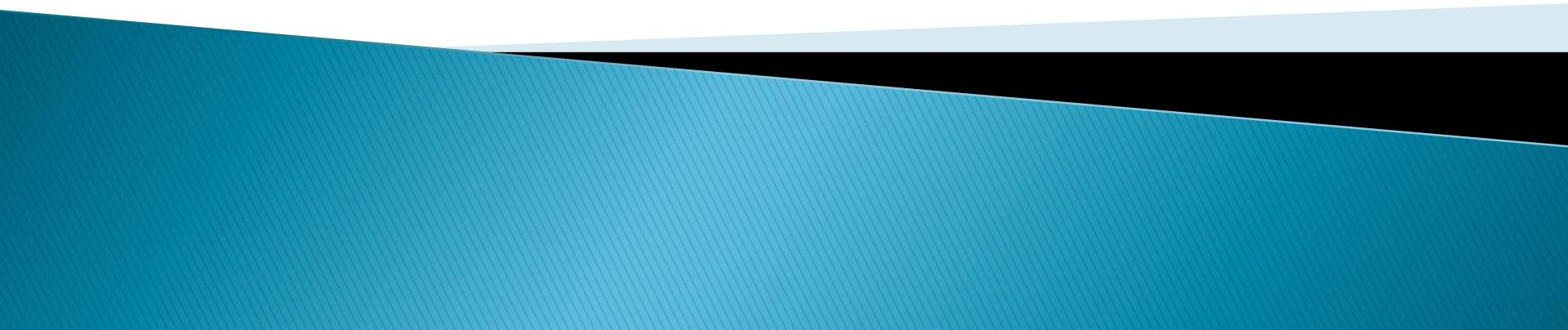
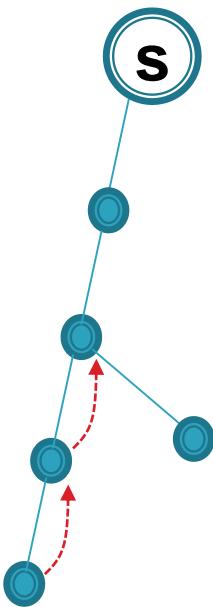


Parcurgerea în adâncime



Parcurea în adâncime



Parcurgerea în adâncime

Se vizitează

- Inițial: vârful de start s – devine vârf curent

Parcurgerea în adâncime

Se vizitează

- **Initial:** vârful de start s – devine vârf curent
- **La un pas:**
 - se trece la primul vecin nevizitat al vârfului curent,
dacă există

Parcurgerea în adâncime

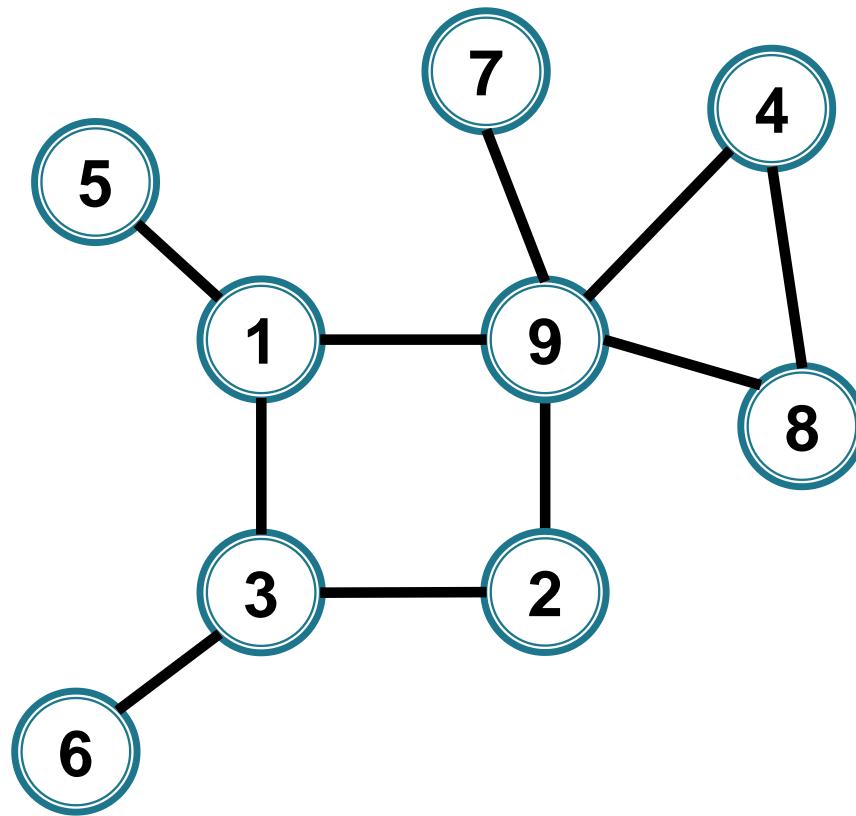
Se vizitează

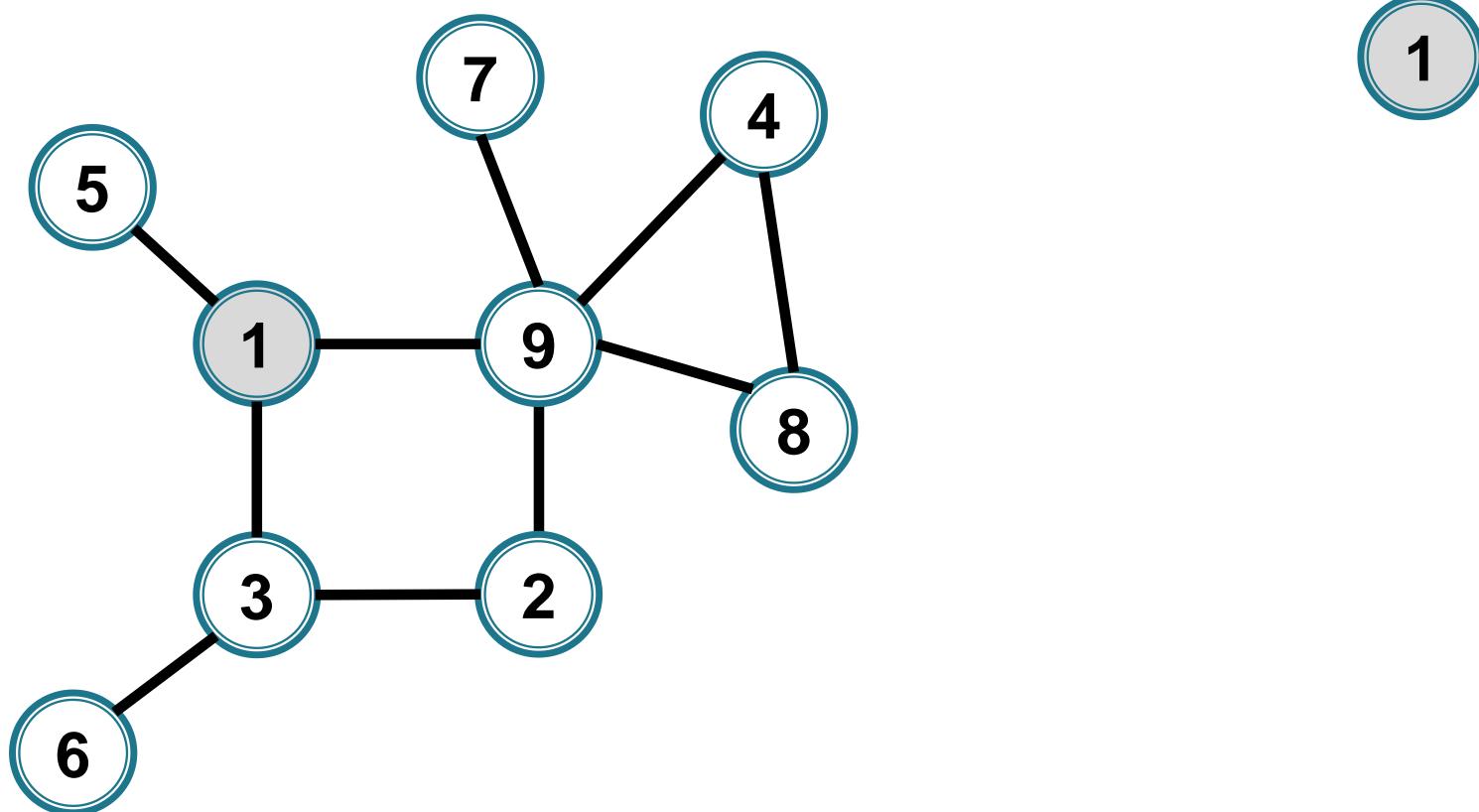
- **Initial:** vârful de start s – devine vârf curent
- **La un pas:**
 - se trece la primul vecin nevizitat al vârfului curent,
dacă există
 - altfel
 - se merge **înapoi** pe drumul de la s la vârful curent,
până se ajunge la un vârf cu vecini nevizitați
 -

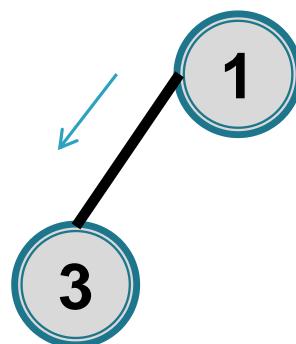
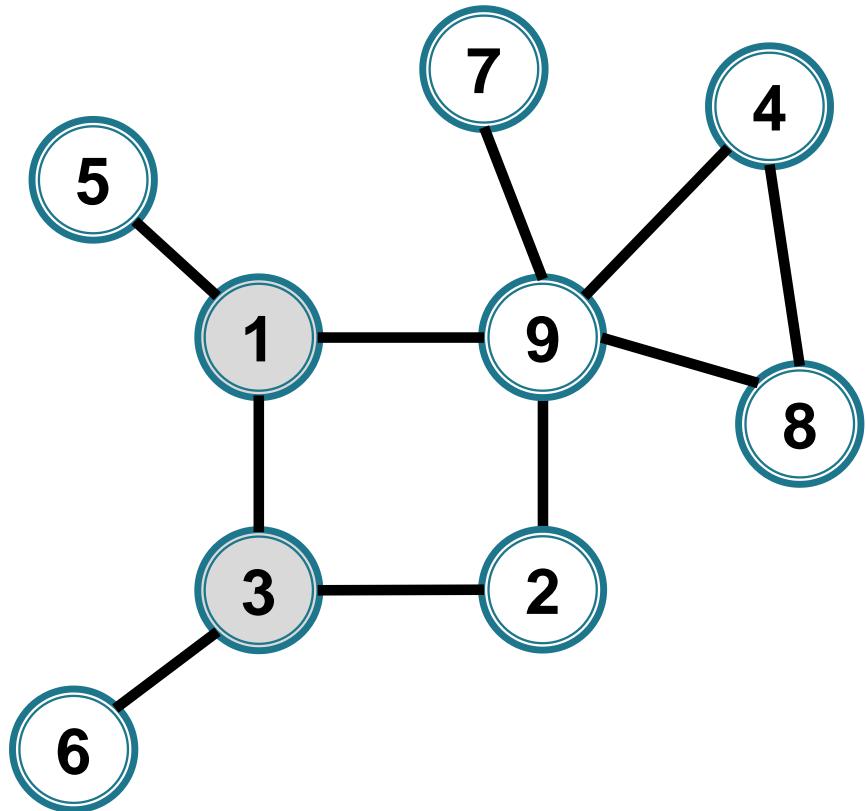
Parcurgerea în adâncime

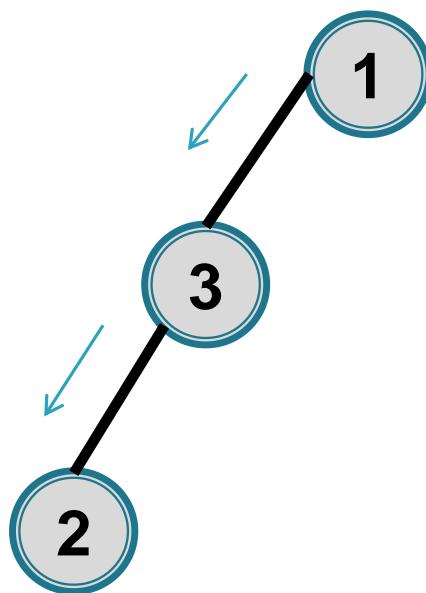
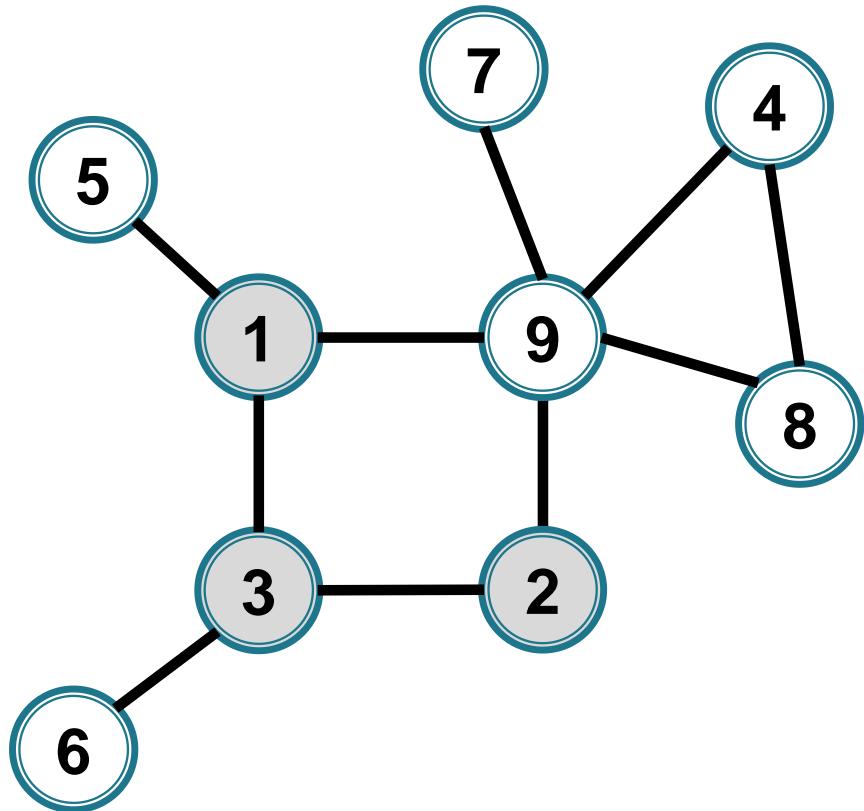
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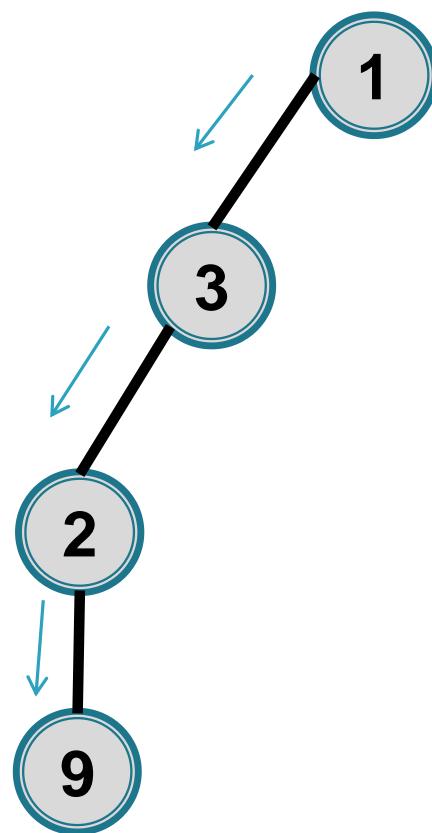
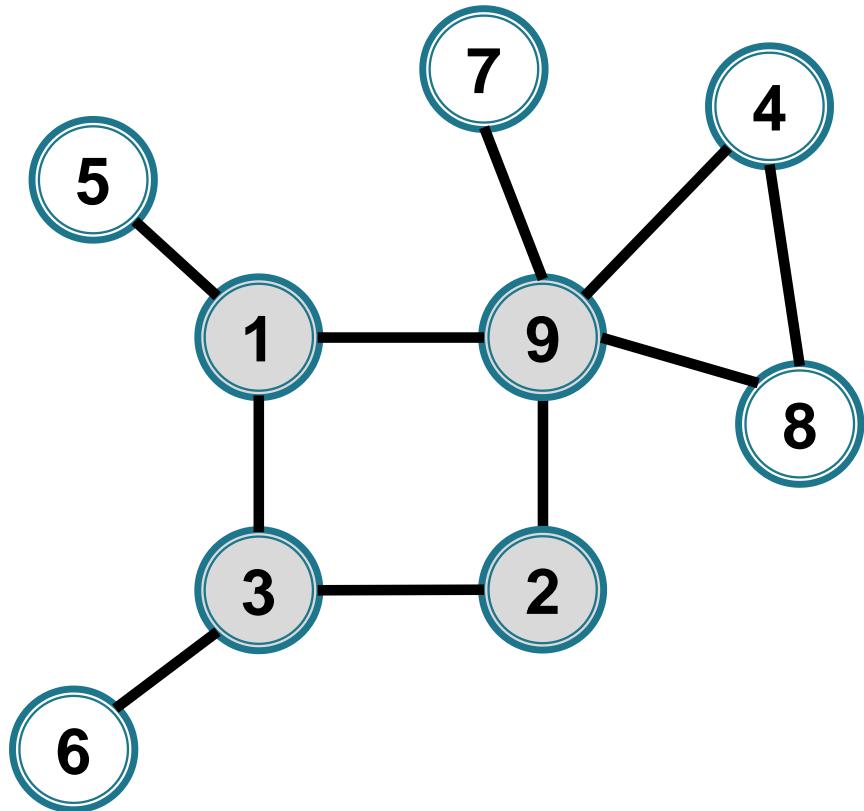
- Inițial: vârful de start s – devine vârf curent
- La un pas:
 - se trece la primul vecin nevizitat al vârfului curent,
dacă există
 - altfel
 - se merge **înapoi** pe drumul de la s la vârful curent,
până se ajunge la un vârf cu vecini nevizitați
 - se trece la **primul** dintre aceștia și se reia procesul

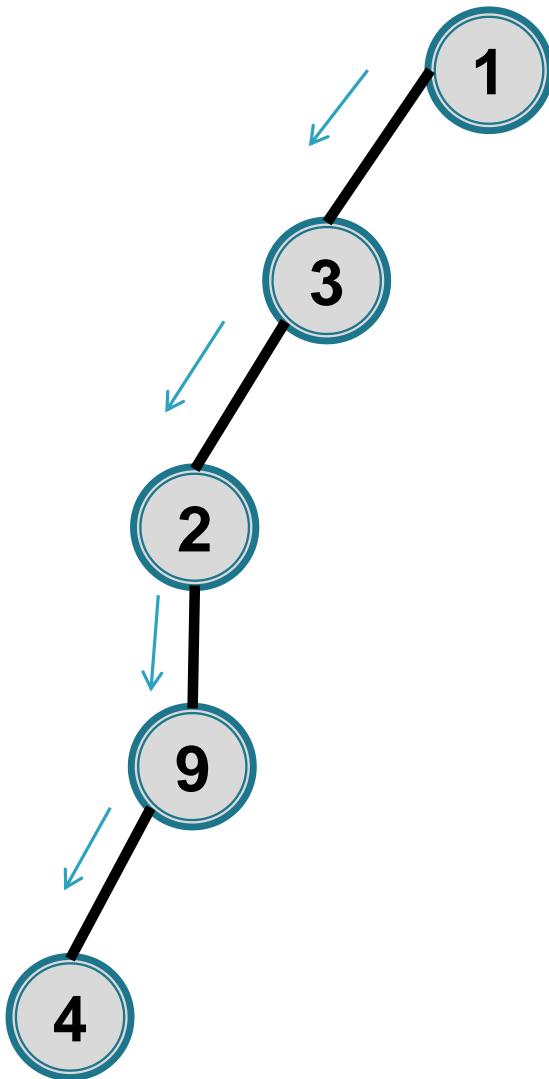
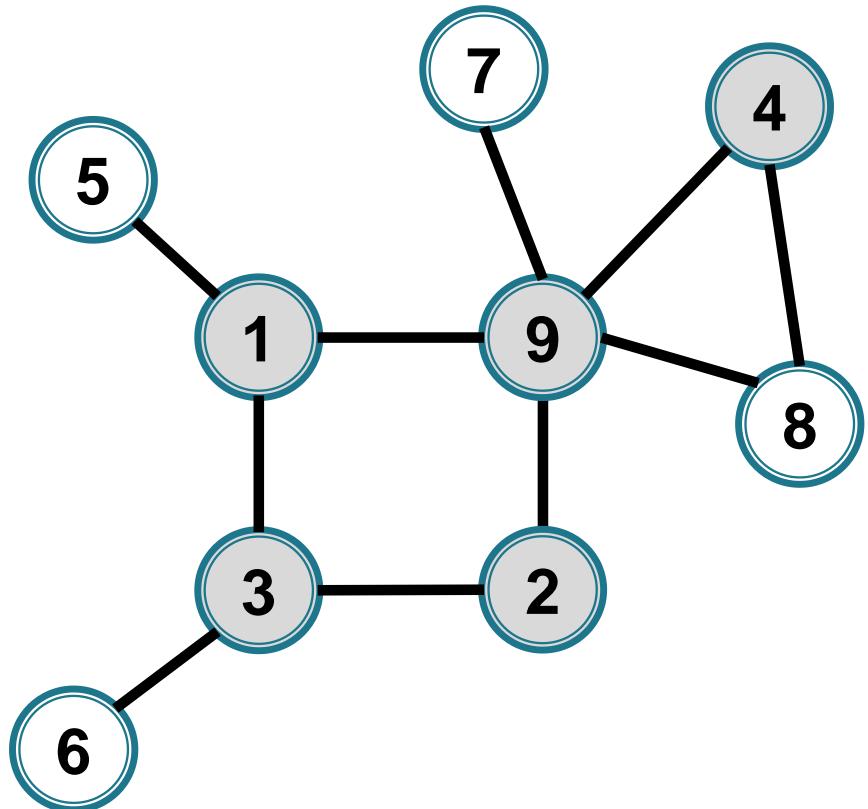


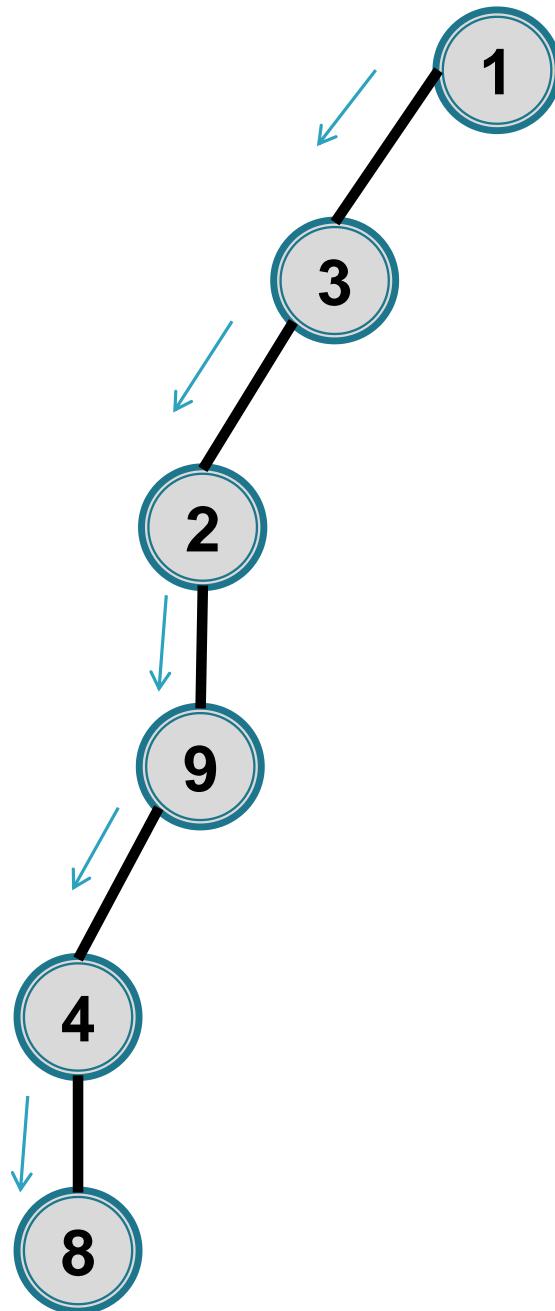
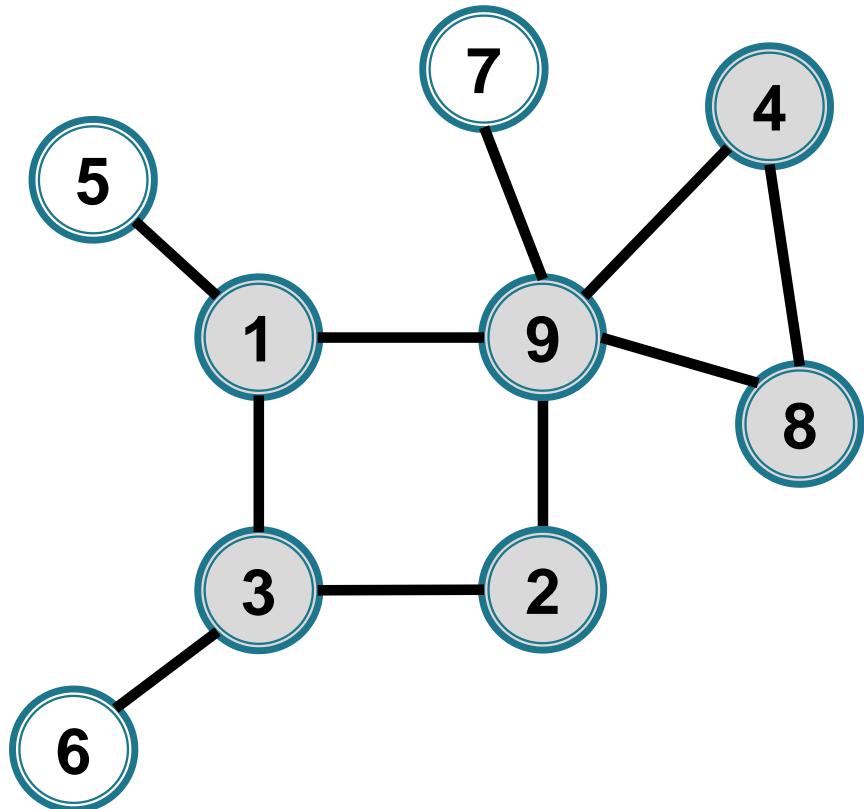


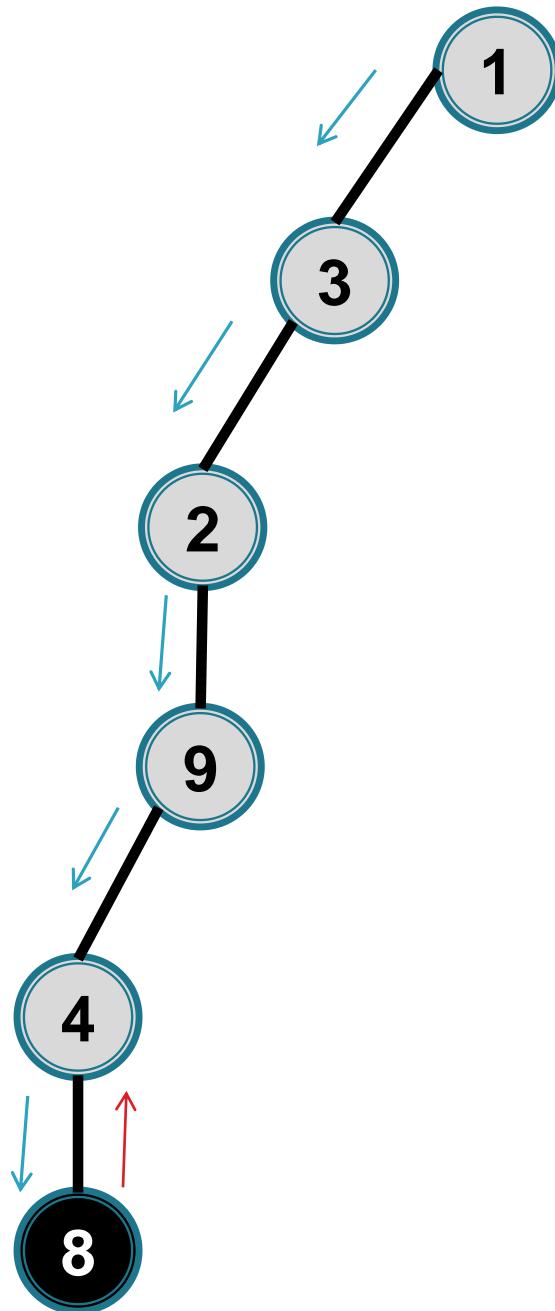
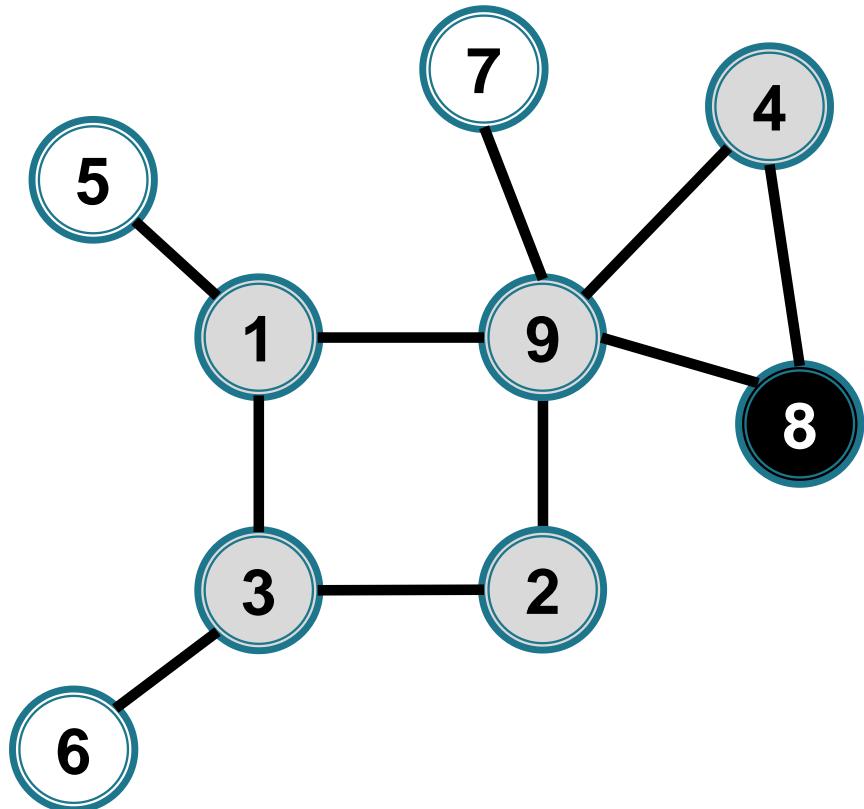


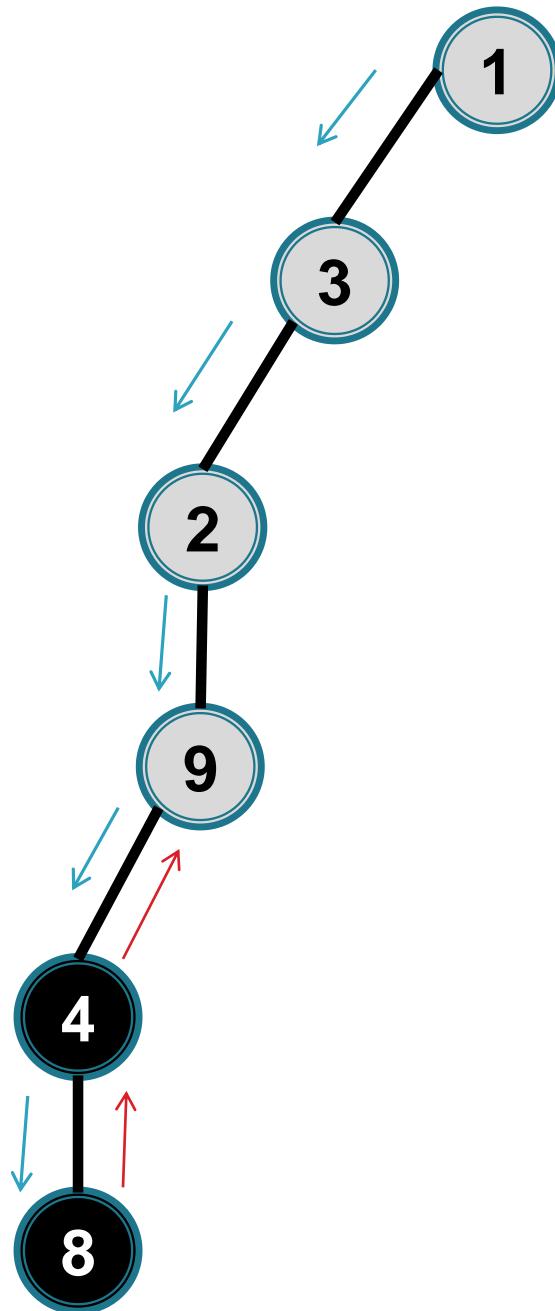
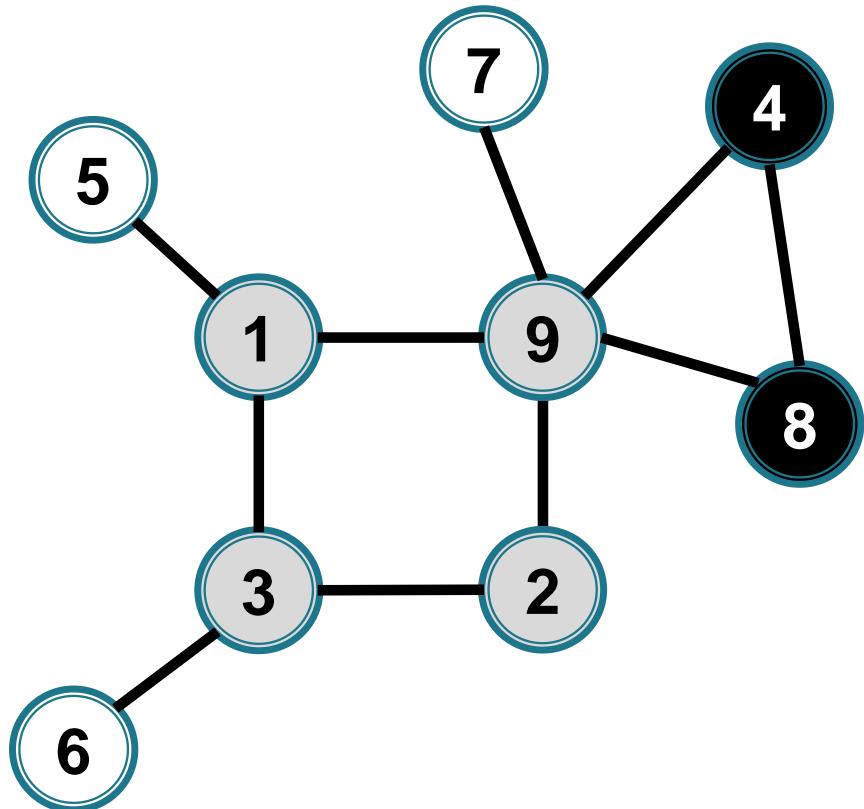


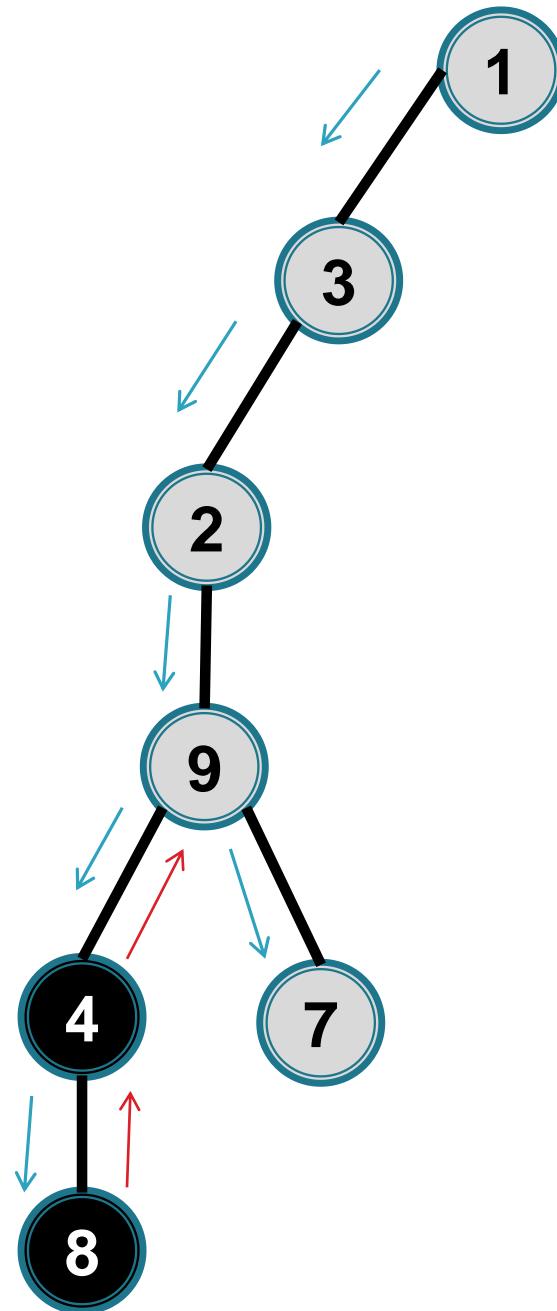
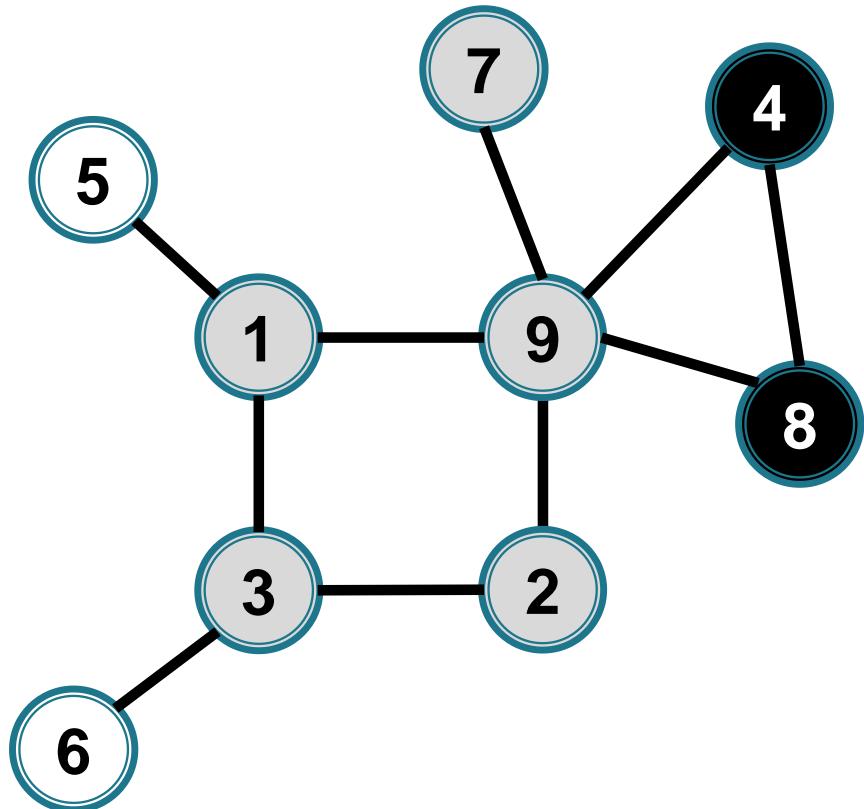


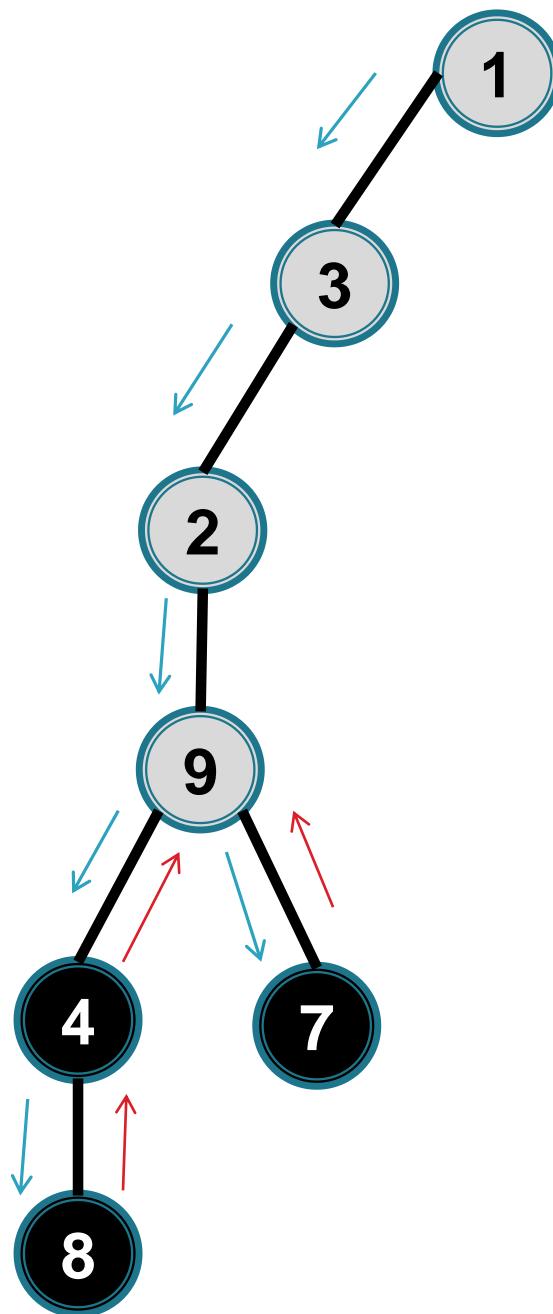
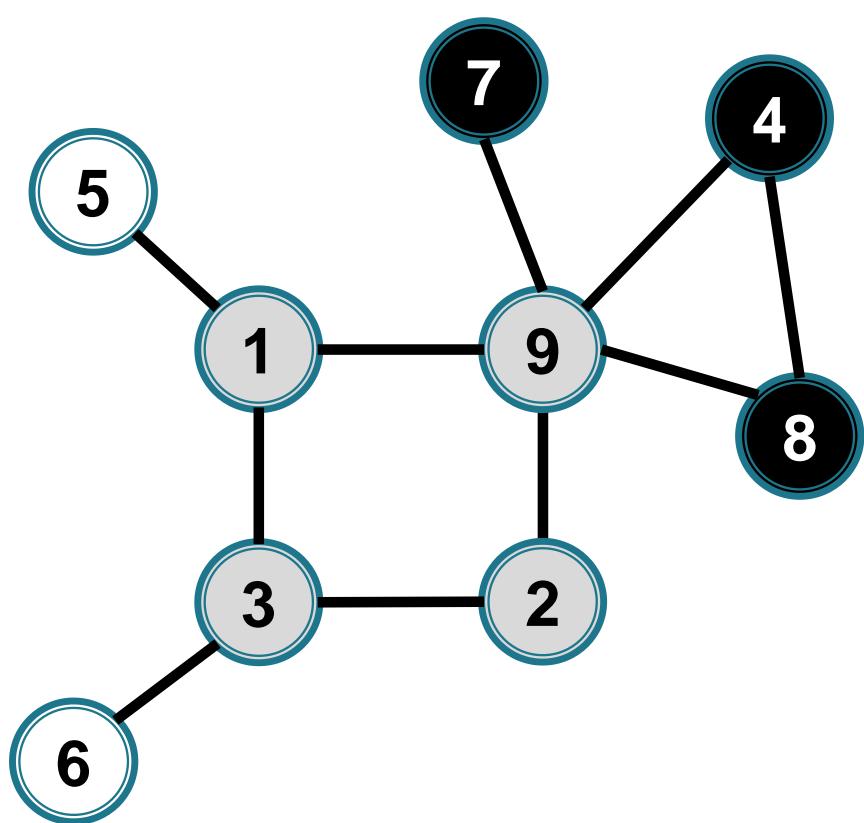


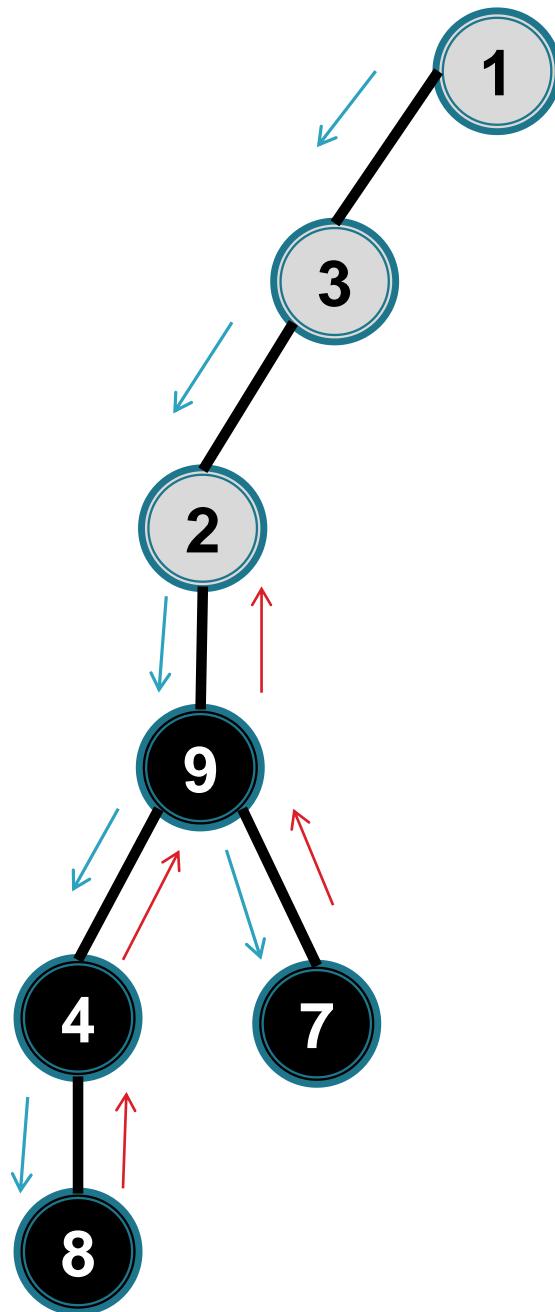
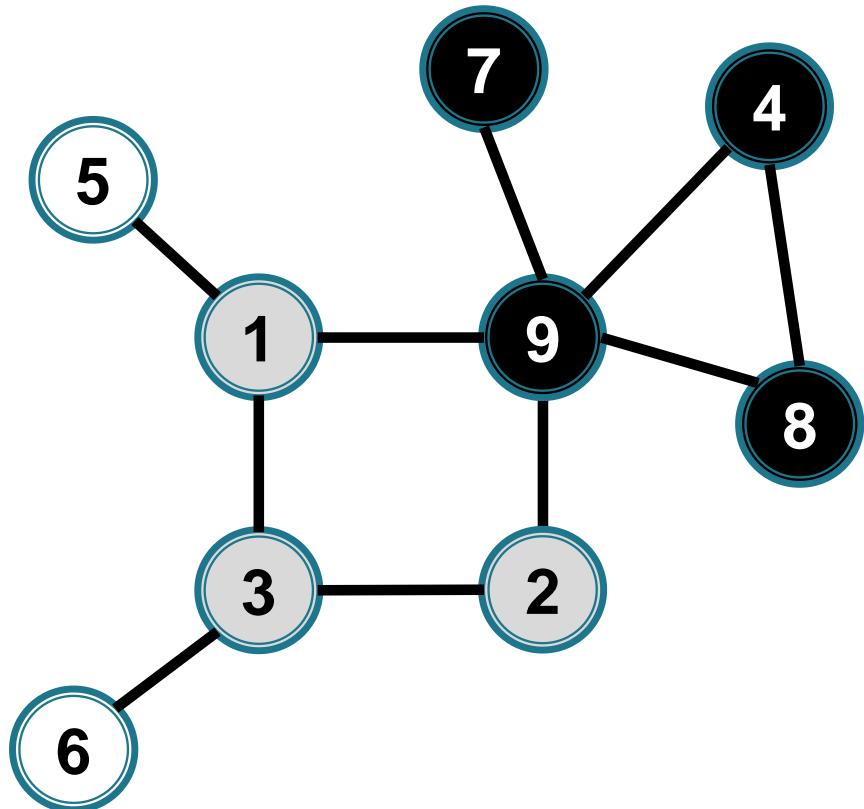


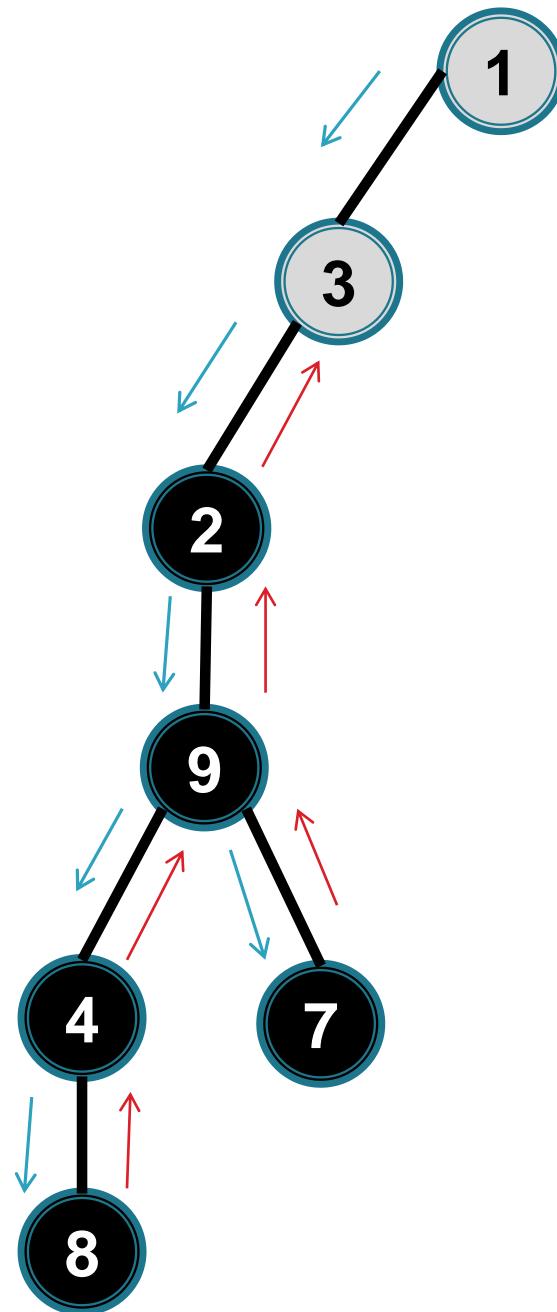
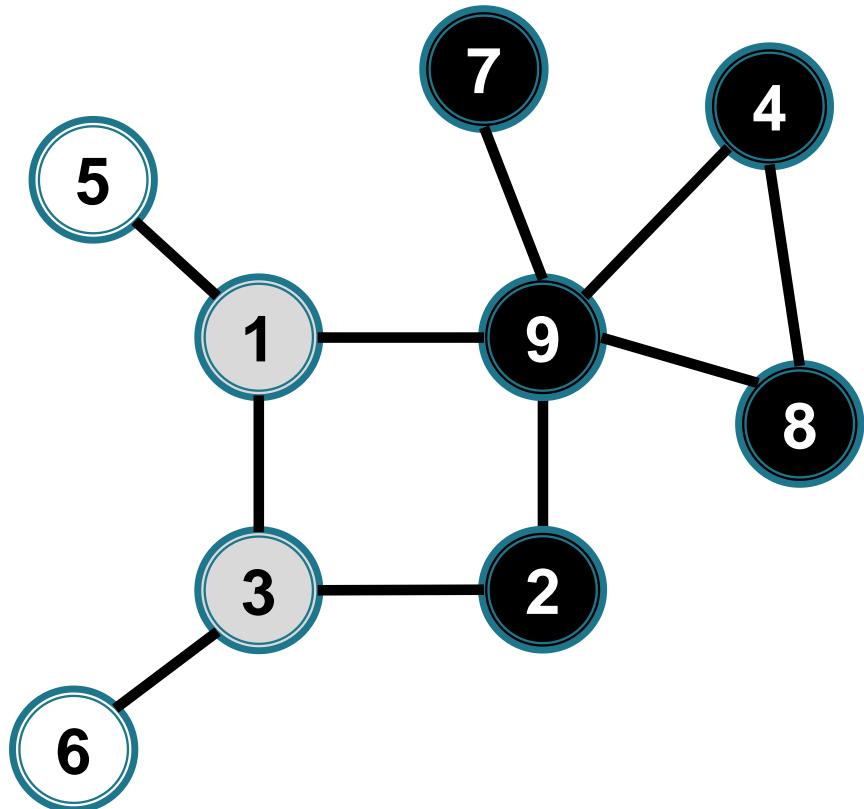


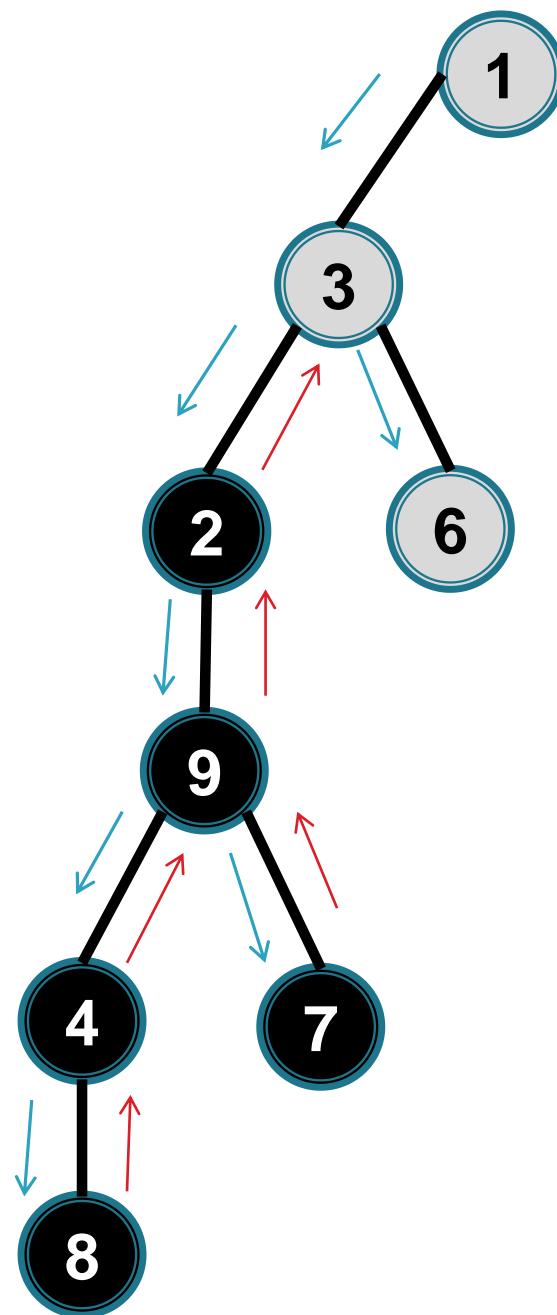
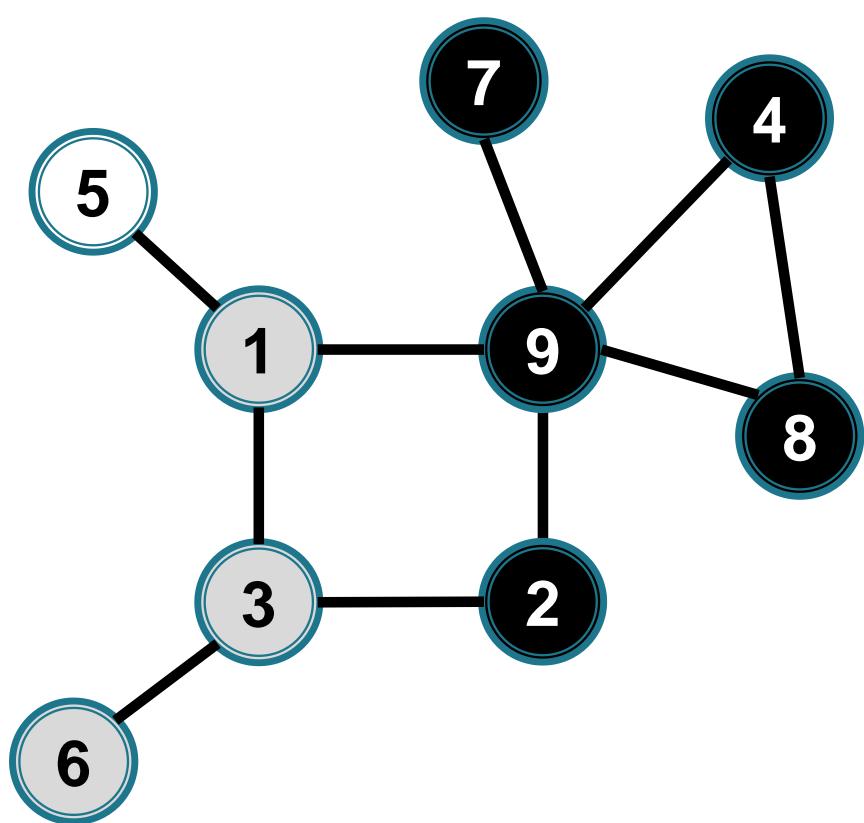


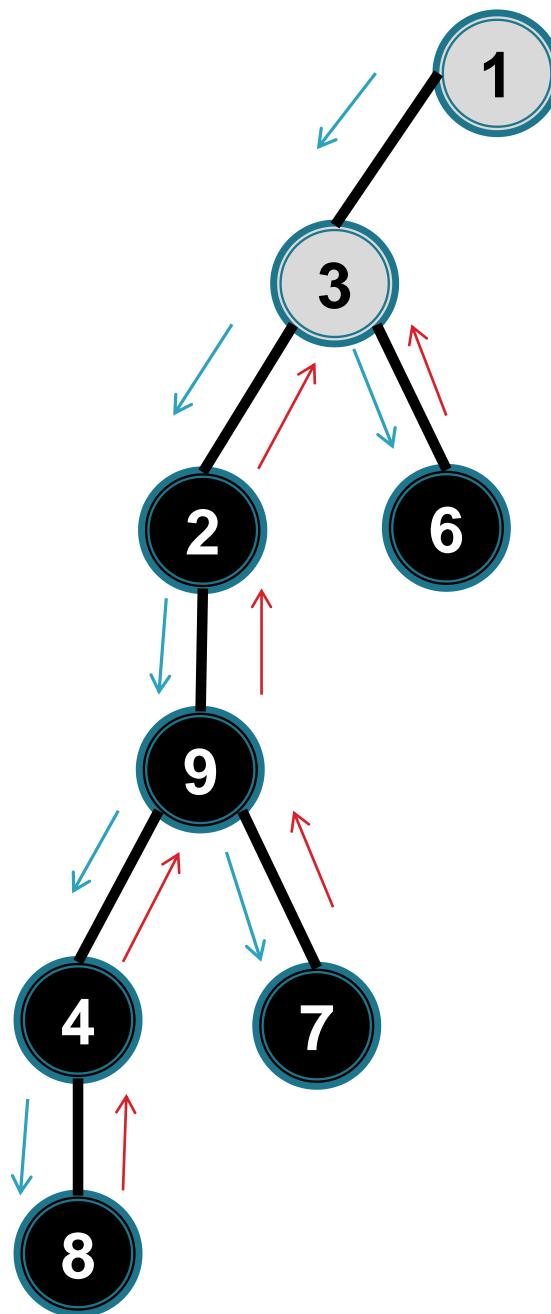
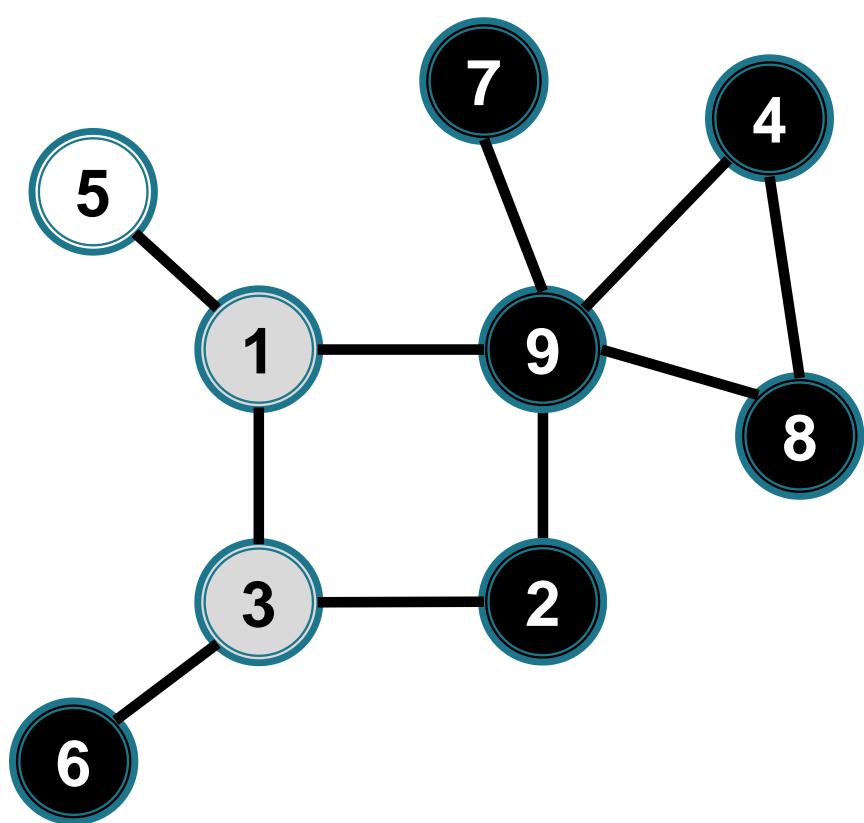


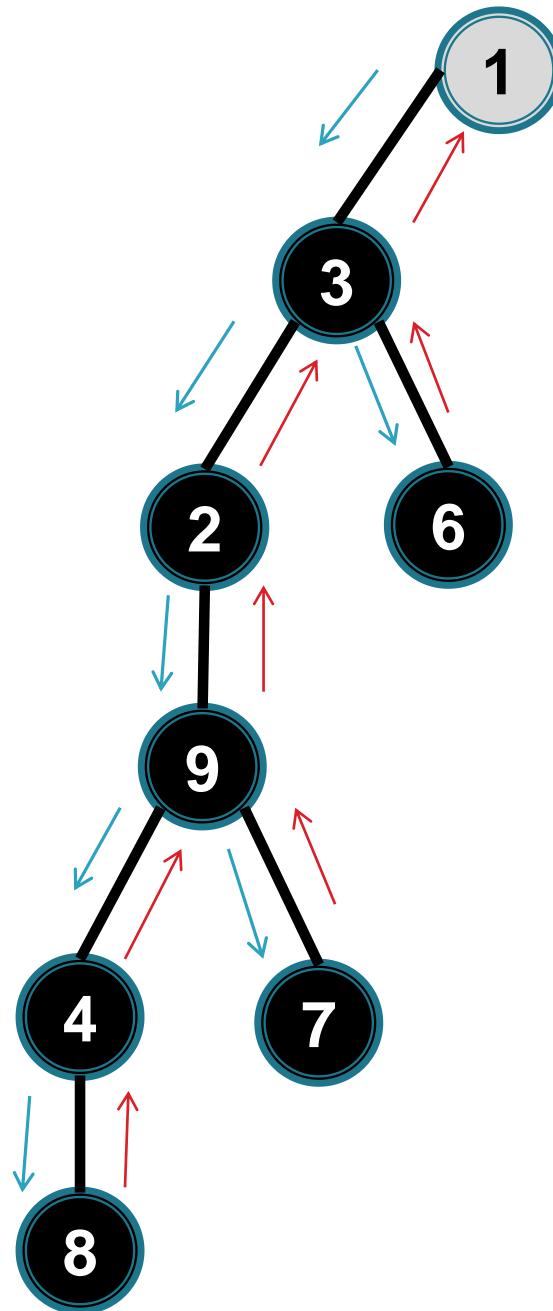
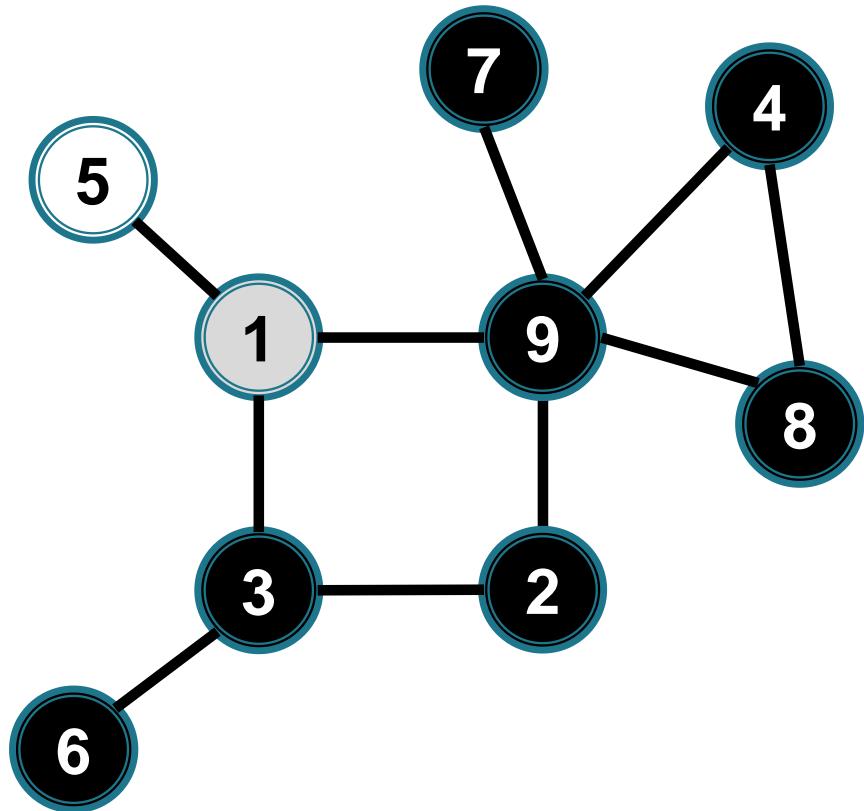


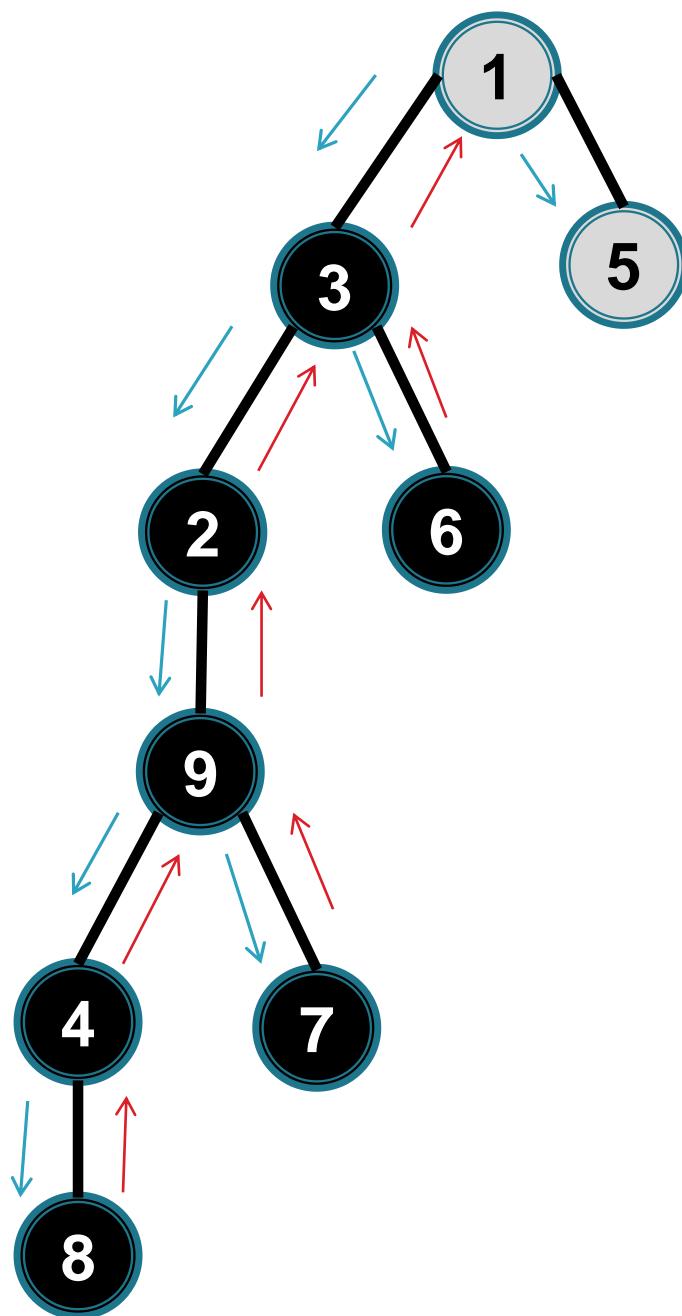
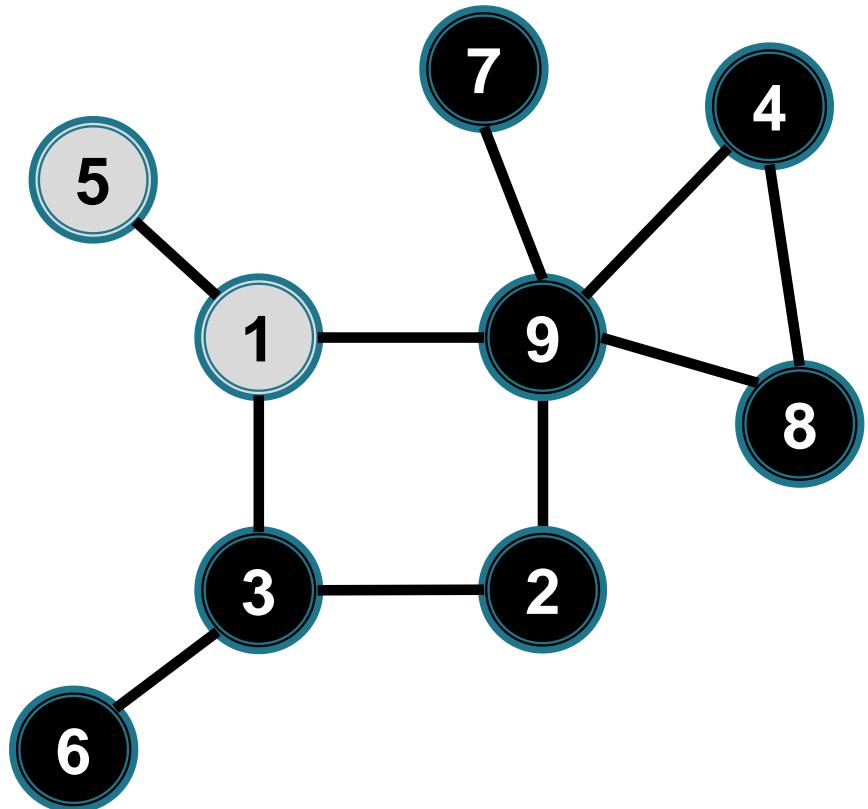


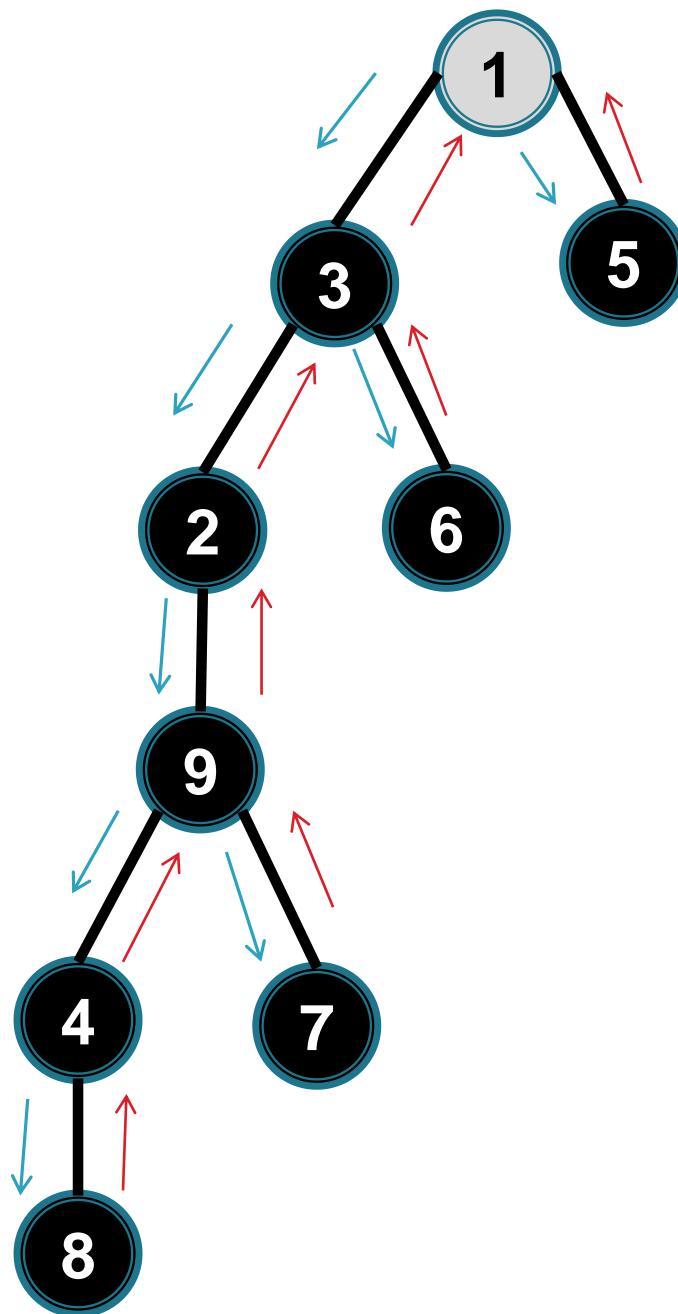
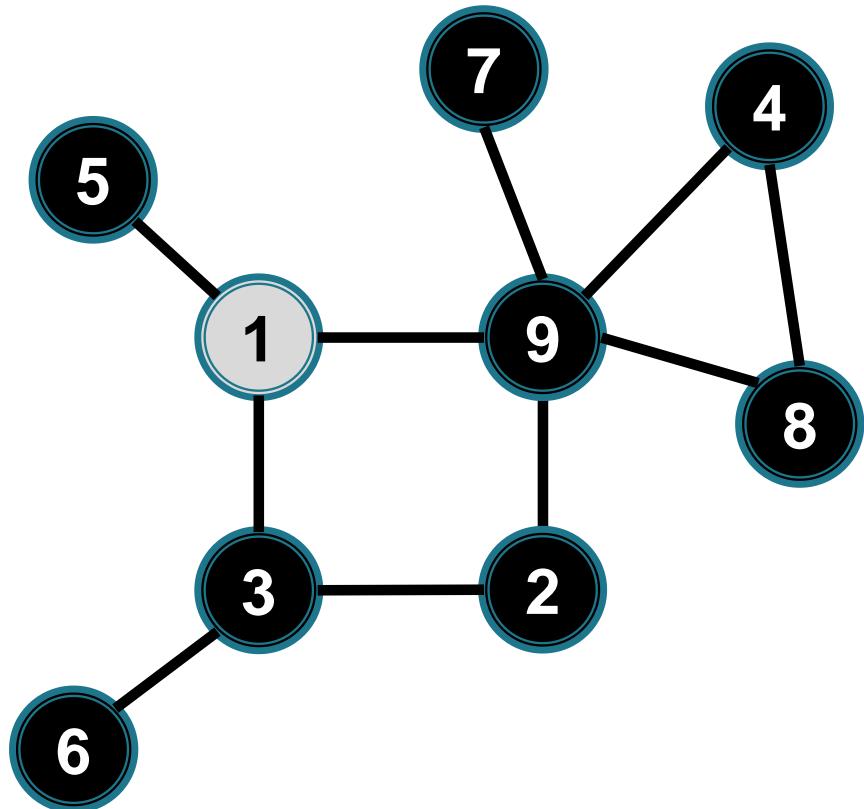


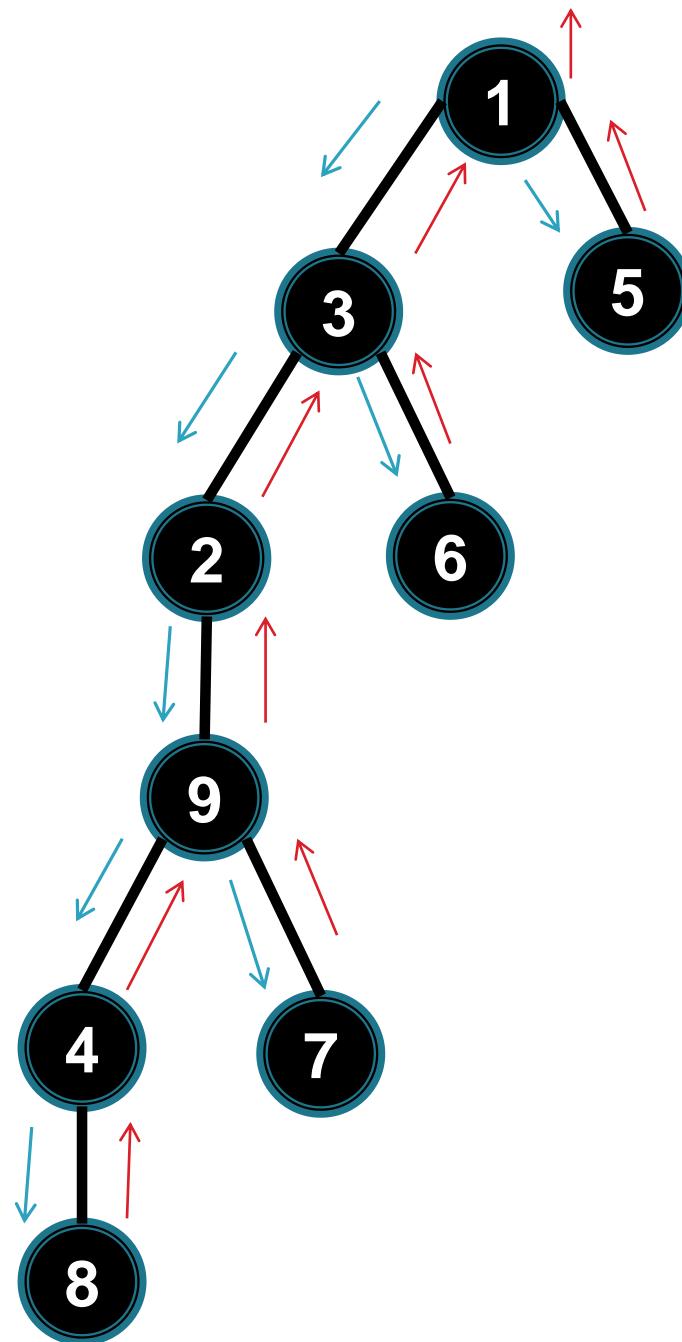
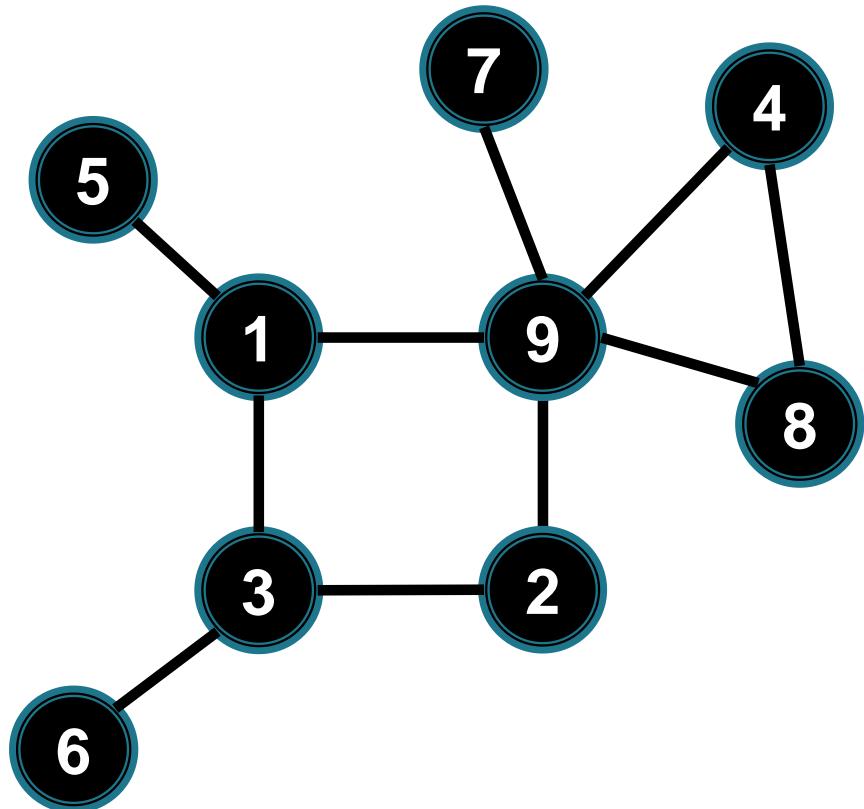


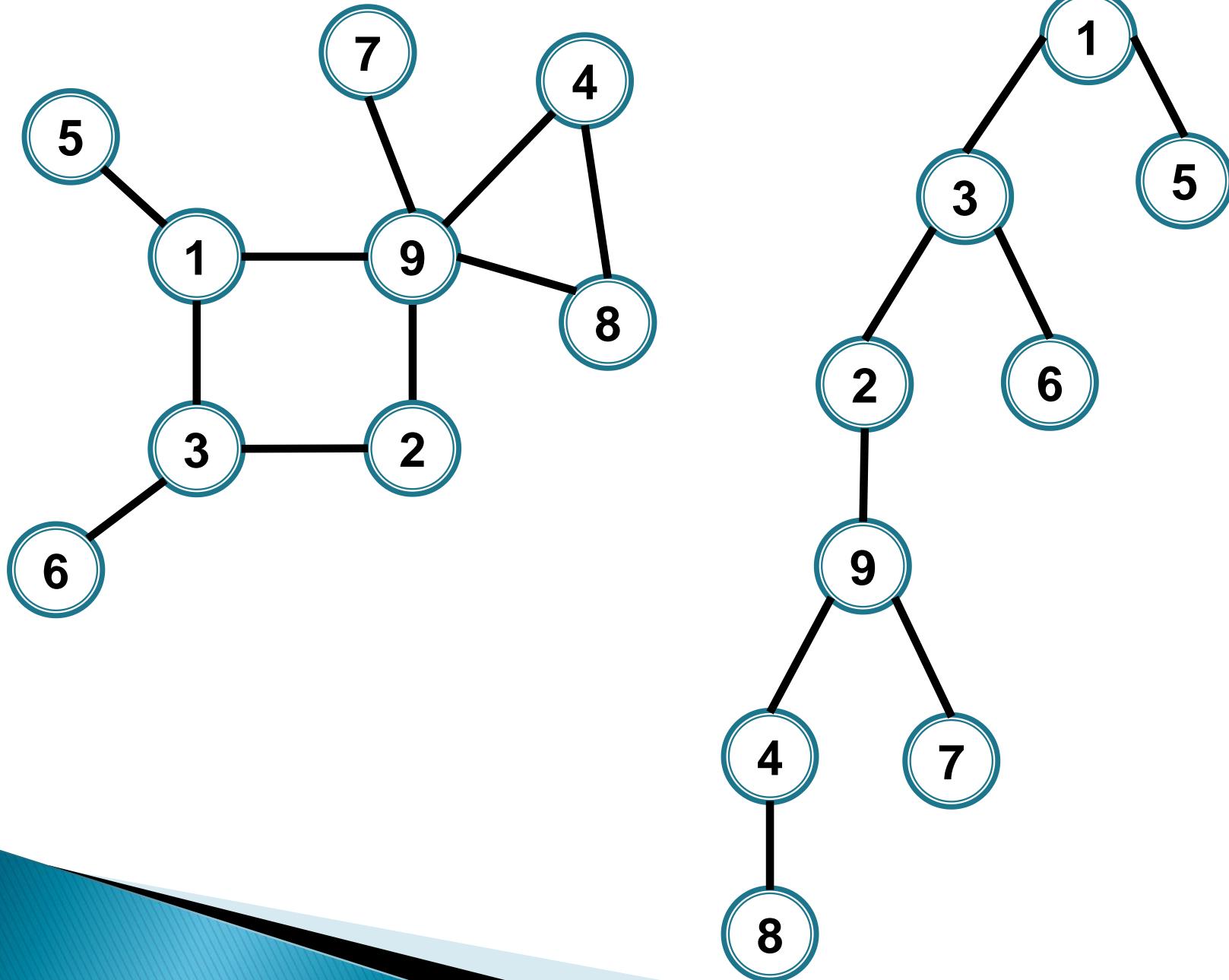












DFS (x)

```
//incepe explorarea varfului x
viz[x] = 1
pentru fiecare xy ∈ E //y vecin al lui x
    daca viz[y]==0 atunci
        tata[y] = x
        d[y] = d[x]+1 //nivel, nu distanta
        DFS(y)
//s-a finalizat explorarea varfului x
```

x alb

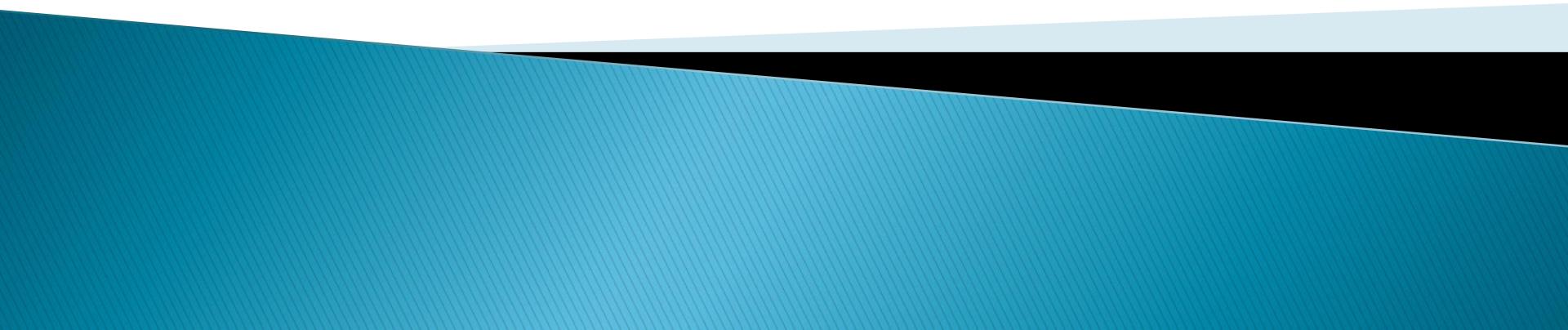
x gri

x negru

Apel:

DFS(s)

Proprietăți



Proprietăți DF

Starea unui vârf:

- **nevizitat** – culoarea albă
- **în explorare** – culoare gri
- **finalizat** – culoare neagră

Proprietăți DF

Dacă menținem pe parcursul algoritmului o variabilă de timp care se modifică atunci când se schimbă starea unui vârf (îl descoperim sau îl finalizăm), putem asocia fiecărui vârf două valori:

- ▶ $\text{desc}[v]$ – momentul la care vârful a fost descoperit
(a devenit **gri**)
- ▶ $\text{fin}[v]$ – momentul la care vârful a fost finalizat
(a devenit **negru**)

Proprietăți DF

Dacă dorim determinarea unor elemente de structură în graf precum circuite, componente tare conexe etc poate fi util să memorăm în parcurgerea DFS culoarea fiecărui vârf și/sau momentul în care a fost descoperit sau finalizat.

Dacă memorăm culoarea fiecărui vârf, nu mai este necesar și vectorul vizitat, deoarece

$$\text{viz}[x] = 0 \Leftrightarrow \text{culoare}[x] = \text{alb}$$

Un pseudocod complet în acest caz este următorul:

DFS (x)

```
culoare[x] = gri
timp = timp + 1
desc[x]= timp; //incepe explorarea varfului x
pentru fiecare xy ∈ E //y vecin al lui x
    daca culoare[y]==alb atunci
        tata[y] = x
        d[y] = d[x]+1 //nivel, nu distanta
        DFS(y)
culoare[x] = negru
timp = timp + 1
fin[x] = timp //s-a finalizat explorarea varfului x
```

Apel:

pentru fiecare x in V executa

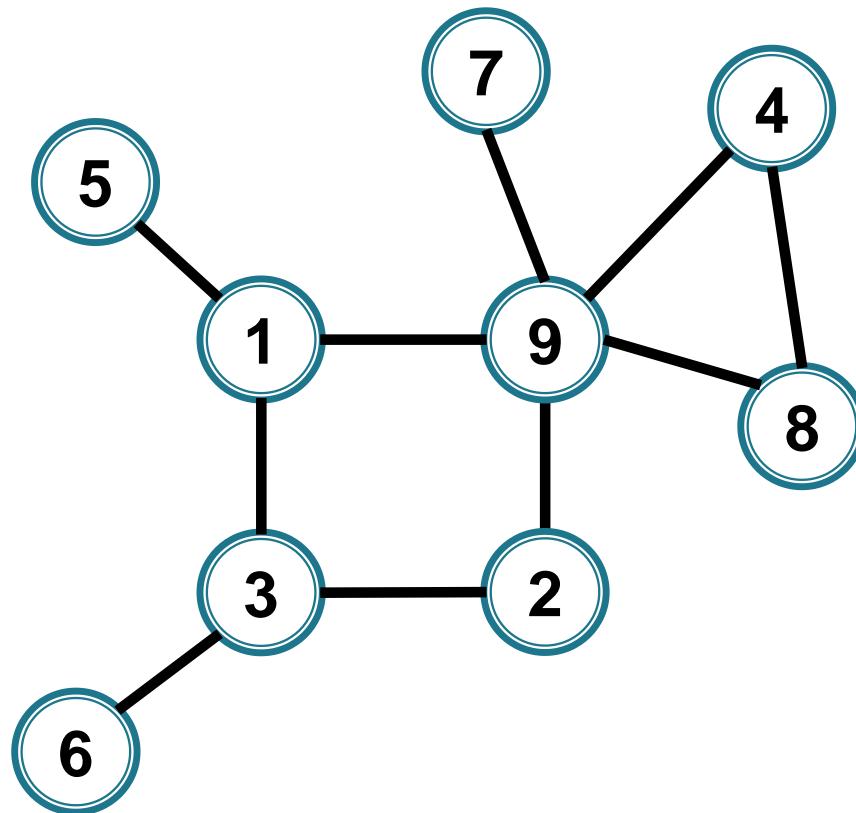
```
    culoare[x] = alb
```

timp = 0

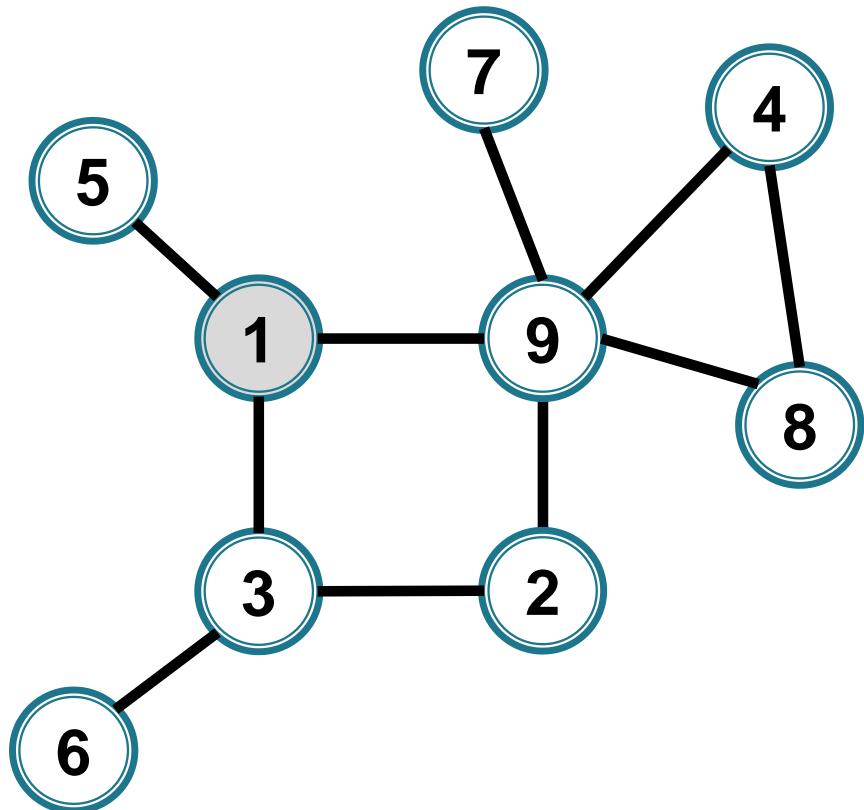
pentru fiecare x in V executa

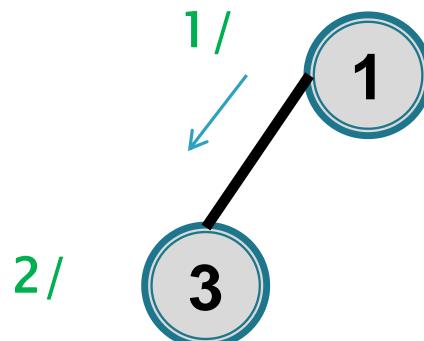
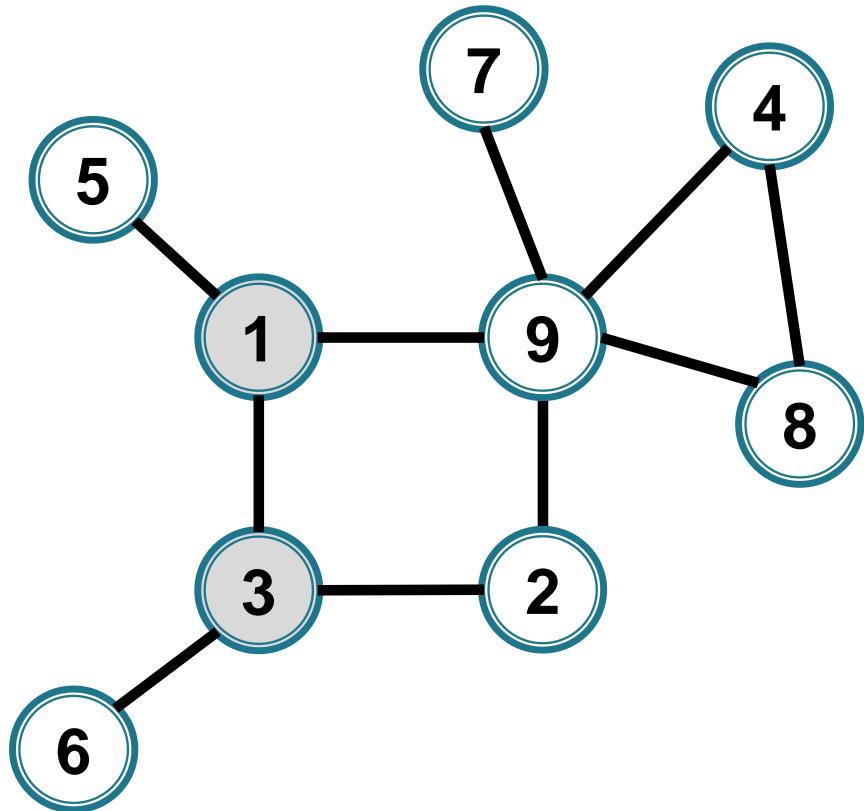
```
    daca culoare[x] == alb atunci
```

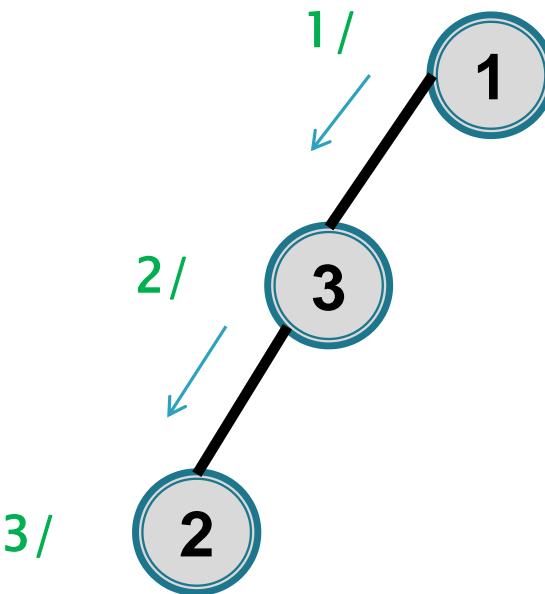
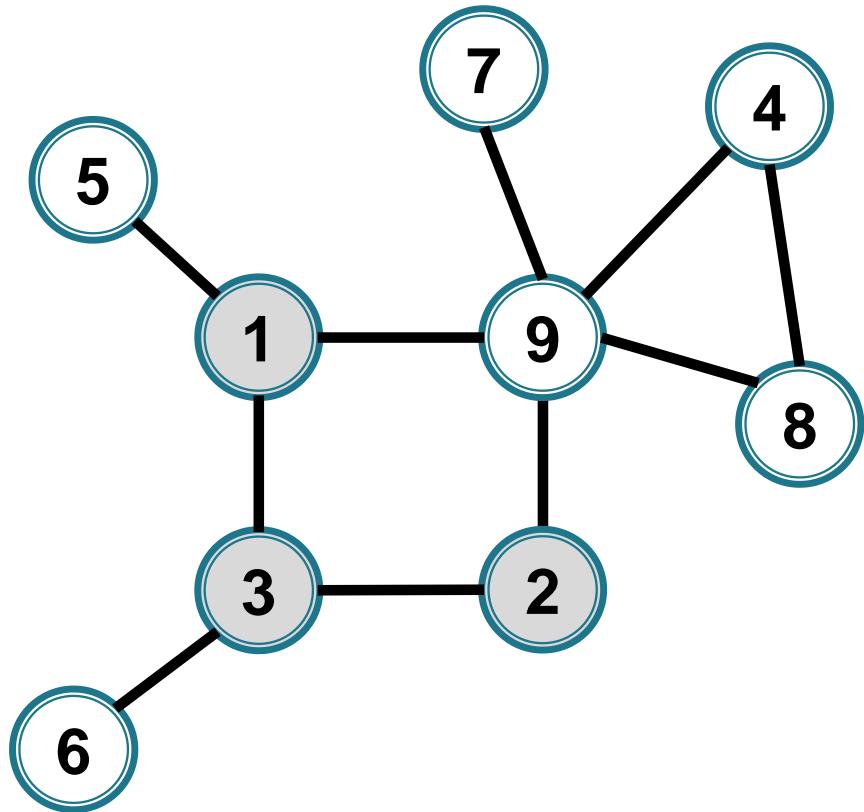
DFS(x)

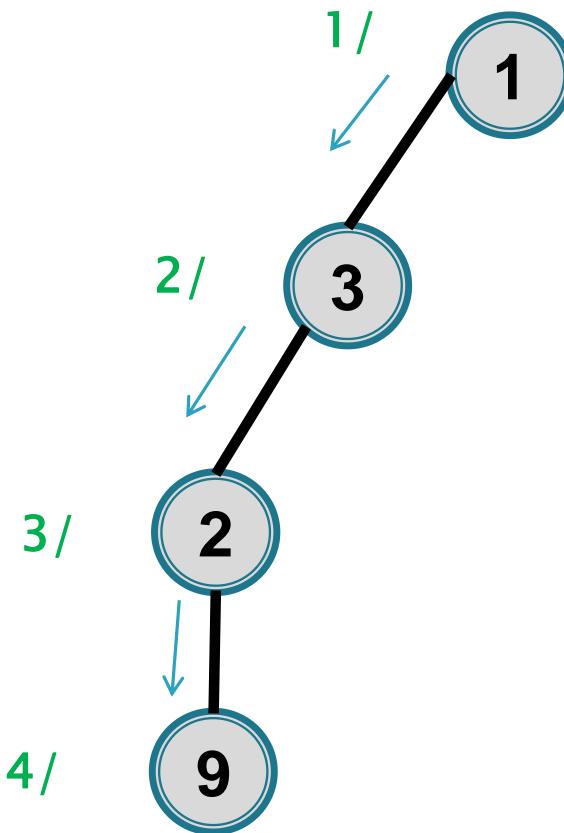
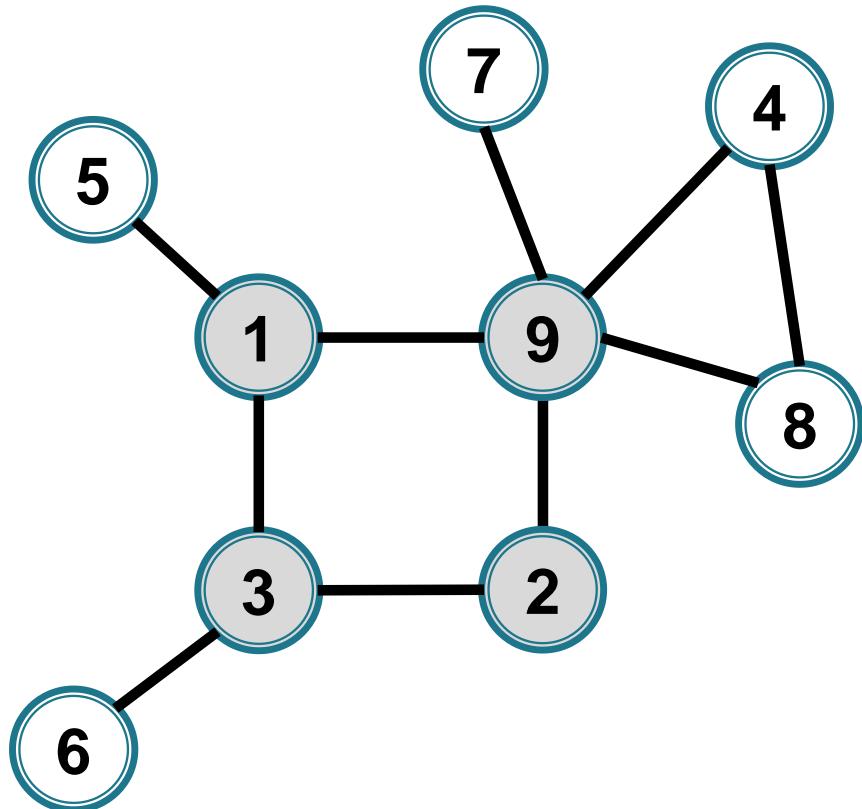


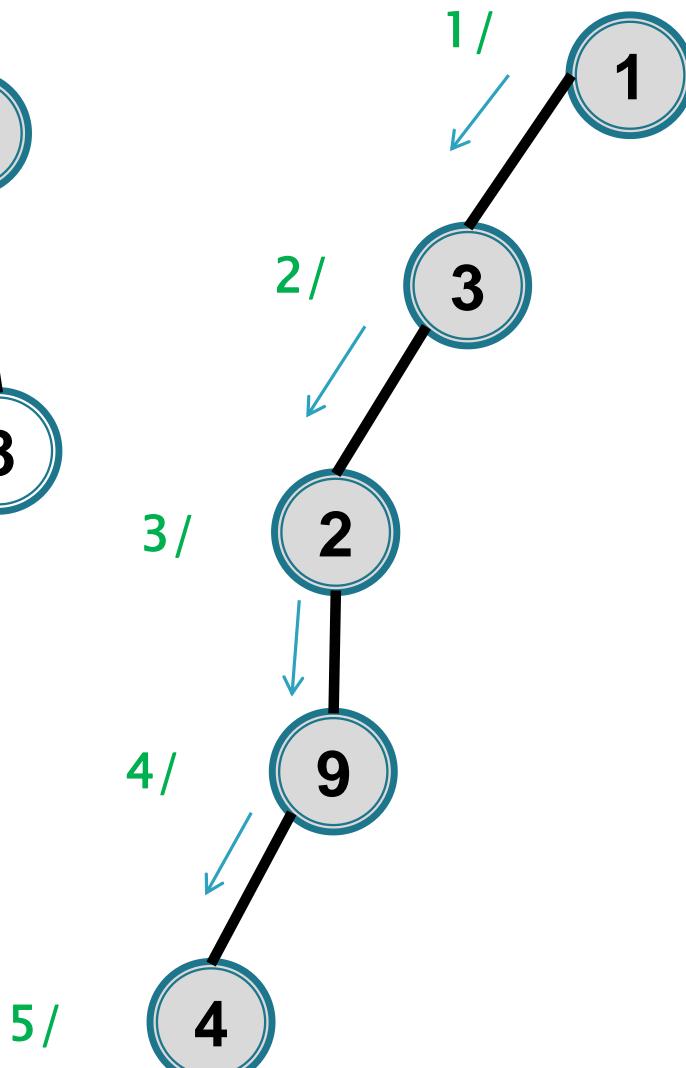
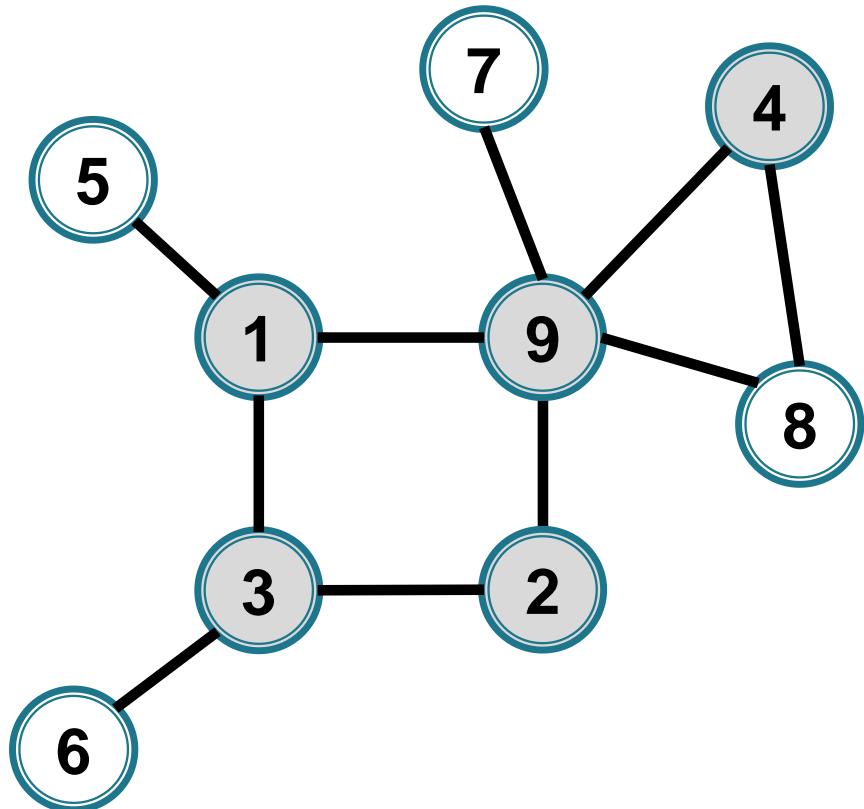
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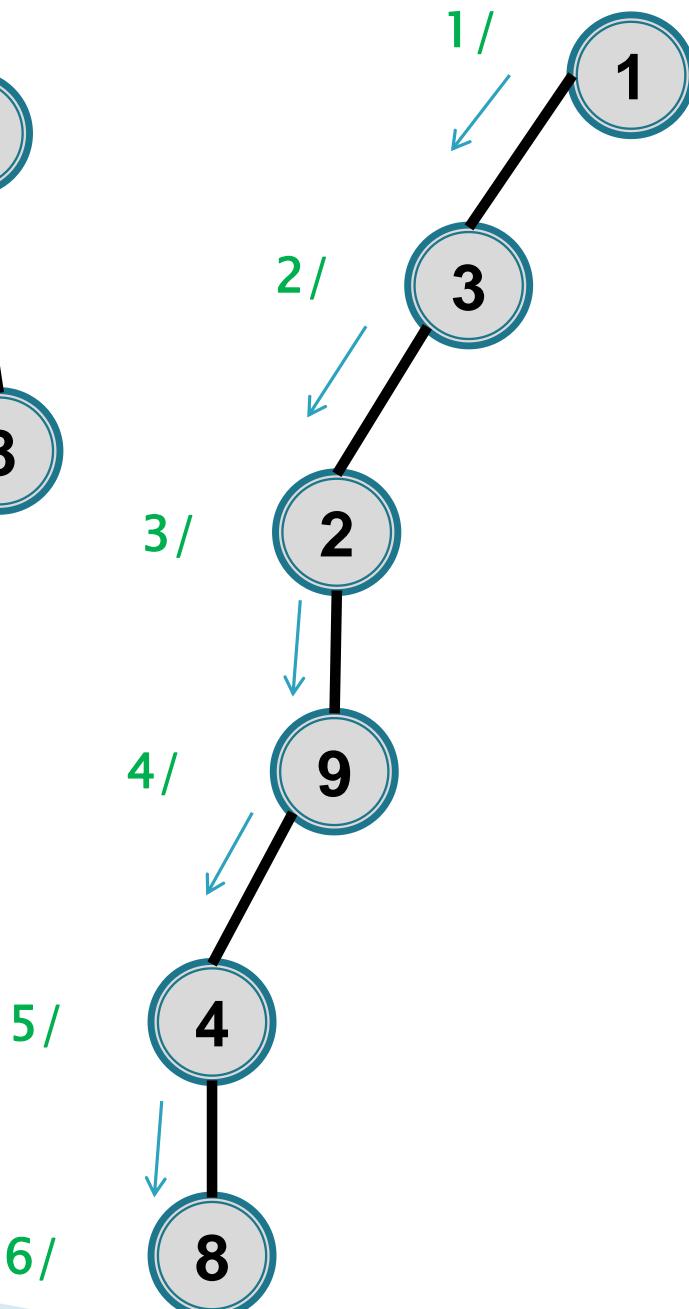
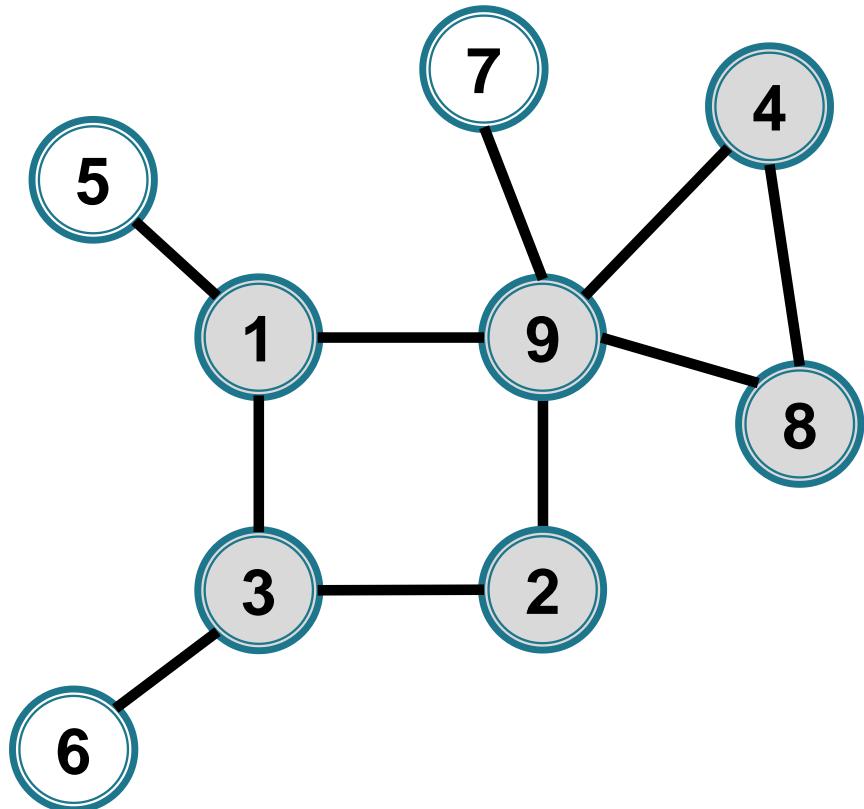


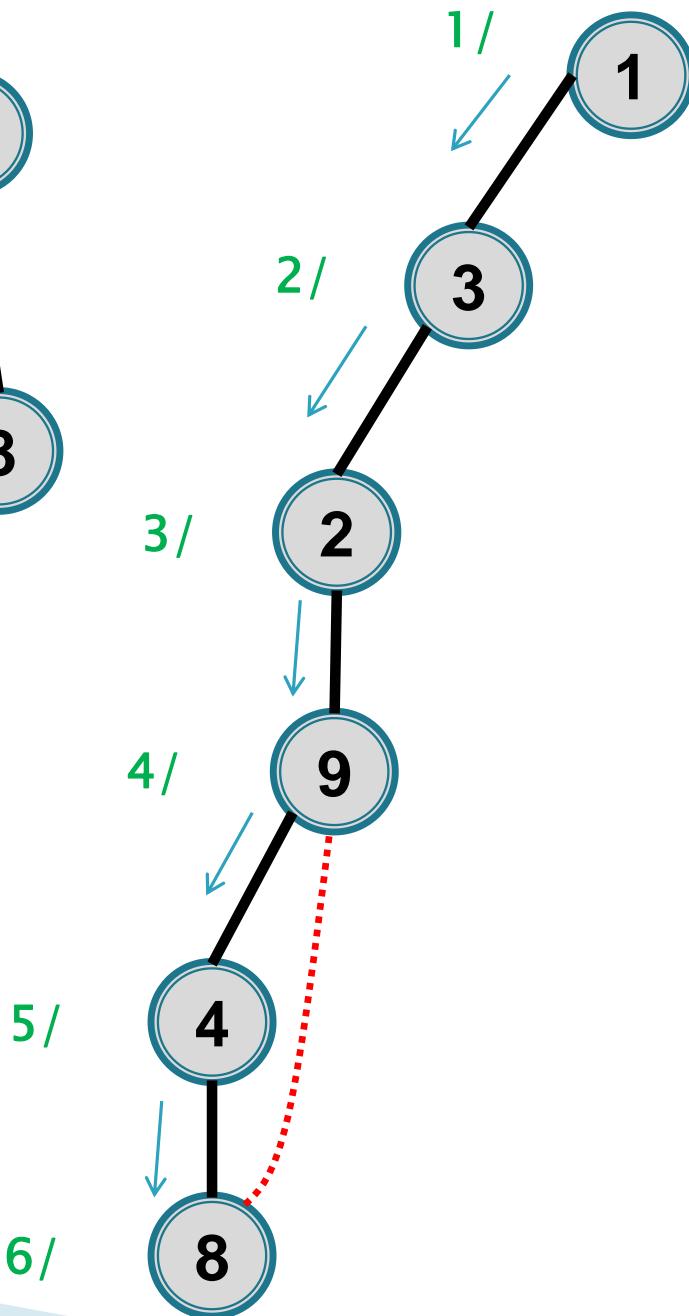
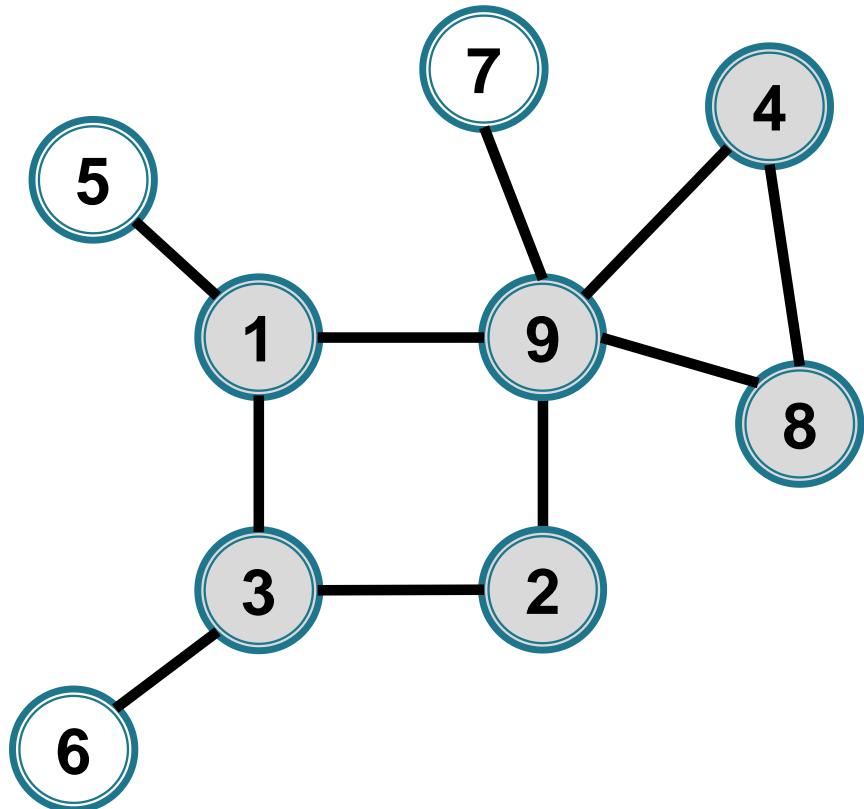


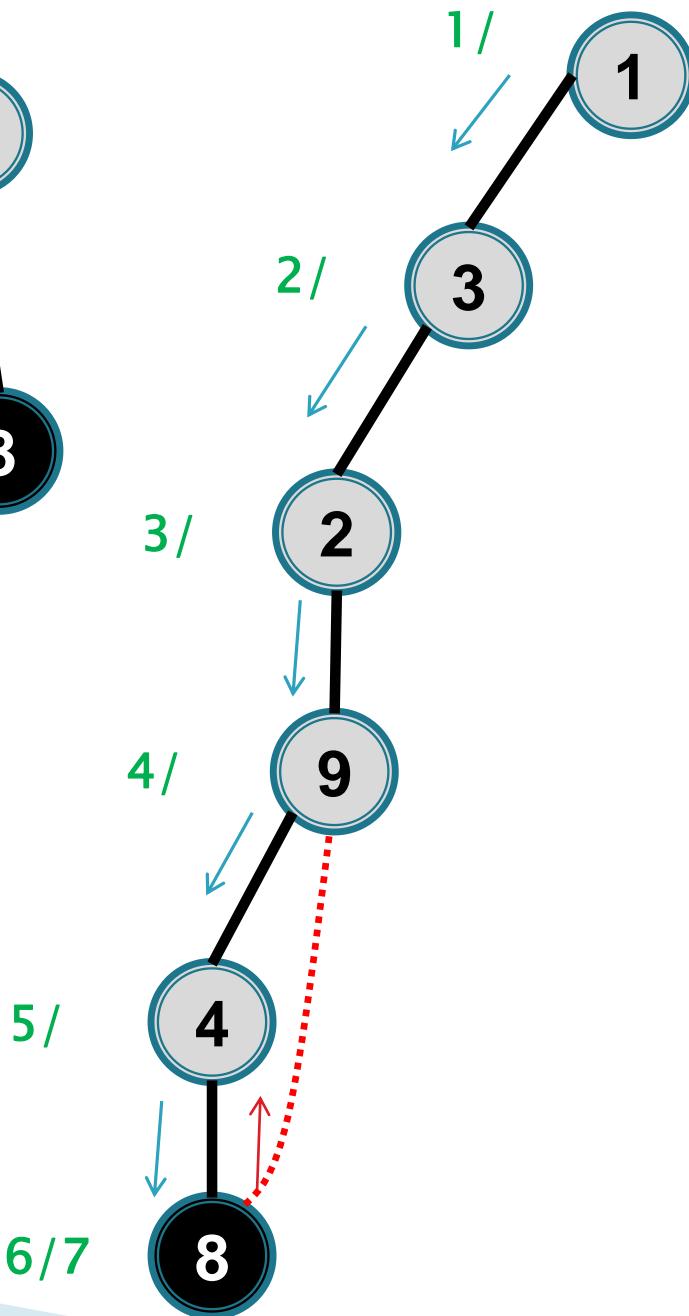
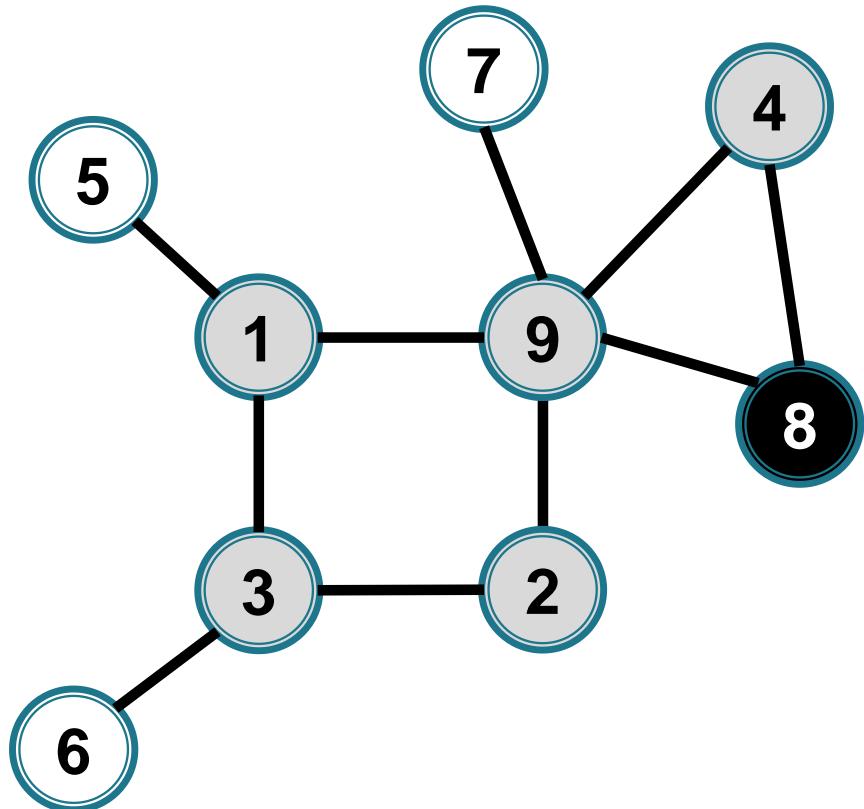


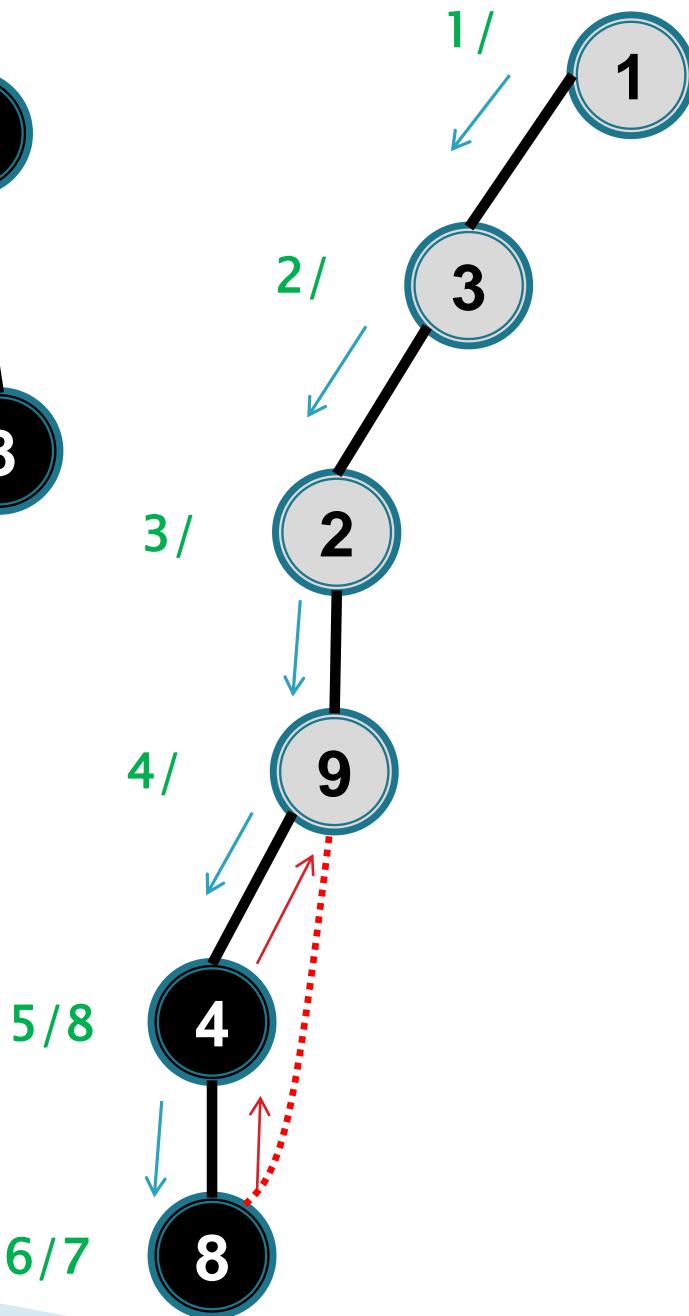
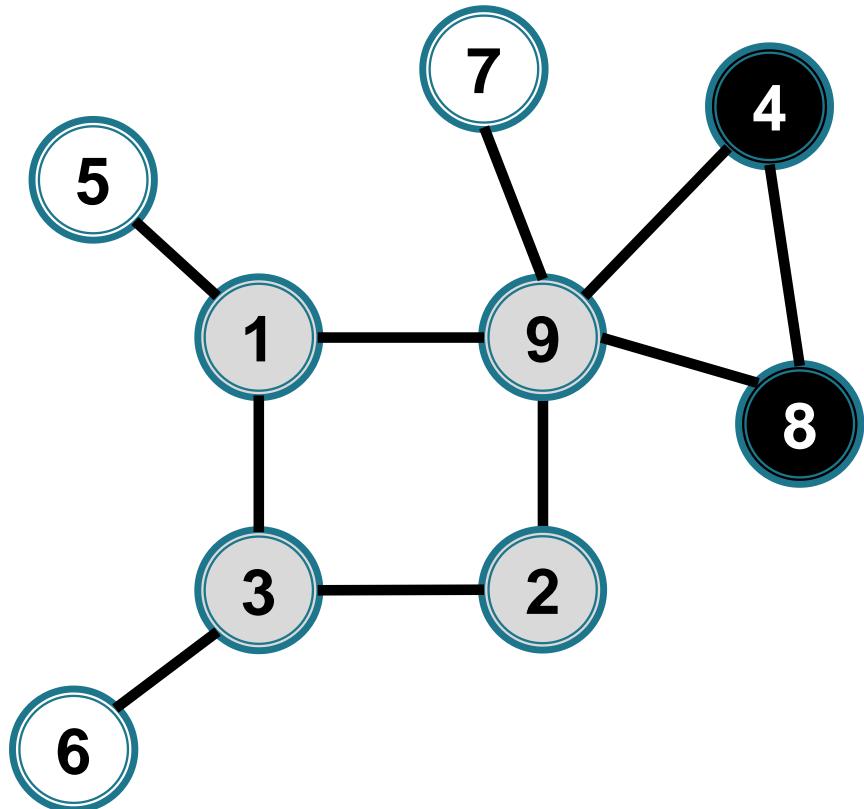


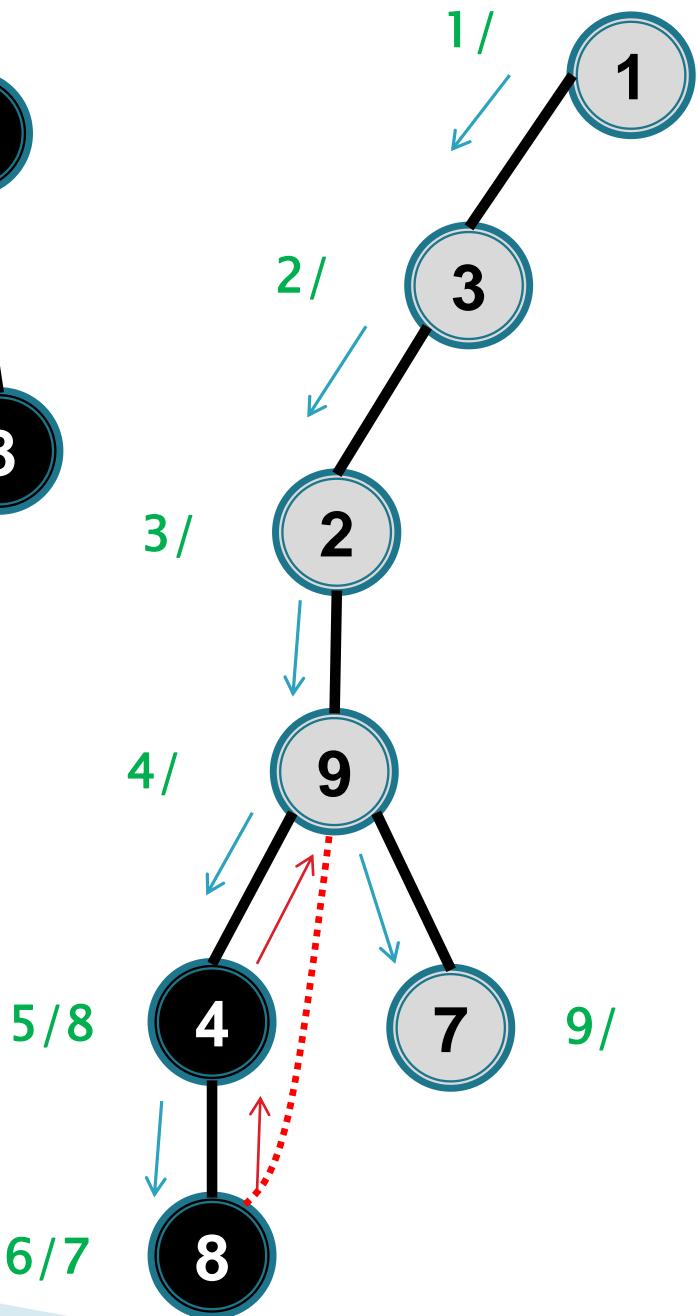
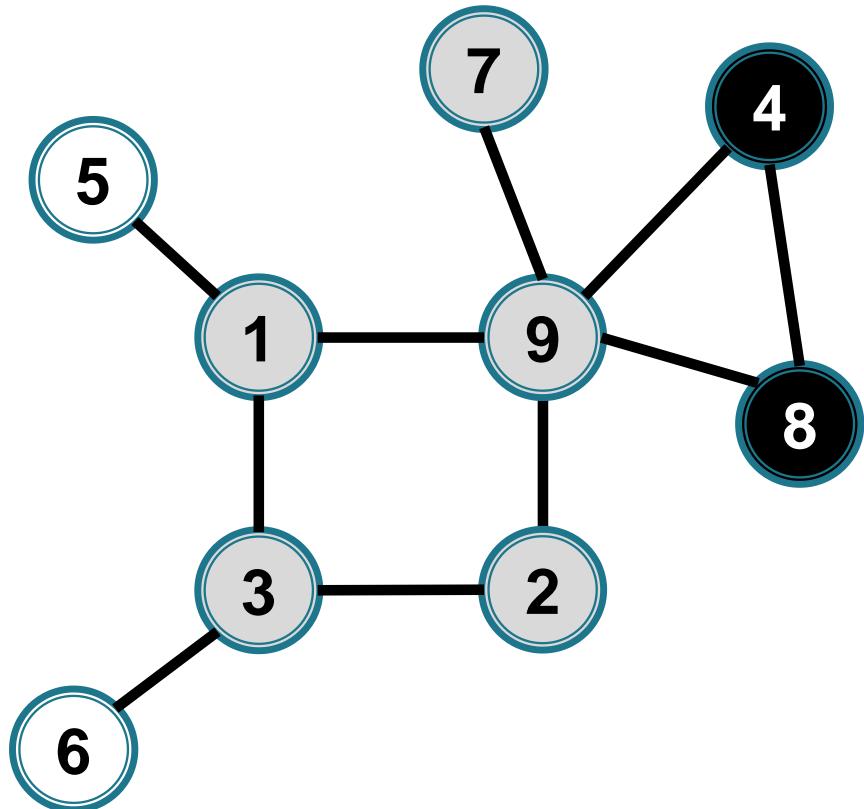


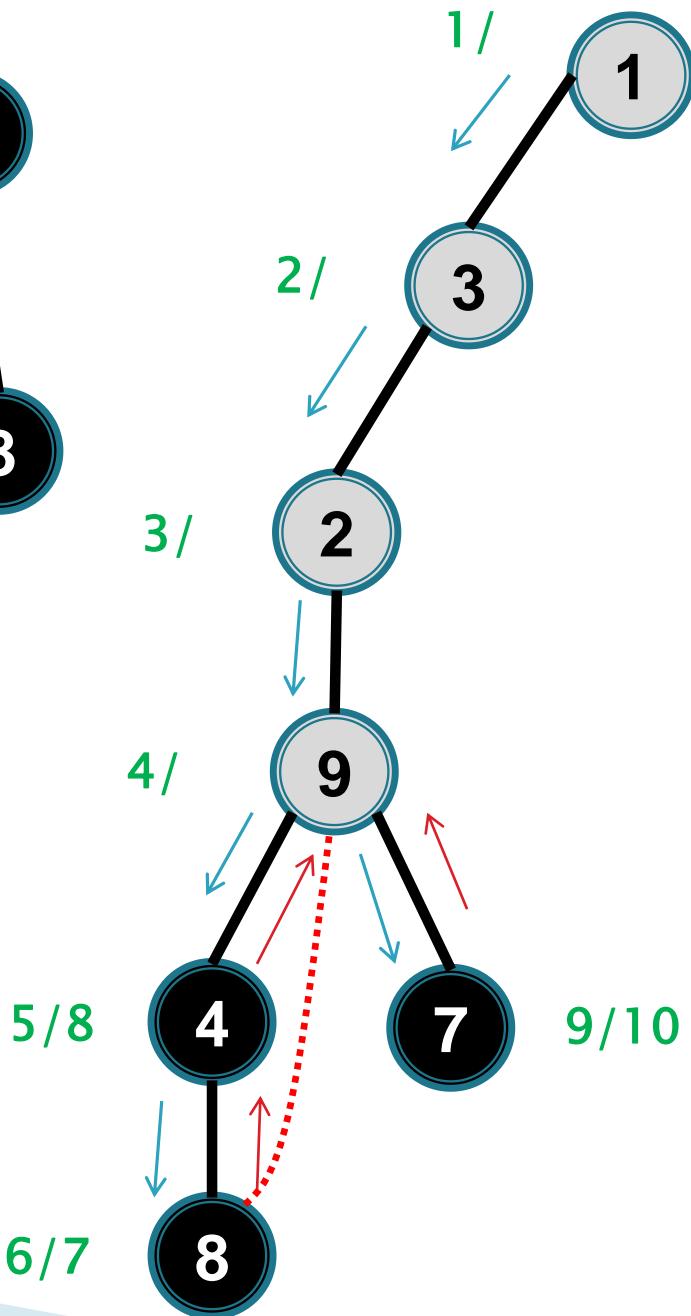
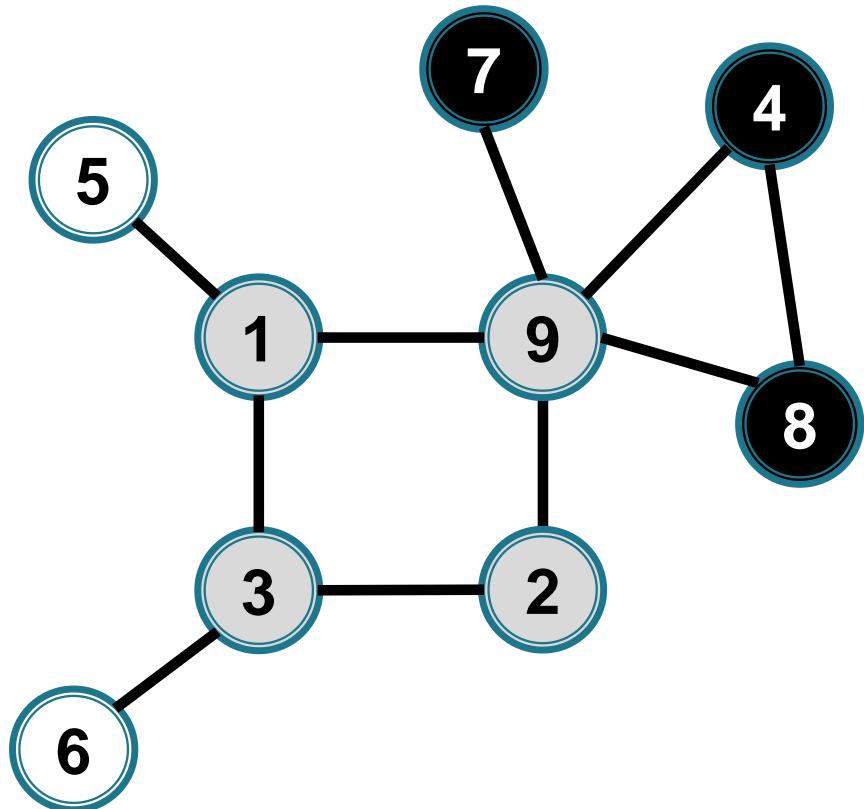


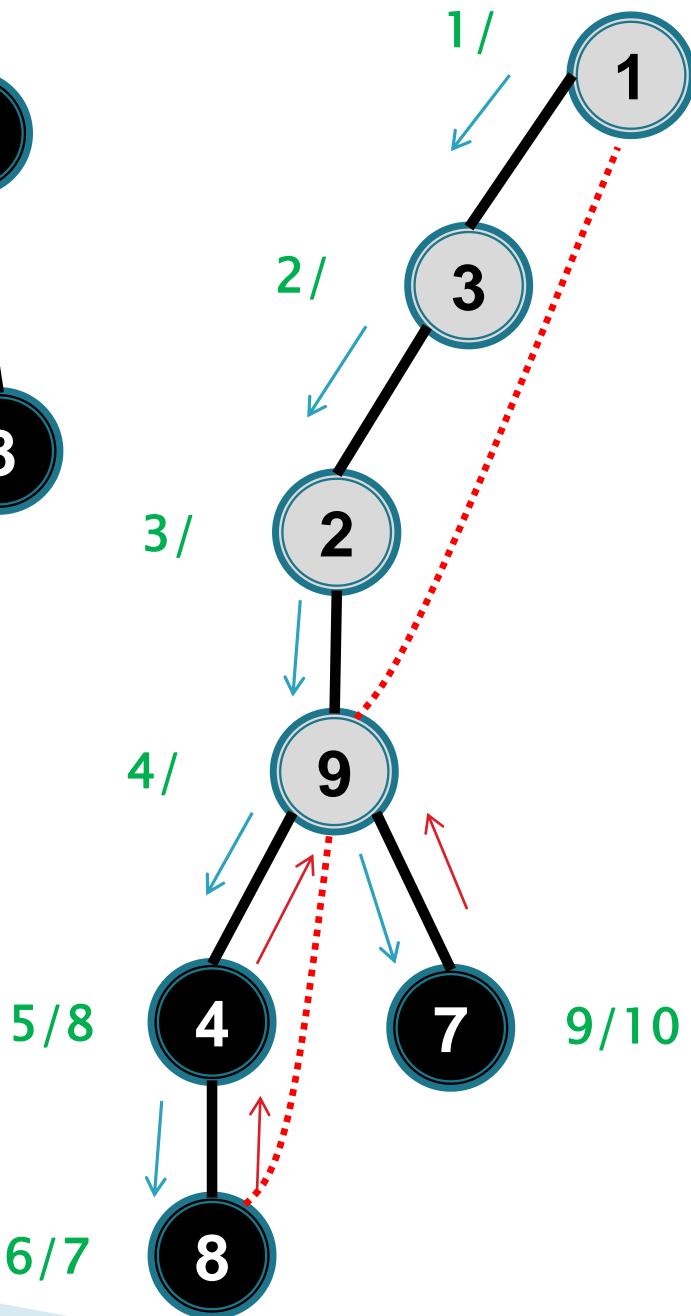
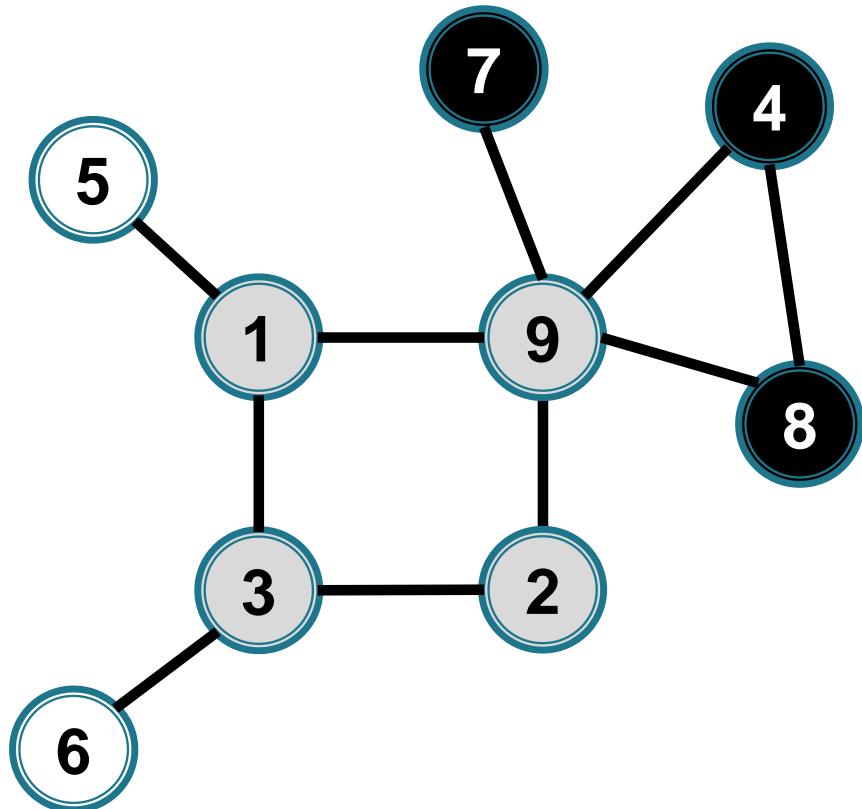


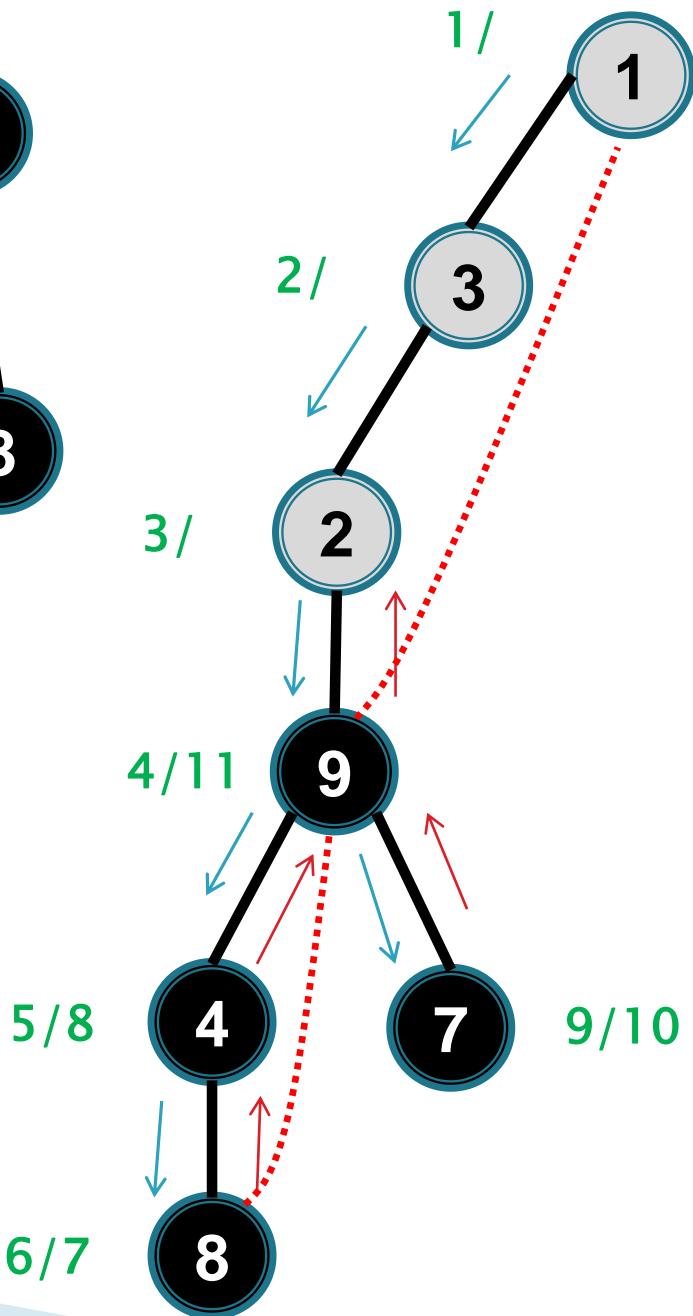
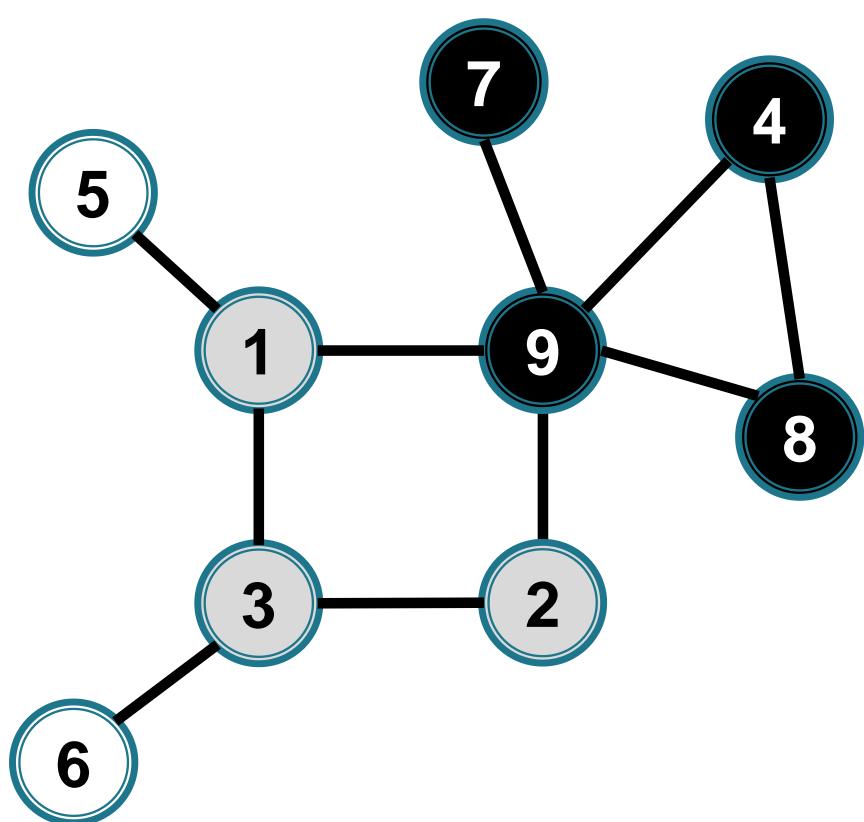


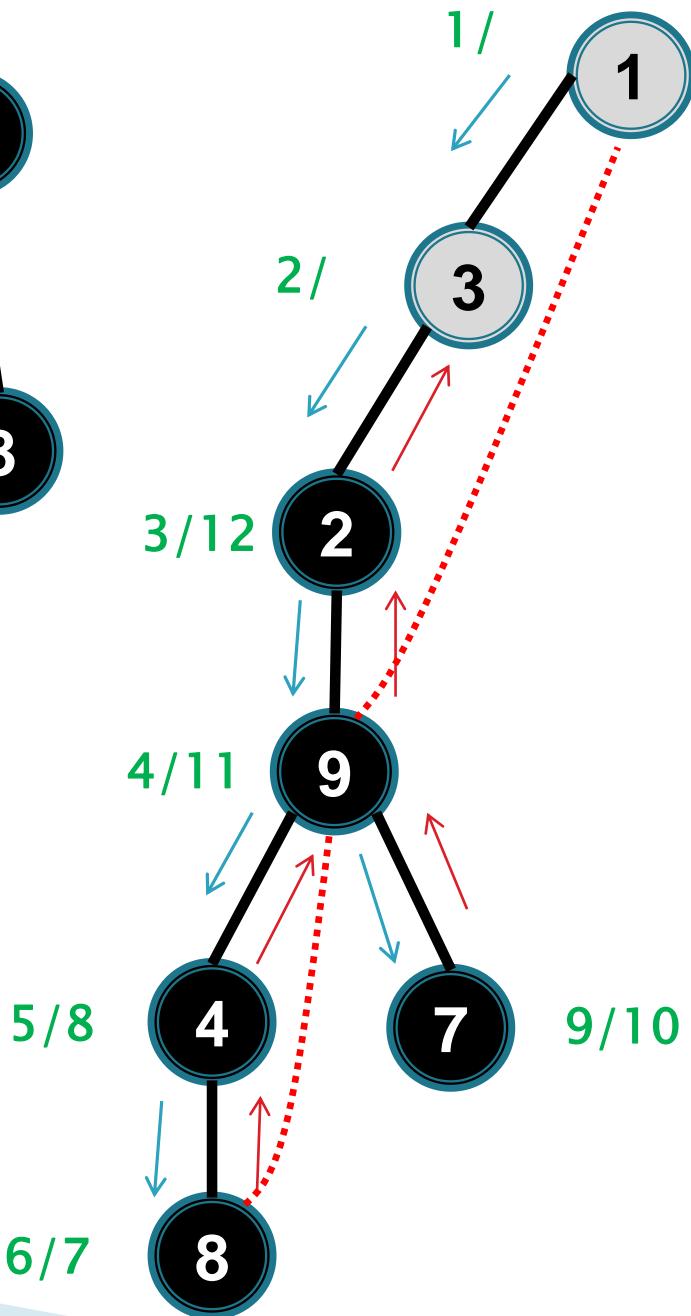
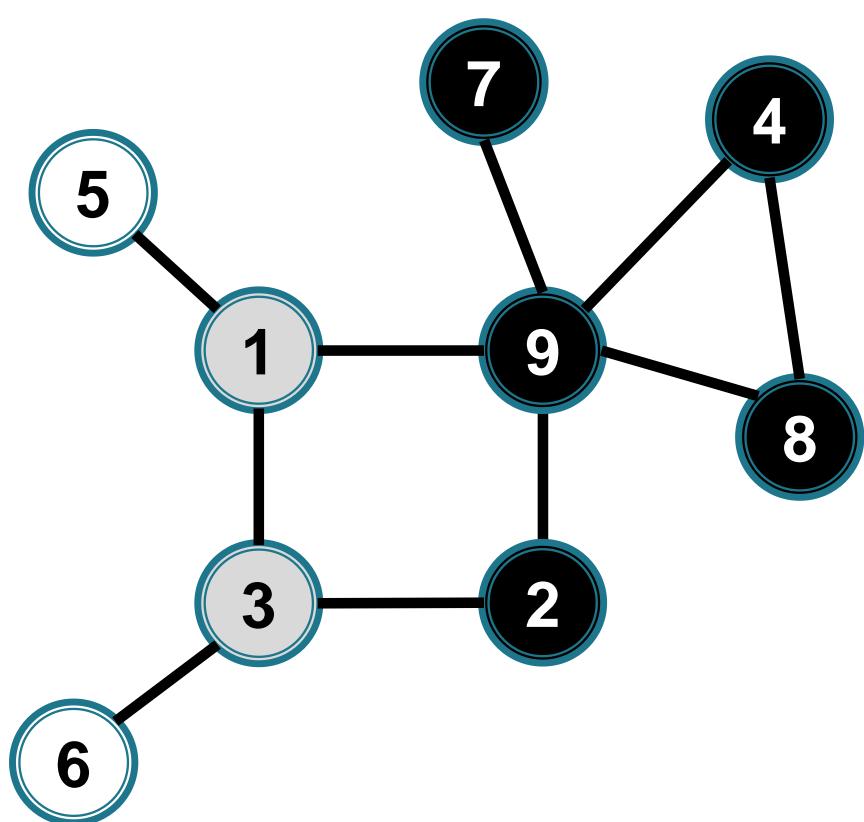


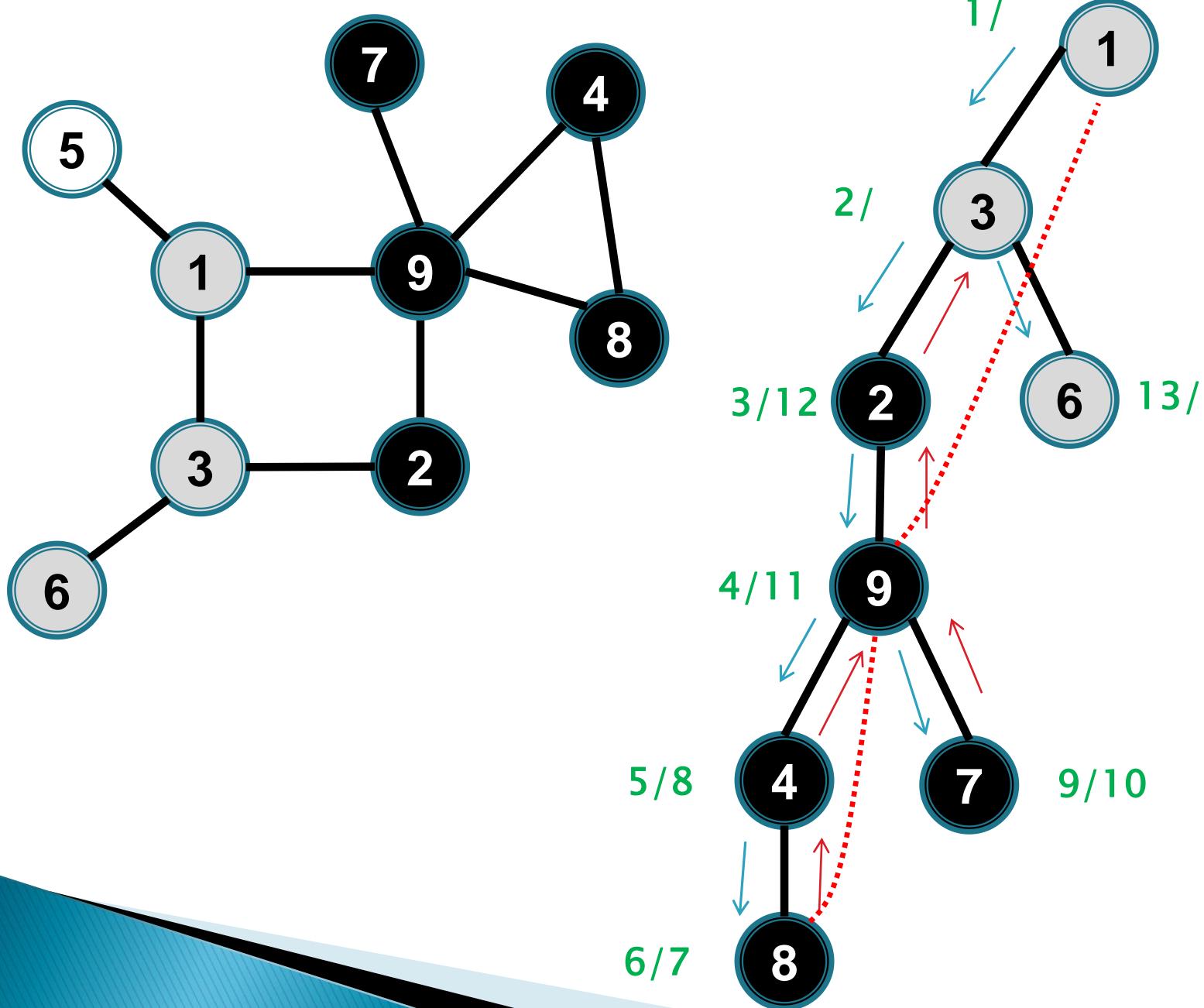


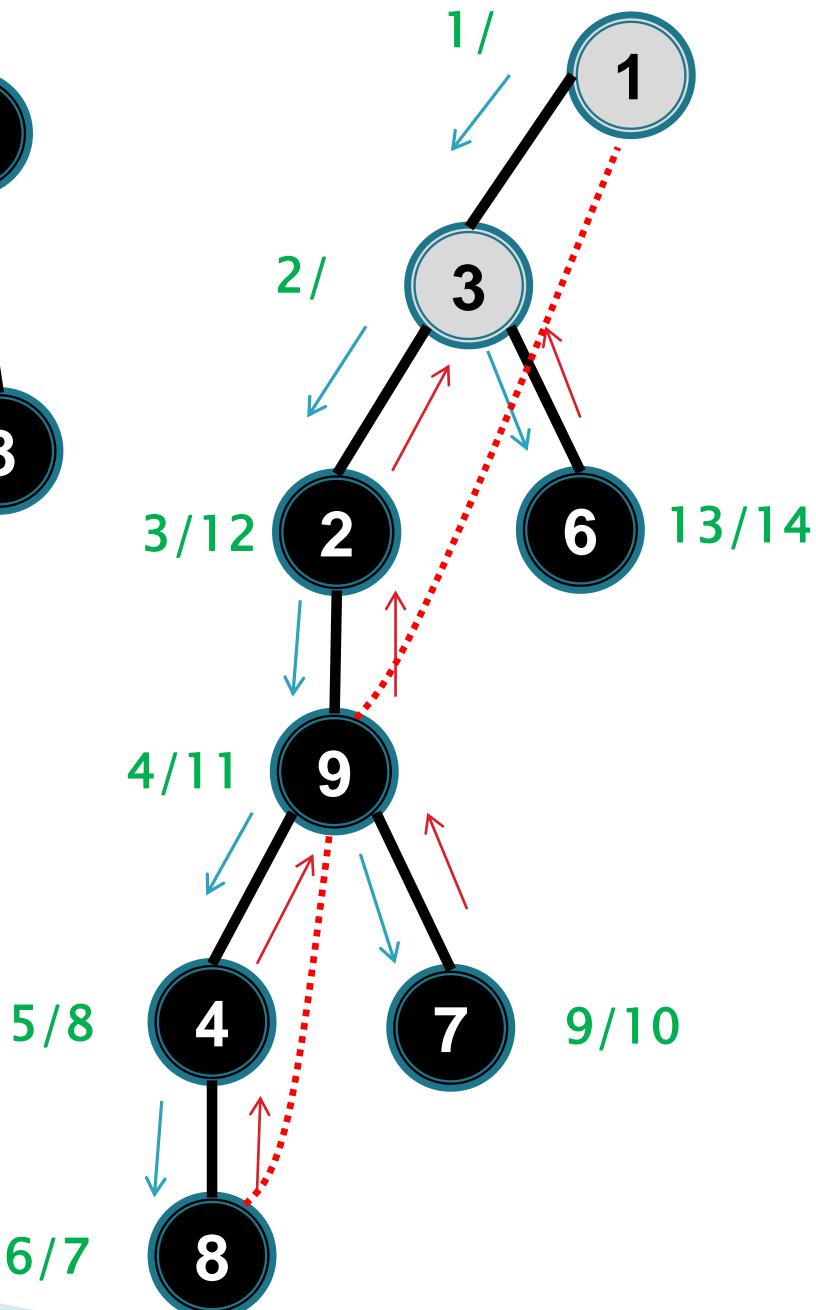
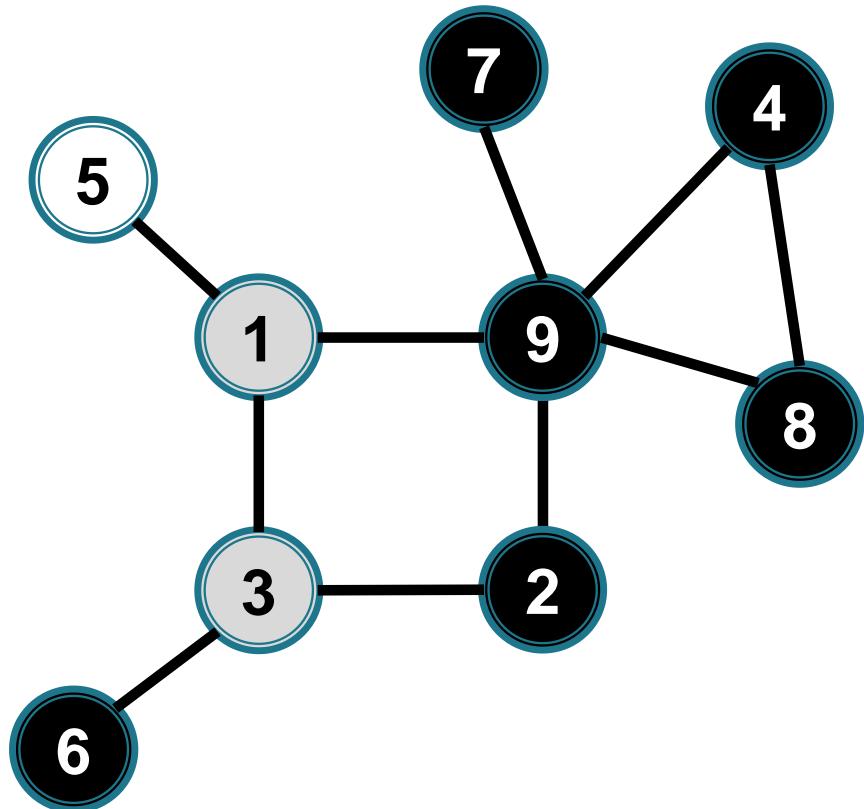


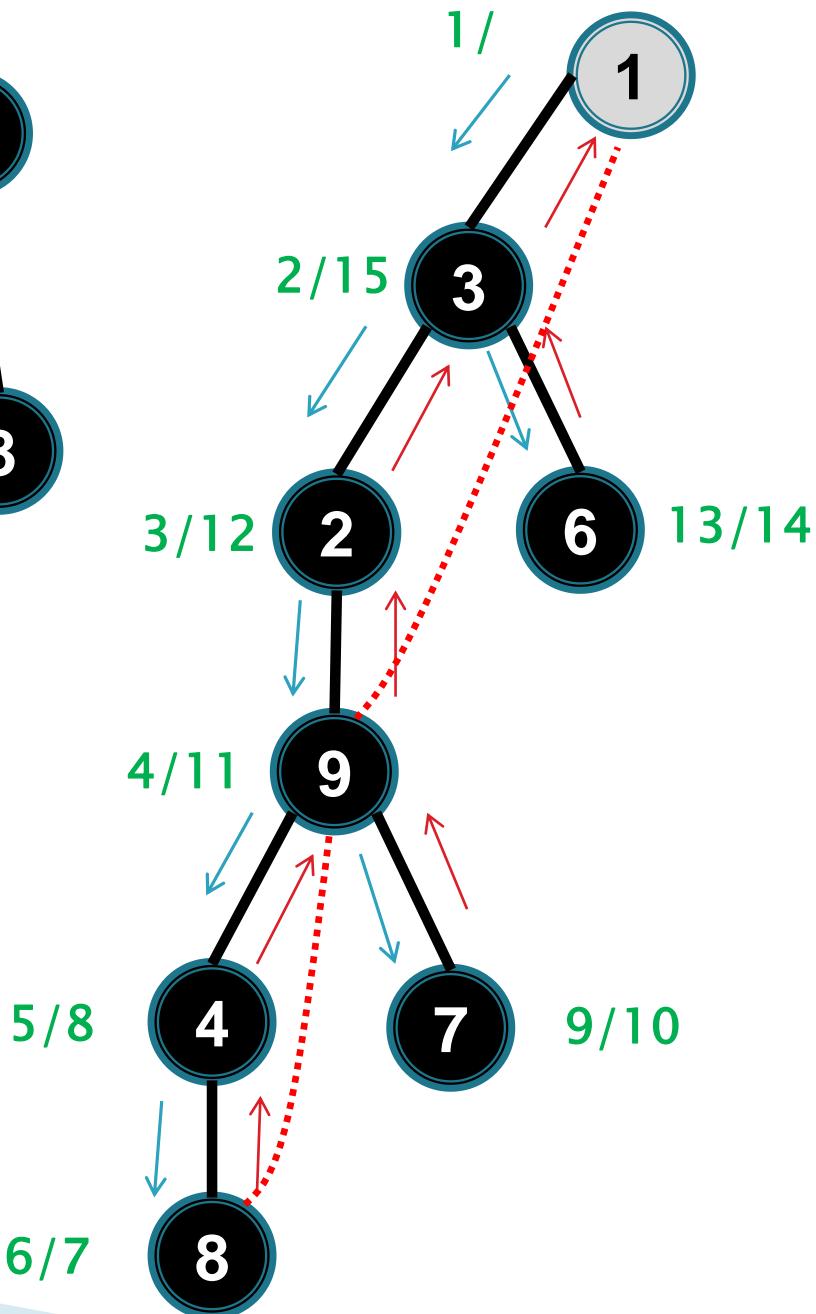
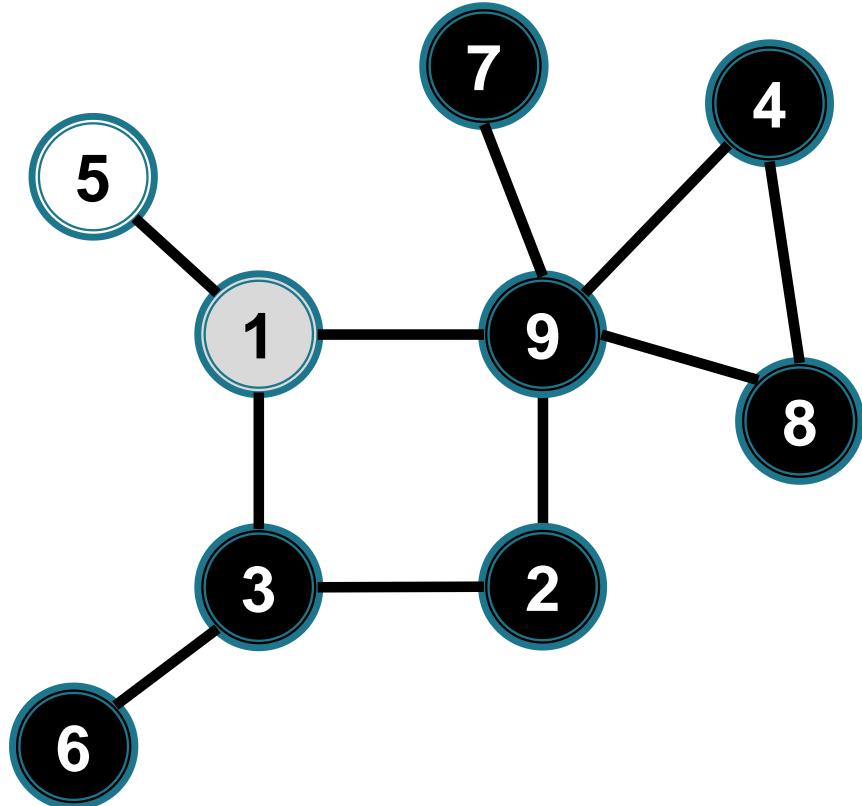


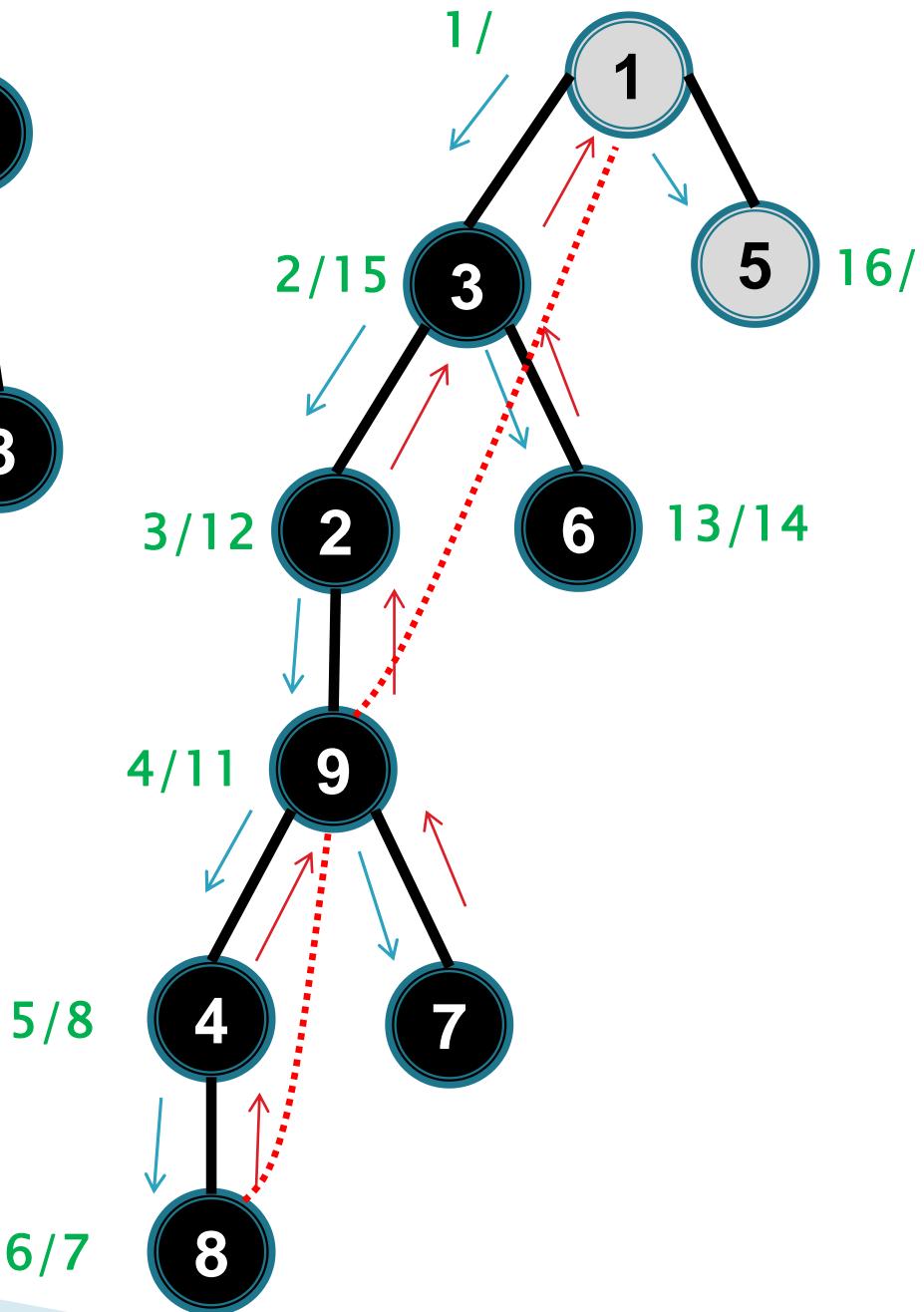
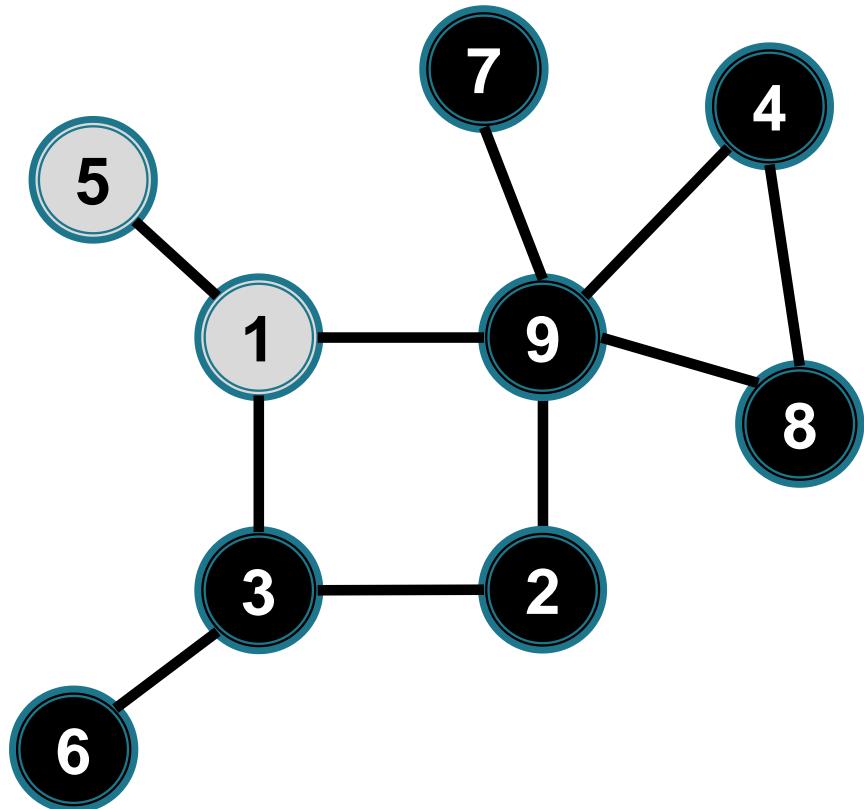


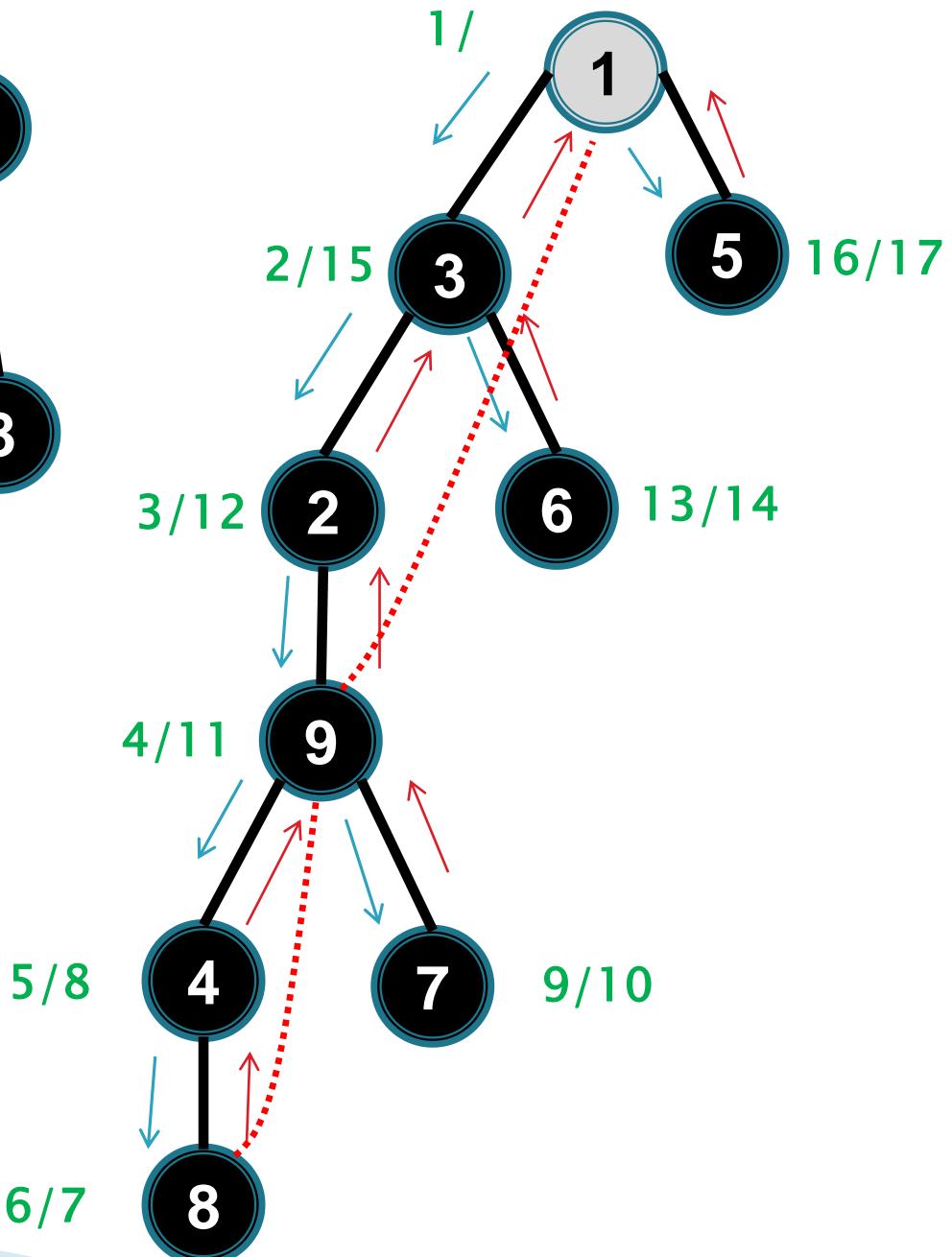
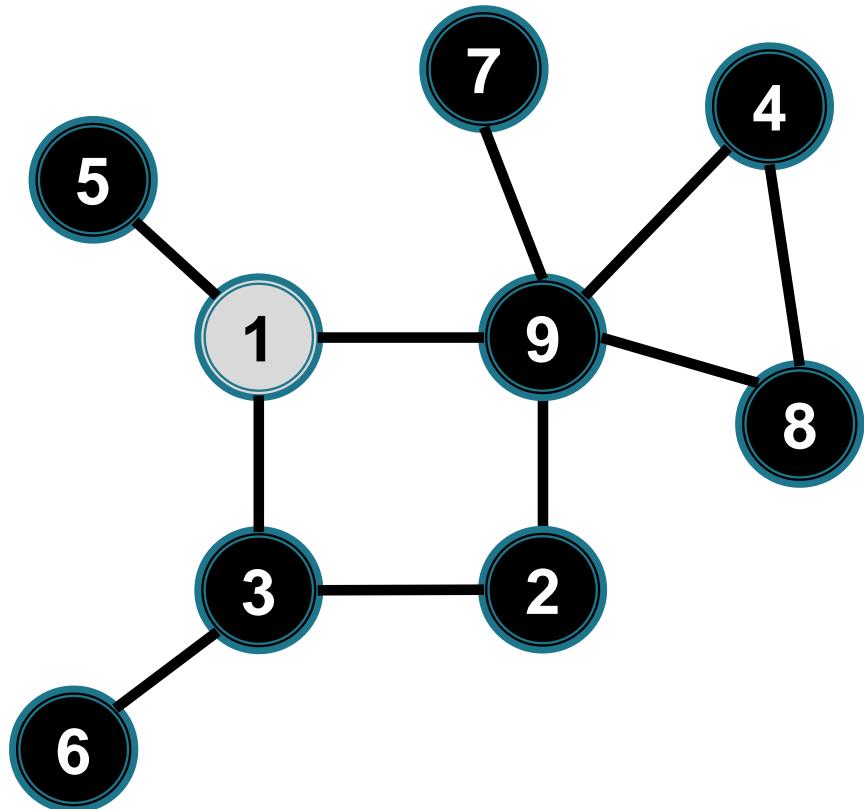


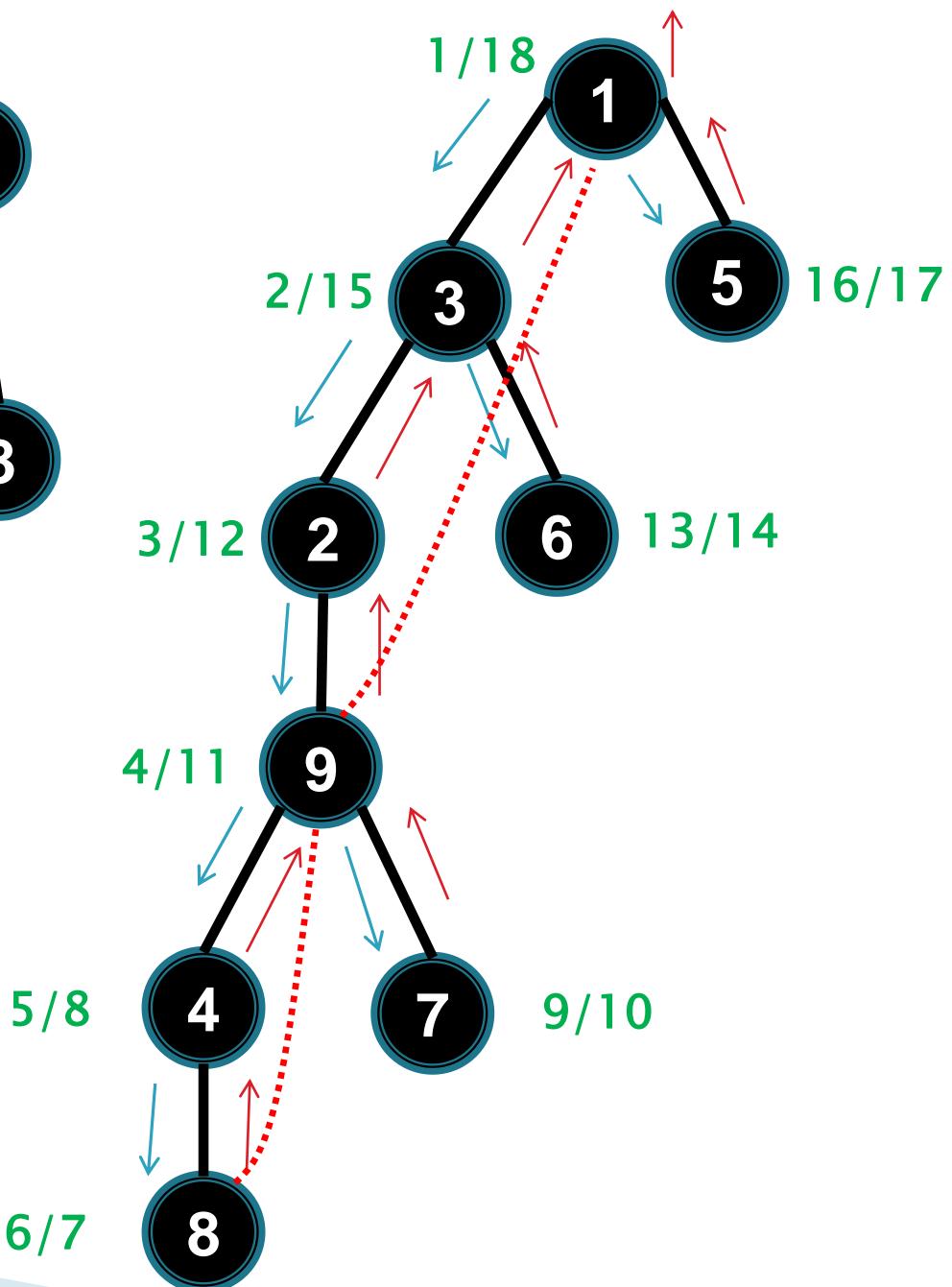
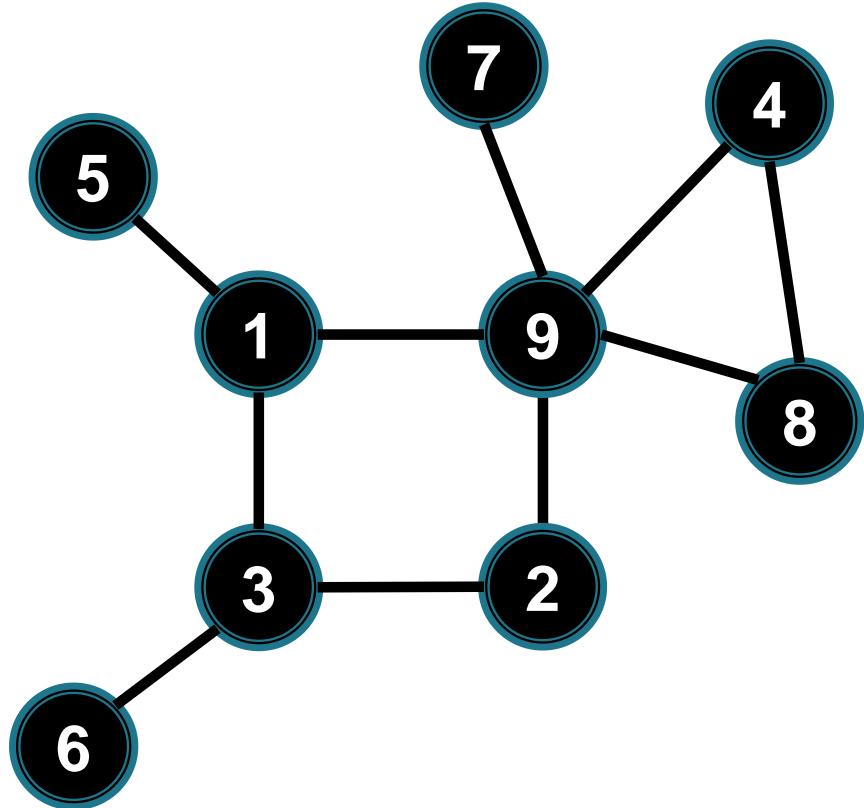




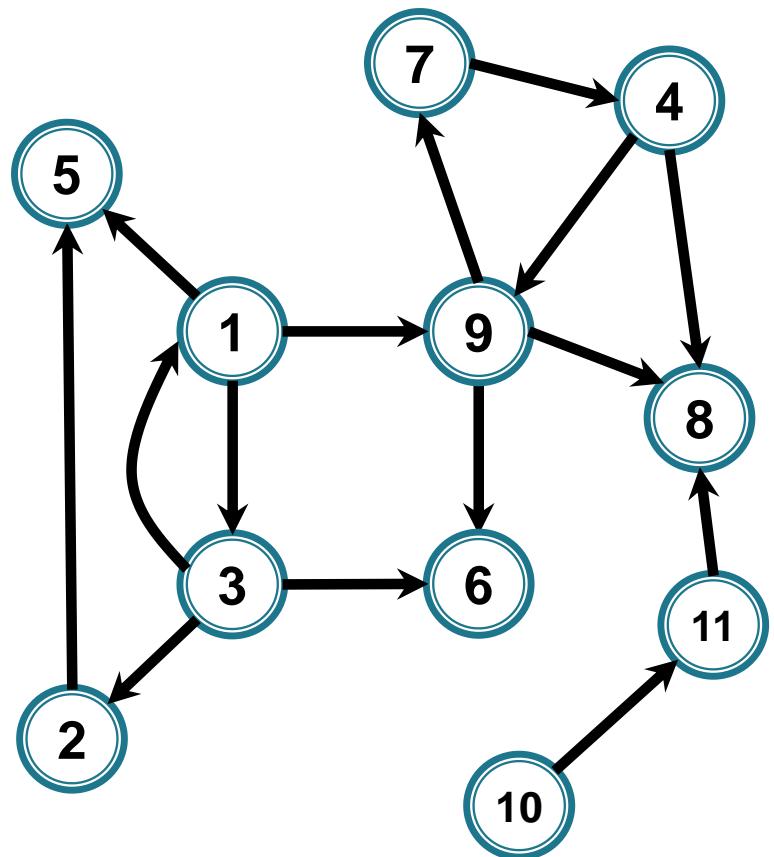








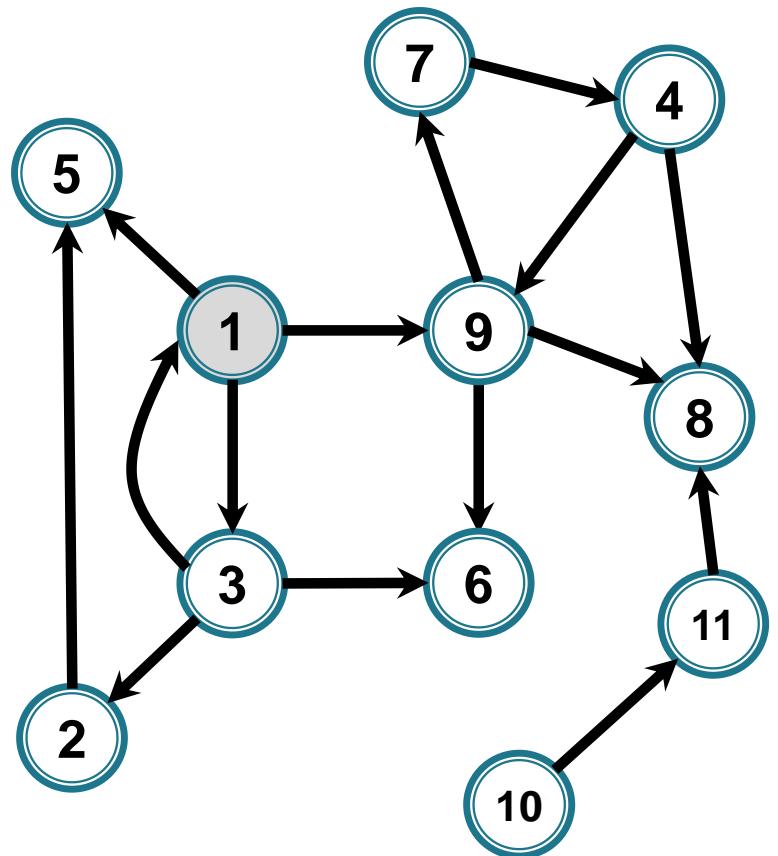
Exemplu graf orientat



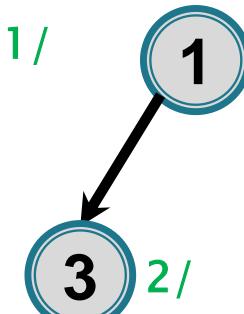
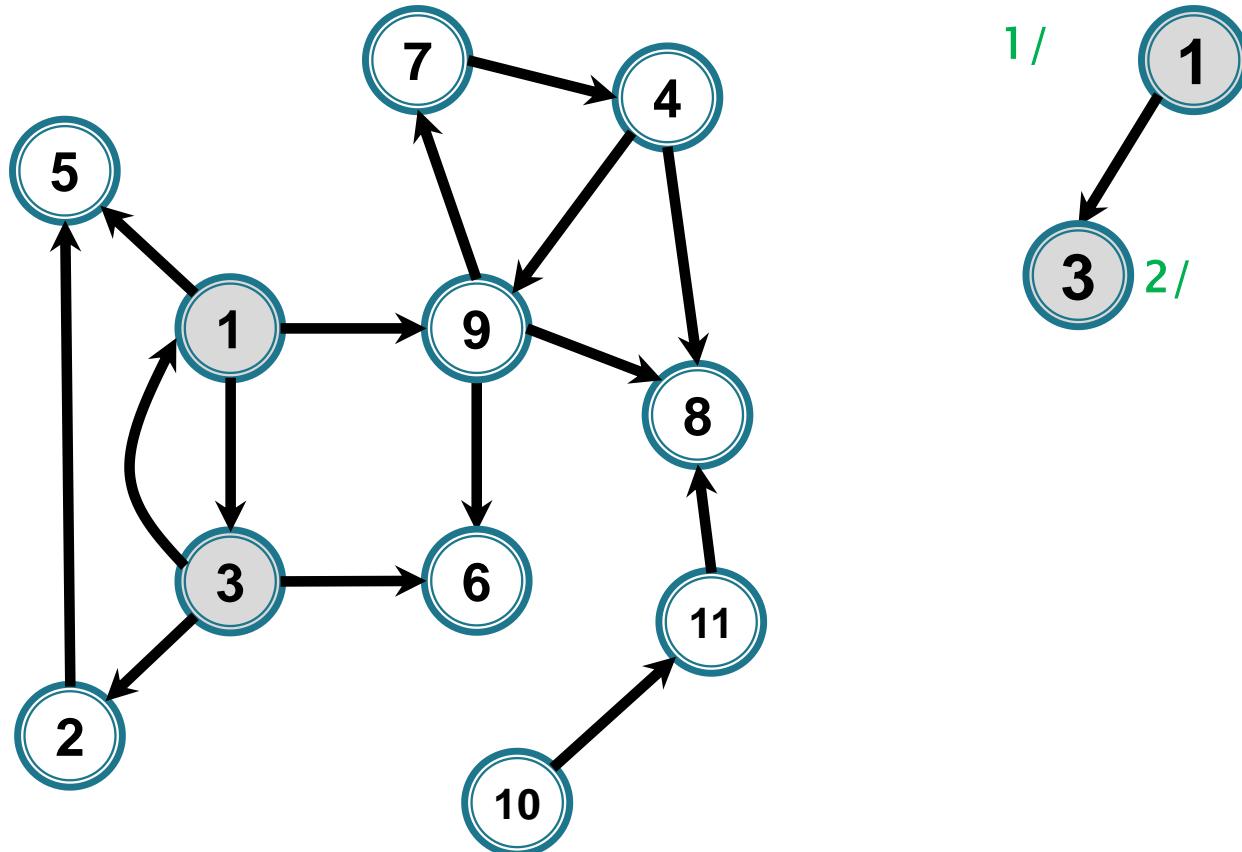
Exemplu graf orientat

1 /

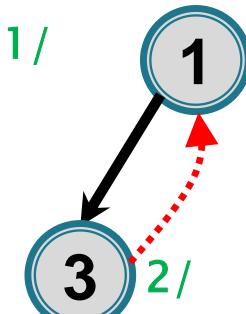
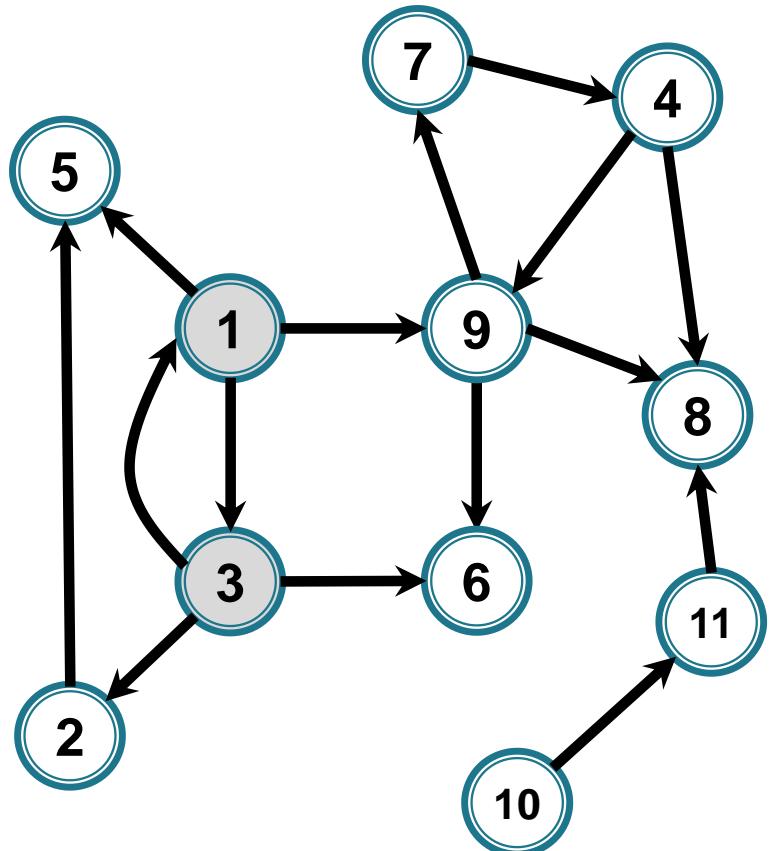
1



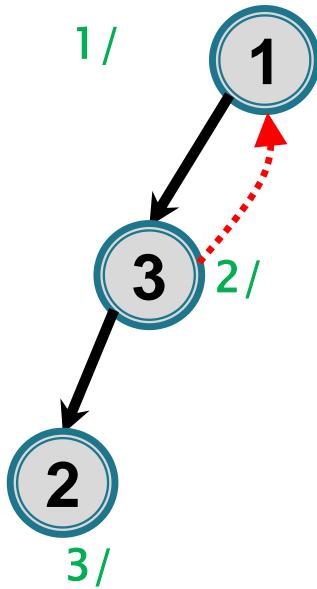
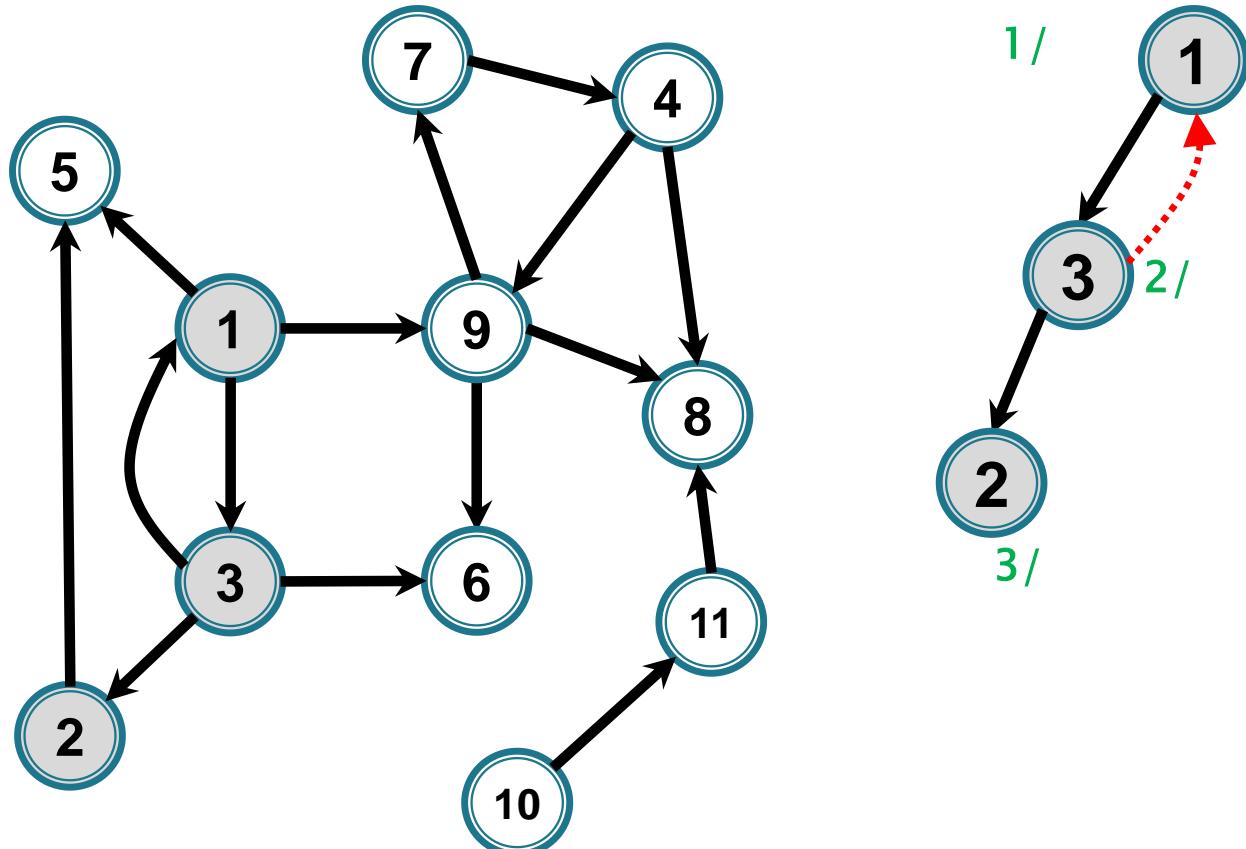
Exemplu graf orientat



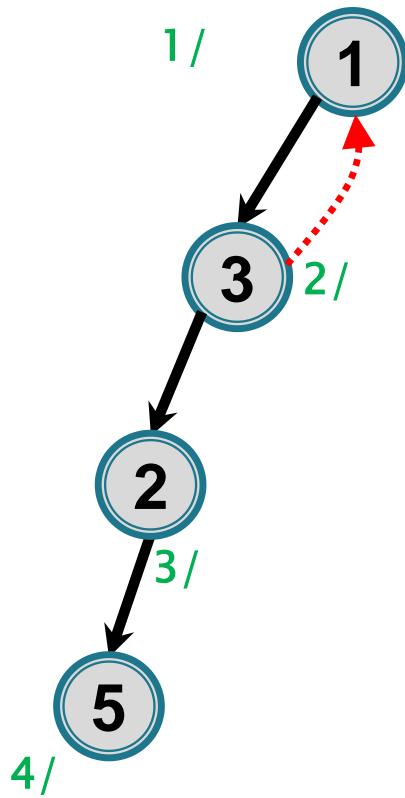
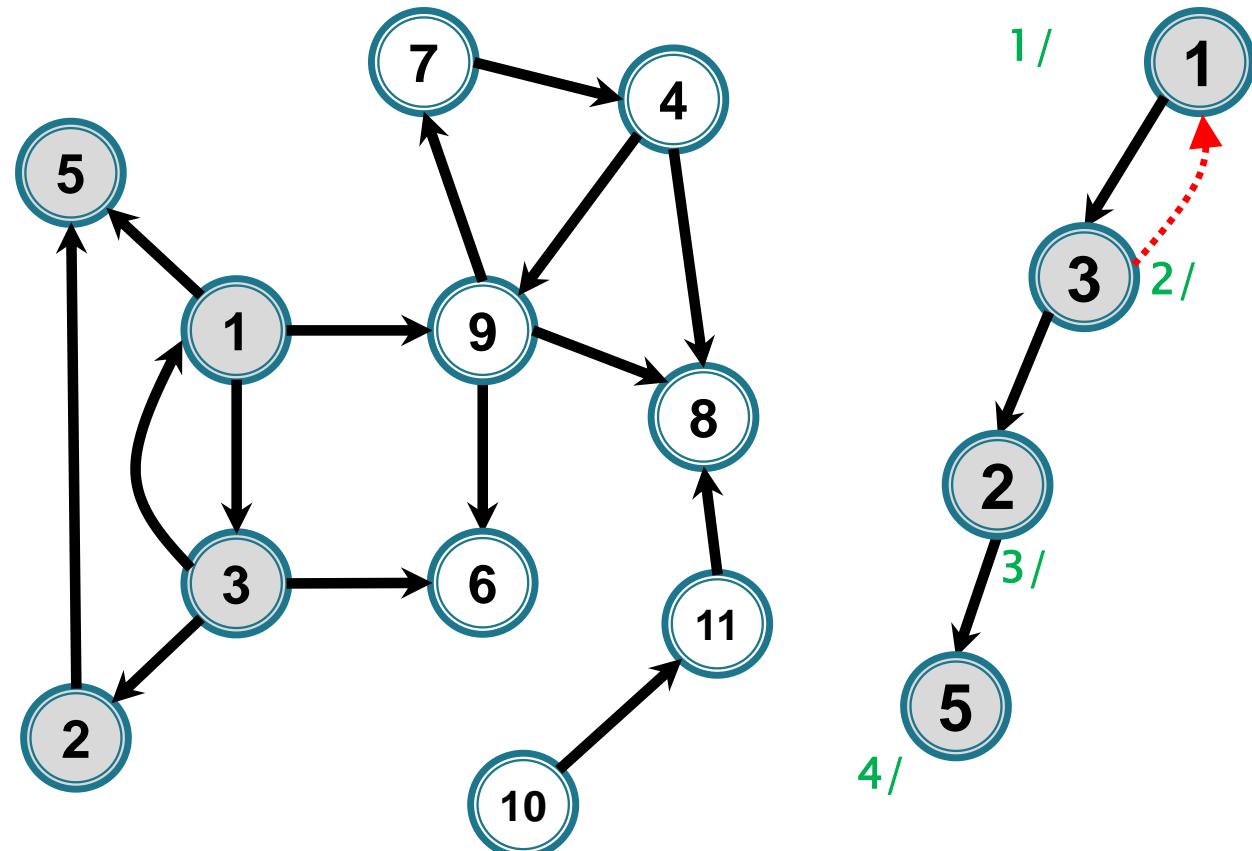
Exemplu graf orientat



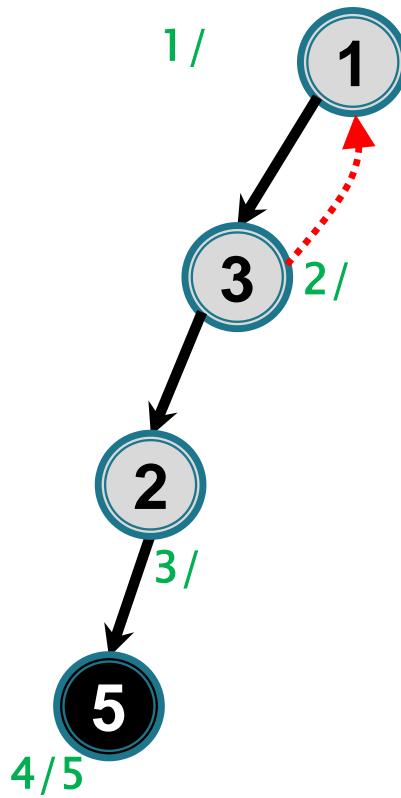
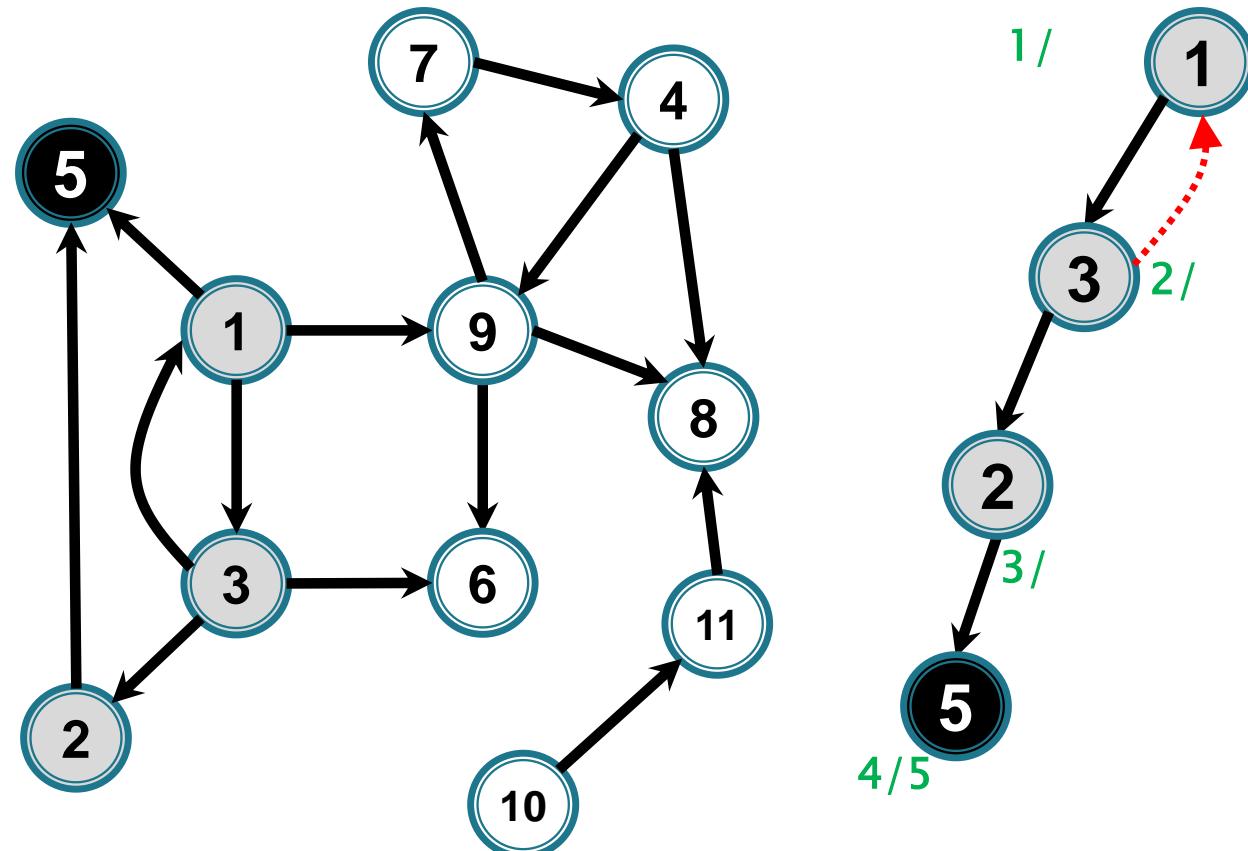
Exemplu graf orientat



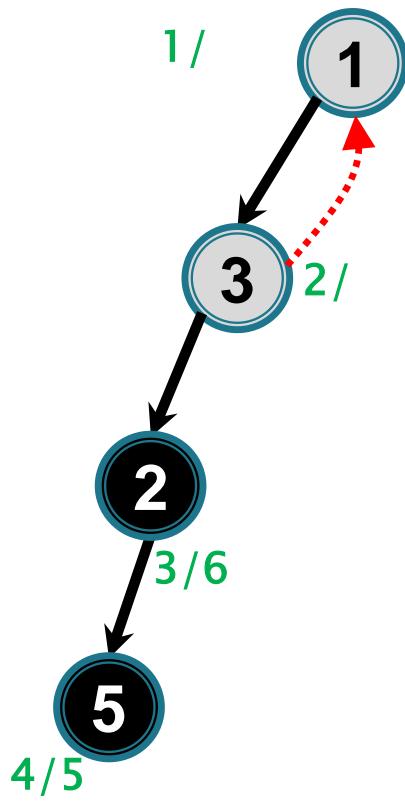
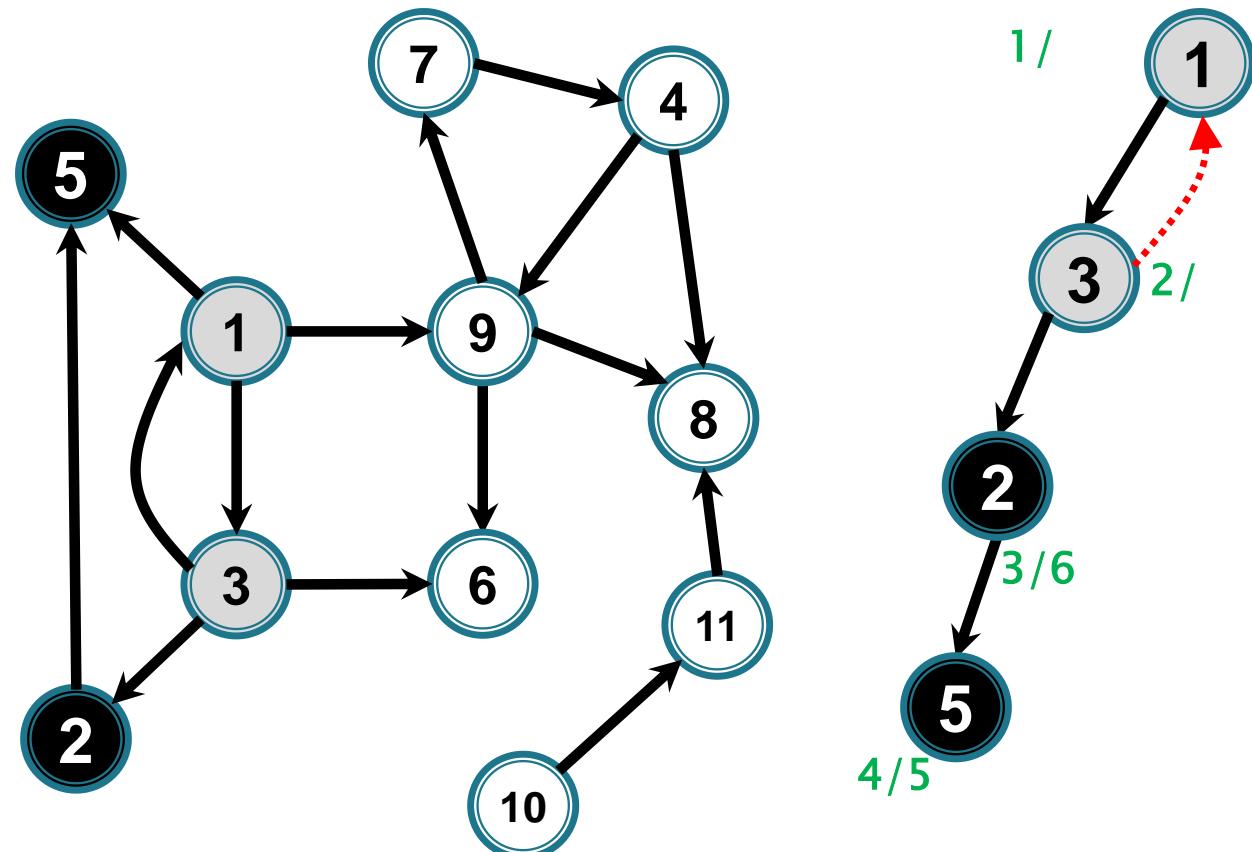
Exemplu graf orientat



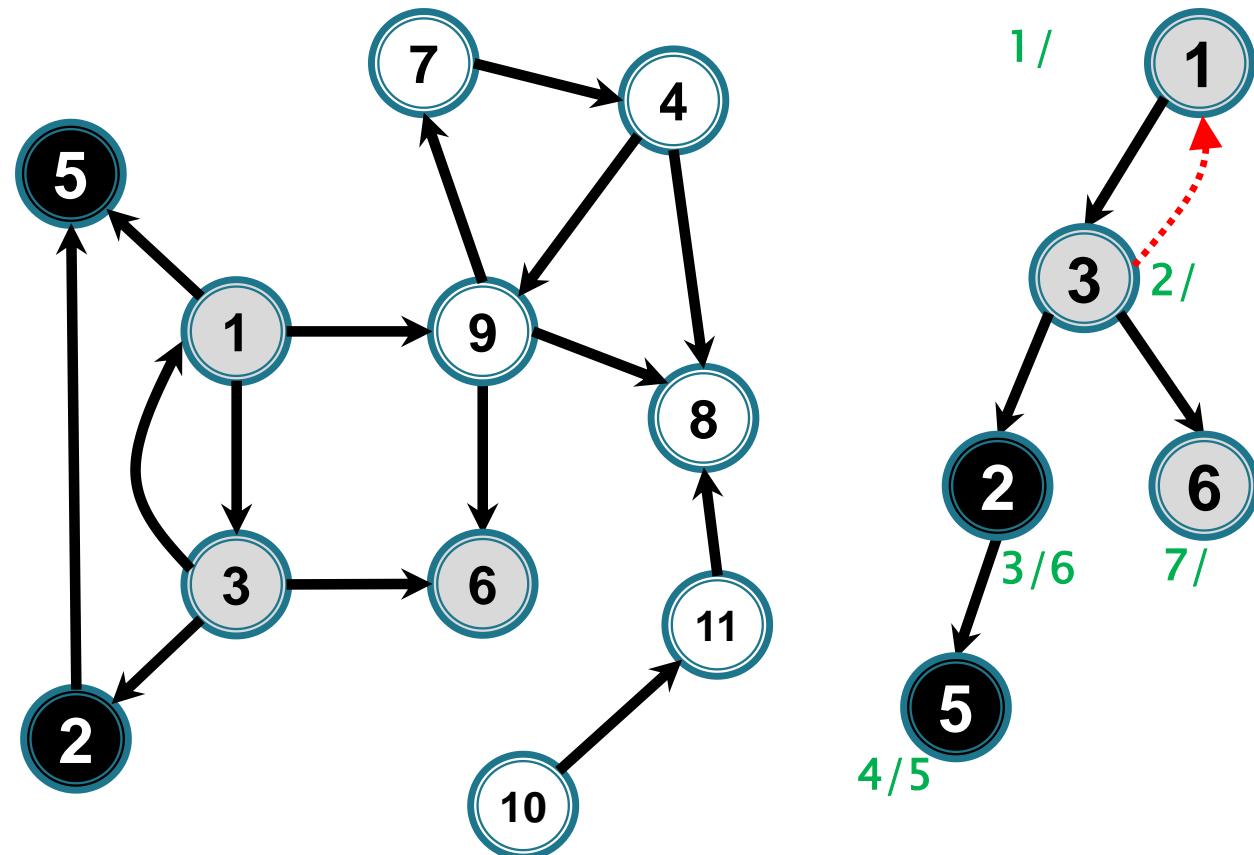
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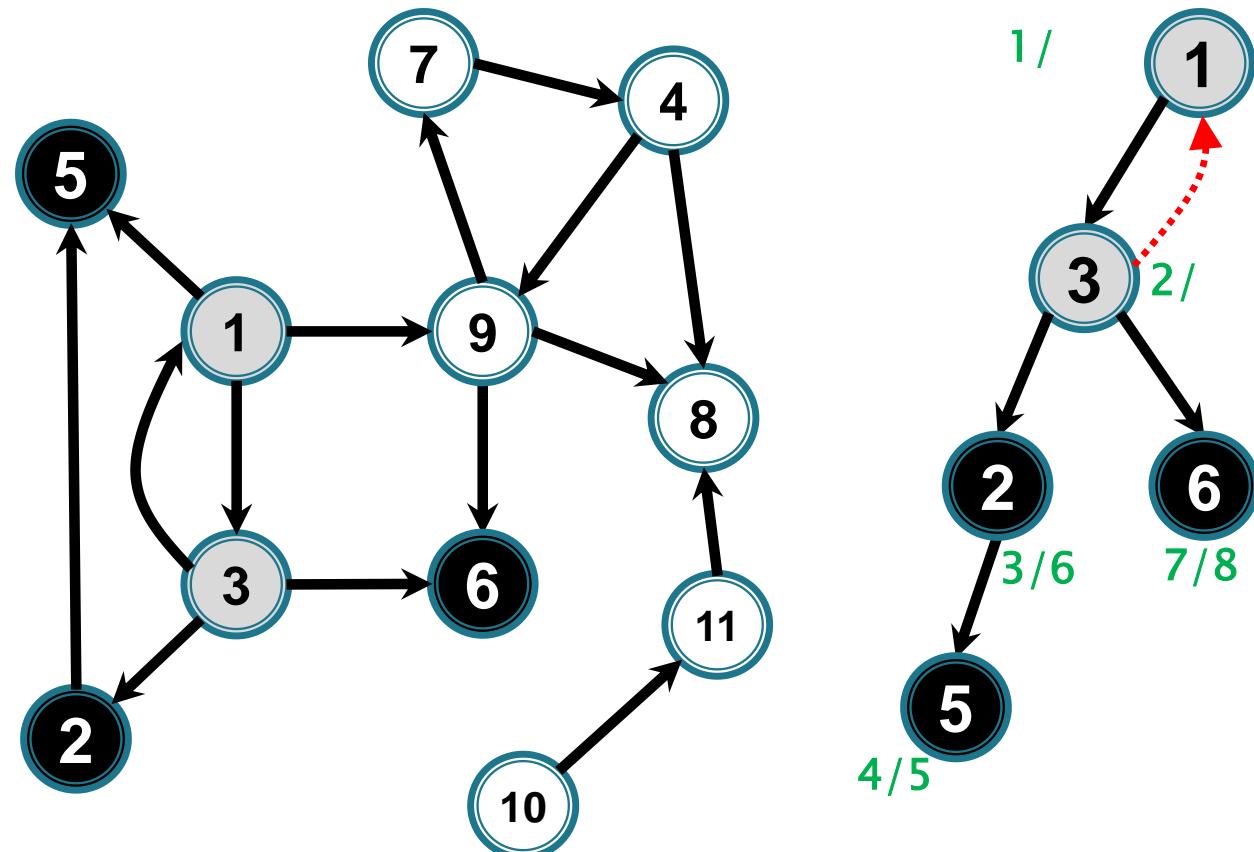
Exemplu graf orientat



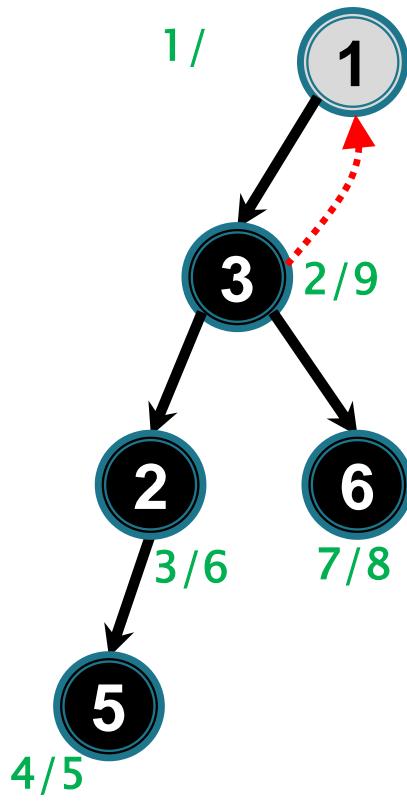
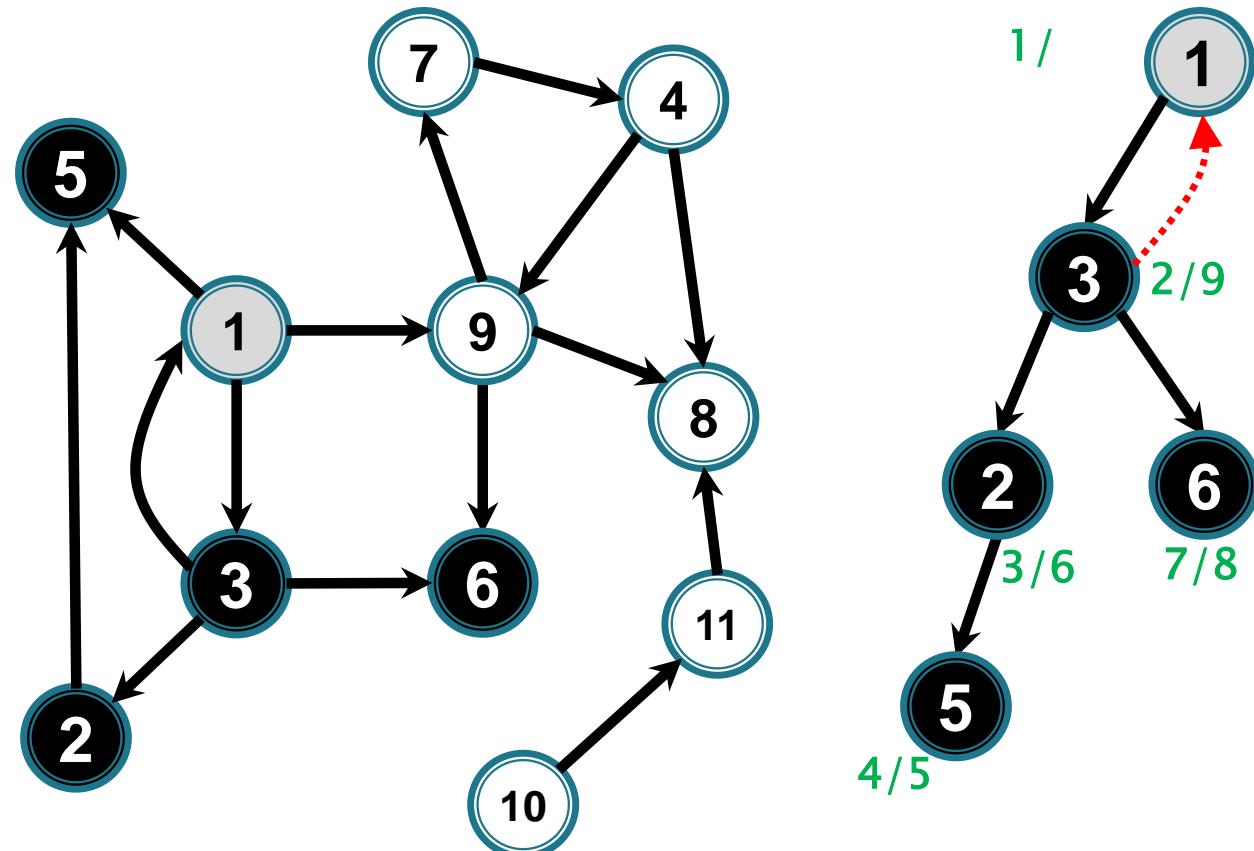
Exemplu graf orientat



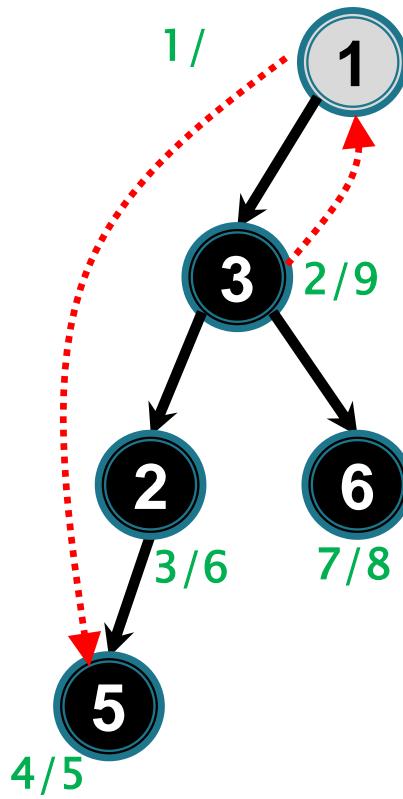
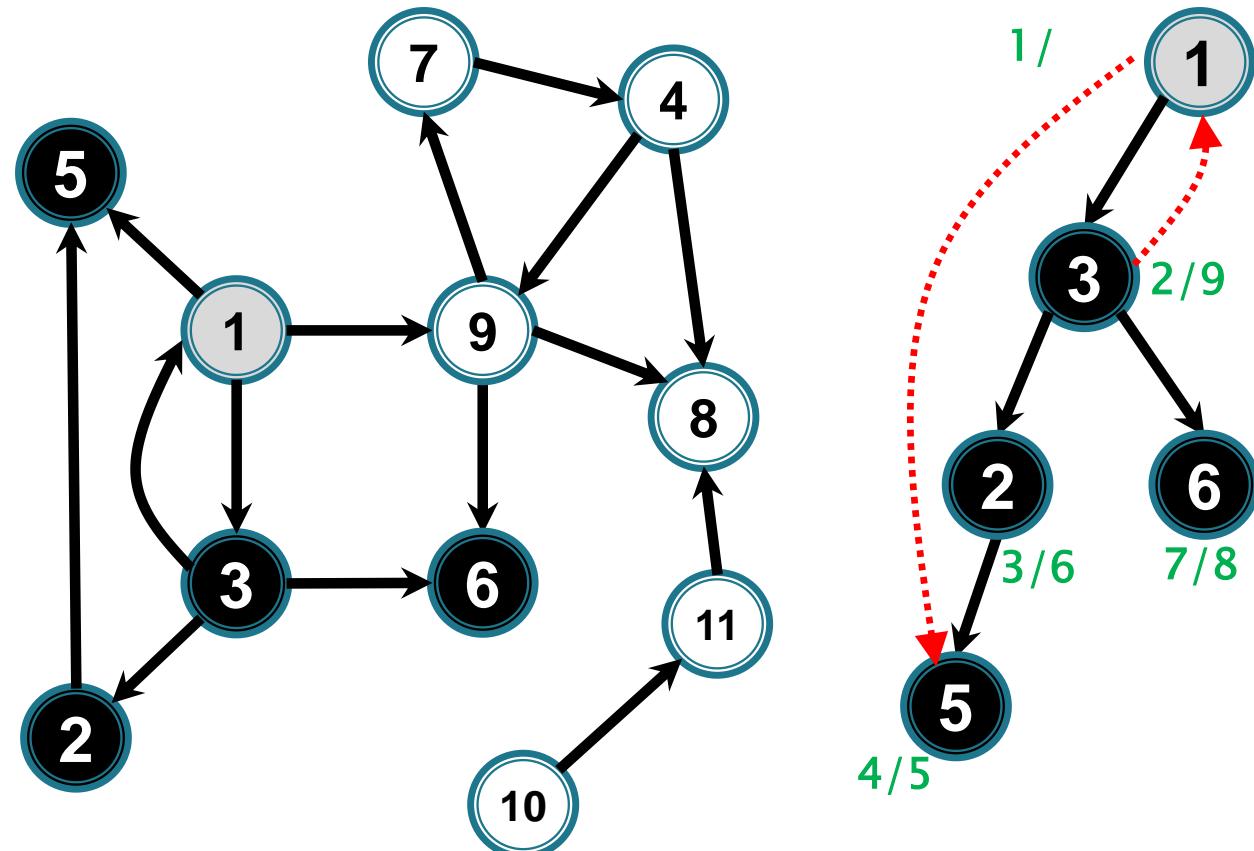
Exemplu graf orientat



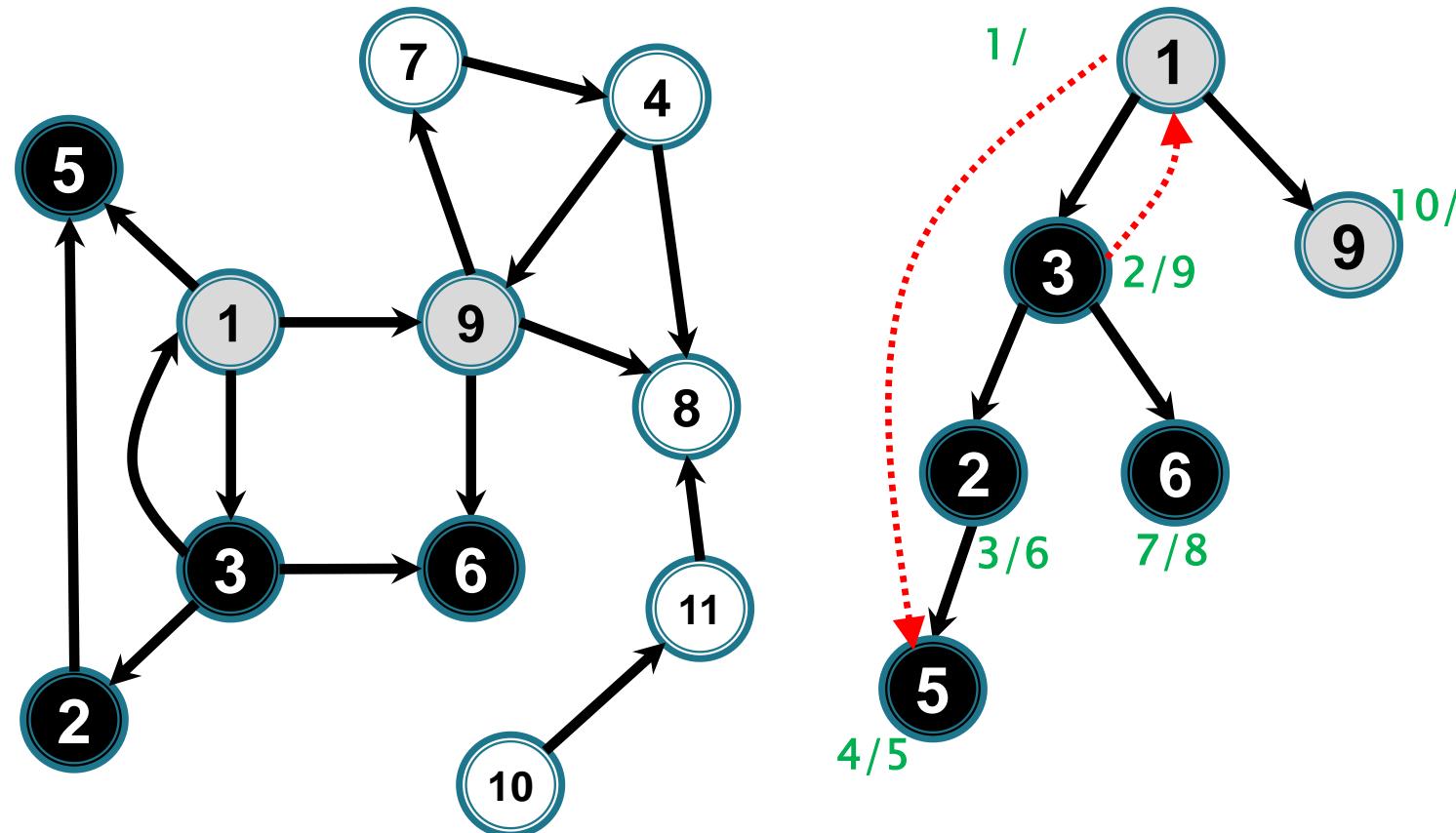
Exemplu graf orientat



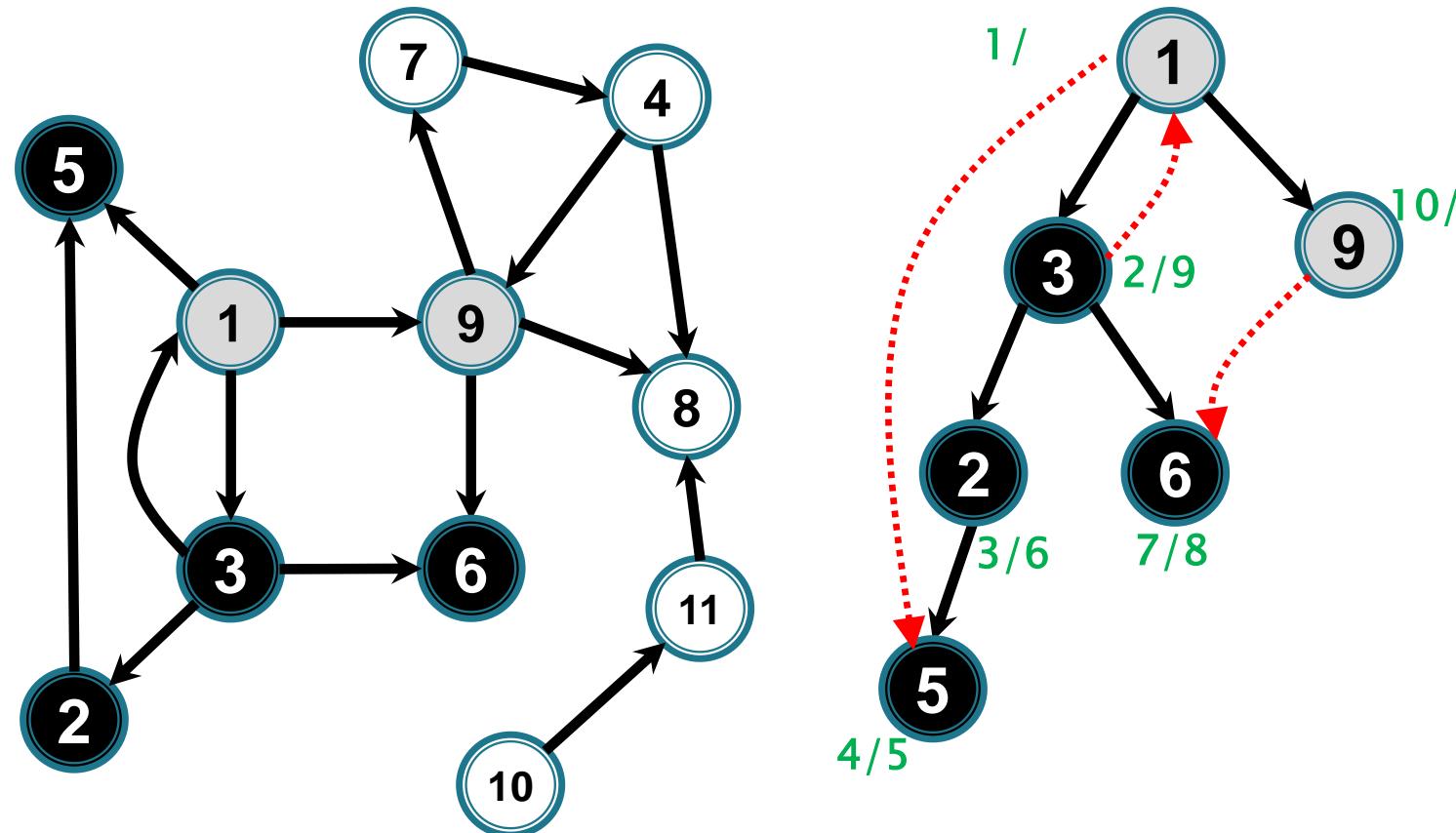
Exemplu graf orientat



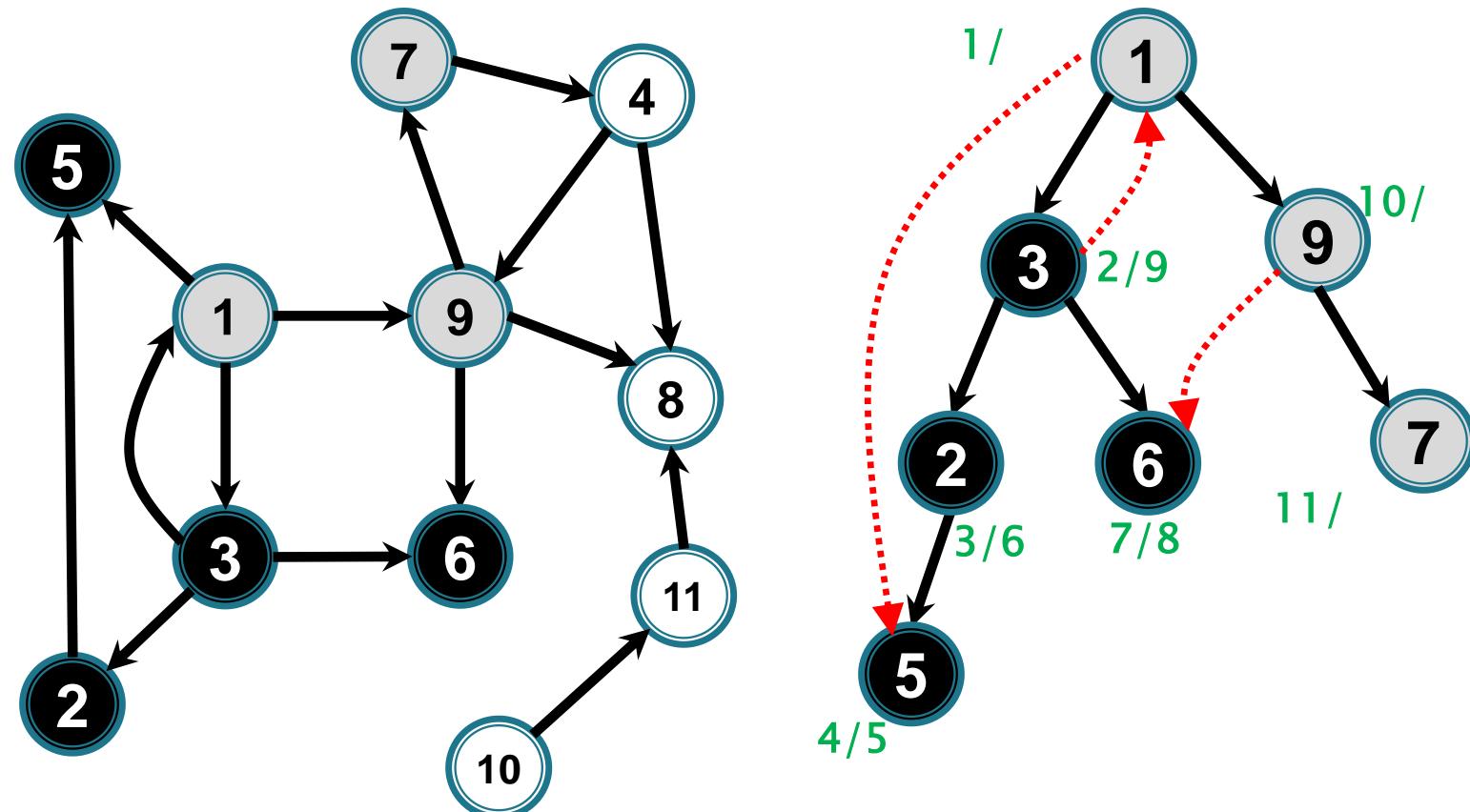
Exemplu graf orientat



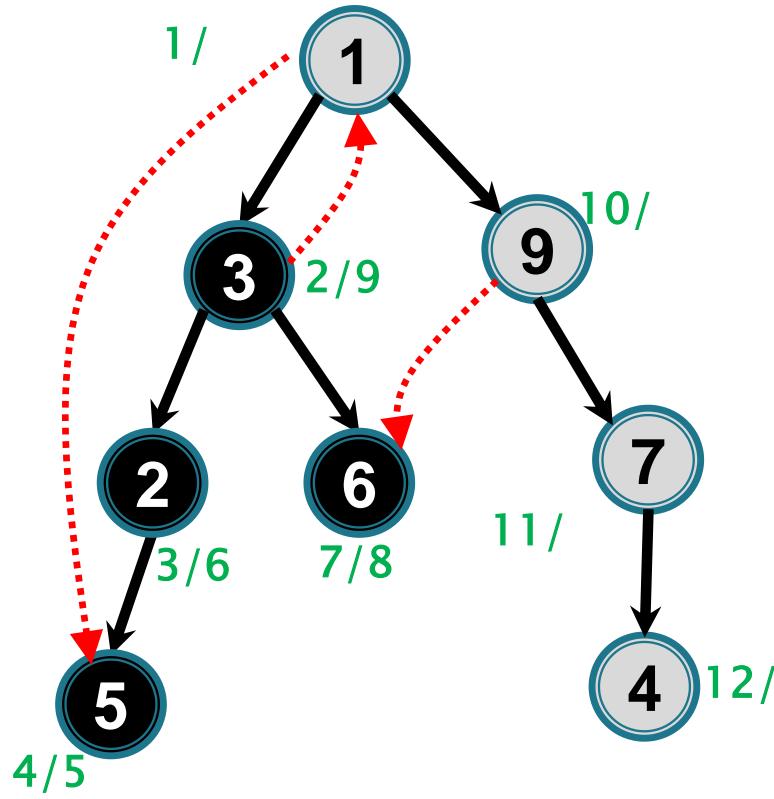
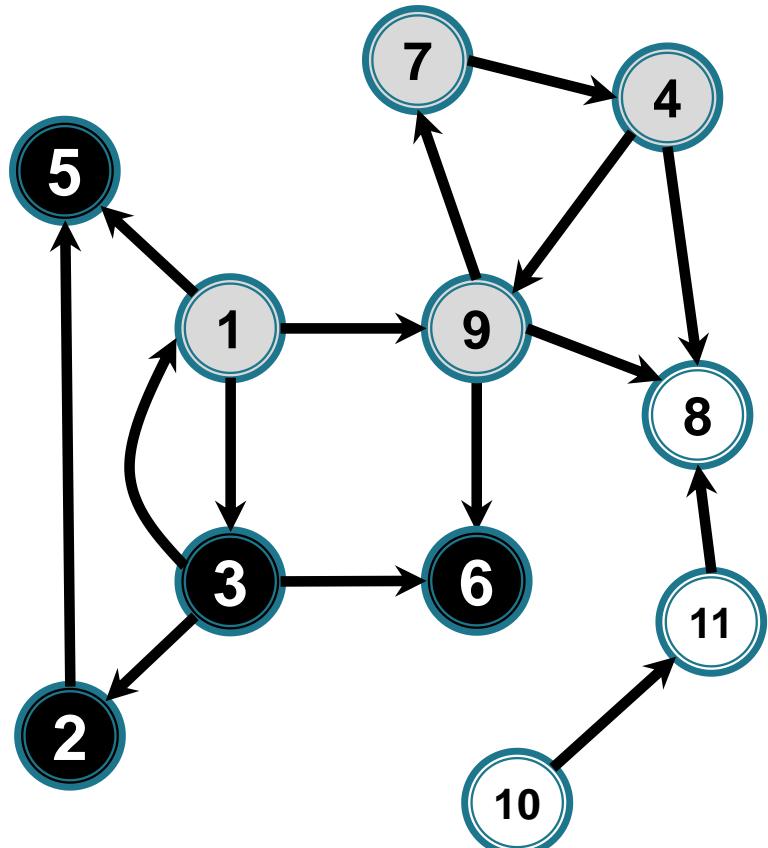
Exemplu graf orientat



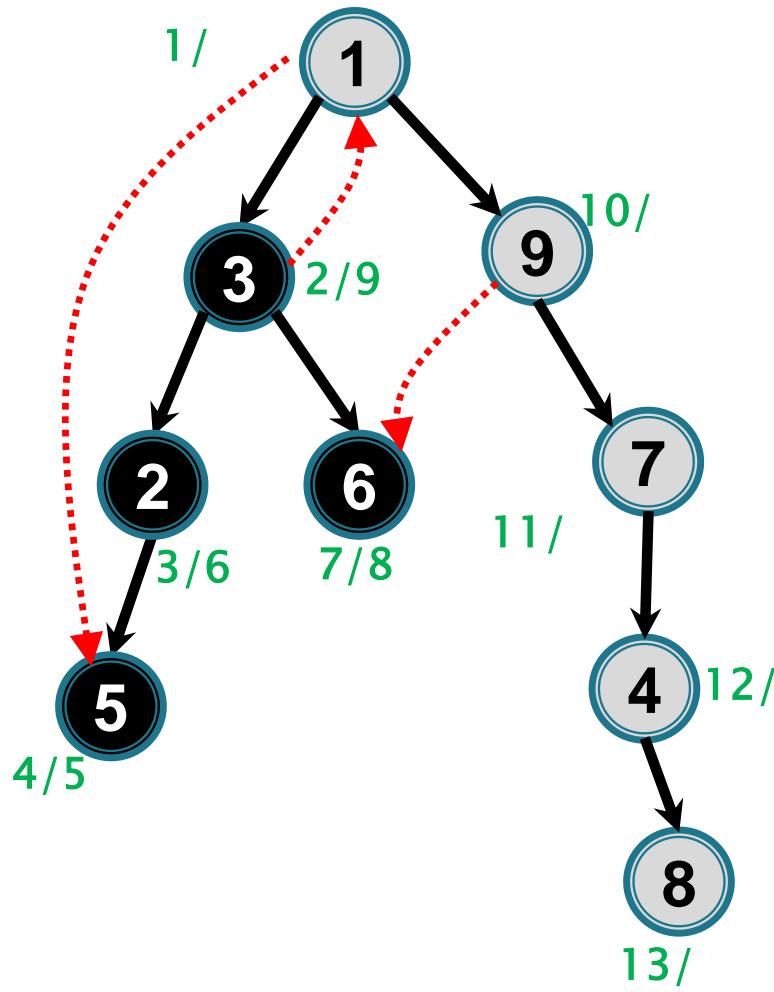
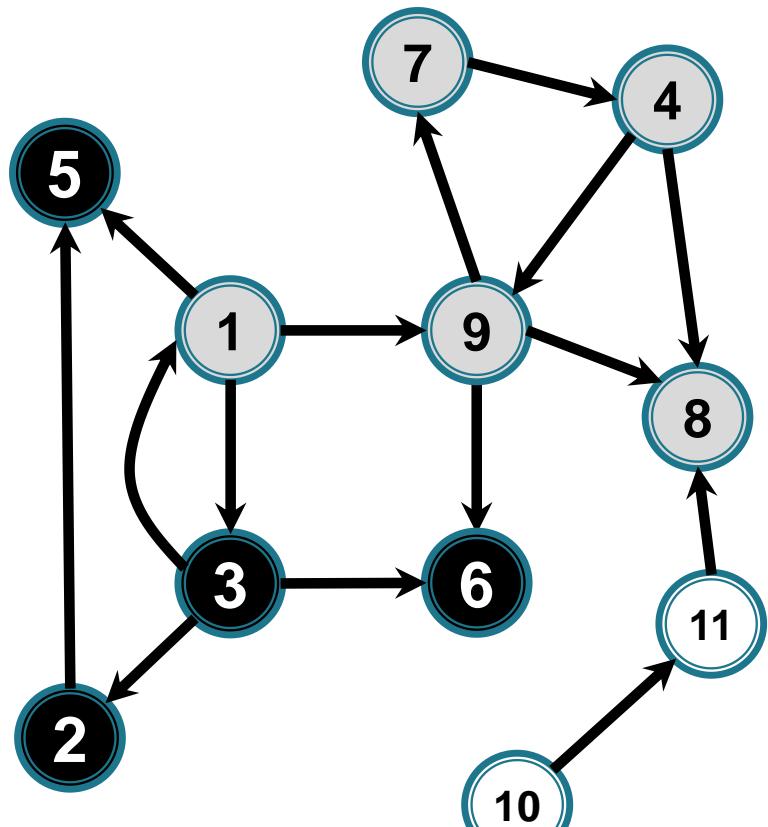
Exemplu graf orientat



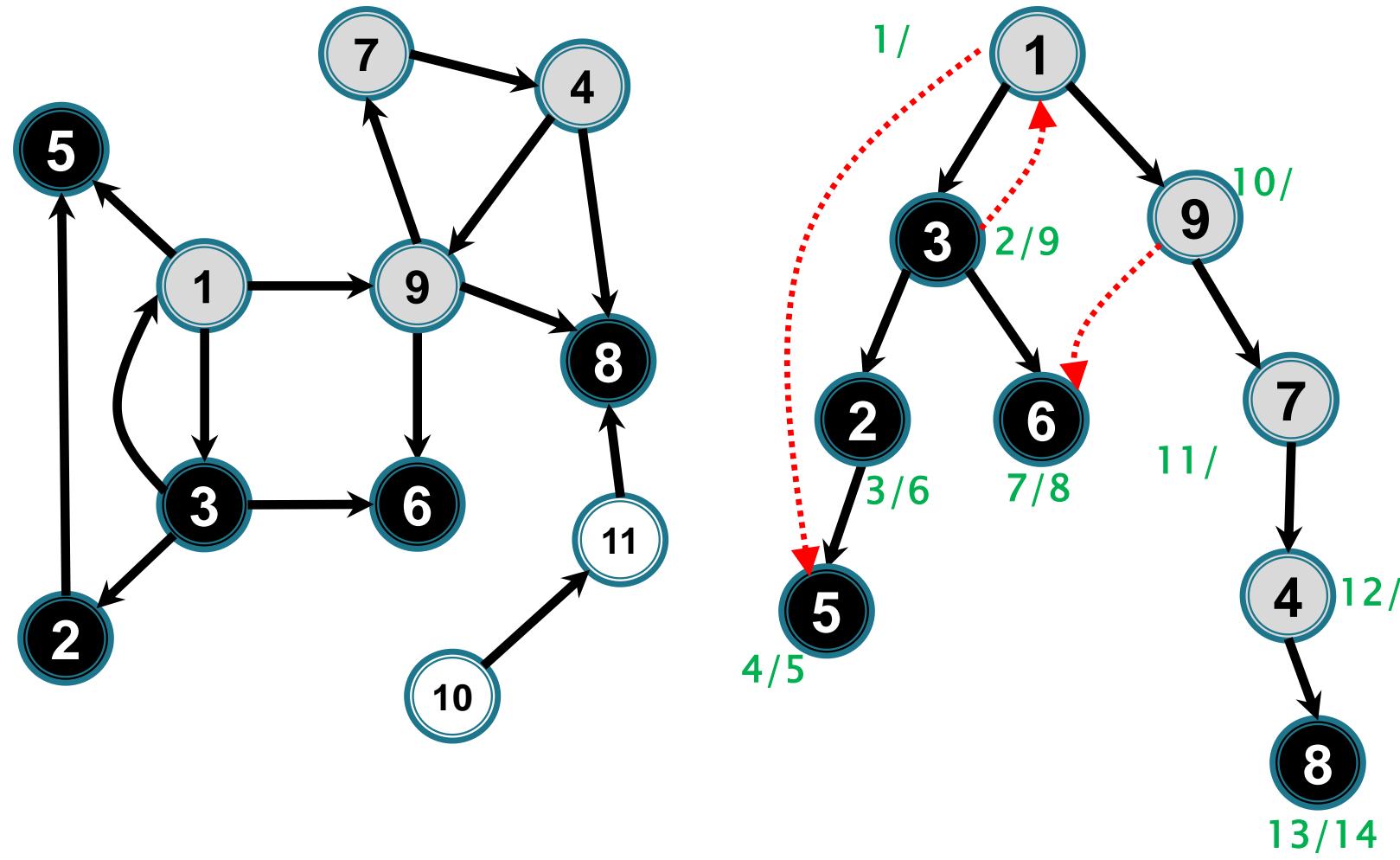
Exemplu graf orientat



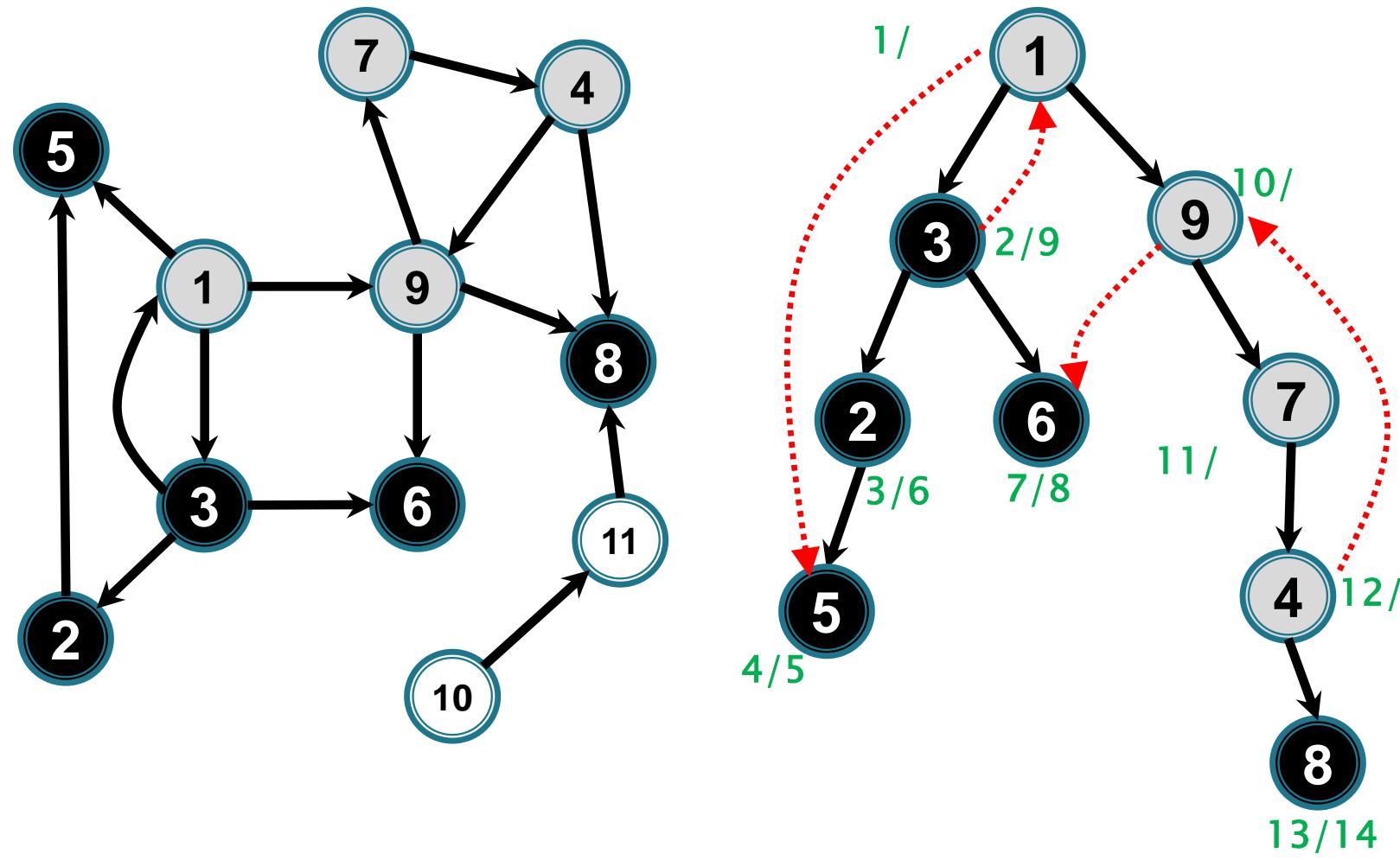
Exemplu graf orientat



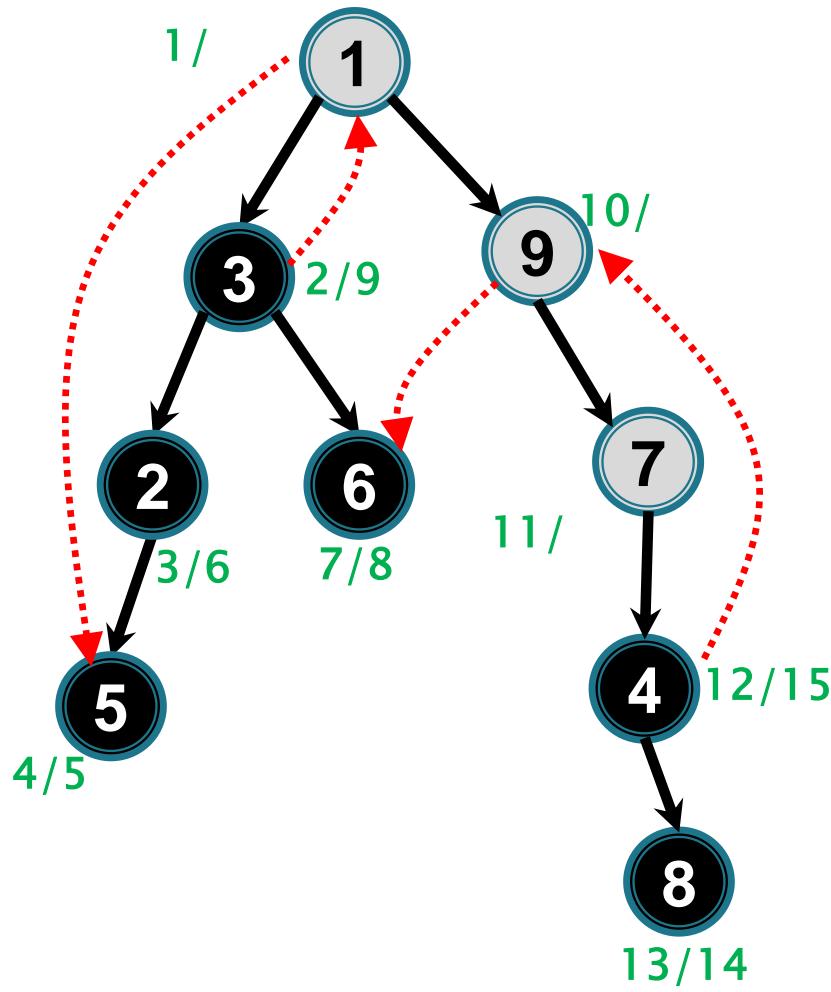
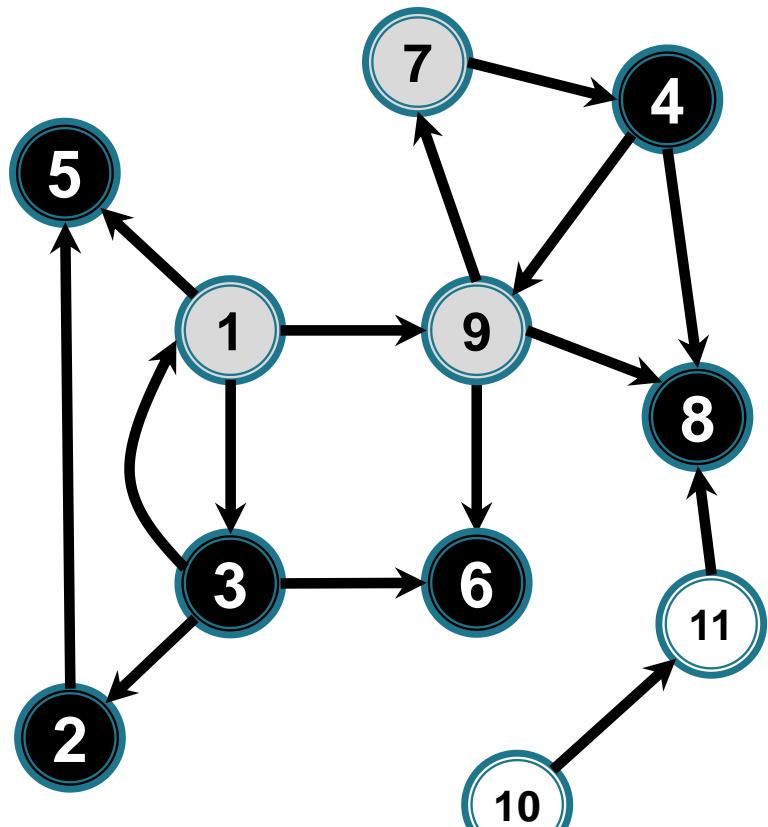
Exemplu graf orientat



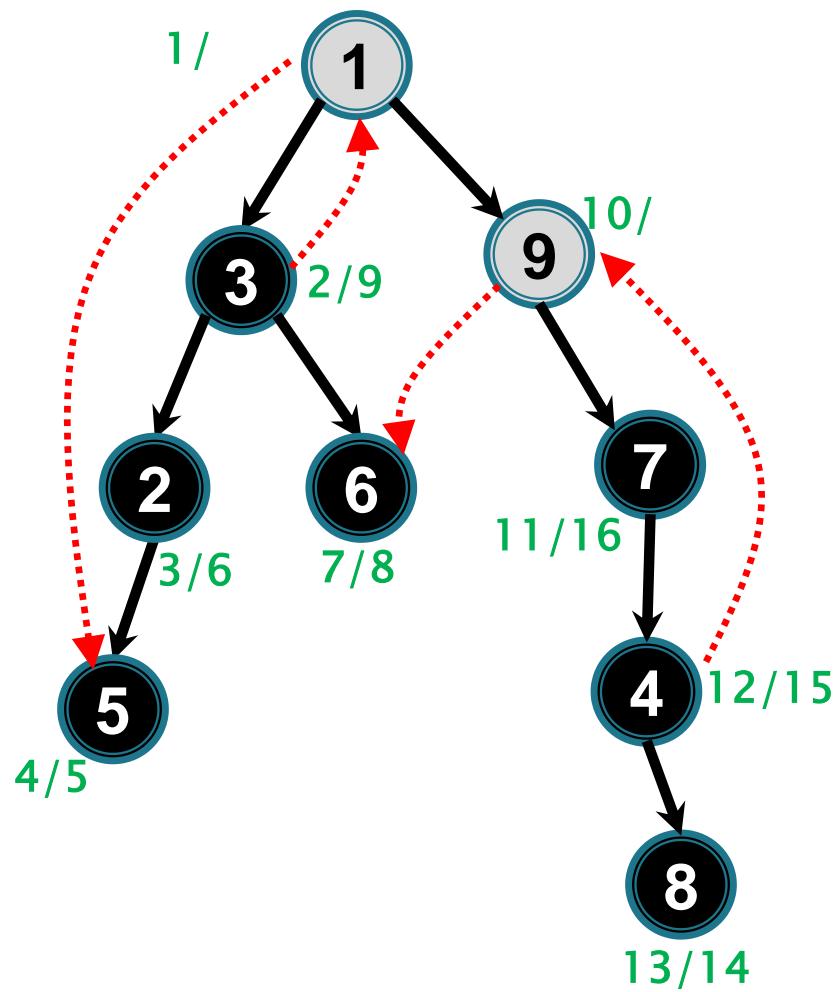
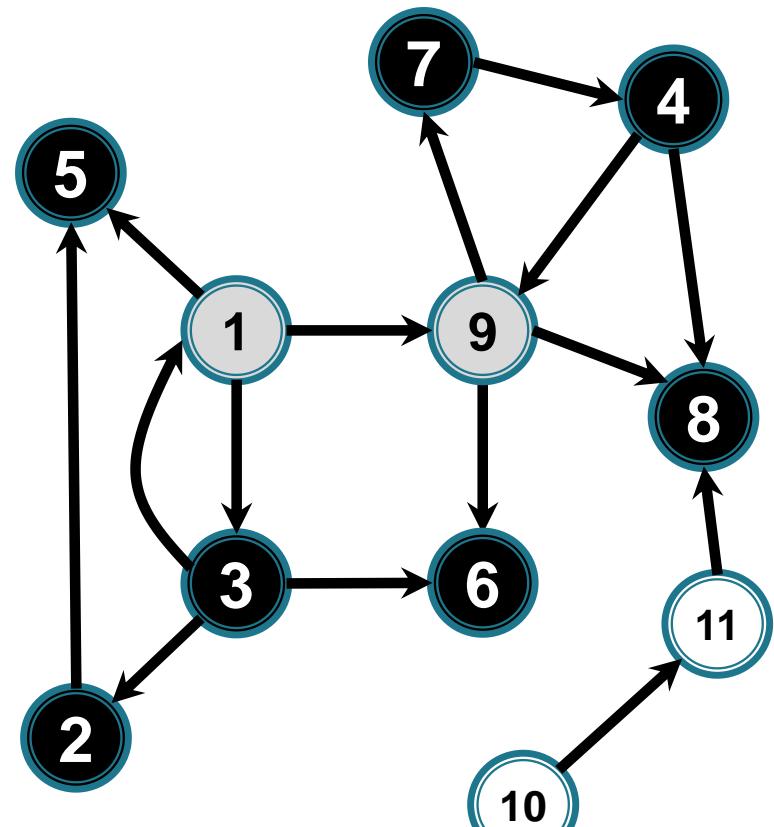
Exemplu graf orientat



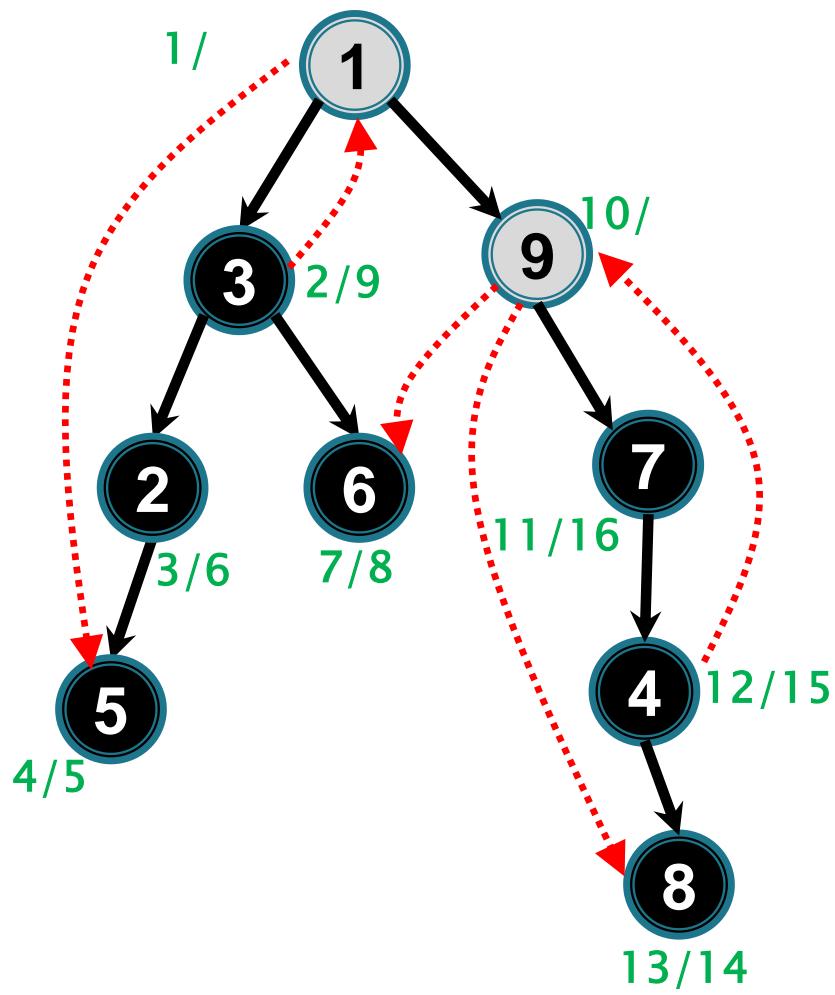
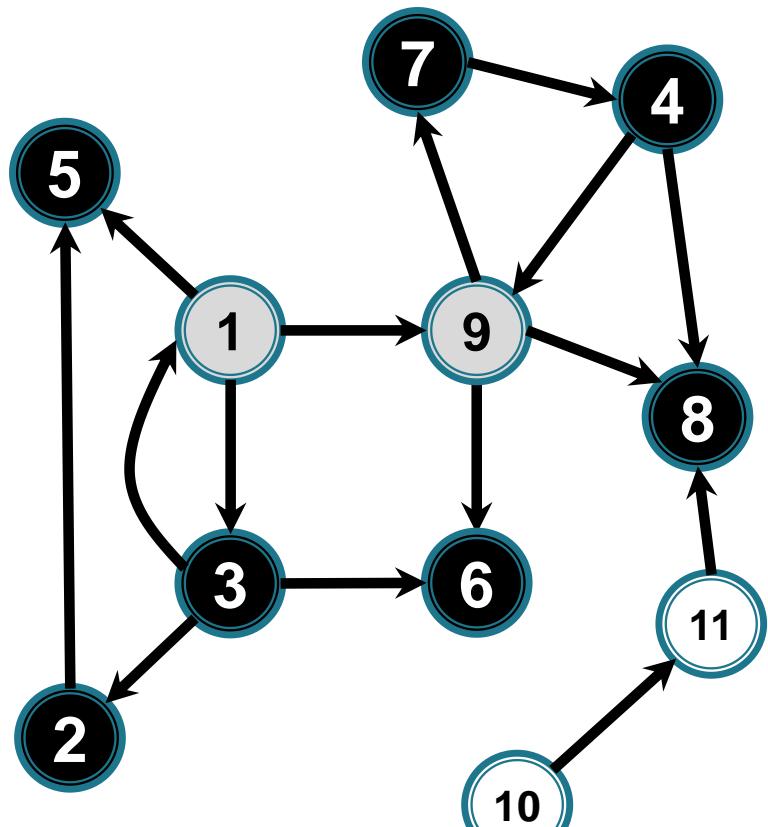
Exemplu graf orientat



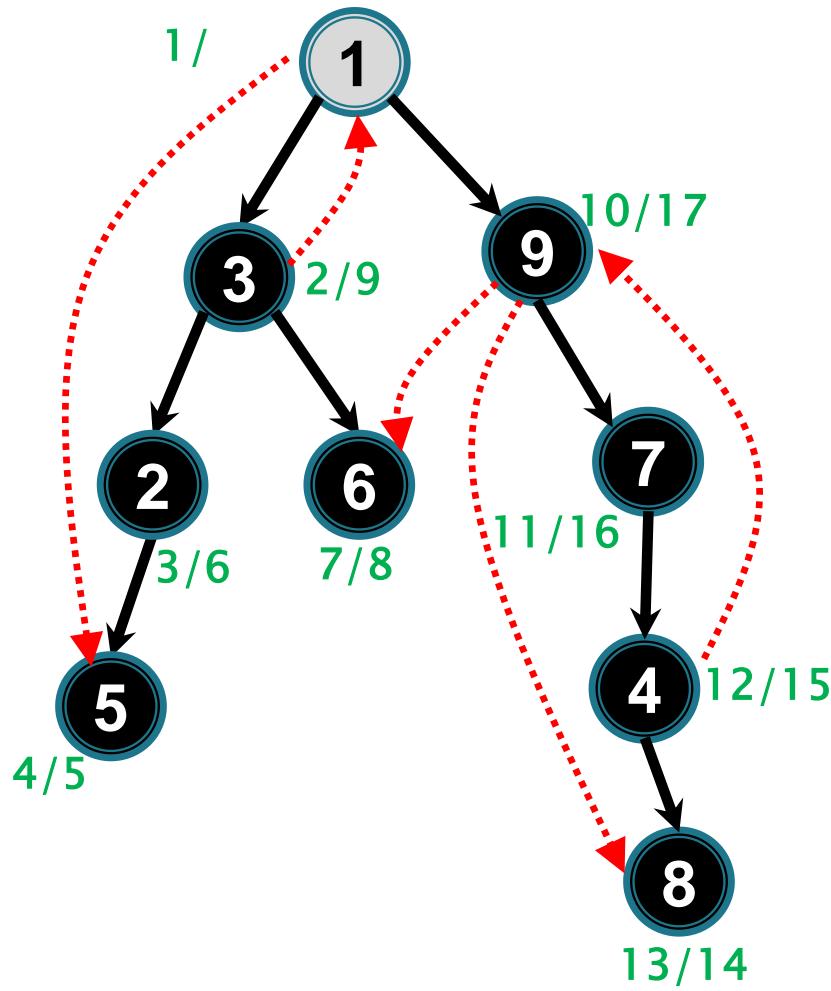
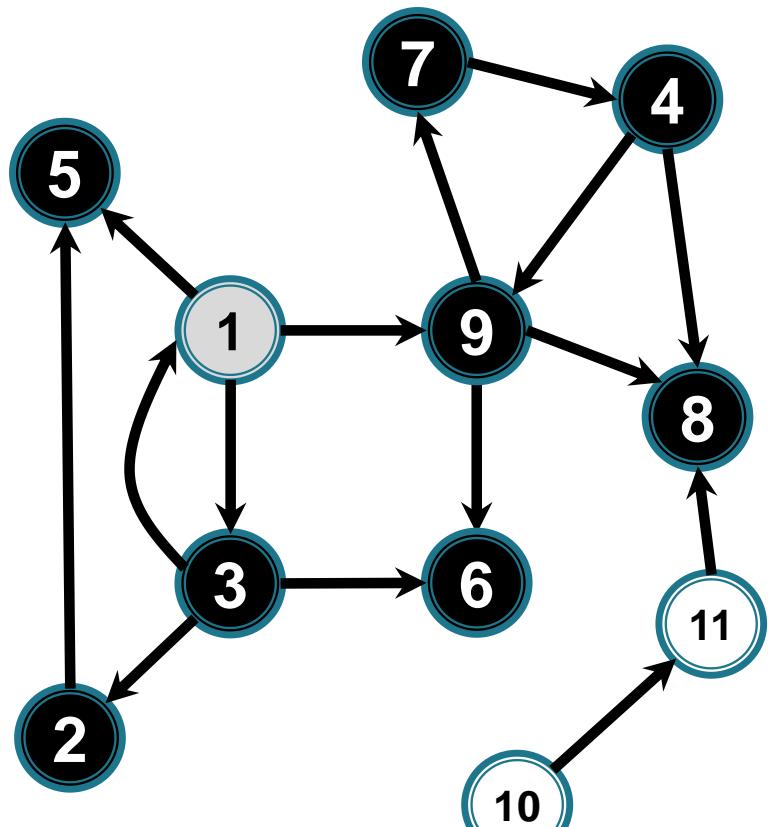
Exemplu graf orientat



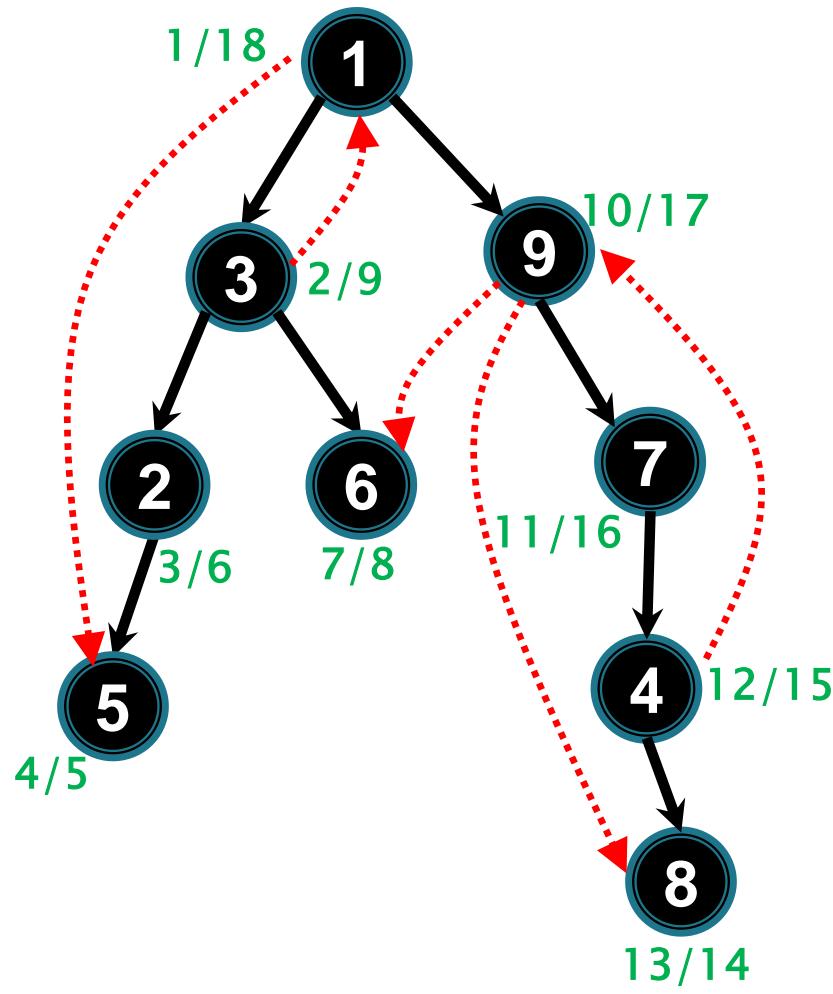
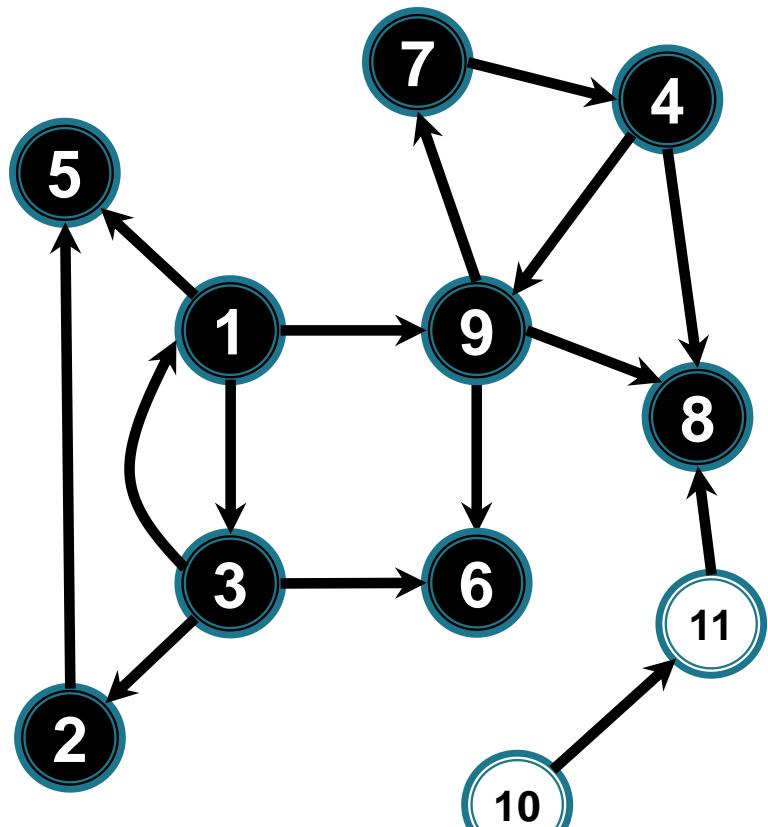
Exemplu graf orientat



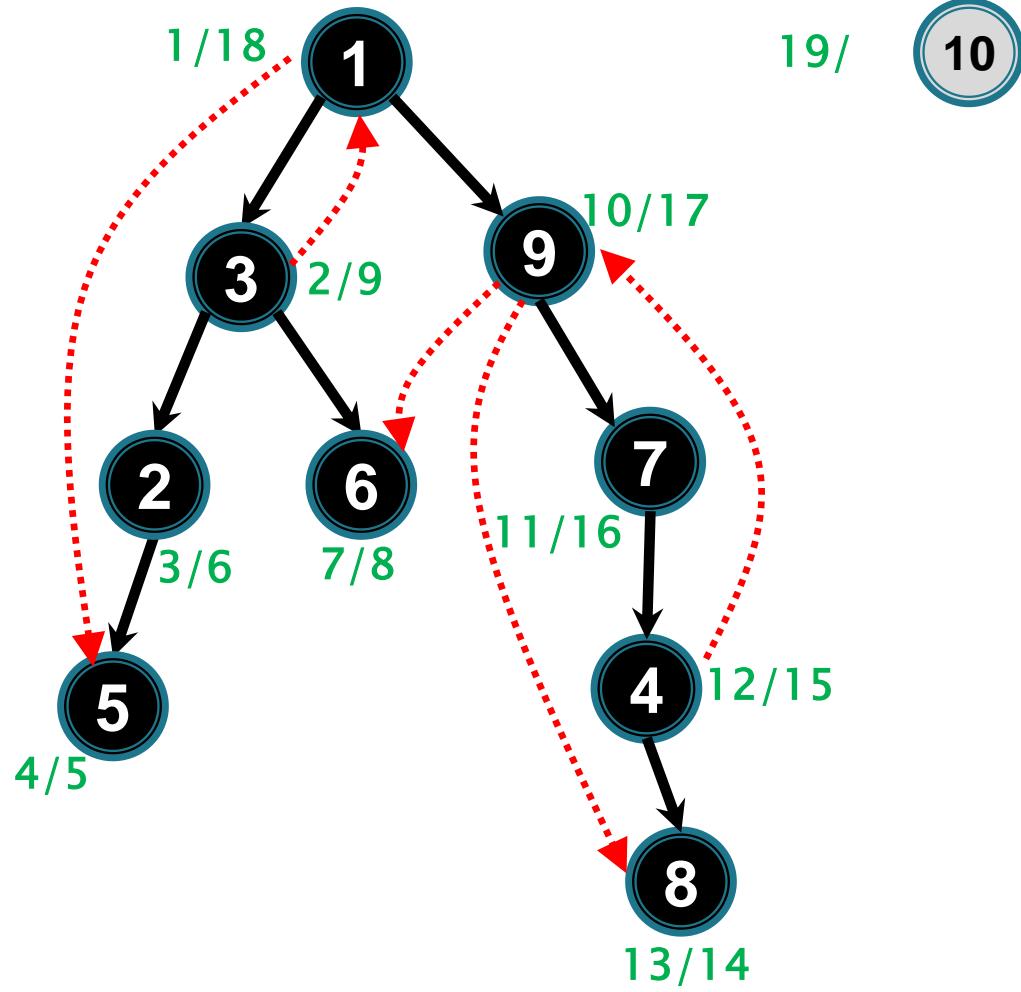
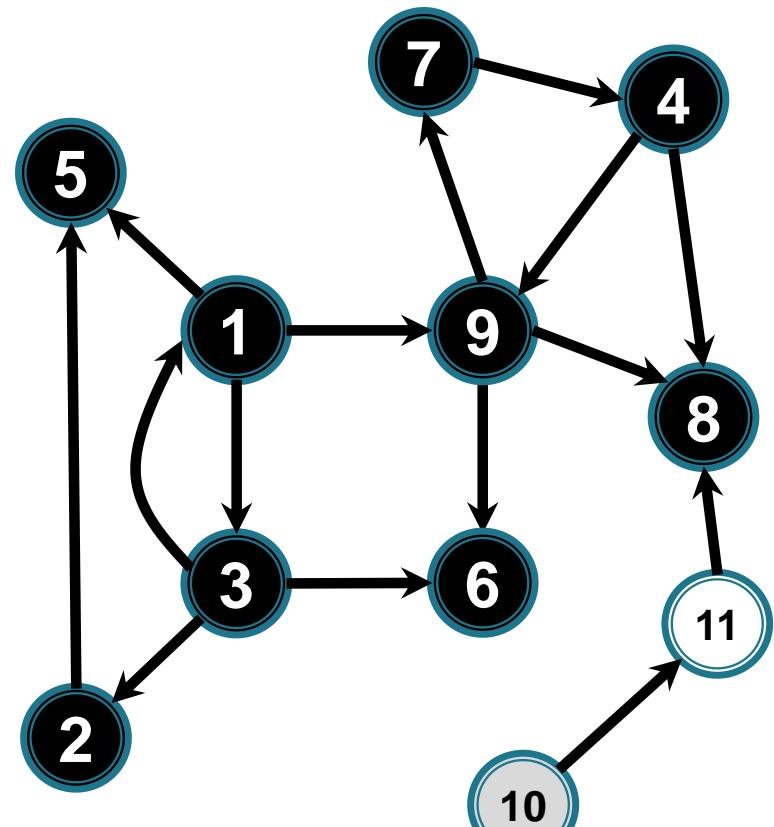
Exemplu graf orientat



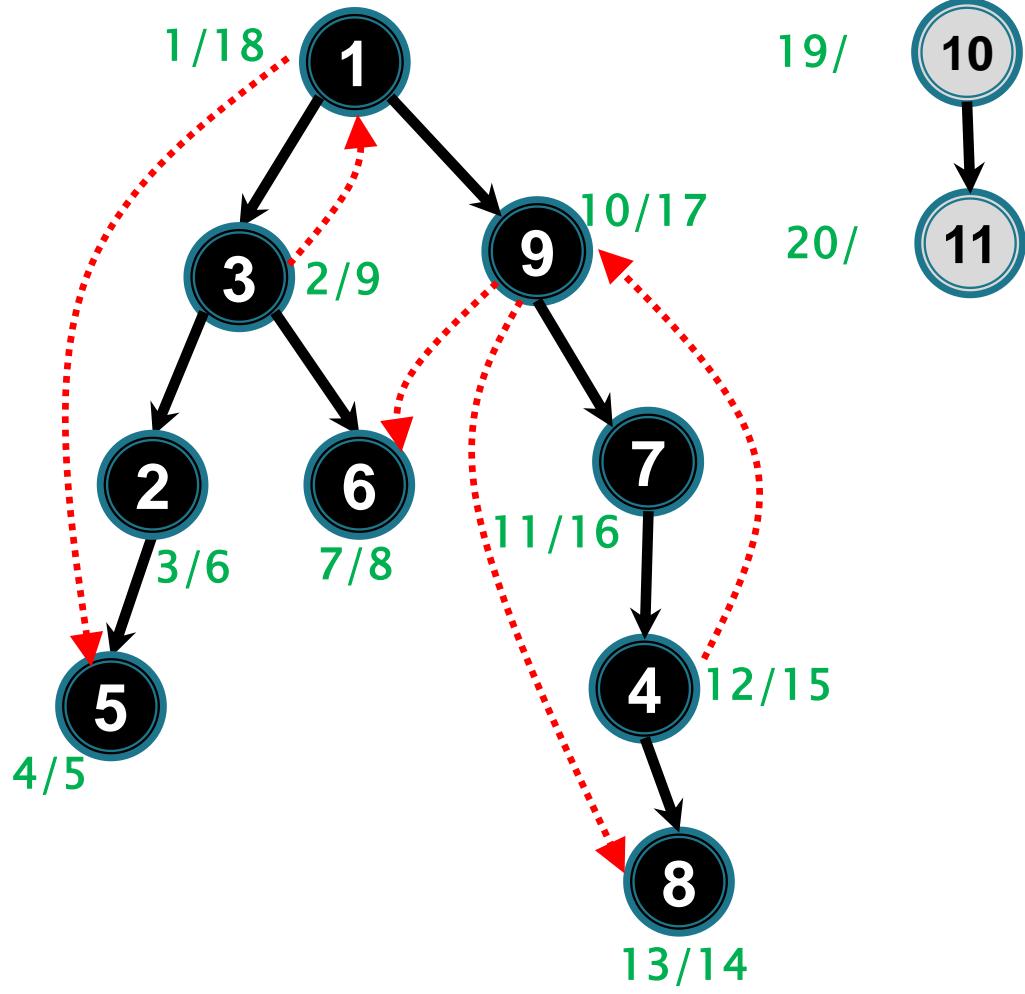
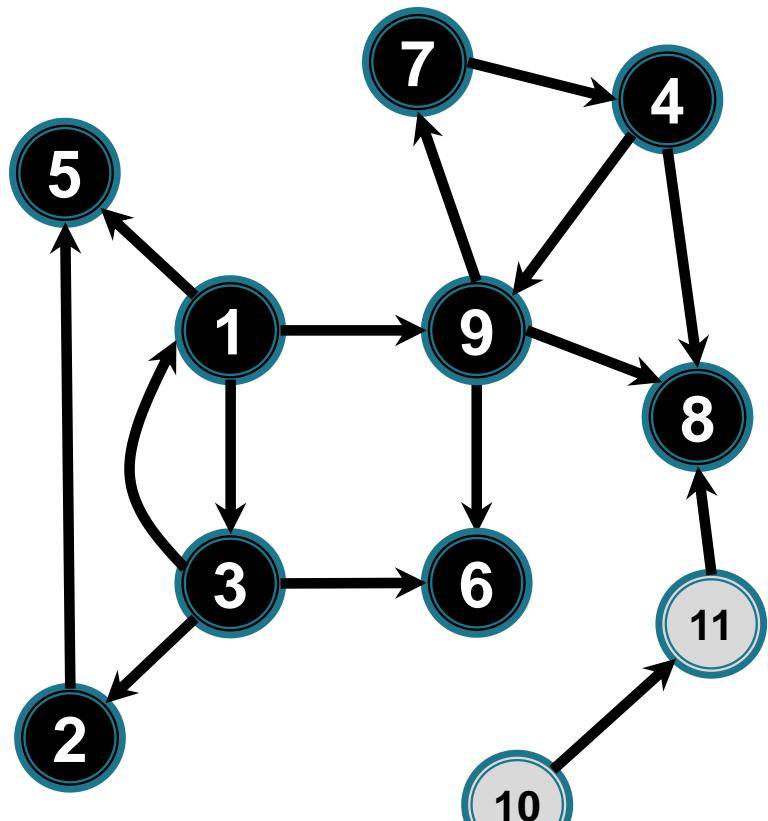
Exemplu graf orientat



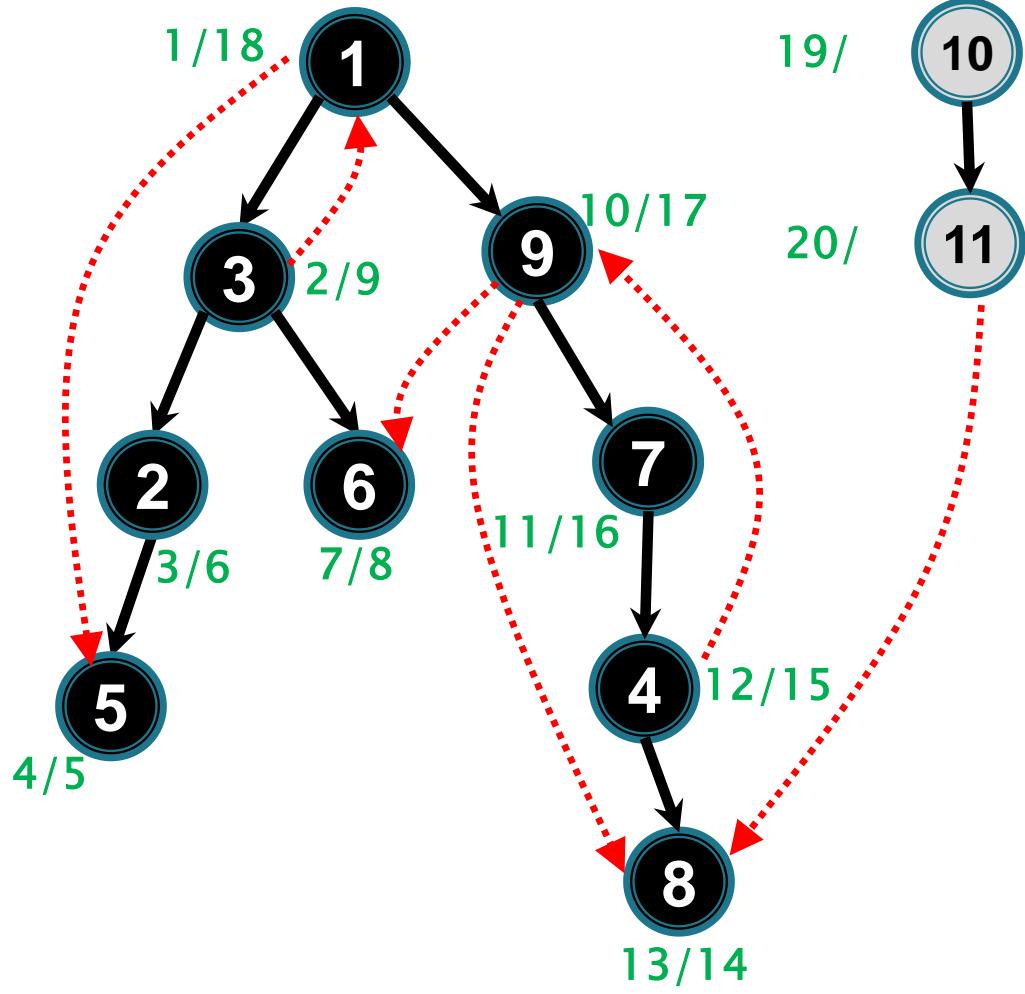
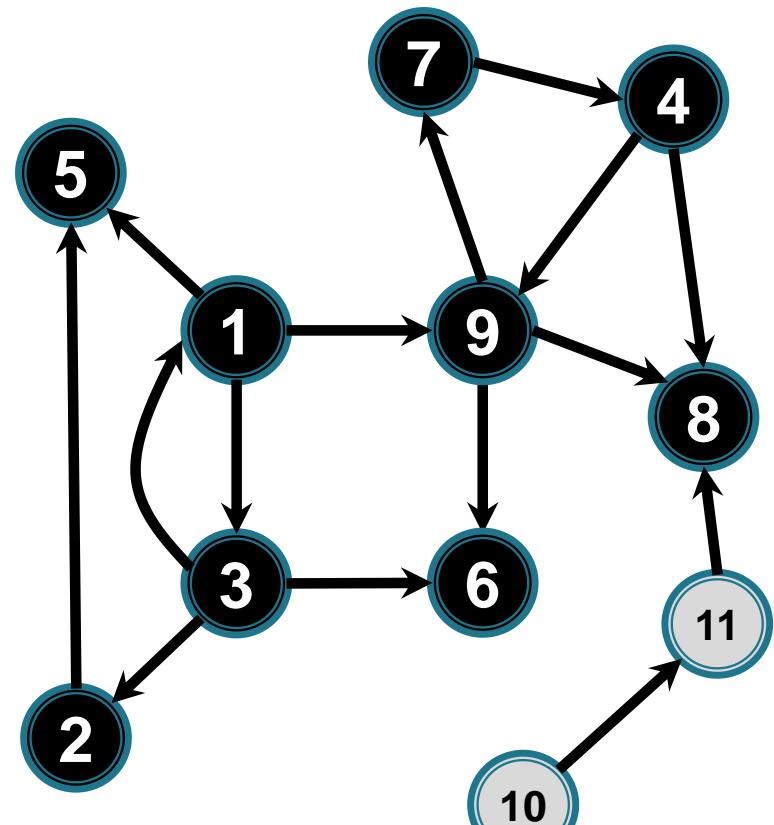
Exemplu graf orientat



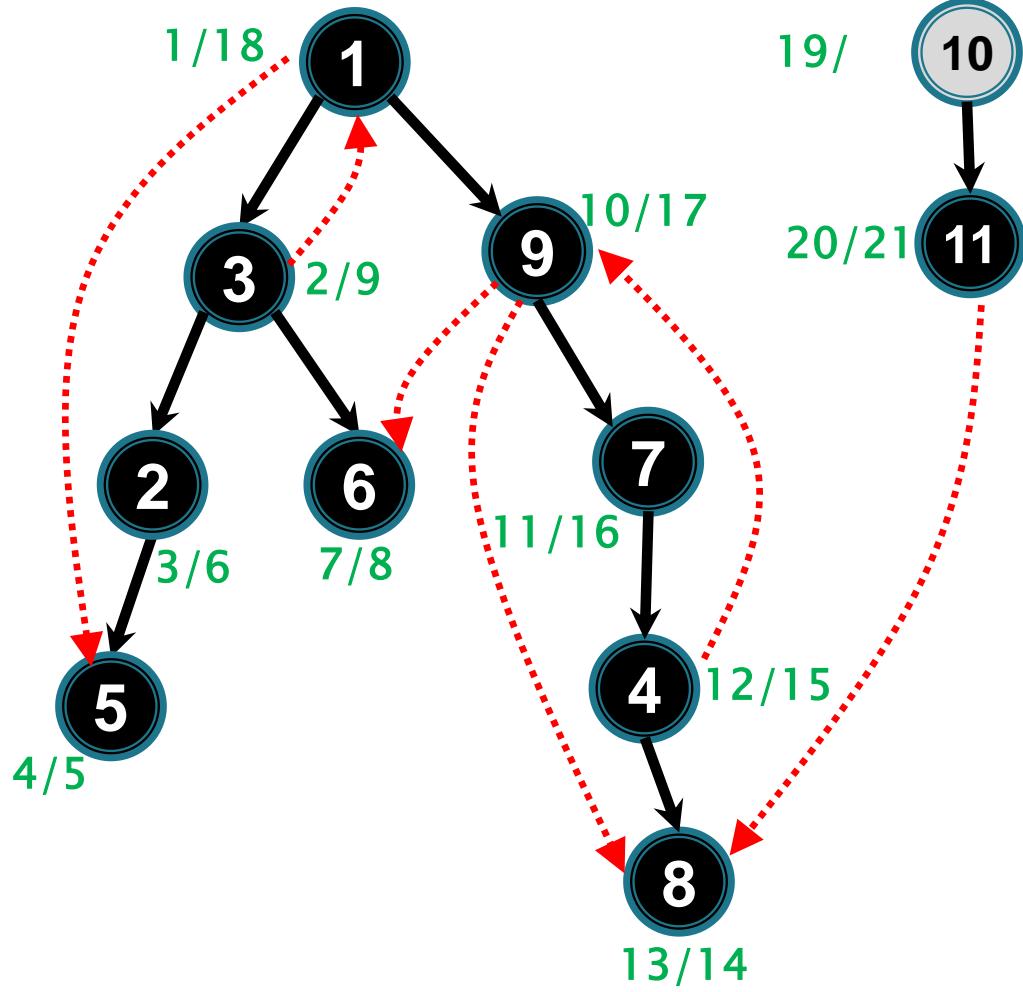
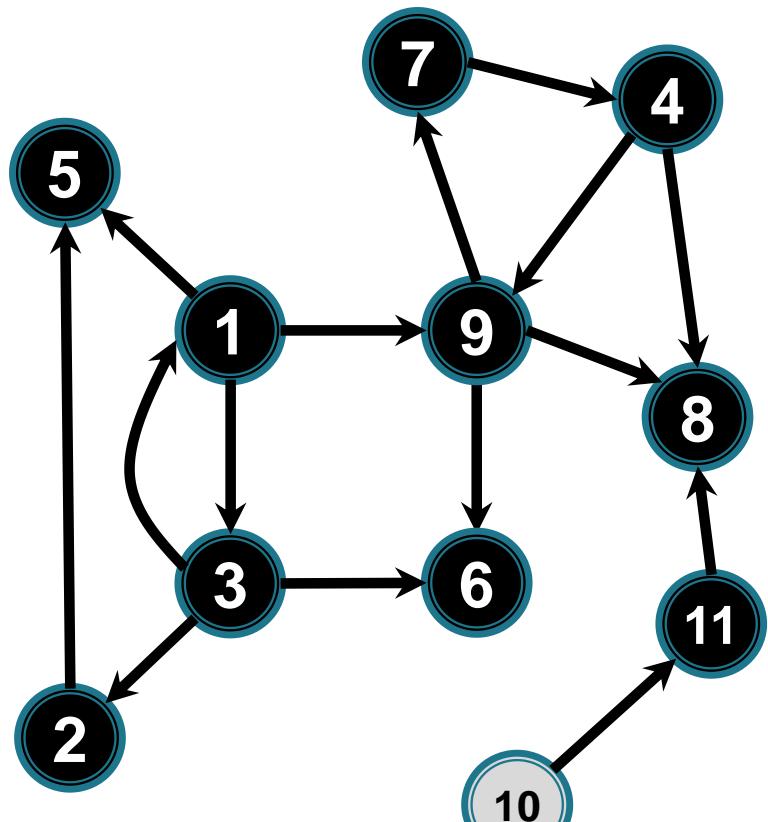
Exemplu graf orientat



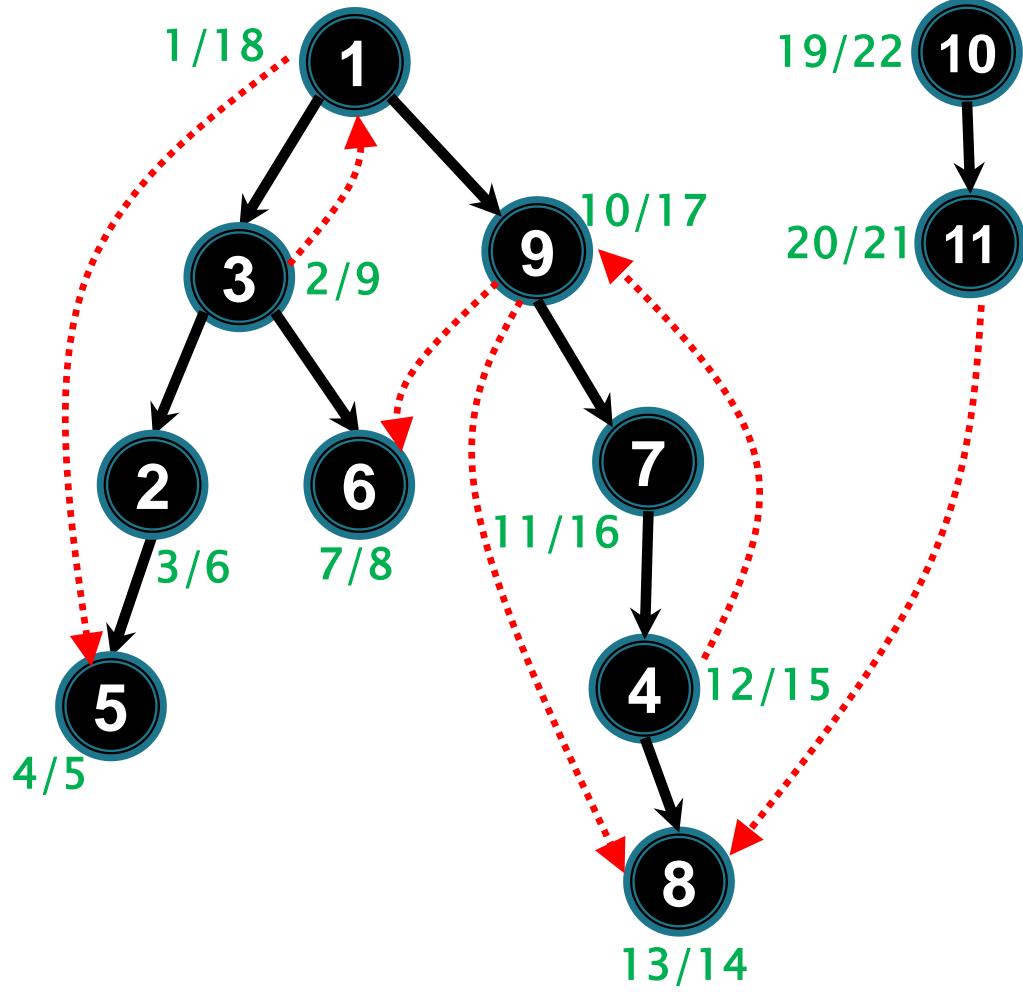
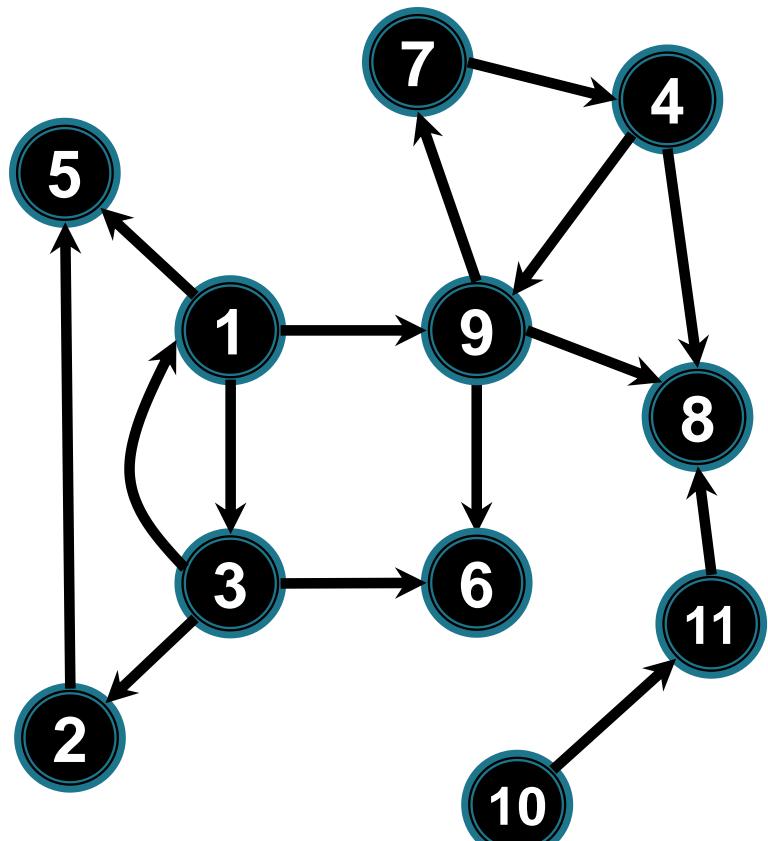
Exemplu graf orientat



Exemplu graf orientat



Exemplu graf orientat



Proprietăți DF

Proprietate

Vârful v este un **descendent** al lui u în pădurea de adâncime DF pentru un graf G (orientat sau neorientat)

dacă și numai dacă

vârful v este descoperit în timp ce u este gri (este încă în explorare)

Au loc rezultate mai generale:

Proprietăți DF

Teorema parantezelor

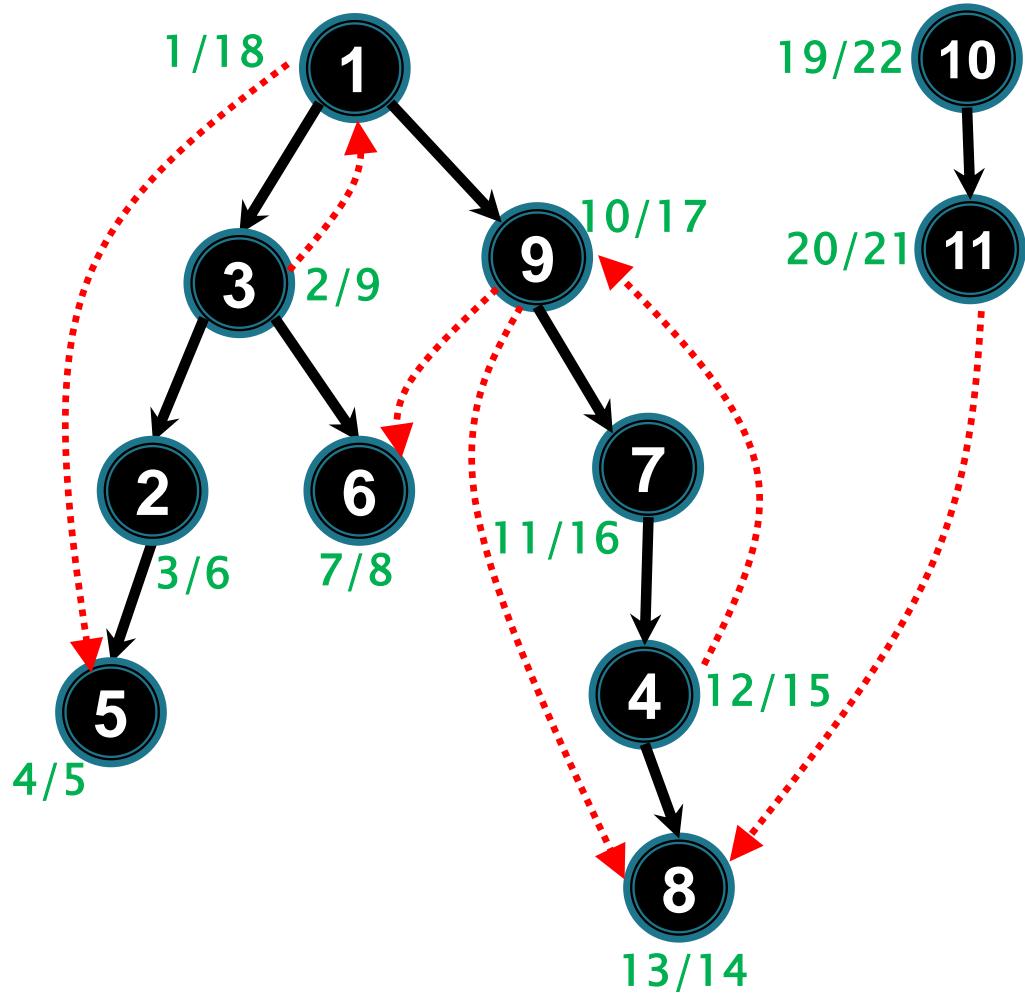
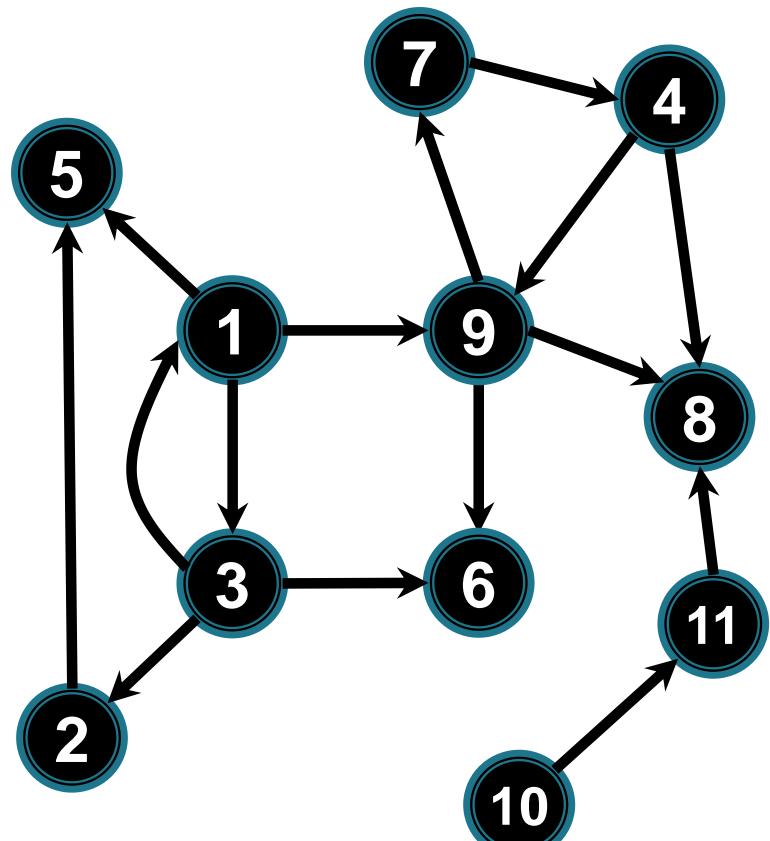
În orice căutare în adâncime a unui graf (orientat sau neorientat) $G = (V, E)$, pentru orice două vârfuri u și v cu

$$\text{desc}[u] < \text{desc}[v]$$

exact una din următoarele condiții este adevărată:

.

.



Proprietăți DF

Teorema parantezelor

În orice căutare în adâncime a unui graf (orientat sau neorientat) $G = (V, E)$, pentru orice două vârfuri u și v cu

$$\text{desc}[u] < \text{desc}[v]$$

exact una din următoarele condiții este adevărată:

- intervalele $[\text{desc}[u], \text{fin}[u]]$ și $[\text{desc}[v], \text{fin}[v]]$ sunt disjuncte și u și v nu sunt unul descendantul celuilalt în arborele/pădurea DF
- $[\text{desc}[v], \text{fin}[v]] \subset [\text{desc}[u], \text{fin}[u]]$,
caz în care v este un descendant al lui u în arborele/pădurea DF

Proprietăți DF

Idee de demonstrație

Avem

$$\text{desc}[u] < \text{desc}[v]$$

- $\text{desc}[v] > \text{fin}[u]$: intervalele sunt disjuncte; u este deja negru când v a fost descoperit, deci v nu este descendant al lui u și nici invers
- $\text{desc}[v] < \text{fin}[u]$: v este descoperit în timp ce u este gri, deci este descendant al lui u; atunci v va fi finalizat înaintea lui u, deci

$$[\text{desc}[v], \text{fin}[v]] \subset [\text{desc}[u], \text{fin}[u]]$$

Proprietăți DF

Proprietate (Incluziunea intervalelor descendenților)

Vârful v este un **descendent** al lui u în pădurea de adâncime DF pentru un graf G (orientat sau neorientat)

\Leftrightarrow

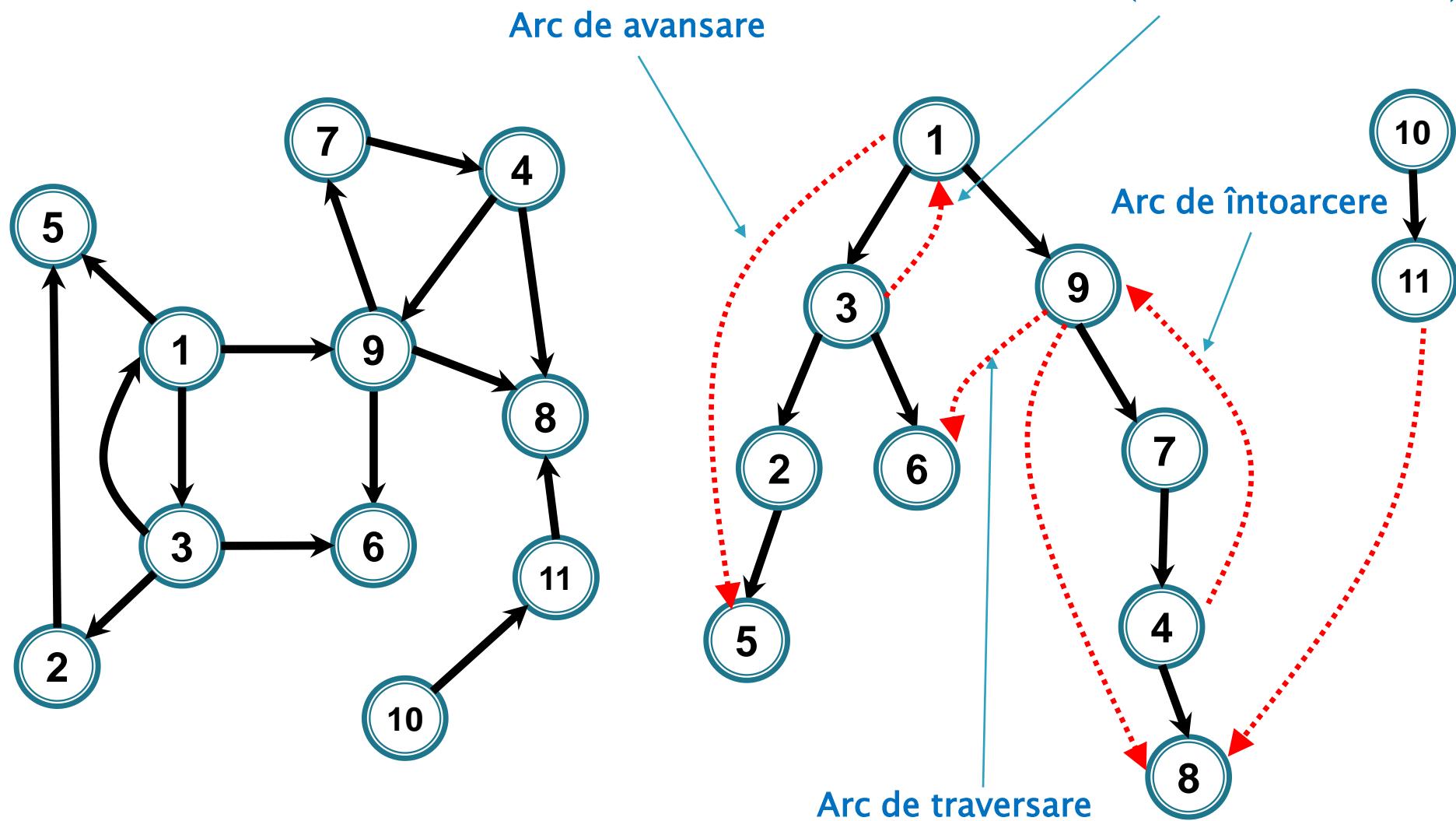
vârful v este descoperit în timp ce u este gri (este încă în explorare)

\Leftrightarrow

$$[\text{desc}[v], \text{fin}[v]] \subset [\text{desc}[u], \text{fin}[u]]$$

Proprietăți DF

- În raport cu pădurea DF muchiile/arcele se împart în 4 categorii:



Proprietăți DF

În raport cu pădurea DF muchiile/arcele se împart în 4 categorii:

▶ **de arbore DF (de avansare directă/ de arbore):**

(u, v) cu v fiu al lui u (v a fost descoperit din u)

▶ **de întoarcere (înapoi) :**

(u, v) cu v strămoș al lui u (și care nu este de arbore)

▶ **de avansare (de avansare înainte) :**

(u, v) cu v descendant al lui u care nu este însă fiu al lui

▶ **de traversare (transversale) :**

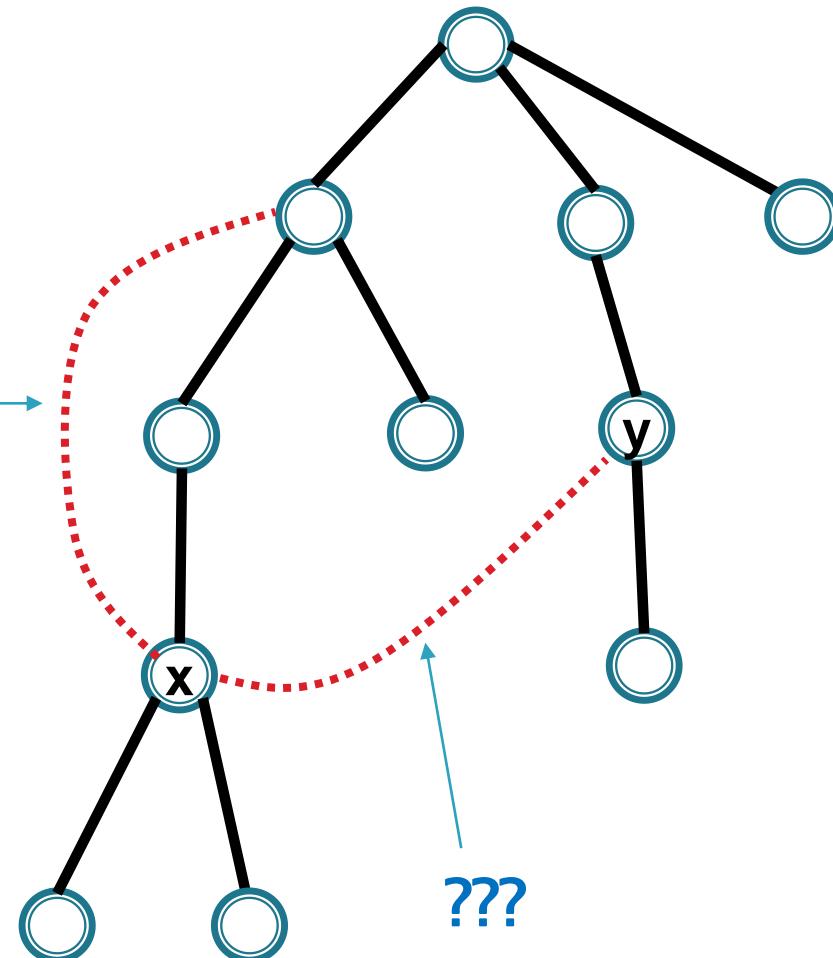
toate celelalte muchii;

pot fi între vârfuri din același arbore DF cu condiția ca unul să nu fie strămoșul celuilalt sau pot uni vârfuri din arbori DF diferiți

Proprietăți DF

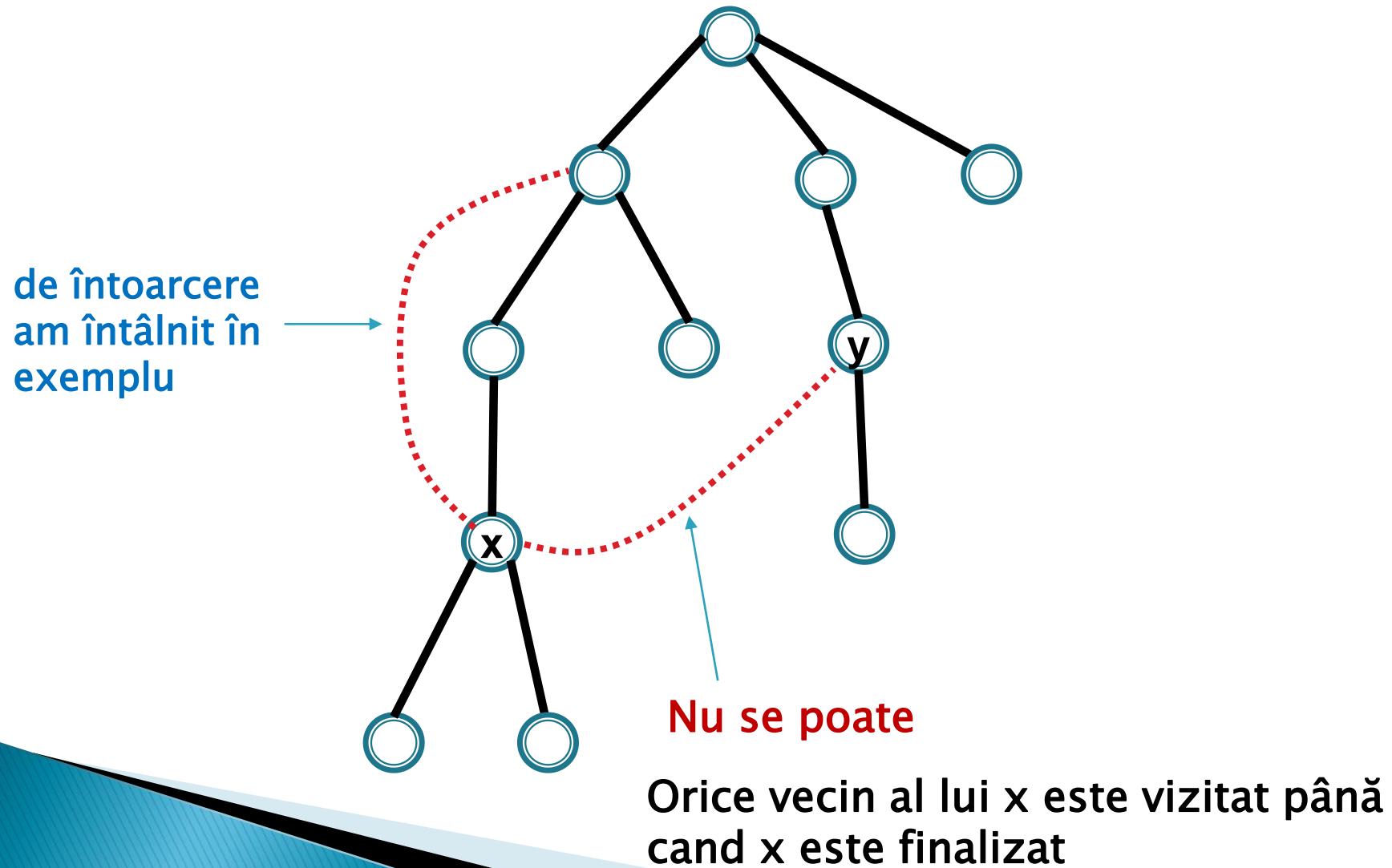
Ce tipuri de muchii pot apărea în cazul unui graf **neorientat** ?

de întoarcere
am întâlnit în
exemplu



Proprietăți DF

Ce tipuri de muchii pot apărea în cazul unui graf **neorientat** ?



Proprietăți DF

În cazul unui graf **neorientat** există doar două tipuri de muchii în raport cu pădurea DF:

- ▶ muchii de arbore (**de avansare**)
- ▶ muchii de întoarcere (**către un ascendent**)
 - !! care nu este tata

Proprietăți DF

În cazul unui graf **neorientat** există doar două tipuri de muchii în raport cu pădurea DF:

- ▶ muchii de arbore (**de avansare**)
- ▶ muchii de întoarcere (**către un ascendent**)

Proprietăți DF

În cazul unui graf **neorientat** există doar două tipuri de muchii în raport cu pădurea DF:

- ▶ muchii de arbore (**de avansare**)
- ▶ muchii de întoarcere (**către un ascendent**)

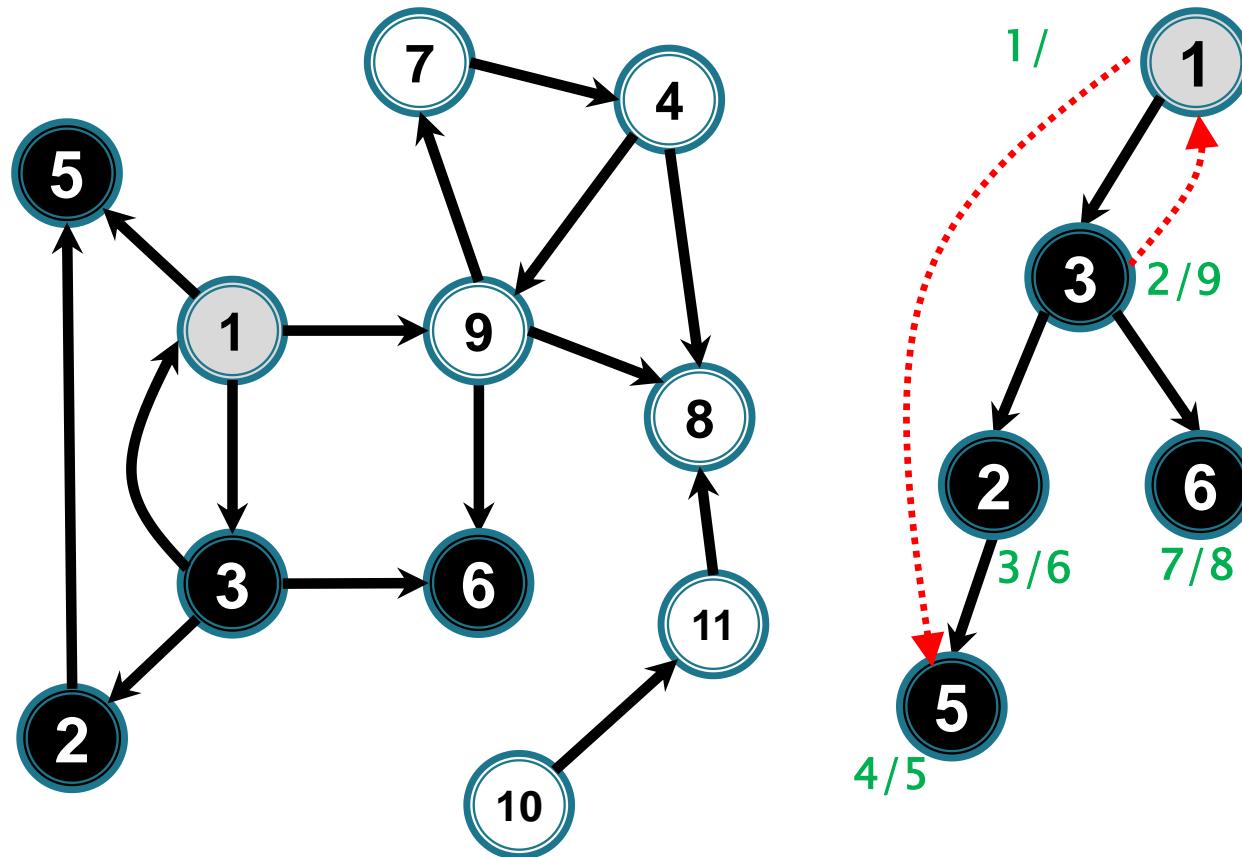
O muchie este detectată în timpul parcurgerii DF ca fiind de întoarcere dacă unește vârful curent cu un vârf **gri** (=vizitat+ascendent al său) care nu este tatăl lui

Un arc (u,v) este detectat ca fiind

- de avansare directă (de arbore): v este nevizitat (alb)
- de avansare înainte:

`desc[u] < desc[v] < fin[v] < fin[u]` și v nu e fiu \Leftrightarrow

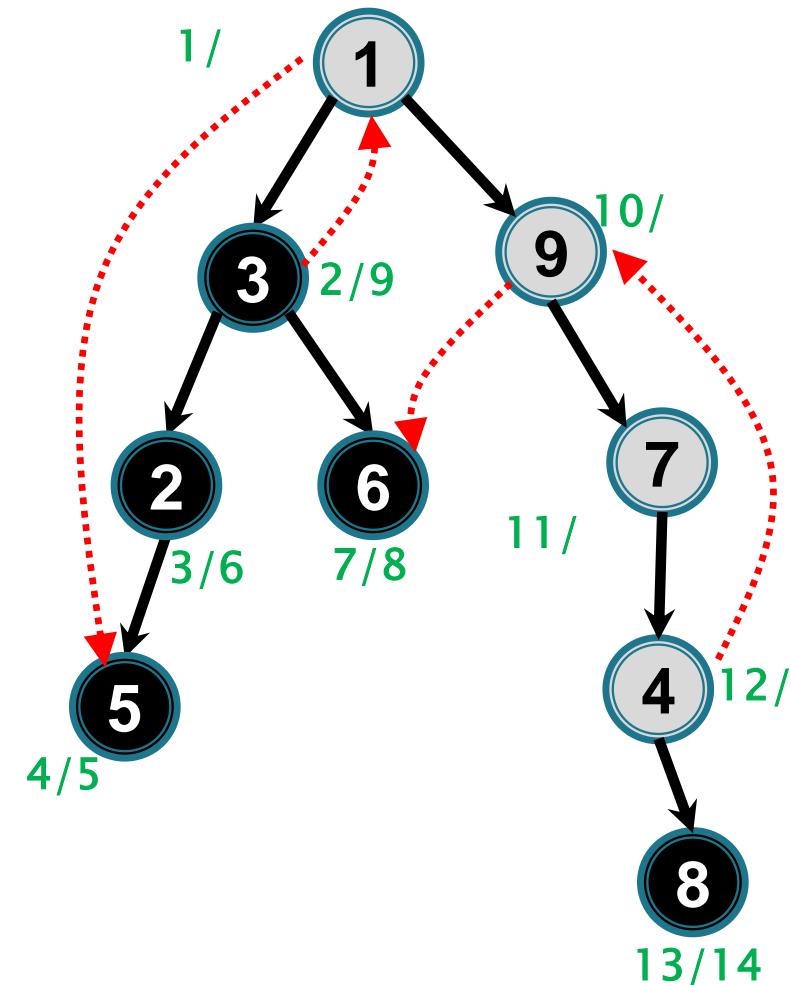
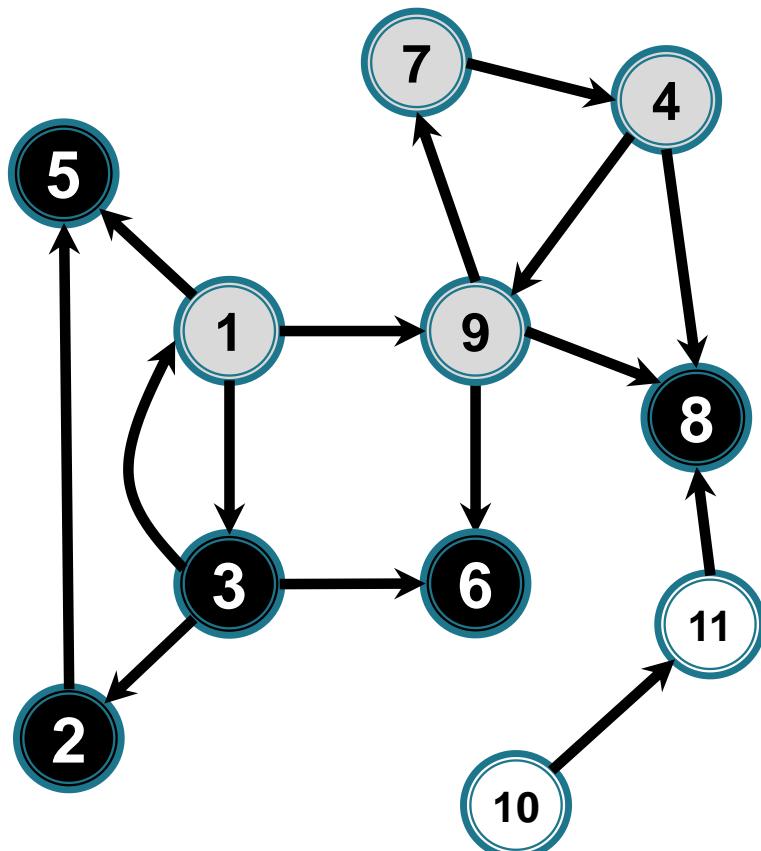
când este parcurs arcul uv , v este negru (finalizat) și este
descendent al lui u , adică $desc[u] < desc[v]$



- de întoarcere:

`desc[v] < desc[u] < fin[u] < fin[v] \Leftrightarrow`

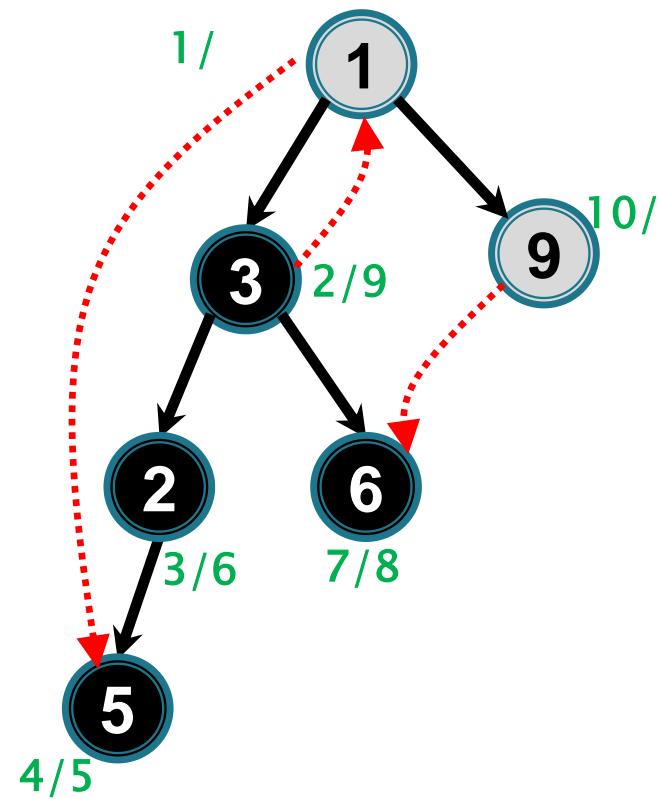
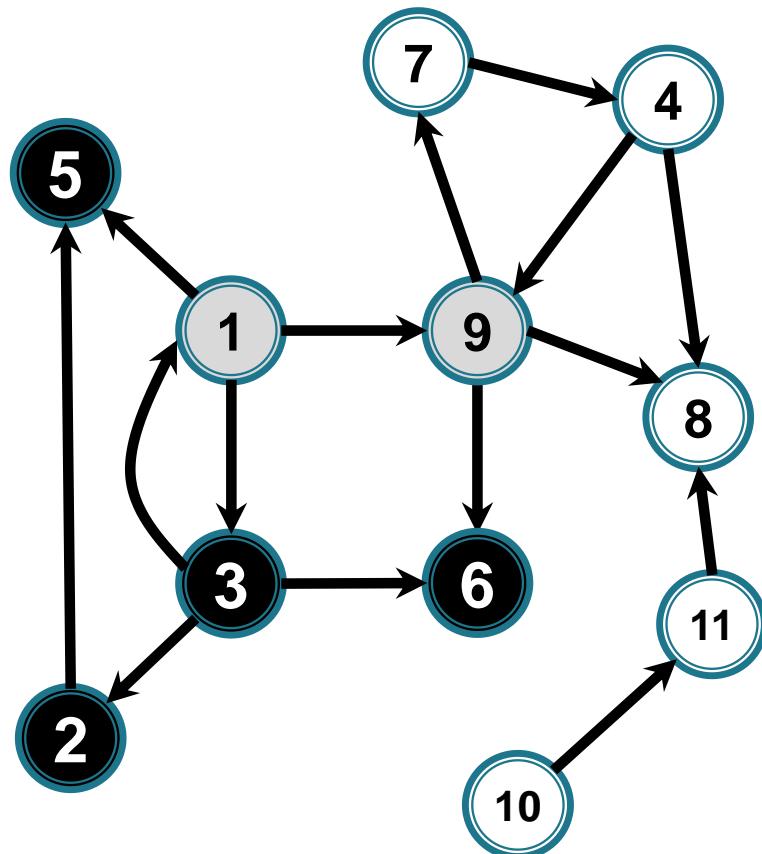
când este parcurs arcul uv , v este încă gri (nefinalizat)



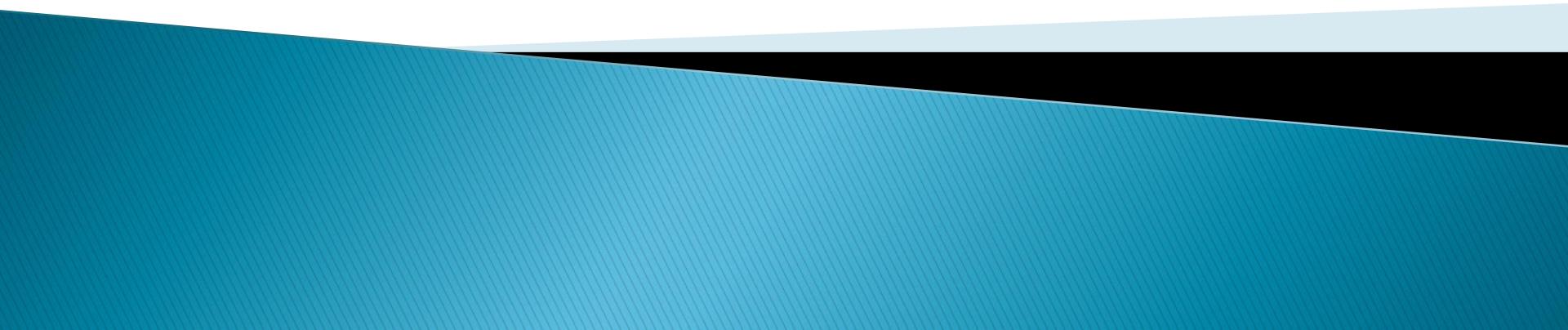
- de traversare:

`desc[v] < fin[v] < desc[u] < fin[u] \Leftrightarrow`

când este parcurs arcul uv , v este negru și nu este
descendent al lui u , adică `desc[u] > desc[v]`



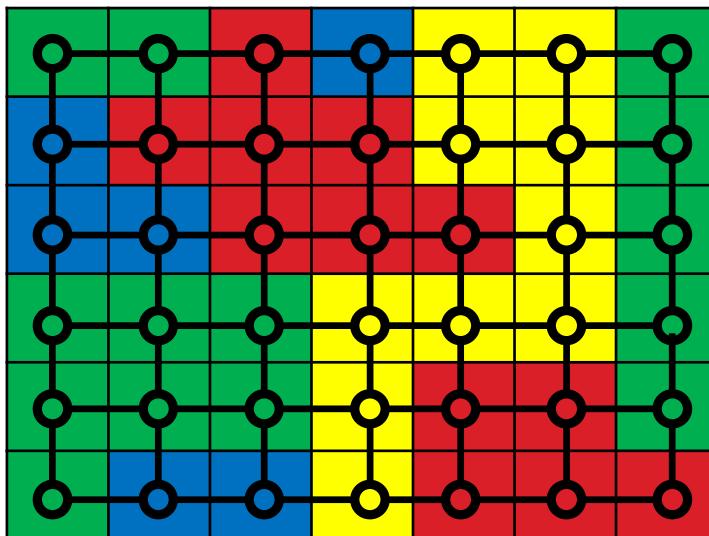
Parcurgerea în adâncime - Aplicații



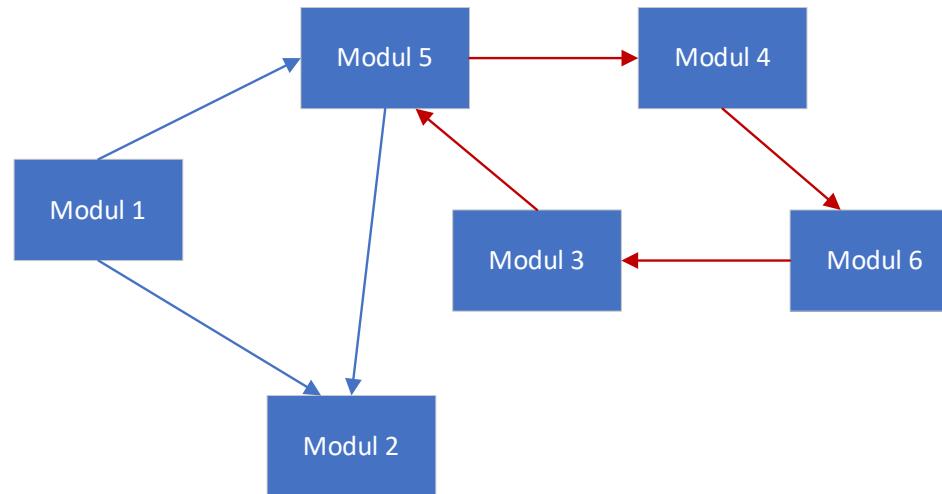
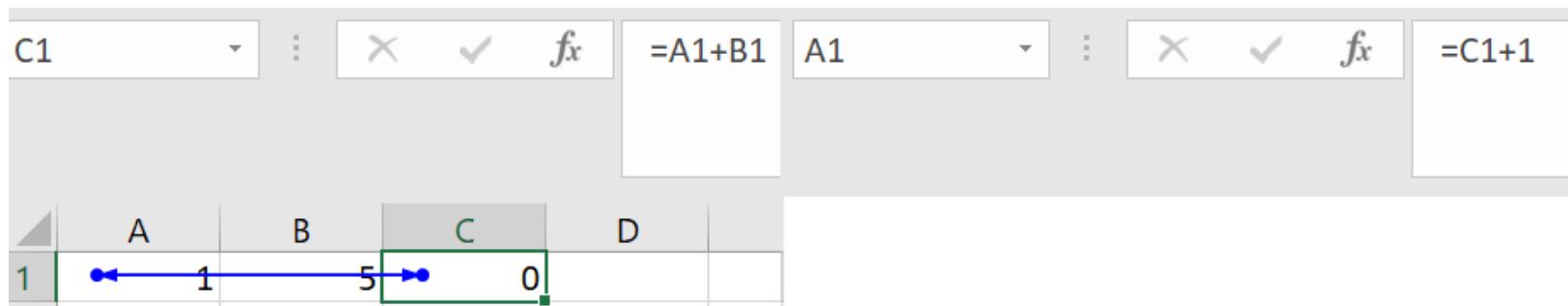
Determinarea componentelor conexe

Determinarea unui arbore parțial

- ▶ Ca și la parcurgerea în lățime
- ▶ Aplicații – algoritm de umplere (fill)



Determinarea de cicluri / circuite



Determinarea de cicluri / circuite

- ▶ Ce fel de muchii/arce închid cicluri/circuite?

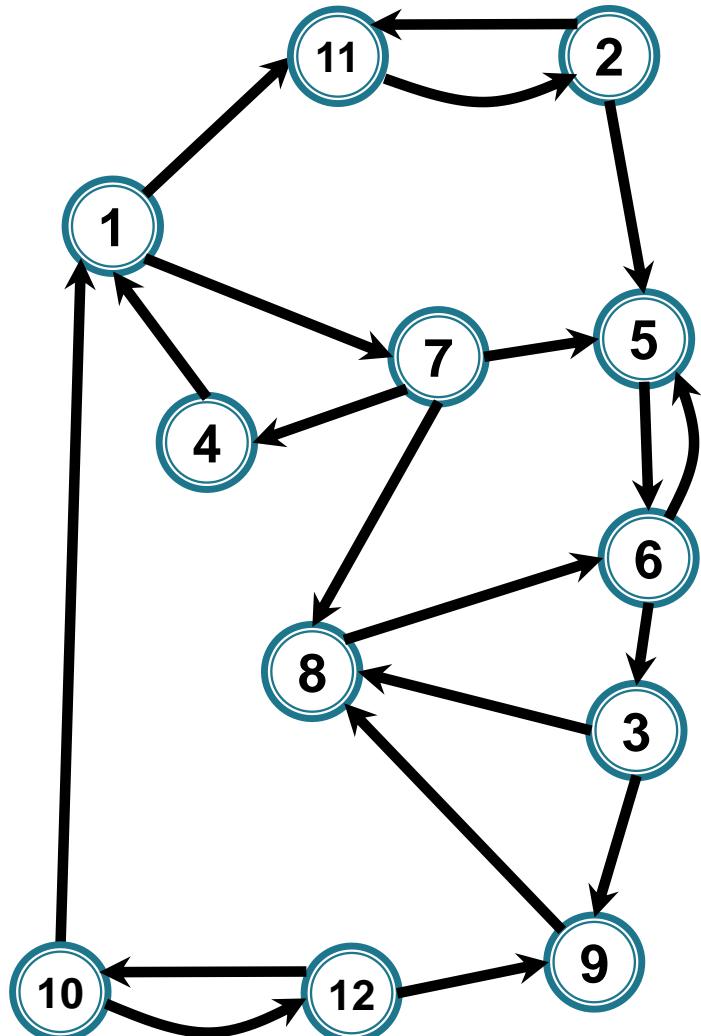
Determinarea de cicluri / circuite

- ▶ Ciclu/circuit – închis doar de muchii/arce de întoarcere

Un graf neorientat/orientat G are ciclu/circuit dacă și numai dacă există muchie/arc de întoarce uv în pădurea DFS

= de la un vârf u la un vârf gri (nefinalizat)

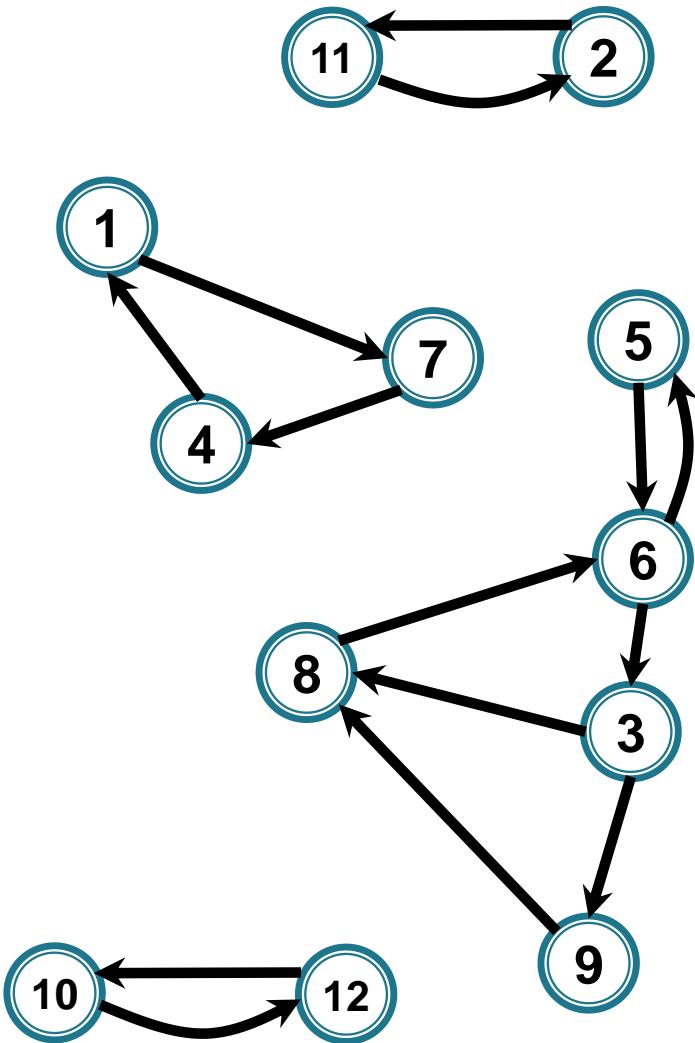
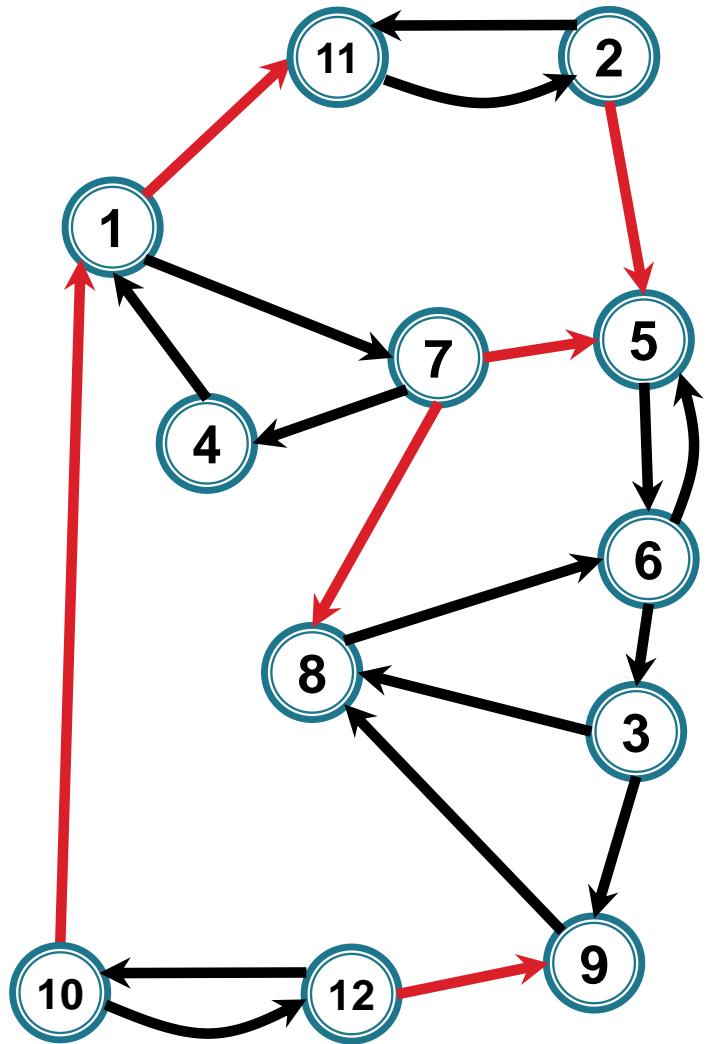
Determinarea componentelor tare conexe ale unui graf orientat



Fie $G=(V,E)$ orientat

- G este **tare conex** dacă între oricare două vârfuri există un drum
- O **componentă tare conexă** a lui G = subgraf inducțional al lui G tare conex, maximal

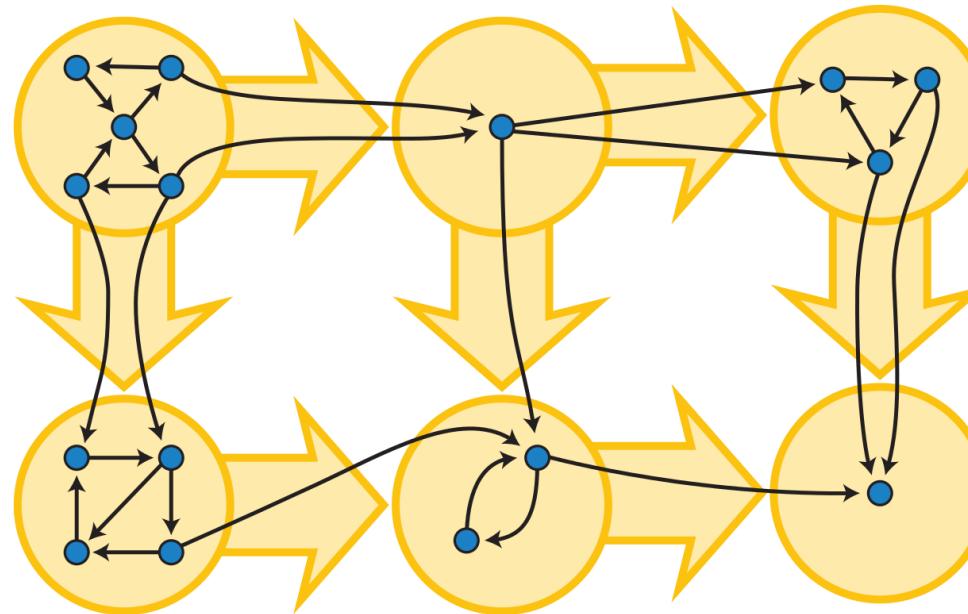
Componente tare conexe



Componentele tare conexe

Componente tare conexe

- ▶ Detectarea de comunități în rețele (sociale, de colaborare/citări, economice)



- ▶ Etape în alți algoritmi, rezolvarea altor probleme, precum 2-SAT

Algoritmi componente tare conexe

- ▶ Folosind mai multe parcurgeri?

Posibilă idee:

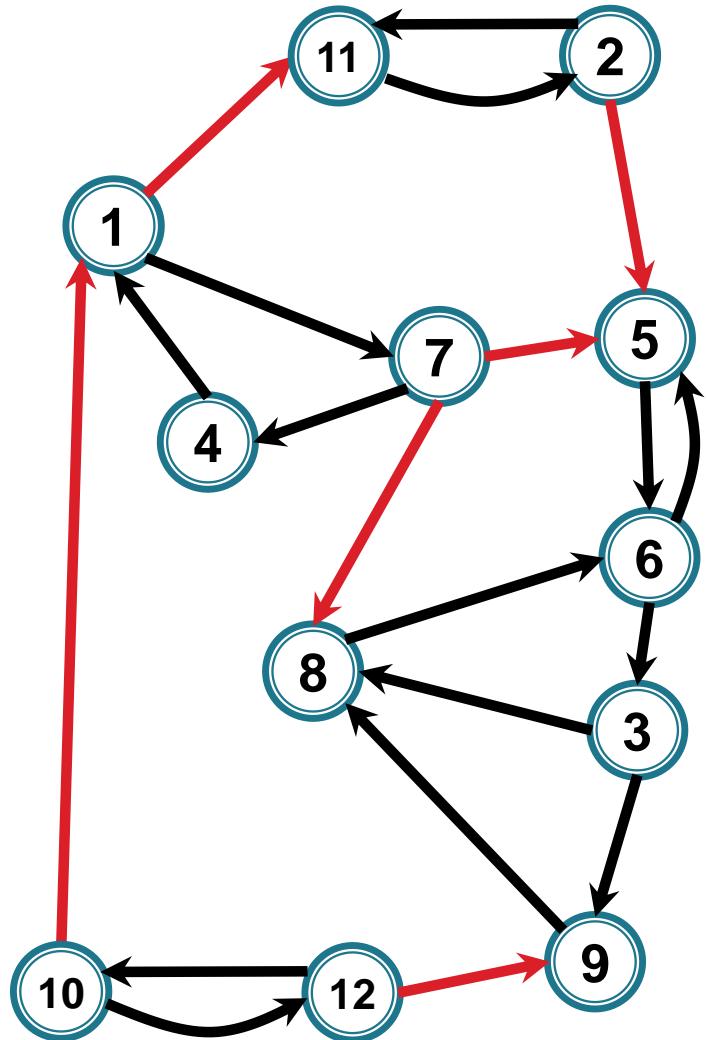
componenta(x) =

multimea vârfurilor accesibile din x în G \cap

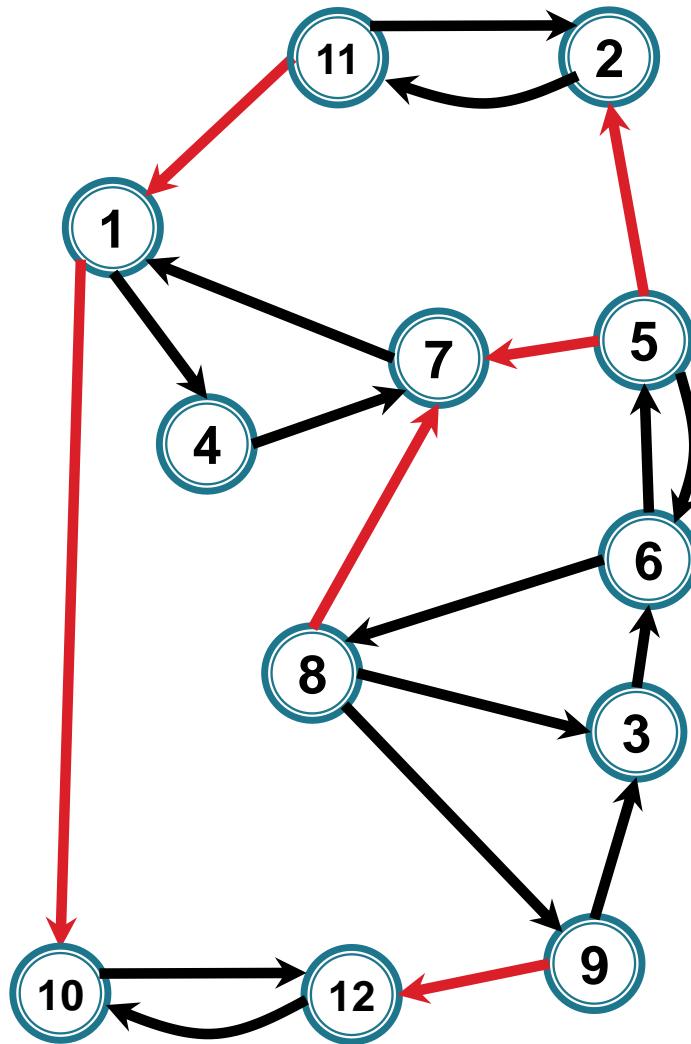
multimea vârfurilor accesibile din x în G^T

unde $G^T = (V, E^T)$, $E^T = \{yx \mid xy \in E\}$

Algoritmi componente tare conexe



G



G^T

Algoritmi componente tare conexe

Componenta tare conexă a vârfului 1 =

multimea vârfurilor accesibile din 1 în G (vizitate în $\text{DFS}(1, G)$)

\cap intersectată cu

multimea vârfurilor accesibile din 1 în G^T (vizitate în $\text{DFS}(1, G^T)$)

Algoritmi componente tare conexe

► Observații

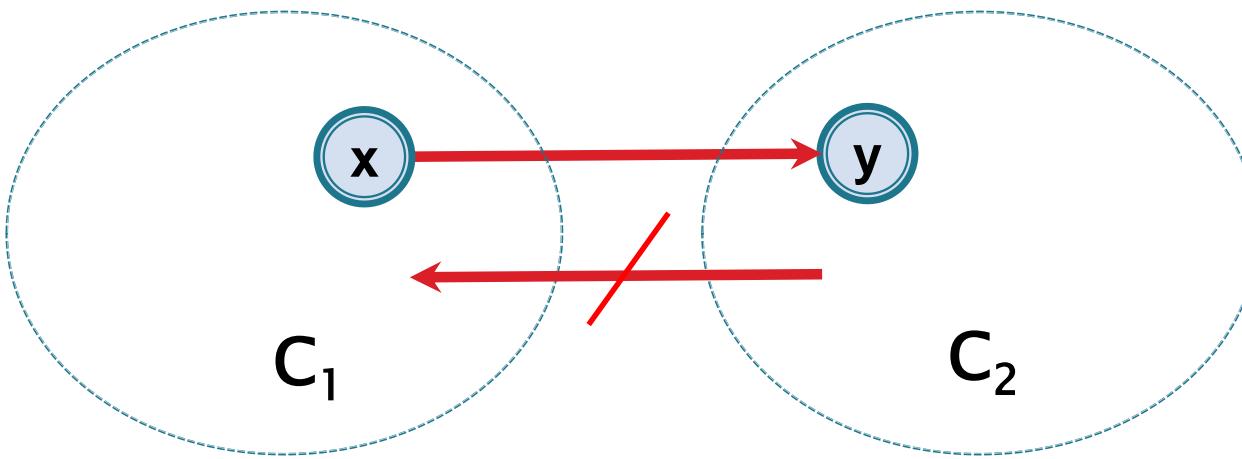
componente tare conexe din $G =$

componente tare conexe din G^T

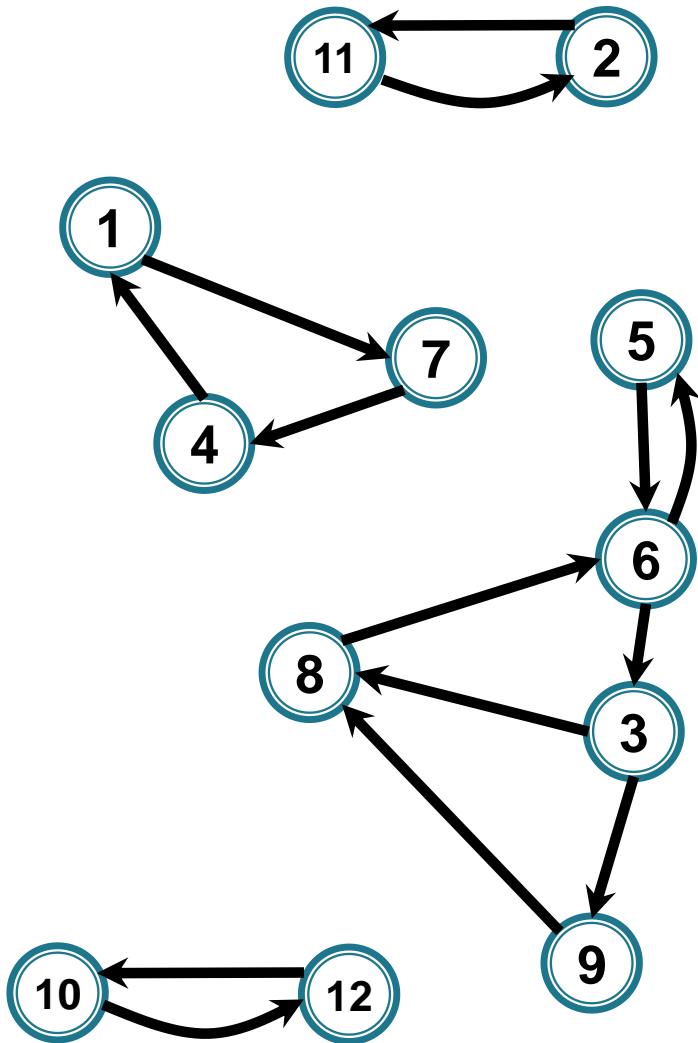
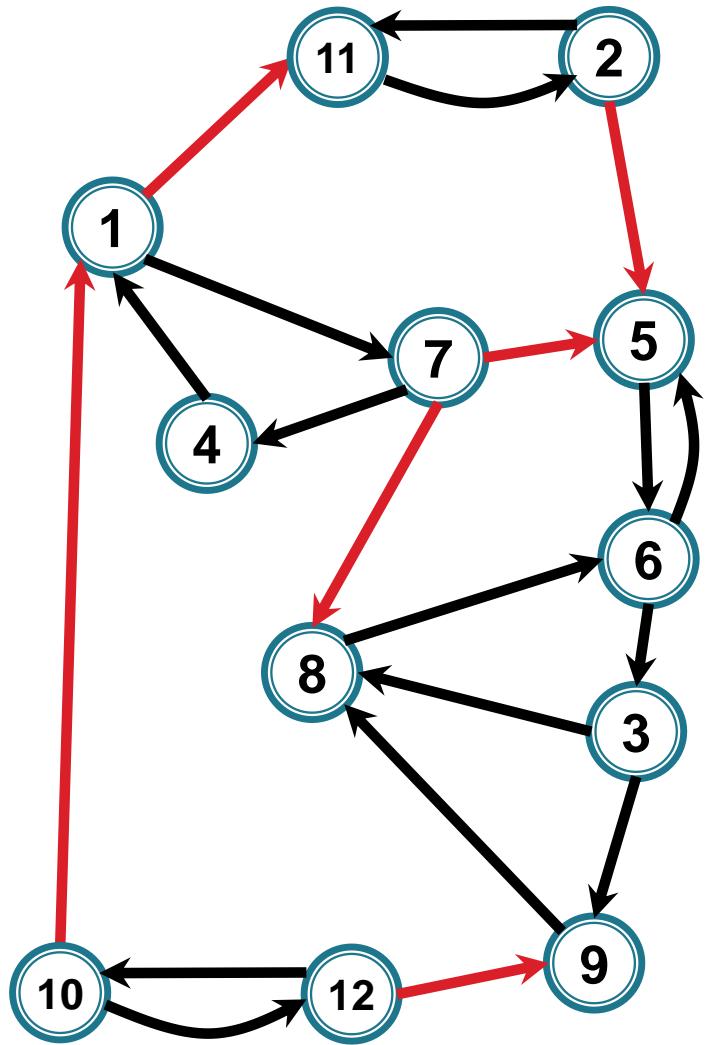
Algoritmi componente tare conexe

▶ Observații

Dacă C_1 și C_2 sunt componente tare conexe aî există arc de la C_1 la C_2 , atunci nu există arc/drum de la C_2 la C_1

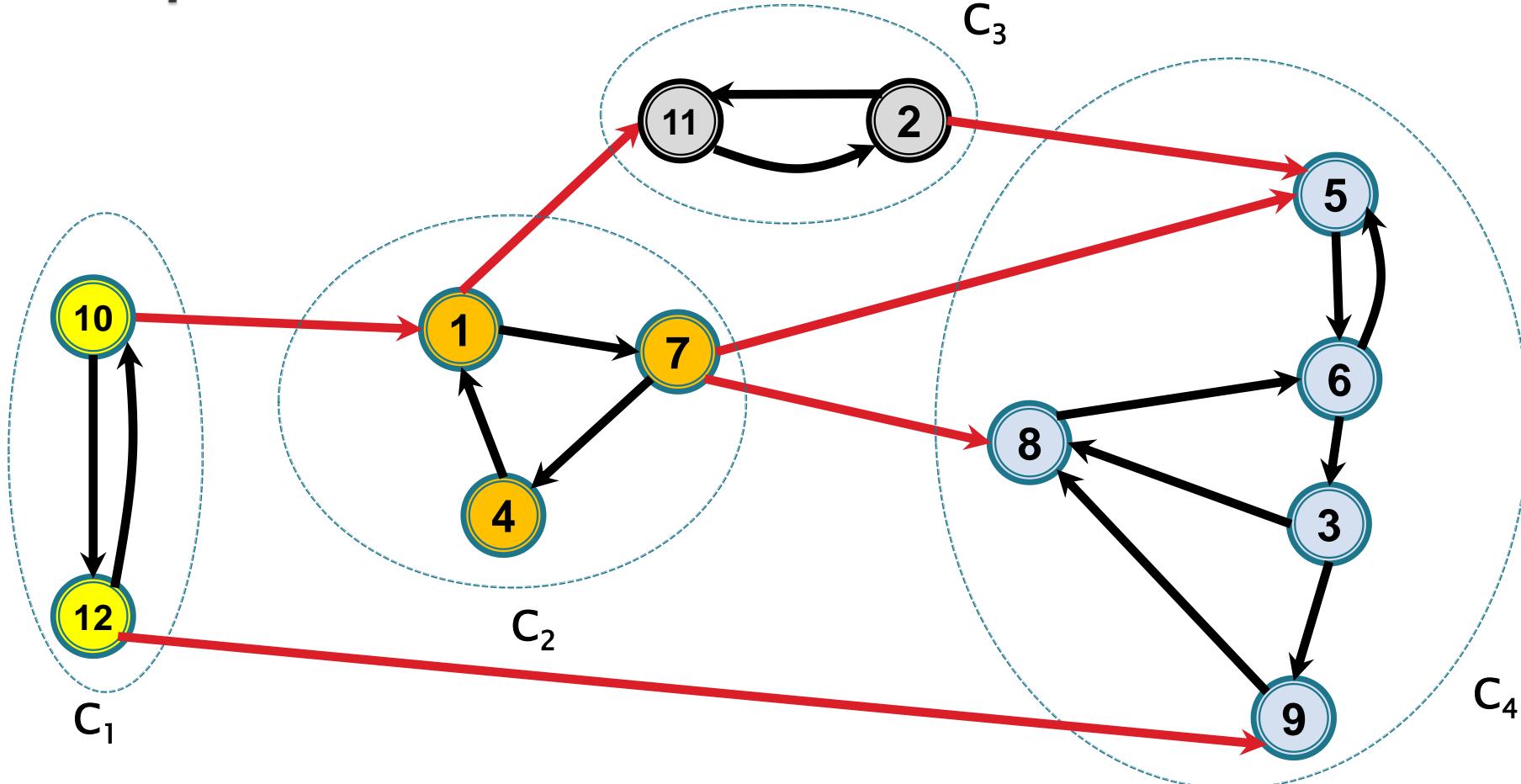


Componente tare conexe

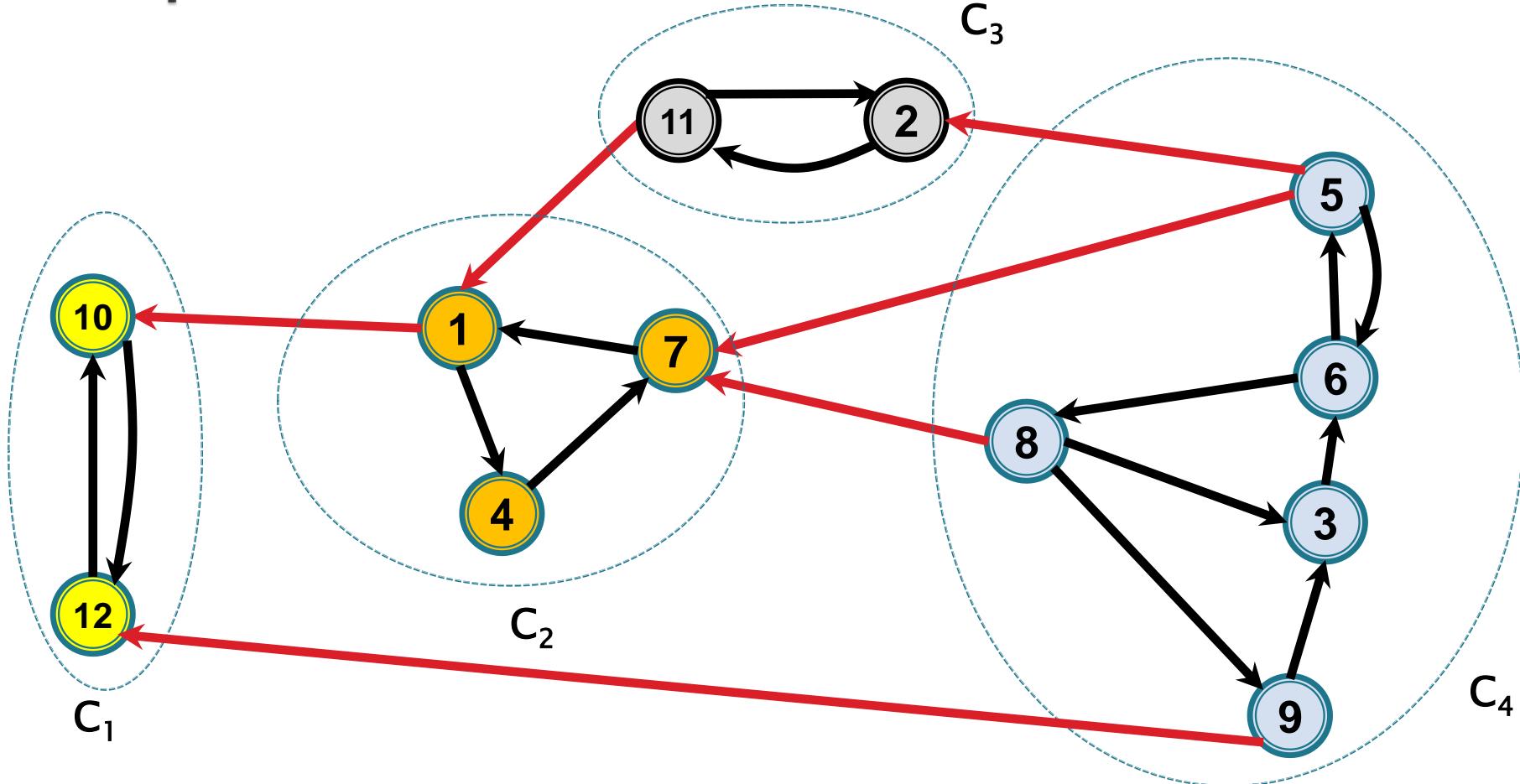


Componentele tare conexe

Componente tare conexe



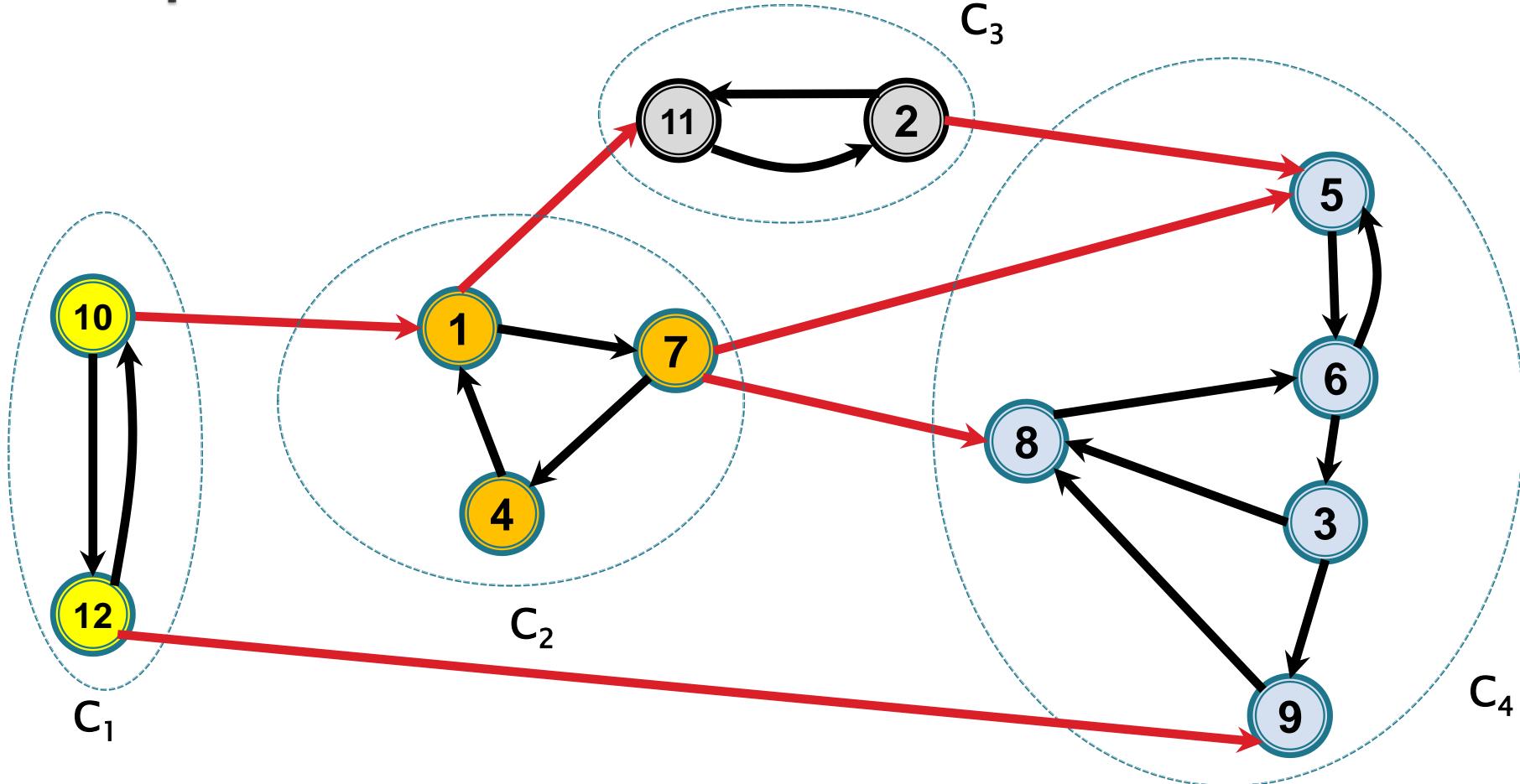
Componente tare conexe



G^T – ar fi bine sa determinăm întâi componenta lui 10: $DF(G^T, 10)$

(să nu se “amestece” componente)

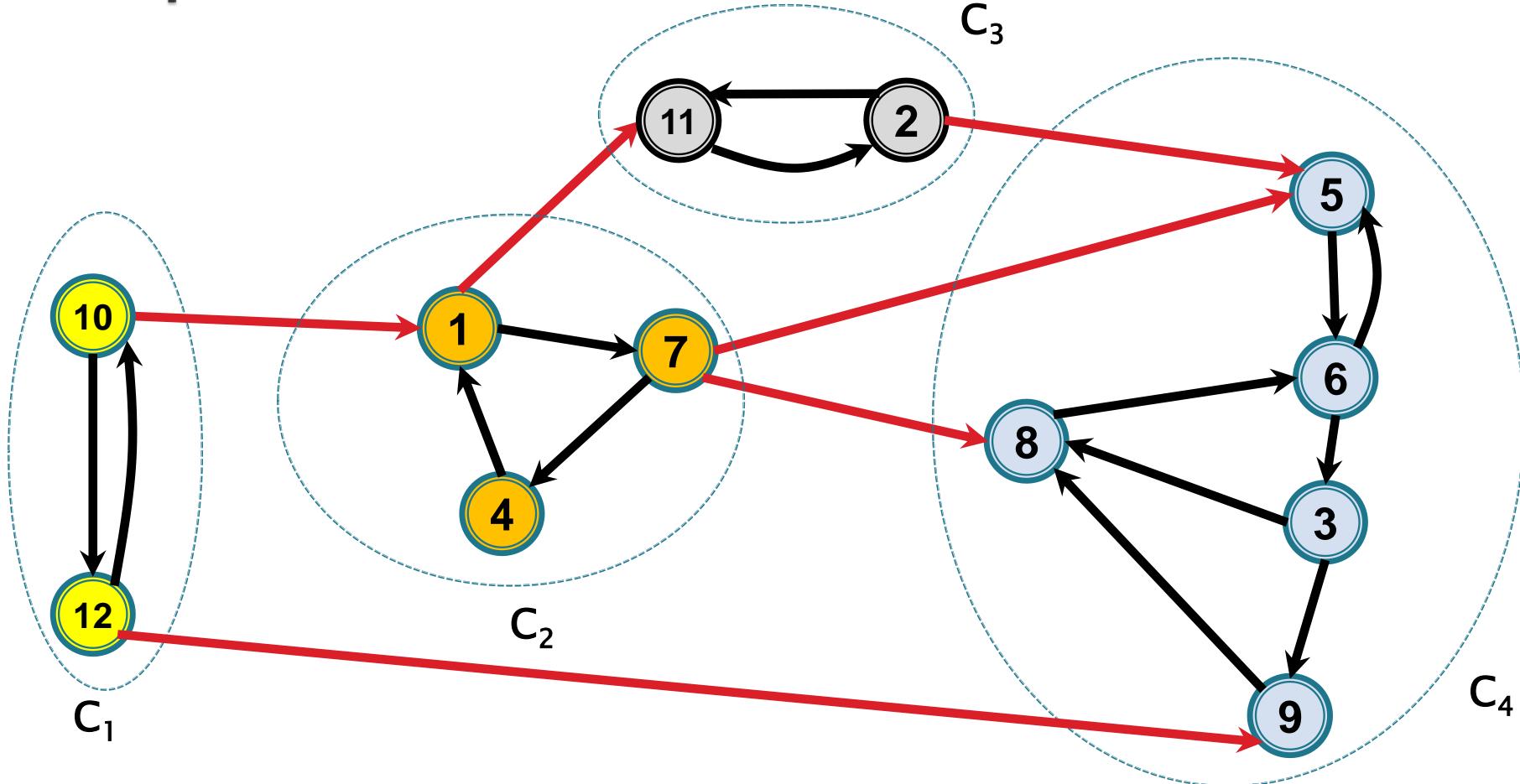
Componente tare conexe



Ar fi bine sa determinăm întâi componenta lui 10 ("de la margine")

Ce proprietate are vîrful 10?

Componente tare conexe



Ar fi bine sa determinăm întâi componenta lui 10 ("de la margine")

Ce proprietate are vîrful 10? => Este **ultimul finalizat** în DF pentru G

Algoritmi componente tare conexe

- ▶ Folosind doar două parcurgeri, una în G și una în G^T ?

DA, dar a doua într-o ordine particulară a vârfurilor (în funcție de ordinea în care au fost finalizate în DF)

⇒ Algoritmul lui Kosaraju

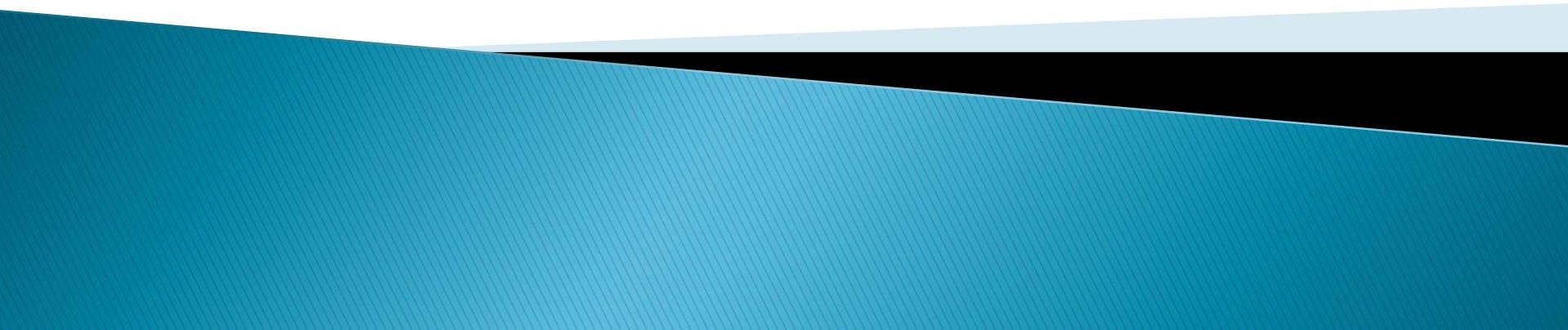
Algoritmi componente tare conexe

- ▶ Dar folosind o singură parcurgere?

DA, folosind o idee similară cu cea de la componente biconexe (vom discuta)

⇒ Algoritmul lui Tarjan ([SUPLIMENTAR](#))

Algoritmul lui Kosaraju



Algoritmul lui Kosaraju

Pasul 1. $\text{DFS}(G, x)$ pentru fiecare vârf x nevizitat + o stivă S în care se introduc vârfurile când sunt finalizate

Pasul 2. $\text{DFS}(G^T, x)$ pentru x (nevizitat) în ordinea în care sunt scoase din S (=descrescător în raport timpul de finalizare – similar cu sortarea topologică)

Avem

vârfuri vizitate în $\text{DFS}(G^T, x)$ = componenta tare conexă a lui x

Algoritmul lui Kosaraju

Complexitate:

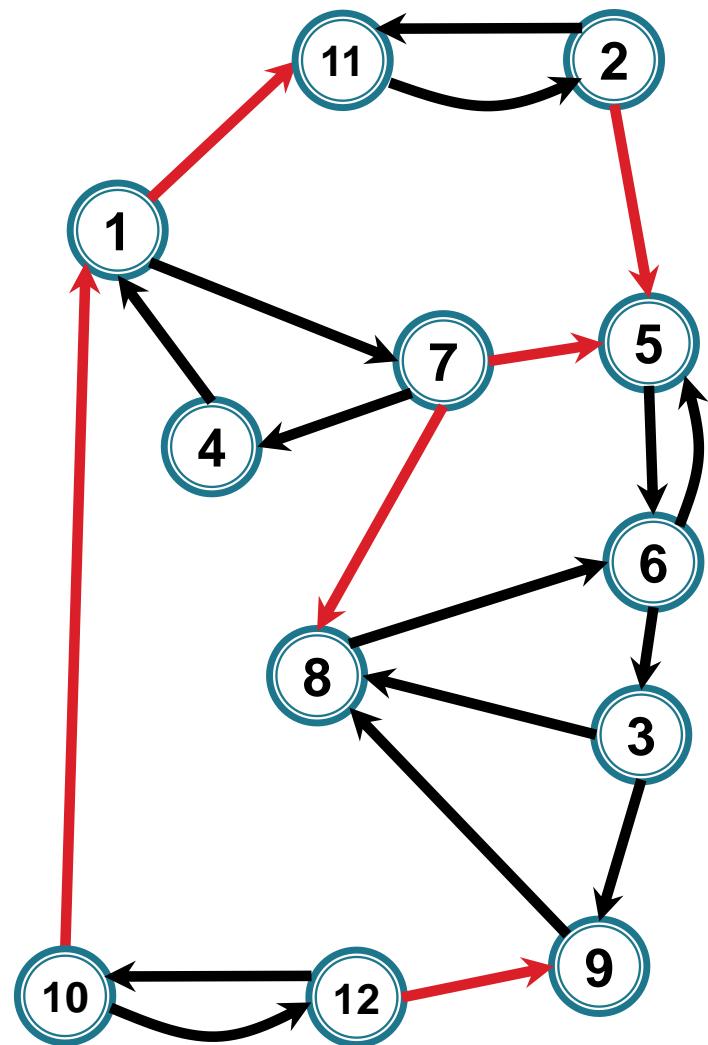
2 parcurgeri + construcția lui $G^T \Rightarrow O(n+m)$

Algoritmul lui Kosaraju

Timp de finalizare

Pasul 1.

DFS(1)

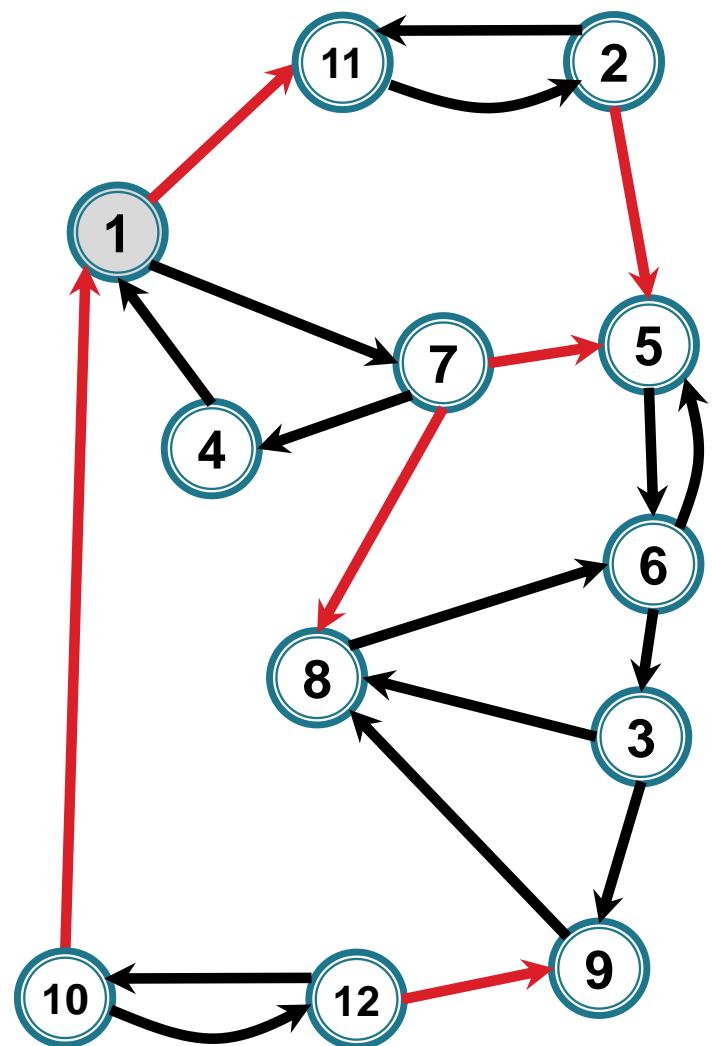


Ordinea descrescătoare finalizare:

Algoritmul lui Kosaraju

Timp de finalizare

Pasul 1.

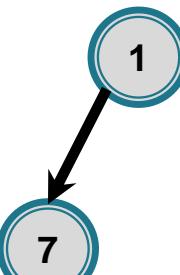
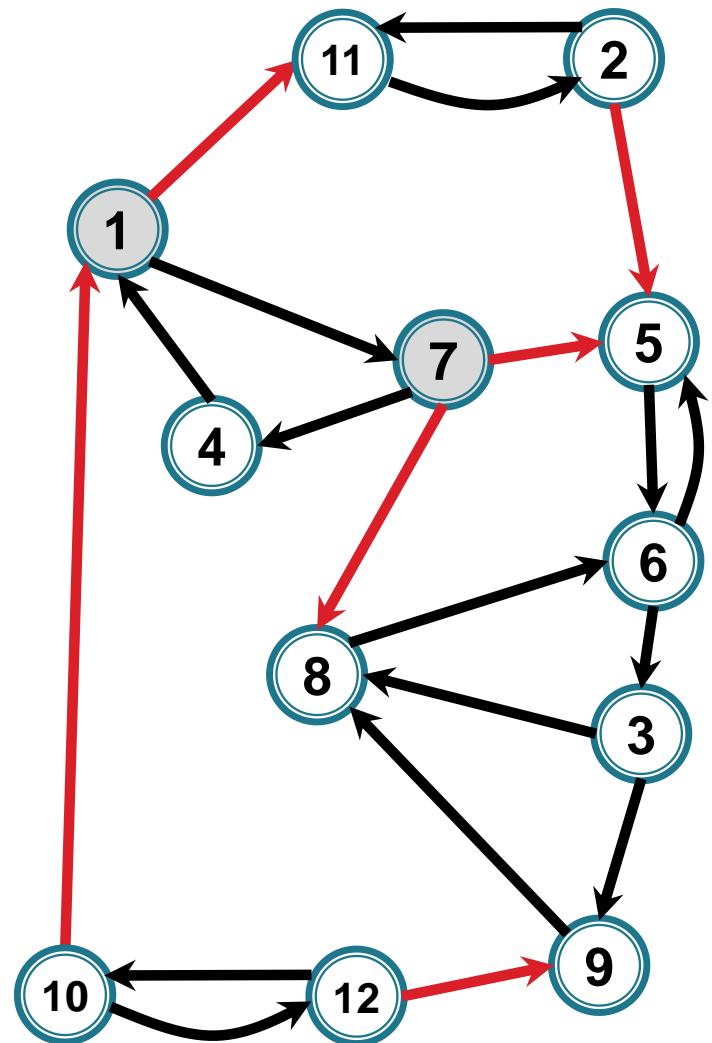


Ordinea descrescătoare finalizare:

Algoritmul lui Kosaraju

Timp de finalizare

Pasul 1.

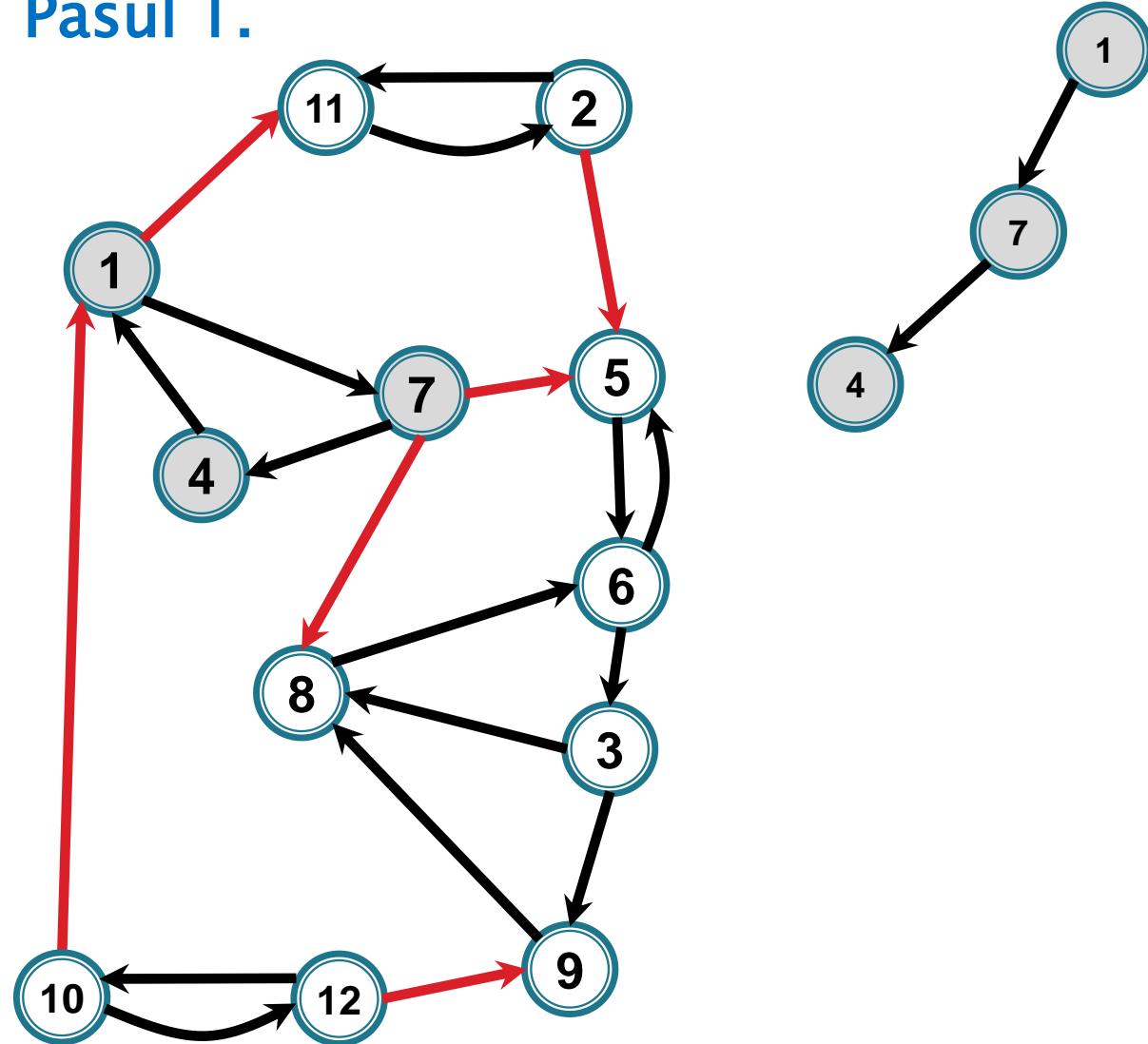


Ordinea descrescătoare finalizare:

Algoritmul lui Kosaraju

Timp de finalizare

Pasul 1.

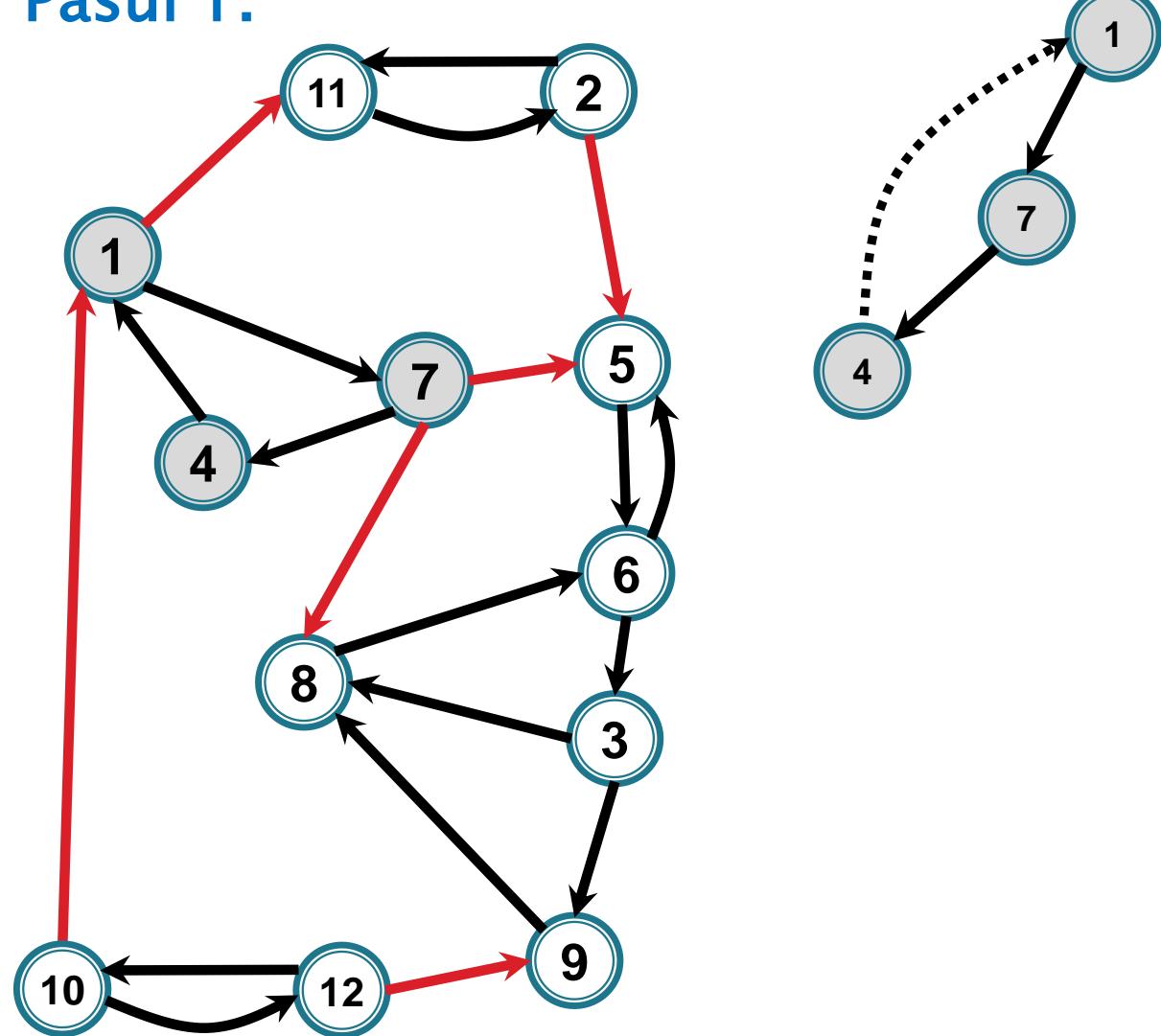


Ordinea descrescătoare finalizare:

Algoritmul lui Kosaraju

Timp de finalizare

Pasul 1.



1

7

4

1

7

4

1

7

4

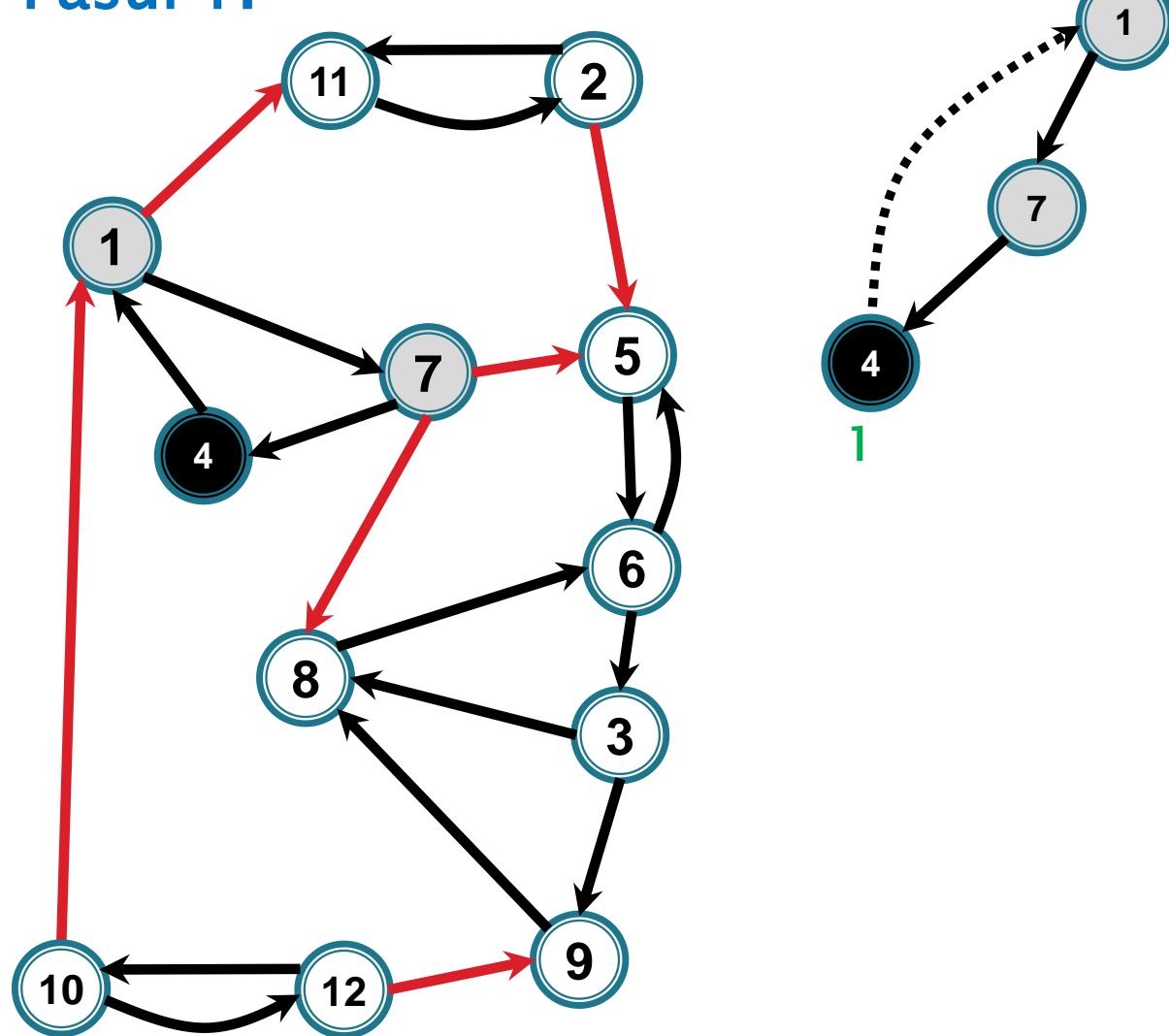
1

Ordinea descrescătoare finalizare:

Algoritmul lui Kosaraju

Timp de finalizare

Pasul 1.

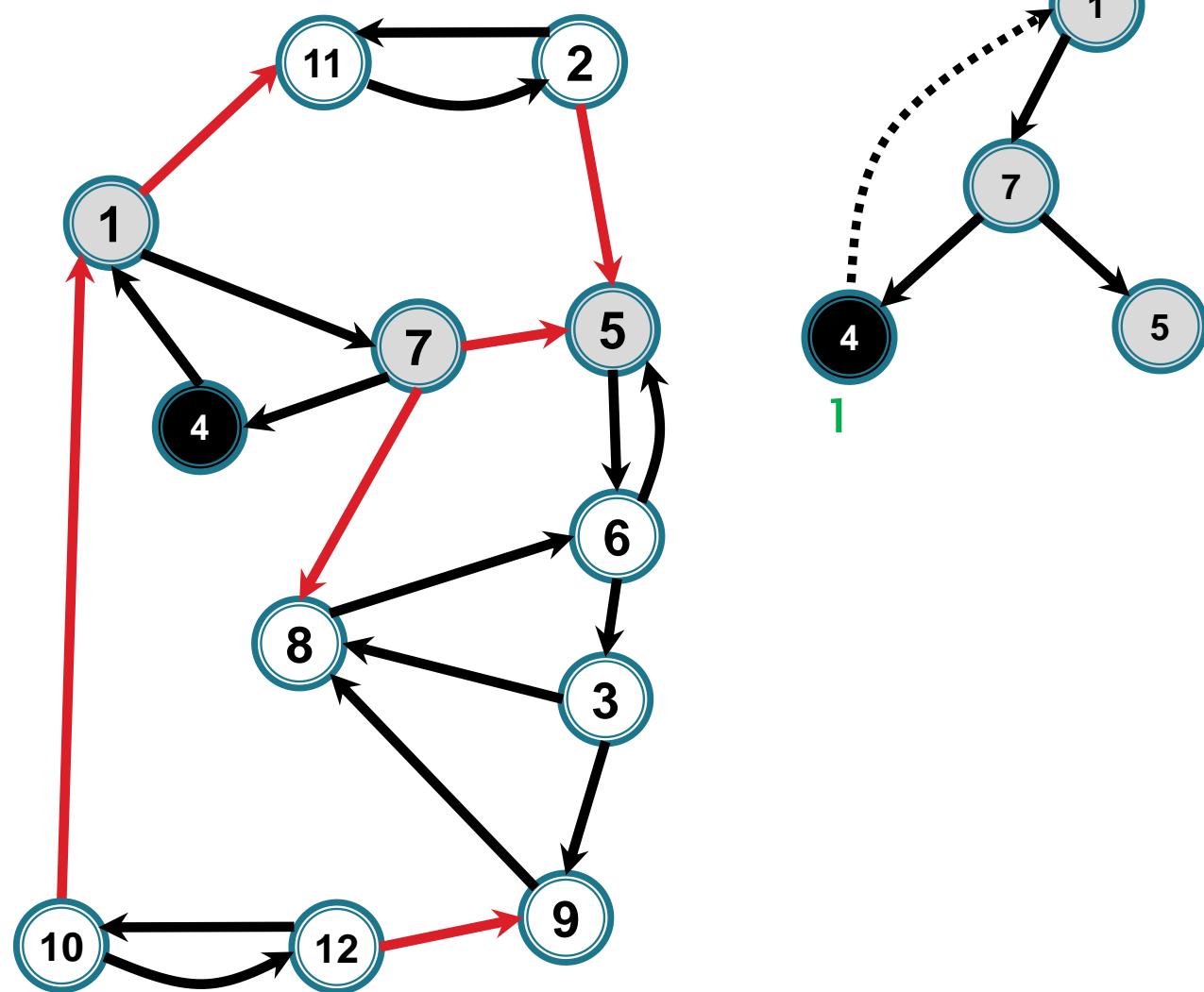


Ordinea descrescătoare finalizare:

Algoritmul lui Kosaraju

Timp de finalizare

Pasul 1.



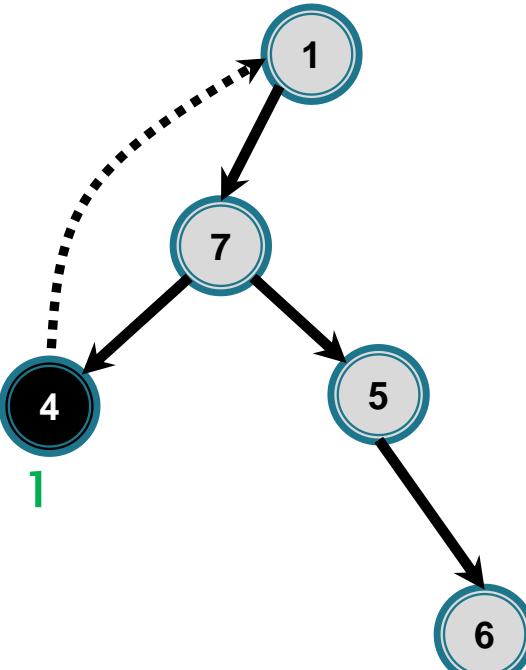
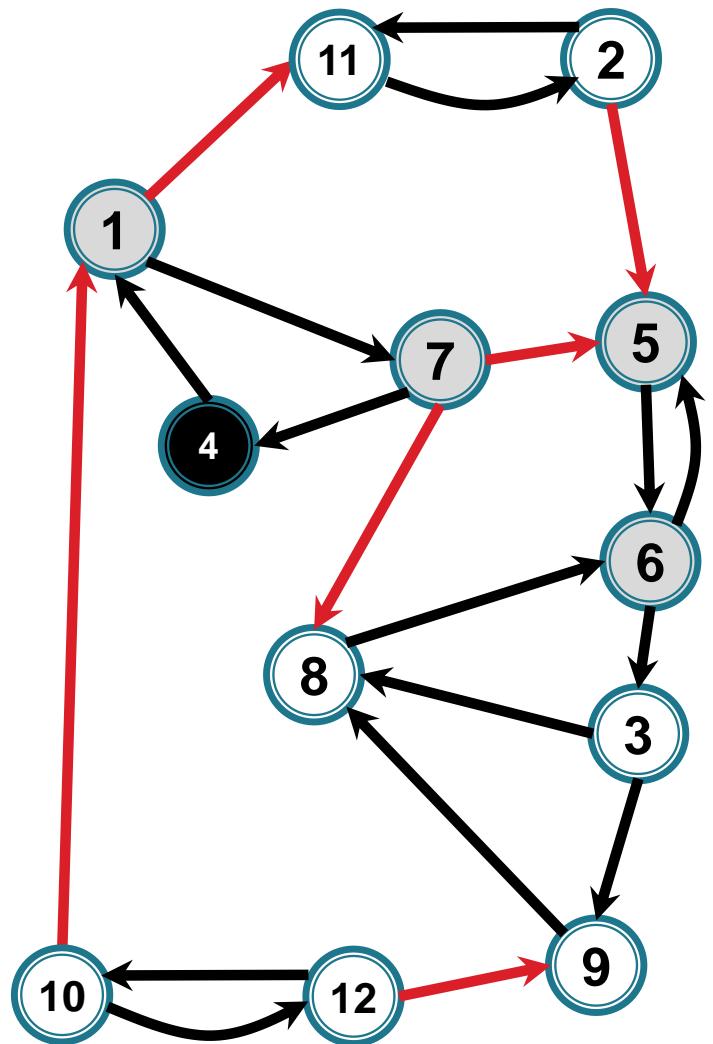
Ordinea descrescătoare finalizare:

1 7 5 4 3 6 8 11 2 9 10 12

Algoritmul lui Kosaraju

Timp de finalizare

Pasul 1.

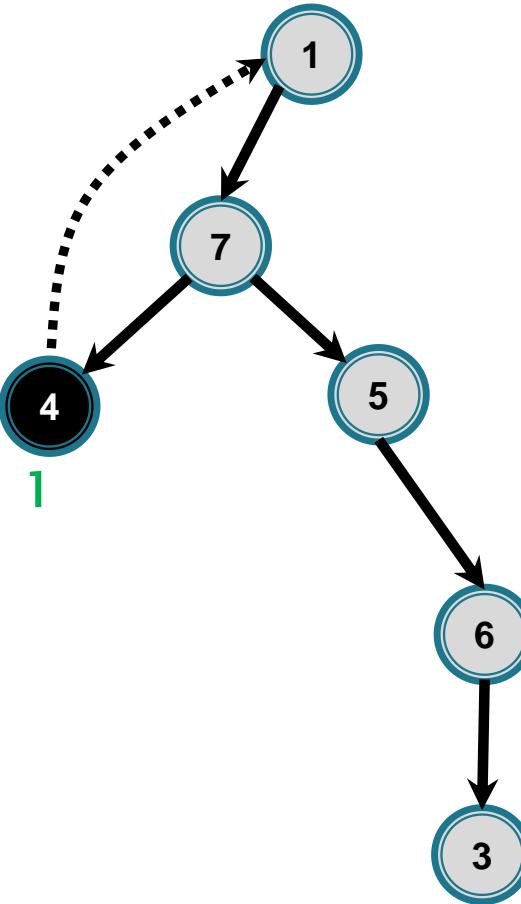
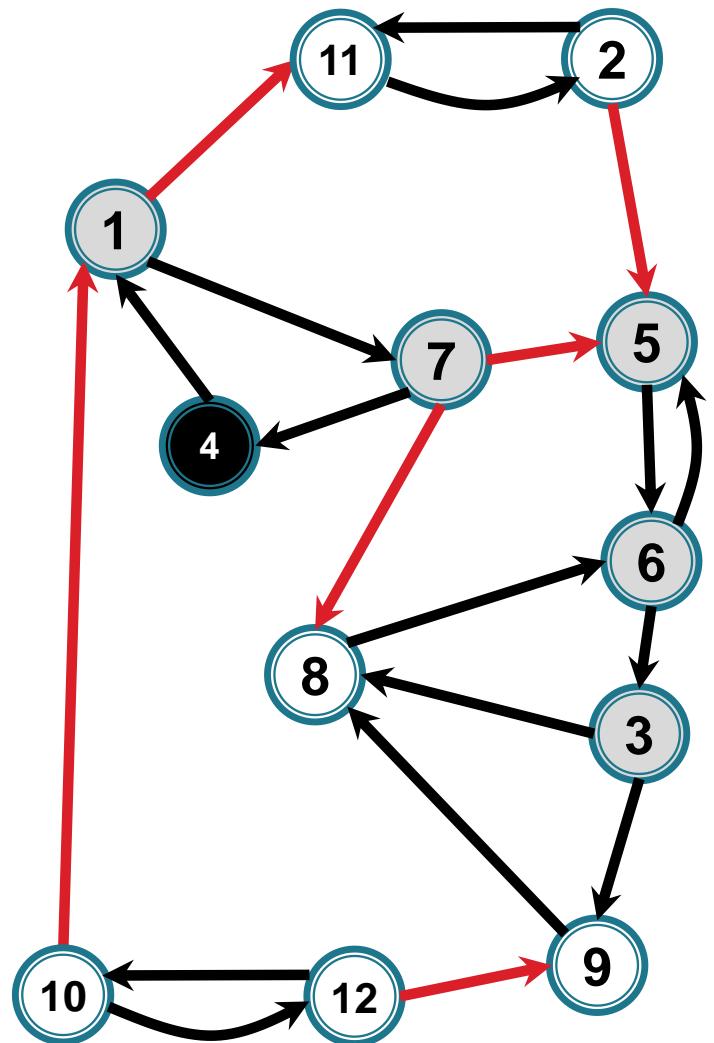


Ordinea descrescătoare finalizare:

Algoritmul lui Kosaraju

Timp de finalizare

Pasul 1.

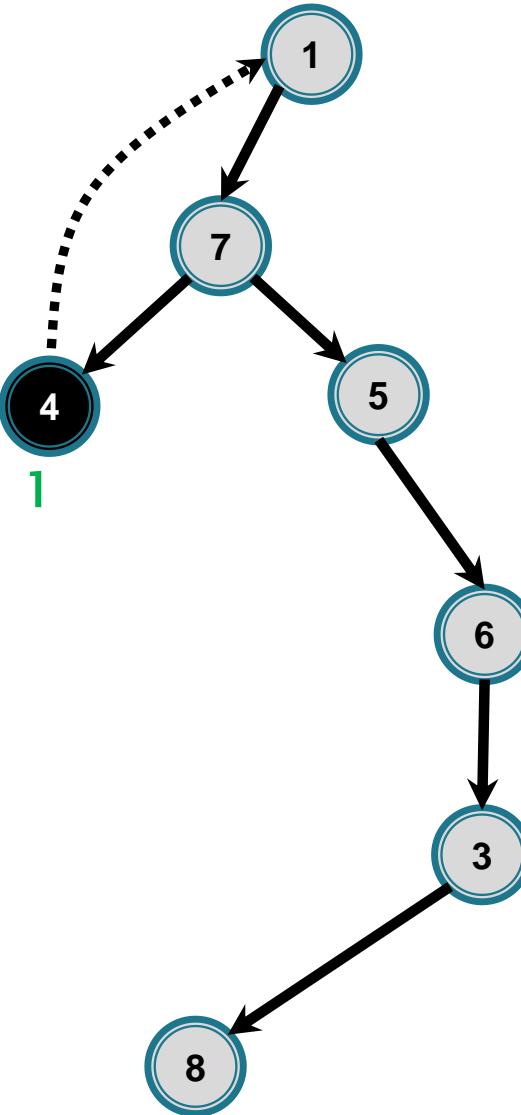
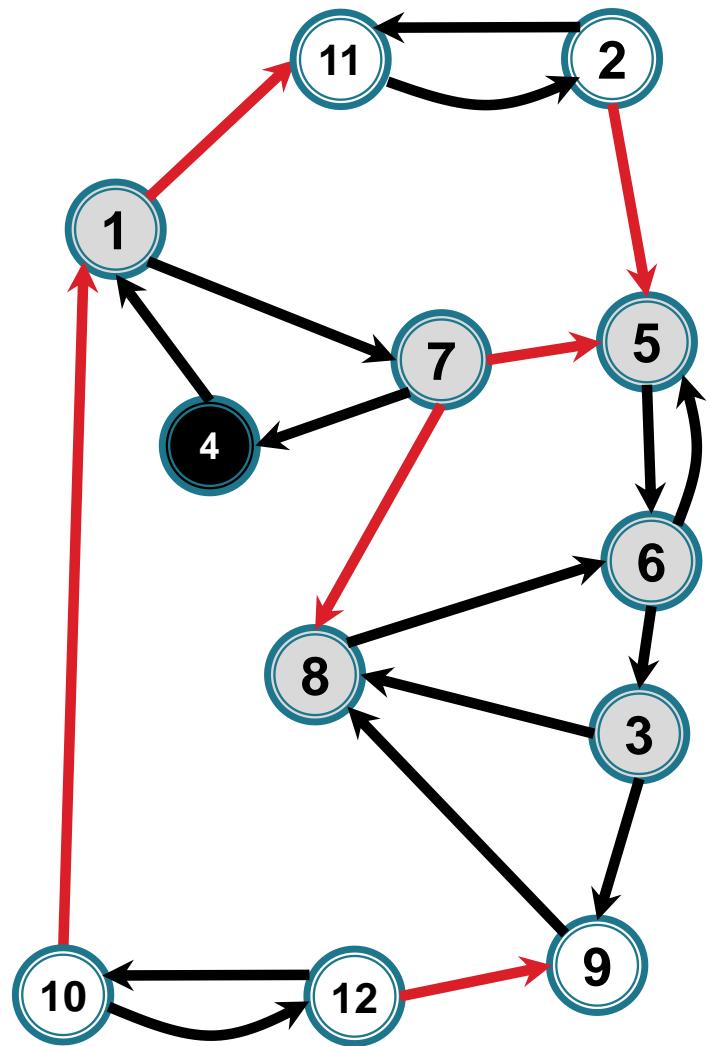


Ordinea descrescătoare finalizare:

Algoritmul lui Kosaraju

Timp de finalizare

Pasul 1.

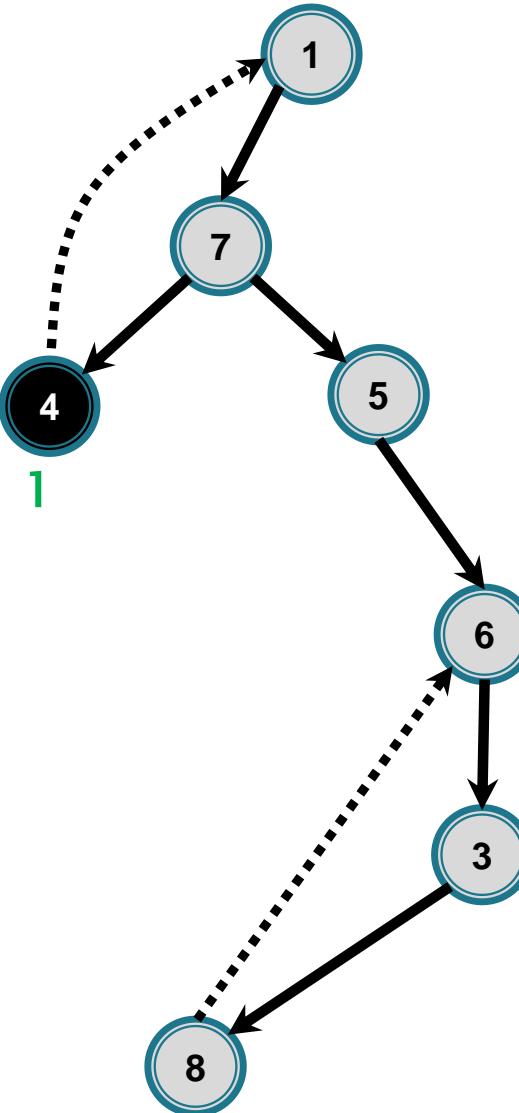
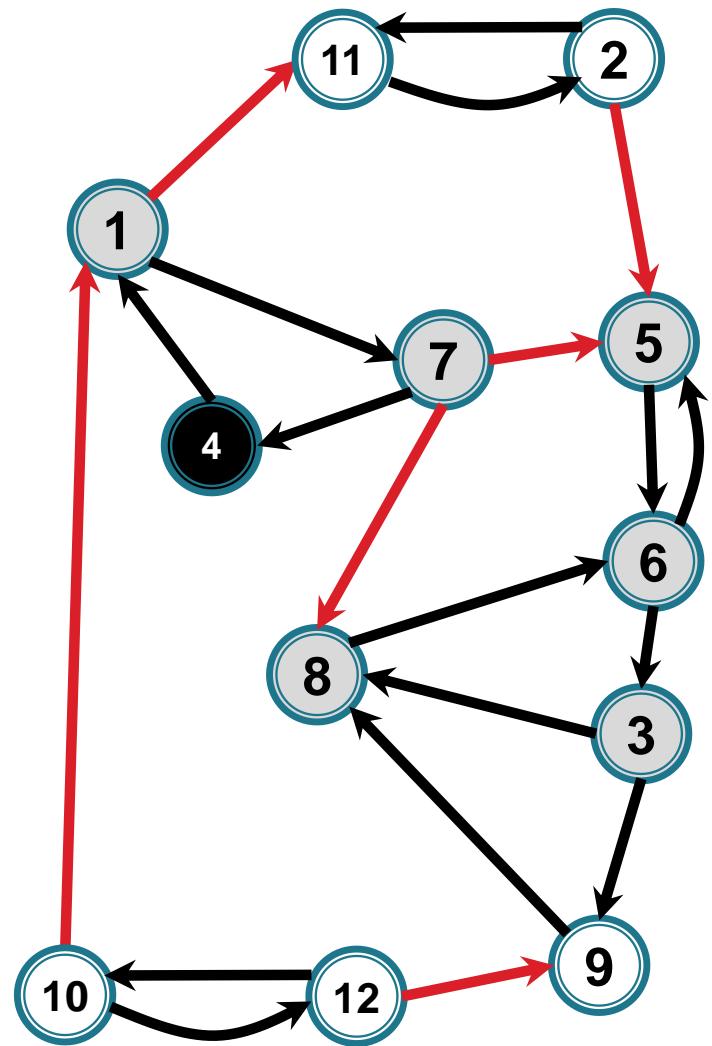


Ordinea descrescătoare finalizare:

Algoritmul lui Kosaraju

Timp de finalizare

Pasul 1.

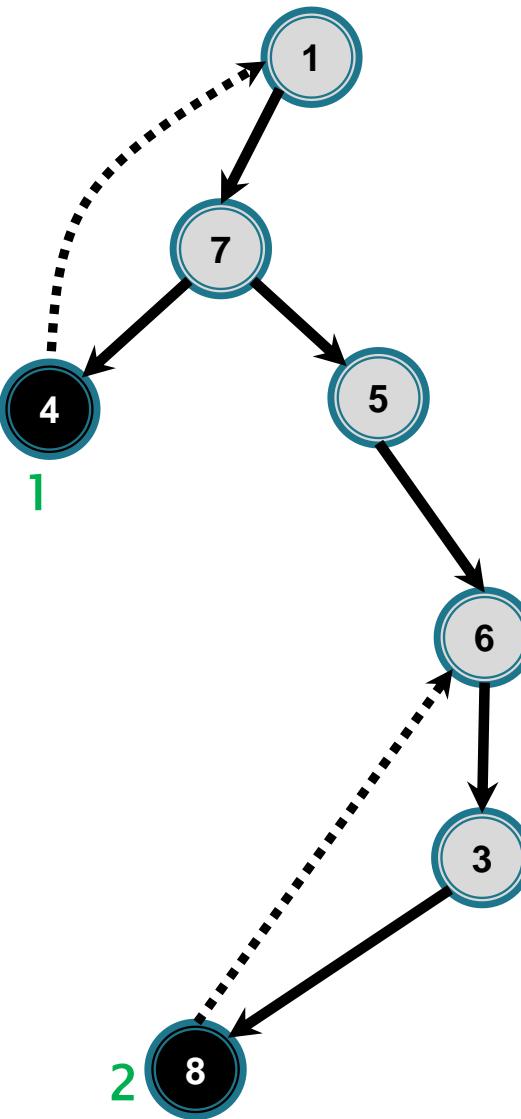
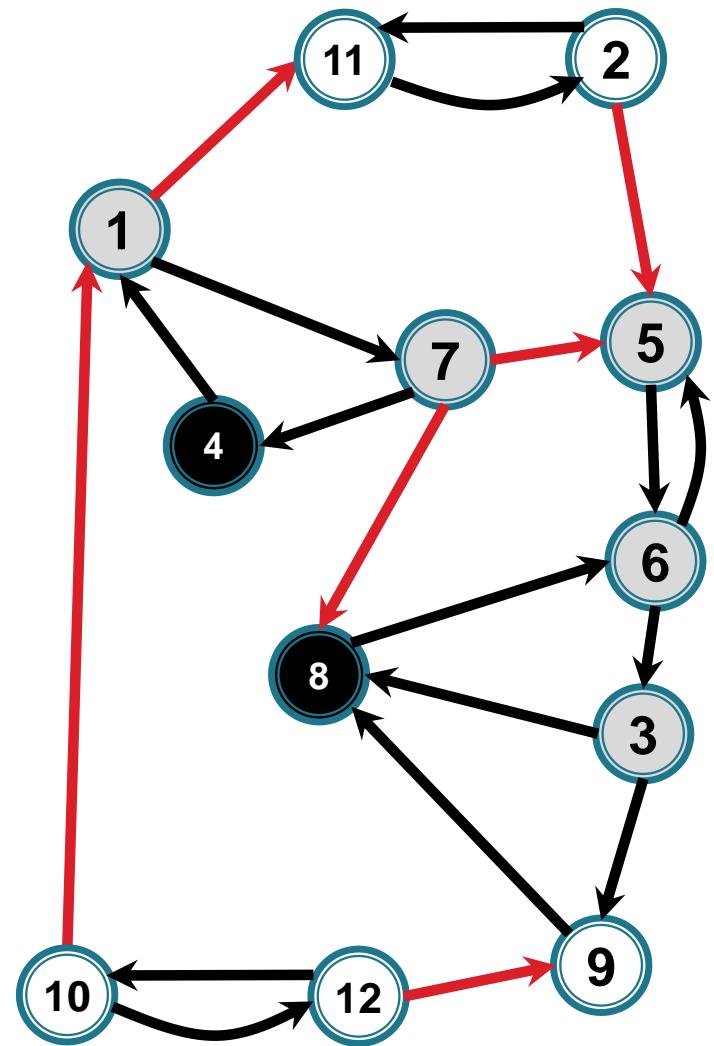


Ordinea descrescătoare finalizare:

Algoritmul lui Kosaraju

Timp de finalizare

Pasul 1.



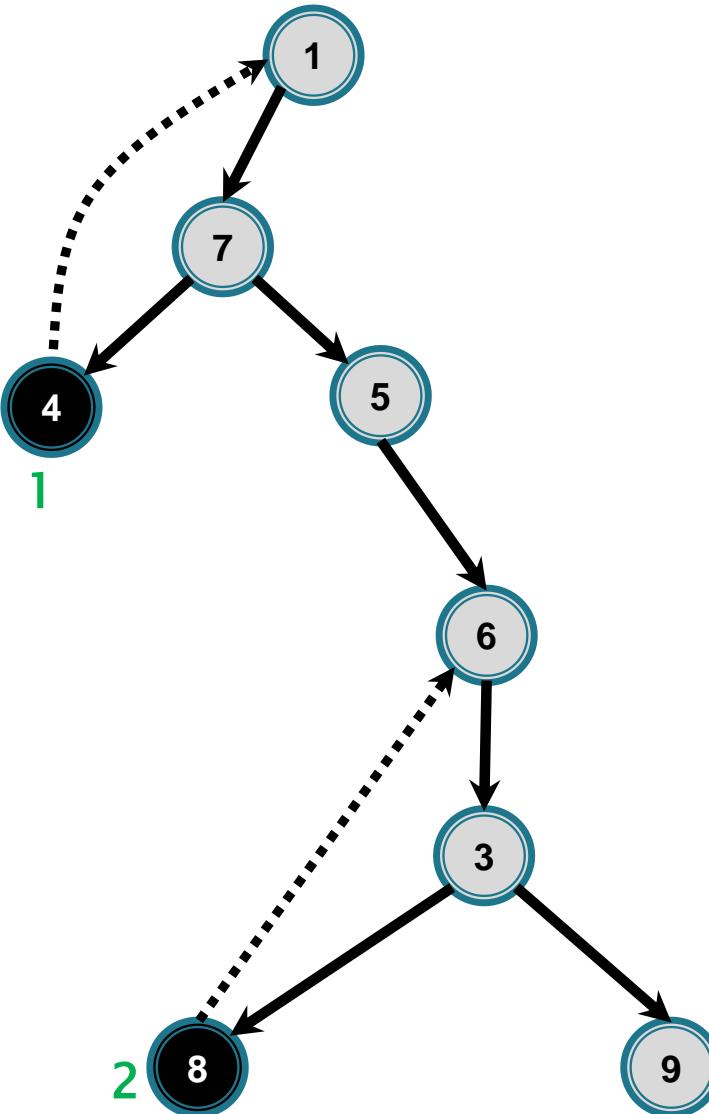
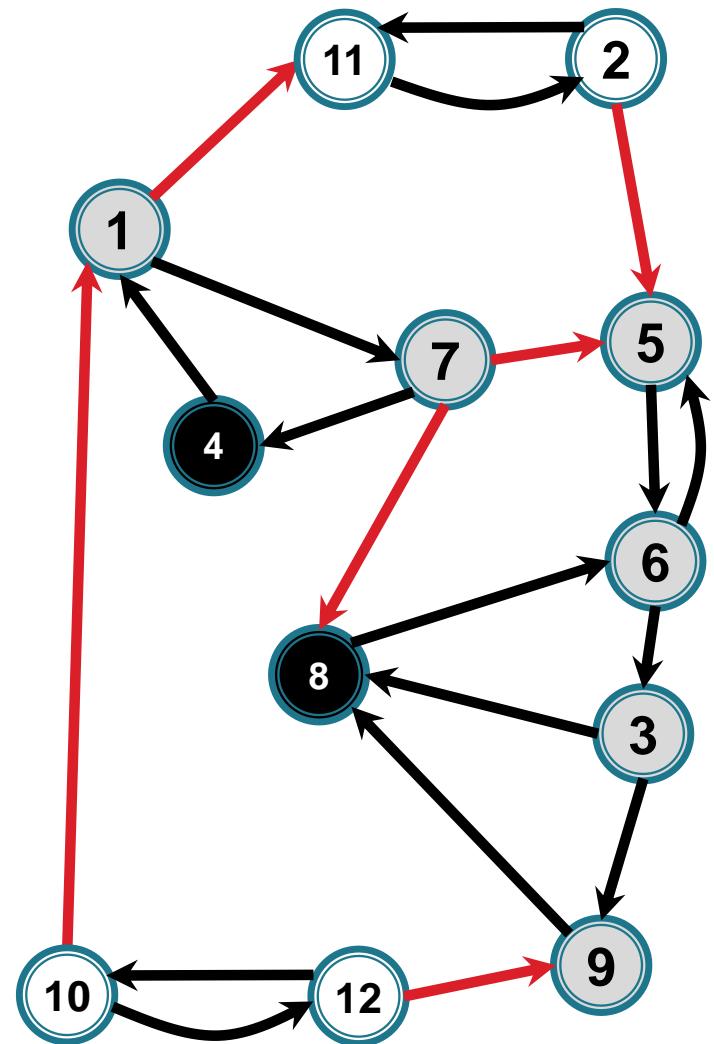
Ordinea descrescătoare finalizare:

8, 4

Algoritmul lui Kosaraju

Timp de finalizare

Pasul 1.



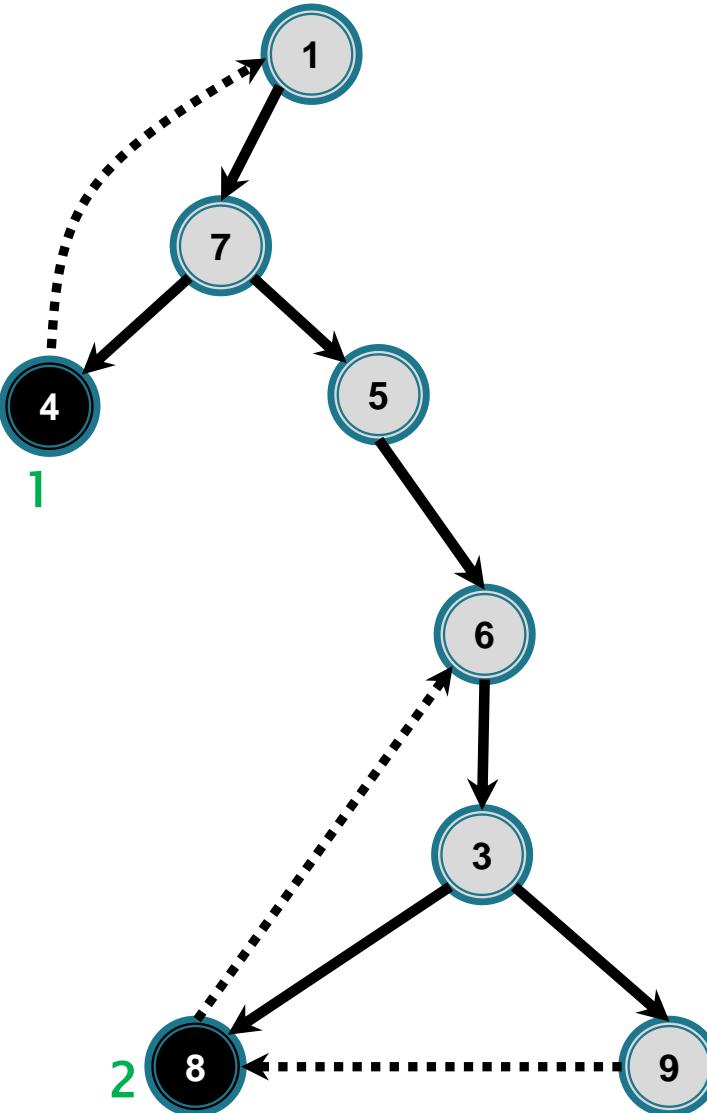
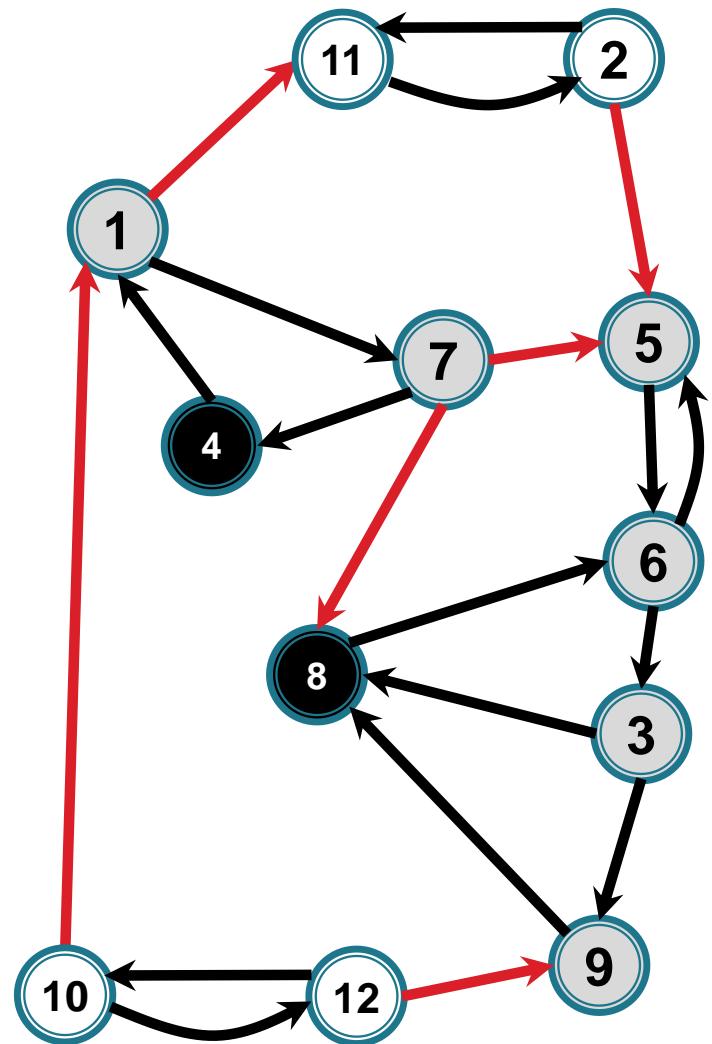
Ordinea descrescătoare finalizare:

8, 4

Algoritmul lui Kosaraju

Timp de finalizare

Pasul 1.



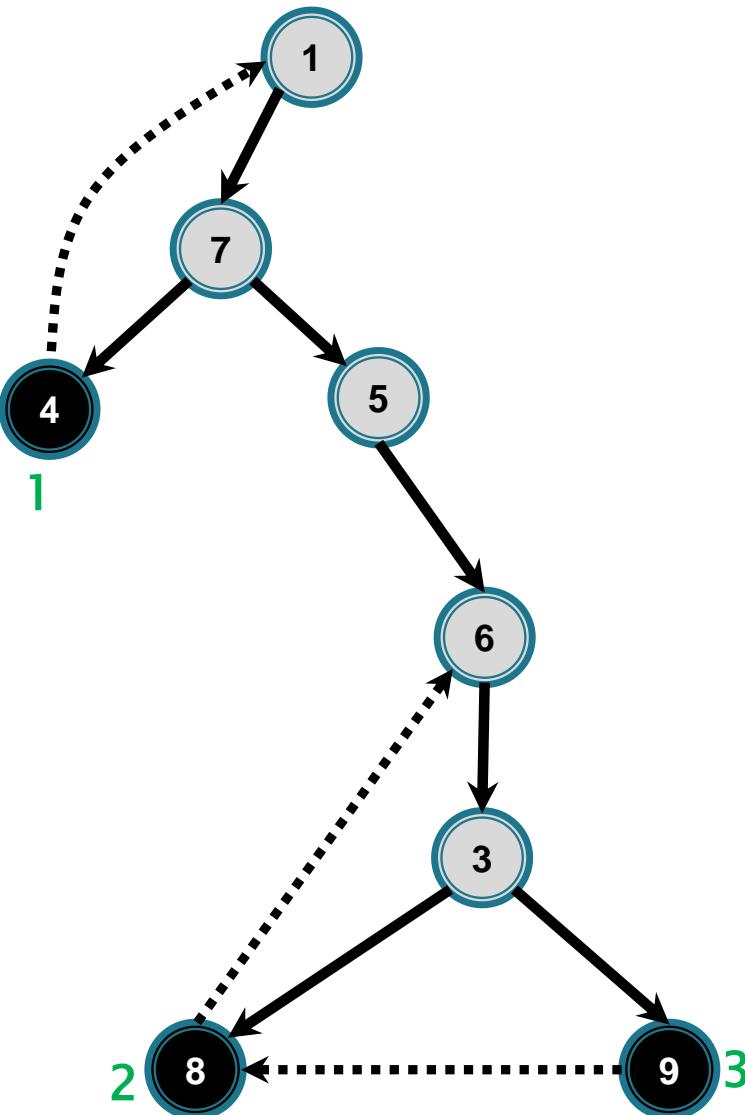
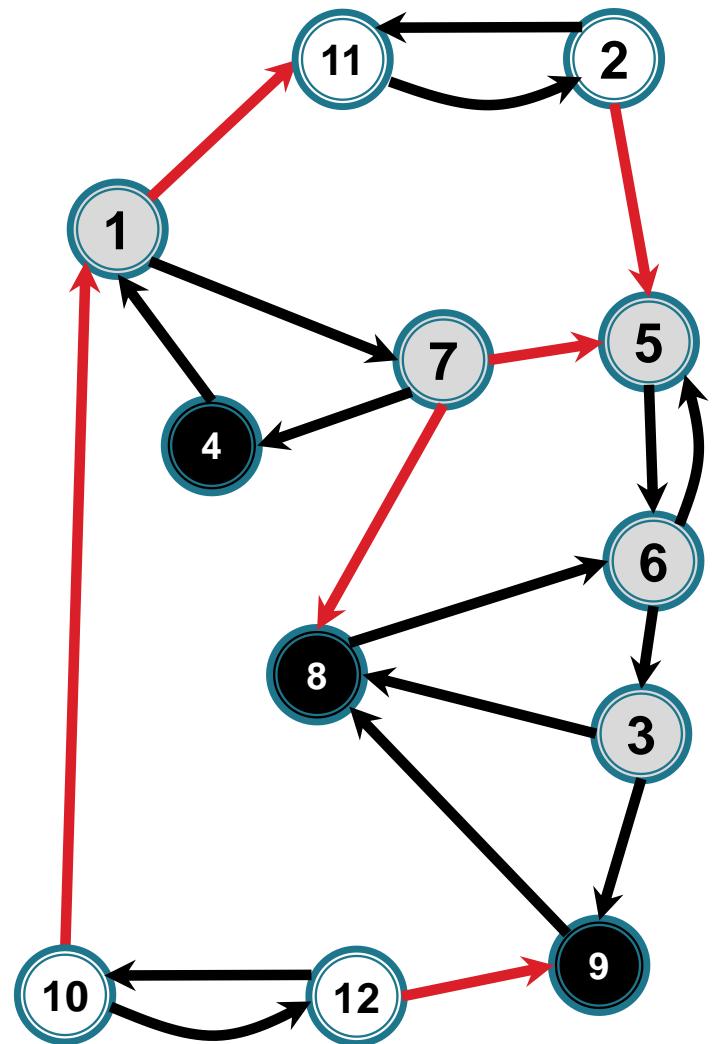
Ordinea descrescătoare finalizare:

8, 4

Algoritmul lui Kosaraju

Timp de finalizare

Pasul 1.



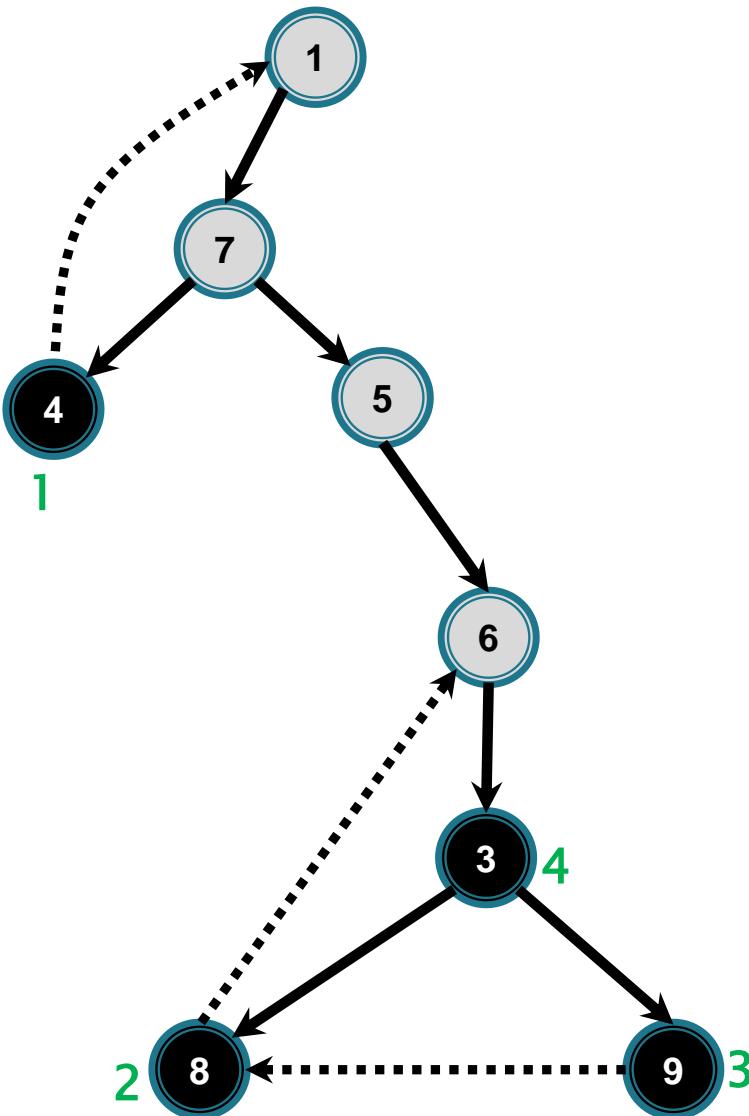
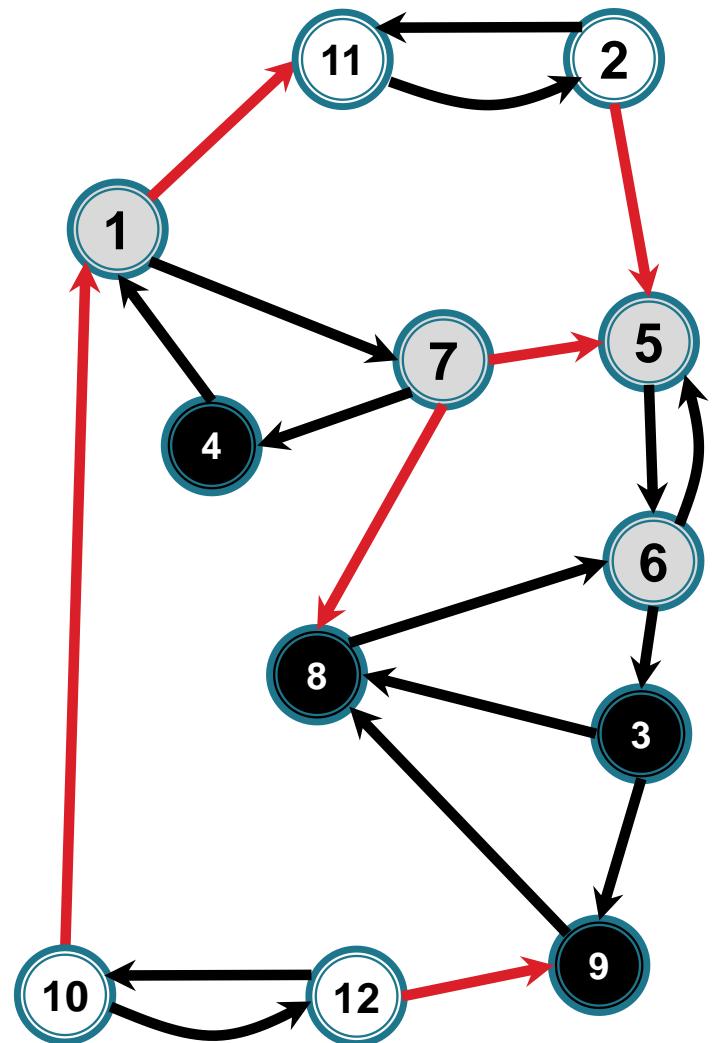
Ordinea descrescătoare finalizare:

9, 8, 4

Algoritmul lui Kosaraju

Timp de finalizare

Pasul 1.



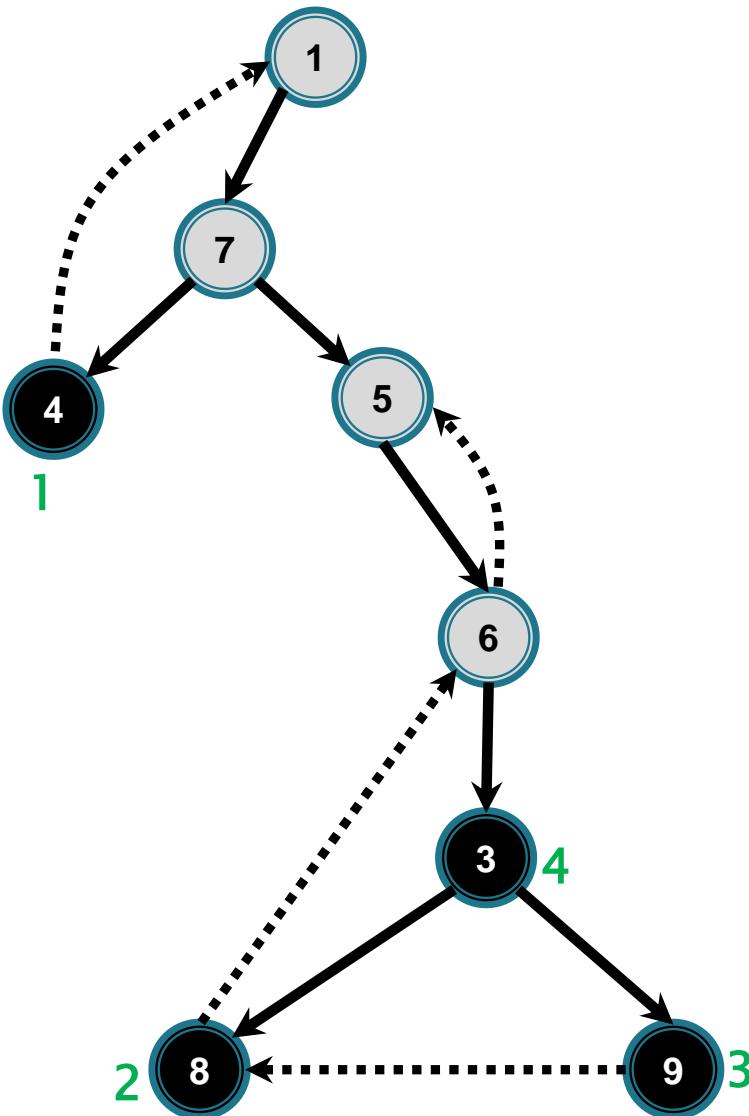
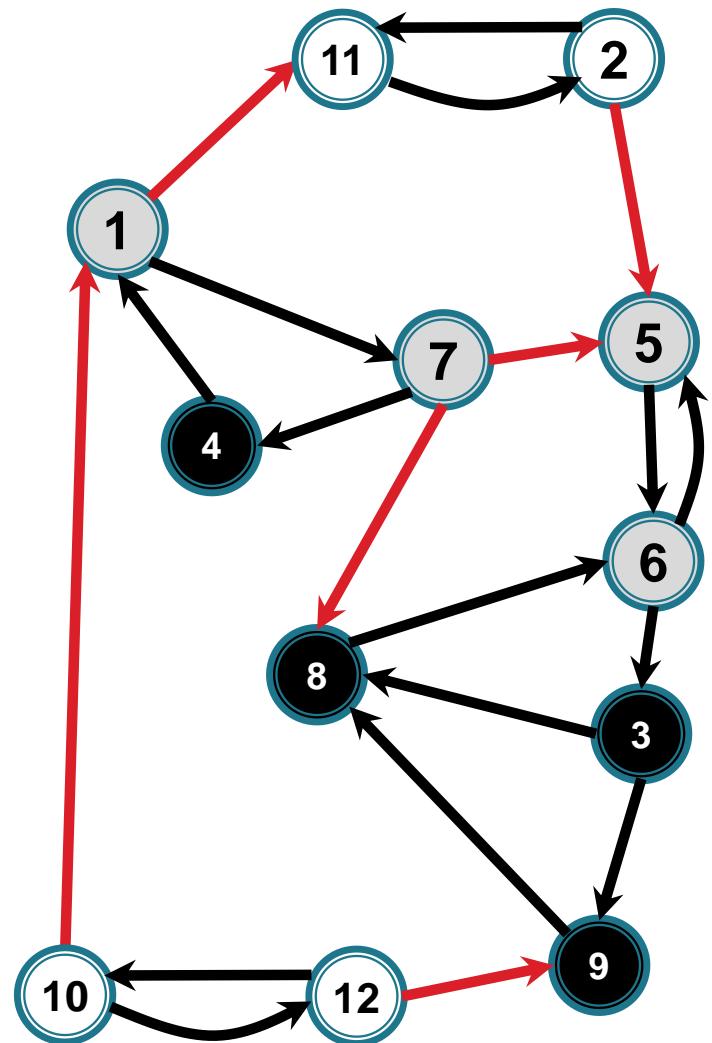
Ordinea descrescătoare finalizare:

3, 9, 8, 4

Algoritmul lui Kosaraju

Timp de finalizare

Pasul 1.



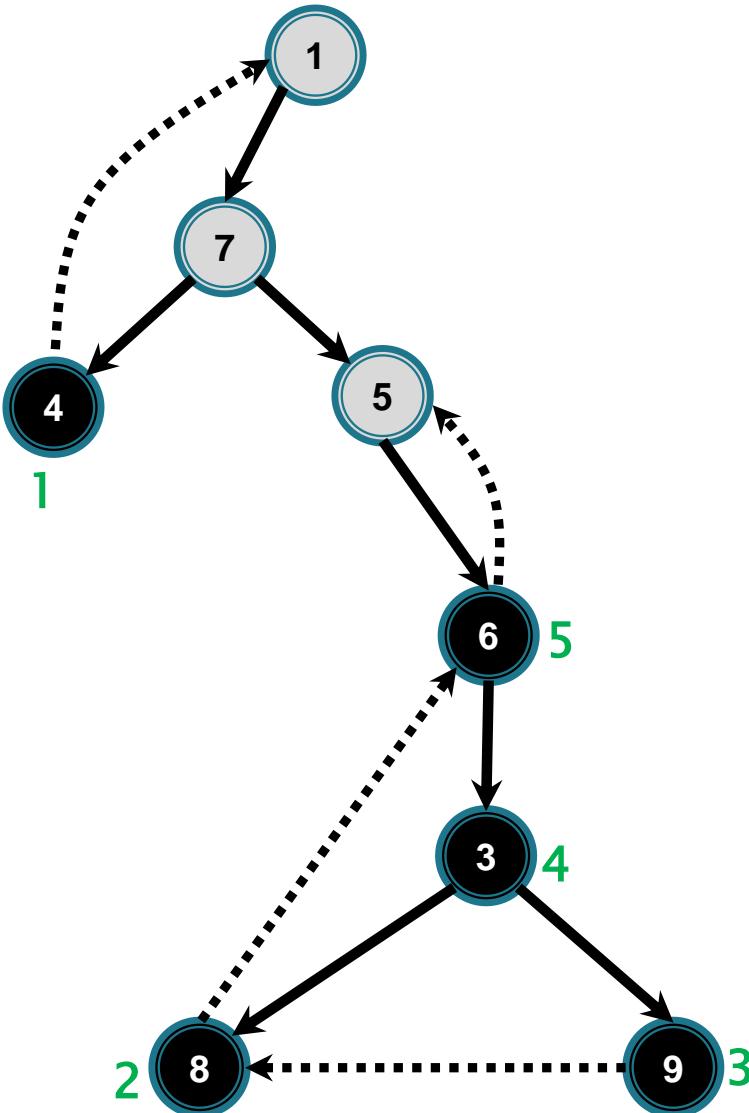
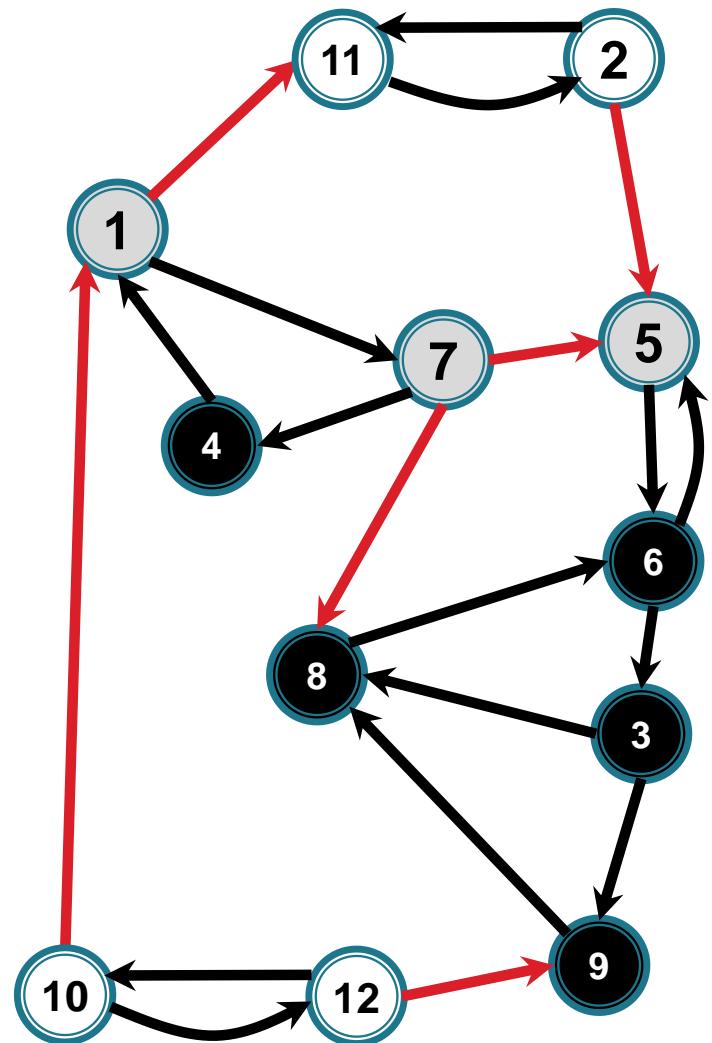
Ordinea descrescătoare finalizare:

3, 9, 8, 4

Algoritmul lui Kosaraju

Timp de finalizare

Pasul 1.



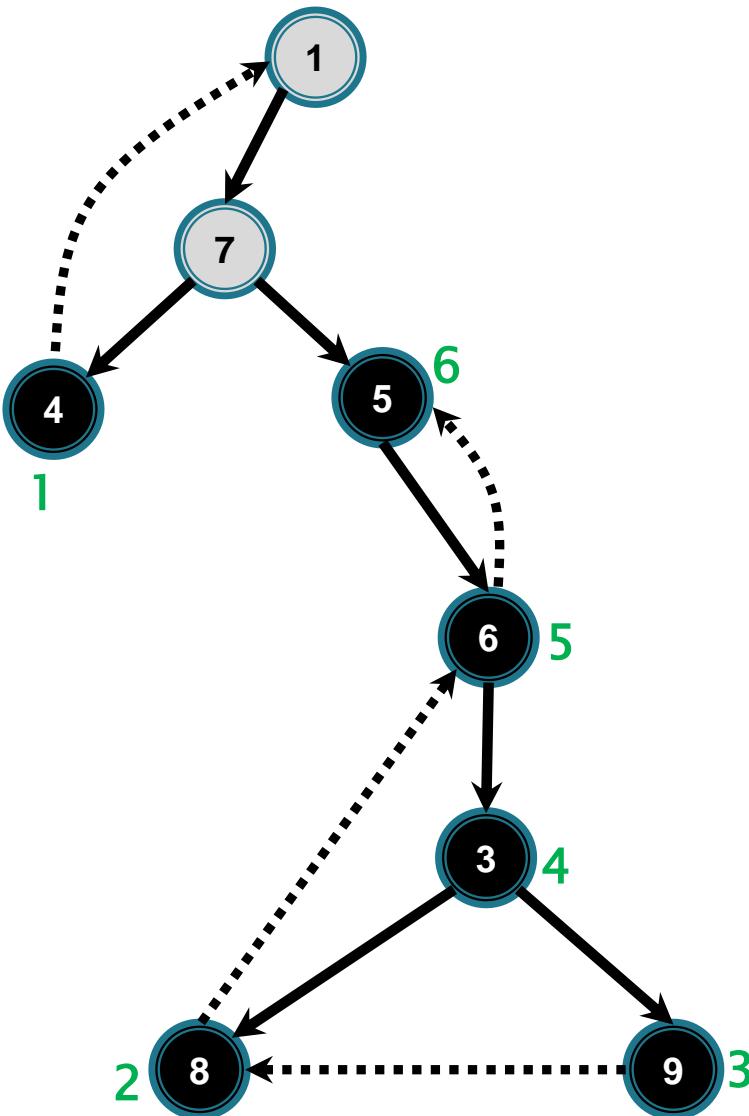
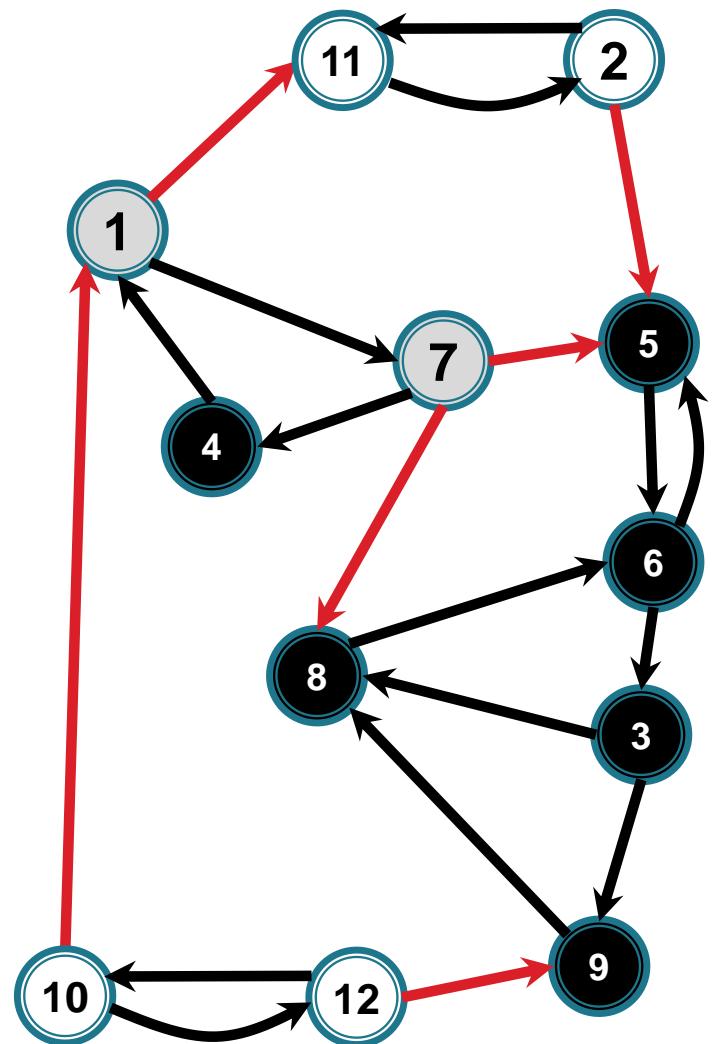
Ordinea descrescătoare finalizare:

6, 3, 9, 8, 4

Algoritmul lui Kosaraju

Timp de finalizare

Pasul 1.



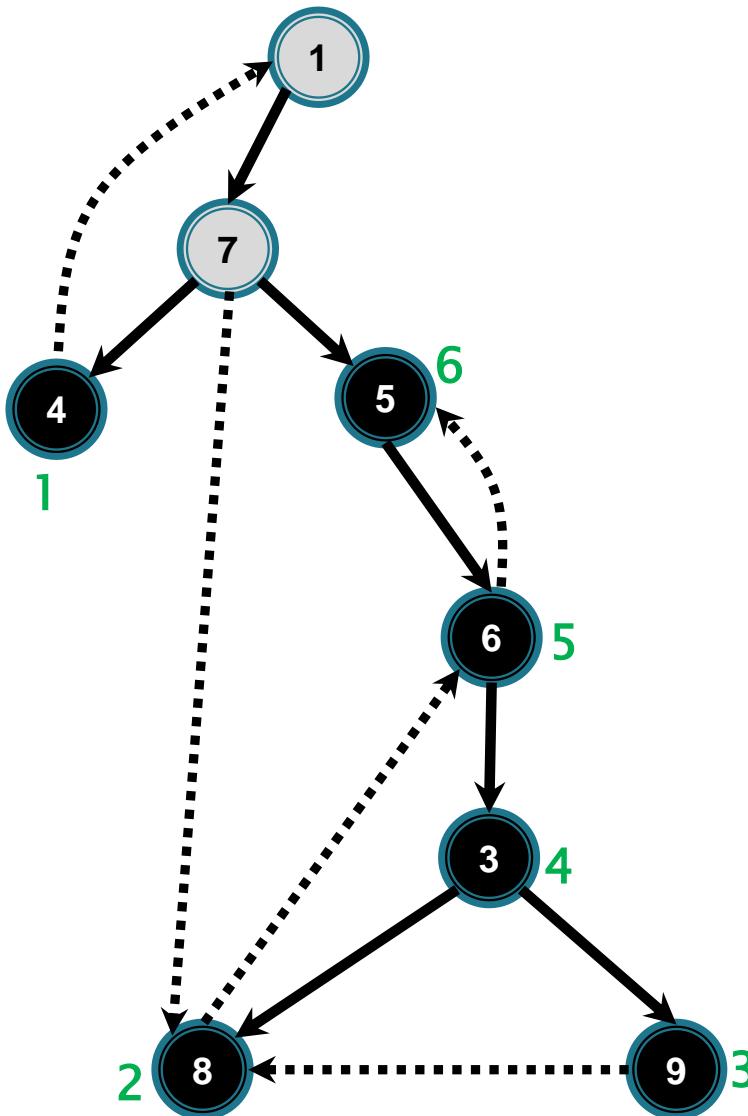
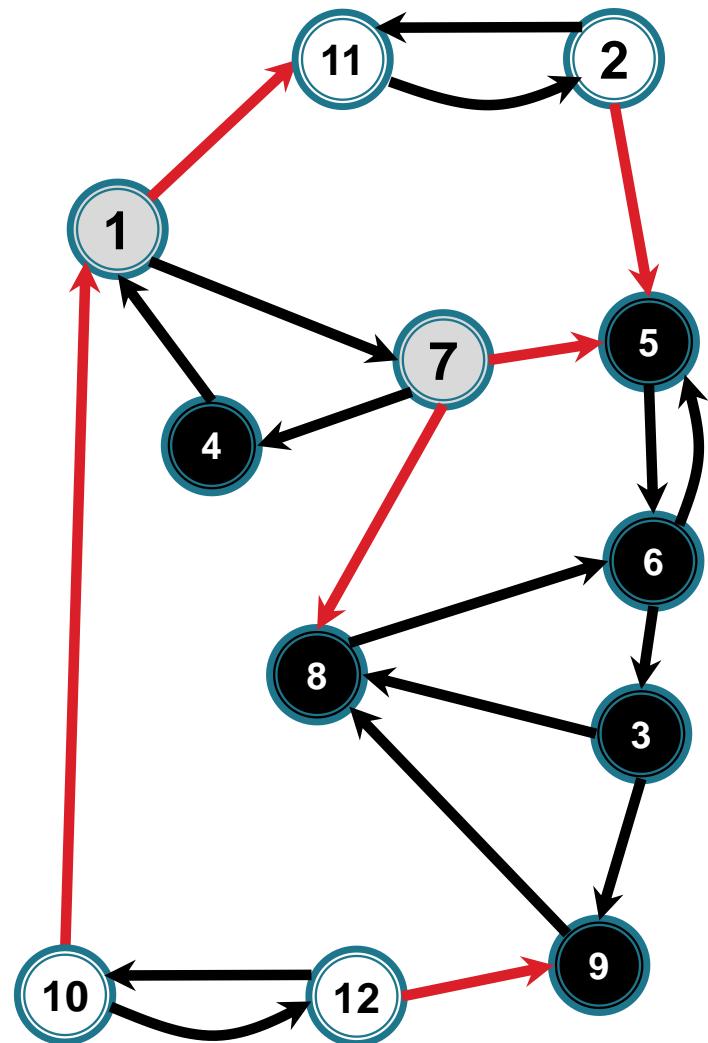
Ordinea descrescătoare finalizare:

5, 6, 3, 9, 8, 4

Algoritmul lui Kosaraju

Timp de finalizare

Pasul 1.



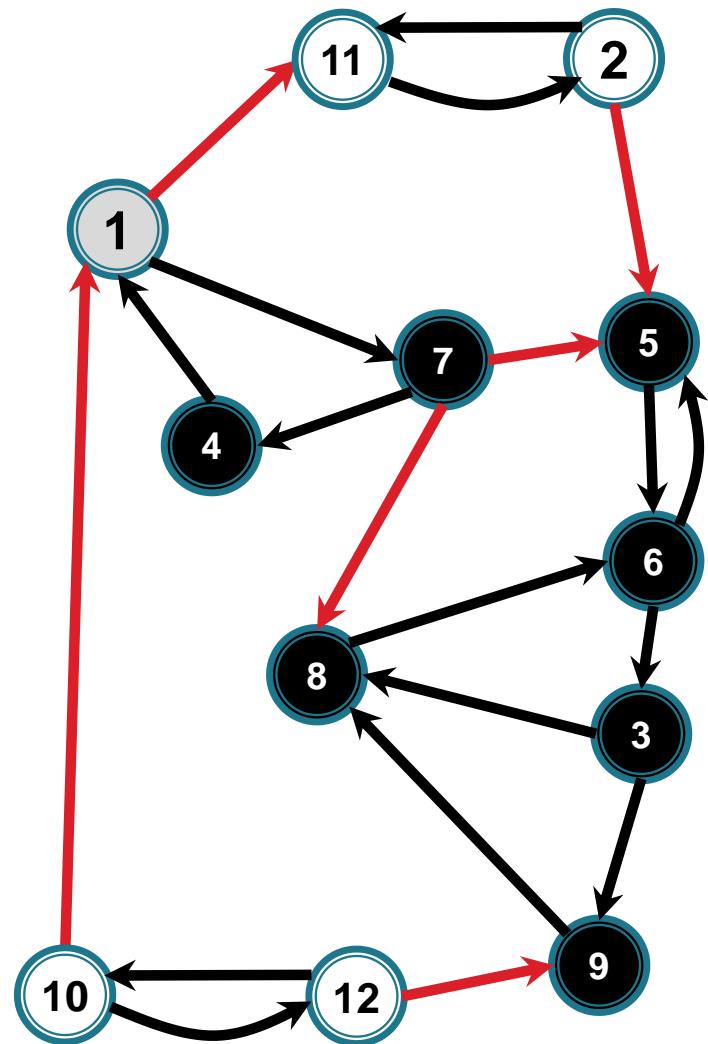
Ordinea descrescătoare finalizare:

5, 6, 3, 9, 8, 4

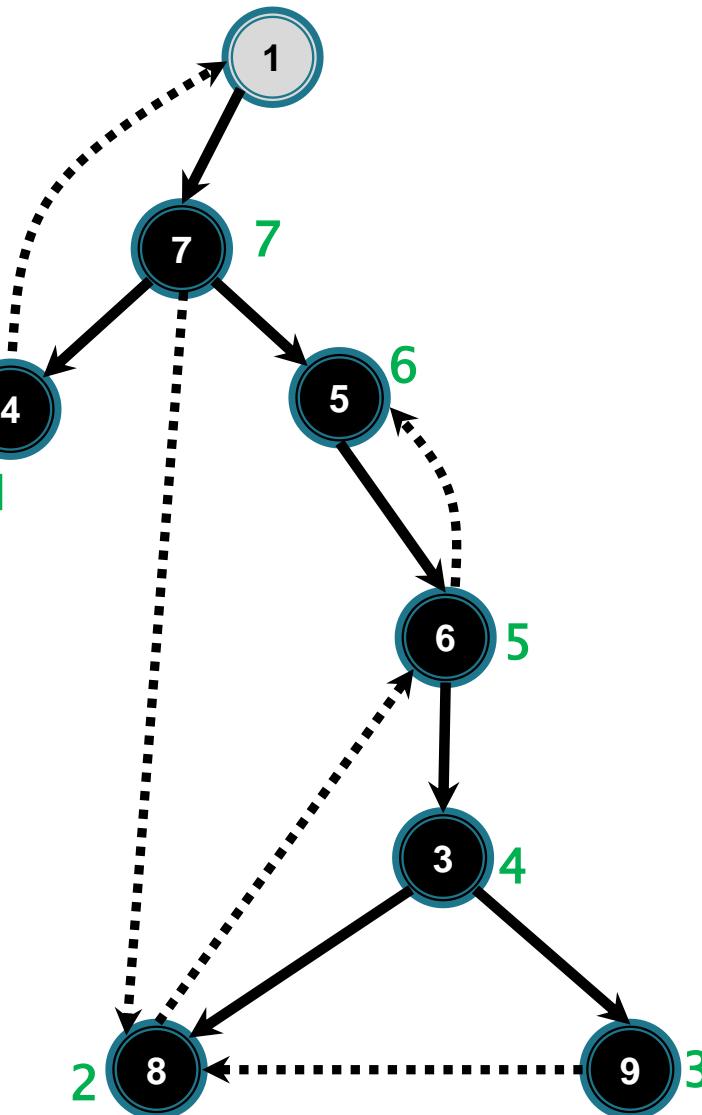
Algoritmul lui Kosaraju

Timp de finalizare

Pasul 1.



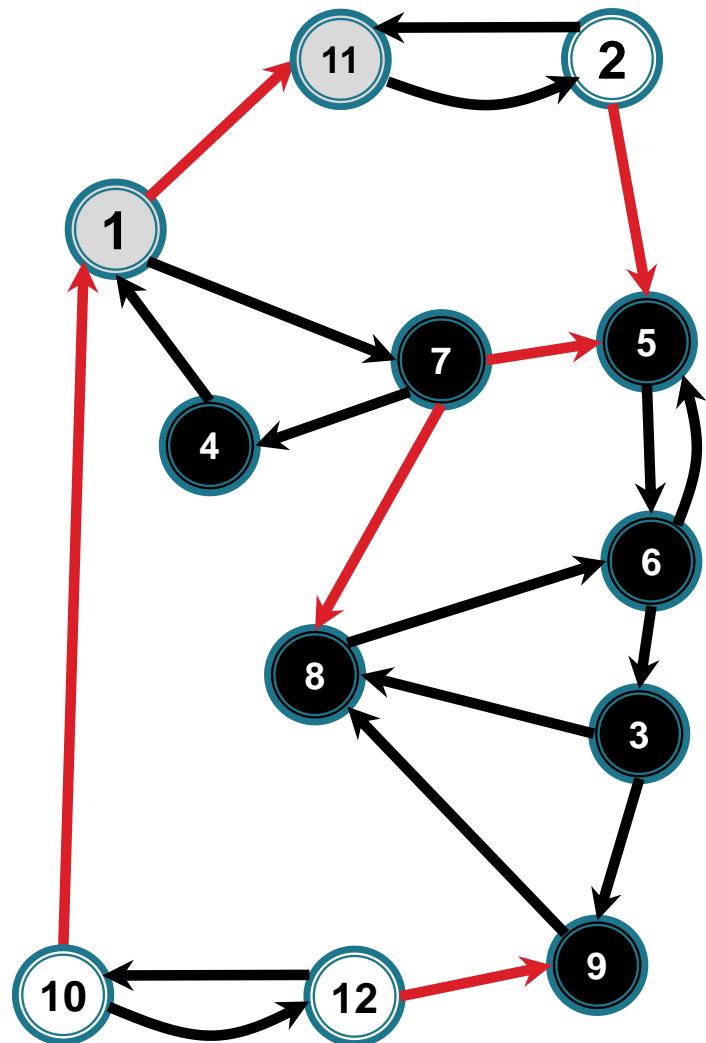
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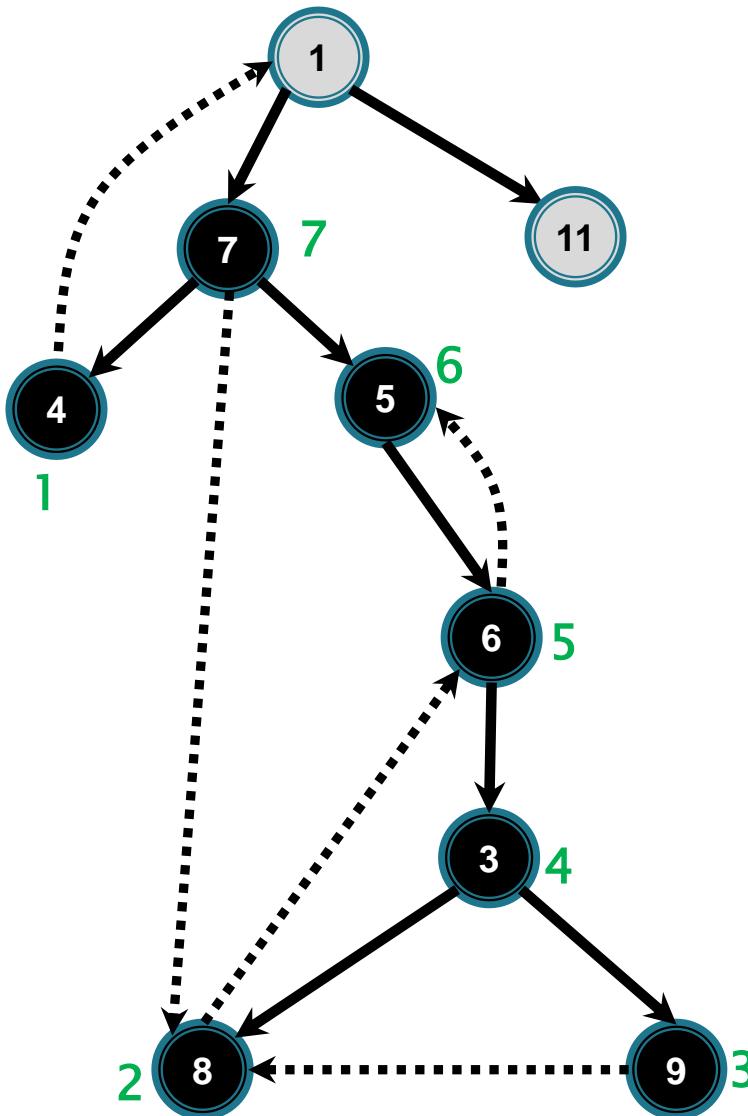
7, 5, 6, 3, 9, 8, 4

Algoritmul lui Kosaraju

Pasul 1.



Timp de finalizare

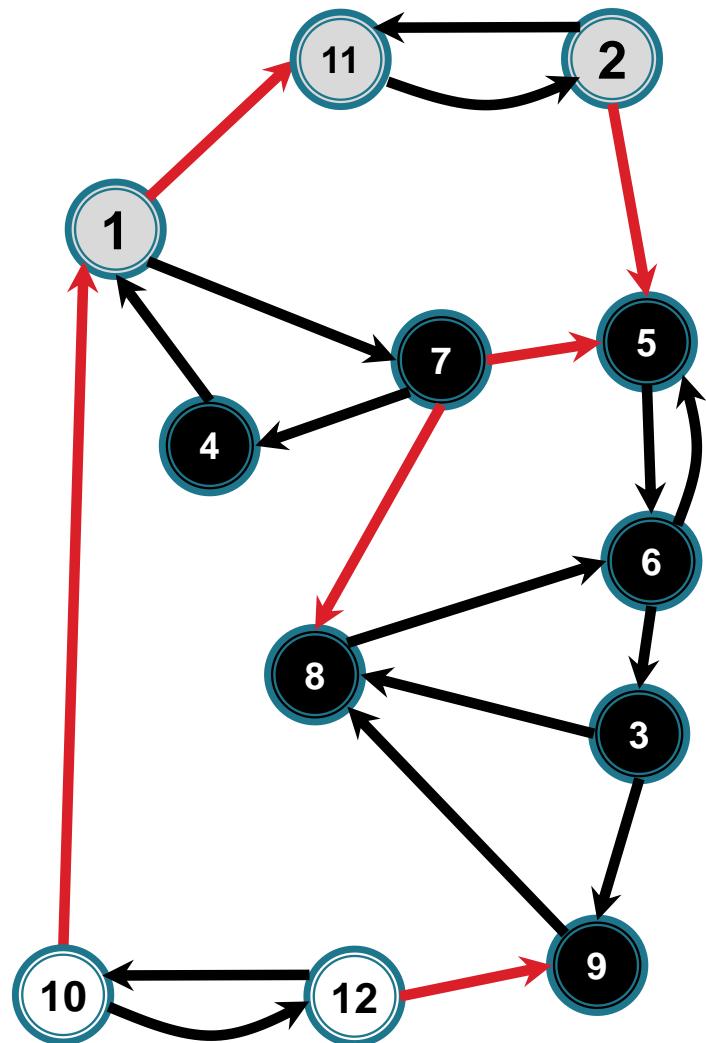


Ordinea descrescătoare finalizare:

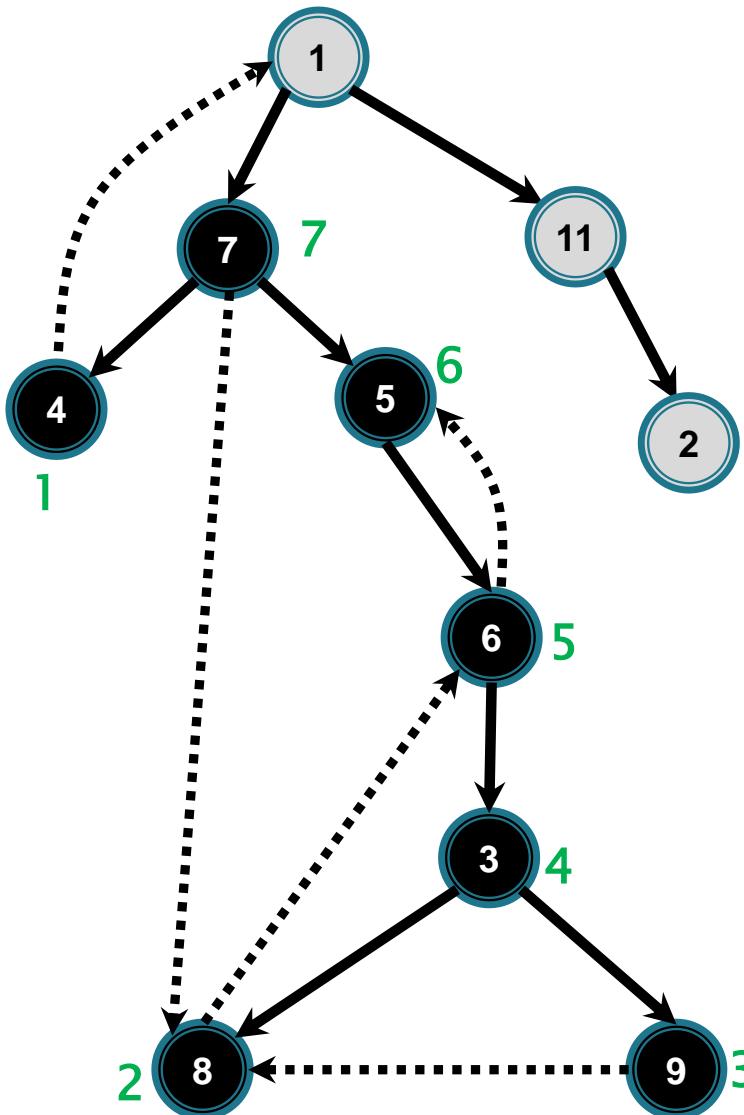
7, 5, 6, 3, 9, 8, 4

Algoritmul lui Kosaraju

Pasul 1.



Timp de finalizare

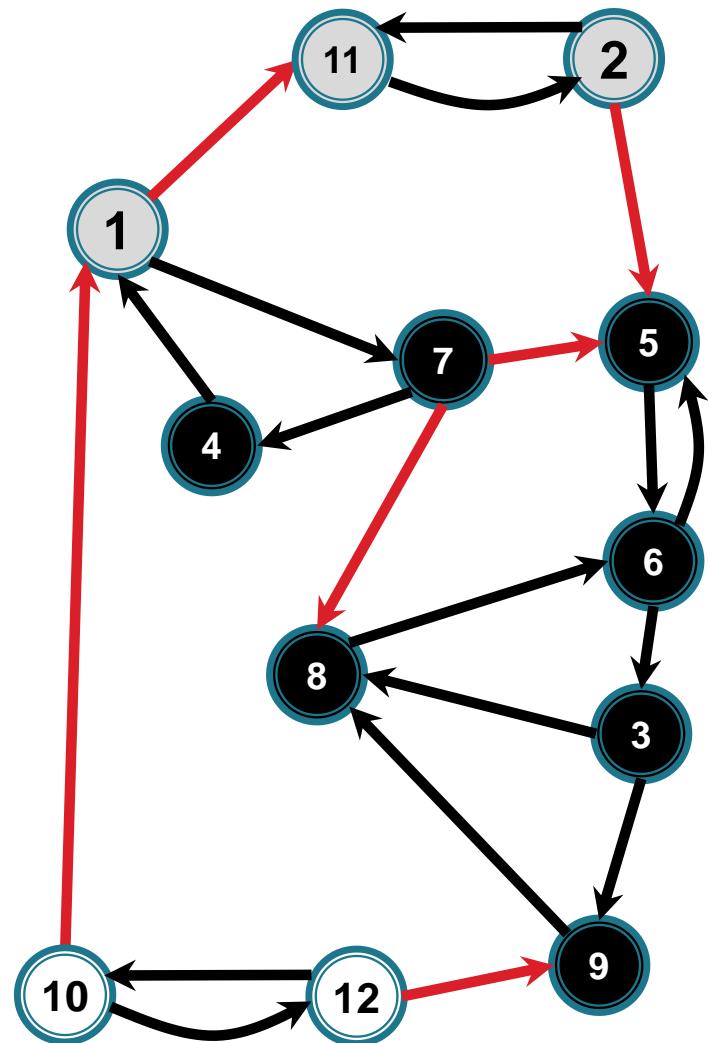


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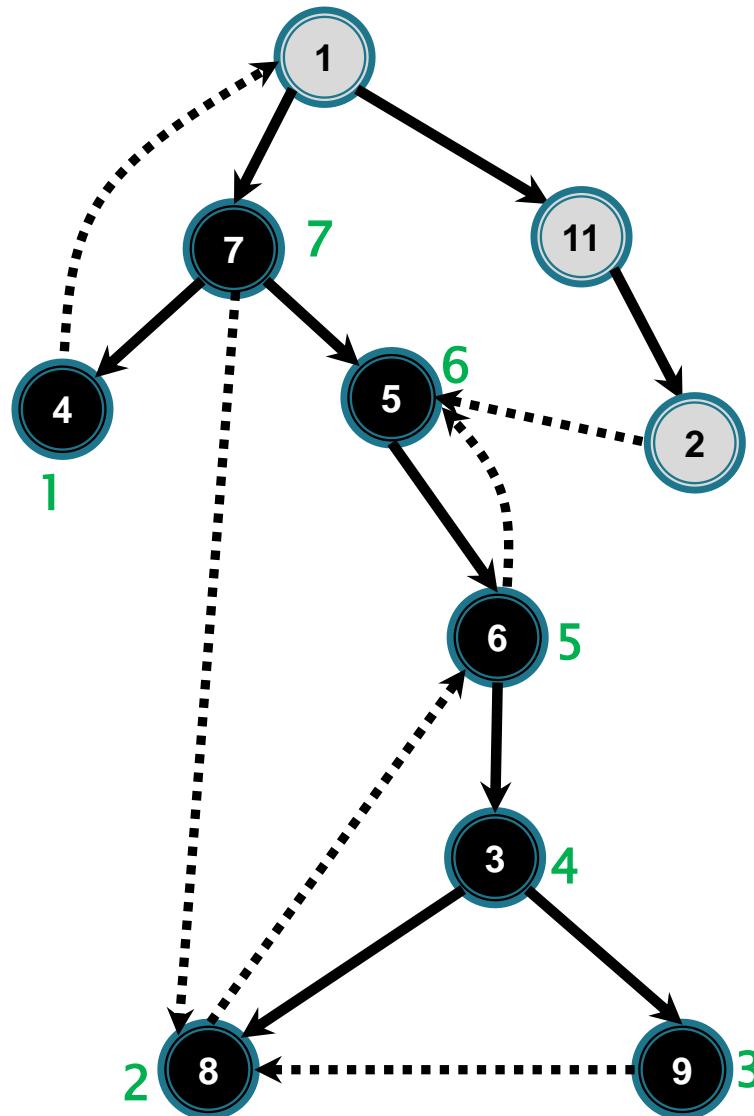
7, 5, 6, 3, 9, 8, 4

Algoritmul lui Kosaraju

Pasul 1.



Timp de finalizare

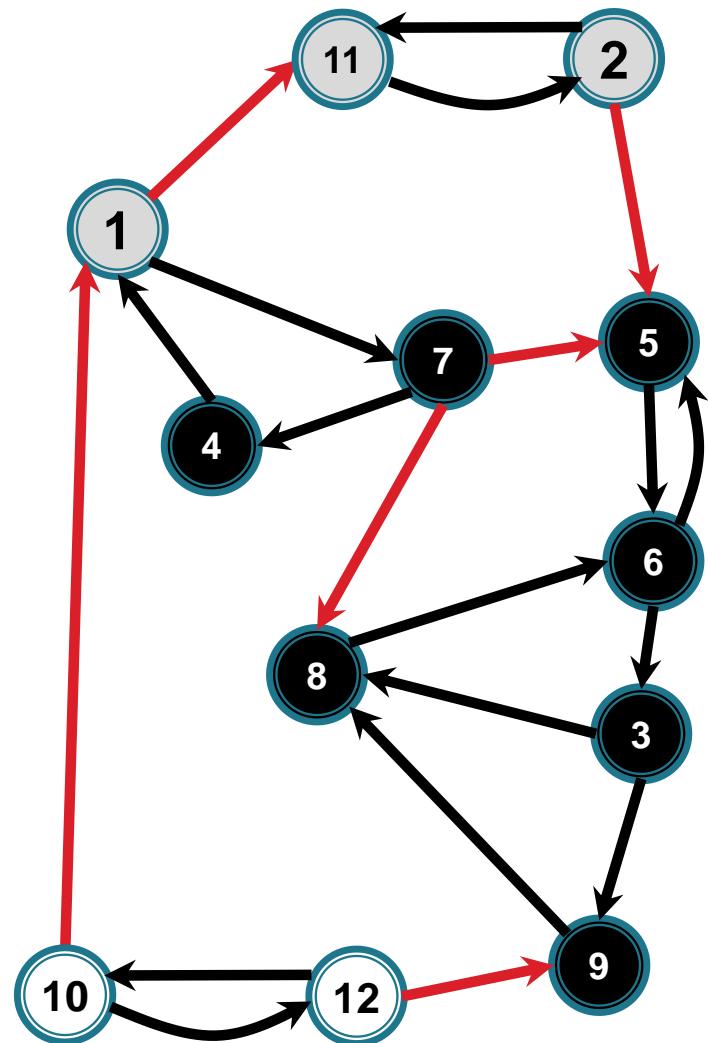


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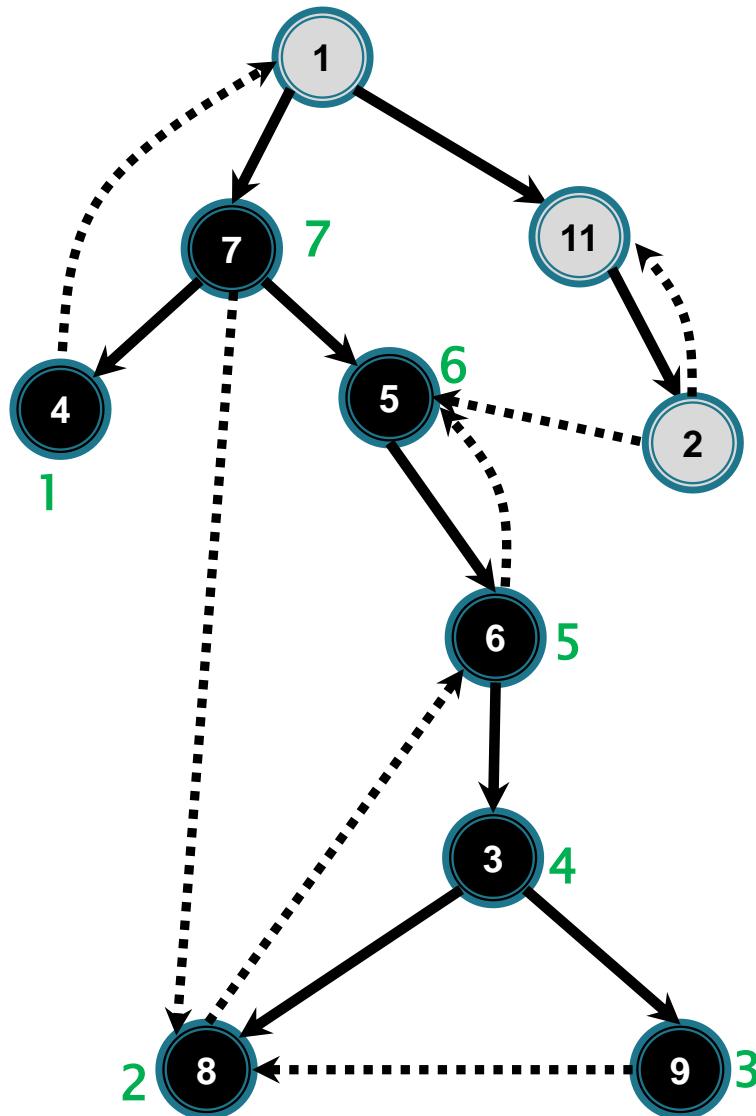
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Algoritmul lui Kosaraju

Pasul 1.



Timp de finalizare

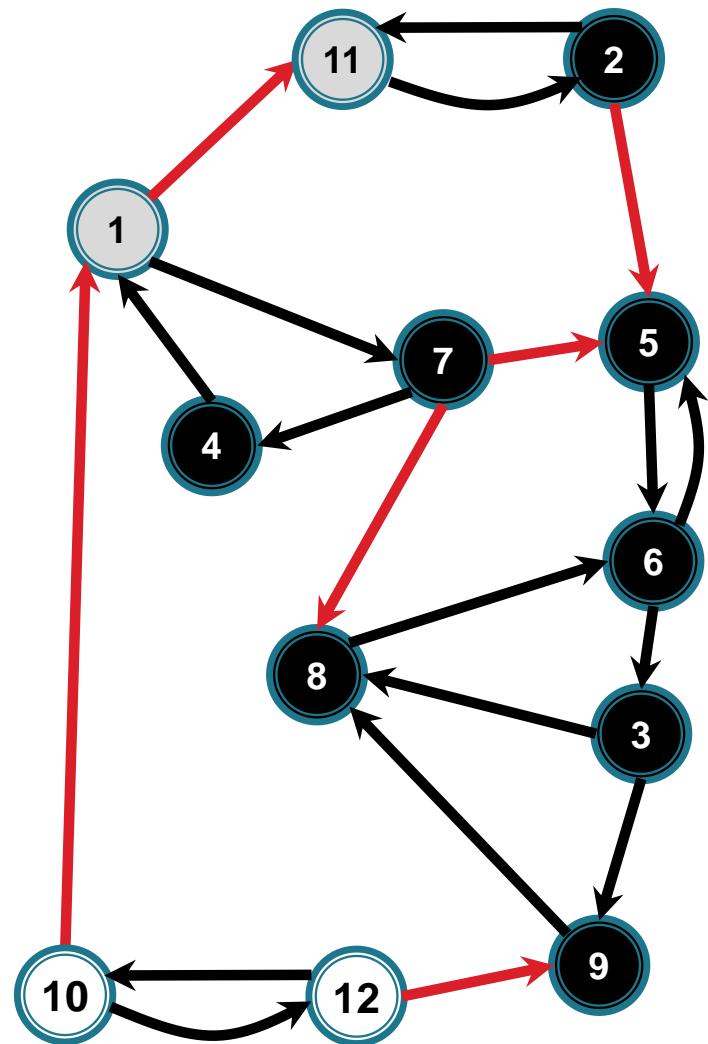


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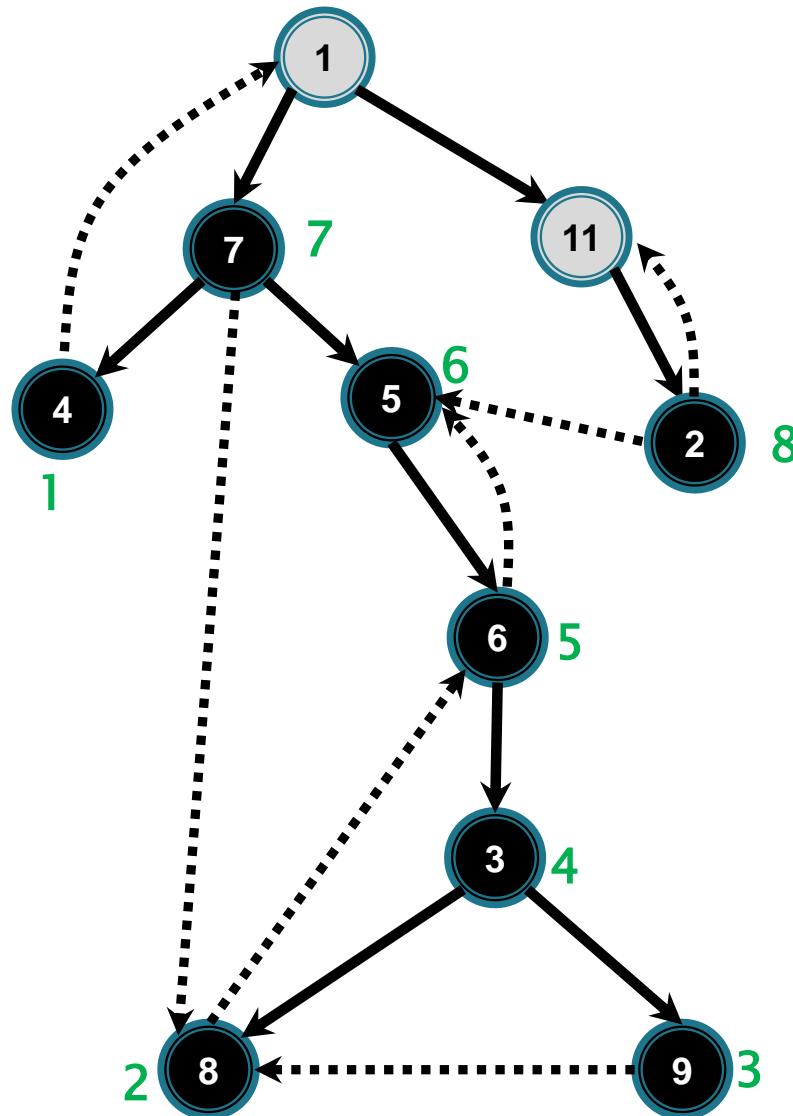
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Algoritmul lui Kosaraju

Pasul 1.



Timp de finalizare

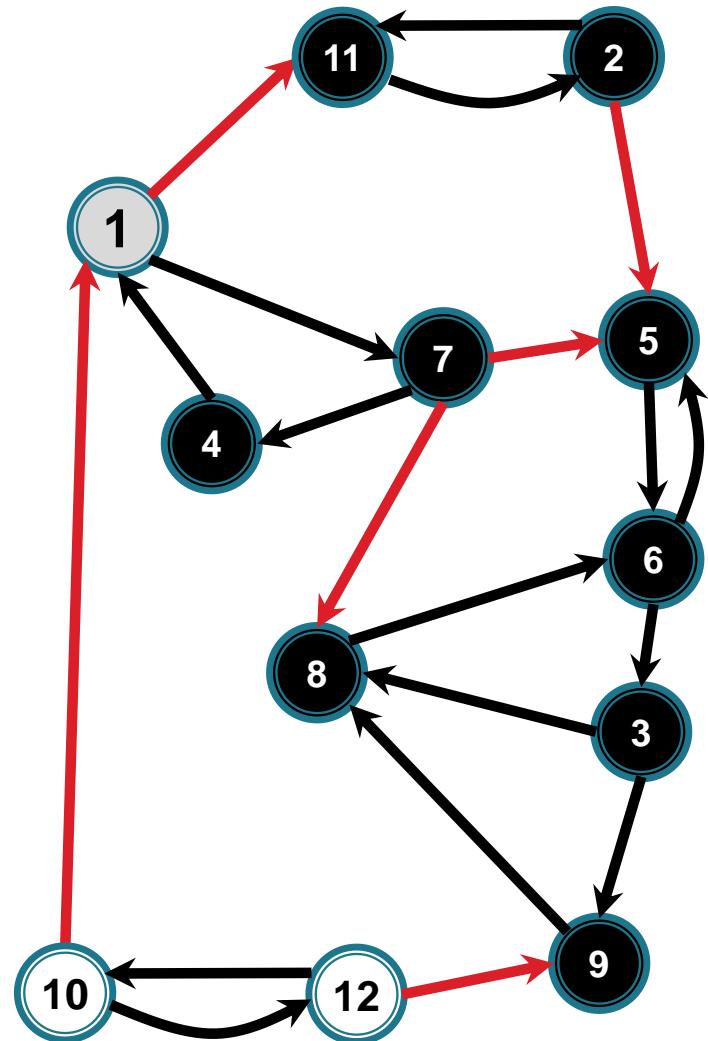


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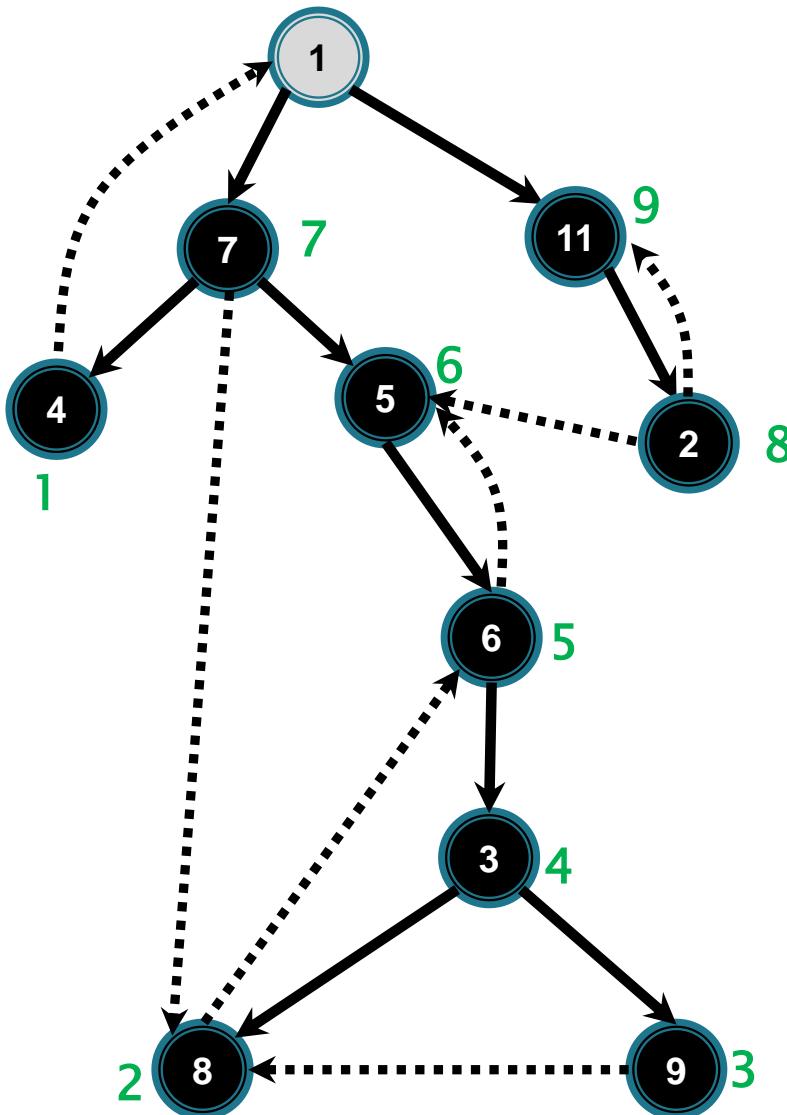
2, 7, 5, 6, 3, 9, 8, 4

Algoritmul lui Kosaraju

Pasul 1.



Timp de finalizare

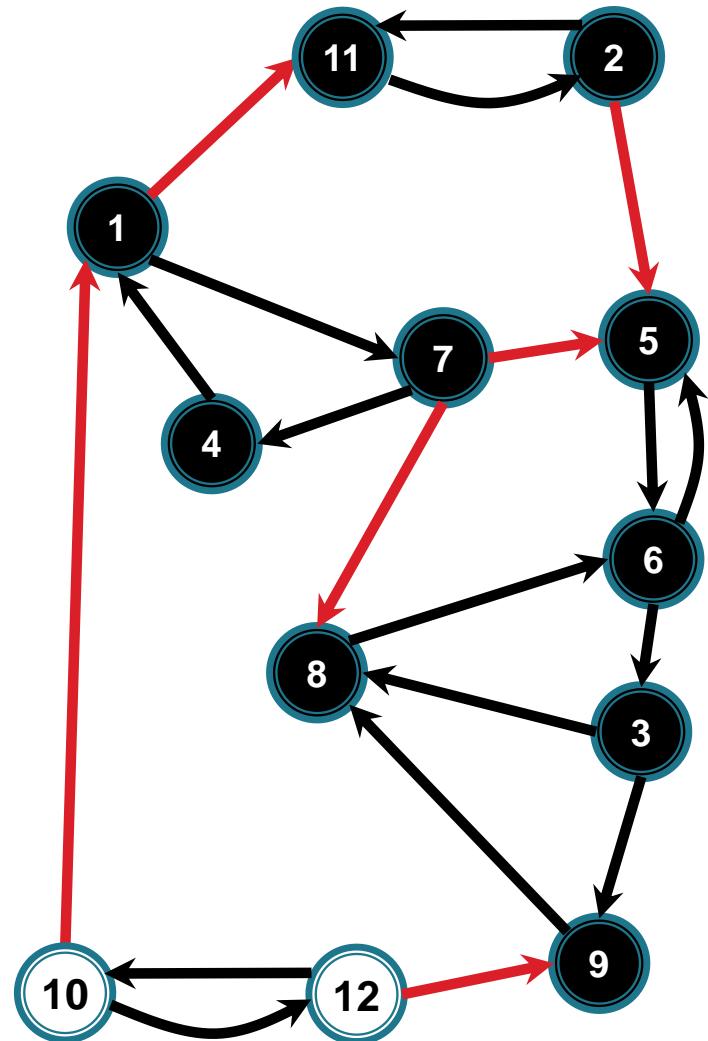


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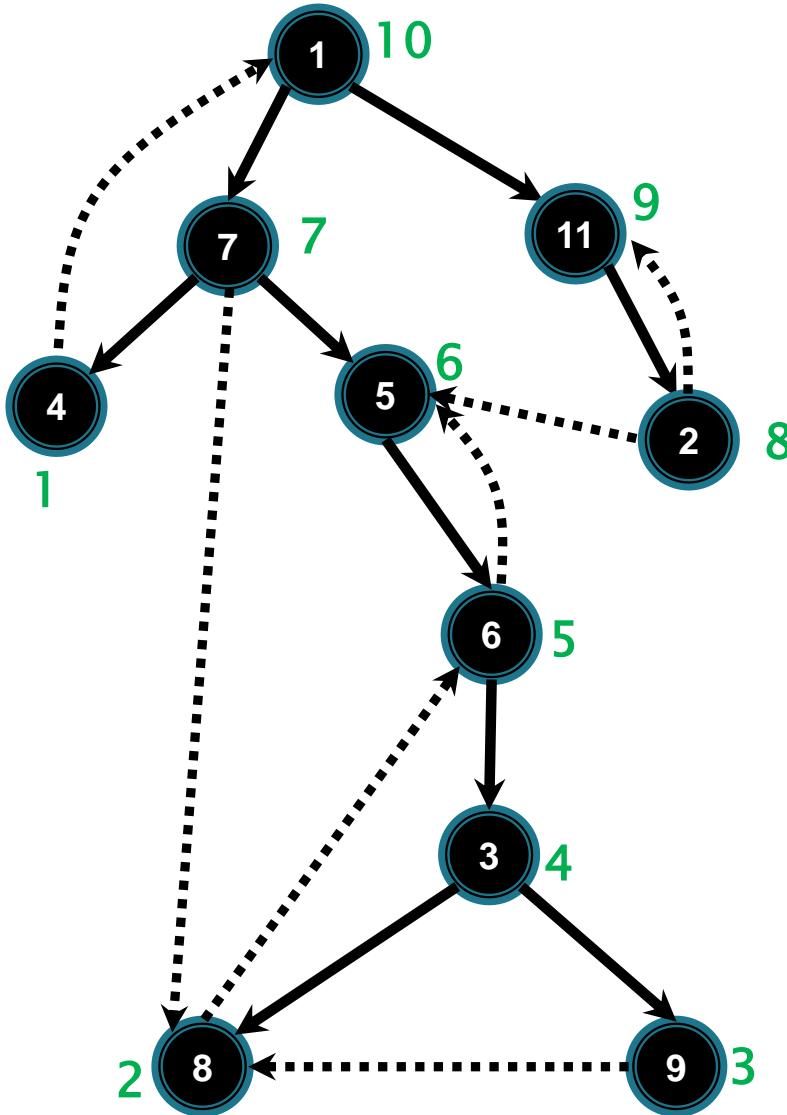
11, 2, 7, 5, 6, 3, 9, 8, 4

Algoritmul lui Kosaraju

Pasul 1.



Timp de finalizare

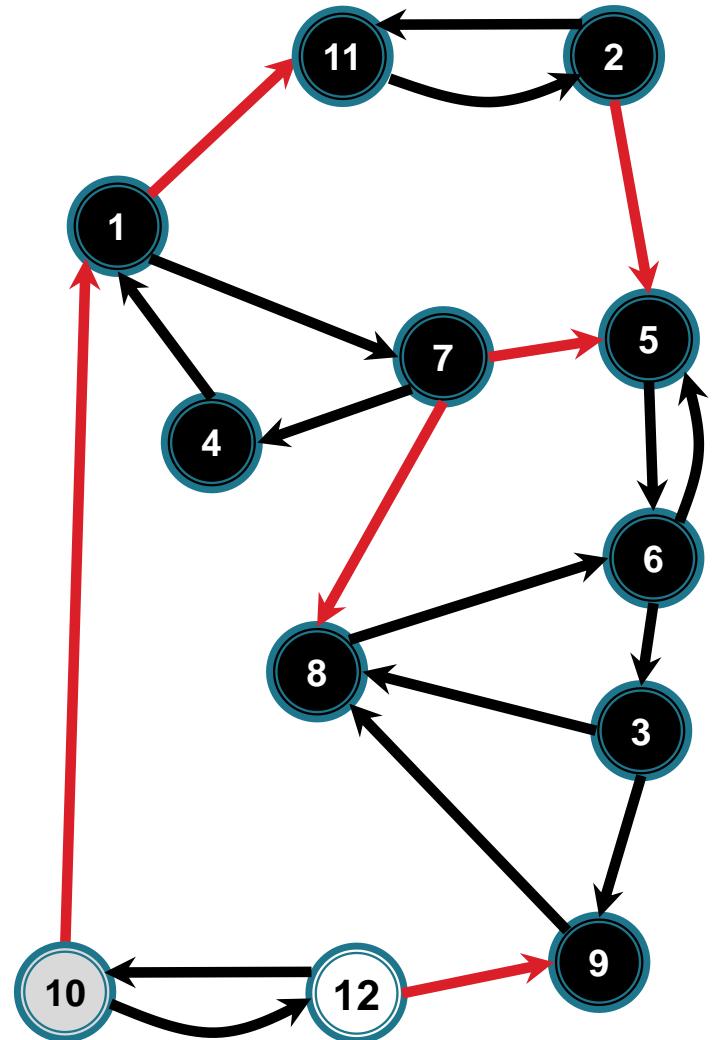


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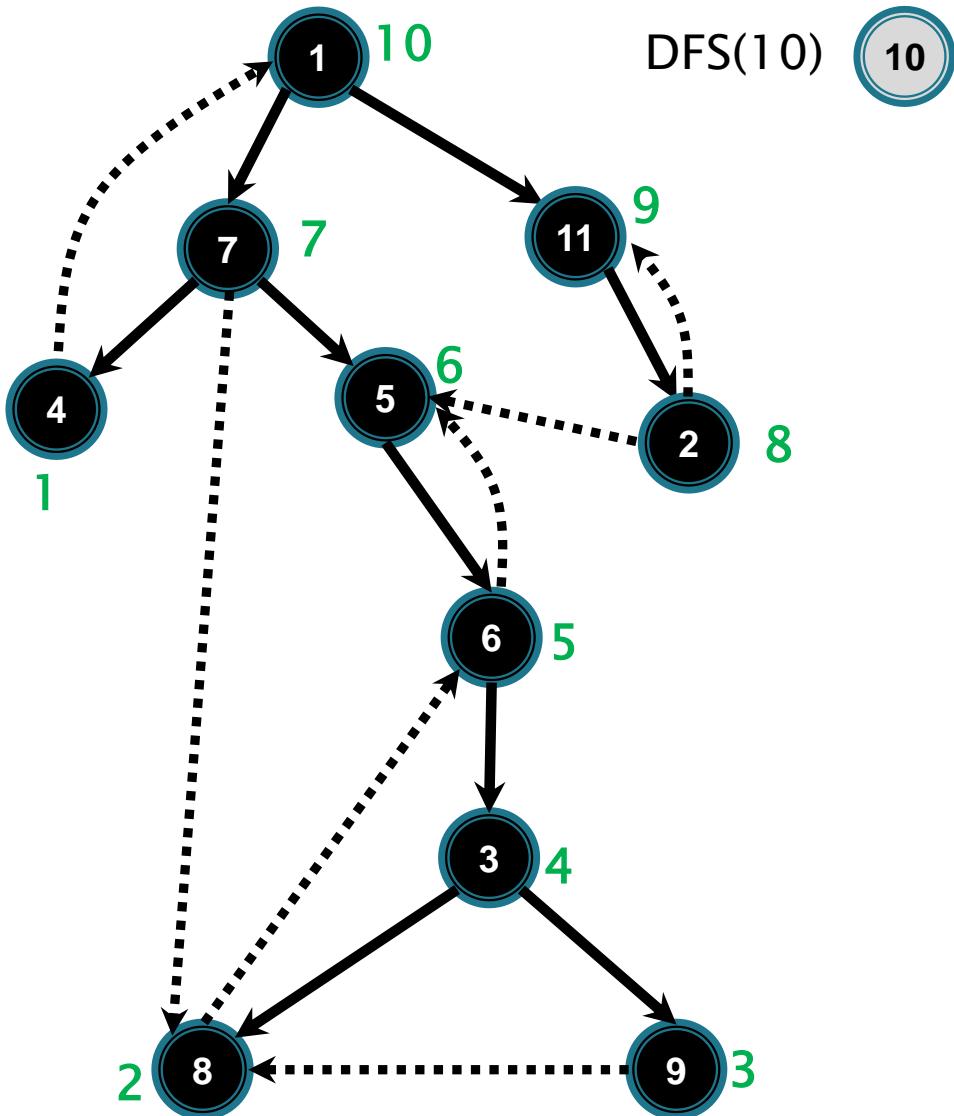
1, 11, 2, 7, 5, 6, 3, 9, 8, 4

Algoritmul lui Kosaraju

Pasul 1.



Timp de finalizare

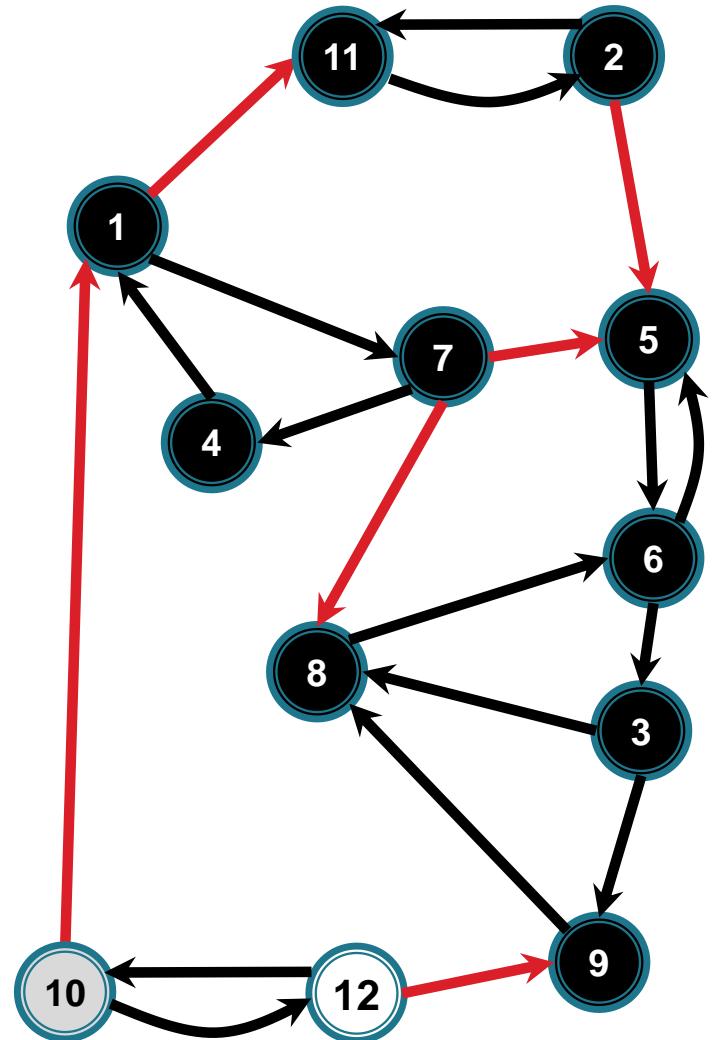


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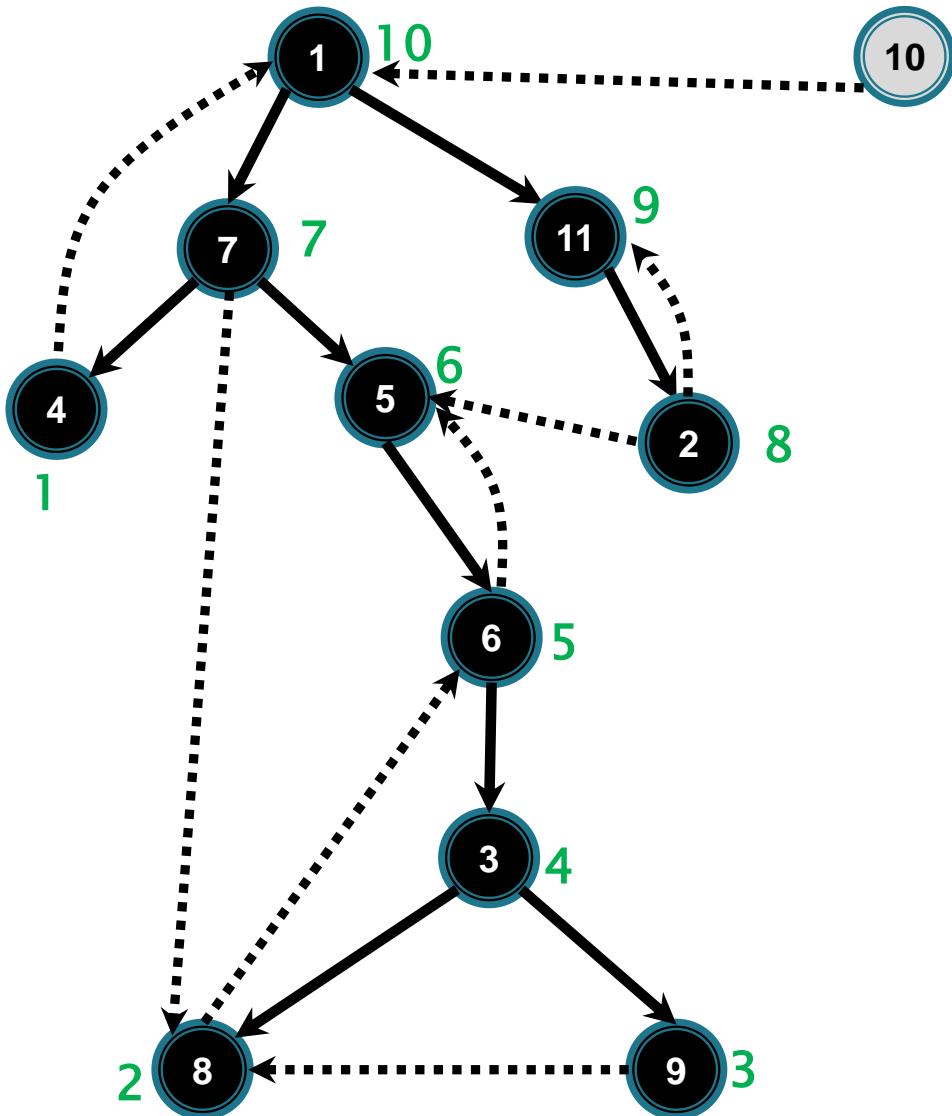
1, 11, 2, 7, 5, 6, 3, 9, 8, 4

Algoritmul lui Kosaraju

Pasul 1.



Timp de finalizare

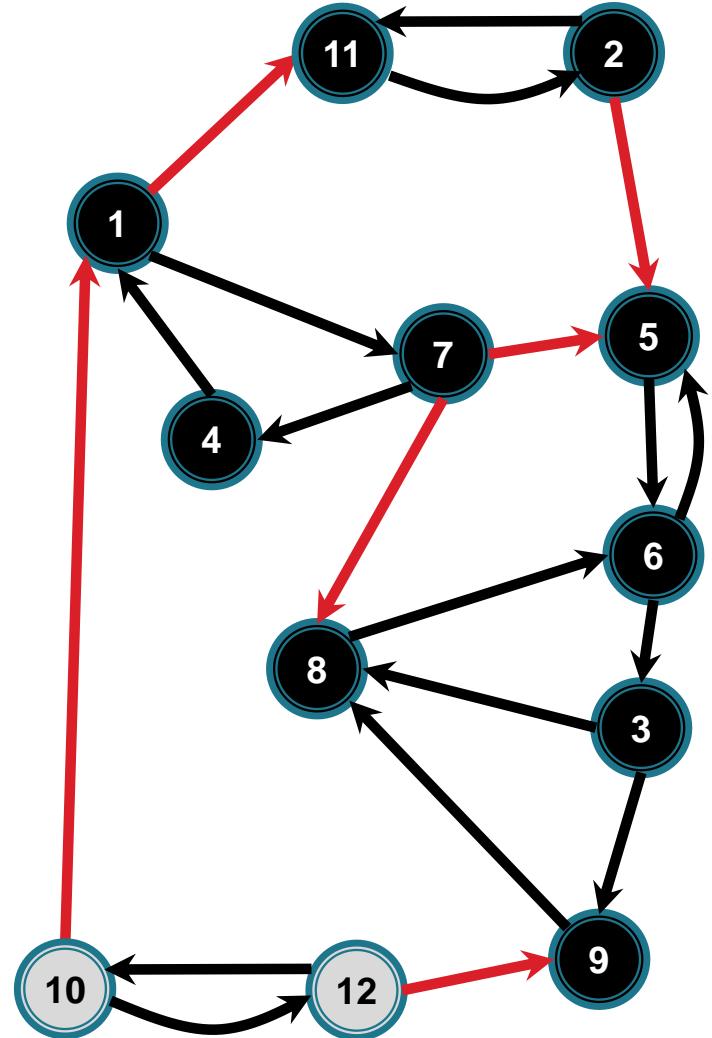


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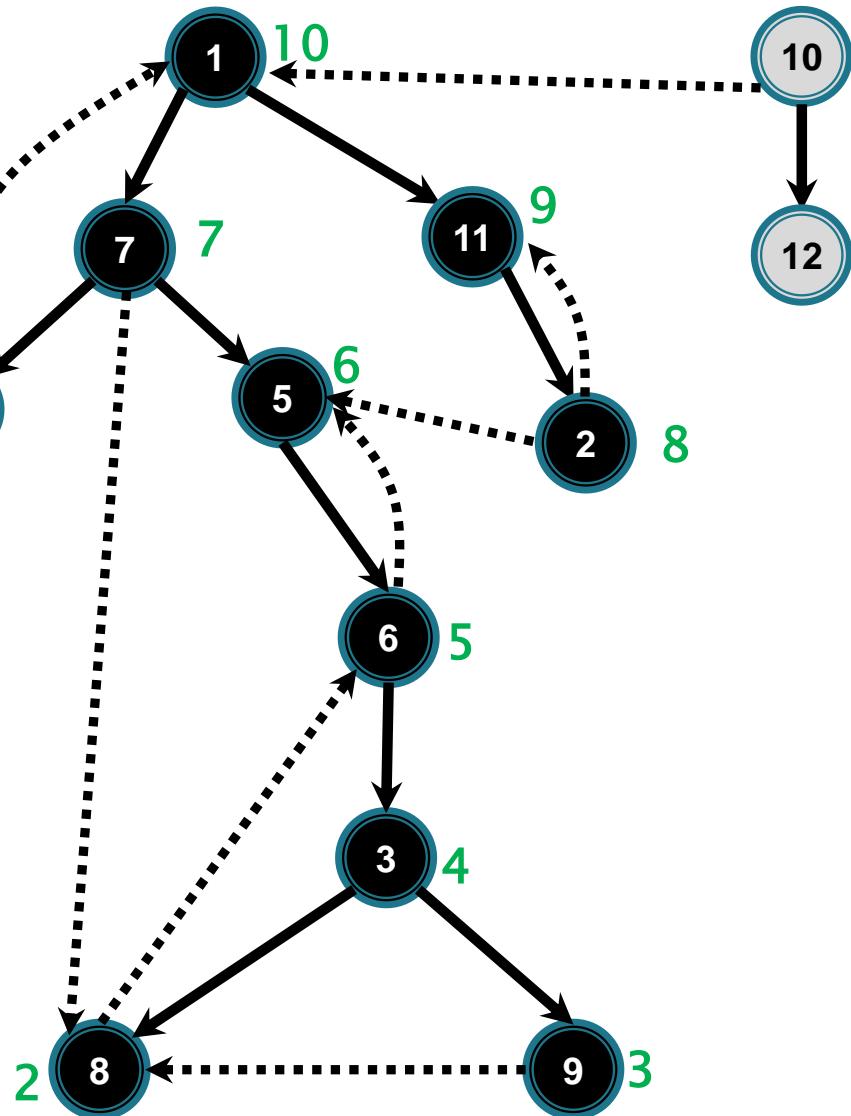
1, 11, 2, 7, 5, 6, 3, 9, 8, 4

Algoritmul lui Kosaraju

Pasul 1.



Timp de finalizare

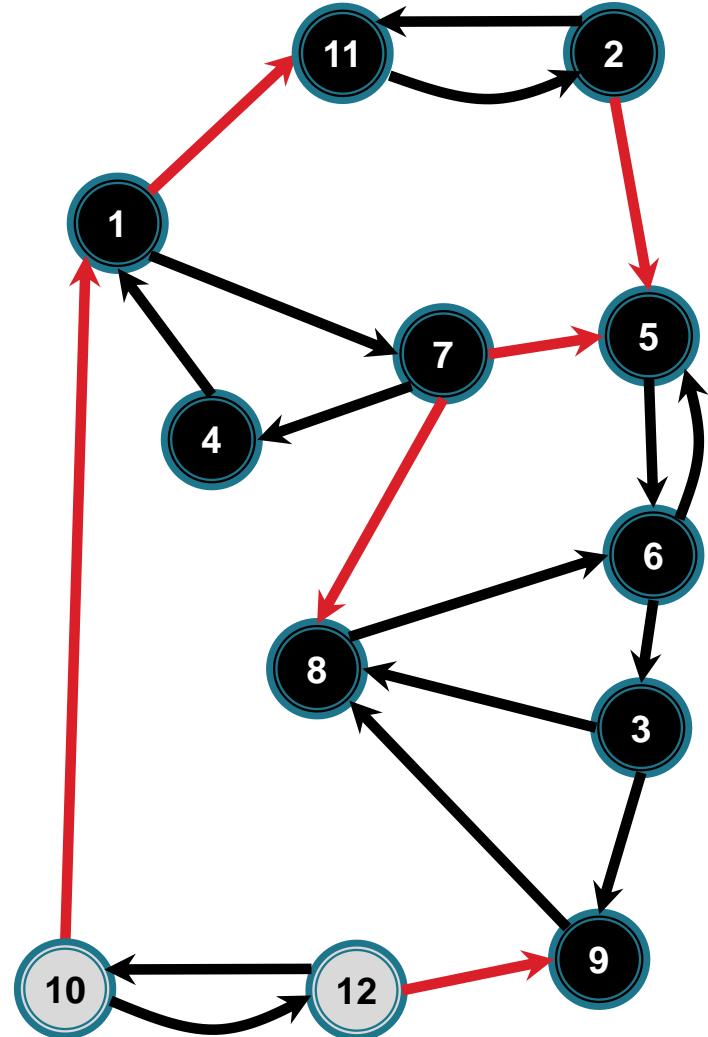


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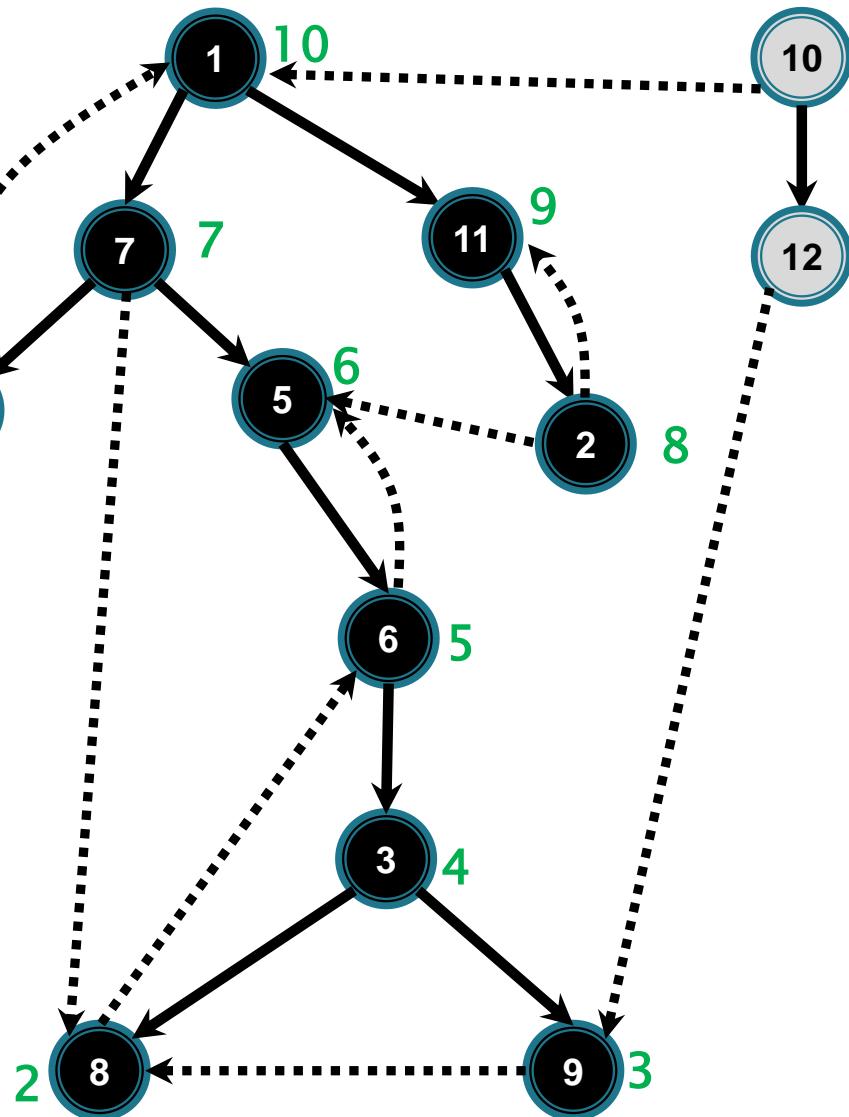
1, 11, 2, 7, 5, 6, 3, 9, 8, 4

Algoritmul lui Kosaraju

Pasul 1.



Timp de finalizare

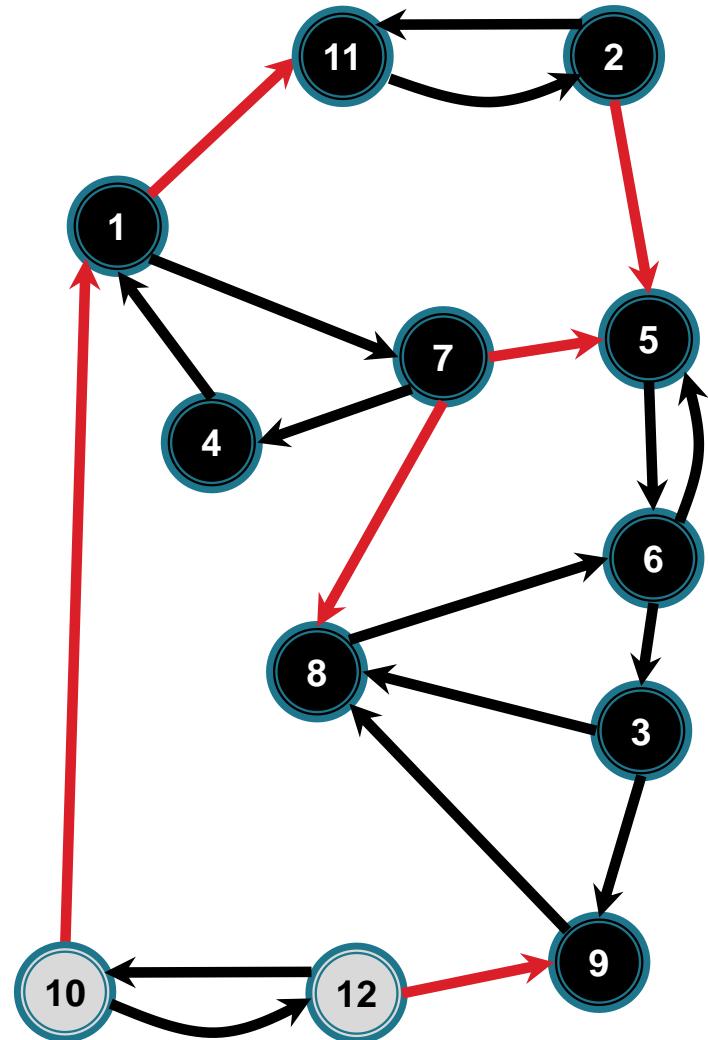


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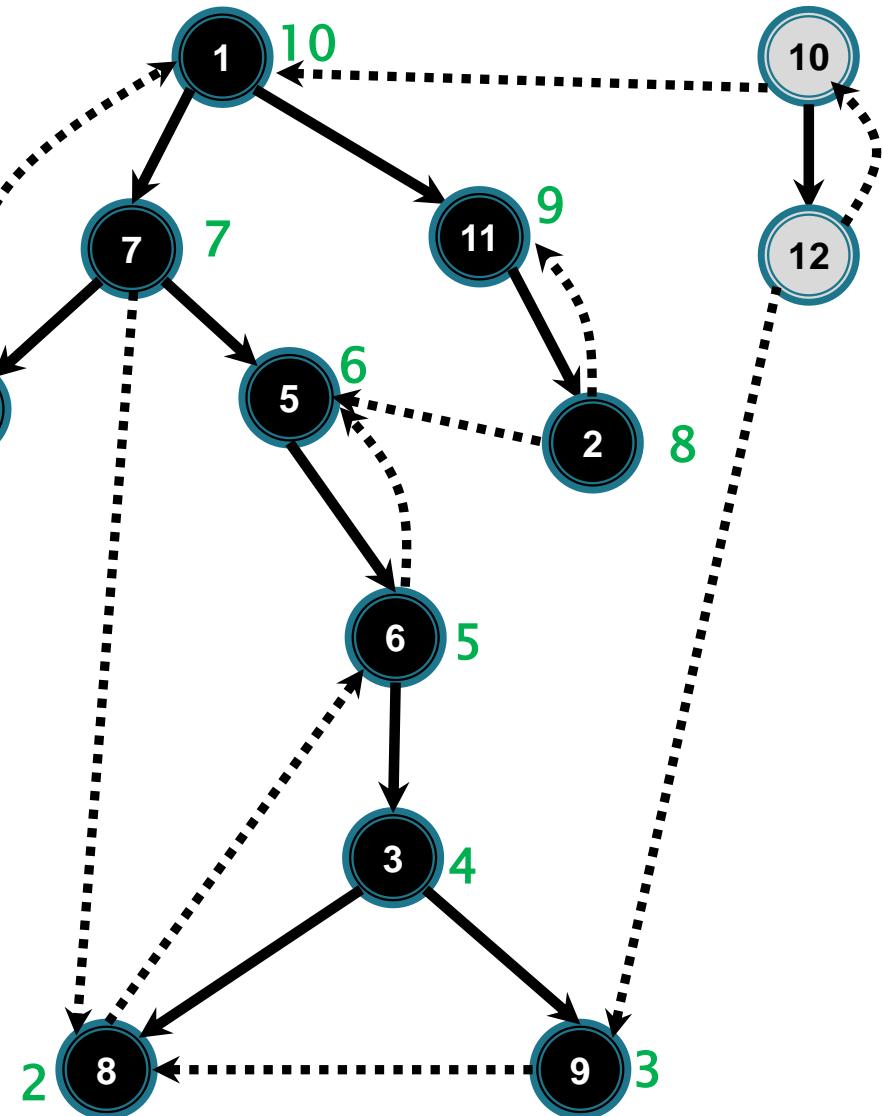
1, 11, 2, 7, 5, 6, 3, 9, 8, 4

Algoritmul lui Kosaraju

Pasul 1.



Timp de finalizare

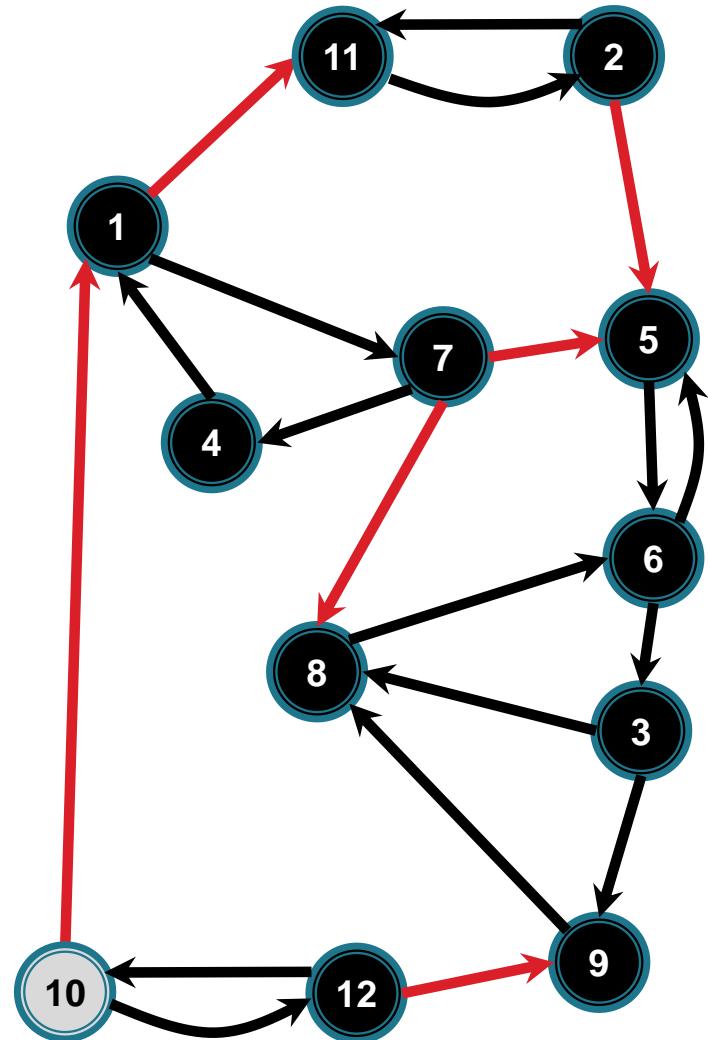


Ordinea descrescătoare finalizare:

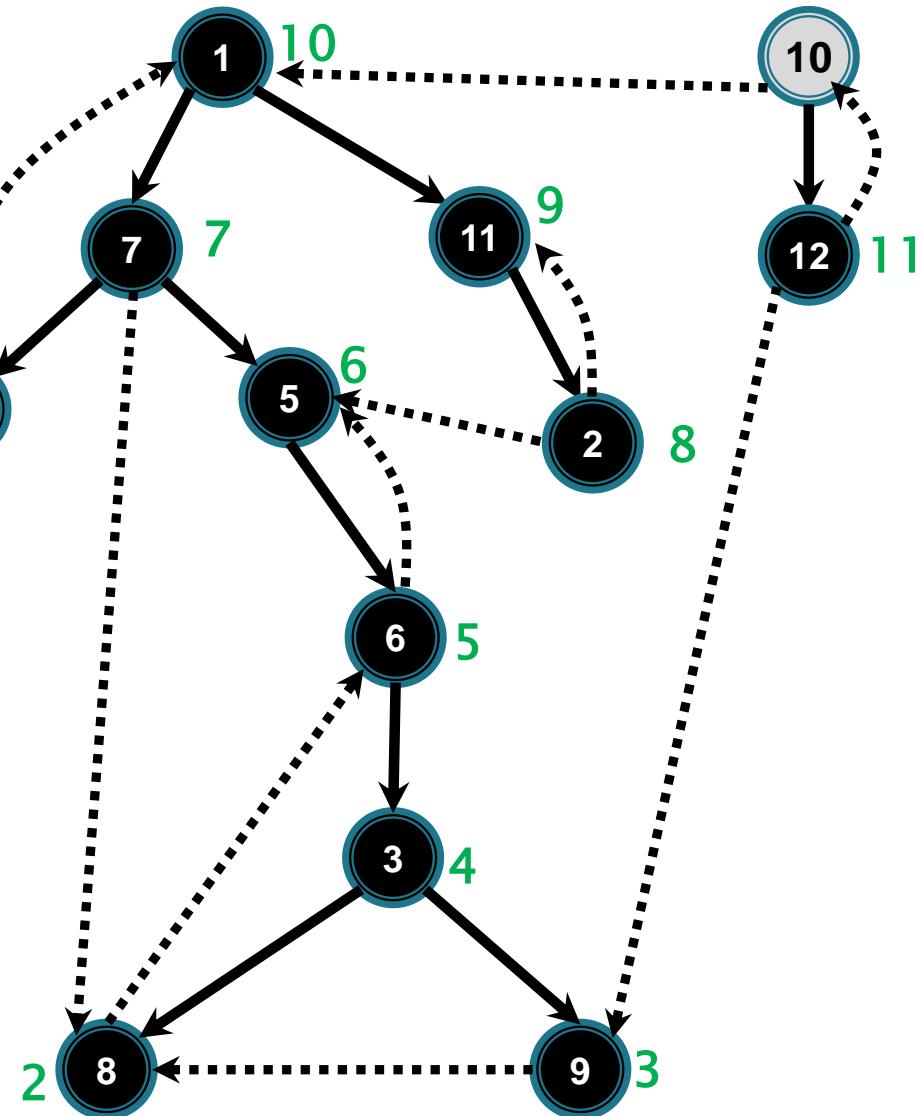
1, 11, 2, 7, 5, 6, 3, 9, 8, 4

Algoritmul lui Kosaraju

Pasul 1.



Timp de finalizare

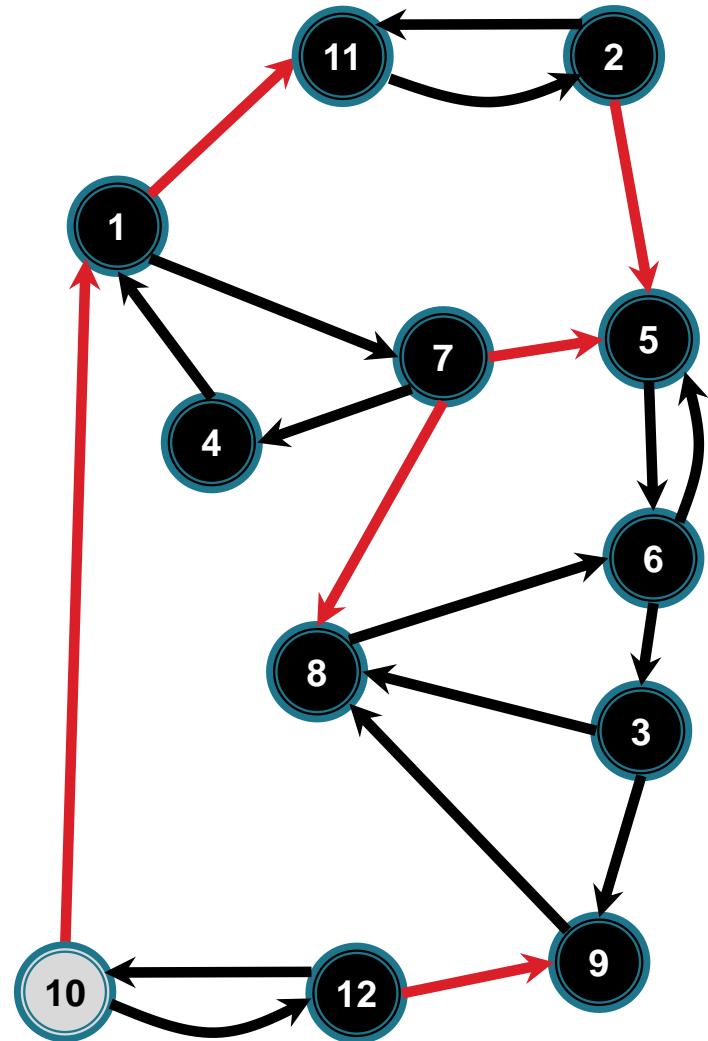


Ordinea descrescătoare finalizare:

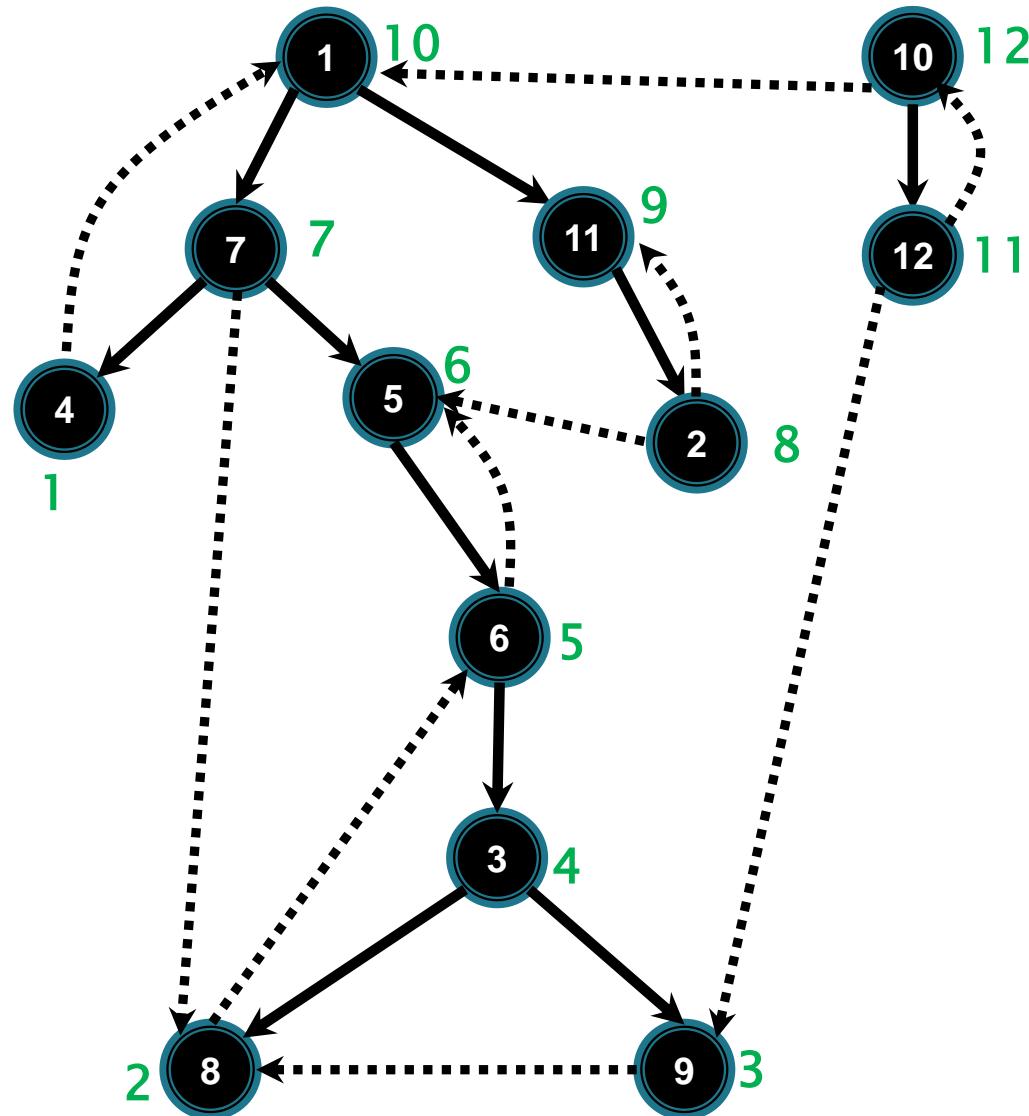
12, 1, 11, 2, 7, 5, 6, 3, 9, 8, 4

Algoritmul lui Kosaraju

Pasul 1.

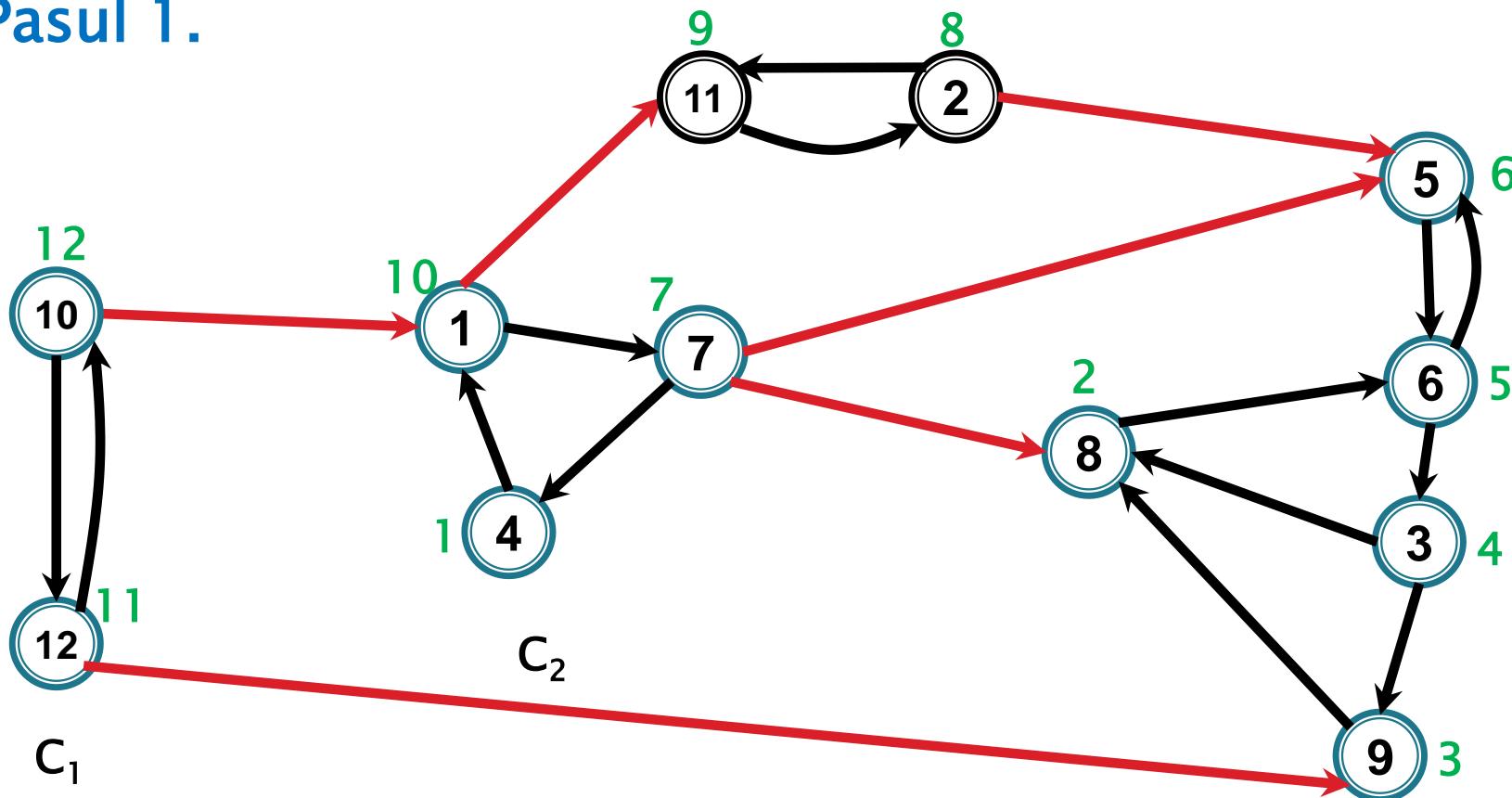


Timp de finalizare



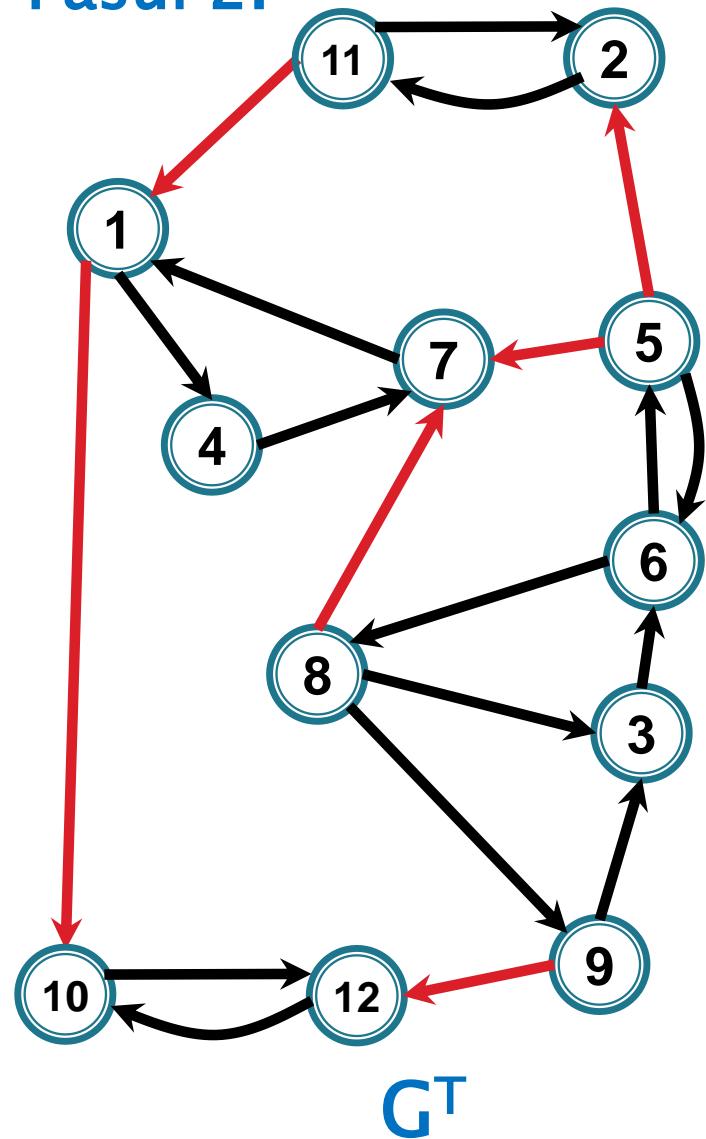
Ordinea descrescătoare finalizare: 10, 12, 1, 11, 2, 7, 5, 6, 3, 9, 8, 4

Pasul 1.



Algoritmul lui Kosaraju

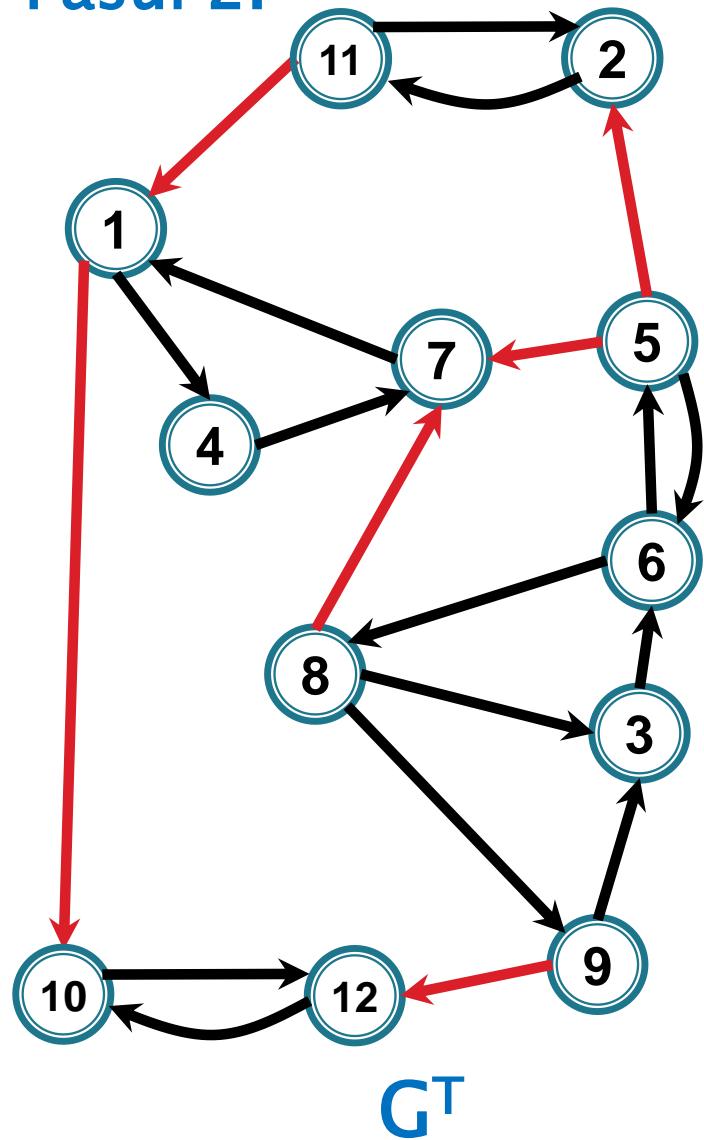
Pasul 2.



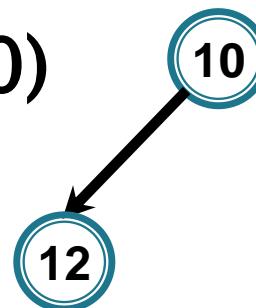
Ordinea descrescătoare finalizare: 10, 12, 1, 11, 2, 7, 5, 6, 3, 9, 8, 4

Algoritmul lui Kosaraju

Pasul 2.



DFS(10)

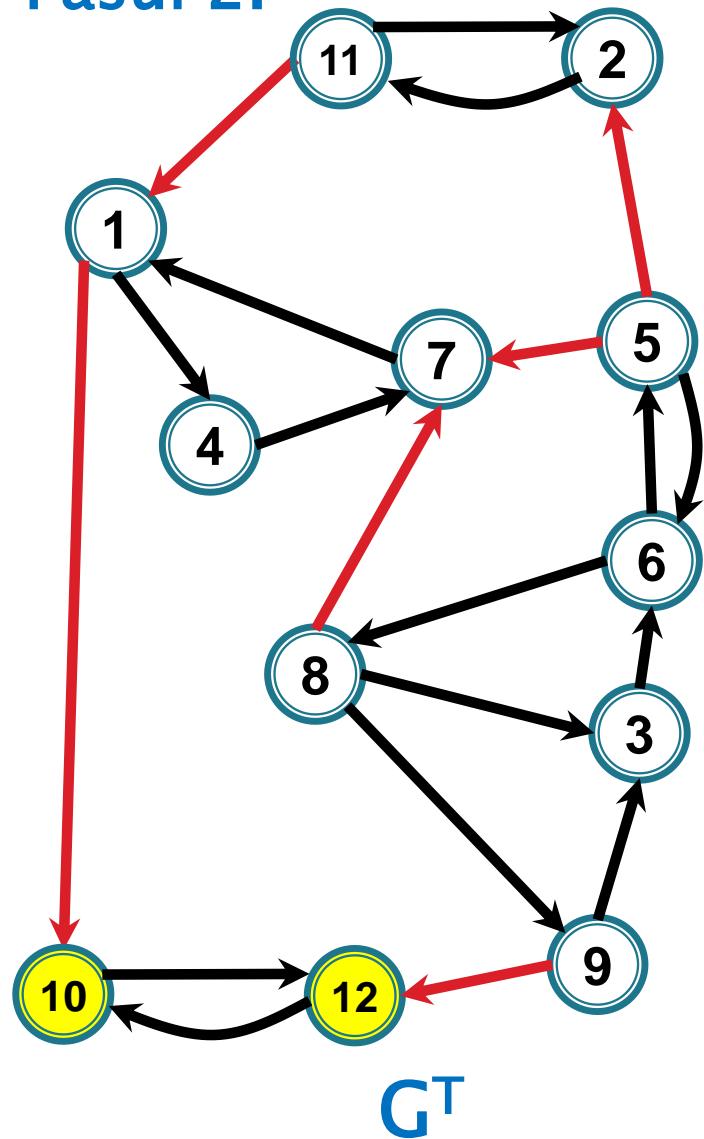


Componenta tare conexă: 10, 12

Ordinea descrescătoare finalizare: 10, 12, 1, 11, 2, 7, 5, 6, 3, 9, 8, 4

Algoritmul lui Kosaraju

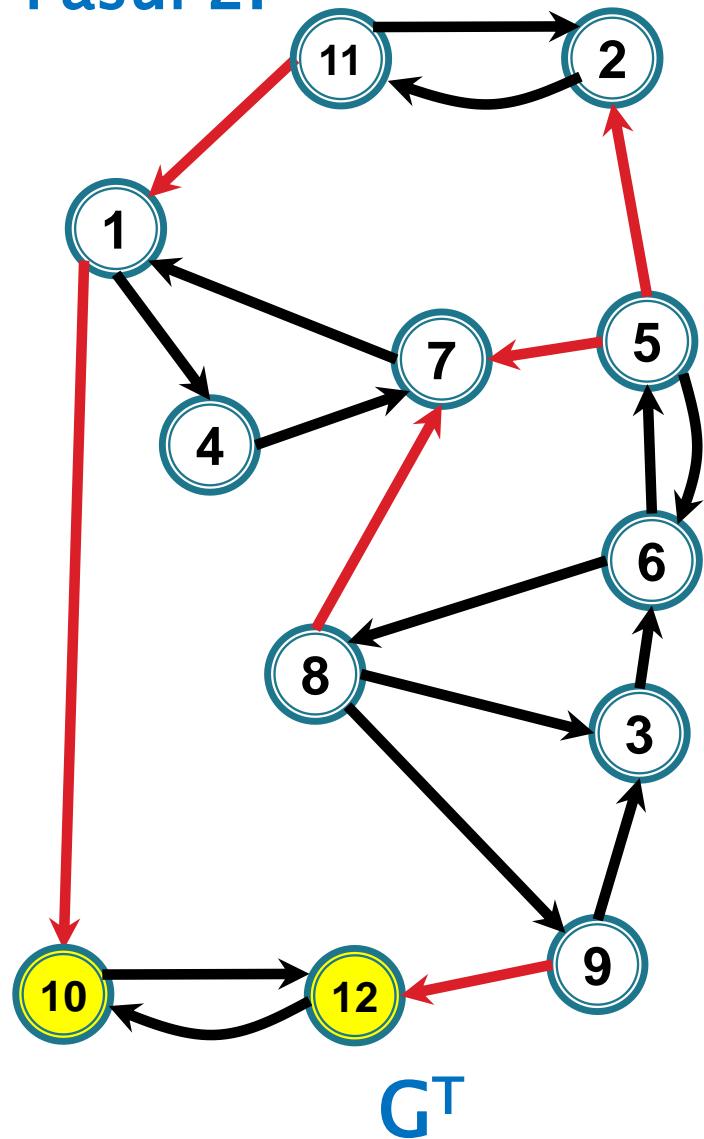
Pasul 2.



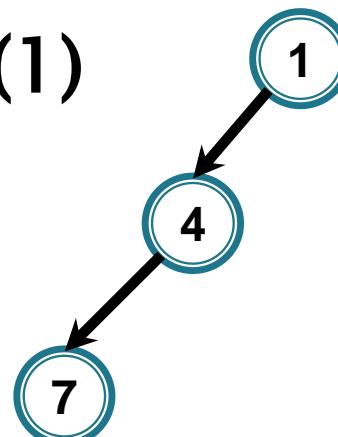
Ordinea descrescătoare finalizare: 10, 12, 1, 11, 2, 7, 5, 6, 3, 9, 8, 4

Algoritmul lui Kosaraju

Pasul 2.



DFS(1)

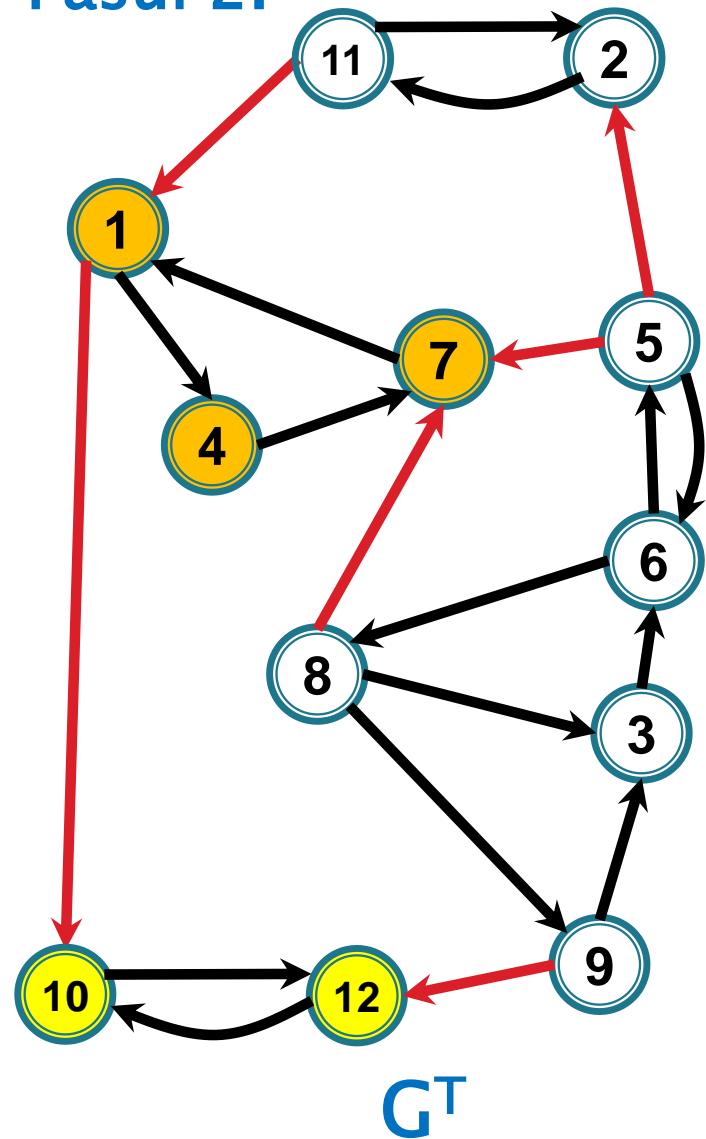


Componenta tare conexă: 1,4,7

Ordinea descrescătoare finalizare: 10, 12, 1, 11, 2, 7, 5, 6, 3, 9, 8, 4

Algoritmul lui Kosaraju

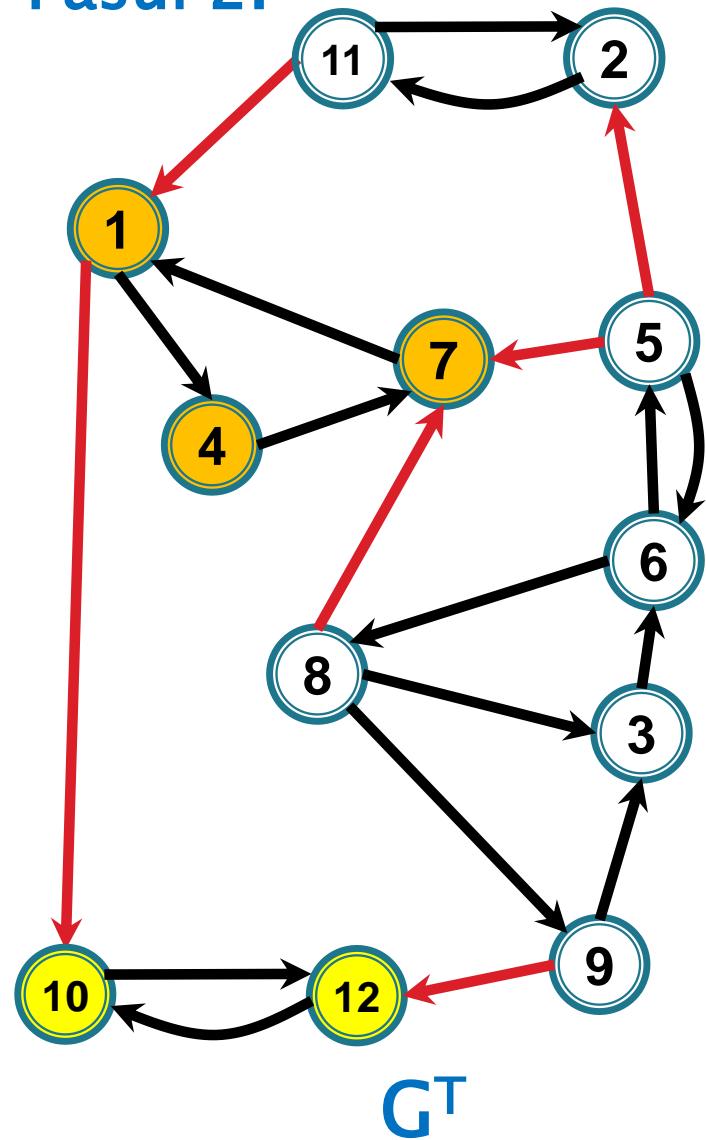
Pasul 2.



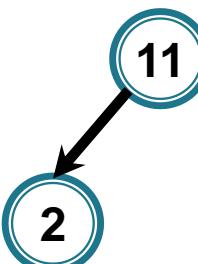
Ordinea descrescătoare finalizare: 10, 12, 1, 11, 2, 7, 5, 6, 3, 9, 8, 4

Algoritmul lui Kosaraju

Pasul 2.



DFS(11)

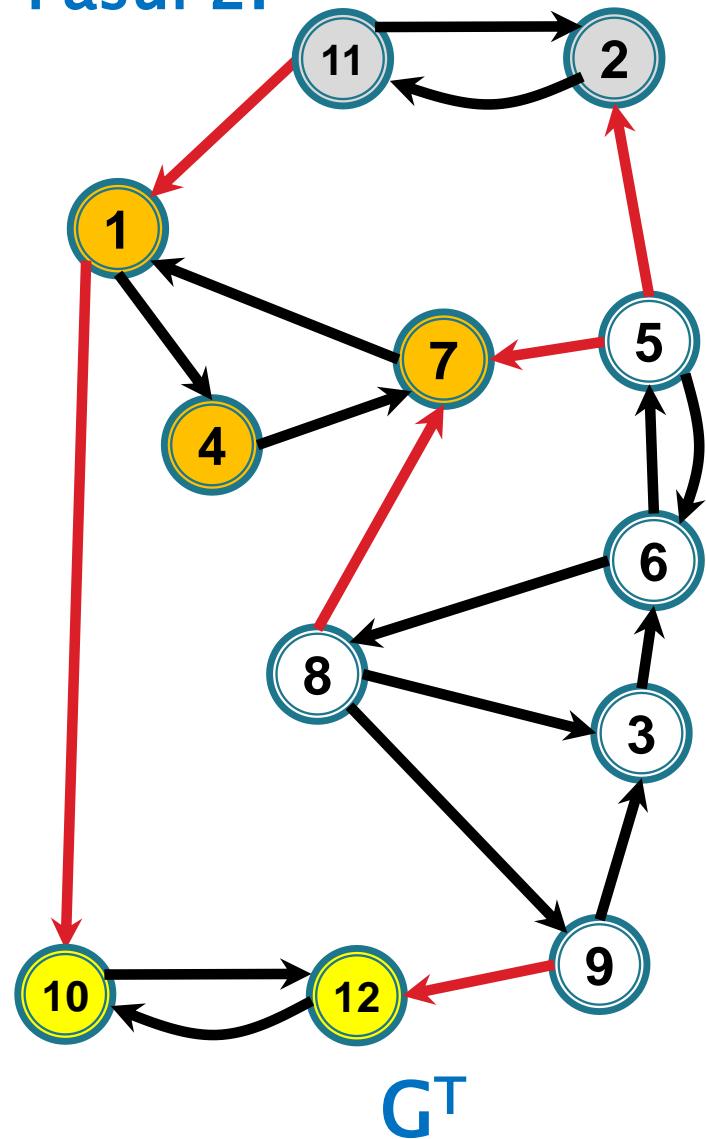


Componenta tare conexă: 11, 2

Ordinea descrescătoare finalizare: 10, 12, 1, 11, 2, 7, 5, 6, 3, 9, 8, 4

Algoritmul lui Kosaraju

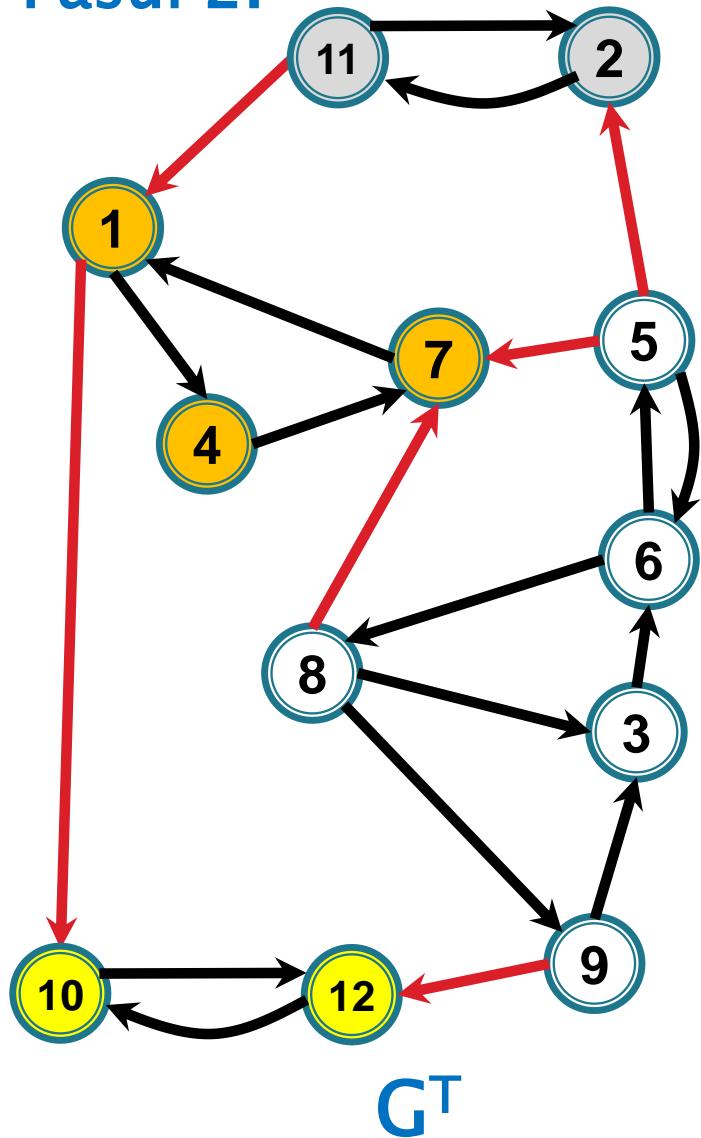
Pasul 2.



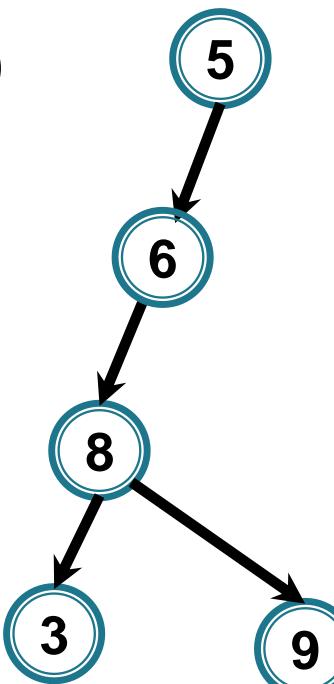
Ordinea descrescătoare finalizare: 10, 12, 1, 11, 2, 7, 5, 6, 3, 9, 8, 4

Algoritmul lui Kosaraju

Pasul 2.



DFS(5)

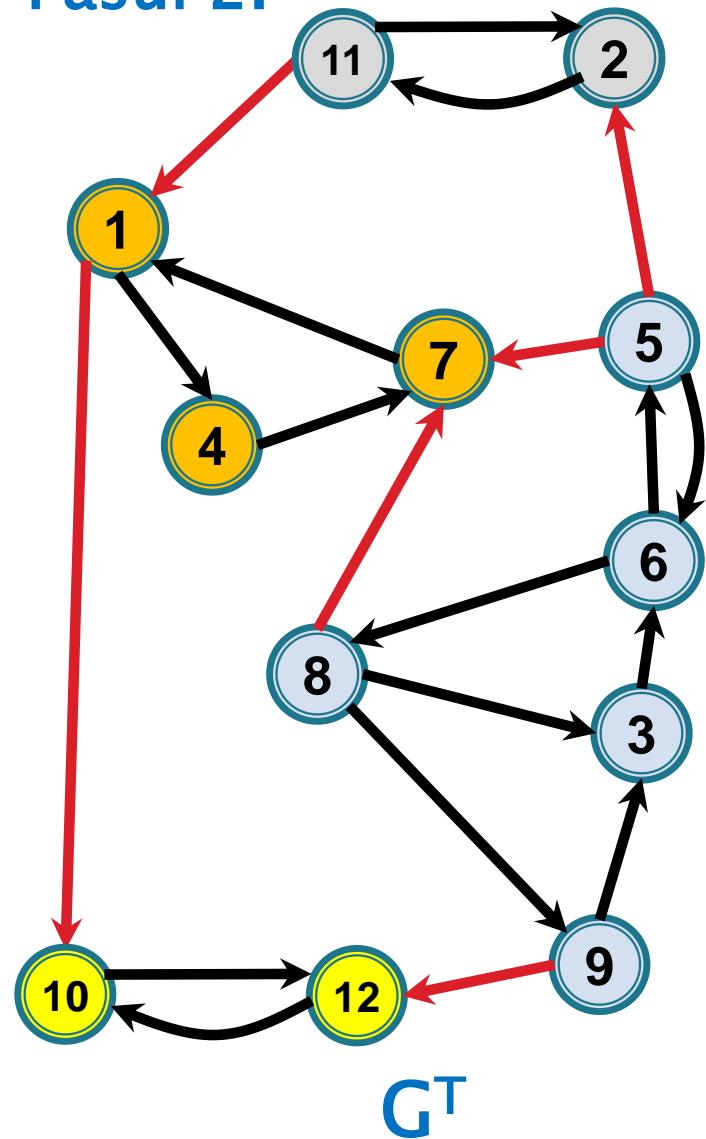


Componenta tare conexă: 5, 6, 8, 3, 9

Ordinea descrescătoare finalizare: 10, 12, 1, 11, 2, 7, 5, 6, 3, 9, 8, 4

Algoritmul lui Kosaraju

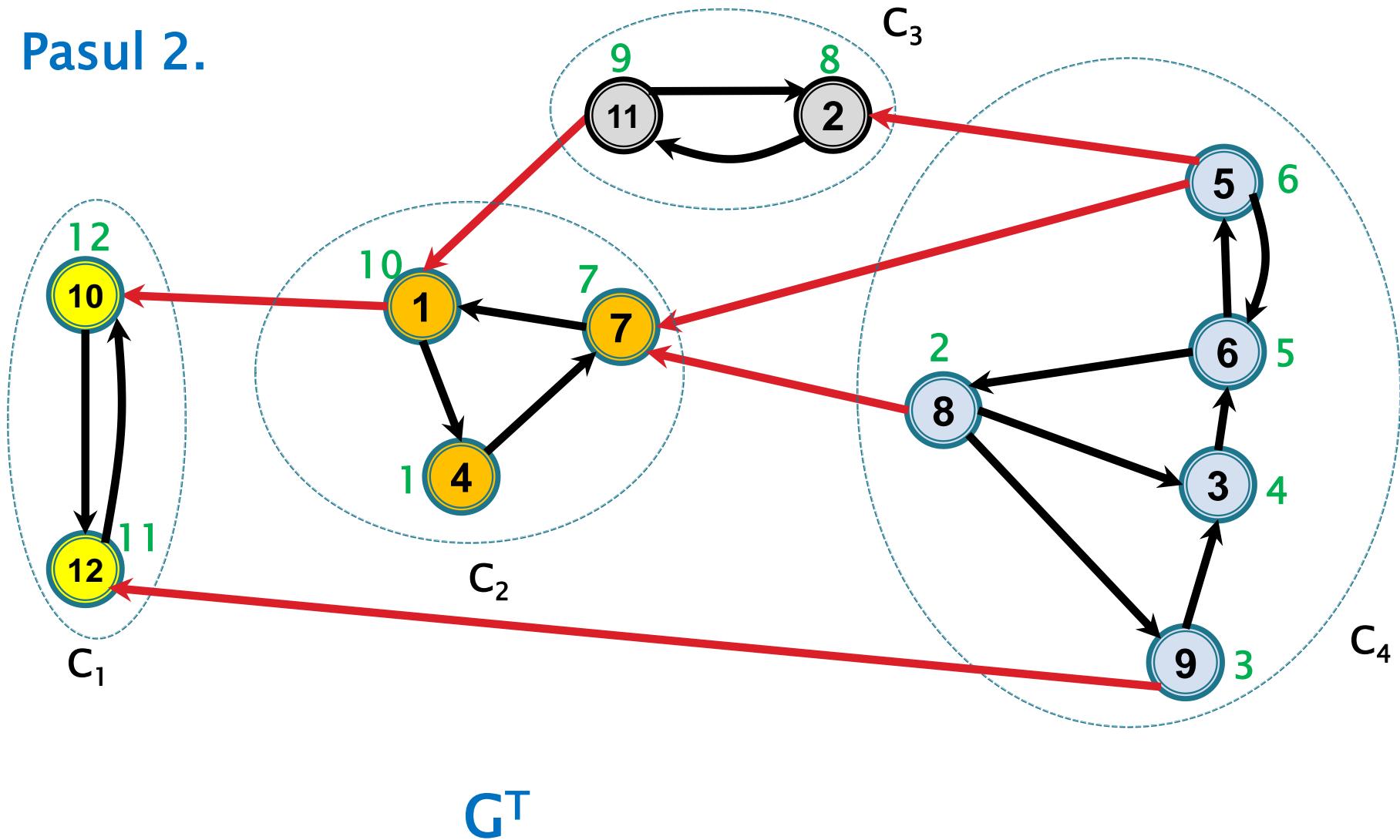
Pasul 2.



Componenta tare conexă: 5, 6, 8, 3, 9

Ordinea descrescătoare finalizare: 10, 12, 1, 11, 2, 7, 5, 6, 3, 9, 8, 4

Pasul 2.



G^T

