Simulation and Modelling



Spring 2023 CS4056

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Introduction	
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Introduction Basics	
ourse Outline	nATIONAL UNIVERSITY of Computer & Emerging Sciences
Hierarchy of knowledge about a system an	nd Modeling Strategy.
• Simulating Probabilities	
Simulating Random Variables	
Simulating Stochastic ProcessesThe Monte Carlo Simulation	
Simulating Queueing Processes	
Statistical Analysis of Simulated Data	
Markov Chains	
Random Variate Generation	
• Random Number Generation	
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4 Quiz 5 Final Project(F)

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What is Simulation

- Simulation is the process of representing a system by a model.
- then executing this model to generate raw data.
- Involves the generation and observation of an artificial history of a system
- The raw data is not useful by itself.
- It must be statistically processed to produce insights about the performance of the system.
- Draw inferences about the characteristics of the real system

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- Simulation can be used as both an analysis tool and a design tool.
 - An analysis tool: To answer "what if" questions about the existing real-world system.

 $\ensuremath{\mathsf{E.g.}}\xspace$, try alternative layout of a production line, try other staff shifts of a service center, test a financial system in some extreme situation, etc.

- $\bullet\,$ A design tool: To study systems in the design stage, before they are built.
- E.g., evaluate designs and operations for new transportation facilities, service organizations, manufacturing systems, etc.
- Simulation is also an important type of numerical methods.

Models

- A model is a representation of a system or problem.
- \bullet A set of assumptions and/or approximations about how the system works will often be imposed.
- It is only necessary to consider those aspects that affect the problem under investigation.
- However, the model should be sufficiently detailed to draw valid conclusions about the real system or problem.
- The trade-off: simplicity vs. accuracy.

Votes			



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conducted with the aid of a computer.

Essentially, running simulation is still one type of numerical methods.
 Real-world simulation models can be large, and such runs are usually

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Classification of Simulation models



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- Simulation models may be classified as being static or dynamic.
- Static: Time does not play a natural role.
 - Example 1 Finance: evaluate portfolio return and risk.
 - Example 2 Project Management: evaluate projects payoff in different scenarios.
 - Often used in the complex numerical calculation in financial engineering, computational physics, etc.
- Dynamic: Time does play a natural role.
 - ullet Example 1 Logistics Management: evaluate the efficiency of a terminal.
 - Example 2 Service Management: evaluate waiting time of customers under different staff shifts.
 - Often used to simulate the logistics/transportation/service systems, whose status naturally changes over time.

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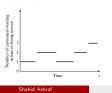
Classification of Simulation models

- Simulation models may be classified as being deterministic or stochastic.
- Deterministic: Everything is known with certainty.
- e.g., patients arrive at a hospital precisely on schedule, the service time is precisely fixed, the transfer among different units is pre-determined.
- Stochastic: Uncertainty exists.
- e.g., arrival times and service times of patients have random variations, the transfer is random.
- Used much more often (uncertainty is more or less involved in a real-world system).



Classification of Simulation models

- Simulation models may be classified discrete or continuous.
- Discrete: System states change only at discrete time points.
- E.g., the number of customers in the bank, changes only when a customer arrives or leaves after service
- Continuous: System states change continuously over time.
- the head of water behind a dam changes continuously during a period of time.



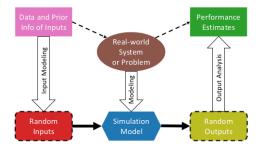
- In summary, simulation models may be classified as being
 - static or dynamic,
 - deterministic or stochastic, and
 - discrete or continuous.
- \bullet For most operational decision-making problems, the suitable simulation models are dynamic, stochastic and discrete.
- The simulation is called Discrete-Event System Simulation
 - The word "event" indicates that the simulation is advanced by the occurrence of events.
 - The word "discrete" means that events occur at discrete points of time.

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Figure: Basic Paradigm of A Simulation Study

Phases of a simulation study



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Consider the situation in Figure below where five people have to wait in a queue at the checkout counter in a supermarket. This situation arises because there is only one cashier and more than one person wants to have access to him. This phenomenon is referred to as queueing. Let us see $\,$ how observation, experimentation, and computation can be used to study this phenomenon.



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Description Description
Customers experience delays longer than 5 minutes. The checkout process has to be speeded up. Potential solutions include changing the cashier and installing a new software system. The raw data to be collected include the delay experienced by each customer $i(D_i)$ which is defined as the difference between his departure time (D_i) and arrival time (A_i) . Problem tween his departure time (D_i) and arrival time (A_i) . Customers, waiting line, and cashier. A customer arrives at the system. If the cashier is free, he will be served immediately. Otherwise, he has to wait. Service time of each customer is random. Model is expressed in Python code. Response time of the system (i.e., the average delay). $T_{avg} = \frac{\sum_i^N D_i}{N_i}$, where N is the number of participating customers. Response time for each possible solu-4 Computer Program 5 Statistical Analysis Response time for each possible solu-Performance Summary tion. Pick the one that gives the best response time as the optimal solution.

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Advantages of Simulation



- There is no need to build the physical system under study and then observe it. Thus, knowledge about the behavior of the system can be acquired with a minimum cost.
- Critical scenarios can be investigated through simulation with less cost and no risk.
- Using a simulation model, the effect of changing values of system variables can be studied with no interruption to the physical system.
- Simulation is more flexible and convenient than mathematical analysis.
- In simulation, there is no need for simplifying assumptions
- · Simulation allows us to compress and expand the behavior of the system under study. For example, several years' worth of system evolution can be studied in a few minutes of computer time.



Limitation of Simulation





- The outcome of a simulation study is an estimate subject to a statistical error. For example, different simulation runs typically produce different numbers although the same simulation model is used.
- Simulation can become costly and time consuming. For example, very powerful computers and skillful people are required.
- Simulation models are not easy to develop. Existing methodologies are not universal. This is why development of simulation models is still an art, not a science.
- Existing programming languages are not designed to support simulation. Thus, a lot of programming is involved.

Practice problem





• The following data yield the arrival times and service times that each customer will require, for the first 13 customers at a single server system. Upon arrival, a customer either enters service if the server is free or joins the waiting line. When the server completes work on a customer, the next one in line (i.e., the one who has been waiting the longest) enters service.

Arrival Times:12 31 63 95 99 154 198 221 304 346 411 455 537 Service Times:40 32 55 48 18 50 47 18 28 54 40 72 12

- a Determine the departure times of these 13 customers.
- b Repeat (a) when there are two servers and a customer can be served by either one.
- c Repeat (a) under the new assumption that when the server completes a service, the next customer to enter service is the one who has been waiting the least time.

Practice problem

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• Consider a service station where customers arrive and are served in their order of arrival. Let A_n , S_n , and D_n denote, respectively, the arrival time, the service time, and the departure time of customer n.

Suppose there is a single server and that the system is initially empty

of customers. $\bullet \ \mbox{With} \ D_0 = 0 \mbox{, argue that for} \ n > 0 \label{eq:decomposition}$

$$D_n - S_n = Maximum\{A_n, D_{n-1}\}$$

- Determine the corresponding recursion formula when there are two
- \bullet Determine the corresponding recursion formula when there are kservers.
- Write a computer program to determine the departure times as a function of the arrival and service times and use it to check your answers in parts (a) and (b) of previous Exercise

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