

Learning from very few data

Few sample Learning (FSL)

a single or a handful of examples!

pre frontal cortex (PFC) : prominent human
working memory in human brain: learning ability

Mapping function:

$$f \in \mathcal{F} : x \rightarrow y$$

$$D_x = \{(x_i, y_i)\}_{i=1}^n$$

joint distribution $P_{x \times y}$

$$\boxed{\mathcal{E}_{ex} = \mathbb{E}_{(x,y) \sim P_{x \times y}} L(f(x), y)}$$

↓ $P_{x \times y}$ is unknown

$$\Sigma_{ex} = \mathbb{E}_{(x,y) \sim D_t} L(f(x), y)$$

Generalization Error:

$$\Sigma = |\Sigma_{ex} - \Sigma_{en}|$$

Σ is big since the Function Space \mathcal{F} is large

$$\min_f \Sigma_{en}, \quad \text{s.t.} \quad \begin{cases} f(x_i) = y_i \\ \forall (x_i, y_i) \in D_t \end{cases}$$

regularization on the function f

Compress the redundant optional space of function f and thereby reduce its generalization

error.

E.G. Miller (2000) Coagulating Algorithm

G. Koch (2015) DL + FSL

Before 2015 (Non-DL):

Generative Model

estimate / $\left\{ \begin{array}{l} \text{joint distribution } P(x, y) \\ \text{conditional distribution } P(x|y) \end{array} \right.$

Coagulating Algorithm

Variational Bayesian Framework (VBF)

Bayesian Program Learning (BPF)

After 2015 (DL):

Data Augmentation
Metric Learning
Meta Learning

Siamese CNN

Matching Nets

MAML

Meta-Learner LSTM

MANN

MetaNet

Prototypical Nets

LGM-Nets

$$D_T = \{D_{\text{trn}}, D_{\text{tst}}\}$$

$$\begin{cases} D_{\text{trn}} = \{(X_i, Y_i)\}_{i=1}^{N_{\text{trn}}} \\ D_{\text{tst}} = \{X_j\}_{j=1}^{N_{\text{tst}}} \end{cases}$$

$$\begin{cases} X_i, X_j \in X_T \subset X \\ Y_i \in Y_T \subset Y \end{cases}$$

$$D_T = \{X_T, P(X_T)\}$$

$P(X_T)$: Marginal probability distribution

C task classes

k (very small, 1, 5) samples per class

$N_{\text{trn}} = Ck$ (C -way k -shot task)

Goal: produce a target predictive function

$$f \in \mathcal{F} : X \rightarrow Y$$

which can make predictions for test samples in D_{test} .

$$D_A = \{ (x_i^a, y_i^a) \}_{i=1}^{N_{\text{aux}}}$$

$$x_i^a \in X_A \subseteq X, \quad y_i^a \in Y_A \subseteq Y$$