

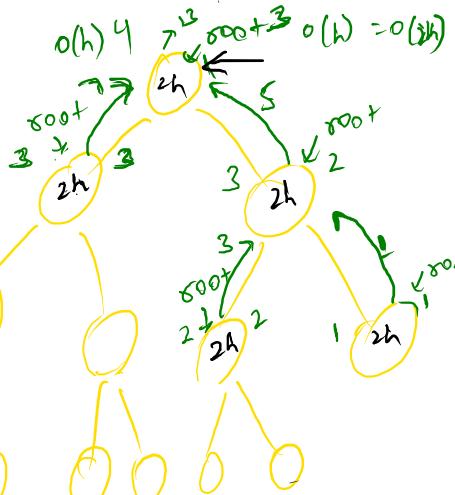
Count Complete tree nodes

$$\textcircled{1} \quad h = \log n$$

$$\textcircled{II} \quad 1 \text{ node} \rightarrow 2^h$$

$$ht + 2 \rightarrow 2h$$

$$O(h^2) \Rightarrow O(\log^2 n)$$



```
public int countNodes(TreeNode root) {
    if(root == null){
        return 0;
    }

    int leftheight = getHeightleft(root);
    int rightheight = getHeightright(root);

    if(leftheight == rightheight ){
        return ((1<<leftheight)-1);  $\Rightarrow 2^h - 1$ 
    }
}
```

```
int left = countNodes(root.left);
int right = countNodes(root.right);

return left+right+1;
```

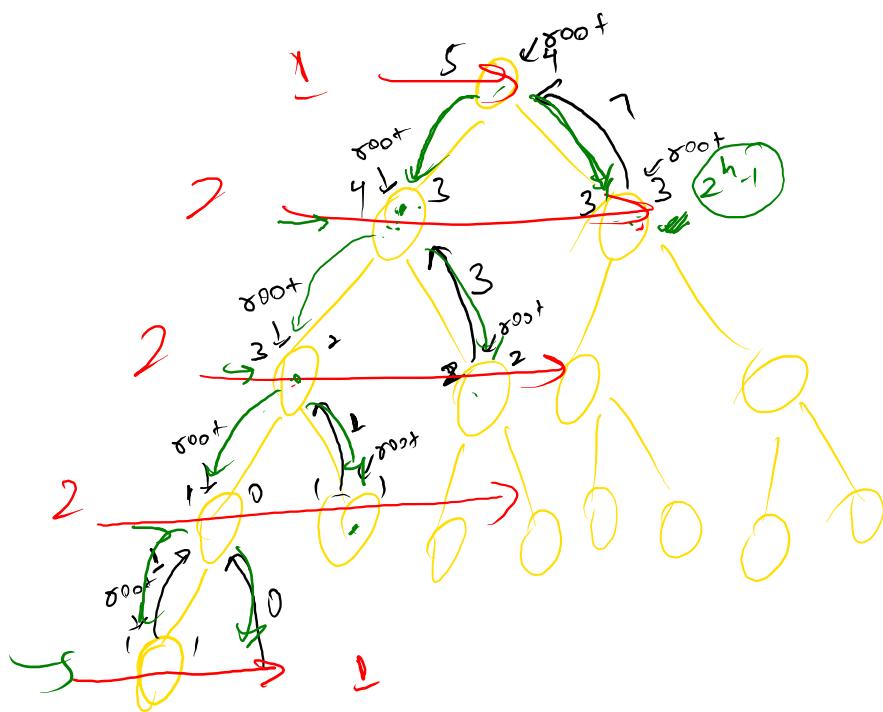
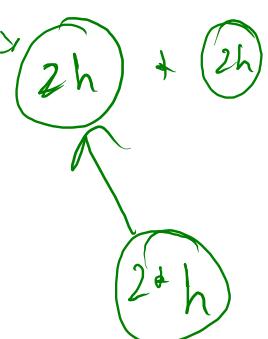
```
public int getHeightleft(TreeNode root){
    int count = 1;
    while(root.left != null){
        root = root.left;
        count++;
    }

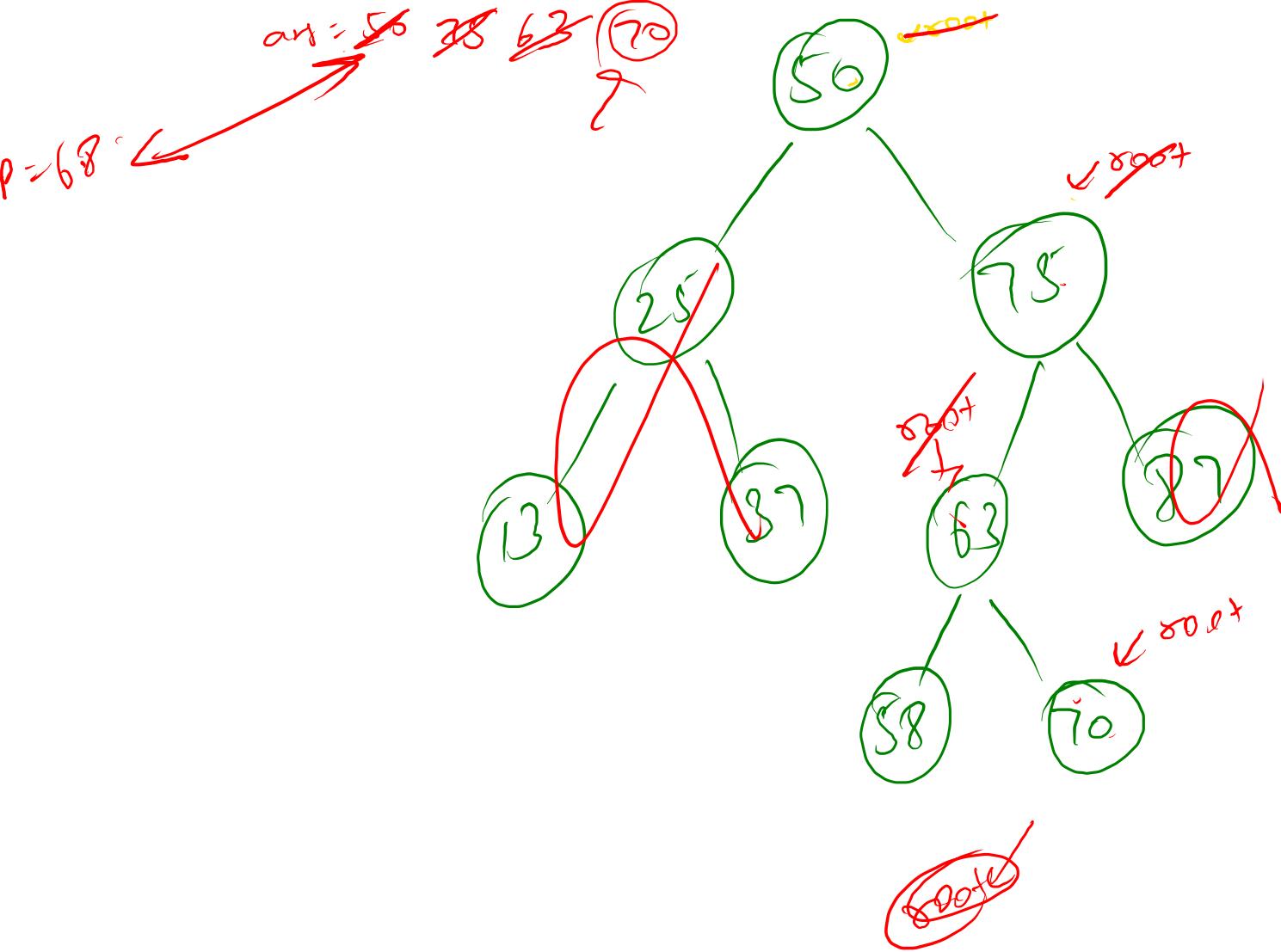
    return count;
}
```

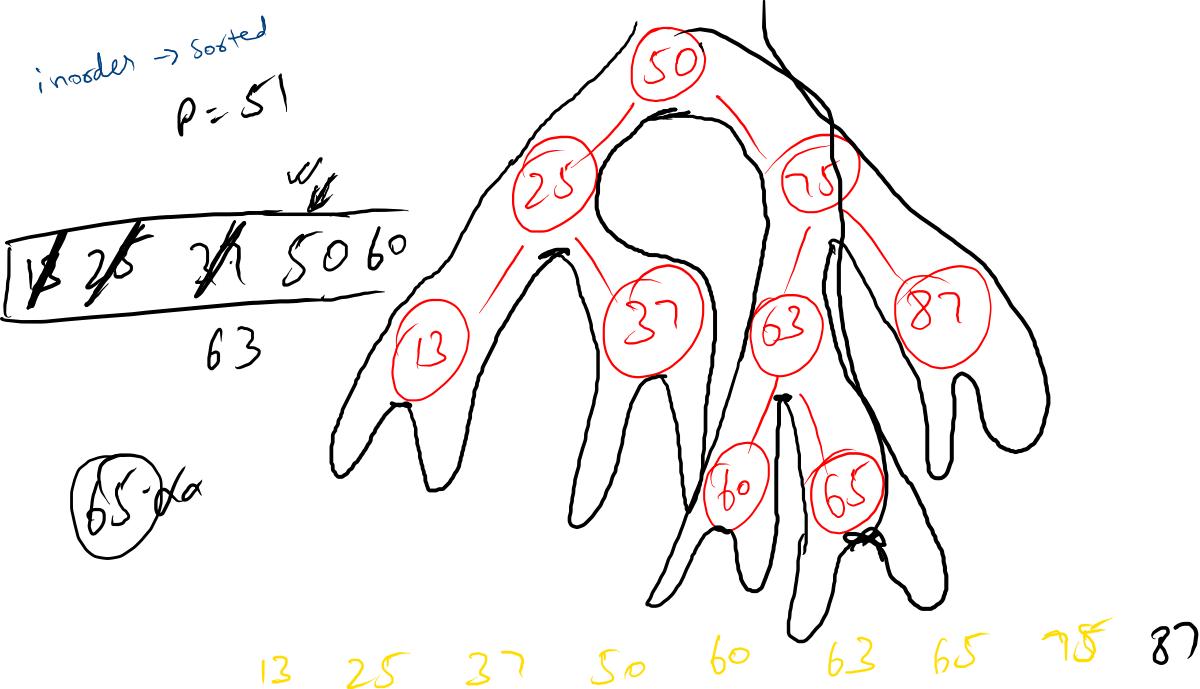
$O(h)$

```
public int getHeightright(TreeNode root){
    int count = 1;
    while(root.right != null){
        root = root.right;
        count++;
    }
}
```

$O(h)$







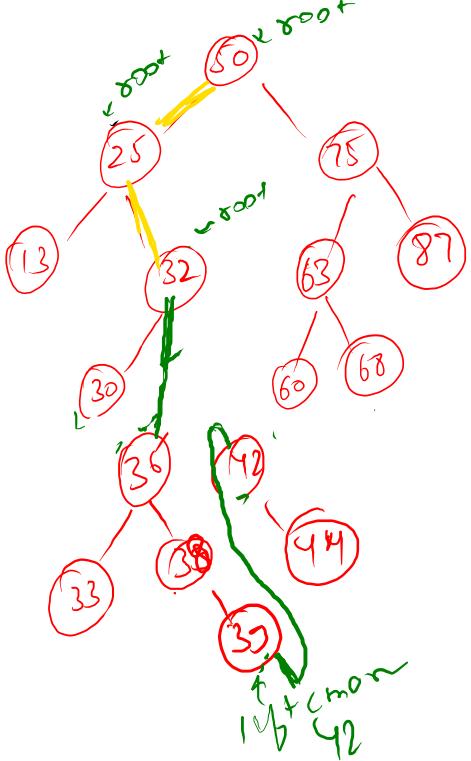
```

class Solution {
    public List<Integer> closestkValues(TreeNode root, double target, int k) {
        LinkedList<Integer> ans = new LinkedList<>();
        traversal(root, target, k, ans);
        return ans;
    }

    public void traversal(TreeNode root, double target, int k, LinkedList<Integer> ans) {
        if (root == null) {
            return;
        }
        traversal(root.left, target, k, ans);
        if (ans.size() < k) {
            ans.addLast(root.val);
        } else {
            boolean flag = false;
            if (Math.abs(target - root.val) < Math.abs(target - ans.peekFirst())) {
                flag = true;
                ans.removeFirst();
                ans.addLast(root.val);
            }
            if (!flag) {
                break;
            }
        }
        traversal(root.right, target, k, ans);
    }
}

```

~~delete node
in a BST~~



TreeNode traversal

```
if(root.val < key) {
    root.right = traversal(key, right);
} else if(root.val > key) {
    root.left = traversal(key, left);
```

} else

```
root = deleteNode(key);
```

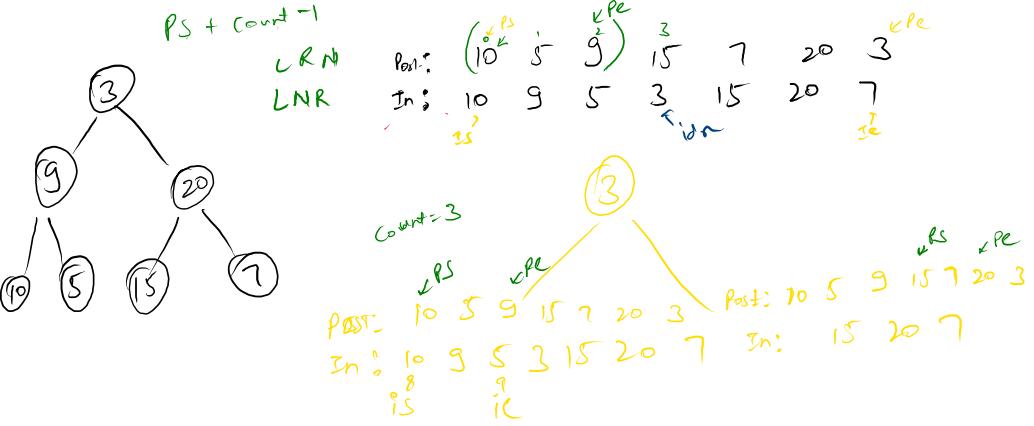
}

return root

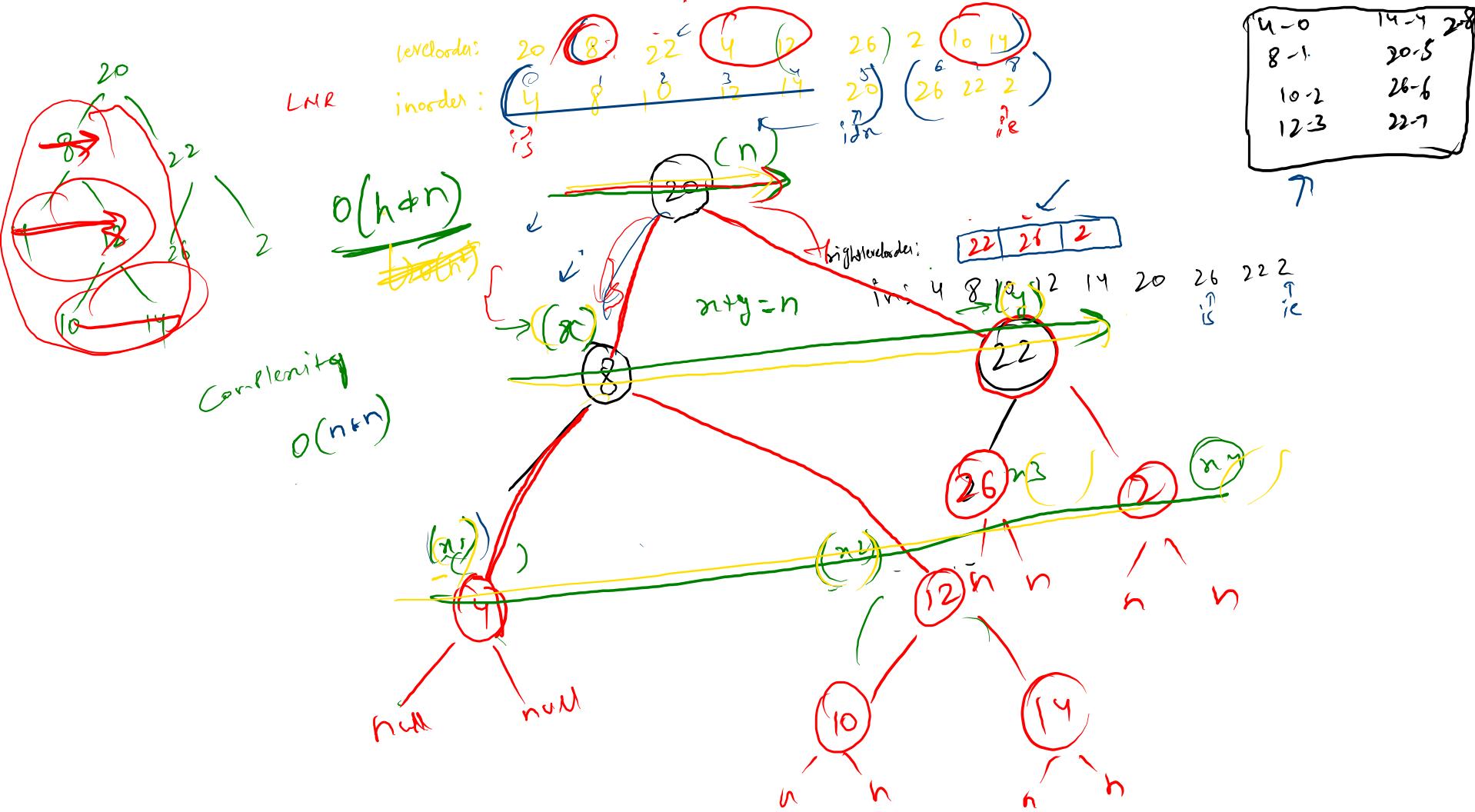
```
public TreeNode delete(TreeNode root){
    if(root.left == null & root.right == null){
        return null;
    } else if(root.left == null){
        return root.right;
    } else if(root.right == null){
        return root.left;
    } else{
        TreeNode rightc = root.right;
        TreeNode leftc = root.left;

        TreeNode leftcmax = leftc;
        while(leftcmax.right != null){
            leftcmax = leftcmax.right;
        }

        leftcmax.right = rightc;
    }
    return leftc;
}
```



Complete



$$\underline{a^b} \% \quad (10^3 + 7)$$

$$(a + a + a) \% \cdot 10^3 + 7$$

$$\left(\left(a \% \cdot 10^3 + 7 \right) + \left(a \% \cdot 10^3 + 7 \right) \right) \% \cdot 10^3 + 7$$

$$(1 \ 2 \ 3 \ 4 \ 5 \ 6 \ 7 \ 8 \ 9 \ 3 \ 9 \% \cdot 10^3 + 7) \% \cdot 10^3 + 7 \rightarrow \text{fast exp.}$$

$$1 \% \cdot 10^3 + 2 = 1234567$$

$$\begin{array}{r} 8 \\ 11) 980 \\ -88 \\ \hline 10 \\ -9 \\ \hline 1 \end{array}$$

$$980 \% \cdot 10^3 + 7$$

$$28 \ 100 \% \ 10^3 + 7$$

$$\boxed{a^{p-1} \% p = 1} \quad p \text{ is a prime no.}$$

$$\boxed{\frac{a^{k(p,i)}}{p^q} \% p = 1} \quad b \ggg$$

format
little
theorem

$$a^b \% m \quad b = (m-1)q_1 + r_1$$

$$\begin{aligned} a^b \% m &= a^{2((m-1)q_1 + r_1)} \% m \xrightarrow{\text{cancel } 2} a^{(m-1)q_1 + r_1} \% m \\ &= (a^{(m-1)q_1} \% m + a^{r_1}) \% m \xrightarrow{\text{cancel } a^{(m-1)q_1}} (a^{r_1}) \% m \end{aligned}$$

$$a^b \% m = \underbrace{a^{r_1}}_{a^b \% m} + \underbrace{a^{b \% (m-1)}}$$

Nim game

42

43

13

$x_{05} > 0 \rightarrow$ non-zero xor value

101100

110001

001110

$x_{05} = 0$

min 1 move

↓
170

| 0 | 1 | 1 | 0 0
↑ ↑ ↓ ↑ ↑ ↓

| 1 | 0 0 | 0 | 1 0
↑ ↓ | ↓ | ↑ ↓

0 0 | 1 | 1 | 1 0

