# pyEDM Version 1.9.1.0 August 7, 2021

pyEDM is a Python package interface to the cppEDM C++ library of empirical dynamic modeling (EDM) algorithms. It returns Pandas DataFrame objects, or Python dictionaries of Pandas DataFrames.

## **Table of Contents**

Introduction	2
Installation	3
Python Package Index (PyPI)	
Manual Compilation	3
OSX and Linux	
Windows	3
Usage	
Parameters	5
Application Programming Interface (API)	6
Embed	6
Simplex	7
SMap	8
CCM	10
Multiview	11
EmbedDimension	13
PredictInterval	14
PredictNonlinear	15
ComputeError	16
SurrogateData	17
Application Notes	
Examples	19
Deferences	20

University of California at San Diego Scripps Institution of Oceangraphy Sugihara Lab

Joseph Park, Cameron Smith

# Introduction

pyEDM is a Python interface to the C++ library cppEDM. Input and output objects are based on Pandas DataFrame objects. Core algorithms are listed in table 1.

Algorithm	API Interface	Reference
Simplex projection	Simplex()	Sugihara and May (1990)
Sequential Locally Weighted Global Linear Maps (S-map)	SMap()	Sugihara (1994)
Predictions from multivariate embeddings	<pre>Simplex(), SMap()</pre>	Dixon et. al. (1999)
Convergent cross mapping	CCM()	Sugihara et. al. (2012)
Multiview embedding	Multiview()	Ye and Sugihara (2016)

Convenience functions to prepare and evaluate data are listed in table 2.

Function	Purpose	Parameter Range
Embed()	Timeseries delay dimensional embedding	User defined
MakeBlock()	Timeseries delay dimensional embedding	User defined
<pre>EmbedDimension()</pre>	Evaluate prediction skill vs. embedding dimension	E = [1, 10]
<pre>PredictInterval()</pre>	Evaluate prediction skill vs. forecast interval	Tp = [1, 10]
PredictNonlinear()	Evaluate prediction skill vs. SMap nonlinear localisation	θ = 0.01, 0.1, 0.3, 0.5, 0.75, 1, 1.5, 2, 3, 4, 5, 6, 7, 8, 9
ComputeError()	Pearson ρ, RMSE, MAE	
Examples()	Example function calls and plots	

## Installation

There are two methods to install pyEDM:

- 1) Python Package Index and pip, which is only supported for certain OSX and Windows platforms
- 2) Download, build and install package.

## Python Package Index (PyPI)

Certain Mac OSX and Windows platforms are supported with prebuilt binary distributions and can be installed using the Python pip module. The module is located at <a href="https://pyebm/">pyebm/</a>.

```
Installation can be executed as:
python -m pip install pyEDM --trusted-host pypi.org --trusted-host
files.pythonhosted.org pyEDM
```

## Manual Compilation

Unfortunately, we do not have the resources to provide pre-built binary distributions for all computer platforms. In this case the user is required to first build the cppEDM library on their machine, and then install the Python package using pip. On OSX and Linux this requires gcc, on Windows, mingw and Microsoft Visual Studio Compiler (MSVC) which can be obtained from Build Tools for Visual Studio 2019. Only the Windows SDK is needed. Note that the LAPACK library is required to build cppEDM.

#### OSX and Linux

```
1) Download pyEDM: git clone https://github.com/SugiharaLab/pyEDM
```

```
2) Build cppEDM library:
cd pyEDM/cppEDM/src
make

3) Build and install package:
cd ../..
python -m pip install . --user --trusted-host pypi.org
```

#### Windows

We do not have resources to maintain windows build support. These suggestions may be useful.

Requires mingw installation. Requires gfortran libraries.

- 1) Download pyEDM: git clone https://github.com/SugiharaLab/pyEDM
- 2) Build cppEDM library: cd pyEDM\cppEDM\src; make
- 3) Adjust paths to find gfortran and openblas libraries (pyEDM/pyEDM/etc/windows/libopenblas.a). You may need to rename libEDM.a to EDM.lib, and openblas.a to openblas.lib.
- 4) Build and install package in pyEDM\: python -m pip install . --user --trusted-host pypi.org

# Usage

```
>>> import pyEDM
>>> pyEDM.Examples()
```

See the Examples section below.

All data input files are assumed to be in .csv format.

The files are required to have a single line header with column names.

It is required that the first column be a vector of times or time indices.

Parameters

API parameter names and purpose are listed in table 3.

dataFile string "" Data file name dataFrame Pandas DataFrame None Input DataFrame pathOut string "./" Output file path predictFile string "" Prediction output file library start: stop row indices pred string "" library start: stop row indices pred int 0 multiview state-space dimension E int 0 multiview state-space dimension E int 0 or 1 prediction interval E int 0 or 1 prediction vector exclusion radius interval include non projected forecast data verbose bool false Echo messages is data an embedding? Include non projected forecast data verbose bool false Echo messages validLib [ bool ] [] Conditional Embedding (CE) smapFite string "" SMap coefficient output file solver sklearn.linear_model None SMap solver untiview int 0 Number of ensembles, 0 = sqrt(N) trainLib bool true Multiview use lib as training library excludeTarget bool true Multiview exclude target from combos libSizes_str string "" CCM library sizes sample int 0 CCM number of random samples? CCM library sizes sample int 0 CCM sample with replacement? includeData bool false CCM sample with replacement? includeData bool false CCM include all projections in return seed unsigned 0 CCM RNG seed, 0 = random seed method alpha	Parameter	Type	Default	Purpose
dataFreme Pandas DataFrame None Input DataFrame pathOut string "./" Output file path predictFile string "" Prediction output file library start: stop row indices predictor start: stop row indices prediction interval kinn of the start of th	pathIn	string	"./"	Input data file path
pathOut string "./" Output file path predictFile string "" Prediction output file lib string "" prediction output file lib string "" prediction output file lib string "" prediction start: stop row indices pred string "" prediction start: stop row indices on the string "" prediction start: stop row indices on the state space dimension int 0 multiview state-space dimension on the string int 0 multiview state-space dimension on the string "" Embedding dimension on the string int 0 multiview sure highbors of the string "" Column names or indices for prediction target string "" Column names or indices for prediction target string "" Target library column name or index embedded bool false Include non projected forecast data verbose bool false Include non projected forecast data verbose bool false Echo messages validLib [bool] [1] Conditional Embedding (CE) smapFile string "" SMap coefficient output file solver sklearn.linear_model None SMap solver multiview int 0 Number of ensembles, 0 = sqrt(N) trainLib bool true Multiview use lib as training library excludeTarget bool true Multiview exclude target from combos libSizes_str string "" CCM library sizes sample int 0 CCM number of random samples random bool true CCM use random samples? cCM sample with replacement? includeData bool false CCM include all projections in return seed method string "ebisusaki" SurrogateData method alpha	dataFile	string	н н	Data file name
predictFile string "" Prediction output file lib string "" prediction output file library start: stop row indices pred string "" prediction start: stop row indices pred int 0 Multiview state-space dimension E int 0 Embedding dimension Prediction interval prediction interval int 0 or 1 Prediction interval prediction interval int 0 Number nearest neighbors tau int 1 on Number nearest neighbors tau int 1 on Prediction interval Embedding delay theta float 0 SMap localisation columns string "" Column names or indices for prediction target string "" Column names or indices for prediction target string "" Column names or indices for prediction target string "" Target library column name or index embedded bool false Is data an embedding? const_pred bool false Echo messages validLib [bool] [] Conditional Embedding (CE) smapFile string "" SMap coefficient output file solver sklearn.linear_model None SMap solver multiview int 0 Number of ensembles, 0 = sqrt(N) trainLib bool true Multiview use lib as training library excludeTarget bool true Multiview use lib as training library true Multiview as training library sizes sample int 0 CCM number of random samples random bool true CCM use random samples? replacement bool false CCM sample with replacement? includeData bool false CCM sample with replacement? includeData bool string "ebisusaki" SurrogateData seasonal noise std dev	dataFrame	Pandas DataFrame	None	Input DataFrame
predictFilestring""Prediction output filelibstring""library start: stop row indicespredstring""prediction start: stop row indicesDint0Multiview state-space dimensionEint0Embedding dimensionTpint0 or 1Prediction intervalknnint0Number nearest neighborstauint0SMap localisationexclusionRadiusint0Prediction vector exclusion radiuscolumnsstring""Column names or indices for predictiontargetstring""Target library column name or indexembeddedboolfalseIs data an embedding?const_predboolfalseInclude non projected forecast dataverboseboolfalseEcho messagesvalidLib[ bool ][ ]Conditional Embedding (CE)smapFilestring""SMap coefficient output filesolversklearn.linear_modelNoneSMap solvermultiviewint0Number of ensembles, 0 = sqrt(N)trainLibbooltrueMultiview use lib as training libraryexcludeTargetbooltrueMultiview exclude target from combossibSizes_strstring""CCM library sizessampleint0CCM number of random samplesreplacementboolfalseCCM include all projections in returnincludeDatabool <td>pathOut</td> <td>string</td> <td>"./"</td> <td>Output file path</td>	pathOut	string	"./"	Output file path
lib string """ prediction start: stop row indices pred string """ prediction start: stop row indices D int 0 Multiview state-space dimension E int 0 E Embedding dimension Tp int 0 or 1 Prediction interval knn int 0 Number nearest neighbors tau int -1 Embedding delay theta float 0 SMap localisation exclusionRadius int 0 Prediction vector exclusion radius columns string "" Column names or indices for prediction target string "" Column names or indices for prediction target string "" Target library column name or index embedded bool false Is data an embedding? const_pred bool false Echo messages validLib [ bool ] [] Conditional Embedding (CE) smapFile string "" SMap coefficient output file solver sklearn.linear_model None SMap solver multiview int 0 Number of ensembles, 0 = sqrt(N) trainLib bool true Multiview use lib as training library excludeTarget bool true Multiview exclude target from combos libSizes_str string "" CCM library sizes sample int 0 CCM number of random samples random bool true CCM use random samples? replacement bool false CCM sample with replacement? includeData bool false CCM RNG seed, 0 = random seed method string "ebisusaki" SurrogateData seasonal noise std dev	predictFile	string	шш	<u>.                                      </u>
pred	lib	string	шш	*
D int 0 0 Embedding dimension  F int 0 or 1 Prediction interval  knn int 0 or 1 Prediction interval  knn int 0 or 1 Embedding dimension  tau int -1 Embedding delay  theta float 0 SMap localisation  exclusionRadius int 0 Prediction vector exclusion radius  columns string "" Column names or indices for prediction  target string "" Target library column name or index  embedded bool false Is data an embedding?  const_pred bool false Include non projected forecast data  verbose bool false Echo messages  validLib [bool] I1 Conditional Embedding (CE)  smapFile string "" SMap coefficient output file  solver sklearn.linear_model None SMap solver  multiview int 0 Number of ensembles, 0 = sqrt(N)  trainLib bool true Multiview use lib as training library  excludeTarget bool true Multiview exclude target from combos  libSizes_str string "" CCM library sizes  sample int 0 CCM number of random samples  random bool true CCM use random samples?  replacement bool false CCM sample with replacement?  includeData bool CCM sample with replacement?  includeData  seed unsigned 0 CCM RNG seed, 0 = random seed  method string "ebisusaki" SurrogateData seasonal noise std dev	pred	string	шш	
Eint0Embedding dimensionTpint0 or 1Prediction intervalknnint0Number nearest neighborstauint-1Embedding delaythetafloat0SMap localisationexclusionRadiusint0Prediction vector exclusion radiuscolumnsstring""Column names or indices for predictiontargetstring""Target library column name or indexembeddedboolfalseIs data an embedding?const_predboolfalseEcho messagesvalidLib[ bool ][1]Conditional Embedding (CE)smapFilestring""SMap coefficient output filesolversklearn.linear_modelNoneSMap solvermultiviewint0Number of ensembles, 0 = sqrt(N)trainLibbooltrueMultiview use lib as training libraryexcludeTargetbooltrueMultiview exclude target from comboslibSizes_strstring""CCM library sizessampleint0CCM number of random samplesrandombooltrueCCM use random samples?replacementboolfalseCCM sample with replacement?includeDataboolGCM sample with replacement?includeDataboolCCM include all projections in returnseedunsigned0CCM RNG seed, 0 = random seedmethodstring"ebisusaki"SurrogateData method	D	int	0	± ±
Tpint0 or 1Prediction intervalknnint0Number nearest neighborstauint-1Embedding delaythetafloat0SMap localisationexclusionRadiusint0Prediction vector exclusion radiuscolumnsstring""Column names or indices for predictiontargetstring""Target library column name or indexembeddedboolfalseIs data an embedding?const_predboolfalseEcho messagesvalidLib[ bool ][ ]Conditional Embedding (CE)smapFilestring""SMap coefficient output filesolversklearn.linear_modelNoneSMap solvermultiviewint0Number of ensembles, 0 = sqrt(N)trainLibbooltrueMultiview use lib as training libraryexcludeTargetbooltrueMultiview exclude target from comboslibSizes_strstring""CCM library sizessampleint0CCM number of random samplesrandombooltrueCCM use random samples?replacementboolfalseCCM sample with replacement?includeDataboolGCM RNG seed, 0 = random seedmethodstring"ebisusaki"SurrogateData methodalphafloatrange / 5SurrogateData seasonal noise std dev	E	int	0	-
tau int -1 Embedding delay  theta float 0 SMap localisation  exclusionRadius int 0 Prediction vector exclusion radius  columns string "" Column names or indices for prediction  target string "" Target library column name or index  embedded bool false Is data an embedding?  const_pred bool false Include non projected forecast data  verbose bool false Echo messages  validLib [bool] I] Conditional Embedding (CE)  smapFile string "" SMap coefficient output file  solver sklearn.linear_model None SMap solver  multiview int 0 Number of ensembles, 0 = sqrt(N)  trainLib bool true Multiview use lib as training library  excludeTarget bool true Multiview exclude target from combos  libSizes_str string "" CCM library sizes  sample int 0 CCM number of random samples  random bool true CCM use random samples?  replacement bool false CCM sample with replacement?  includeData bool false CCM sample with replacement?  includeData bool string "ebisusaki" SurrogateData method  alpha float range / 5 SurrogateData seasonal noise std dev	Тр	int	0 or 1	0
tau int float 0 SMap localisation exclusionRadius int 0 Prediction vector exclusion radius columns string "" Column names or indices for prediction target string "" Target library column name or index embedded bool false Is data an embedding? const_pred bool false Include non projected forecast data verbose bool false Echo messages validLib [bool] I1 Conditional Embedding (CE) smapFile string "" SMap coefficient output file solver sklearn.linear_model None SMap solver multiview int 0 Number of ensembles, 0 = sqrt(N) trainLib bool true Multiview use lib as training library excludeTarget bool true Multiview exclude target from combos libSizes_str string "" CCM library sizes sample int 0 CCM number of random samples random bool true CCM use random samples? replacement bool false CCM sample with replacement? includeData bool false CCM sample with replacement? includeData bool false CCM sample with replacement? includeData string "ebisusaki" SurrogateData method alpha float range / 5 SurrogateData method	knn	int	0	Number nearest neighbors
theta float 0 SMap localisation exclusionRadius int 0 Prediction vector exclusion radius columns string "" Column names or indices for prediction target string "" Target library column name or index embedded bool false Is data an embedding? const_pred bool false Include non projected forecast data verbose bool false Echo messages validLib [bool] [l] Conditional Embedding (CE) smapFile string "" SMap coefficient output file solver sklearn.linear_model None SMap solver multiview int 0 Number of ensembles, 0 = sqrt(N) trainLib bool true Multiview use lib as training library excludeTarget bool true Multiview exclude target from combos libSizes_str string "" CCM library sizes sample int 0 CCM number of random samples random bool true CCM use random samples? replacement bool false CCM sample with replacement? includeData bool false CCM include all projections in return seed unsigned 0 CCM RNG seed, 0 = random seed method string "ebisusaki" SurrogateData method alpha float range / 5 SurrogateData seasonal noise std dev	tau	int	-1	<u> </u>
exclusionRadius int 0 Prediction vector exclusion radius columns string """ Column names or indices for prediction target string """ Target library column name or index embedded bool false Is data an embedding? const_pred bool false Include non projected forecast data verbose bool false Echo messages validLib [bool] [l] Conditional Embedding (CE) smapFile string "" SMap coefficient output file solver sklearn.linear_model None SMap solver multiview int 0 Number of ensembles, 0 = sqrt(N) trainLib bool true Multiview use lib as training library excludeTarget bool true Multiview exclude target from combos libSizes_str string "" CCM library sizes sample int 0 CCM number of random samples random bool true CCM use random samples? replacement bool false CCM sample with replacement? includeData bool false CCM include all projections in return seed unsigned 0 CCM RNG seed, 0 = random seed method alpha float range / 5 SurrogateData method	theta	float	0	
target string "" Target library column name or index embedded bool false Is data an embedding? const_pred bool false Include non projected forecast data verbose bool false Echo messages validLib [bool] [l] Conditional Embedding (CE) smapFile string "" SMap coefficient output file solver sklearn.linear_model None SMap solver multiview int 0 Number of ensembles, 0 = sqrt(N) trainLib bool true Multiview use lib as training library excludeTarget bool true Multiview exclude target from combos libSizes_str string "" CCM library sizes sample int 0 CCM number of random samples random bool true CCM use random samples? replacement bool false CCM sample with replacement? includeData bool false CCM include all projections in return seed unsigned 0 CCM RNG seed, 0 = random seed method string "ebisusaki" SurrogateData method alpha float range / 5 SurrogateData seasonal noise std dev	exclusionRadius	int	0	*
target string "" Target library column name or index embedded bool false Is data an embedding? const_pred bool false Include non projected forecast data verbose bool false Echo messages validLib [ bool ] [] Conditional Embedding (CE) smapFile string "" SMap coefficient output file solver sklearn.linear_model None SMap solver multiview int 0 Number of ensembles, 0 = sqrt(N) trainLib bool true Multiview use lib as training library excludeTarget bool true Multiview exclude target from combos libSizes_str string "" CCM library sizes sample int 0 CCM number of random samples random bool true CCM use random samples? replacement bool false CCM sample with replacement? includeData bool false CCM include all projections in return seed unsigned 0 CCM RNG seed, 0 = random seed method string "ebisusaki" SurrogateData seasonal noise std dev	columns	string	11 11	Column names or indices for prediction
embeddedboolfalseIs data an embedding?const_predboolfalseInclude non projected forecast dataverboseboolfalseEcho messagesvalidLib[ bool ][]Conditional Embedding (CE)smapFilestring""SMap coefficient output filesolversklearn.linear_modelNoneSMap solvermultiviewint0Number of ensembles, 0 = sqrt(N)trainLibbooltrueMultiview use lib as training libraryexcludeTargetbooltrueMultiview exclude target from comboslibSizes_strstring""CCM library sizessampleint0CCM number of random samplesrandombooltrueCCM use random samples?replacementboolfalseCCM sample with replacement?includeDataboolfalseCCM include all projections in returnseedunsigned0CCM RNG seed, 0 = random seedmethodstring"ebisusaki"SurrogateData methodalphafloatrange / 5SurrogateData seasonal noise std dev	target	string		
const_predboolfalseInclude non projected forecast dataverboseboolfalseEcho messagesvalidLib[ bool ][]Conditional Embedding (CE)smapFilestring""SMap coefficient output filesolversklearn.linear_modelNoneSMap solvermultiviewint0Number of ensembles, 0 = sqrt(N)trainLibbooltrueMultiview use lib as training libraryexcludeTargetbooltrueMultiview exclude target from comboslibSizes_strstring""CCM library sizessampleint0CCM number of random samplesrandombooltrueCCM use random samples?replacementboolfalseCCM sample with replacement?includeDataboolfalseCCM include all projections in returnseedunsigned0CCM RNG seed, 0 = random seedmethodstring"ebisusaki" SurrogateData methodalphafloatrange / 5SurrogateData seasonal noise std dev	embedded	bool	false	
verboseboolfalseEcho messagesvalidLib[ bool ][]Conditional Embedding (CE)smapFilestring""SMap coefficient output filesolversklearn.linear_modelNoneSMap solvermultiviewint0Number of ensembles, 0 = sqrt(N)trainLibbooltrueMultiview use lib as training libraryexcludeTargetbooltrueMultiview exclude target from comboslibSizes_strstring""CCM library sizessampleint0CCM number of random samplesrandombooltrueCCM use random samples?replacementboolfalseCCM sample with replacement?includeDataboolfalseCCM include all projections in returnseedunsigned0CCM RNG seed, 0 = random seedmethodstring"ebisusaki"SurrogateData methodalphafloatrange / 5SurrogateData seasonal noise std dev	const_pred	bool	false	
validLib	verbose	bool	false	
smapFilestring""SMap coefficient output filesolversklearn.linear_modelNoneSMap solvermultiviewint0Number of ensembles, 0 = sqrt(N)trainLibbooltrueMultiview use lib as training libraryexcludeTargetbooltrueMultiview exclude target from comboslibSizes_strstring""CCM library sizessampleint0CCM number of random samplesrandombooltrueCCM use random samples?replacementboolfalseCCM sample with replacement?includeDataboolfalseCCM include all projections in returnseedunsigned0CCM RNG seed, 0 = random seedmethodstring"ebisusaki" SurrogateData methodalphafloatrange / 5SurrogateData seasonal noise std dev	validLib	[ bool ]	[]	
solver sklearn.linear_model None SMap solver  multiview int 0 Number of ensembles, 0 = sqrt(N)  trainLib bool true Multiview use lib as training library  excludeTarget bool true Multiview exclude target from combos  libSizes_str string "" CCM library sizes  sample int 0 CCM number of random samples  random bool true CCM use random samples?  replacement bool false CCM sample with replacement?  includeData bool false CCM include all projections in return  seed unsigned 0 CCM RNG seed, 0 = random seed  method string "ebisusaki" SurrogateData method  alpha float range / 5 SurrogateData seasonal noise std dev	smapFile	string		g , ,
multiview int 0 Number of ensembles, 0 = sqrt(N) trainLib bool true Multiview use lib as training library excludeTarget bool true Multiview exclude target from combos libSizes_str string "" CCM library sizes sample int 0 CCM number of random samples random bool true CCM use random samples? replacement bool false CCM sample with replacement? includeData bool false CCM include all projections in return seed unsigned 0 CCM RNG seed, 0 = random seed method string "ebisusaki" SurrogateData method alpha float range / 5 SurrogateData seasonal noise std dev	solver	sklearn.linear_model	None	*
trainLib bool true Multiview use lib as training library excludeTarget bool true Multiview exclude target from combos libSizes_str string "" CCM library sizes sample int 0 CCM number of random samples random bool true CCM use random samples? replacement bool false CCM sample with replacement? includeData bool false CCM include all projections in return seed unsigned 0 CCM RNG seed, 0 = random seed method string "ebisusaki" SurrogateData method alpha float range / 5 SurrogateData seasonal noise std dev	multiview	int	0	<u>=</u>
excludeTarget bool true Multiview exclude target from combos libSizes_str string "" CCM library sizes sample int 0 CCM number of random samples random bool true CCM use random samples? replacement bool false CCM sample with replacement? includeData bool false CCM include all projections in return seed unsigned 0 CCM RNG seed, 0 = random seed method string "ebisusaki" SurrogateData method alpha float range / 5 SurrogateData seasonal noise std dev	trainLib	bool	true	- · · · · · · · · · · · · · · · · · · ·
libSizes_str string "" CCM library sizes sample int 0 CCM number of random samples random bool true CCM use random samples? replacement bool false CCM sample with replacement? includeData bool false CCM include all projections in return seed unsigned 0 CCM RNG seed, 0 = random seed method string "ebisusaki" SurrogateData method alpha float range / 5 SurrogateData seasonal noise std dev	excludeTarget	bool	true	
sample int 0 CCM number of random samples random bool true CCM use random samples? replacement bool false CCM sample with replacement? includeData bool false CCM include all projections in return seed unsigned 0 CCM RNG seed, 0 = random seed method string "ebisusaki" SurrogateData method alpha float range / 5 SurrogateData seasonal noise std dev	libSizes_str	string	шш	
random bool true CCM use random samples? replacement bool false CCM sample with replacement? includeData bool false CCM include all projections in return seed unsigned 0 CCM RNG seed, 0 = random seed method string "ebisusaki" SurrogateData method alpha float range / 5 SurrogateData seasonal noise std dev	sample	int	0	
replacement bool false CCM sample with replacement? includeData bool false CCM include all projections in return seed unsigned 0 CCM RNG seed, 0 = random seed method string "ebisusaki" SurrogateData method alpha float range / 5 SurrogateData seasonal noise std dev	random	bool	true	
includeData bool false CCM include all projections in return seed unsigned 0 CCM RNG seed, 0 = random seed method string "ebisusaki" SurrogateData method alpha float range / 5 SurrogateData seasonal noise std dev	replacement	bool	false	
seed unsigned 0 CCM RNG seed, 0 = random seed method string "ebisusaki" SurrogateData method alpha float range / 5 SurrogateData seasonal noise std dev	includeData	bool	false	
alpha float range / 5 SurrogateData seasonal noise std dev	seed	unsigned	0	
alpha float range / 5 SurrogateData seasonal noise std dev	method	string	"ebisusaki'	
	alpha	float		
SurrogateData seasonal spline smooth	smooth	float	0.8	SurrogateData seasonal spline smooth

## Application Programming Interface (API)

#### **Embed**

Create a data block of Takens (1981) time-delay embedding from each of the columns in the csv file or dataFrame. The columns parameter can be a list of column names, or a list of column indices. If columns is a list of indices, then column names are created as V1, V2...

Note: The returned DataFrame will have tau\*(E-1) fewer rows than the input data from the removal of partial vectors as a result of the embedding.

Note: The returned DataFrame will not have the time column.

## Simplex

Simplex projection of the input data file or DataFrame. The returned DataFrame has 3 columns "Time", "Observations", "Predictions". nan values are inserted where there is no observation or prediction. See the Parameters table for parameter definitions.

#### **Parameters**

lib and pred specify [start stop] row indices of the input data for the library and predictions.

If embedded is false the data columns are embedded to dimension E with delay tau. If embedded is true the data columns are assumed to be a multivariable data block.

If knn is not specified, and embedded is false, it is set equal to E+1. If embedded is true, knn is set equal to the number of columns + 1.

exclusionRadius defines the number of library rows excluded from the state-space library with respect to a temporal "radius" from the prediction state. If exclusionRadius = 1, library state-space points from observation time series that are within  $\pm 1$  sequential observation row of the prediction state are not included in the library. Note that units of the radius are time series rows, not time values.

validLib implements conditional embedding (CE). It is a boolean vector the same length as the number of time series rows. A false entry means that the state-space vector derived from the corresponding time series row will not be included in the state-space library.

## **SMap**

SMap projection of the input data file or DataFrame. See the Parameters table for parameter definitions.

SMap() returns a dict with two DataFrames:

The predictions DataFrame has 3 columns "Time", "Observations", "Predictions". nan values are inserted where there is no observation or prediction. If predictFile is provided the predictions will be written to it in csv format.

The coefficients DataFrame will have E+2 columns. The first column is the "Time" vector, the remaining E+1 columns are the SMap SVD fit coefficients. The first column "C0" is the bias term, following coefficients are  $\partial$  columns[i] /  $\partial$  target.

#### **Parameters**

lib and pred specify [start, stop] row indices of the input data for the library and predictions.

If embedded is False the data columns are embedded to dimension E with delay tau. If embedded is True the data columns are assumed to be a multivariable data block. If smapFile is provided the coefficients will be written to it in csy format.

If a multivariate data set is used (number of columns > 1) it must use embedded = true with E equal to the number of columns. This prevents the function from internally time-delay embedding the multiple columns to dimension E. If the internal time-delay embedding is performed, then state-space columns will not correspond to the intended dimensions in the matrix inversion, coefficient assignment, and prediction. In the multivariate case, the user should first prepare the embedding (using Embed() for time-delay embedding if desired), then pass this embedding to SMap with appropriately specified columns, E, and embedded = true.

If knn is not specified, it is set equal to the library size. If knn is specified, it must be greater than E+1.

exclusionRadius defines the number of library rows excluded from the state-space library with respect to a temporal "radius" from the prediction state. If exclusionRadius = 1, library state-space points from observation time series that are within  $\pm 1$  sequential observation row of the prediction state are not included in the library. Note that units of the radius are time series rows, not time values.

validLib implements conditional embedding (CE). It is a boolean vector the same length as the number of time series rows. A false entry means that the state-space vector derived from the corresponding time series row will not be included in the state-space library.

The default solver for the SMap coefficient matrix is the LAPACK SVD function dgelss(). This can be replaced with a user-instantianted class object from the python sklearn.linear\_model: Linear\_Models. Supported solvers include: LinearRegression, Ridge, Lasso, ElasticNet, RidgeCV, LassoCV, ElasticNetCV. See the pyEDM/tests/smapSolverTest.py script for examples.

```
//-----
= ""
                                                                                       lib
                                                                                                                                                                                                    = ""
                                                                                        pred
                                                                                        E
                                                                                                                                                                                                               = 0,
                                                                                        Tp
                                                                                                                                                                                                                   = 1,
                                                                                       knn
                                                                                                                                                                                                                  = -1,
                                                                                        tau
                                                                                        theta
                                                                                        exclusionRadius = 0,
                                                                                       columns = ""
                                                                                    columns
target
smapFile
derivatives
solver
embedded
verbose
const_pred
showPlot
target
= "",
characterist,
e "",
solver
= None,
e "",
                                                                                                                                                                                                                                                                         // Not implemented
```

#### **CCM**

Convergent cross mapping via Simplex of the first vector specified in columns against target. The data cannot be multivariable, the first vector in columns is time-delay embedded to dimension E. See the Parameters table for parameter definitions.

If includeData is False, the returned DataFrame has 3 columns. The first column is "LibSize", the second and third columns are Pearson correlation coefficients for "column: target" and "target: column" cross mapping. If includeData is True, a dict is returned with the LibMeans DataFrame, and a DataFrames of prediction statistics for all predictions in the ensembles.

#### **Parameters**

The libSizes parameter is a string of whitespace or comma separated library sizes. If the string has 3 values, and, if the third value is less than the second value, then the three values are interpreted as a sequence generator specifying "start stop increment" row values, i.e. "10 80 10" will evaluate library sizes from 10 to 80 in increments of 10.

If random is true, sample observations are radomly selected from the subset of each library size. If seed=0, then a random seed is generated for the random number generator. Otherwise, seed is used to initialise the random number generator.

If random is false, sample is ignored and contiguous library rows up to the current library size are used.

Note: Cross mappings are performed between column : target, and target : column. The default is to do this in separate threads. Threading can be disabled in the makefile by removing - DCCM\_THREADED.

Note: The entire prediction vector is used in the Simplex prediction at each library subset size.

#### Multiview

Multiview embedding and forecasting of the input data file or DataFrame. See the Parameters table for parameter definitions.

The Predictions DataFrame has 3 columns "Time", "Observations", "Predictions". nan values are inserted where there is no observation or prediction. If predictFile is provided the Predictions will be written to it in csy format.

The View DataFrame will have E+3 columns. The first E columns are the the column indices in the input data DataFrame that are embedded and applied to Simplex prediction. The last three columns are "rho", "MAE", "RMSE" corresponding to the prediction Pearson correlation, maximum absolute error and root mean square error.

#### **Parameters**

D represents the number of variables to combine for each assessment, if not specified, it is the number of columns.

E is the embedding dimension of each variable. If E = 1, no time delay embedding is done.

multiview is the number of top-ranked D-dimensional predictions to "average" for the final prediction. Corresponds to parameter k in Ye & Sugihara with default  $k = \operatorname{sqrt}(C)$  where C is the number of combinations C(n,D) available from the embedding columns taken D at-a-time.

trainLib specifies whether projections used to rank the column combinations are done in-sample (pred = lib, the default), or, using the lib and pred specified as input options (trainLib false).

lib and pred specify [start, stop] row indices of the input data for the library and predictions.

If knn is not specified, it is set equal to D+1.

numThreads defines the number of worker threads.

```
//-----
pred
               = 0,
       D
       Ε
               = 1,
       Тр
               = 1,
       knn
               = 0,
       tau
              = "",
= "",
       columns
       target
               = 0,
       multiview
       exclusionRadius = 0,
       trainLib = True,
       excludeTarget = False,
```

## EmbedDimension

Evaluate Simplex prediction skill for embedding dimensions from 1 to 10. The returned DataFrame has columns "E" and "rho". See the Parameters table for parameter definitions.

Note: numThreads defines the number of worker threads for the 10 embeddings. The maximum number of threads is 10.

## PredictInterval

Evaluate Simplex prediction skill for forecast intervals from 1 to 10. The returned DataFrame has columns "Tp" and "rho". See the Parameters table for parameter definitions.

Note: numThreads defines the number of worker threads for the 10 prediction interval forecasts. The maximum number of threads is 10.

#### PredictNonlinear

Evaluate SMap prediction skill for localisation parameter  $\theta$  (default from 0.01 to 9). The returned DataFrame has columns "theta" and "rho". See the Parameters table for parameter definitions.

If knn is not specified, it is set equal to the library size. If knn is specified, it must be greater than E.

Note: numThreads defines the number of worker threads for the  $\theta$  value forecasts.

```
//-----
DataFrame PredictNonlinear( pathIn = "./", dataFile = "", dataFrame = None,
                           pathOut = "./",
                           predictFile = ""
                                = "",
                           lib
                           pred
                          theta
                           Е
                                      = 0,
                           knn
                           Tp
                                      = 1,
                           tau
                          columns = "",
target = "",
embedded = False,
verbose = False,
                           numThreads = 4,
                           showPlot = False );
```

## Compute Error

Compute Pearson correlation coefficient, maximum absolute error (MAE) and root mean square error (RMSE) between two vectors.

ComputeError() returns a dict:

## SurrogateData

Generate surrogate data using one of three methods.

#### 1) random\_shuffle:

Sample the data with a uniform distribution.

#### 2) ebisuzaki:

Journal of Climate. A Method to Estimate the Statistical Significance of a Correlation When the Data Are Serially Correlated.

https://doi.org/10.1175/1520-0442(1997)010<2147:AMTETS>2.0.CO;2

Presumes data are serially correlated with low pass coherence. It is: "resampling in the frequency domain. This procedure will not preserve the distribution of values but rather the power spectrum (periodogram). The advantage of preserving the power spectrum is that resampled series retains the same autocorrelation as the original series."

#### 3) seasonal:

Presume a smoothing spline represents the seasonal trend. The smooth parameter can range from 0 to 1. See <a href="scipy.interpolate.UnivariateSpline">scipy.interpolate.UnivariateSpline</a> parameter s.

Each surrogate is a summation of the trend, resampled residuals, and possibly additive Gaussian noise. Default noise has a standard deviation (alpha) that is the data range / 5.

Note: It is presumed the first column of the dataFrame is a time vector. It is set as the first column of the returned DataFrame.

# **Application Notes**

All data input files are assumed to be in .csv format.

The files are required to have a single line header with column names. It is required that the first column be a vector of times or time indices.

SMap() should be called with DataFrame that have columns explicitly corresponding to dimensions E. This means that if a multivariate data set is used, it should Not be called with an embedding from Embed() since Embed() will add lagged coordinates for each variable. These extra columns will then not correspond to the intended dimensions in the matrix inversion and prediction reconstruction. In this case, use the embedded parameter set to true so that the columns selected correspond to the proper dimension.

## **Examples**

```
from pyEDM import *
df = EmbedDimension( dataFrame = sampleData["TentMap"],
                      lib = "1 100", pred = "201 500",
                      columns = "TentMap", showPlot = True )
df = PredictInterval( dataFrame = sampleData["TentMap"],
                       lib = "1 100", pred = "201 500", E = 2,
                       columns = "TentMap", showPlot = True )
df = PredictNonlinear( dataFrame = sampleData["TentMapNoise"],
                        lib = "1 100", pred = "201 500", E = 2,
                        columns = "TentMap", showPlot = True )
df = Simplex( dataFrame = sampleData["block 3sp"],
              lib = "1 99", pred = "100 198", E = 3,
              columns = "x_t y_t z_t", target = "x_t",
              embedded = True, showPlot = True )
df = Simplex( dataFrame = sampleData["block 3sp"],
              lib = "1 99", pred = "100 195", E = 3,
              columns = "x t", target = "x t", showPlot = True )
M = Multiview( dataFrame = sampleData["block_3sp"],
               lib = "1 100", pred = "101 198", E = 3, columns = "x_t y_t z_t", target = "x_t", showPlot = True )
S = SMap( dataFrame = sampleData["circle"],
          lib = "1 100", pred = "101 198", E = 2, theta = 4,
          columns = "x y", target = "x", embedded = True, showPlot = True )
df = CCM( dataFrame = sampleData["sardine anchovy sst"],
          E = 3, Tp = 0, columns = "anchovy", target = "np_sst",
          libSizes = "5 75 5", sample = 100, showPlot = True )
```

## References

Dixon, P. A., M. Milicich, and G. Sugihara, 1999. Episodic fluctuations in larval supply. Science 283:1528–1530.

Sugihara G. and May R. 1990. Nonlinear forecasting as a way of distinguishing chaos from measurement error in time series. Nature, 344:734–741.

Sugihara G. 1994. Nonlinear forecasting for the classification of natural time series. Philosophical Transactions: Physical Sciences and Engineering, 348 (1688): 477–495.

Sugihara G., May R., Ye H., Hsieh C., Deyle E., Fogarty M., Munch S., 2012. Detecting Causality in Complex Ecosystems. Science 338:496-500.

Takens, F. Detecting strange attractors in turbulence. Lect. Notes Math. 898, 366–381 (1981).

Ye H., and G. Sugihara, 2016. Information leverage in interconnected ecosystems: Overcoming the curse of dimensionality. Science 353:922–925.