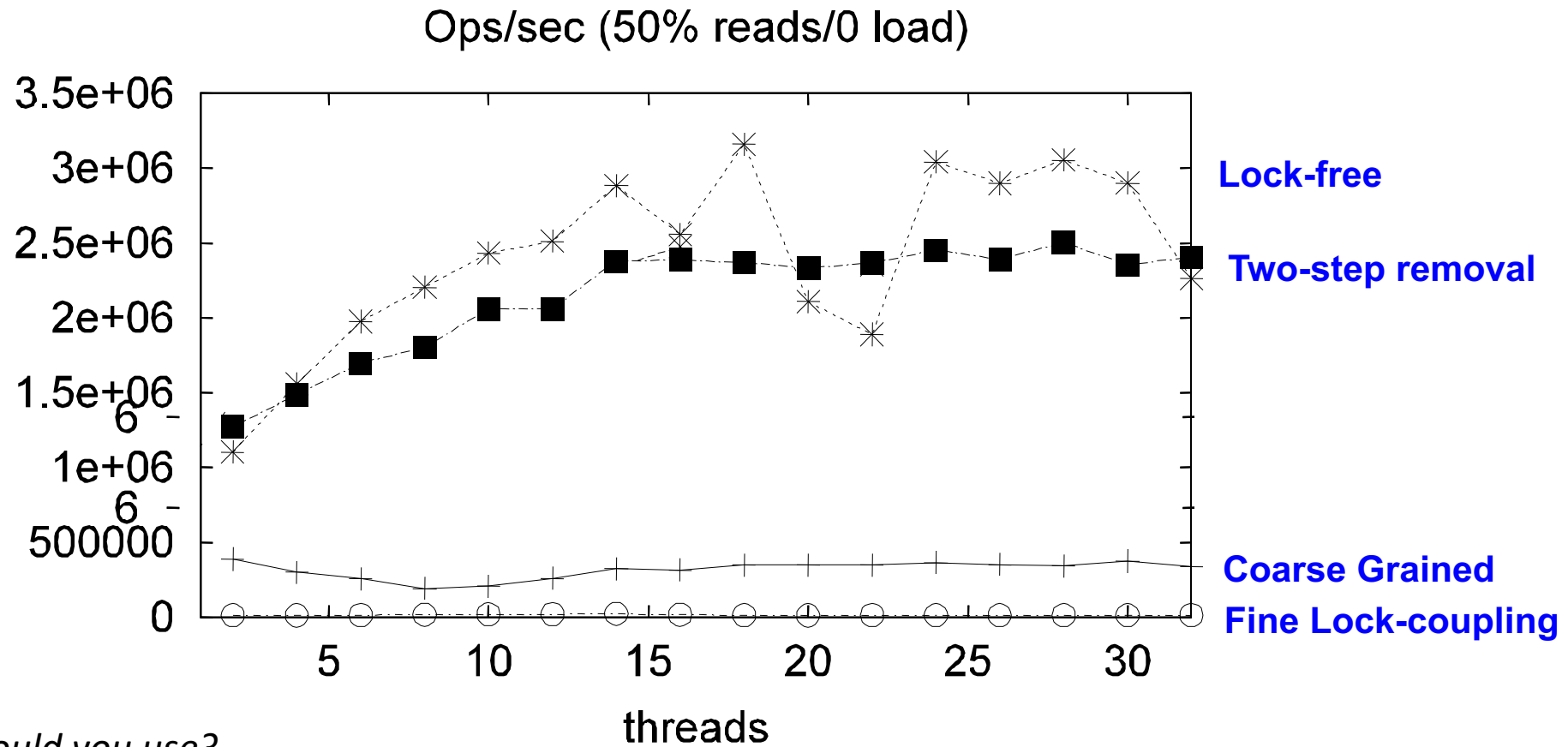
# Low Contains Ratio

noisy!



# Low Contains Ratio

noisy!



*Which one should you use?*

# Schedule

- Finish up linked-list
- **Concurrent Queues**
  - Input/Output Queues
  - Synchronous Producer/Consumer Queue
  - Async Producer/Consumer Queue

# Concurrent Queues

- New API
- List of items, accessed in a first-in first-out (FIFO) way
- *duplicates allowed*
- Methods
  - **enq(x)** put **x** in the list at the head
  - **deq()** remove the item at the tail of the queue and return it.
  - **size()** returns how many items are in the queue

# Concurrent Queues

- General implementation given in Chapter 10 of the book.
- Similar types of reasoning as the linked list
  - Lots of reasoning about node insertion, node deletion
  - Using atomic RMWs (CAS) in clever ways
- We will think about specialized queues
  - Implementations can be simplified!

# Input/Output Queues

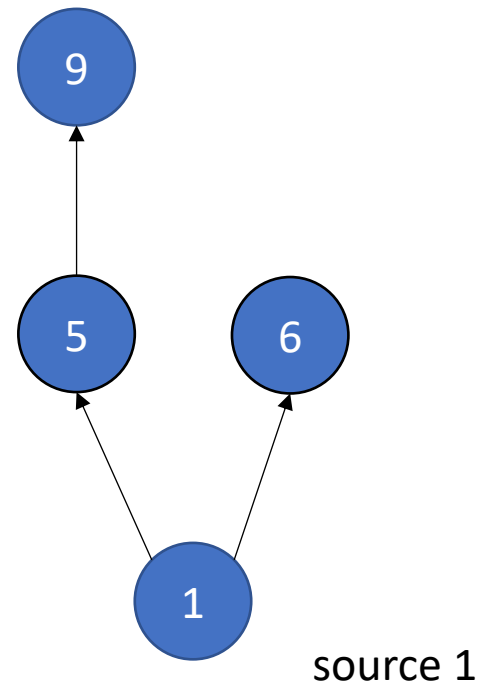
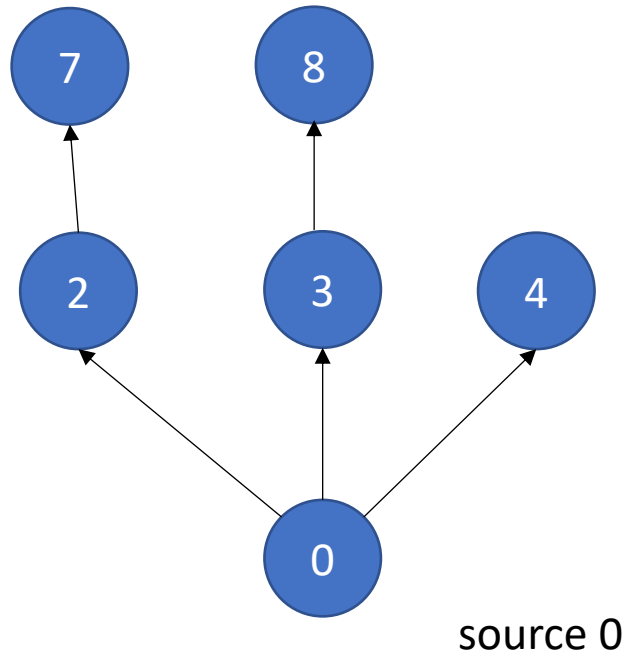
- Queue in which multiple threads read (deq), or write (enq), but not both.
- Why would we want a thing?
- Computation done in phases:
  - First phase prepares the queue (by writing into it)
  - All threads join
  - Second phase reads values from the queue.

# Input/Output Queues

- Example: Information flow in graph applications:

# Input/Output Queues

- Example: Information flow in graph applications:



queue 1

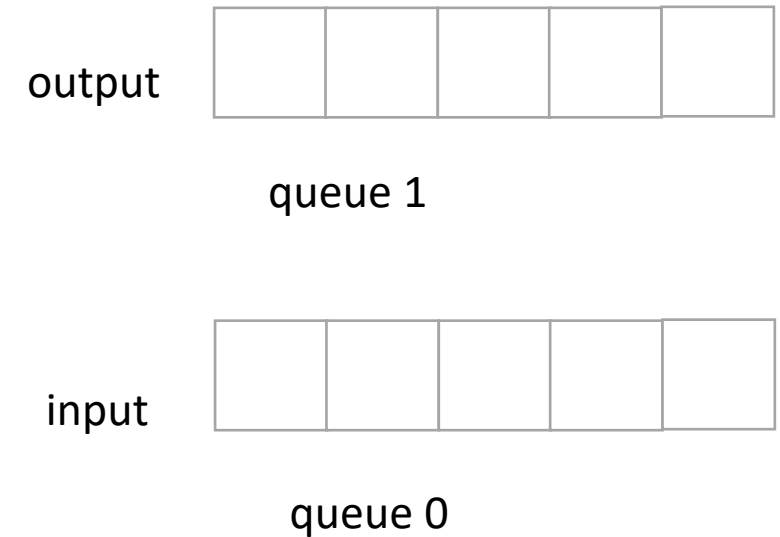
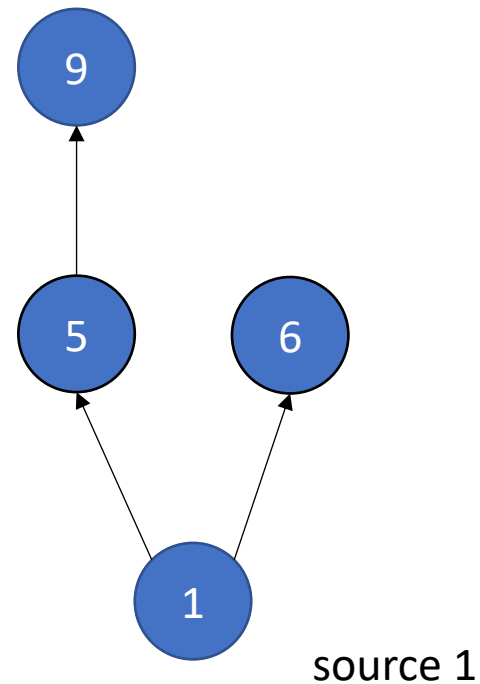
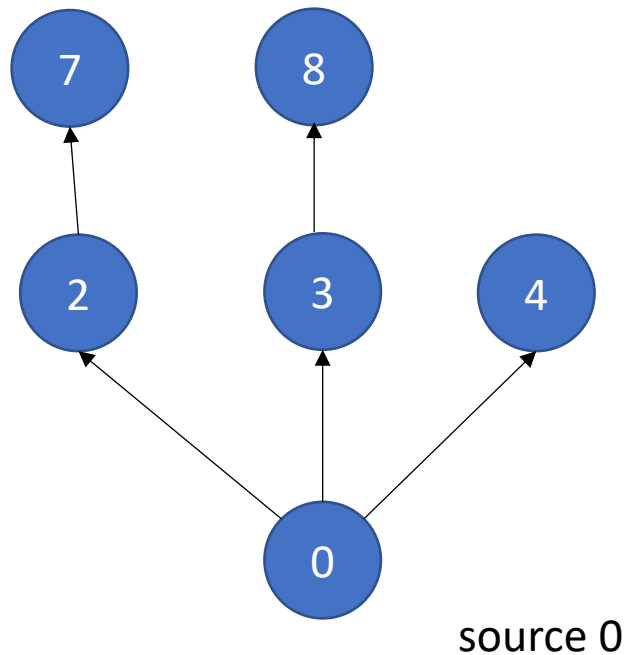


queue 0



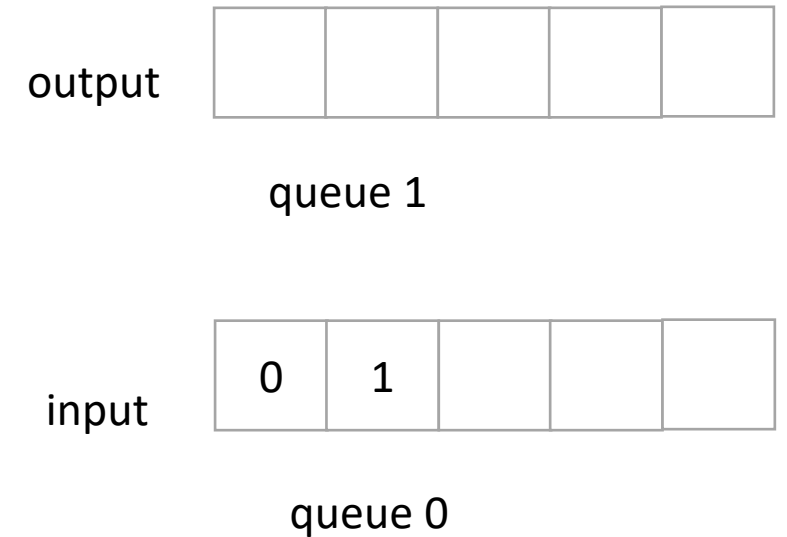
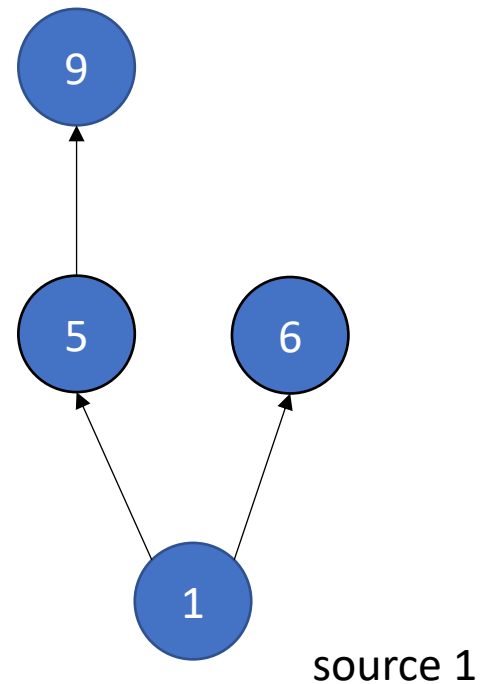
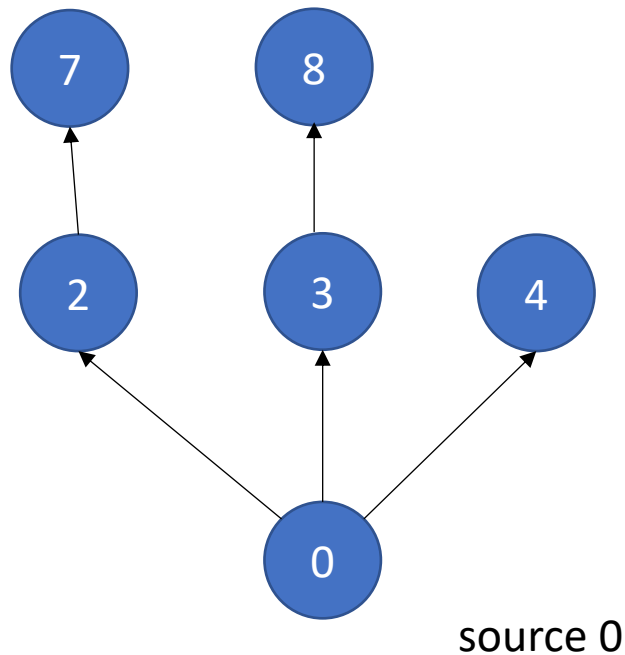
# Input/Output Queues

- Example: Information flow in graph applications:



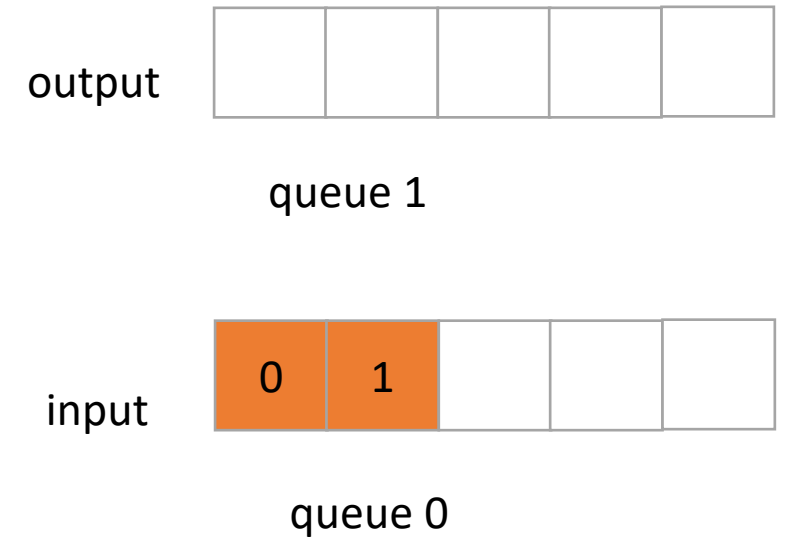
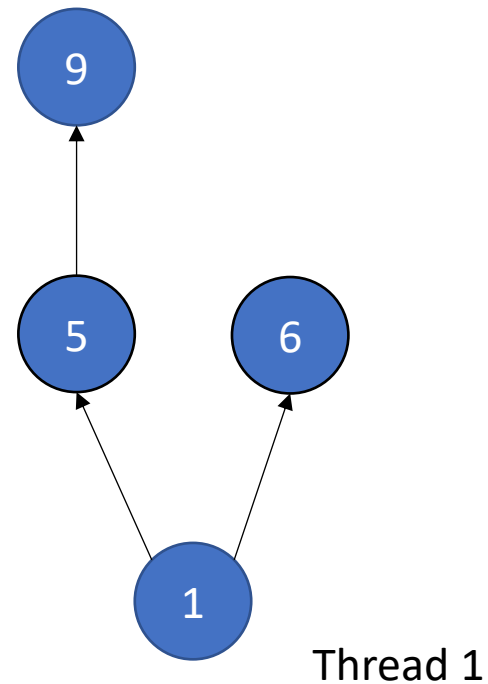
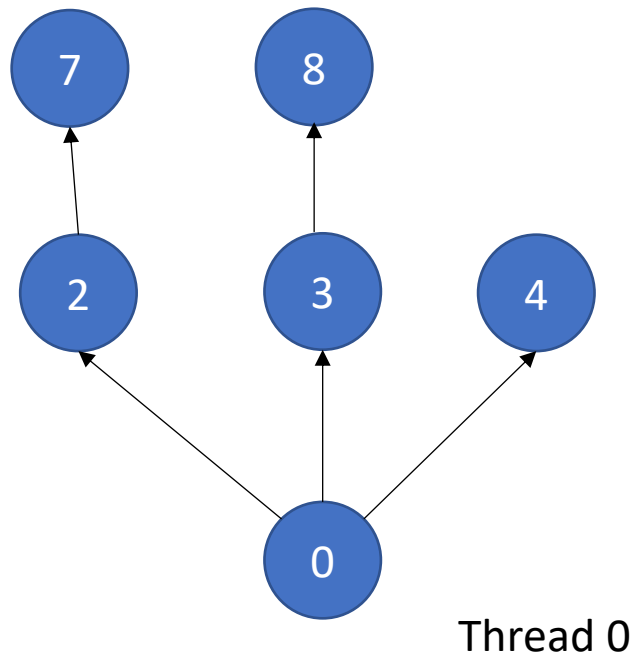
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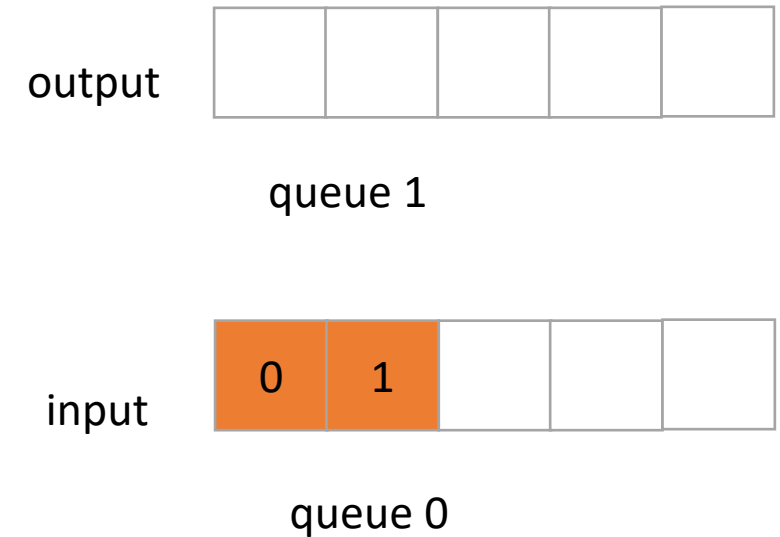
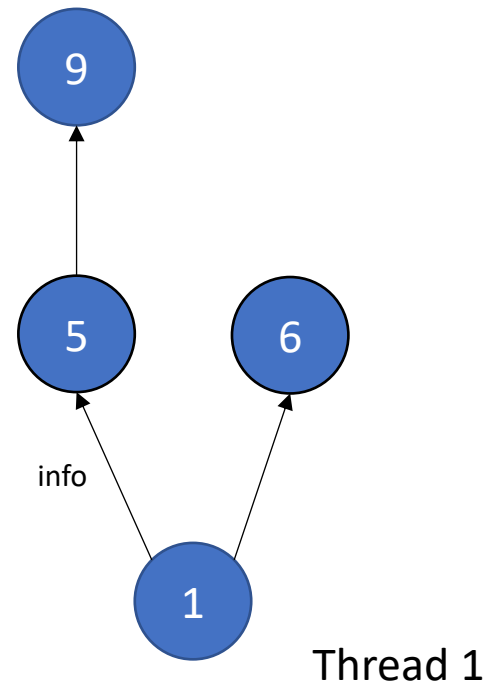
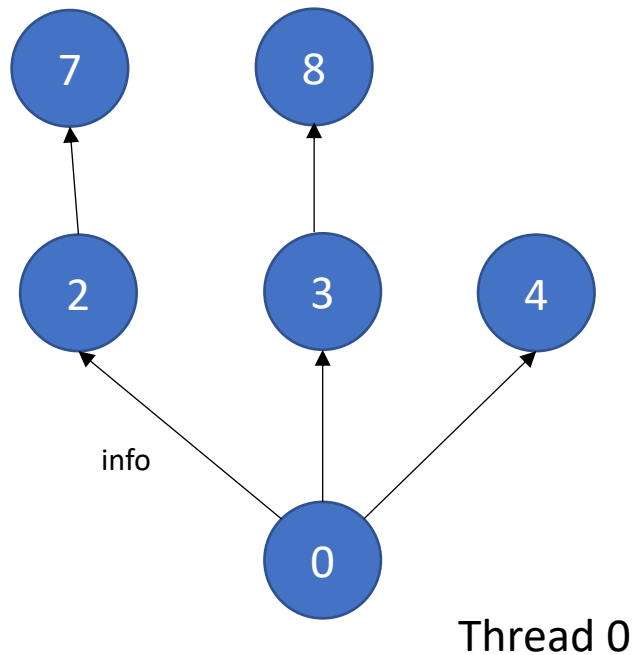
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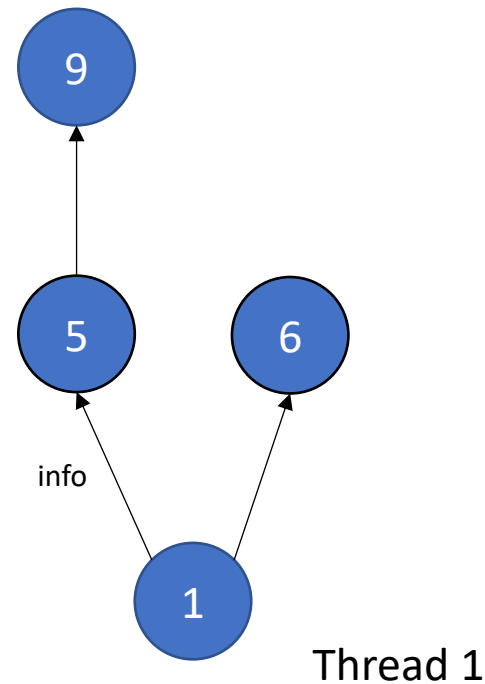
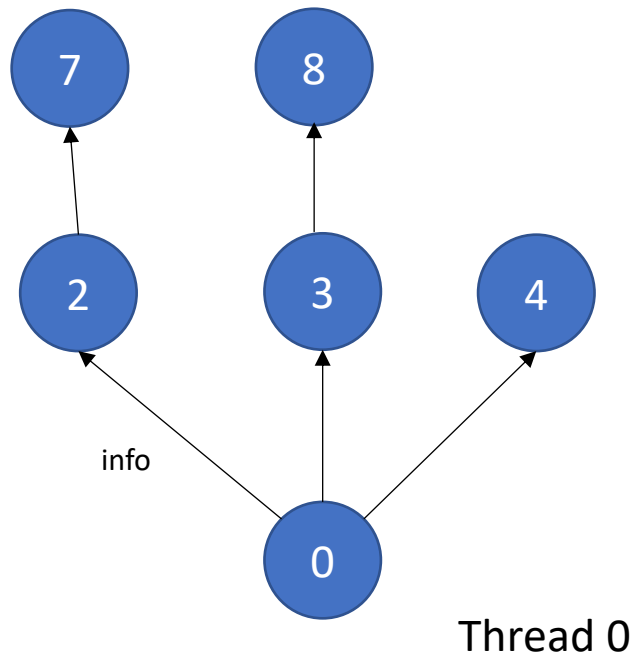
# Input/Output Queues

- Example: Information flow in graph applications:

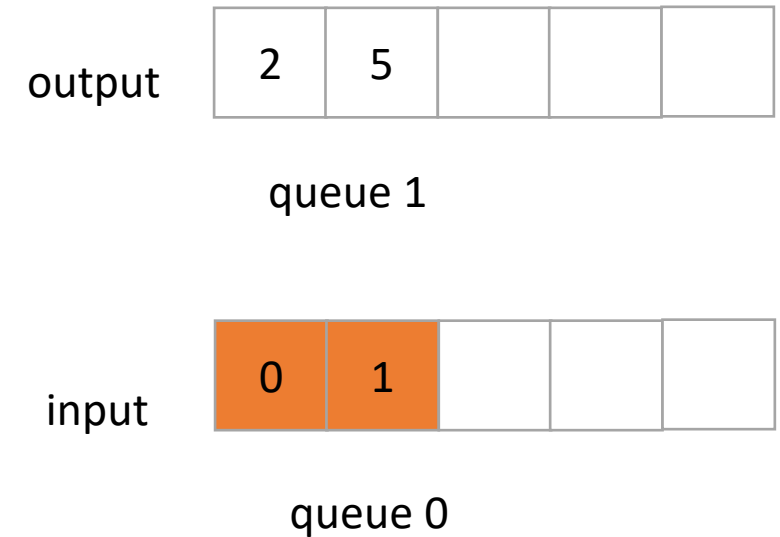


# Input/Output Queues

- Example: Information flow in graph applications:

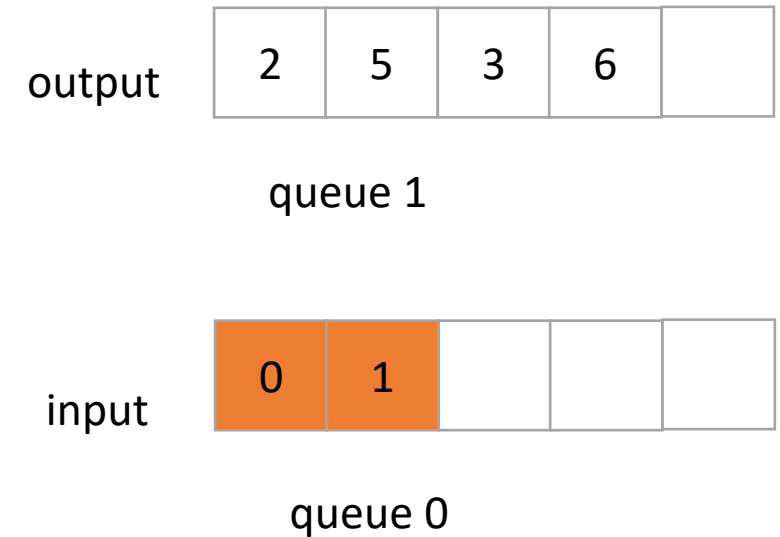
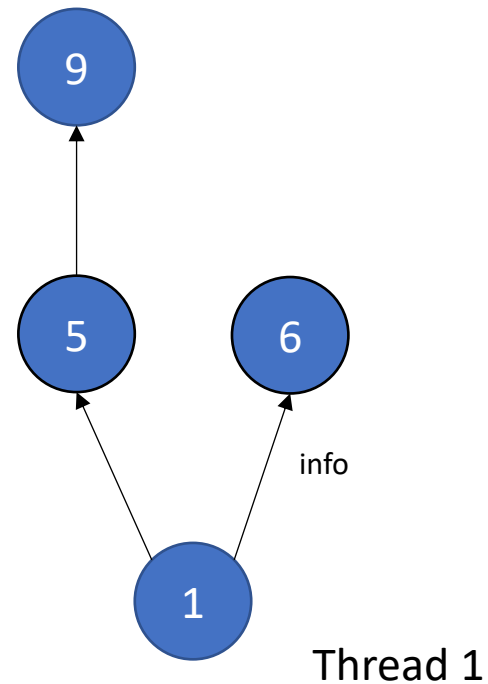
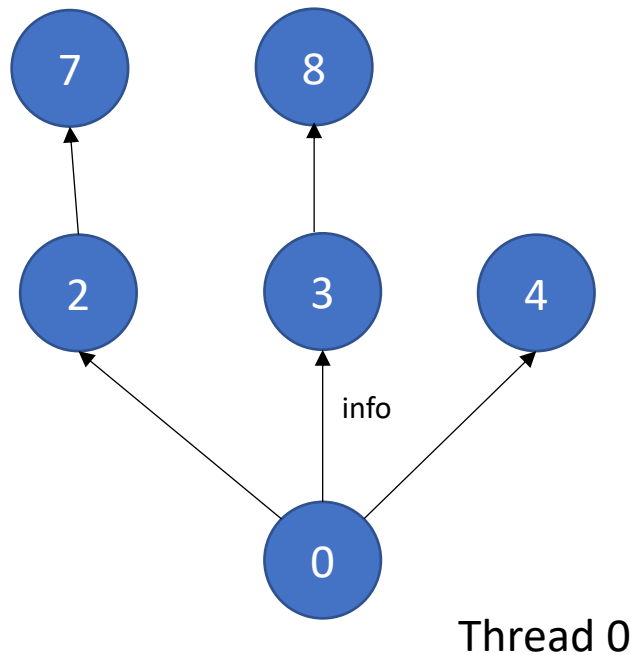


concurrent enqueues!



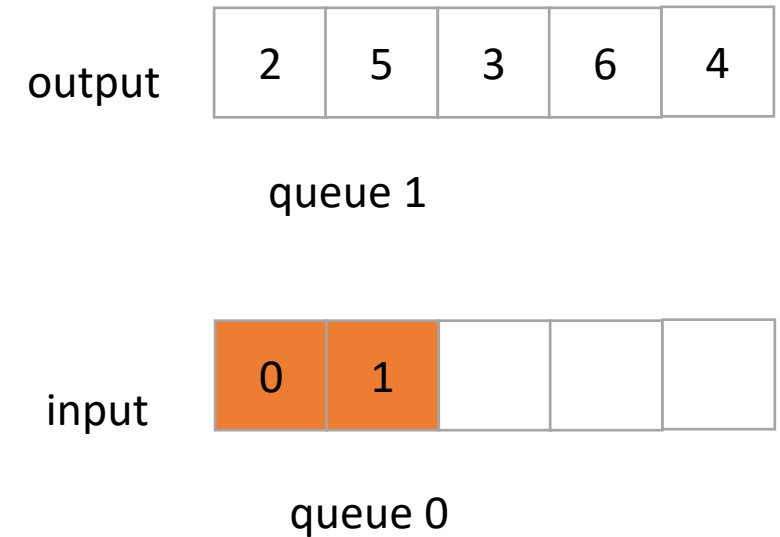
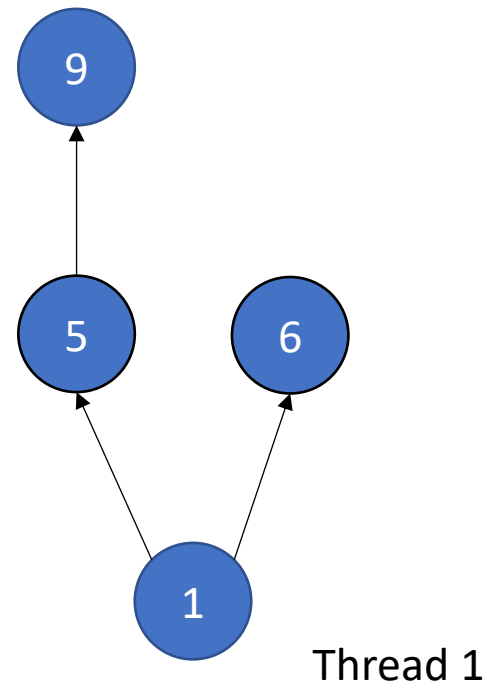
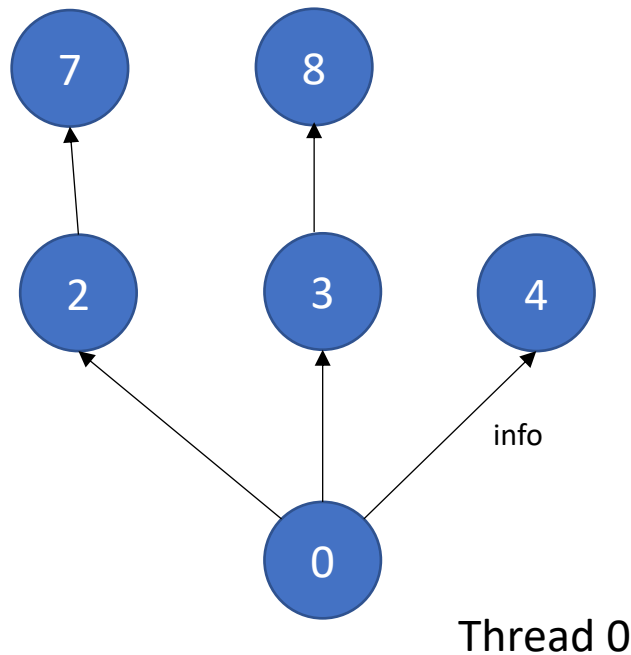
# Input/Output Queues

- Example: Information flow in graph applications:



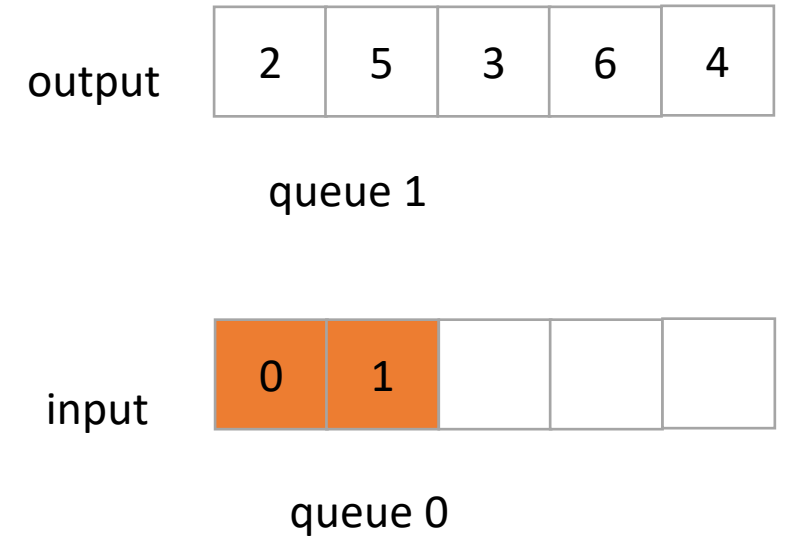
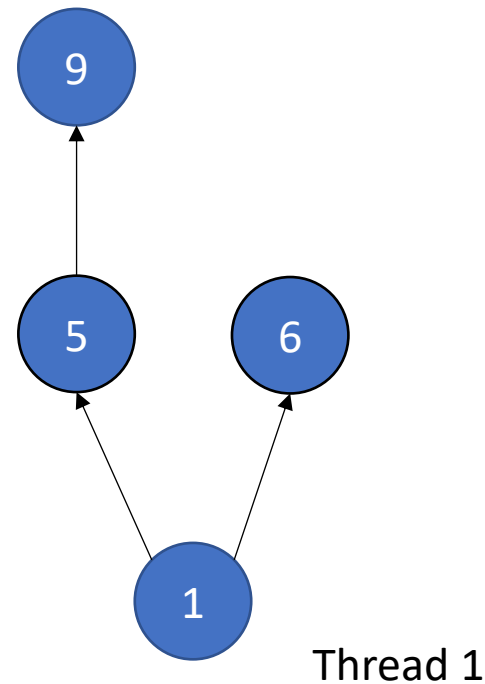
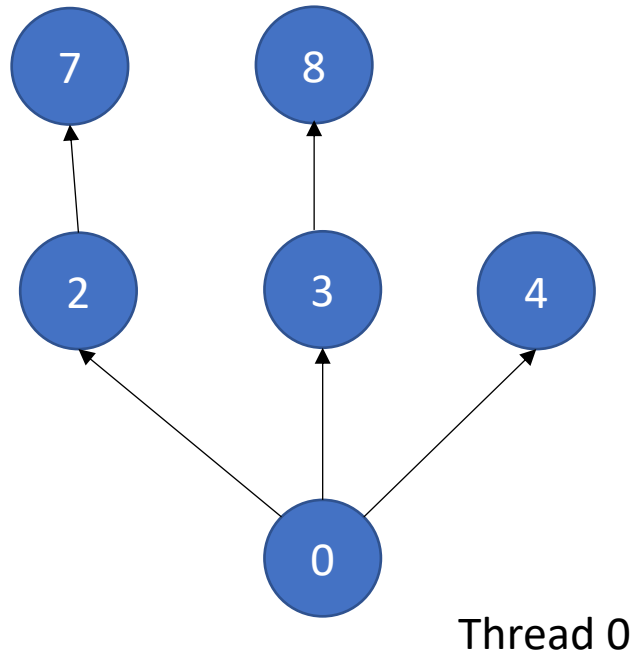
# Input/Output Queues

- Example: Information flow in graph applications:



# Input/Output Queues

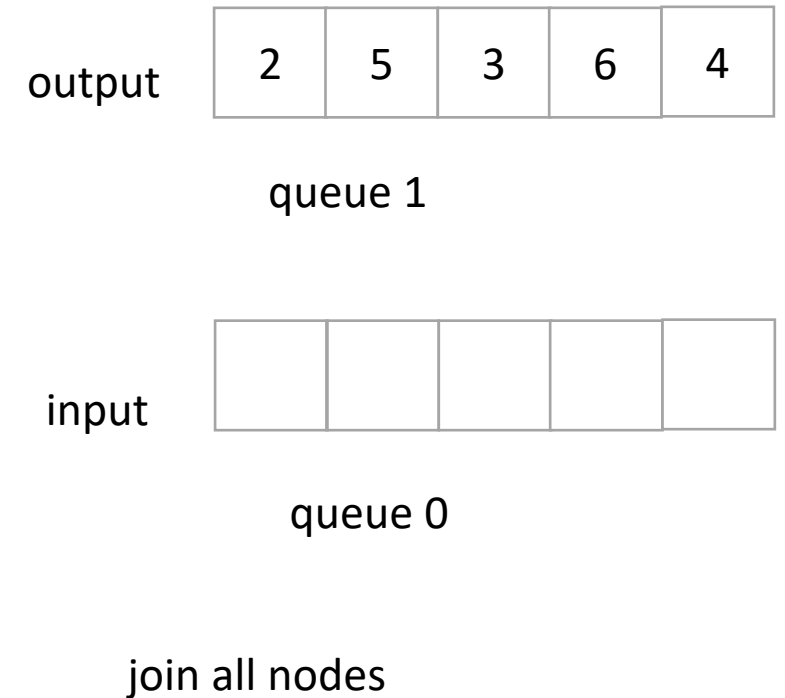
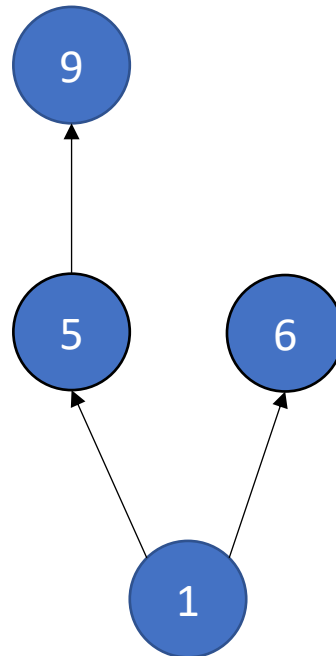
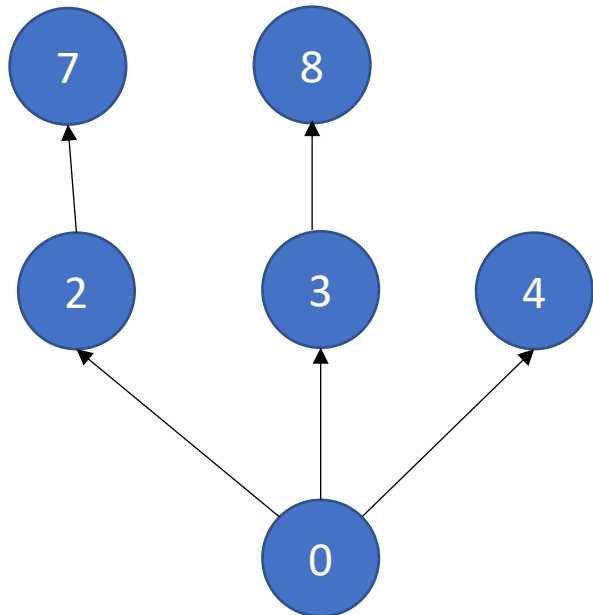
- Example: Information flow in graph applications:





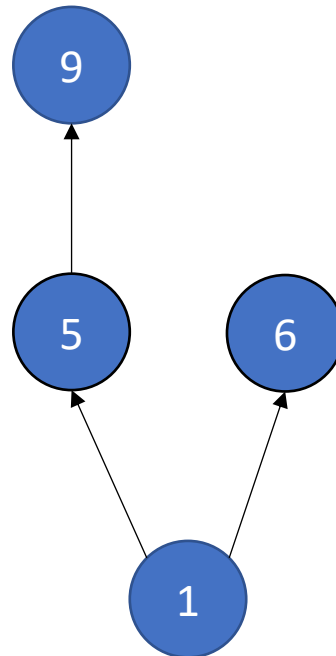
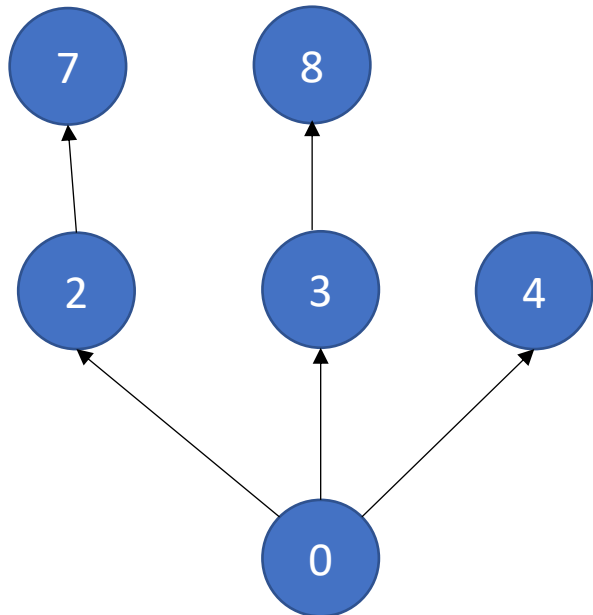
# Input/Output Queues

- Example: Information flow in graph applications:



# Input/Output Queues

- Example: Information flow in graph applications:



input

2	5	3	6	4
---	---	---	---	---

swap!

queue 1

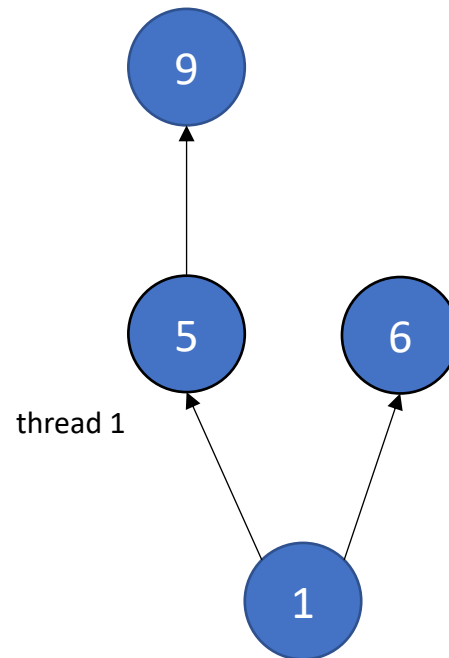
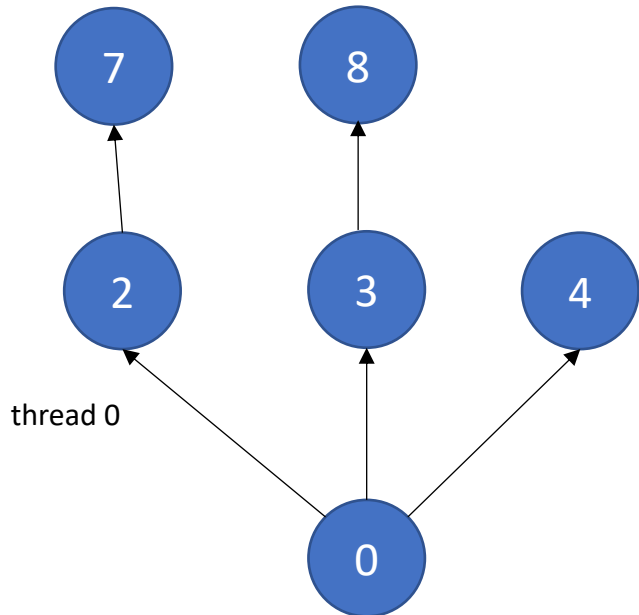
output

--	--	--	--	--

queue 0

# Input/Output Queues

- Example: Information flow in graph applications:



input



queue 1

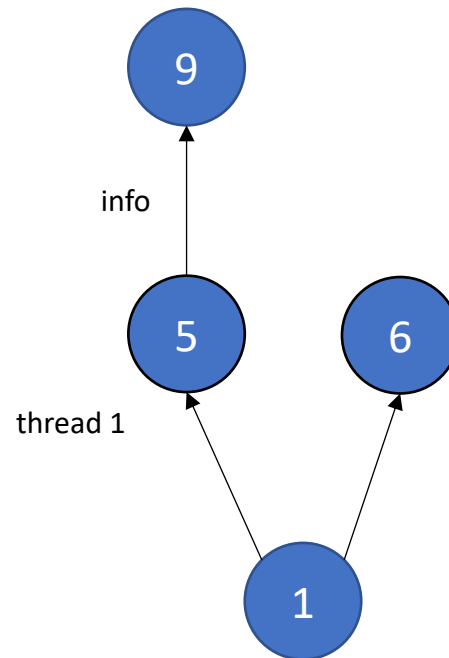
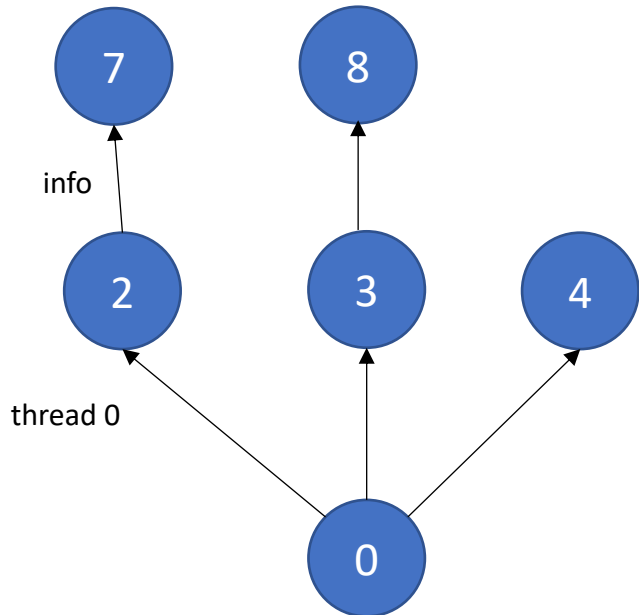
output



queue 0

# Input/Output Queues

- Example: Information flow in graph applications:



input



queue 1

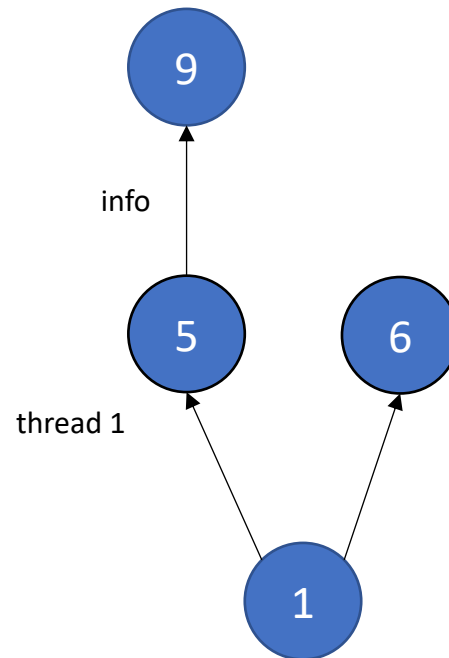
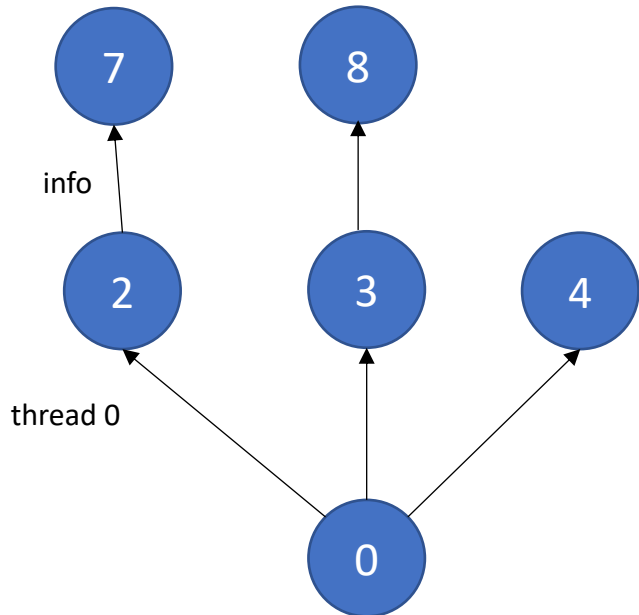
output



queue 0

# Input/Output Queues

- Example: Information flow in graph applications:



input

2	5	3	6	4
---	---	---	---	---

queue 1

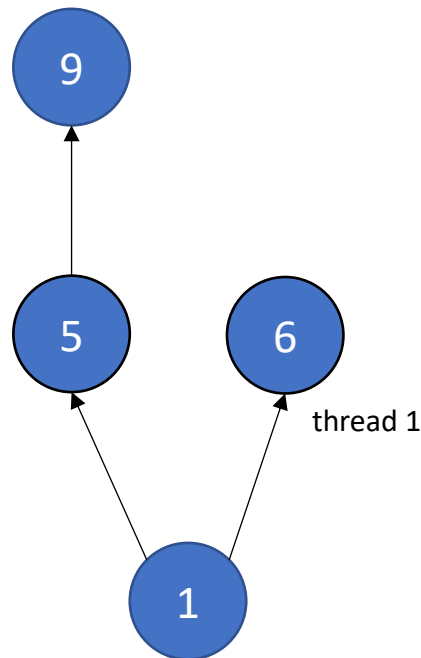
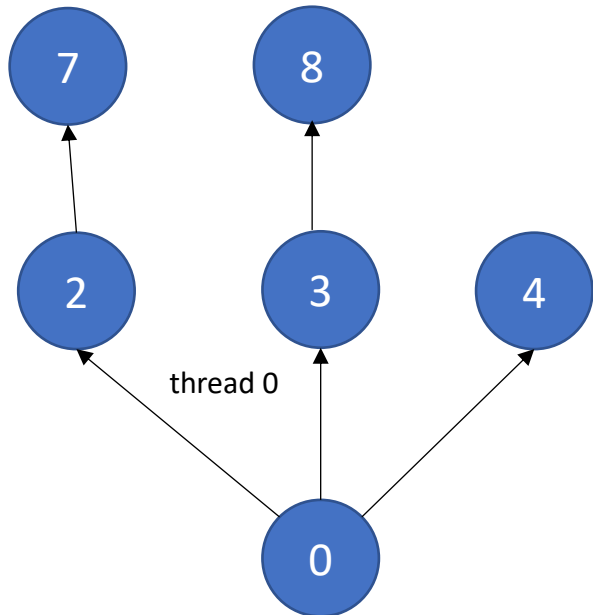
output

7	9			
---	---	--	--	--

queue 0

# Input/Output Queues

- Example: Information flow in graph applications:



input

2	5	3	6	4
---	---	---	---	---

queue 1

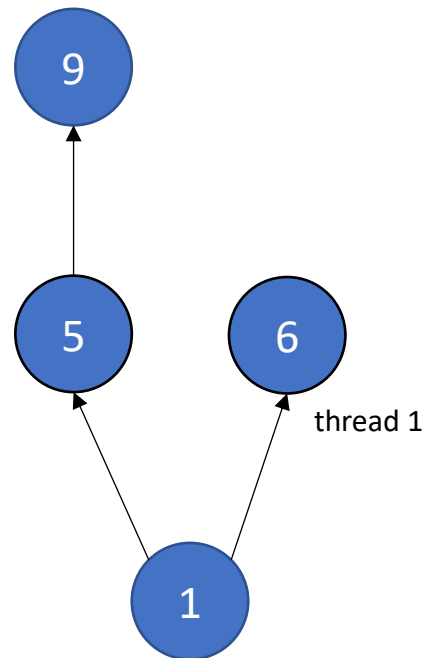
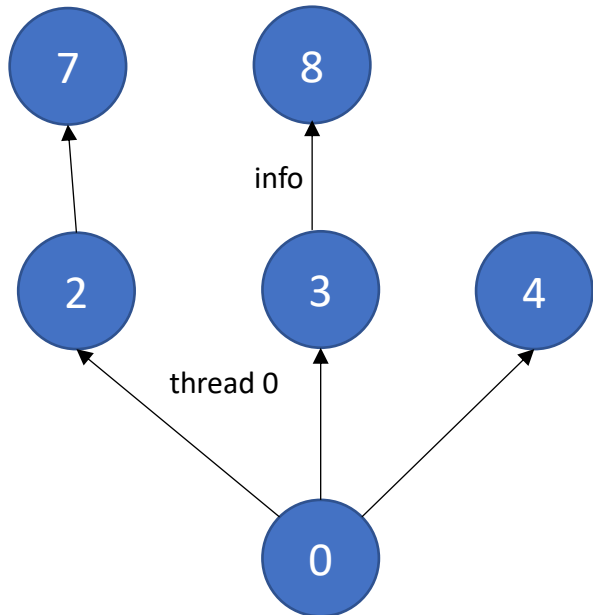
output

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queue 0

# Input/Output Queues

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queue 1

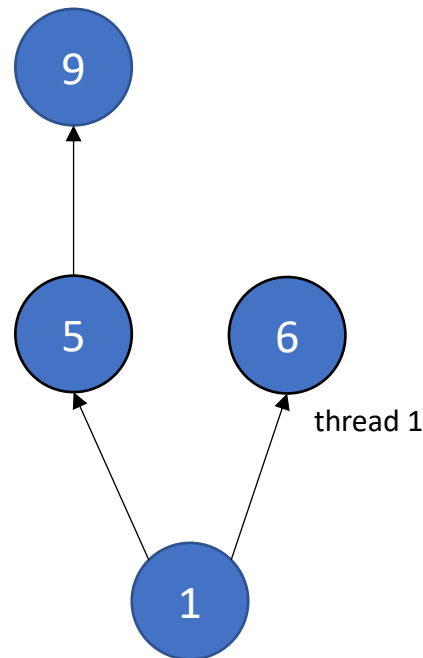
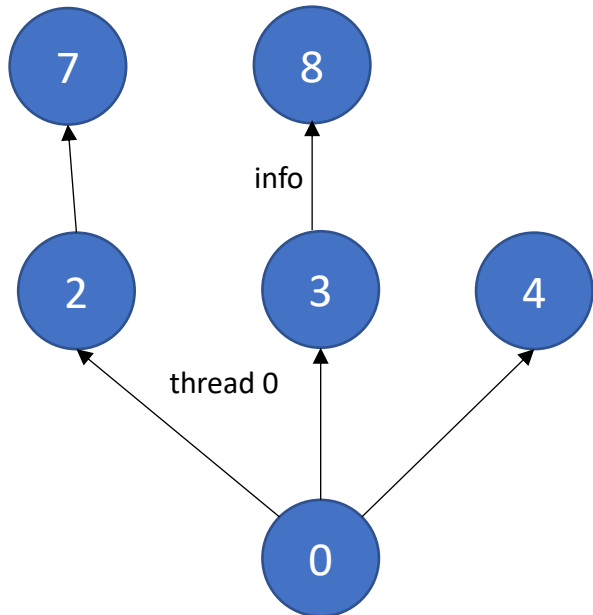
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7	9			
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queue 0

# Input/Output Queues

- Example: Information flow in graph applications:



input

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---	---	---	---	---

queue 1

output

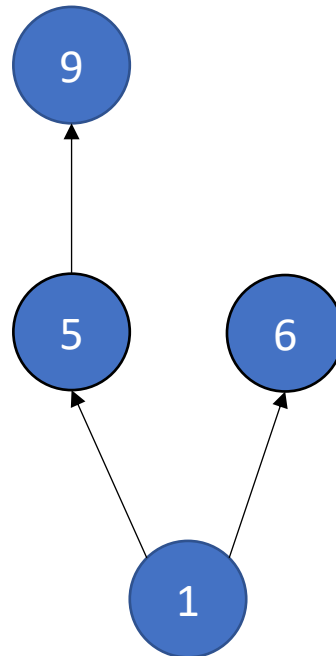
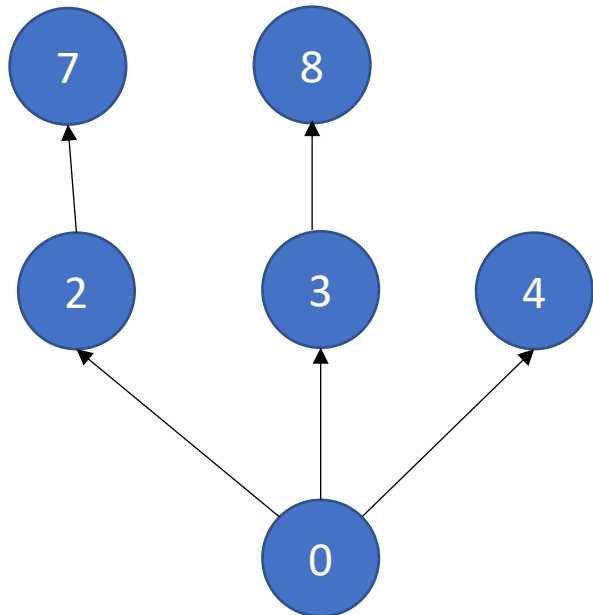
7	9	8		
---	---	---	--	--

queue 0



# Input/Output Queues

- Example: Information flow in graph applications:



input

2	5	3	6	4
---	---	---	---	---

queue 1

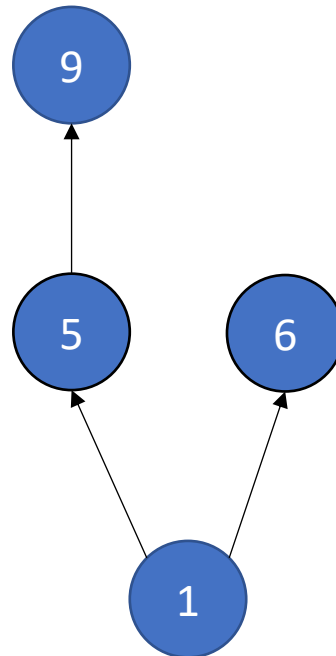
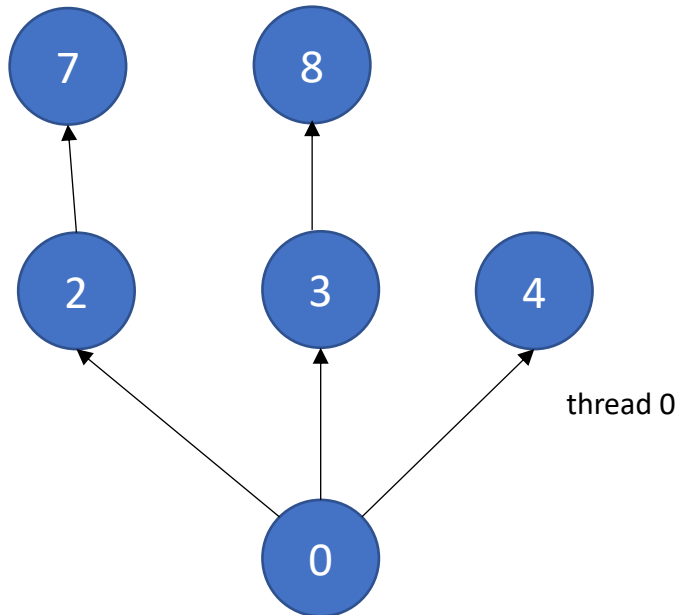
output

7	9	8		
---	---	---	--	--

queue 0

# Input/Output Queues

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input

2	5	3	6	4
---	---	---	---	---

queue 1

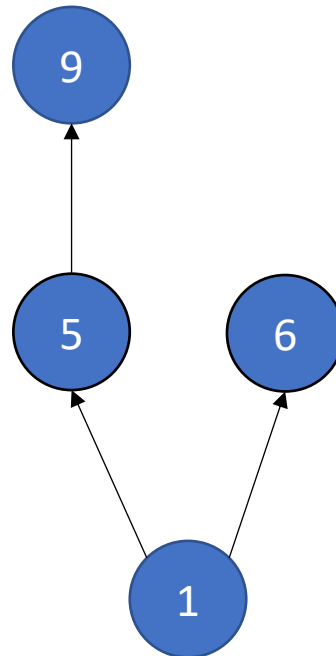
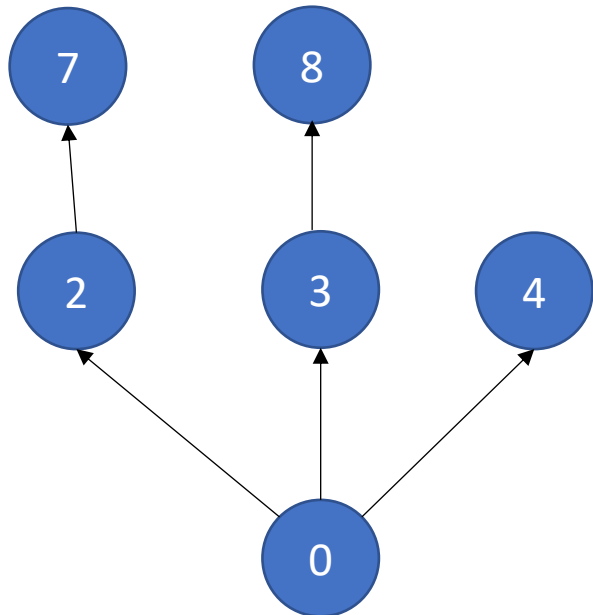
output

7	9	8		
---	---	---	--	--

queue 0

# Input/Output Queues

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input

2	5	3	6	4
---	---	---	---	---

queue 1

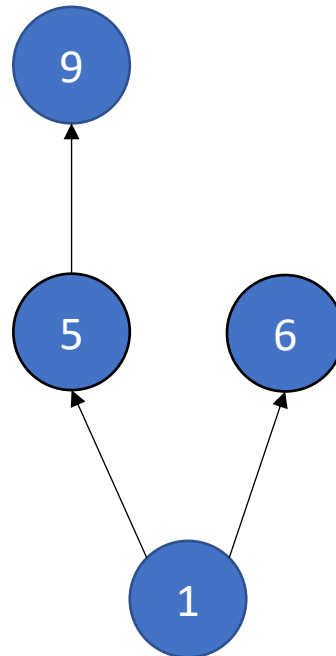
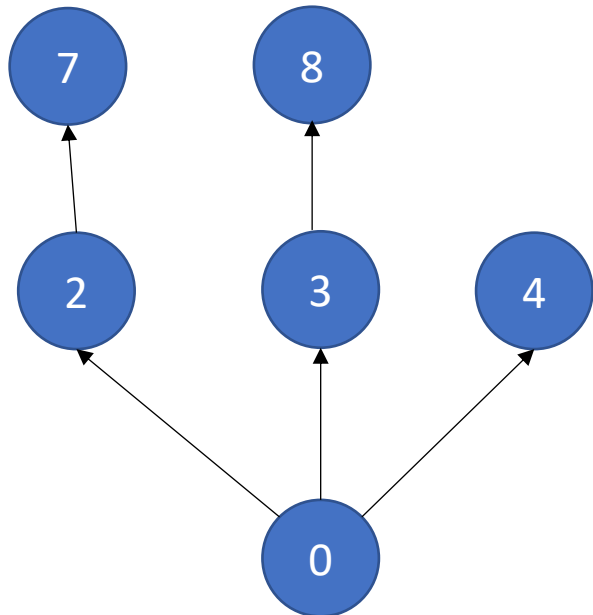
output

7	9	8		
---	---	---	--	--

queue 0

# Input/Output Queues

- Example: Information flow in graph applications:



*and so on...*

output



queue 1

input



queue 0

# Implementation

# Implementation

Allocate a contiguous array



Pros:

?

Cons:

?

# Implementation

Allocate a contiguous array



Pros:

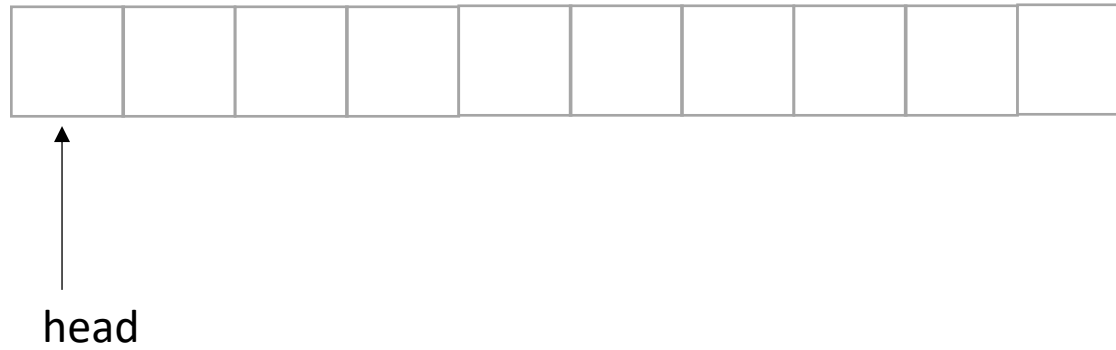
- + fast!

- + we can use indexes instead of addresses

Cons:

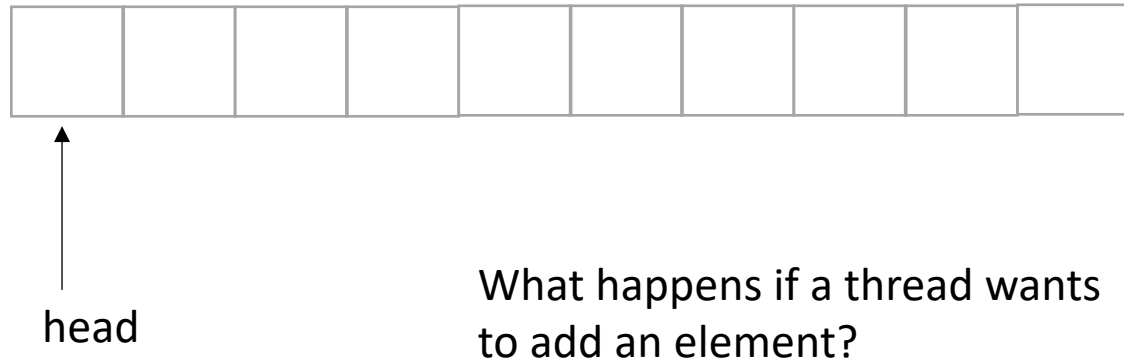
- need to reason about overflow!

# Implementation

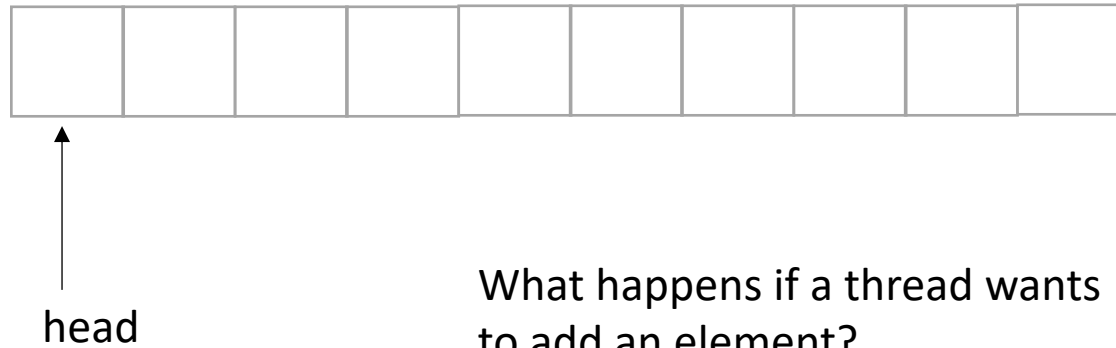




# Implementation



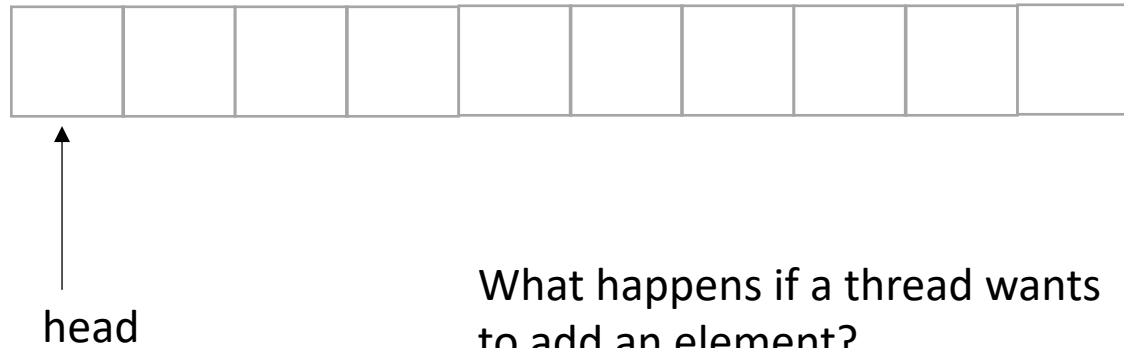
# Implementation



What happens if a thread wants to add an element?

Think sequentially:

# Implementation



What happens if a thread wants to add an element?

Think sequentially:

- \*reserve a space - increment head

# Implementation

reserved!



head

What happens if a thread wants to add an element?

Think sequentially:

\*reserve a space - increment tail

# Implementation

reserved!



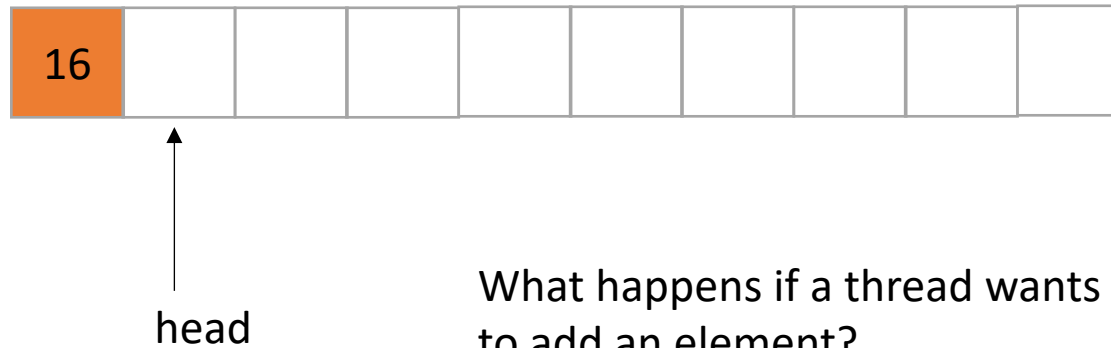
head

What happens if a thread wants to add an element?

Think sequentially:

- \* reserve a space - increment head
- \* add the element

# Implementation

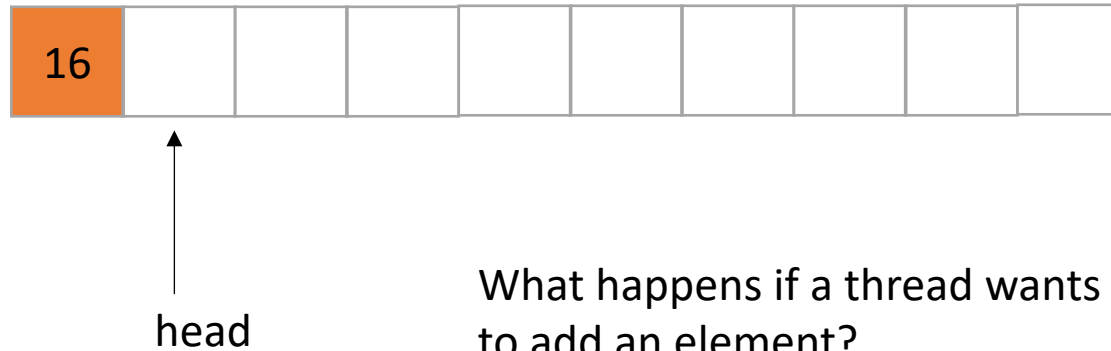


What happens if a thread wants to add an element?

Think sequentially:

- \* reserve a space - increment head
- \* add the element

# Implementation



What happens if a thread wants to add an element?

Think sequentially:

- \* reserve a space - increment head
- \* add the element

done!

# Implementation



What happens if a thread wants to add an element?

Think concurrently:

*Two threads cannot reserve the same space!  
We've seen this before*



# Implementation

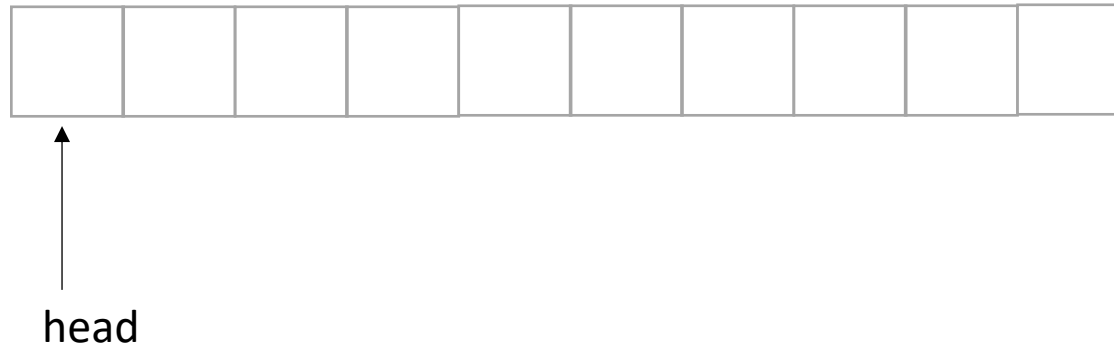


What happens if a thread wants to add an element?

Think concurrently:

```
reserved_index = atomic_fetch_add(&head, 1);
```

# Implementation



Thread 0:  
*enq(6);*

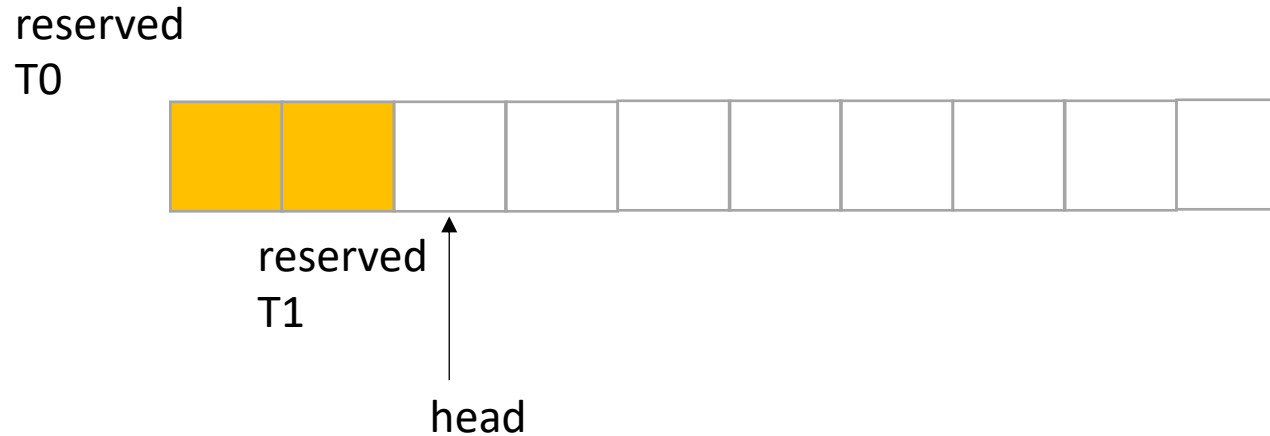
Thread 1:  
*enq(7);*

What happens if a thread wants  
to add an element?

Think concurrently:

```
reserved_index = atomic_fetch_add(&head, 1);
```

# Implementation



Thread 0:  
*enq(6);*

Thread 1:  
*enq(7);*

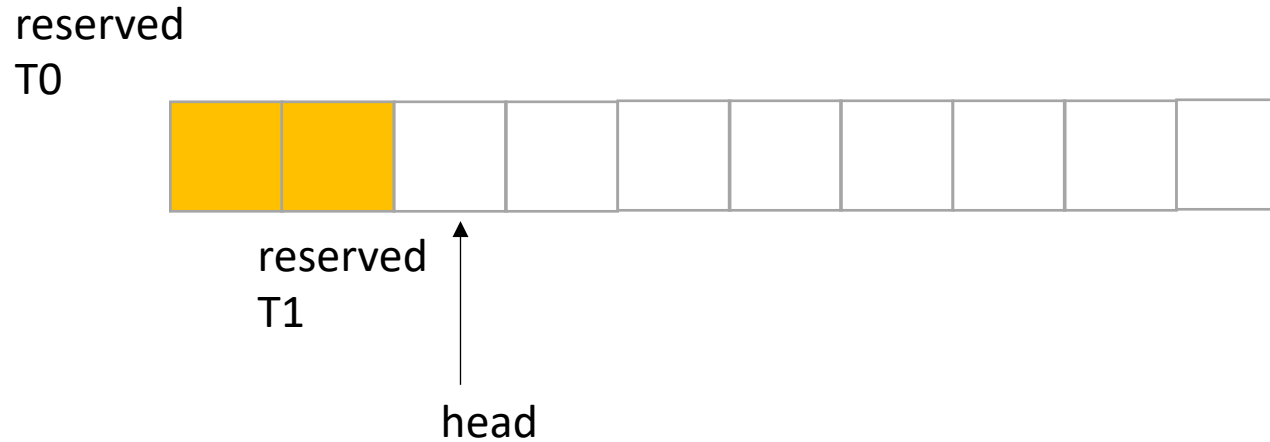
What happens if a thread wants to add an element?

Think concurrently:

```
reserved_index = atomic_fetch_add(&head, 1);
```

# Implementation

*does it matter which order  
threads add their data?*



Thread 0:  
`enq(6);`

Thread 1:  
`enq(7);`

What happens if a thread wants  
to add an element?

Think concurrently:

```
reserved_index = atomic_fetch_add(&head, 1);
```

# Implementation

*does it matter which order  
threads add their data?*

reserved  
T0



head

Thread 0:  
`enq(6);`

Thread 1:  
`enq(7);`

What happens if a thread wants  
to add an element?

Think concurrently:

```
reserved_index = atomic_fetch_add(&head, 1);
```

# Implementation

*does it matter which order  
threads add their data? No!  
Because there are no deqs!*

reserved  
T0



head

Thread 0:  
*enq(6);*

Thread 1:  
*enq(7);*

What happens if a thread wants  
to add an element?

Think concurrently:

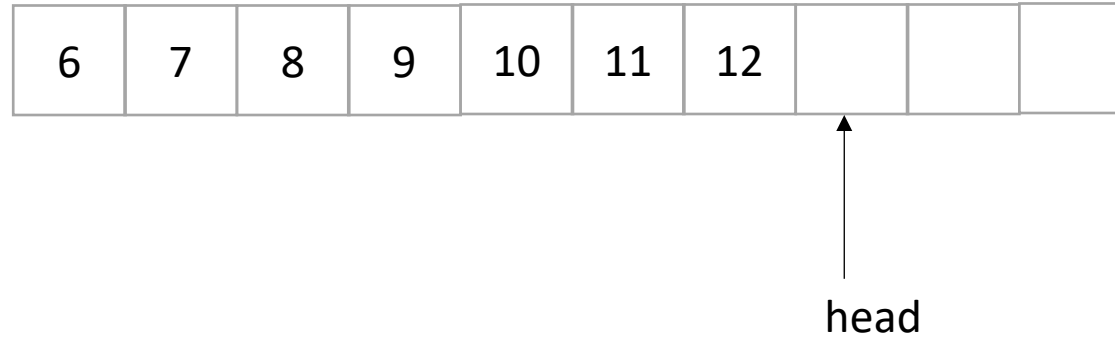
```
reserved_index = atomic_fetch_add(&head, 1);
```

```
class InputOutputQueue {  
    private:  
        atomic_int head;  
        int list[SIZE];  
  
    public:  
        InputOutputQueue() {  
            head = 0;  
        }  
  
        void enq(int x) {  
            int reserved_index = atomic_fetch_add(&head, 1);  
            list[reserved_index] = x;  
        }  
  
        int size() {  
            return head.load();  
        }  
}
```

How to protect against overflows?

# What about Input?

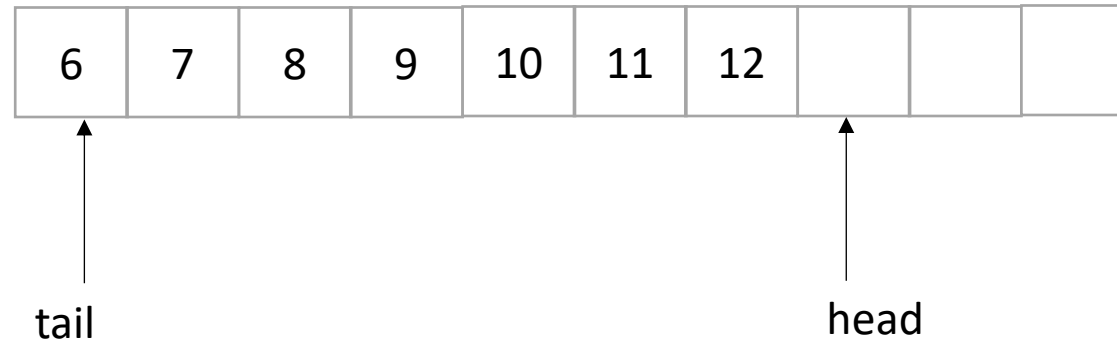
- Now we only do deqs





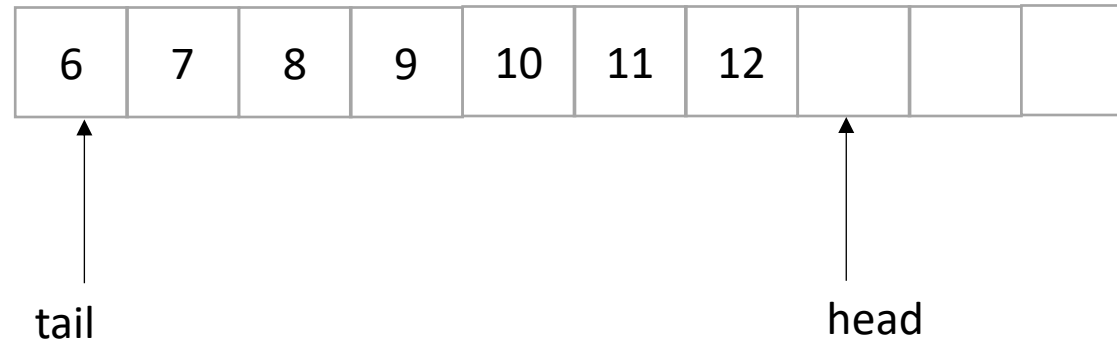
# What about Input?

- Now we only do deqs



# What about Input?

- Now we only do deqs



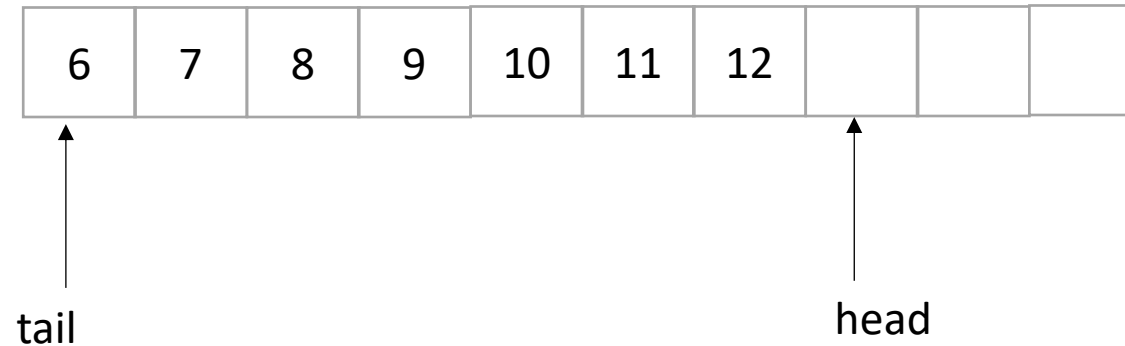
What happens if a thread wants to add an element?

Think concurrently:

```
data_index = atomic_fetch_add(&tail, 1);
```

# What about Input?

- Now we only do deqs



Thread 0:  
*deq();*

Thread 1:  
*deq();*

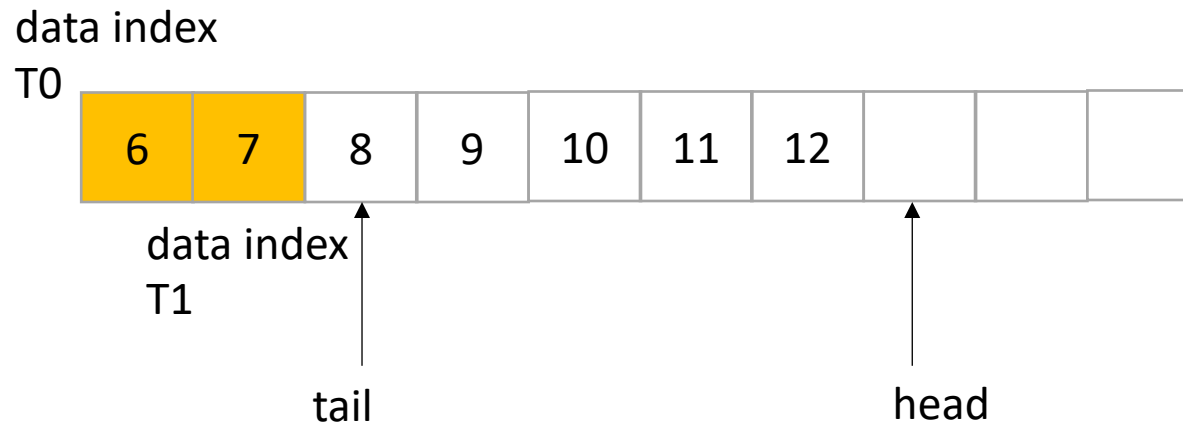
What happens if a thread wants to add an element?

Think concurrently:

```
data_index = atomic_fetch_add(&tail, 1);
```

# What about Input?

- Now we only do deqs



Thread 0:  
*deq();*

Thread 1:  
*deq();*

What happens if a thread wants  
to add an element?

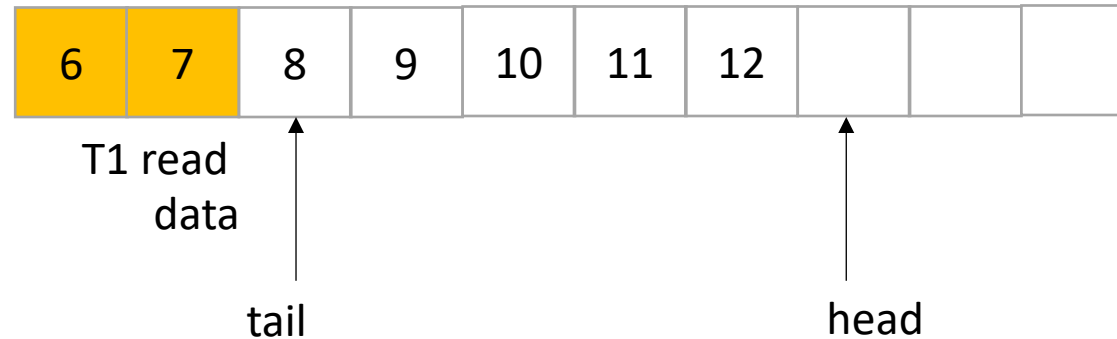
Think concurrently:

```
data_index = atomic_fetch_add(&tail, 1);
```

# What about Input?

- Now we only do deqs

T0 read data



T1 read  
data

tail

head

Thread 0:  
*deq(); // reads 6*

Thread 1:  
*deq(); // reads 7*

What happens if a thread wants  
to add an element?

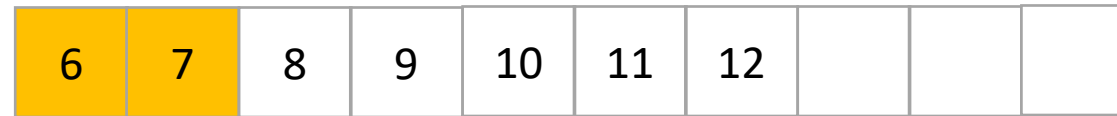
Think concurrently:

```
data_index = atomic_fetch_add(&tail, 1);
```

# What about Input?

- Now we only do deqs

T0 read data



T1 read  
data

tail

head

How to implement  
a stack?

Thread 0:  
*deq(); // reads 6*

Thread 1:  
*deq(); // reads 7*

What happens if a thread wants  
to add an element?

Think concurrently:

```
data_index = atomic_fetch_add(&tail, 1);
```

```
class InputOutputQueue {
    private:
        atomic_int head;
        atomic_int tail;
        int list[SIZE];

    public:
        InputOutputQueue() {
            head = tail = 0;
        }

        void enq(int x) {
            int reserved_index = atomic_fetch_add(&head, 1);
            list[reserved_index] = x;
        }

        void deq() {
            int reserved_index = atomic_fetch_add(&tail, 1);
            return list[reserved_index];
        }

        int size() {
            return head.load();
        }
}
```

```
class InputOutputQueue {
    private:
        atomic_int head;
        atomic_int tail;
        int list[SIZE];

    public:
        InputOutputQueue() {
            head = tail = 0;
        }

        void enq(int x) {
            int reserved_index = atomic_fetch_add(&head, 1);
            list[reserved_index] = x;
        }

        void deq() {
            int reserved_index = atomic_fetch_add(&tail, 1);
            return list[reserved_index];
        }

        int size() {
            return head.load();
        }
}
```

how about size?



```
class InputOutputQueue {
    private:
        atomic_int head;
        atomic_int tail;
        int list[SIZE];

    public:
        InputOutputQueue() {
            head = tail = 0;
        }

        void enq(int x) {
            int reserved_index = atomic_fetch_add(&head, 1);
            list[reserved_index] = x;
        }

        void deq() {
            int reserved_index = atomic_fetch_add(&tail, 1);
            return list[reserved_index];
        }

        int size() {
            return head.load() - tail.load();
        }
}
```

how about size?

how do we reset?

```

class InputOutputQueue {
    private:
        atomic_int head;
        atomic_int tail;
        int list[SIZE];

    public:
        InputOutputQueue() {
            head = tail = 0;
        }

        void enq(int x) {
            int reserved_index = atomic_fetch_add(&head, 1);
            list[reserved_index] = x;
        }

        void deq() {
            int reserved_index = atomic_fetch_add(&tail, 1);
            if (reserved_index > SIZE) throw exception
            return list[reserved_index];
        }

        int size() {
            return head.load() - tail.load();
        }
}

```

how about size?

how do we reset?

does the list need  
to be atomic?

# Schedule

- Finish up linked-list
- **Concurrent Queues**
  - Input/Output Queues
  - **Synchronous Producer/Consumer Queue**
  - Async Producer/Consumer Queue

5 minute break

# Producer Consumer Queues

- 1 enq, 1 deq
  - enq'er cannot deq
  - deq cannot enq
- Example: printf:
  - your program equeues values to print
  - the terminal process dequeues values and prints them

# Synchronous Producer Consumer Queues

- First implementation:
  - Synchronous
  - Slow
  - Good for debugging

# Synchronous Producer Consumer Queues

- First implementation:
  - Synchronous
  - Slow
  - Good for debugging
- enq does not return until value is deq'ed

# Synchronous Producer Consumer Queues

Producer Thread

enq( 7 );



Consumer Thread

deq( );



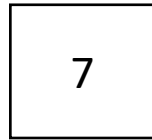
# Synchronous Producer Consumer Queues

Producer Thread

`enq( 7 );`



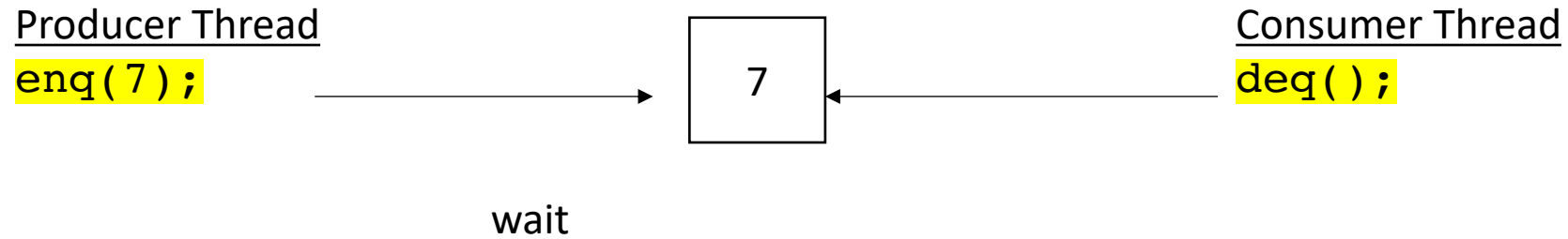
wait



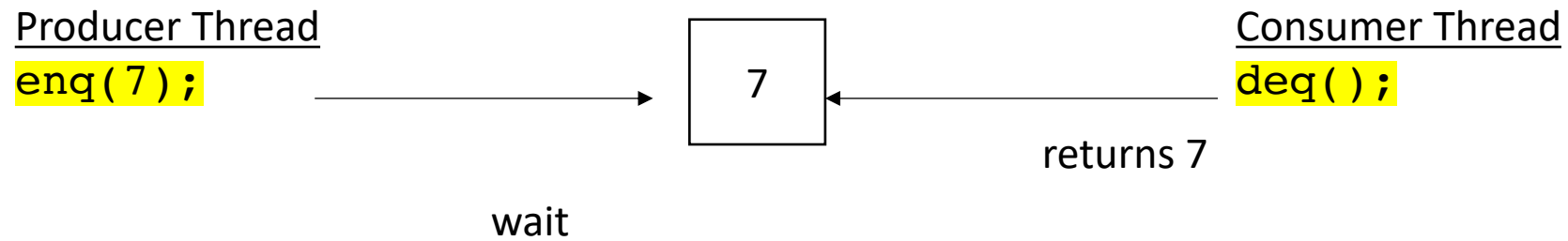
Consumer Thread

`deq( );`

# Synchronous Producer Consumer Queues



# Synchronous Producer Consumer Queues



# Synchronous Producer Consumer Queues

Producer Thread

enq( 7 );



Consumer Thread

deq( );

both can continue

# Synchronous Producer Consumer Queues

Producer Thread

```
sleep();  
enq(7);
```



Consumer Thread

```
deq();
```

# Synchronous Producer Consumer Queues

Producer Thread

`sleep();`

`enq(7);`

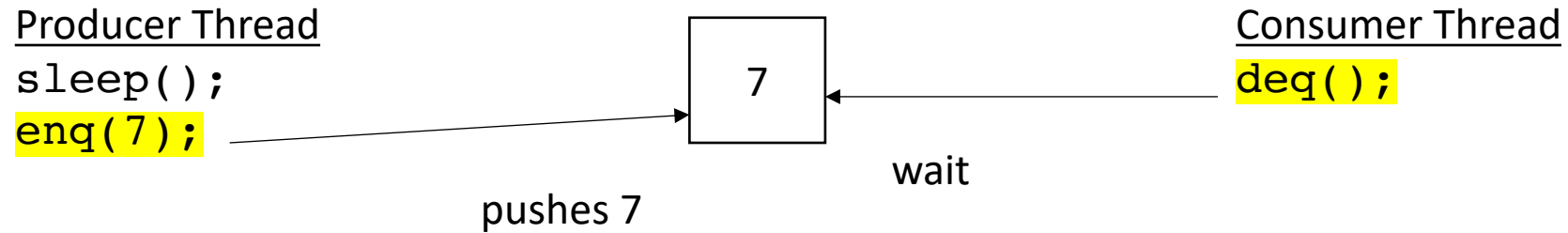


Consumer Thread

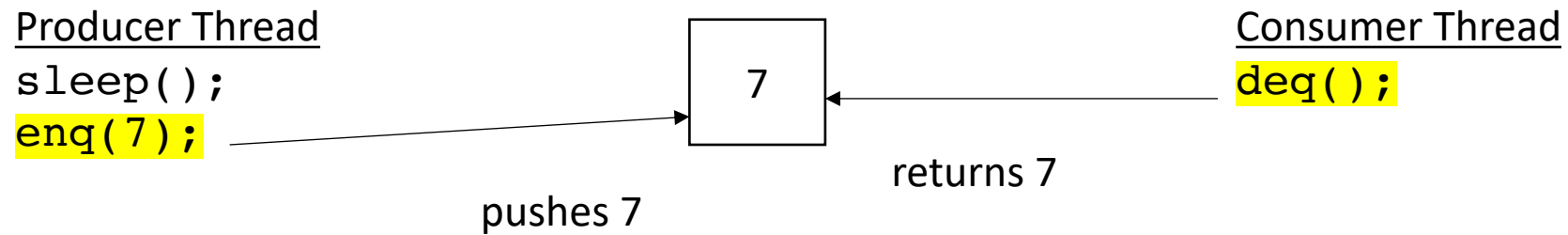
`deq();`

wait

# Synchronous Producer Consumer Queues



# Synchronous Producer Consumer Queues



They both can continue



# Synchronous Producer Consumer Queues

Producer Thread

enq( 7 );



Consumer Thread

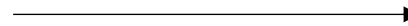
deq( );

# Synchronous Producer Consumer Queues

Producer Thread  
`enq( 7 );`



Consumer Thread  
`deq( );`



*can the consumer just read?*

# Synchronous Producer Consumer Queues

Producer Thread  
`enq( 7 );`



Consumer Thread  
`deq( );`

*can the consumer just read?  
Needs to wait for a value to appear*

# Synchronous Producer Consumer Queues

Producer Thread  
`enq( 7 );`



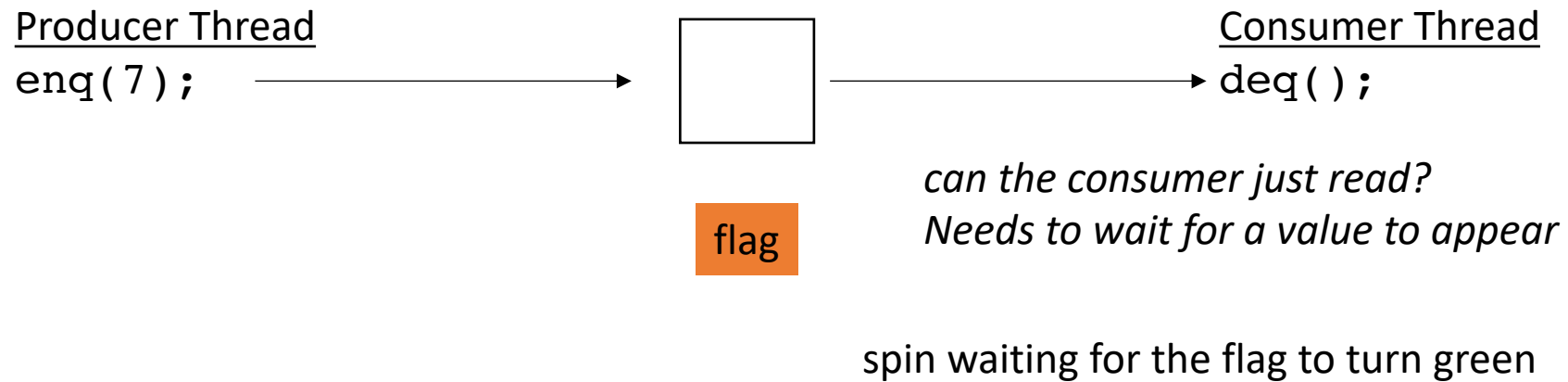
Consumer Thread  
`deq( );`

flag

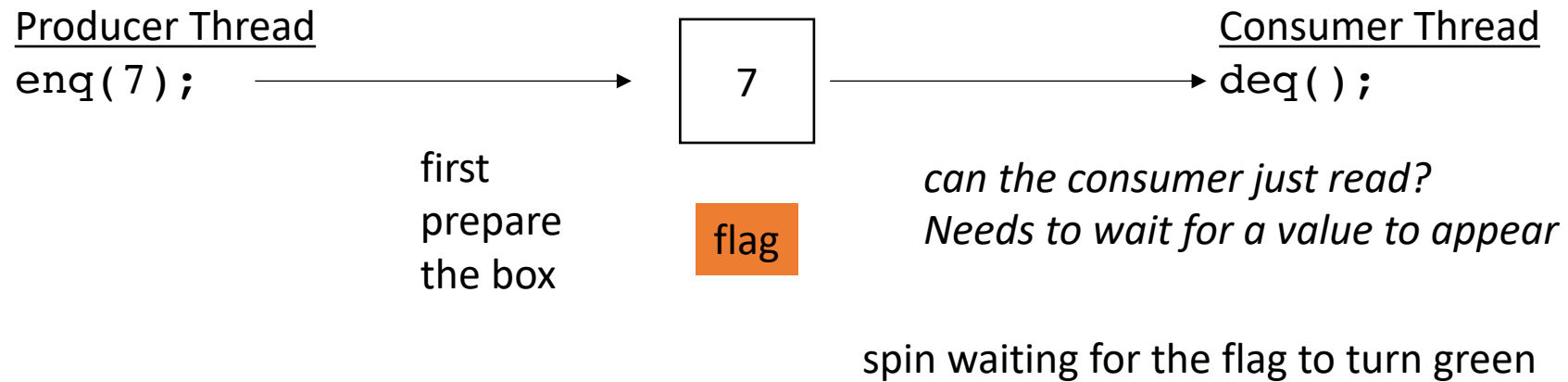
*can the consumer just read?  
Needs to wait for a value to appear*

spin waiting for the flag to turn green

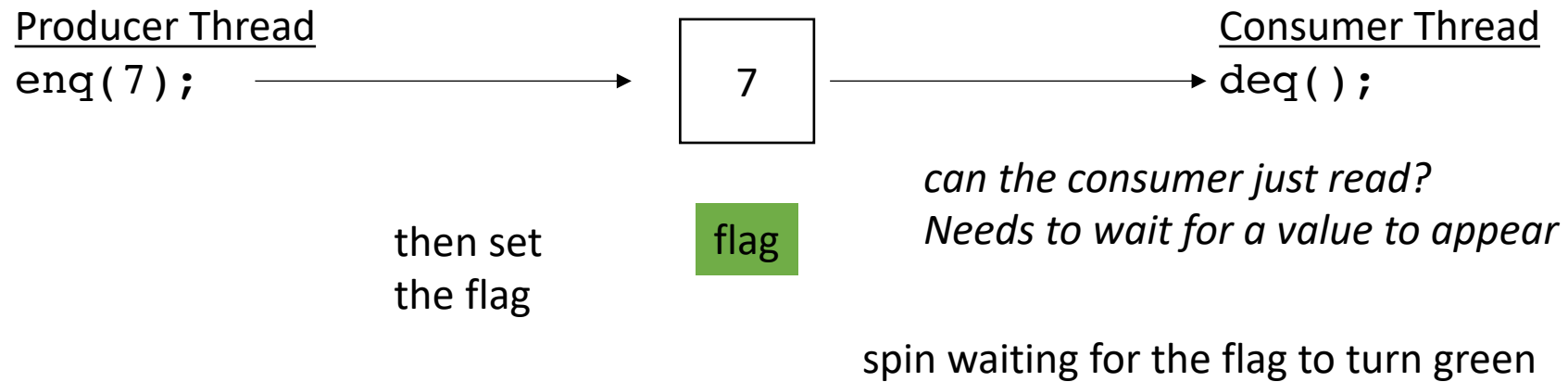
# Synchronous Producer Consumer Queues



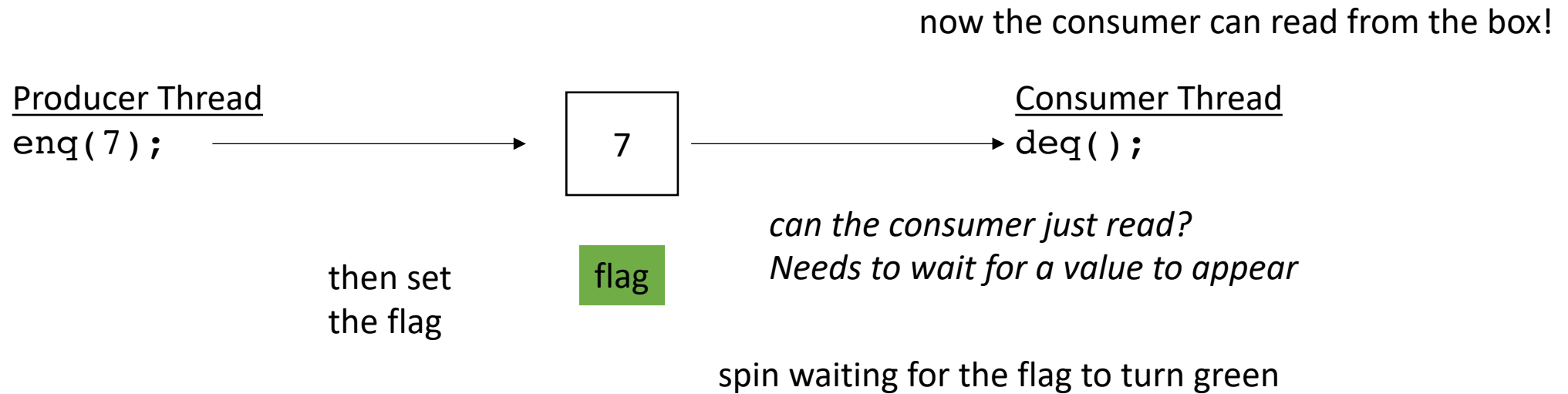
# Synchronous Producer Consumer Queues



# Synchronous Producer Consumer Queues



# Synchronous Producer Consumer Queues





# Synchronous Producer Consumer Queues

Producer Thread

enq(7);



flag

Consumer Thread

deq();

```
class SyncQueue {  
    private:  
        atomic_int box;  
        atomic_bool flag;  
  
    public:  
        void enq(int x) {  
            // put value in box  
            // set flag  
        }  
        void deq() {  
            // wait for flag to be set  
            // read from the box  
        }  
}
```

# Synchronous Producer Consumer Queues

Producer Thread

enq(7);



flag

Consumer Thread

deq();

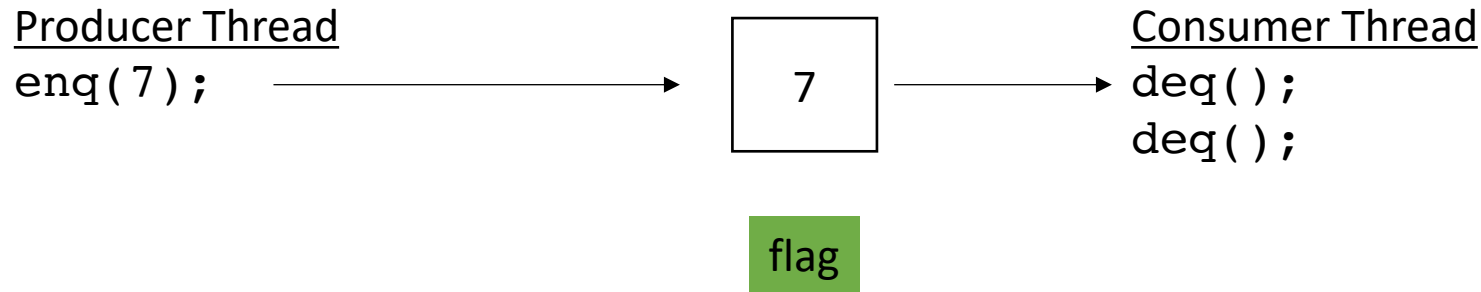
deq();

what happens  
when there are  
two deqs?

```
class SyncQueue {
    private:
        atomic_int box;
        atomic_bool flag;

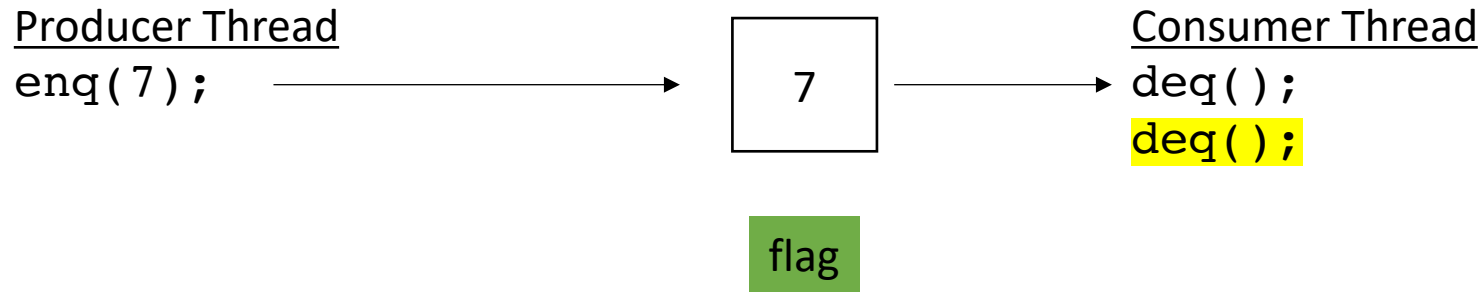
    public:
        void enq(int x) {
            // put value in box
            // set flag
        }
        void deq() {
            // wait for flag to be set
            // read from the box
        }
}
```

# Synchronous Producer Consumer Queues



```
class SyncQueue {  
    private:  
        atomic_int box;  
        atomic_bool flag;  
  
    public:  
        void enq(int x) {  
            // put value in box  
            // set flag  
        }  
        void deq() {  
            // wait for flag to be set  
            // read from the box  
        }  
}
```

# Synchronous Producer Consumer Queues

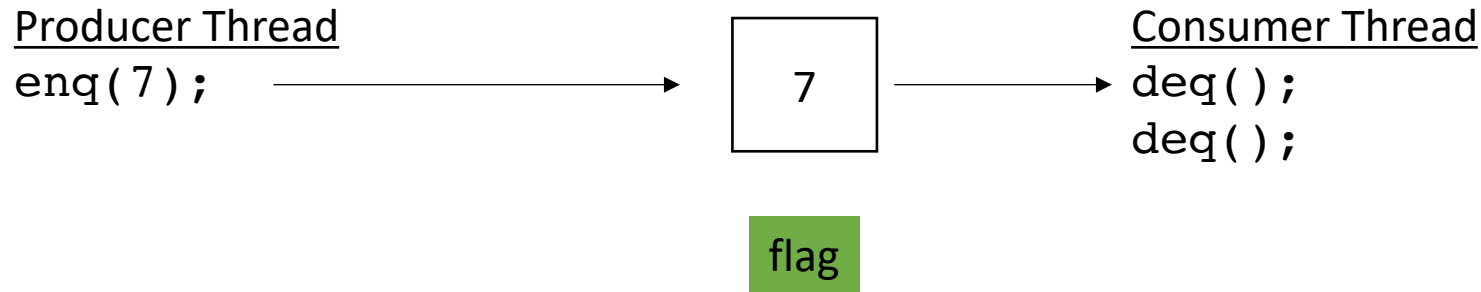


```
class SyncQueue {  
    private:  
        atomic_int box;  
        atomic_bool flag;  
  
    public:  
        void enq(int x) {  
            // put value in box  
            // set flag  
        }  
        void deq() {  
            // wait for flag to be set  
            // read from the box  
        }  
}
```

what happens in the  
next deq?

How to fix?

# Synchronous Producer Consumer Queues

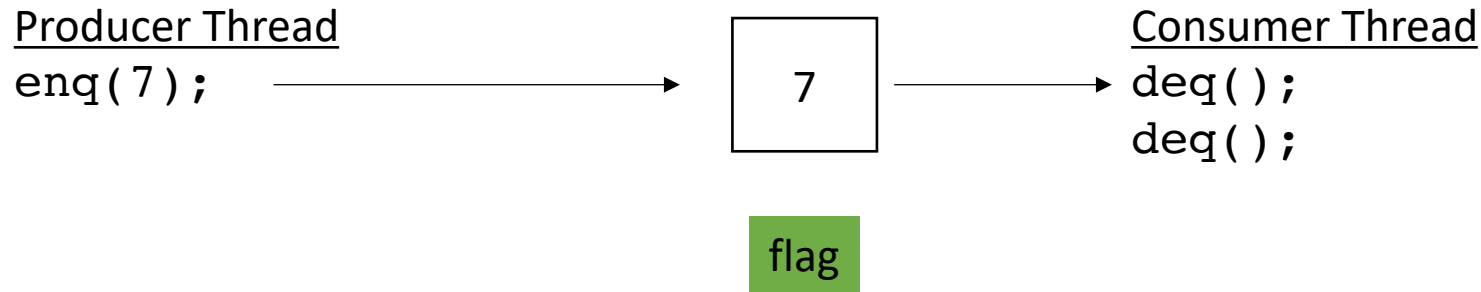


what happens in the  
next `deq`?

How to fix?

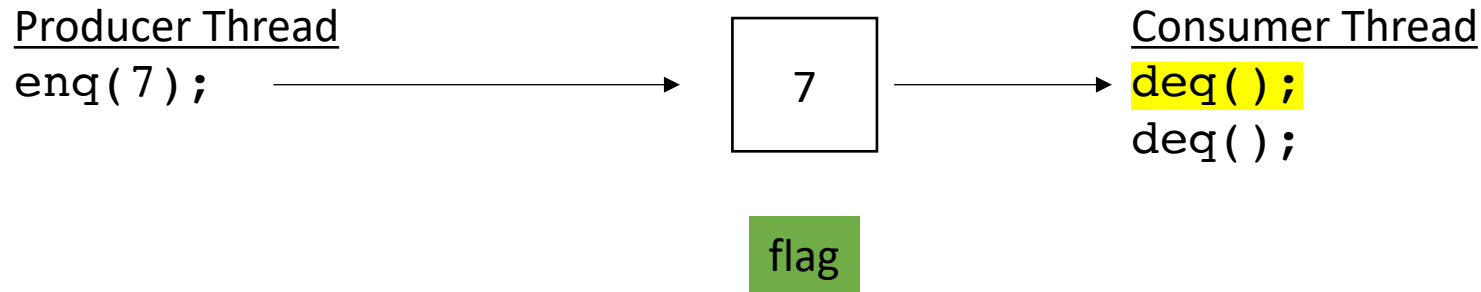
```
class SyncQueue {  
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    public:  
        void enq(int x) {  
            // put value in box  
            // set flag  
        }  
        void deq() {  
            // wait for flag to be set  
            // read from the box  
            // reset flag  
        }  
}
```

# Synchronous Producer Consumer Queues



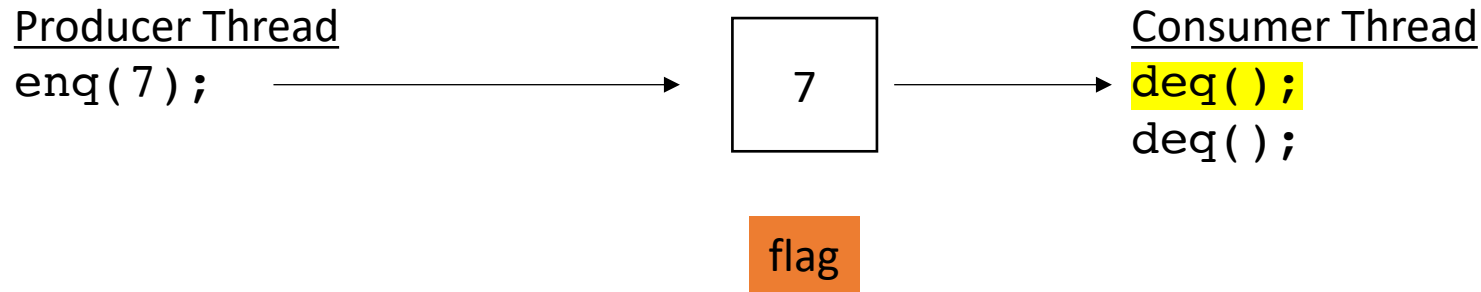
```
class SyncQueue {  
    private:  
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        atomic_bool flag;  
  
    public:  
        void enq(int x) {  
            // put value in box  
            // set flag  
        }  
        void deq() {  
            // wait for flag to be set  
            // read from the box  
            // reset flag  
        }  
}
```

# Synchronous Producer Consumer Queues



```
class SyncQueue {  
    private:  
        atomic_int box;  
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    public:  
        void enq(int x) {  
            // put value in box  
            // set flag  
        }  
        void deq() {  
            // wait for flag to be set  
            // read from the box  
            // reset flag  
        }  
}
```

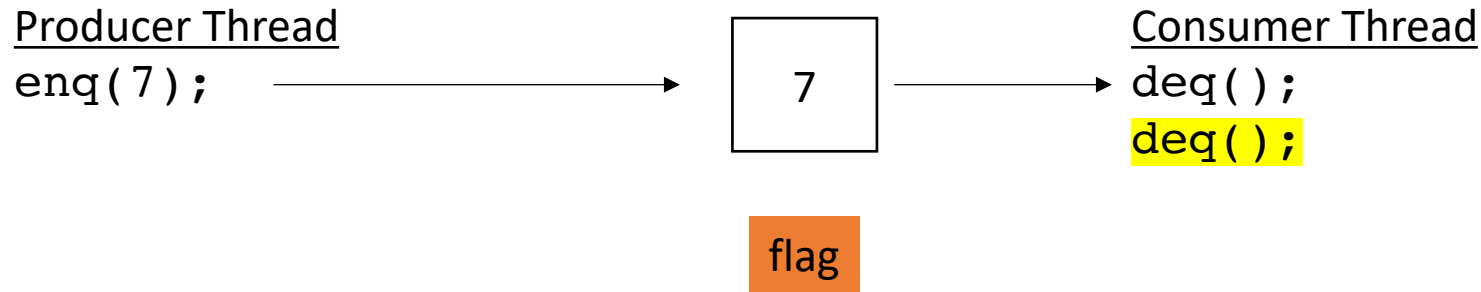
# Synchronous Producer Consumer Queues



```
class SyncQueue {  
    private:  
        atomic_int box;  
        atomic_bool flag;  
  
    public:  
        void enq(int x) {  
            // put value in box  
            // set flag  
        }  
        void deq() {  
            // wait for flag to be set  
            // read from the box  
            // reset flag  
        }  
}
```



# Synchronous Producer Consumer Queues



waiting like we are  
supposed to

```
class SyncQueue {  
    private:  
        atomic_int box;  
        atomic_bool flag;  
  
    public:  
        void enq(int x) {  
            // put value in box  
            // set flag  
        }  
        void deq() {  
            // wait for flag to be set  
            // read from the box  
            // reset flag  
        }  
}
```

# Synchronous Producer Consumer Queues

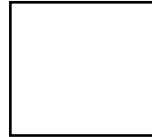
reset (now with extra enq)

Producer Thread

enq(7);

enq(8);

extra enq



flag

Consumer Thread

deq();

deq();

```
class SyncQueue {  
    private:  
        atomic_int box;  
        atomic_bool flag;  
  
    public:  
        void enq(int x) {  
            // put value in box  
            // set flag  
        }  
        void deq() {  
            // wait for flag to be set  
            // read from the box  
            // reset flag  
        }  
}
```

# Synchronous Producer Consumer Queues

Producer Thread

**enq(7);**

enq(8);

7

flag

Consumer Thread

deq();

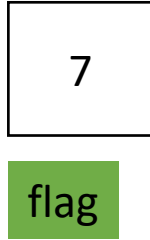
deq();

```
class SyncQueue {  
    private:  
        atomic_int box;  
        atomic_bool flag;  
  
    public:  
        void enq(int x) {  
            // put value in box  
            // set flag  
        }  
        void deq() {  
            // wait for flag to be set  
            // read from the box  
            // reset flag  
        }  
}
```

# Synchronous Producer Consumer Queues

Producer Thread

```
enq(7);  
enq(8);
```



Consumer Thread

```
deq();  
deq();
```

```
class SyncQueue {  
    private:  
        atomic_int box;  
        atomic_bool flag;  
  
    public:  
        void enq(int x) {  
            // put value in box  
            // set flag  
        }  
        void deq() {  
            // wait for flag to be set  
            // read from the box  
            // reset flag  
        }  
}
```

# Synchronous Producer Consumer Queues

Producer Thread

enq(7);

enq(8);

8

flag

Consumer Thread

deq();

deq();

*7 was dropped!*

*how to fix?*

```
class SyncQueue {
private:
    atomic_int box;
    atomic_bool flag;

public:
    void enq(int x) {
        // put value in box
        // set flag
    }
    void deq() {
        // wait for flag to be set
        // read from the box
        // reset flag
    }
}
```

# Synchronous Producer Consumer Queues

Producer Thread

enq(7);

enq(8);

8

flag

Consumer Thread

deq();

deq();

*7 was dropped!*

*how to fix?*

```
class SyncQueue {
    private:
        atomic_int box;
        atomic_bool flag;

    public:
        void enq(int x) {
            // put value in box
            // set flag
            // wait for flag to be reset
        }
        void deq() {
            // wait for flag to be set
            // read from the box
            // reset flag
        }
}
```

# Synchronous Producer Consumer Queues

reset

Producer Thread

enq(7);  
enq(8);



flag

Consumer Thread

deq();  
deq();

```
class SyncQueue {  
    private:  
        atomic_int box;  
        atomic_bool flag;  
  
    public:  
        void enq(int x) {  
            // put value in box  
            // set flag  
            // wait for flag to be reset  
        }  
        void deq() {  
            // wait for flag to be set  
            // read from the box  
            // reset flag  
        }  
}
```

# Synchronous Producer Consumer Queues

Producer Thread

**enq(7);**

enq(8);

7

flag

Consumer Thread

deq();

deq();

```
class SyncQueue {
    private:
        atomic_int box;
        atomic_bool flag;

    public:
        void enq(int x) {
            // put value in box
            // set flag
            // wait for flag to be reset
        }
        void deq() {
            // wait for flag to be set
            // read from the box
            // reset flag
        }
}
```



# Synchronous Producer Consumer Queues

Producer Thread

**enq(7);**

enq(8);

7

flag

Consumer Thread

**deq();**

deq();

```
class SyncQueue {  
    private:  
        atomic_int box;  
        atomic_bool flag;  
  
    public:  
        void enq(int x) {  
            // put value in box  
            // set flag  
            // wait for flag to be reset  
        }  
        void deq() {  
            // wait for flag to be set  
            // read from the box  
            // reset flag  
        }  
}
```

# Synchronous Producer Consumer Queues

Producer Thread

**enq(7);**

enq(8);

7

flag

Consumer Thread

**deq();**

deq();

```
class SyncQueue {
    private:
        atomic_int box;
        atomic_bool flag;

    public:
        void enq(int x) {
            // put value in box
            // set flag
            // wait for flag to be reset
        }
        void deq() {
            // wait for flag to be set
            // read from the box
            // reset flag
        }
}
```

# Synchronous Producer Consumer Queues

Producer Thread

enq(7);  
enq(8);

7

flag

Consumer Thread

deq();  
deq();

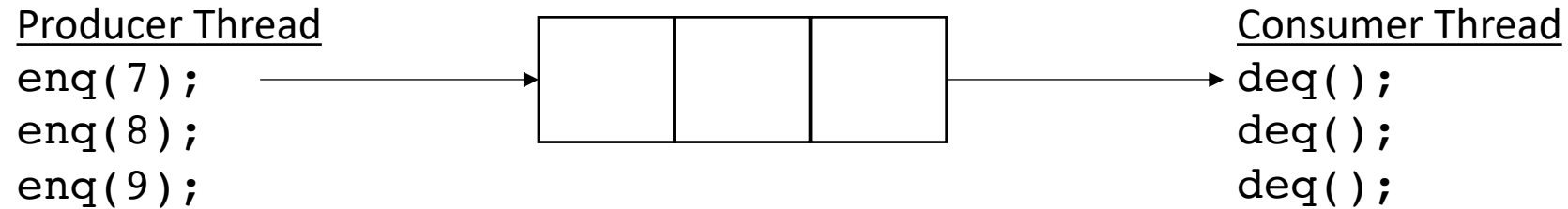
```
class SyncQueue {  
    private:  
        atomic_int box;  
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    public:  
        void enq(int x) {  
            // put value in box  
            // set flag  
            // wait for flag to be reset  
        }  
        void deq() {  
            // wait for flag to be set  
            // read from the box  
            // reset flag  
        }  
}
```

# Schedule

- Finish up linked-list
- **Concurrent Queues**
  - Input/Output Queues
  - Synchronous Producer/Consumer Queue
  - **Async Producer/Consumer Queue**

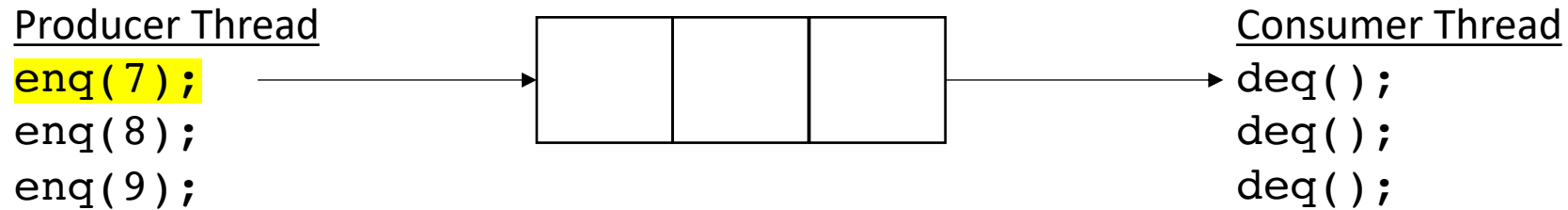
# Producer Consumer Queues

- Asynchronous:



# Producer Consumer Queues

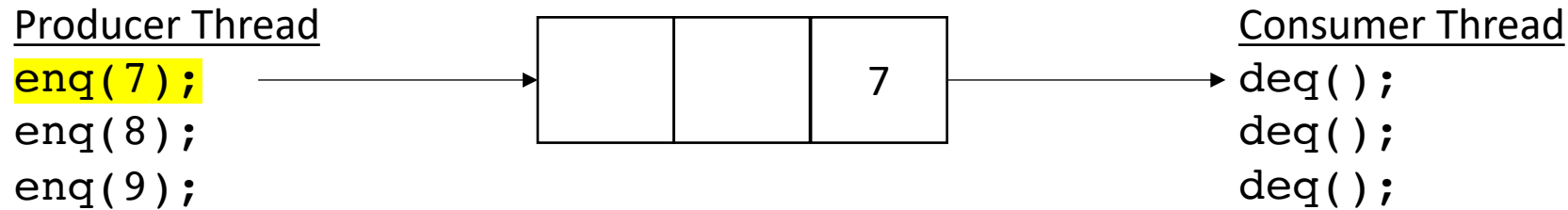
- Asynchronous:



no waiting for producer (while there is room)

# Producer Consumer Queues

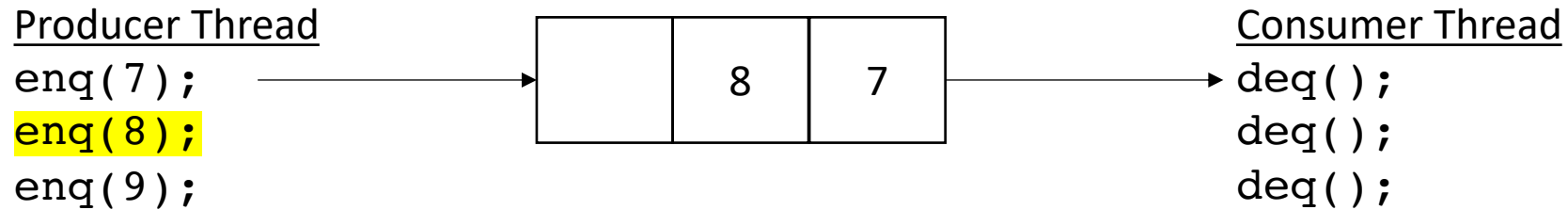
- Asynchronous:



no waiting for producer (while there is room)

# Producer Consumer Queues

- Asynchronous:

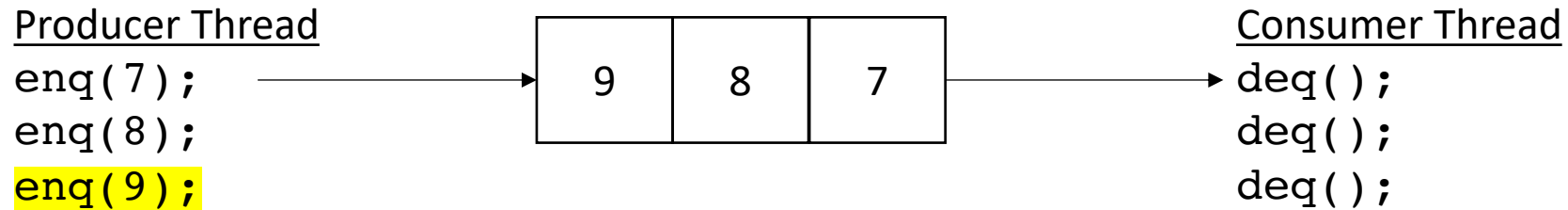


no waiting for producer (while there is room)



# Producer Consumer Queues

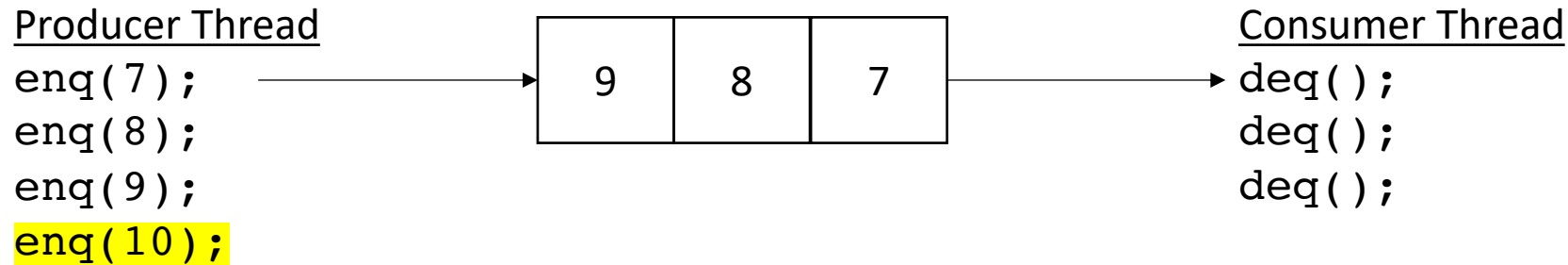
- Asynchronous:



no waiting for producer (while there is room)

# Producer Consumer Queues

- Asynchronous:



no waiting for producer (while there is room)

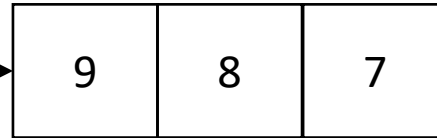
when there is no room, the queue will wait

# Producer Consumer Queues

- Asynchronous:

Producer Thread

```
enq(7);  
enq(8);  
enq(9);  
enq(10);
```



Consumer Thread

```
deq();  
deq();  
deq();
```

no waiting for producer (while there is room)

returns 7

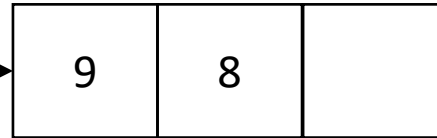
when there is no room, the queue will wait

# Producer Consumer Queues

- Asynchronous:

Producer Thread

```
enq(7);  
enq(8);  
enq(9);  
enq(10);
```



Consumer Thread

```
deq();  
deq();  
deq();
```

no waiting for producer (while there is room)

returns 7

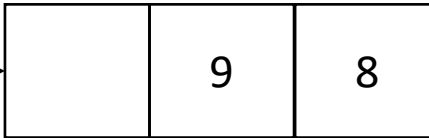
when there is no room, the queue will wait

# Producer Consumer Queues

- Asynchronous:

Producer Thread

```
enq(7);  
enq(8);  
enq(9);  
enq(10);
```



Consumer Thread

```
deq();  
deq();  
deq();
```

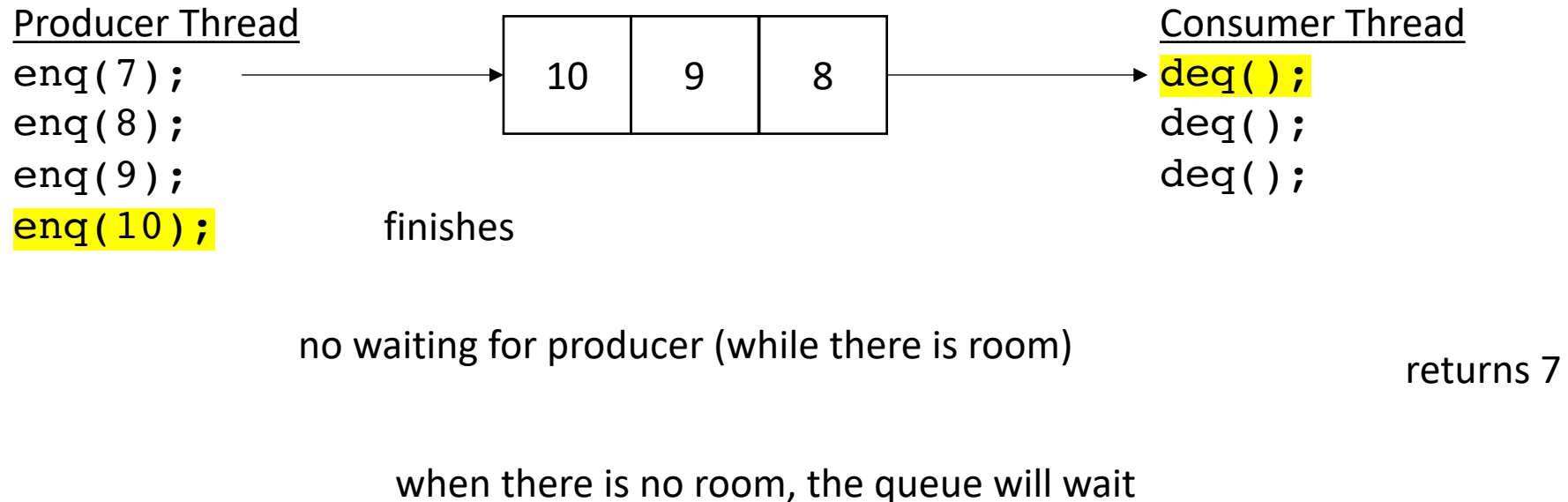
no waiting for producer (while there is room)

returns 7

when there is no room, the queue will wait

# Producer Consumer Queues

- Asynchronous:

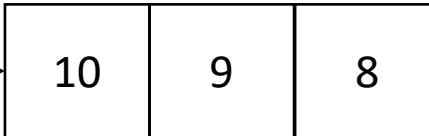


# Producer Consumer Queues

- Asynchronous:

Producer Thread

```
enq(7);  
enq(8);  
enq(9);  
enq(10);
```



Consumer Thread

```
deq();  
deq();  
deq();
```

no waiting for producer (while there is room)

returns 7

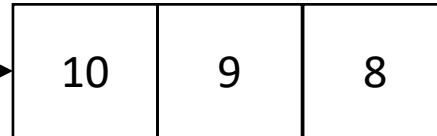
when there is no room, the queue will wait

# Producer Consumer Queues

- Asynchronous:

Producer Thread

```
enq(7);  
enq(8);  
enq(9);  
enq(10);
```



Consumer Thread

```
deq();  
deq();  
deq();
```

no waiting for producer (while there is room)

returns 8

when there is no room, the queue will wait

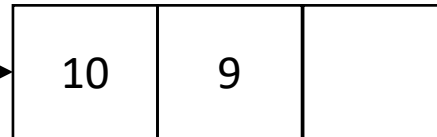


# Producer Consumer Queues

- Asynchronous:

Producer Thread

```
enq(7);  
enq(8);  
enq(9);  
enq(10);
```



Consumer Thread

```
deq();  
deq();  
deq();
```

no waiting for producer (while there is room)

returns 8

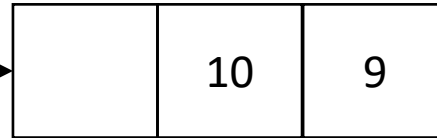
when there is no room, the queue will wait

# Producer Consumer Queues

- Asynchronous:

Producer Thread

```
enq(7);  
enq(8);  
enq(9);  
enq(10);
```



Consumer Thread

```
deq( );  
deq( );  
deq( );
```

no waiting for producer (while there is room)

returns 8

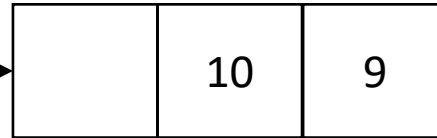
when there is no room, the queue will wait

# Producer Consumer Queues

- Asynchronous:

Producer Thread

```
enq(7);  
enq(8);  
enq(9);  
enq(10);
```



Consumer Thread

```
deq();  
deq();  
deq();
```

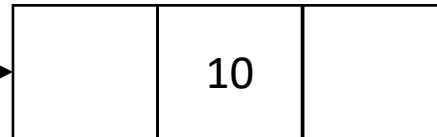
returns 9

# Producer Consumer Queues

- Asynchronous:

Producer Thread

enq( 7 );  
enq( 8 );  
enq( 9 );  
enq( 10 );

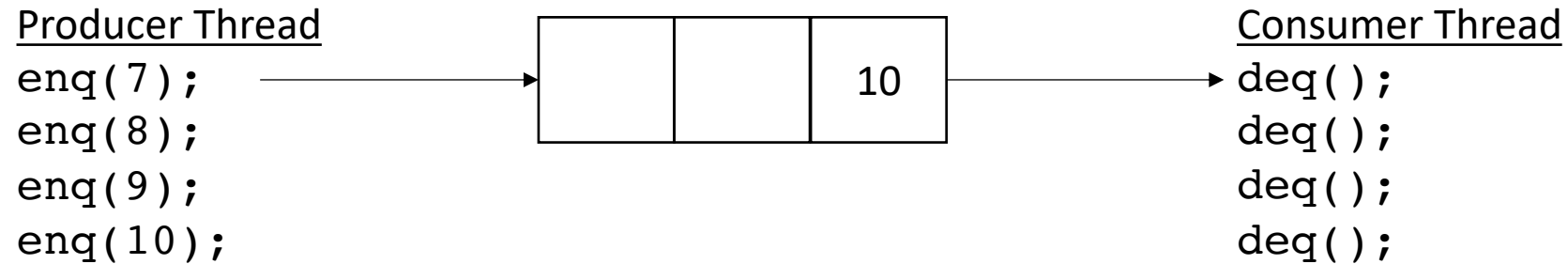


Consumer Thread

deq( );  
deq( );  
deq( );

# Producer Consumer Queues

- Asynchronous:



# Producer Consumer Queues

- Asynchronous:

Producer Thread

enq( 7 );  
enq( 8 );  
enq( 9 );  
enq( 10 );



Consumer Thread

deq( ) ;  
deq( ) ;  
deq( ) ;  
deq( ) ;

# Producer Consumer Queues

- Asynchronous:

Producer Thread

```
enq( 7 );  
enq( 8 );  
enq( 9 );  
enq(10 );
```



Consumer Thread

```
deq( ) ;  
deq( ) ;  
deq( ) ;  
deq( ) ;  
deq( ) ;
```

blocks when there is nothing in the queue

# Producer Consumer Queues

- How do we implement it?



# Producer Consumer Queues

- Start with a fixed size array



# Producer Consumer Queues

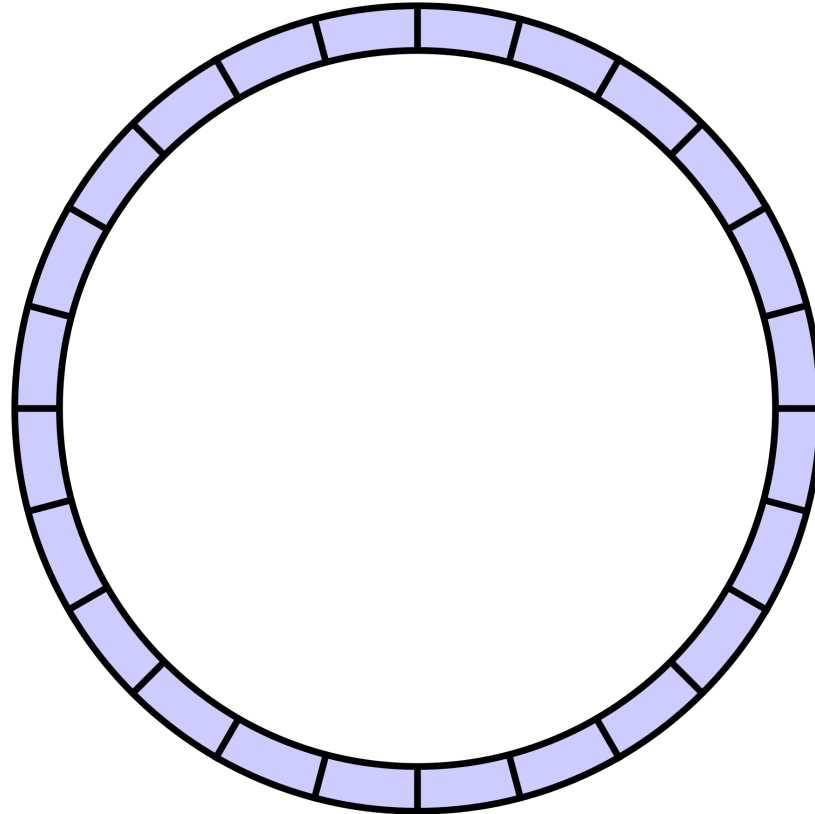
- Start with a fixed size array



We will use what is called a *circular buffer method*

# Producer Consumer Queues

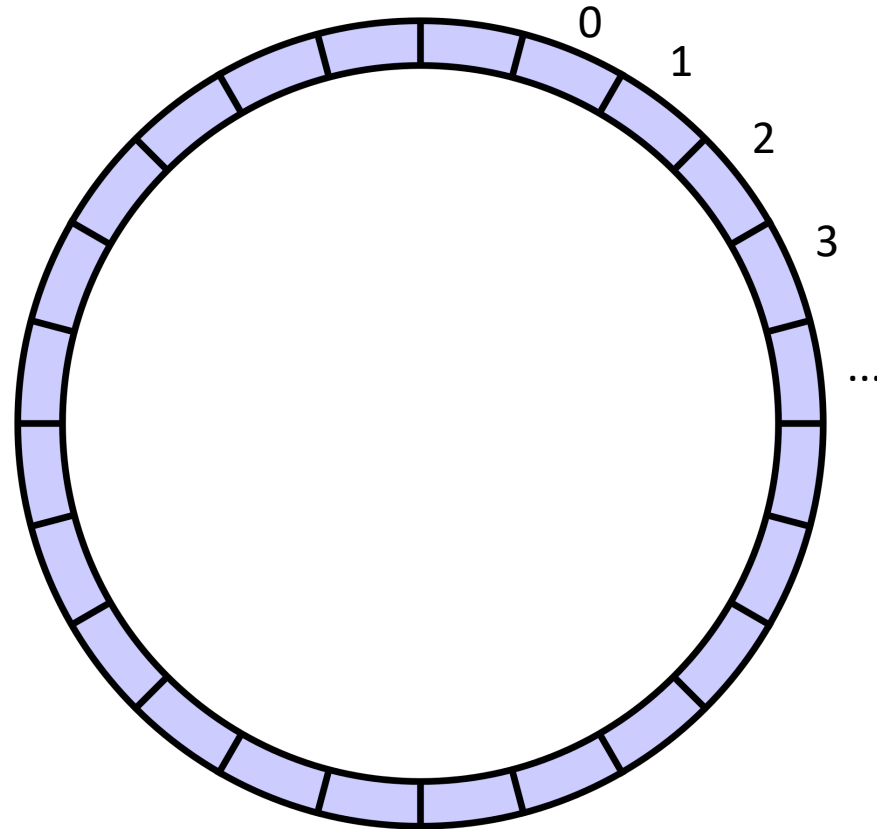
- Start with a fixed size array



conceptually it is a circle

# Producer Consumer Queues

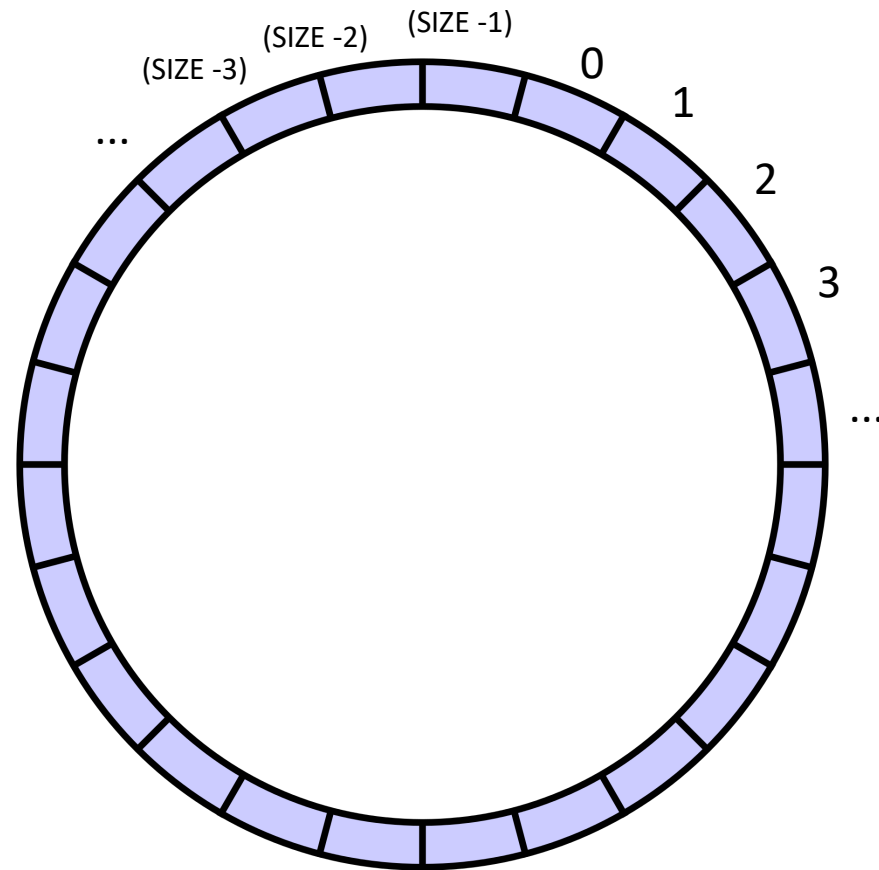
- Start with a fixed size array



conceptually it is a circle

# Producer Consumer Queues

- Start with a fixed size array



indexes will  
circulate in  
order and  
wrap around

conceptually it is a circle

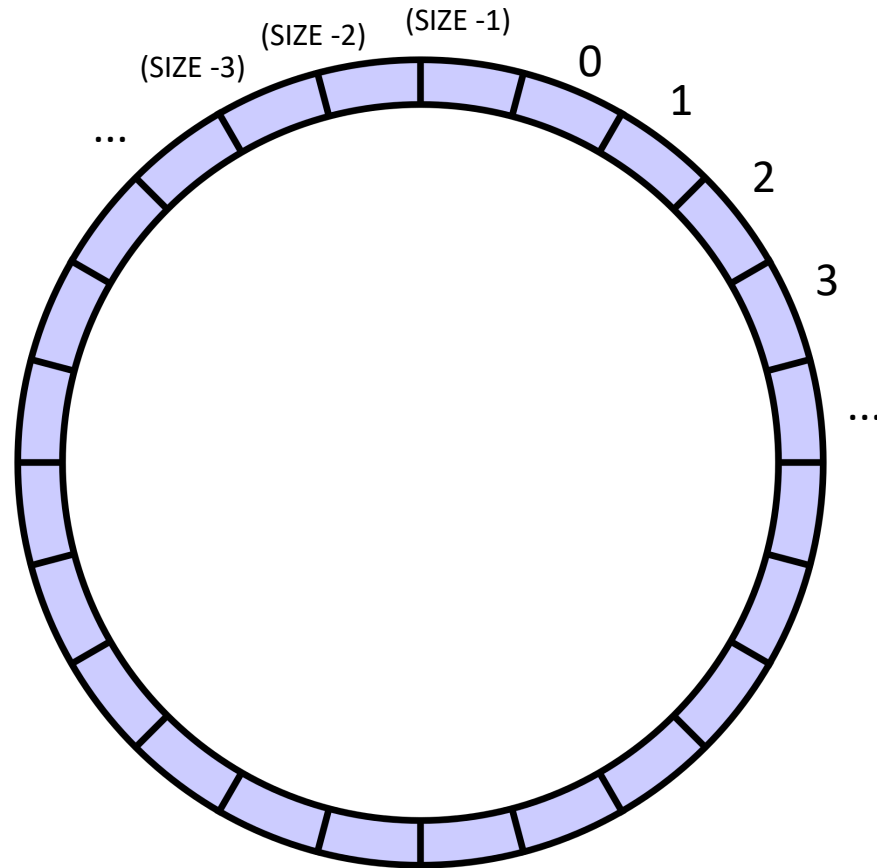
# Producer Consumer Queues

- Start with a fixed size array

we will assume modular arithmetic:

if  $x = (\text{SIZE} - 1)$  then  
 $x + 1 == 0$ ;

conceptually it is a circle



indexes will  
circulate in  
order and  
wrap around

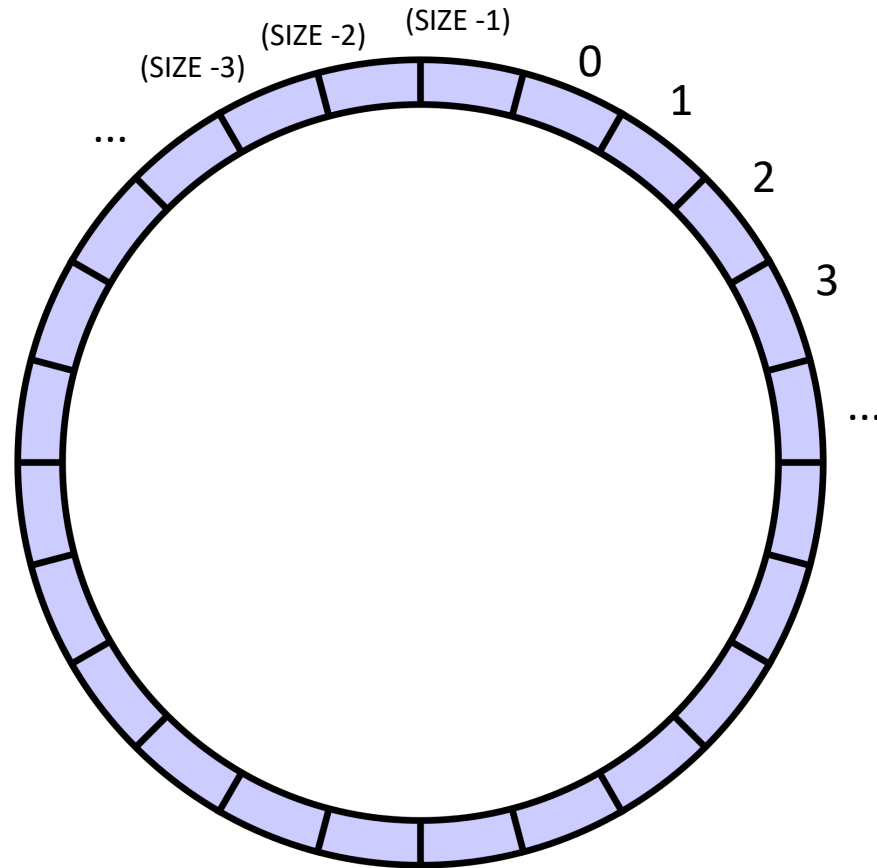
# Producer Consumer Queues

- Start with a fixed size array

Two variables to keep track of  
where to deq and enq:

head and tail

conceptually it is a circle



indexes will  
circulate in  
order and  
wrap around

# Producer Consumer Queues

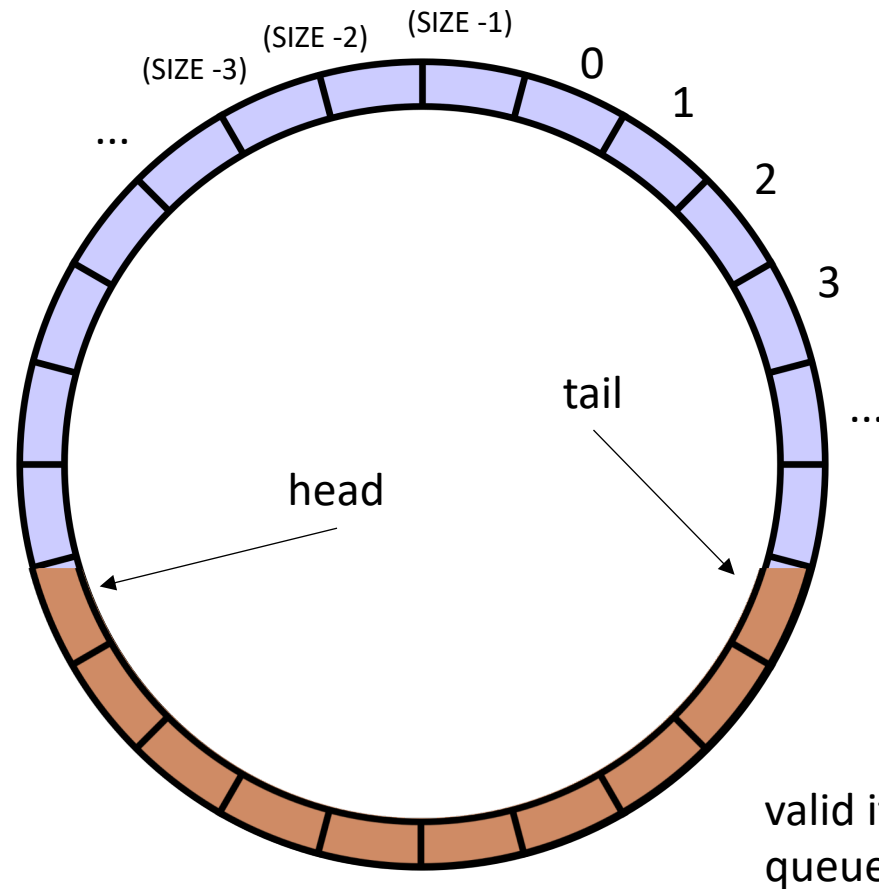
- Start with a fixed size array

Two variables to keep track of where to deq and enq:

head and tail:

enq to the head, deq from the tail

conceptually it is a circle



indexes will circulate in order and wrap around



# Producer Consumer Queues

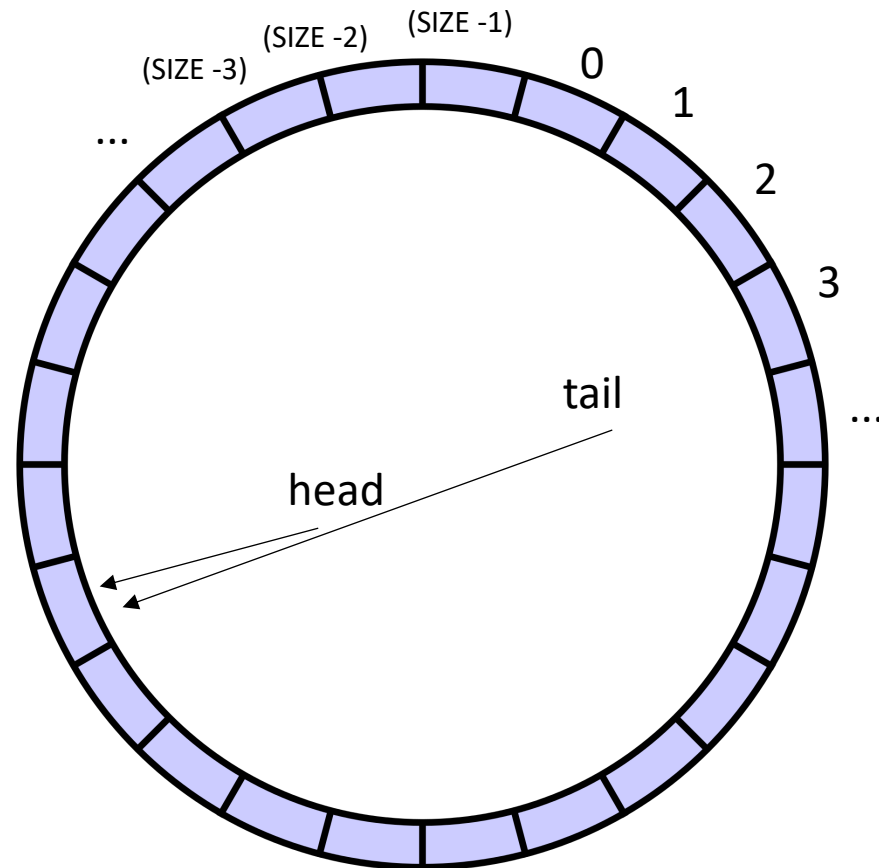
- Start with a fixed size array

Two variables to keep track of  
where to deq and enq:

head and tail

Empty queue is when  
 $\text{head} == \text{tail}$

conceptually it is a circle



indexes will  
circulate in  
order and  
wrap around

# Producer Consumer Queues

- Start with a fixed size array

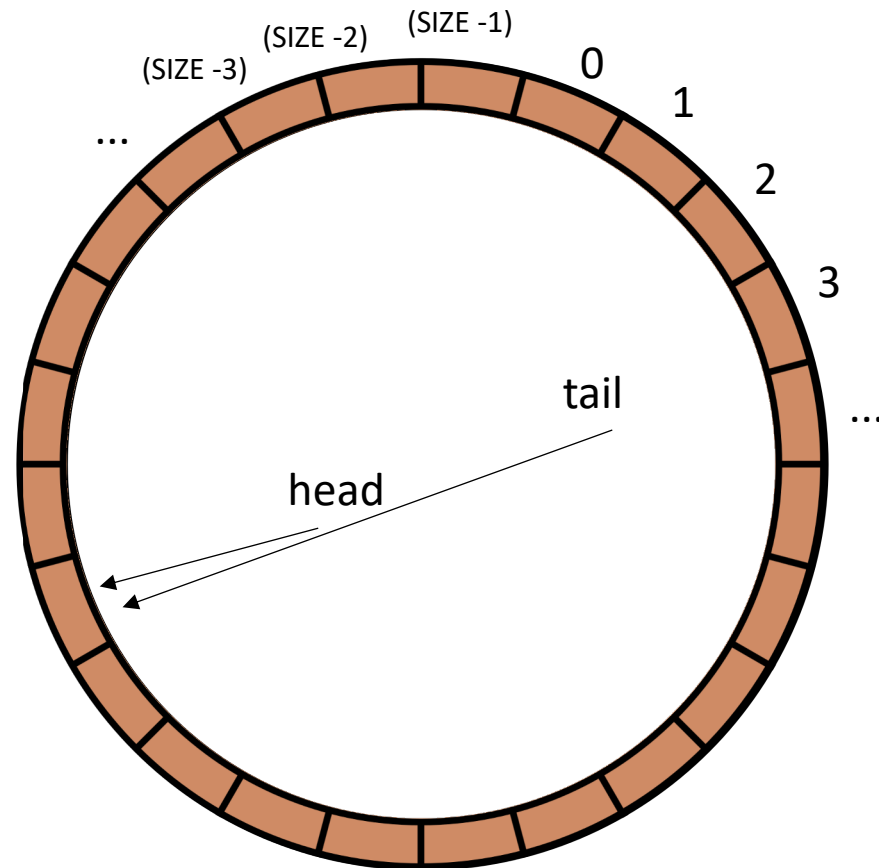
Two variables to keep track of where to deq and enq:

head and tail

Empty queue is when  
 $\text{head} == \text{tail}$

Full queue is when  
 $\text{head} == \text{tail}?$

conceptually it is a circle



indexes will  
circulate in  
order and  
wrap around

# Producer Consumer Queues

- Start with a fixed size array

Two variables to keep track of where to deq and enq:

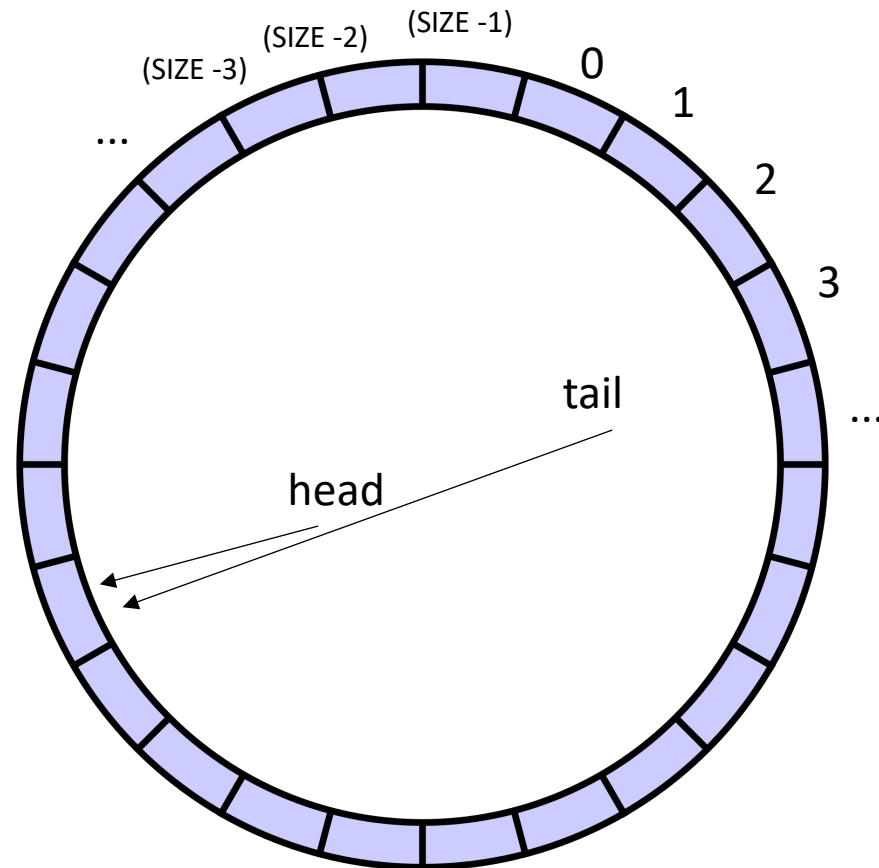
head and tail

Empty queue is when  
 $\text{head} == \text{tail}$

Full queue is when  
 $\text{head} == \text{tail}?$

conceptually it is a circle

but then  
how to tell  
full queue from  
empty?



indexes will  
circulate in  
order and  
wrap around

# Producer Consumer Queues

- Start with a fixed size array

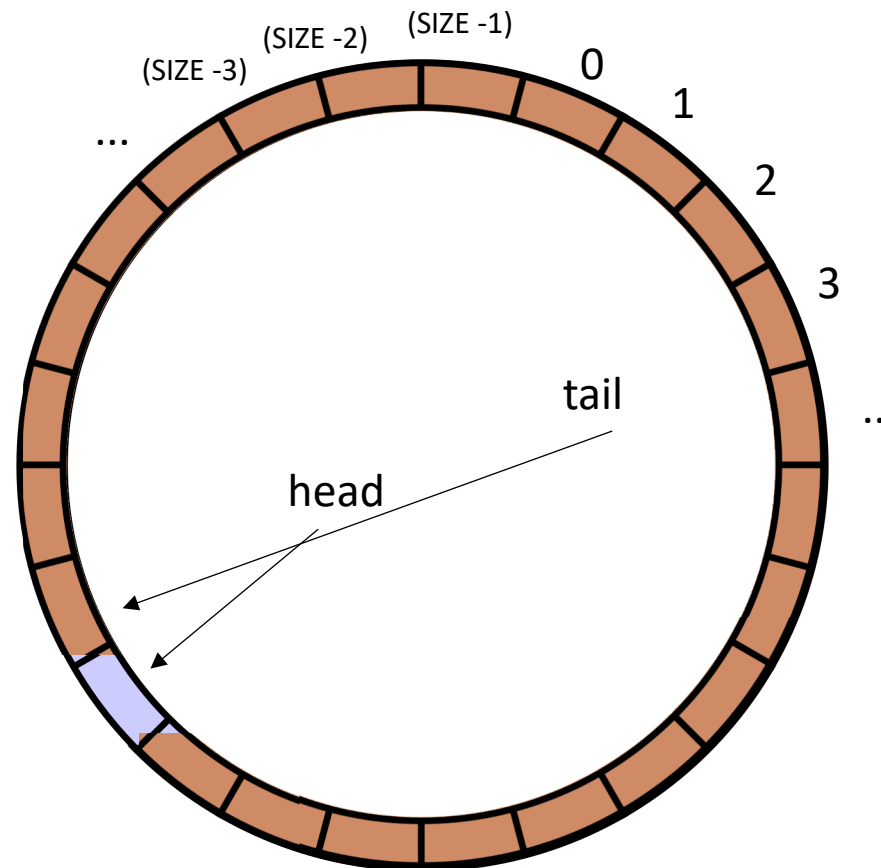
Two variables to keep track of where to deq and enq:

head and tail

Empty queue is when  
 $\text{head} == \text{tail}$

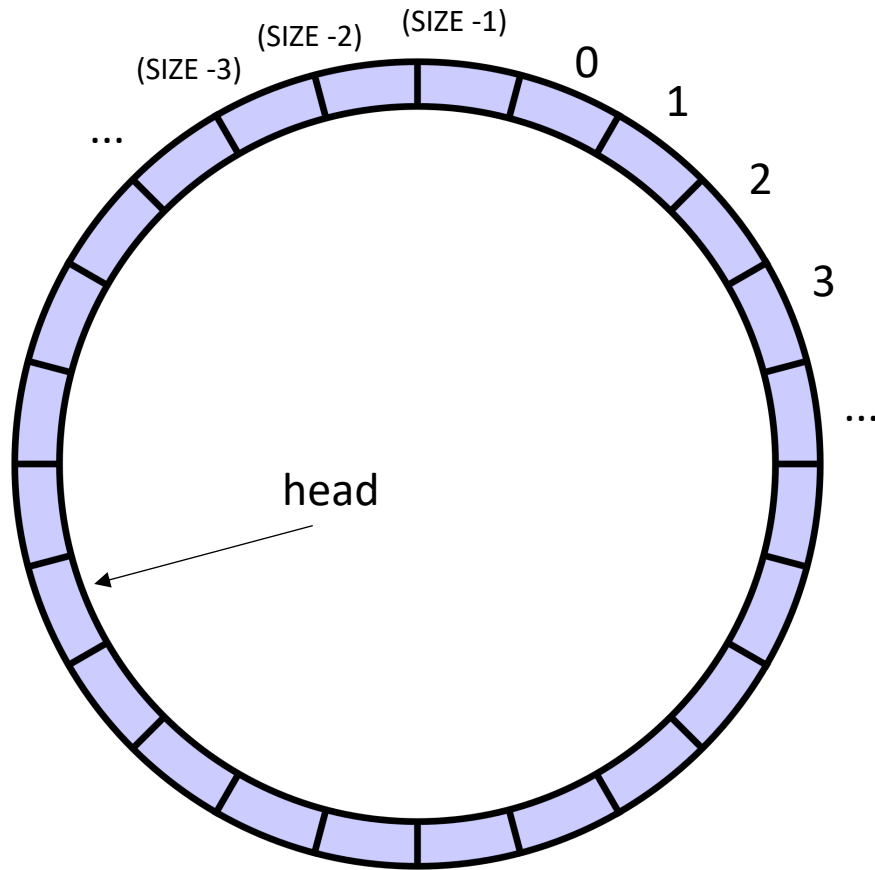
Full queue is when  
 $\text{head} + 1 == \text{tail}$

conceptually it is a circle

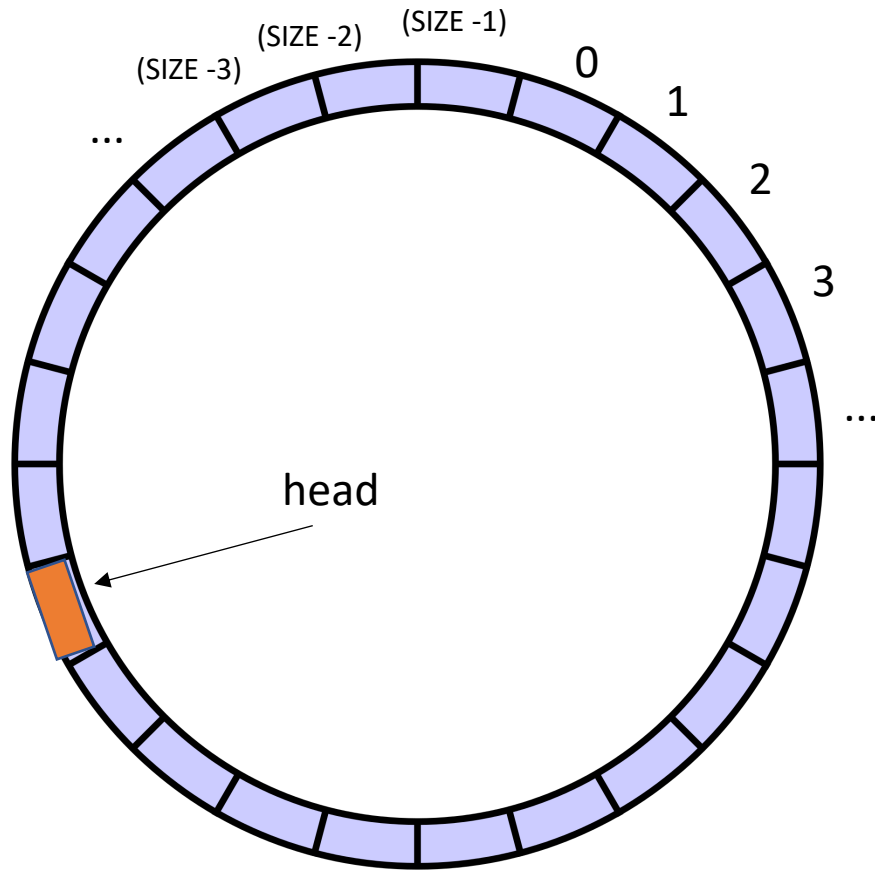


indexes will circulate in order and wrap around

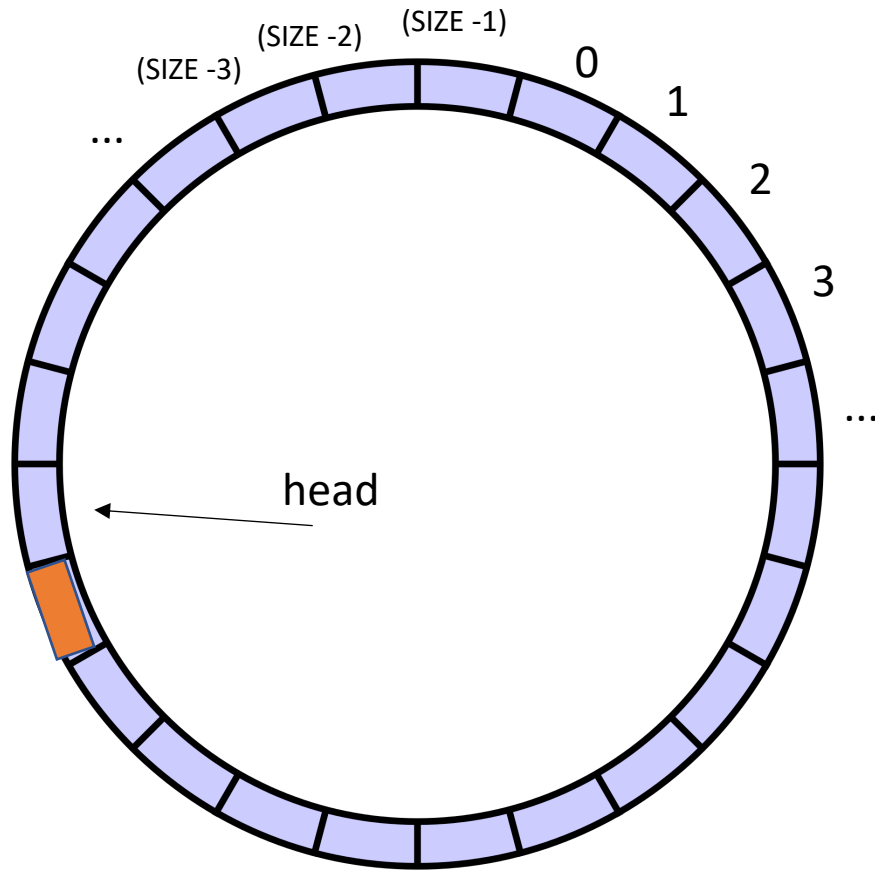
wasting one location, but its okay...



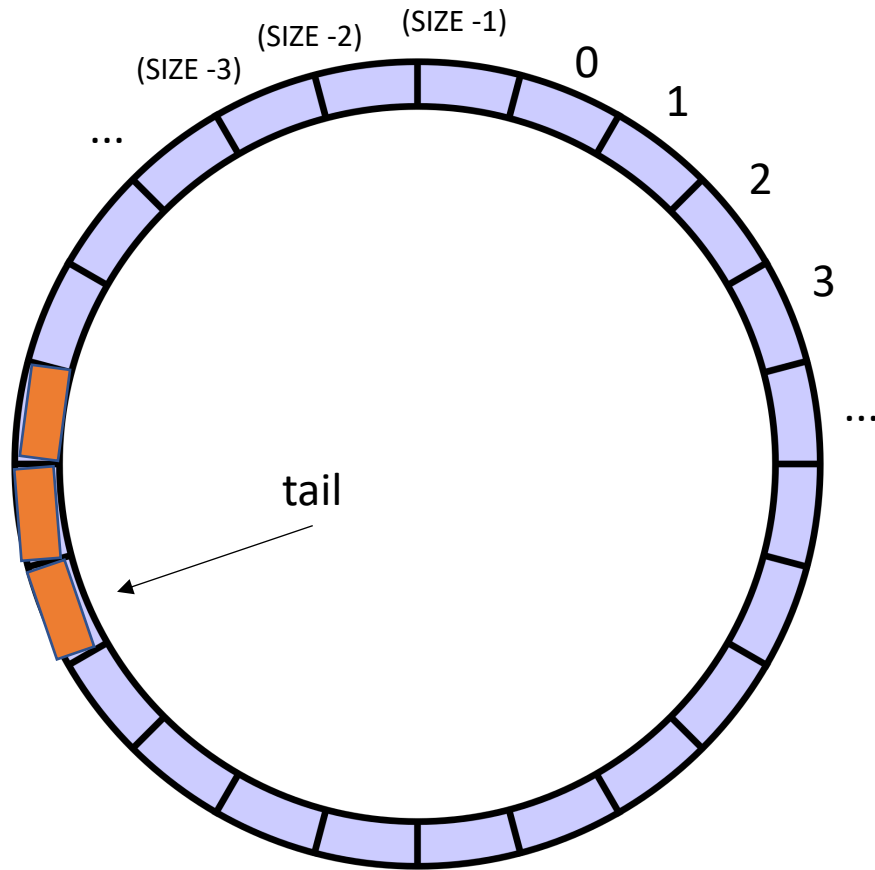
```
class ProdConsQueue {  
    private:  
        atomic_int head;  
        atomic_int tail;  
        int buffer[SIZE];  
  
    public:  
        void enq(int x) {  
            // store value at head  
            // increment head  
        }  
}
```



```
class ProdConsQueue {  
    private:  
        atomic_int head;  
        atomic_int tail;  
        int buffer[SIZE];  
  
    public:  
        void enq(int x) {  
            // store value at head  
            // increment head  
        }  
}
```

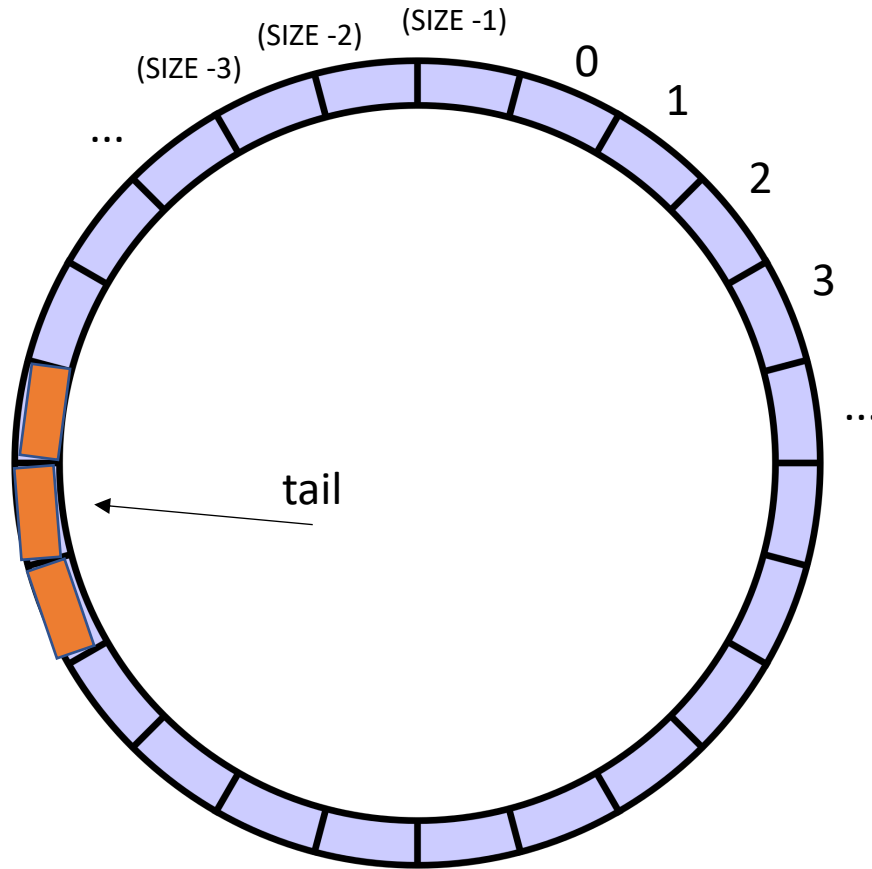


```
class ProdConsQueue {  
    private:  
        atomic_int head;  
        atomic_int tail;  
        int buffer[SIZE];  
  
    public:  
        void enq(int x) {  
            // store value at head  
            // increment head  
        }  
}
```



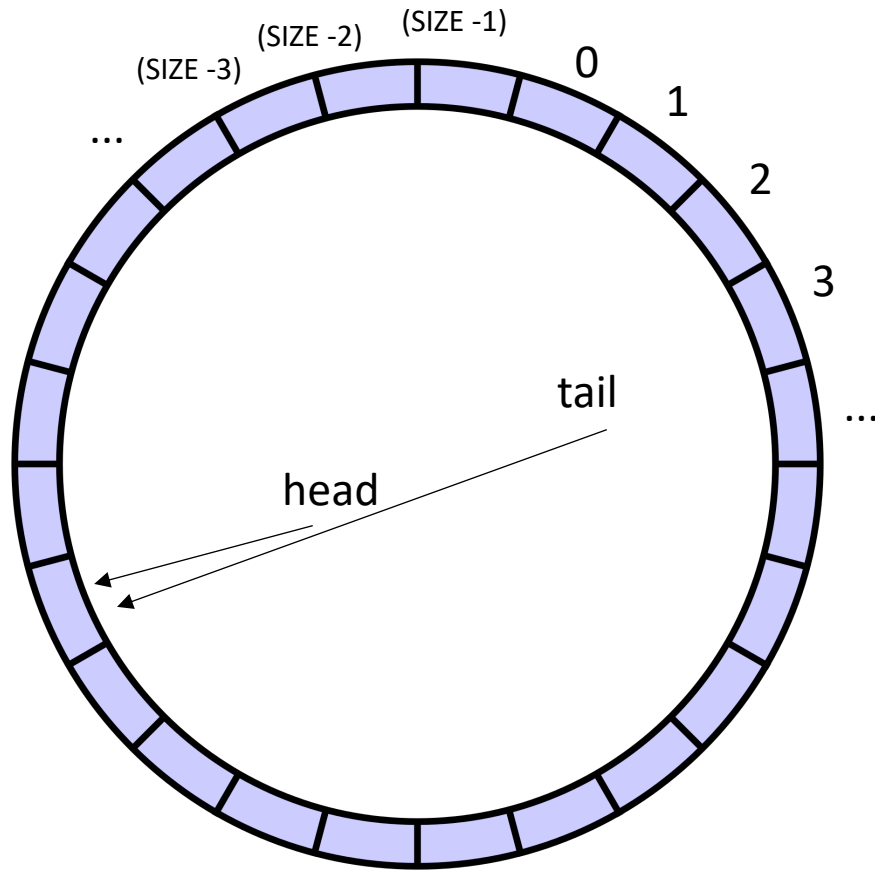
```
class ProdConsQueue {  
    private:  
        atomic_int head;  
        atomic_int tail;  
        int buffer[SIZE];  
  
    public:  
        void enq(int x) {  
            // store value at head  
            // increment head  
        }  
        int deq() {  
            // get value at tail  
            // increment tail  
        }  
}
```





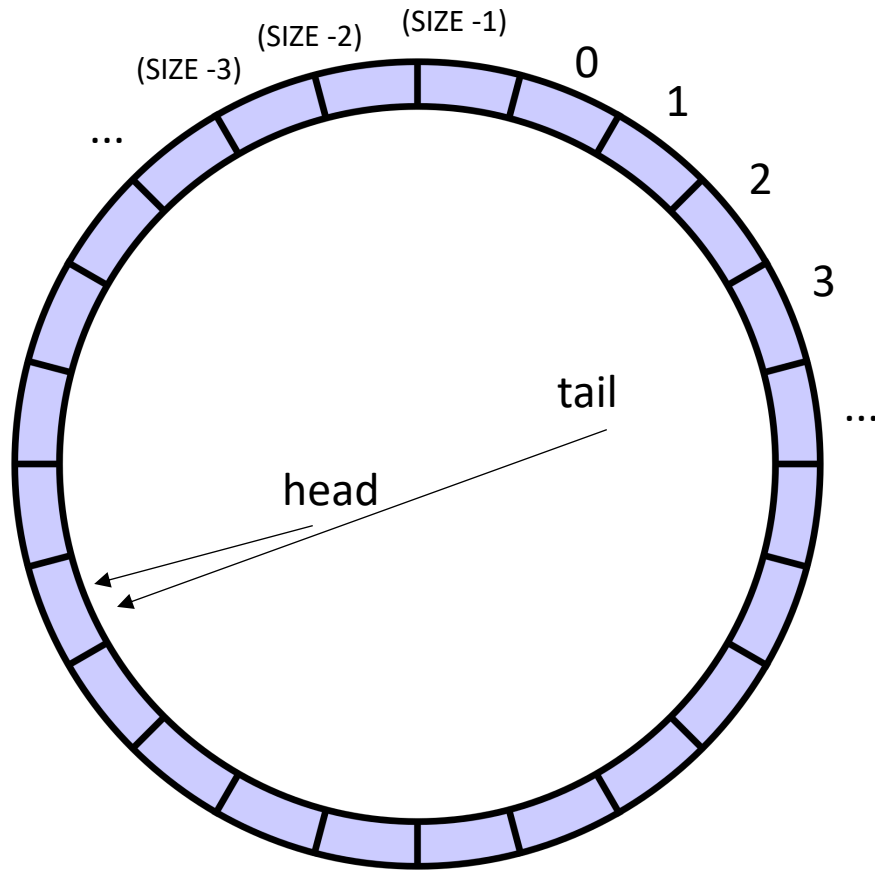
```
class ProdConsQueue {  
    private:  
        atomic_int head;  
        atomic_int tail;  
        int buffer[SIZE];  
  
    public:  
        void enq(int x) {  
            // store value at head  
            // increment head  
        }  
        int deq() {  
            // get value at tail  
            // increment tail  
        }  
}
```

This looks like the two threads don't even share head and tail! What is missing?

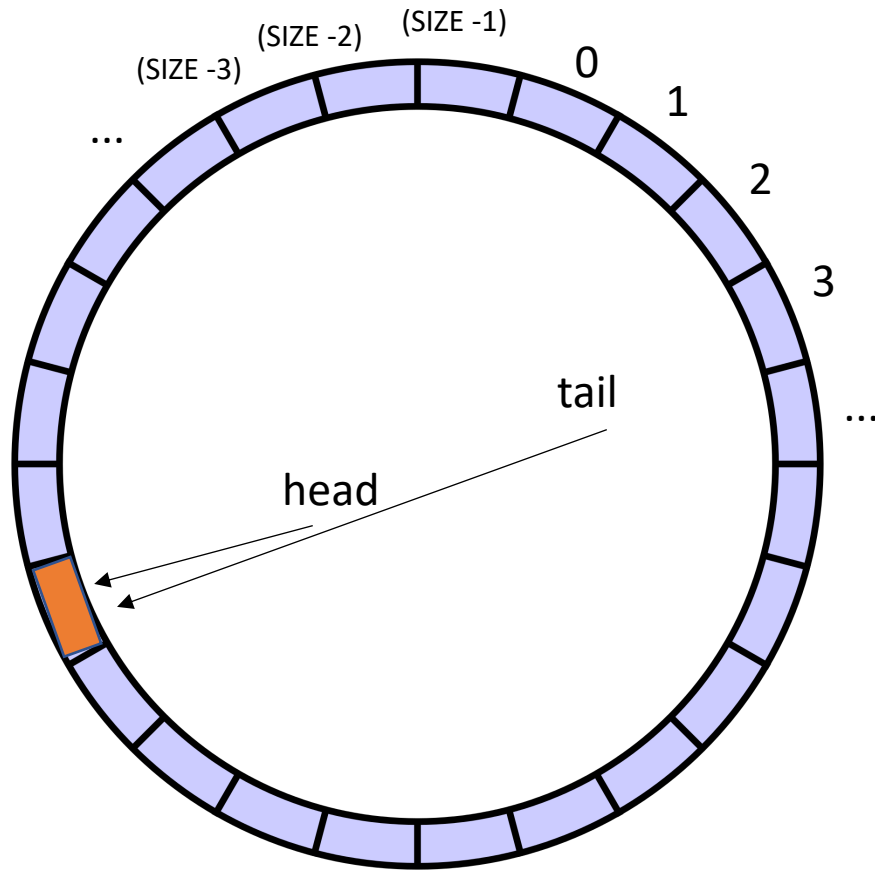


```
class ProdConsQueue {  
    private:  
        atomic_int head;  
        atomic_int tail;  
        int buffer[SIZE];  
  
    public:  
        void enq(int x) {  
            // store value at head  
            // increment head  
        }  
        int deq() {  
            // get value at tail  
            // increment tail  
        }  
}
```

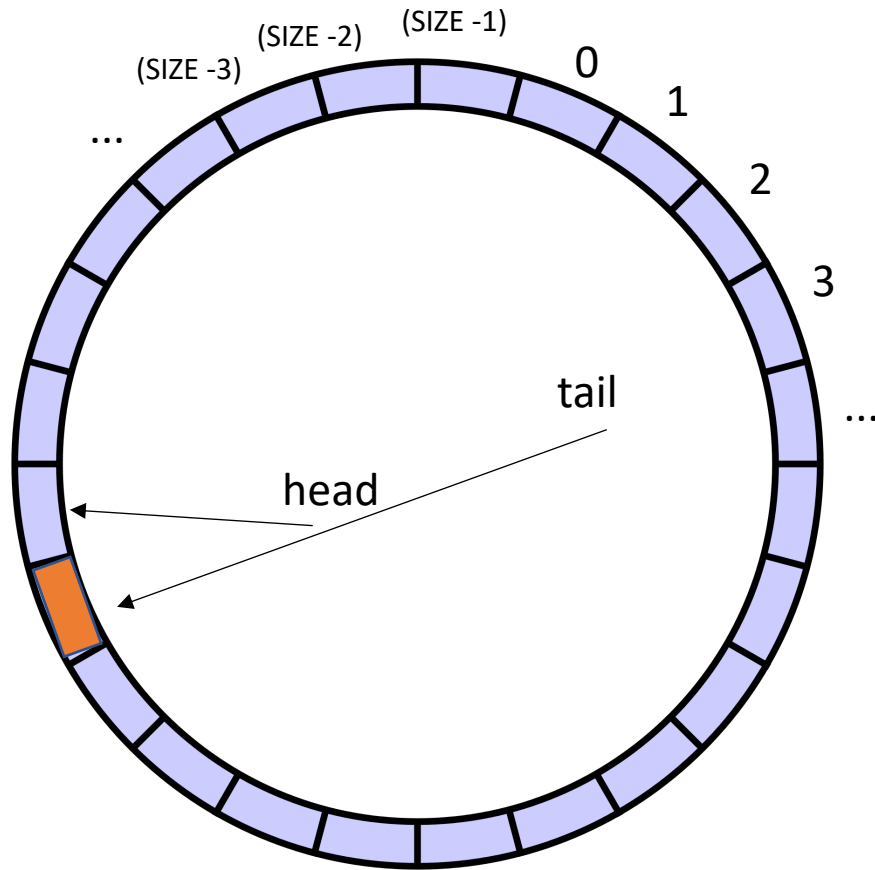
what happens if we try to dequeue here?



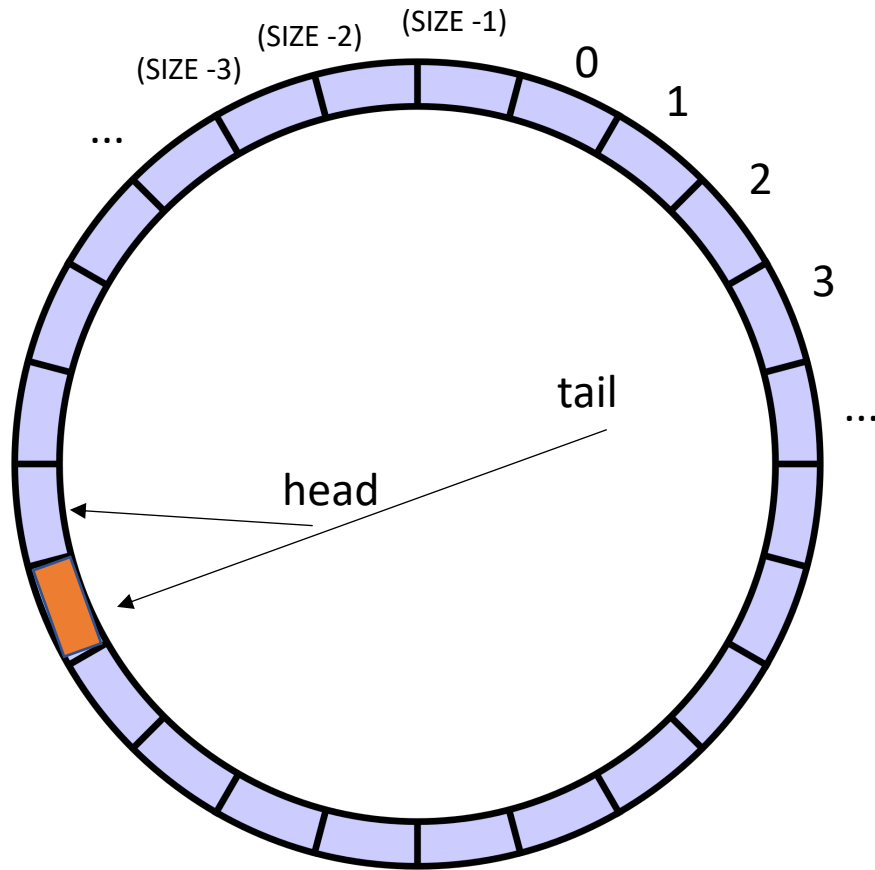
```
class ProdConsQueue {  
    private:  
        atomic_int head;  
        atomic_int tail;  
        int buffer[SIZE];  
  
    public:  
        void enq(int x) {  
            // store value at head  
            // increment head  
        }  
        int deq() {  
            // wait while queue is not empty  
            // get value at tail  
            // increment tail  
        }  
}
```



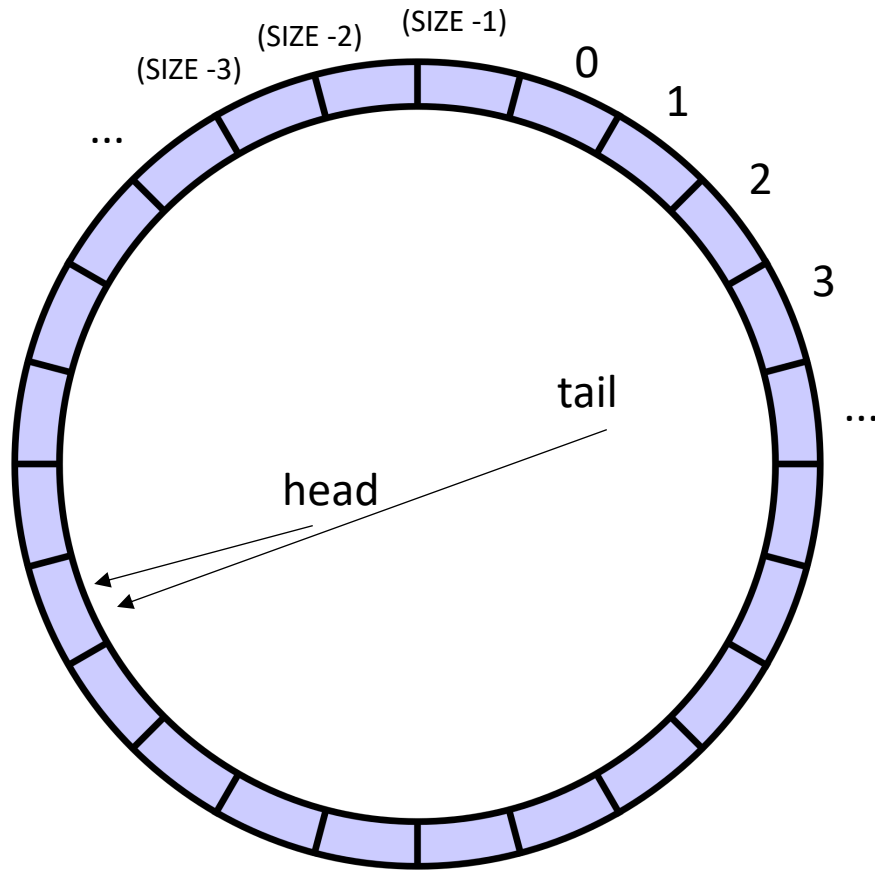
```
class ProdConsQueue {  
    private:  
        atomic_int head;  
        atomic_int tail;  
        int buffer[SIZE];  
  
    public:  
        void enq(int x) {  
            // store value at head  
            // increment head  
        }  
        int deq() {  
            // wait while queue is not empty  
            // get value at tail  
            // increment tail  
        }  
}
```



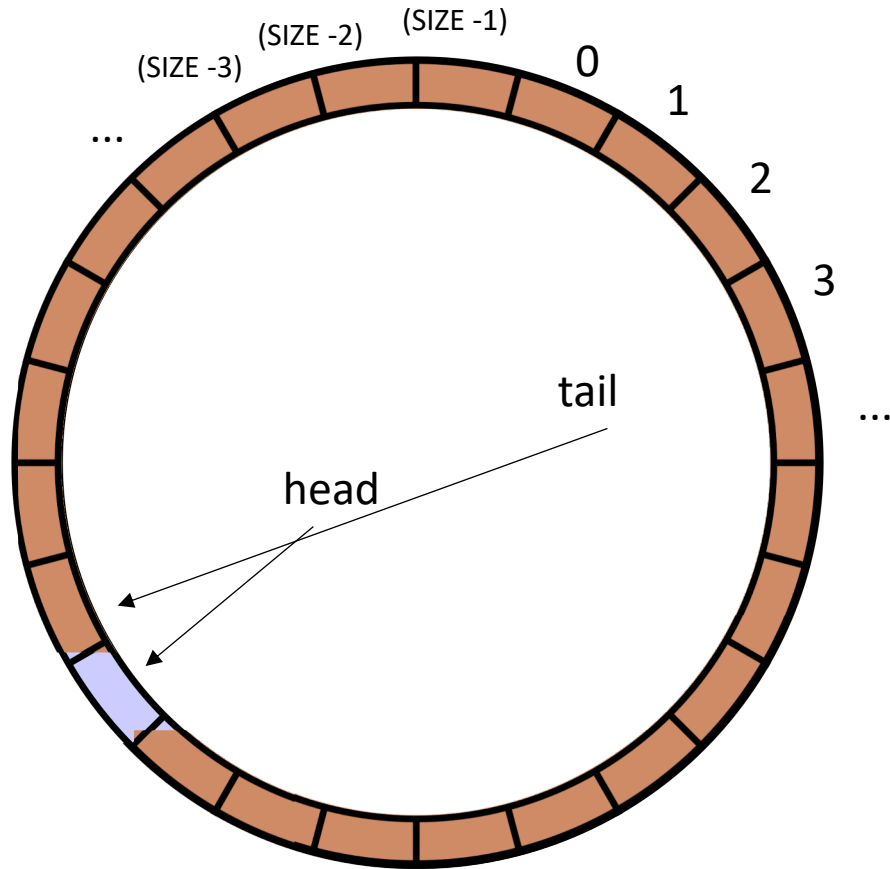
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class ProdConsQueue {  
    private:  
        atomic_int head;  
        atomic_int tail;  
        int buffer[SIZE];  
  
    public:  
        void enq(int x) {  
            // store value at head  
            // increment head  
        }  
        int deq() {  
            // wait while queue is not empty  
            // get value at tail  
            // increment tail  
        }  
}
```



```
class ProdConsQueue {  
    private:  
        atomic_int head;  
        atomic_int tail;  
        int buffer[SIZE];  
  
    public:  
        void enq(int x) {  
            // store value at head  
            // increment head  
        }  
        int deq() {  
            // wait while queue is not empty  
            // get value at tail  
            // increment tail  
        }  
}
```



```
class ProdConsQueue {  
    private:  
        atomic_int head;  
        atomic_int tail;  
        int buffer[SIZE];  
  
    public:  
        void enq(int x) {  
            // store value at head  
            // increment head  
        }  
        int deq() {  
            // wait while queue is not empty  
            // get value at tail  
            // increment tail  
        }  
}
```

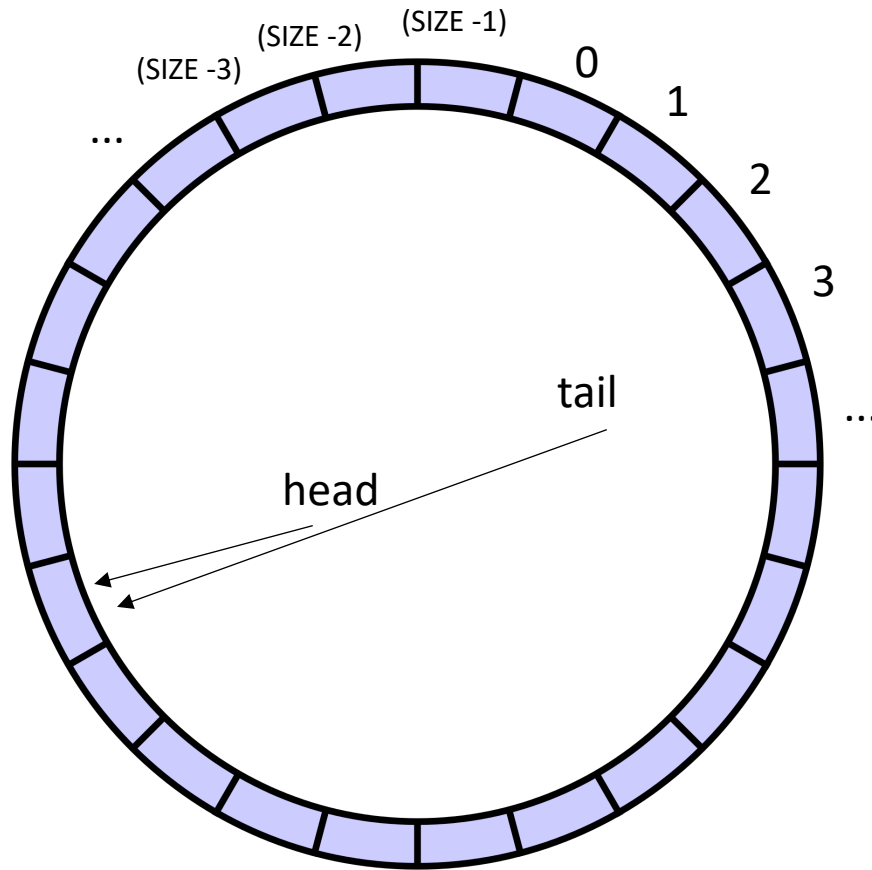


similarly for enqueue

```
class ProdConsQueue {  
    private:  
        atomic_int head;  
        atomic_int tail;  
        int buffer[SIZE];  
  
    public:  
        void enq(int x) {  
            // store value at head  
            // increment head  
        }  
        int deq() {  
            // wait while queue is not empty  
            // get value at tail  
            // increment tail  
        }  
}
```

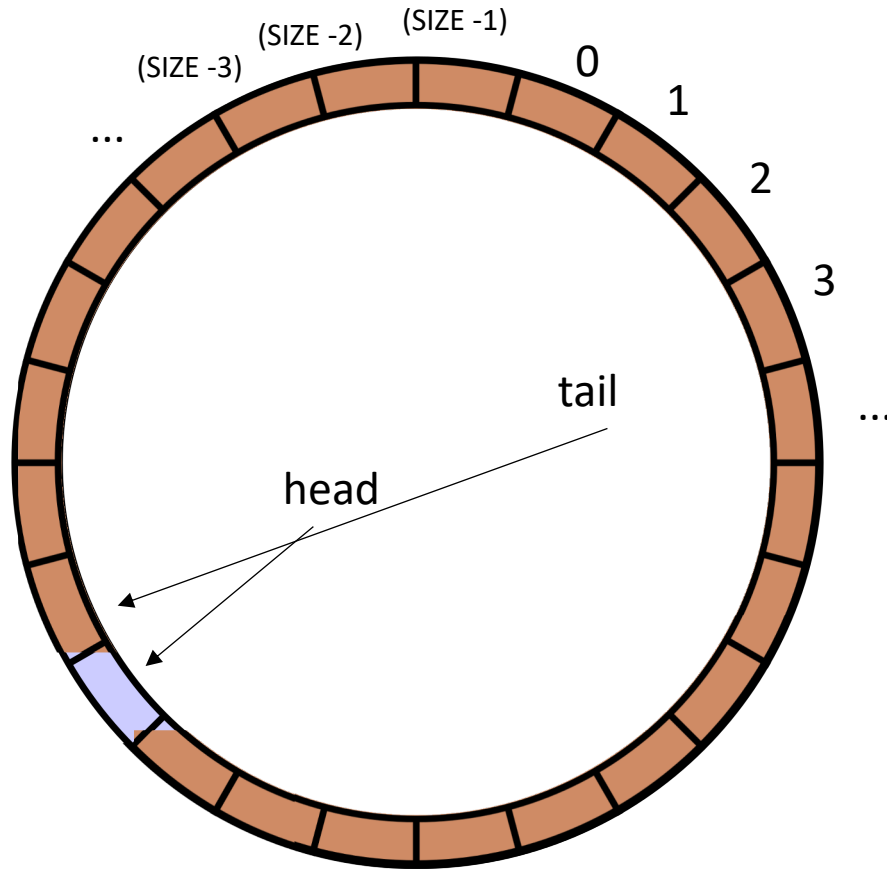
but why can't we enqueue?





```
class ProdConsQueue {  
    private:  
        atomic_int head;  
        atomic_int tail;  
        int buffer[SIZE];  
  
    public:  
        void enq(int x) {  
            // store value at head  
            // increment head  
        }  
        int deq() {  
            // wait while queue is not empty  
            // get value at tail  
            // increment tail  
        }  
}
```

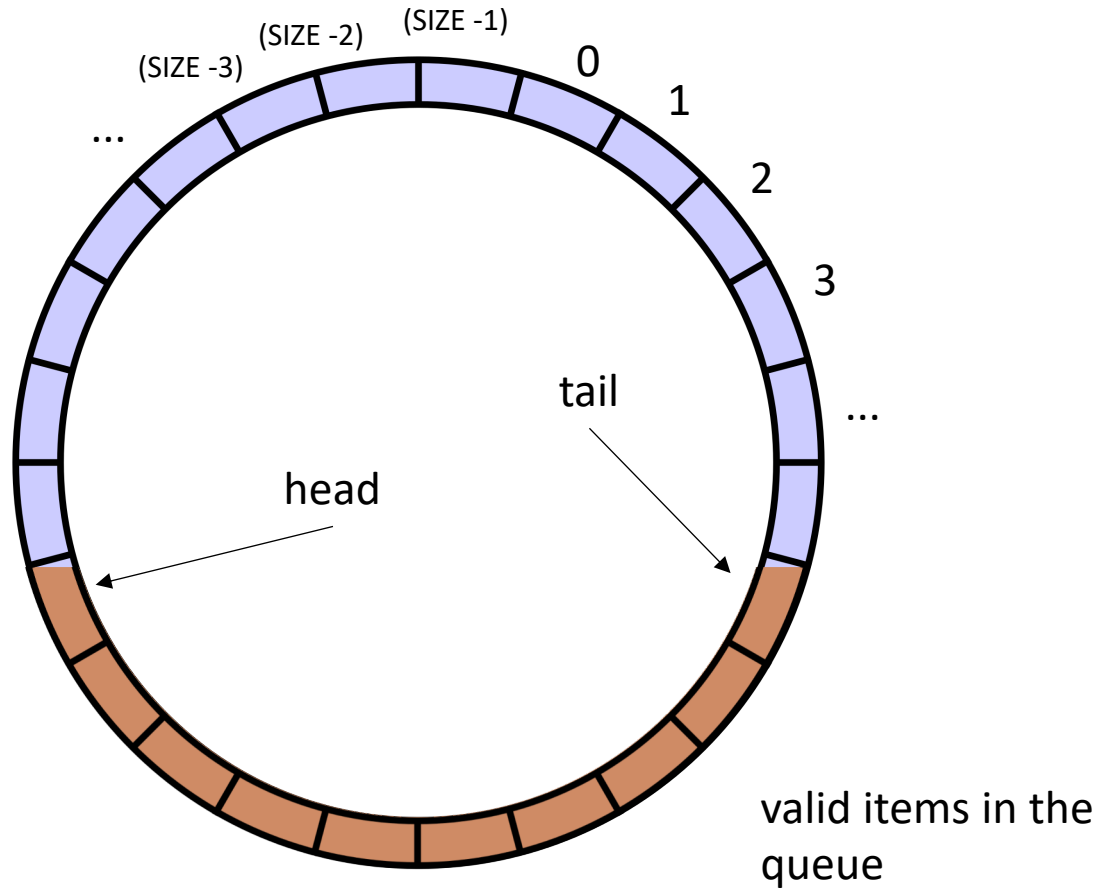
*incrementing the head would make it empty!*



we need to wait for there  
to be room

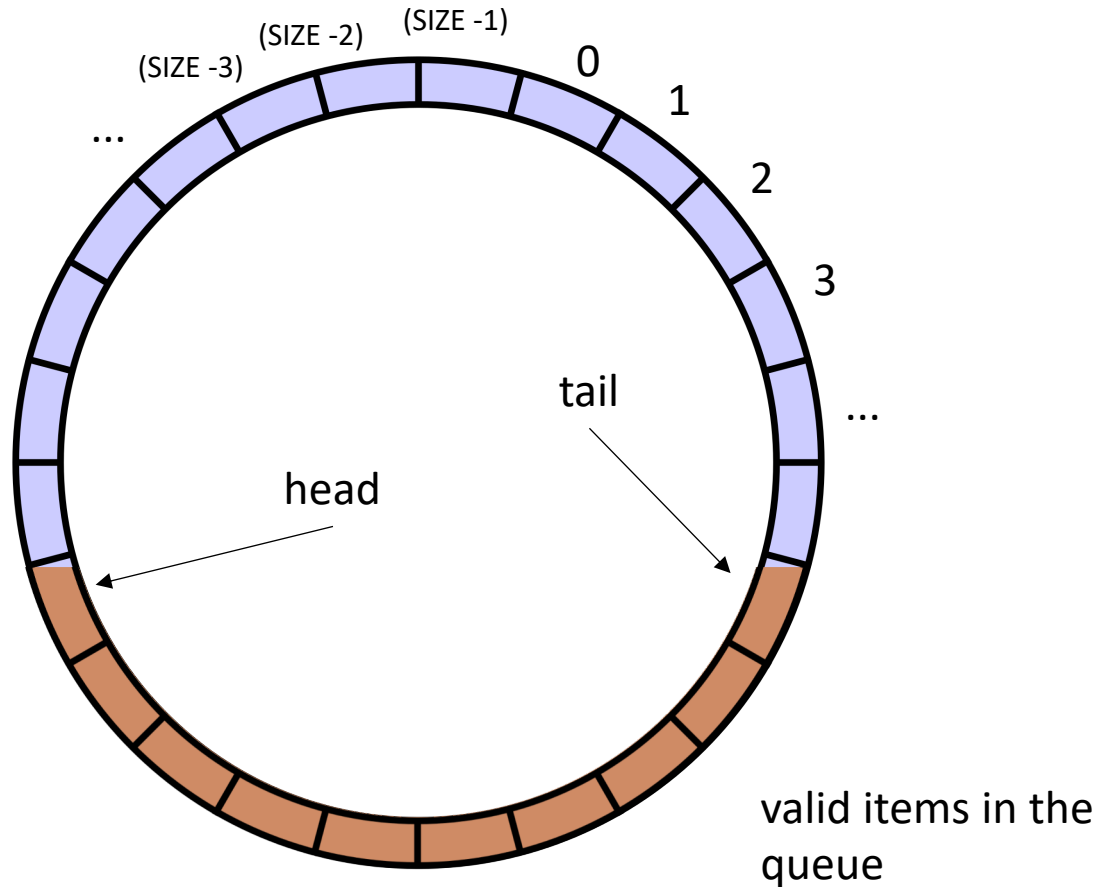
```
class ProdConsQueue {  
    private:  
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        void enq(int x) {  
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            // increment head  
        }  
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            // wait while queue is not empty  
            // get value at tail  
            // increment tail  
        }  
}
```

Other questions:



```
class ProdConsQueue {  
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            // increment head  
        }  
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            // get value at tail  
            // increment tail  
        }  
}
```

Other questions:



```
class ProdConsQueue {  
    private:  
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        }  
        int deq() {  
            // wait while queue is not empty  
            // get value at tail  
            // increment tail  
        }  
}
```

# Next week

- Workstealing!
- Good luck on the exam and HW!