

NE585 – Nuclear fuel cycle analysis  
Project 5 – Monte Carlo methods and MCNP

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## **Preface**

For problems 1 – 3 use Monte Carlo techniques to obtain the solutions.

## 1 Evaluating an integral I

(30)

Solve for  $G$  using Monte Carlo techniques. Solve the integral analytically and graph  $g(x)$ . Also plot  $G$  v  $N$  for  $N = 10, 10^2, 10^3, 10^4, 10^5, 10^6$ .

$$G = \int_0^1 g(x) dx \quad (1)$$

$$g(x) = 1 - e^{-x} \quad (2)$$

## 2 Evaluating an integral II

(30)

Do the same for the following function. This  $g(x)$  does not have an analytical solution. However, you can use another numerical solver to compare the Monte Carlo result.

$$\int_0^{\frac{\pi}{2}} \sin(x^2) dx \quad (3)$$

### 3 Approximation

(30)

Approximate  $\sqrt{2}$  in a similar manner to the way we approximated  $\pi$ .

## 4 Hot cell modeling

(50)

Conduct a short modeling study of the metal fuel alloy for the hot cell facility using -

- [4\\_ff.alloy.inp](#) (flux)
- [4d\\_ff.alloy.inp](#) (dose)

See also the related [paper on hot cell shielding](#) for more information.

Apply the following procedure –

- (a) Look at the original geometry in the plotter/VisEd.
- (b) Modify the facility to only include the SE and SW cells.
- (c) Use MCNP to compute the volume averaged (F4) flux tallies for the SE cell and SW cell.
- (d) Use a neutron emission rate of  $1.1 \times 10^7$  n/s/g for 24 grams of material.
- (e) Increase NPS from the original files to reduce standard error.
- (f) Start with a wall thickness of 15 cm using the material already included in the deck. It is a form of borated concrete that is common to these kinds of facilities. Increase the wall thickness until the dose rate falls below  $1 \mu\text{Sv}/h$  and the relative flux falls below 0.01.
- (g) Plot dose rate v wall thickness and the relative flux v wall thickness.
- (h) Justify that the results are scientifically sound.

*Is this wall thickness reasonable? As in, could a facility be practically built like this using current engineering design techniques?*

*Include the MCNP file at the end in an appendix.*

## Criticality modeling

For the criticality models, to get full credit –

- (i) Include a screenshot of the model from the VisEd/plotter.
- (ii) Use finite geometries.
- (iii) Design geometries that will minimize leakage. Show (as part of making the mcnp file and results; not calculating by hand) that leakage has been minimized.
- (iv) For criticality, try to get to 3 9s or 0s (.999x, 1.000x) for the mean, and 68% confidence. Bonus for 4 9s/0s.
- (v) Report output in a table – k, standard deviation, 68% confidence, 95% confidence, and 99% confidence.
- (vi) Justify the results are scientifically sound.
- (vii) Include the input deck in the appendix.

**PROTIP** – k can vary weird when your trying to get the critical radius to 4 or 5 decimal places. Study the KCODE parameters. You could also add more particles on KSRC, but be careful where you place them.

## 5 Critical mass I

(20)

What is the critical mass of a bare sphere of plutonium containing (1) 95.5%  $^{239}\text{Pu}$  and (2) 80%  $^{239}\text{Pu}$ , where the rest is  $^{238}\text{Pu}$ ?



## 6 Critical mass with reflector

(20)

What is the critical mass for the above, but with a thin nickel shell of 0.10 cm?

## 7 Critical mass II

(20)

What is the critical mass of pure  $^{239}\text{Pu}$  of a bare cylinder?

## Reflector modeling

For the next three problems, select 3 – 5 typical reflector materials for each fissionable source. Make a table for each source with results from the reflectors.

## 8 Critical mass I

(30)

Taking the bare sphere  $^{239}\text{Pu}$  model, what is the ‘optimal’ reflector that minimizes the *critical mass*? Pick at least one reflector material that is ‘exotic’; e.g., maybe for a reactor powering a Mars Rover style robot mining on an asteroid or a moon. Consider cost in the analysis of optimal material, generally estimate; no need to research specific costs.

## 9 Critical mass II

(30)

Do the same for  $^{235}\text{U}$ .

## 10 Critical mass III

(30)

Do the same for  $^{233}\text{U}$ .

## 11 Reflector analysis

(20)

Put all the results from the reflector problems together in a table. Which reflector material is minimal and why, neutronically speaking?

## 12 Geometry challenge

(50)

Three unreflected aluminum cylinders contain  $U(93.2)O_2F_2$  water solutions. The inside cylinder diameter and critical height measured 20.3 cm and 41.4 cm. The aluminum container had a density of  $2.71 \text{ g/cm}^3$  and was 0.15 cm thick. The three cylinders were set in an equilateral configuration with a surface separation of 0.38 cm. The solution concentration parameters were  $0.90 \text{ g}(^{235}\text{U})/\text{cm}^3$  with  $H : ^{235}\text{U} = 309$ .

- (a) It was estimated that the solution density was approximately  $1.131 \text{ g/cm}^3$  and consisted of  $0.0021345 \text{ }^{235}\text{U}$ ,  $0.00015382 \text{ }^{238}\text{U}$ ,  $0.33383 \text{ O}$ ,  $0.65930 \text{ H}$ ,  $0.0045756 \text{ F atoms/b - cm}$ .
- (b) MCNP gives  $k = 0.9991 \pm 0.0011$ . *Get within 15% for full credit.*

Reproduce the model to get the result. See the [MCNP benchmark document](#) for guidance.



## 13 Critical mass IV

(20)

Find the critical mass for a bare cylinder of 10.9% enriched U with a density of 18.63 g/cc.

## 14 Critical mass V

(20)

Find the minimum critical mass for an infinite graphite reflected 93.5% enriched U sphere. Use 18.8 g/cc for the U density and just use carbon for the graphite.

## 15 Critical mass VI

(20)

Find the critical mass of 97.67% enriched U cube in an infinite water reflector. Use a density of 18.794 g/cc.

## Tables

## Figures

## **Appendix I: Hot cell MCNP input decks**

## **Appendix II: Criticality MCNP input decks**