# NE585 – Nuclear fuel cycle analysis Project 3 – Front end of the nuclear fuel cycle

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### **Preface**

Refer to these references to start for aqueous reprocessing –

- (1) Countercurrent equilibrium extraction
- (2) Nuclear fuel reprocessing
- (3) Principles of stagewise separation process calculations
- (4) Liquid-liquid extraction example problem I
- (5) Liquid-liquid extraction example problem II

Use standard assumptions -

- Constant distribution coefficient
- Complete mixing
- Fresh solvent

Required for full credit – In problems 3 - 8, please address how the solution will affect the engineering design of a commercial scale PUREX facility.

# 1 Volume flow

**(10)** 

Derive an expression for  $\frac{F}{P}$  and  $\frac{W}{P}$  explicitly in terms of  $x_F,\ x_P,\ x_W.$ 

## 2 SWU

### **(10)**

Plot  $\frac{SWU}{/}P$  as a function of  $x_P$ . There is an interesting implication(s) of this curve, which we talked about, in terms of the JPCOA. What is it? Note that medical isotopes require  $x_P = 0.20$ .

## 3 Extract concentration

**(20)** 

Prove that the extract concentration  $(y_N)$  can be expressed as -

$$y_N = \frac{\beta^N - 1}{\beta - 1} (Dx_1 - y_0) + y_0.$$

# 4 Material balance

#### **(20)**

Now eliminate  $x_1$  by applying an 'overall material balance' to the above expression; i.e., a material balance on stage 1 and stage N.

# **5** Extraction factor

### **(20)**

Finally, using the definition of fractional recovery of the extractable component  $(\rho)$  and extraction factor  $(\beta)$ , into the result from (4) above, and eliminate  $y_N$ .

# 6 Decontamination factor

**(20)** 

Derive the contamination factor  $(f_{AB})$  based on the result in (5) for both  $y_0 = 0$  and  $y_0 \neq 0$ . What does the decontamination factor actually mean? How does the efficiency compare if  $y_0 = 0$  or  $y_0 \neq 0$ ?

## 7 Maximum decontamination factor

#### **(25)**

- (a) Consider a multistage extraction system with two extractable components. What is the theoretical maximum for the decontamination factor?
- (b) If the extraction factor for U is 5 and for Tc is 0.01. What is the decontamination factor? What does it physically mean?

## 8 Extraction limit

#### **(25)**

Show *with math* that for an extraction factor less than unity, complete extraction is impossible, even if an infinite number of stages is available. When (or would) there be a case where the extraction factor would be less than unity?

# 9 Uranium tails

**(50)** 

How are uranium tails managed? Critically discuss this issue.

# 10 Enrichment

### **(50)**

What would be the speed and radius of a gas centrifuge that would make it equivalent to gas diffusion? What are the dimensions of the gas centrifuge? Which is better?

### 11 Cost analysis

(50)

Taking the cost equation, what is the driver or limited factor for cost? What needs to happen for a plant to be profitable? What challenges are there? Feel free to make graph(s).

$$c_P = [V_P - V_F - (x_P - x_F) \frac{V_F - V_W}{x_f - x_w}]c_S + (\frac{x_P - x_W}{x_F - x_w})c_F$$

 $c_P$  = enriched U price

 $c_S = SWU price$ 

 $c_F$  = natural uranium price

 $V_i = V(x_i)$ ; i.e., value function

# **Tables**

# **Figures**