

Draw a box around your answer. Show your work. Pens/calculators not allowed.

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1. Evaluate  $\int_1^2 \int_{1/x}^{2/x} x e^x dy dx$ .

- Correctly integrate inside function (4 pts)
- Correctly evaluate inside integral (3 pts)
- Correctly evaluate outside integral (3 pts)

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2. Evaluate  $\int_0^1 \int_{\sqrt{y}}^1 \frac{3}{1+x^3} dx dy$ .

- Draw region of integration correctly (3 pts)
  - Set up new bounds of integration correctly (4 pts)
  - Correctly evaluate new double iterated integral (3 pts)
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3. Express the area of the region between the curves  $y = 4 - x^2$  and  $y = x^2 - 4$  as a double iterated integral. **Do not evaluate the integral.**
- Use correct formula  $A = \iint_R dA$  (3 pts)
  - Draw region of integration correctly (3 pts)
  - Set up bounds of integration correctly (3 pts)
  - Write correct double iterated integral (1 pt)
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4. Express the average value of the function  $f(x, y) = 3xy^2$  over the triangle with sides given by the lines  $x = 4$ ,  $y = 0$ ,  $x = 2y$  as a multiple of a double iterated integral. **Do not evaluate the integral.**

- Use correct formula  $\frac{1}{\text{area of } R} \iint_R f(x, y) dA$  (3 pts)
  - Find area of the triangular/rectangular region (2 pts)
  - Set up bounds of integration correctly (3 pts)
  - Write correct multiple of double iterated integral (2 pts)
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5. Evaluate  $\int_0^1 \int_0^z \int_0^{x+z} 36xz \, dy \, dx \, dz$ .

- Evaluate inner integral correctly (4 pts)
  - Evaluate inner & middle integrals correctly (3 pts)
  - Evaluate entire triple iterated integral correctly (3 pts)
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6. Express the volume of the region in  $xyz$  space in the first octant bounded by the coordinate planes and the plane  $x + 3y + 2z = 6$  as a triple iterated integral. **Do not evaluate the integral.**

- Set up integral of the form  $\int_{\text{constant}}^{\text{constant}} \int_{\leq 1 \text{ var}}^{\leq 1 \text{ var}} \int_{\leq 2 \text{ var}}^{\leq 2 \text{ var}} dV$  (4 pts)
  - Set up innermost bounds correctly (3 pts)
  - Set up all bounds correctly (3 pts)
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7. Find a transformation  $x(u, v)$ ,  $y(u, v)$  from the triangle with coordinates  $(0, 0)$ ,  $(1, 0)$ , and  $(1, 1)$  in the  $uv$  plane into the triangle with vertices  $(0, 0)$ ,  $(2, 2)$ , and  $(1, 4)$  in the  $xy$  plane.
- Draw picture of regions in  $uv$  and  $xy$  planes (2 pts)
  - Label sides of regions in both planes correctly (3 pts)
  - Relate sides of regions in both planes correctly (3 pts)
  - Solve the system of equations for the correct transformation (2 pts)
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8. Using the transformation  $x = 3u - 2v$ ,  $y = 2u + 4v$  from the unit square in the  $uv$  plane into the parallelogram  $R$  with vertices  $(0, 0)$ ,  $(3, 2)$ ,  $(1, 6)$ , and  $(-2, 4)$  in the  $xy$  plane, evaluate

$$\iint_R (2x - y) \, dx \, dy$$

- Substitute  $x(u, v)$ ,  $y(u, v)$  for  $x$ ,  $y$  (2 pts)
  - Evaluate the Jacobian correctly, multiply the entire function by its absolute value (3 pts)
  - Set up the correct new bounds of integration (2 pts)
  - Evaluate the integral correctly (3 pts)
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9. Evaluate  $\int_0^2 \int_0^{\sqrt{4-x^2}} 3\sqrt{x^2+y^2} dy dx$ .

- Draw the region of integration correctly (3 pts)
  - Set up new polar bounds of integration (3 pts)
  - Replace  $x, y$  with  $r \cos \theta, r \sin \theta$  and replace  $dA$  with  $r dr d\theta$  (2 pts)
  - Evaluate the integral correctly (2 pts)
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10. Express the volume of the solid inside the sphere  $x^2 + y^2 + z^2 = 4$  ( $\rho = 2$ ) and above the cone  $z = \frac{\sqrt{3}}{2}\sqrt{x^2 + y^2}$  ( $\phi = \pi/6$ ) as a triple iterated integral using spherical coordinates. **Do not evaluate the integral.**

- Use volume formula  $\iiint_D dV$  (3 pts)
  - Set up spherical bounds of integration (4 pts)
  - Replace  $dV$  with  $\rho^2 \sin \phi d\rho d\phi d\theta$  (3 pts)
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Include extra scratch work below:

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