

DeFi

Decentralized Finance

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## TradFi (Traditional Finance)

**vs.**

## DeFi (Decentralized Finance)

- Centralized
- Many intermediaries  
(brokers, market makers, clearing houses, exchanges)
- More or less transparency  
(depends on regulations and oversight)
- KYC (Know Your Customer)

- Decentralized
- No intermediaries  
(from wallet to smart contract exchanges directly)
- Fully transparent  
(data and code written in clear on the blockchain)
- Permissionless

# Bridging DeFi and TradFi

Two operations bridge the gap between DeFi and TradFi

- **On-Ramp**  
Purchasing cryptocurrency with actual FIAT\* currency
- **Off-Ramp**  
Selling cryptocurrency to get actual FIAT\* currency

\* FIAT is government-issued currency like CAD, USD, EURO

# DeFi Summary

- Decentralized Exchanges (a.k.a Automated Market Makers)
- DeFi Staking
- Price Discovery Through Arbitrage
- Borrowing and Lending
- Flash Loans
- Stablecoins
- Yield Farming

# Decentralized Exchanges

a.k.a Automated Market Makers



# [Recap] ERC-20 Tokens

A fungible token is a smart contract that maintains all user balances

```
mapping(address => uint256) balances
```

ERC-20 is a standard API for fungible tokens

```
function transfer(address to, uint256 value) returns (bool)
```

```
function transferFrom(address from, address to, uint256 value) returns (bool)
```

```
function approve(address spender, uint256 value) returns (bool)
```

```
function totalSupply() view returns (uint256)
```

```
function balanceOf(address owner) view returns (uint256)
```

```
function allowance(address owner, address spender) view returns (uint256)
```

# Concept of Exchange (a.k.a market maker)

**An exchange** converts one currency to another given an exchange rate

How is the exchange rate defined ?

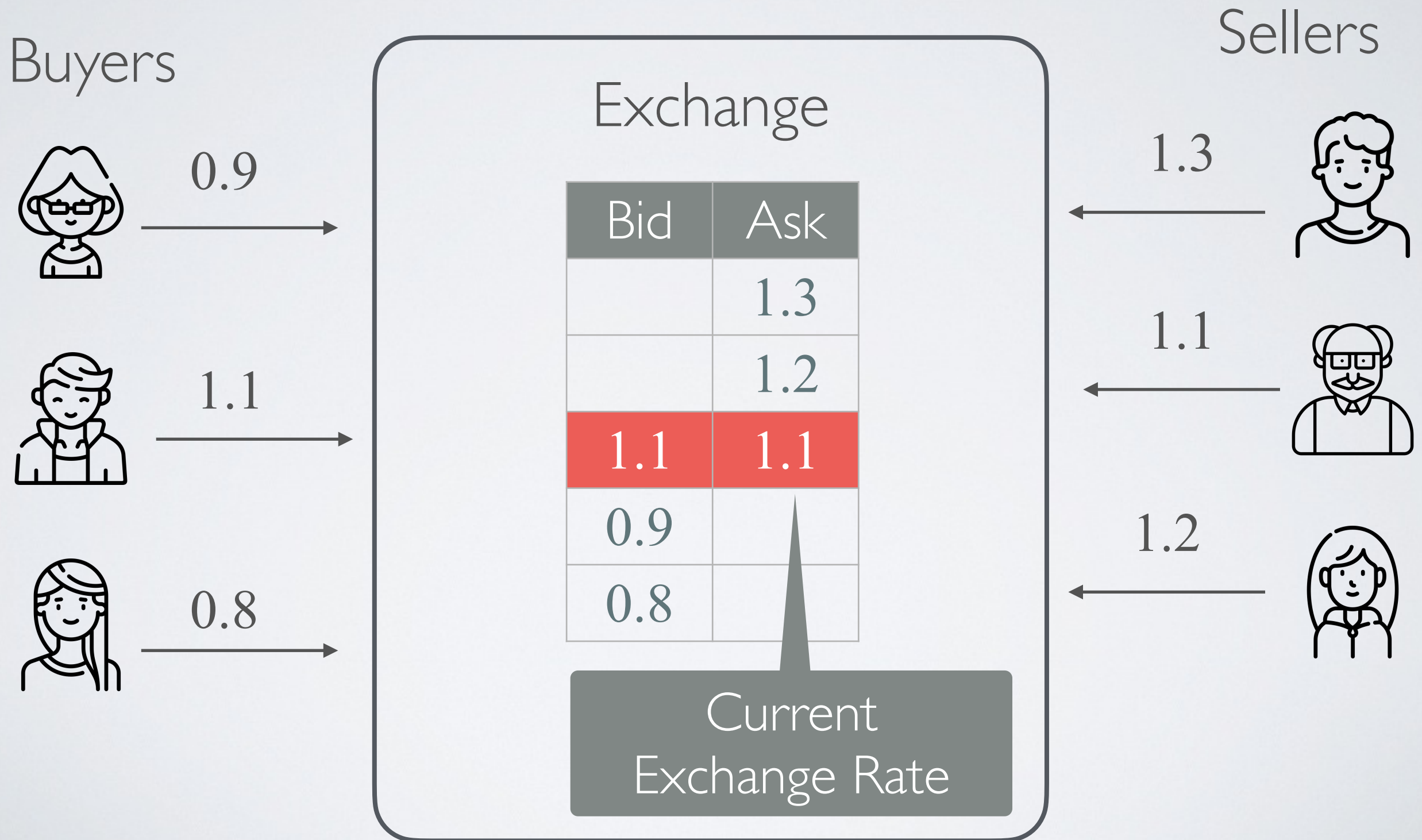
- It can be set arbitrary (unfair market)
- It can be calculated dynamically based on supply/demand (fair market)

But how to calculate an exchange rate dynamically?

- some people wants to sell token  $T_A$  to buy  $T_B$
  - other people wants to sell token  $T_B$  to buy  $T_A$
- ➡ an exchange connects buyers and sellers together

✓ The exchange rate is the result of this dynamic process

# Order Book-based approach (commonly used in TradFi)





# CEX - Centralized Exchange

Can you create a platform that implements an automated order book-based exchange?

➡ Yes, build a platform with :

- a backend to collect user orders
- a wallet to collect money (escrow transaction)

⦿ Limitation : centralized approach!

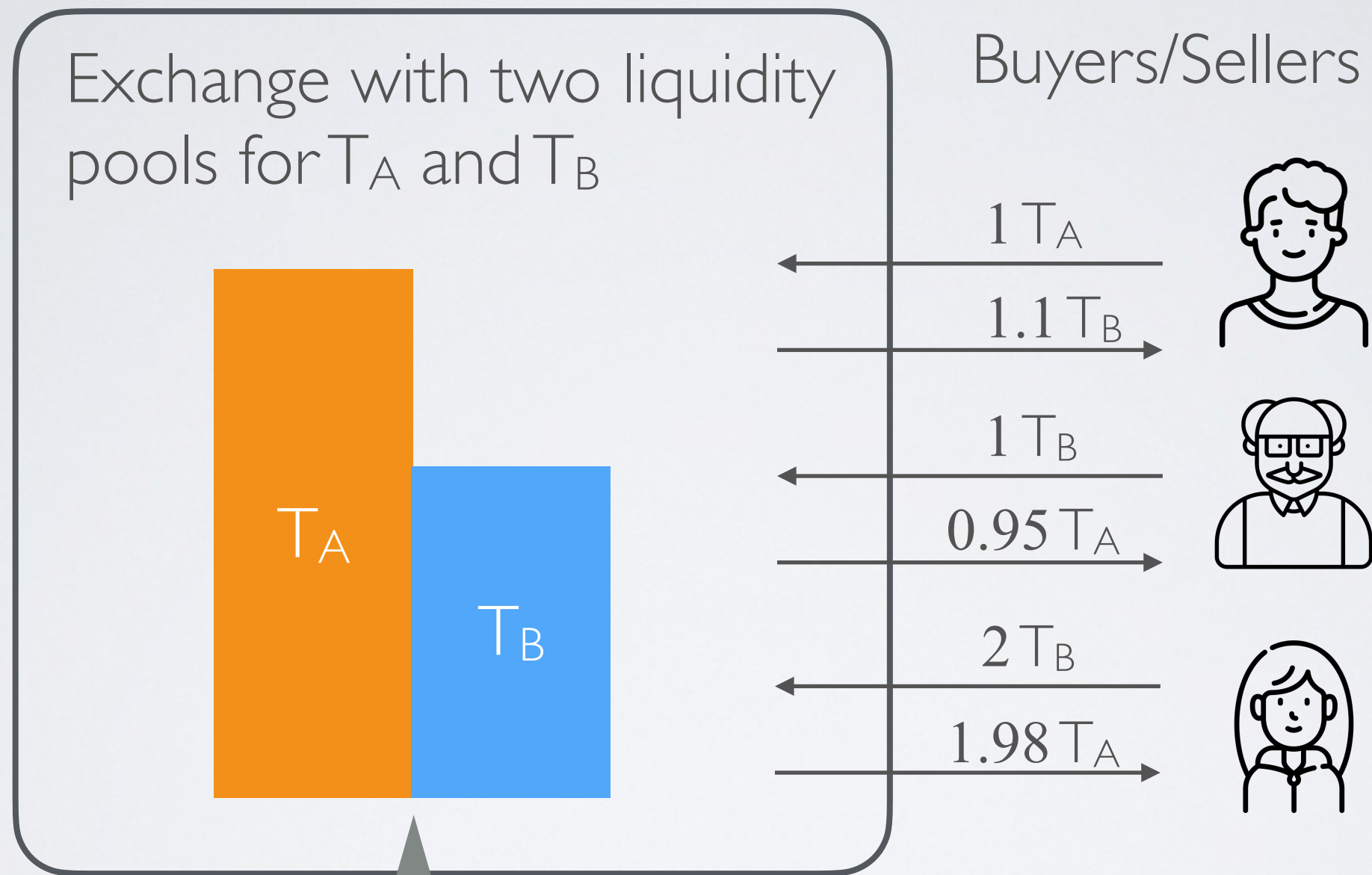
Users must trust the backend to do the right thing and to be always available

# Decentralized version of an order book-based exchange

Can you write a smart contract that implements an automated order book-based exchange?

- ➔ Technically yes but **no in practice** because of gas
- Matching (i.e ordering) buy/sell orders is expensive
  - Placing, withdrawing and fulfilling orders is expensive

# A Better Approach : Liquidity Pools



Current Exchange Rate is calculated based on the pool levels

# Dynamic pricing using the Constant Product Market Maker

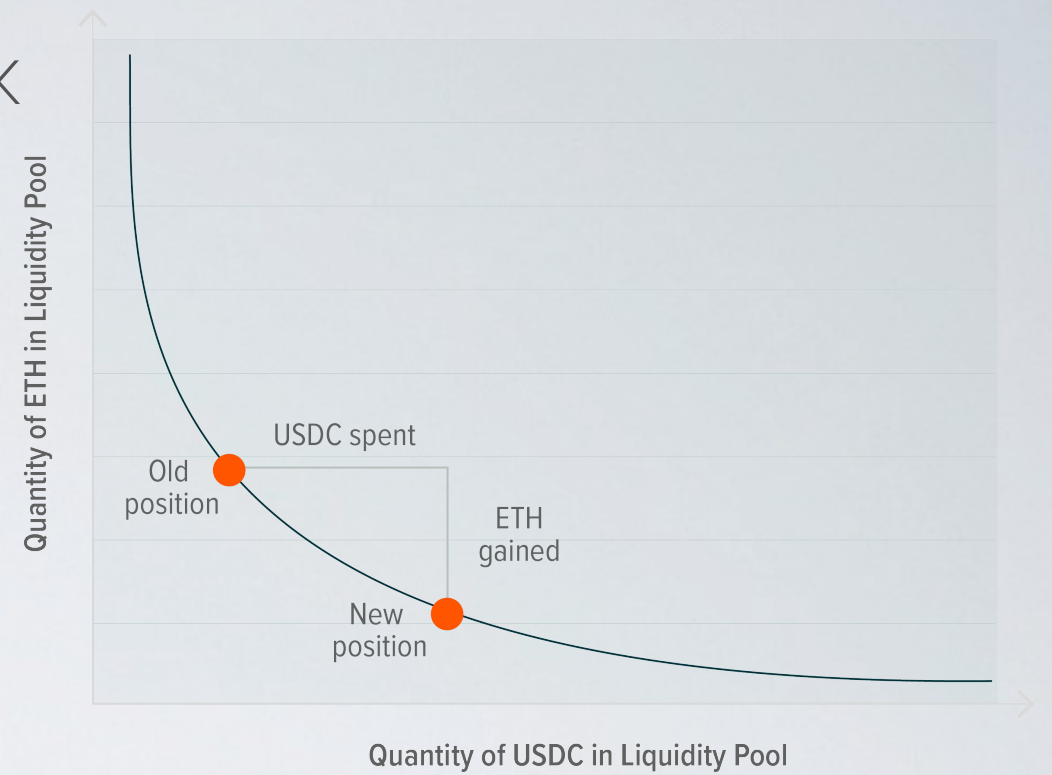
The Constant Product Market Maker is about maintaining a value  $k$  constant between two liquidity pools

$$k = \text{vol}(T_A) \times \text{vol}(T_B)$$

- ➔ Using this constant, we can calculate swap values  
i.e what quantity of  $T_B$  must be withdrawn when adding adding  
a given quantity of  $T_A$  to keep  $k$  constant (and vice versa)
- ✓ This determines the exchange rate



# Calculating the exchange rate



- Swapping **a** amount of  $T_A$  for **b** amount of  $T_B$

$$\text{Since } \text{vol}(T_A) \times \text{vol}(T_B) = (\text{vol}(T_A) + a) \times (\text{vol}(T_B) - b)$$

$$\text{Then } b = (a \times \text{vol}(T_B)) / (a + \text{vol}(T_A))$$

- Swapping **b** amount of  $T_B$  for **a** amount of  $T_A$

$$\text{Since } \text{vol}(T_A) \times \text{vol}(T_B) = (\text{vol}(T_A) - a) \times (\text{vol}(T_B) + b)$$

$$\text{Then } a = (b \times \text{vol}(T_A)) / (b + \text{vol}(T_B))$$

A liquidity pool cannot be emptied

# Example of exchange rate evolution

Swap Order	Out	Rate ( $T_B/T_A$ )	vol( $T_A$ )	vol( $T_B$ )	k
			12	10	120
$4T_A$	$2.5T_B$	0.625	16	7.5	120
$4T_A$	$1.5T_B$	0.375	20	6	120
$4T_B$	$8T_A$	0.5	12	10	120
$2T_B$	$2T_A$	1	10	12	120
$6T_A$	$4.5T_B$	0.75	16	7.5	120

# Side Effects of the Dynamic Pricing

When a user submits an exchange transaction, the actual exchange may varies depending on other transactions executed before

- ➡ Slippage (common to TradFi and DeFi)  
Difference between the exchange rate when quoted and the actual one when executed
- ✓ Most DEXes implement a slippage protection mechanism that allow users to specify a slippage tolerance limit
- ➡ Sandwich Attack a.k.a front-running attack (specific to DeFi)  
An attacker can monitor transactions in the mempool and emit concurrent transactions that will take advantage of dynamic exchange rate
- ✓ Some DEXes implement swap protection mechanism (e.g *Uniswap v4*)

# Slippage Example

## Beforehand

- When Alice wants to do a swap, the pool contains  $12 T_A$  and  $10 T_B$
- So she gets quoted that swapping  $4 T_A$  will get her  $2.5 T_B$  (0.62 exchange rate)
- She submits the swap transaction to the mempool **allowing 20% slippage**

## Scenario #1

- Bob submits a swap request for **1  $T_A$**  at the same time (i.e within the same block)
  - However, Bob's transaction is executed before Alice's changing the levels of liquidity pools and moving the current exchange rate down
  - When Alice's request is executed, she actually gets  $2.17 T_B$  (0.54 exchange rate)
- ✓ The slippage is 15% ( $0.62 / 0.54 \sim 1.15$ ) and the swap is executed

## Scenario #2

- Bob submits a swap request for **2  $T_A$**  at the same time (i.e within the same block)
  - When Alice's request is executed, she actually gets  $1.90 T_B$  (0.48 exchange rate)
- ⦿ The slippage is 30% ( $0.62 / 0.48 = 1.30$ ) and the swap is not executed



# Sandwich Attack Example

- Alice submits a transaction to the mempool to swap  $4 T_A$  with a 20% slippage
  - Mallory monitors the mempool and **sees Alice's transaction**
  - Mallory immediately submits two transactions :
    1. swap  $1.2 T_A$  **(high tip)**
    2. swap  $0.9 T_B$  (low tip)
  - Transactions are executed as follows:
    1. Mallory's transaction (high priority) **swaps  $1.2 T_A$  into  $0.9 T_B$**
    2. Alice's transaction (medium priority) swaps  $4 T_A$  into  $2.12 T_B$  (which is just within the 20% slippage limit)
    3. Mallory's transaction (low priority) swaps  $0.9 T_B$  **into  $1.98 T_A$**
- ➡ Mallory **pockets  $0.78 T_A$**  (risk free) with two simple transactions

# Simple DEX Example

```
95
96 function swap(address _fromToken, uint256 _amountIn) external returns (uint256 amountOut) {
97     require(_amountIn > 0, "Amount must be greater than zero");
98     require(_fromToken == address(token1) || _fromToken == address(token2), "Invalid token");
99
100     bool isToken1 = _fromToken == address(token1);
101     IERC20 from = isToken1 ? token1 : token2;
102     IERC20 to = isToken1 ? token2 : token1;
103     uint256 reserveIn = isToken1 ? reserve1 : reserve2;
104     uint256 reserveOut = isToken1 ? reserve2 : reserve1;
105
106     // deduct the fee from in
107     uint256 amountMinusFee = (_amountIn * (FEE_DIVISOR - FEE_PERCENT)) / FEE_DIVISOR;
108
109     // calculate the amount of token to swap out
110     amountOut = (amountMinusFee * reserveOut) / (reserveIn + amountMinusFee);
111
112     // update the reserves
113     if (isToken1) {
114         reserve1 += _amountIn;
115         reserve2 -= amountOut;
116     } else {
117         reserve2 += _amountIn;
118         reserve1 -= amountOut;
119     }
120     // transfer the tokens from user to contract
121     require(from.transferFrom(msg.sender, address(this), _amountIn), "Swap transfer in failed");
122     // transfer the tokens from contract to user
123     require(to.transfer(msg.sender, amountOut), "Swap transfer out failed");
124 }
```

Deduct the fees

Calculate the swap

Update the pools

Transfer the tokens

# DEX Staking



# Incentive for Liquidity Pool Providers

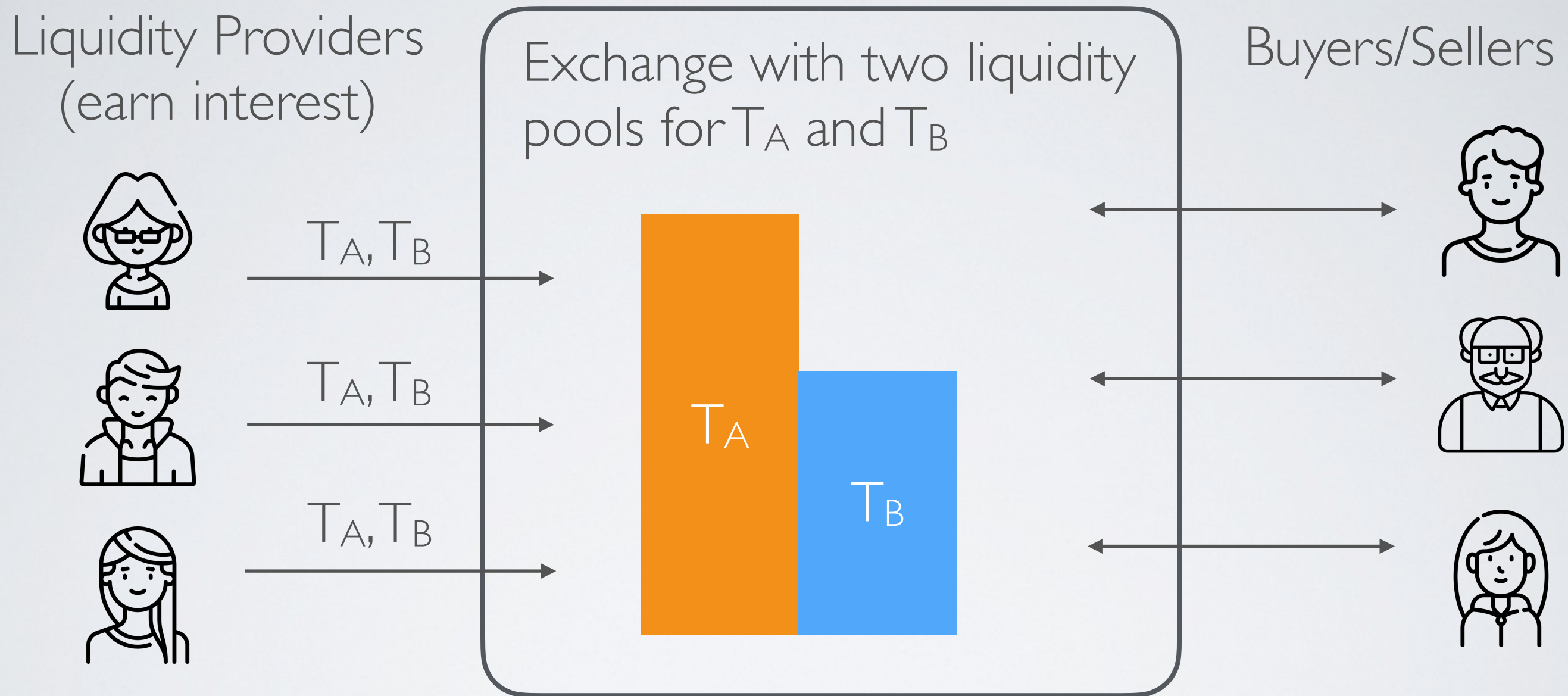
To be efficient, liquidity pools must stash large volumes of cryptocurrencies to absorb a great quantity of possibly unbalanced transactions

So what is the incentive to stake into DEX liquidity pools?

- ➡ Have a fee for every swap transaction and reward liquidity pool providers (0.30% on *Uniswap* for instance)
- This is "DEX Staking"  
(not be confused with "Consensus Layer Staking" in PoS)



# Liquidity Providers



- ➔ The liquidity providers provide both  $T_A$  and  $T_B$  and are rewarded from fees collected on every swap

# Liquidity Token

Liquidity providers must **add or withdraw  $T_A$  and  $T_B$**  from/to the pools **while preserving the ratio** (i.e the exchange rate)

➔ Have a token  $T_L$  that represents the contribution to the liquidity pools

✓ **addingLiquidity** mints  $T_L$  tokens representing the amount of tokens  $T_A$  and  $T_B$  deposited by the user to the pools

✓ **removeLiquidity** burns  $T_L$  tokens allowing the user to withdraws the corresponding amount of tokens  $T_A$  and  $T_B$  (plus interest generated from fees collected during staking period)

# Example

Call	Returns	vol( $T_A$ )	vol( $T_B$ )	real( $T_A$ )	real( $T_B$ )
addLiq(12, 10)	14,400 $T_L$	12	10	12	10
addLiq(6, 5)	7,200 $T_L$	18	15	18	15
swap(2.06 $T_A$ )	1.5 $T_B$	20	13.5	20.06	13.5
swap(4.635 $T_B$ )	5 $T_A$	15	18	15.06	18.135
rmLiq(7,200 $T_L$ )	5.02 $T_A$ 6.045 $T_B$	10	12	10.04	12.09



```

40 function addLiquidity(uint256 amount1, uint256 amount2) external {
41     require(amount1 > 0 && amount2 > 0, "Amounts must be greater than zero");
42
43     uint256 correctAmount2;
44     uint256 liquidityMinted;
45     // check if the reserves are empty
46     if (reserve1 == 0 && reserve2 == 0) {
47         // if empty, the amount of token 1 and 2 set pool ratio (a.k.a the exchange rate)
48         correctAmount2 = amount2;
49         // and the amount of lpToken to mint is (amount1* amount2)^2
50         liquidityMinted = amount1 * amount2 * amount1 * amount2;
51     } else {
52         // calculate the right amount of token2 to add to preserve the liquidity pool ratio
53         correctAmount2 = (amount1 * reserve2) / reserve1;
54         require(amount2 >= correctAmount2, "Insufficient token2 amount provided");
55         amount2 = correctAmount2;
56         // calculate the amount of lpToken to mint
57         liquidityMinted = amount1 * lpToken.totalSupply() / reserve1;
58     }
59
60     uint256 amount1ToPay = amount1;
61     uint256 amount2ToPay = correctAmount2;
62
63     uint256 token1Reward;
64     uint256 token2Reward;
65     (token1Reward, token2Reward) = calculateReward(msg.sender);
66     amount1ToPay -= token1Reward;
67     amount2ToPay -= token2Reward;
68
69     // mint the lpToken
70     lpToken.mint(msg.sender, liquidityMinted);
71     isStaking[msg.sender] = true;
72
73     // update rewardPerTokenPaid
74     rewardPerToken1Paid[msg.sender] = rewardPerToken1;
75     rewardPerToken2Paid[msg.sender] = rewardPerToken2;
76
77     // update the reserves
78     reserve1 += amount1;
79     reserve2 += correctAmount2;
80
81     // transfer the funds from user to contract
82     require(token1.transferFrom(msg.sender, address(this), amount1ToPay), "Token1 transfer failed");
83     require(token2.transferFrom(msg.sender, address(this), amount2ToPay), "Token2 transfer failed");
84 }
85

```



```

86
87 function removeLiquidity(uint256 lpAmount) external {
88     require(lpAmount > 0, "Invalid LP token amount");
89     require(lpToken.balanceOf(msg.sender) >= lpAmount, "Insufficient LP balance");
90
91     // calculate the amounts of token1 and token 2
92     uint256 totalSupply = lpToken.totalSupply();
93     uint256 amount1 = (lpAmount * reserve1) / totalSupply;
94     uint256 amount2 = (lpAmount * reserve2) / totalSupply;
95
96     uint256 token1Reward;
97     uint256 token2Reward;
98     (token1Reward, token2Reward) = calculateReward(msg.sender);
99
100    // update rewardPerTokenPaid
101    rewardPerToken1Paid[msg.sender] = rewardPerToken1;
102    rewardPerToken2Paid[msg.sender] = rewardPerToken2;
103
104    // update the reserves
105    reserve1 -= amount1;
106    reserve2 -= amount2;
107
108    // burn the lpTokens
109    lpToken.burn(msg.sender, lpAmount);
110    isStaking[msg.sender] = (lpToken.balanceOf(msg.sender) > 0);
111
112    // transfer the funds from contract to user
113    require(token1.transfer(msg.sender, amount1 + token1Reward), "Token1 transfer failed");
114    require(token2.transfer(msg.sender, amount2 + token2Reward), "Token2 transfer failed");
115 }

```

# The risk Behind Staking a.k.a Impermanent Loss

When liquidity provider deposits  $10 T_A$  and  $5 T_B$ , the exchange rate is 2

➔ So the amount deposited is worth  **$20 T_A$  when staking**

When the liquidity providers withdraws the whole stake for  $14 T_A$  and  $3.5 T_B$  and the exchange rate is 4

➔ This amount is worth  **$28 T_A$  after withdrawing**

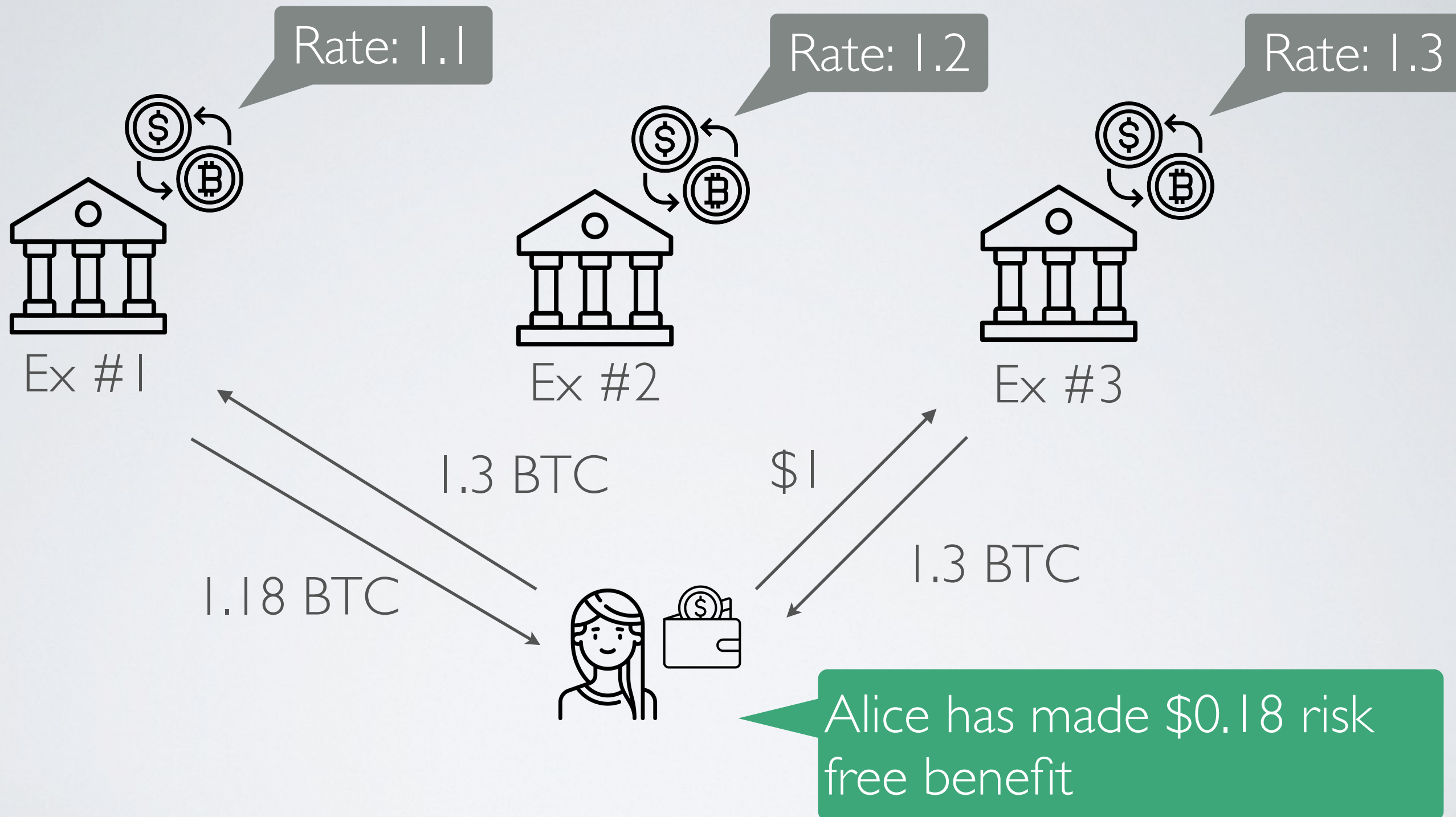
However, the **initial stake is now worth  $30 T_A$  without staking**

⦿ This is an **impermanent loss**

It is an unrealized loss until the liquidity provider withdraws its stake

# Automatic Price Discovery

# In a decentralized world



- ➔ Alice can repeat the operation over and over while there are exchanges with different rates



# The concept of Arbitrage

**Arbitrage** (common to TradFi and DeFi)

Exploiting price differences between markets

- ➔ Traders do take advantage of rate differences between exchanges to make risk-free profits

# Automatic Price Discovery resulting from Arbitrage

As traders take advantages of arbitrage, the market as a whole move to a state where no one can make these profits (also called *Nash Equilibrium*)

➡ All exchanges converge to the same rate  
a.k.a the market price

✓ This process is called **automatic price discovery**

# Borrowing and Lending

# Concept of Lending Market

**Lenders** make money available to borrow and earn interest



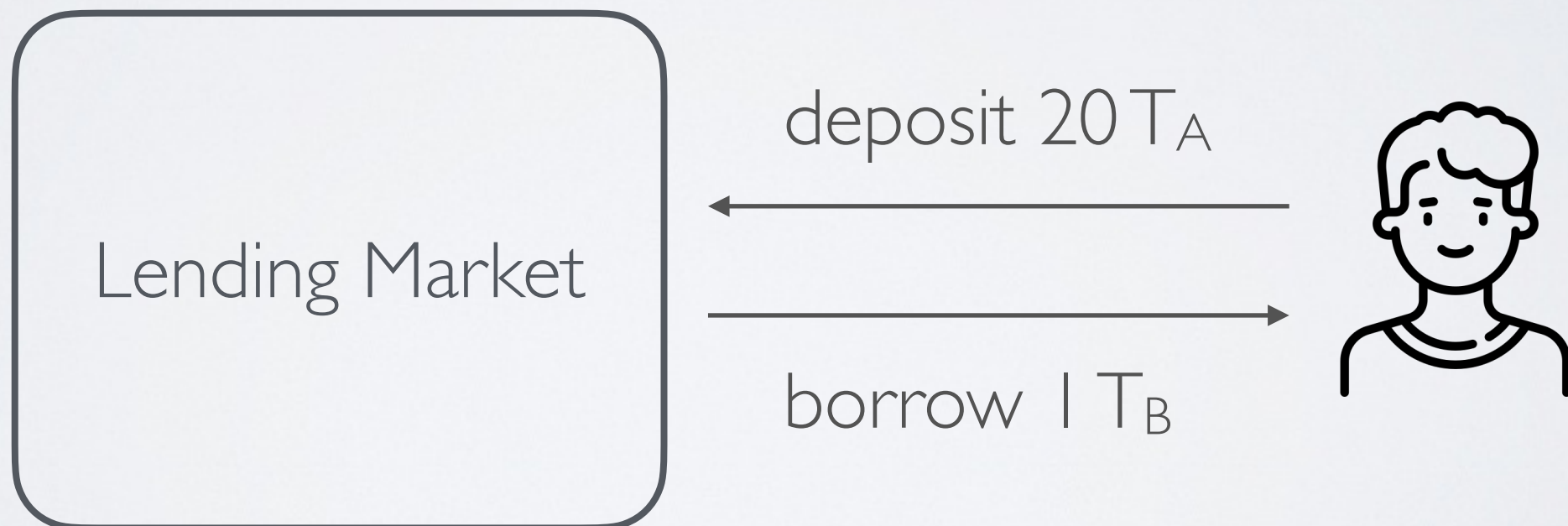
**Borrowers** can take out a loan and repay it with interest before maturity date



# The concept of collateral

What if a lender defaults on a loan?

- ➔ When taking out a loan, the lender must deposit a **collateral** i.e assets that serve as a security deposit



# Undercollateralized vs overcollateralized

## **Undercollateralized**

Borrower must provide a collateral that is less than the value of the loan

$$\text{val(collateral)} < \text{val(loan)}$$

## **Overcollateralized**

Borrower must provide a collateral that is more than the value of the loan

$$\text{val(collateral)} > \text{val(loan)}$$

- ⦿ Problem : over time the value of the loan might increase compared to the value of the collateral (because of exchange rate)
  - ➡ An undercollateralized loan might become further undercollateralized
  - ➡ An overcollateralized loan might become undercollateralized

# Collateral factor

Throughout the whole loan period, the value of collateral must not fall below a threshold called **collateral factor**

➔ i.e  $\text{val}(\text{collateral}) \times k > \text{val}(\text{loan})$  must remain true

This factor is usually

- $>1$  for undercollateralized loan
- $<1$  for overcollateralized loan

# The role of collateral

After taking a loan, two things can happen:

1. The lender repays the loan with interest
  - ➡ Collateral is returned
2. The lender defaults (i.e. does not repay before maturity date)
  - ➡ The loan is **liquidated** (i.e. repaid with collateral) with a penalty
3. Before maturity date, the value of collateral falls under
  - ➡ The loan is **liquidated** with a penalty



# CeFi vs DeFi

**CeFi** - both undercollateralized and overcollateralized lending schemes are common (enabled by laws and regulations)

- e.g mortgage (overcollateralized)
- e.g credit card (undercollateralized)

**DeFi** - only overcollateralized lending schemes are common

- e.g *Aave, Compound, Curve Finance*

# Example of Overcollateralized Loan

A borrower deposits **\$15,000 USDC** as collateral to borrow **5 ETH** (priced at \$2,000 USD each) in lending market with:

- Collateralization required: 1.5 (150%)
- Collateralization factor: 1.2 (120%)
- Penalty: 0.1 (10%)
- Interest rate: 0.05 (5%)

What can happen:

- Either the borrower repays 5.25 ETH and \$15,000 USDC are returned
- Or the borrower defaults when 1 ETH is \$2,200 USDC, \$12,100 USDC (worth 5.5 ETH) are liquidated and \$2,900 USDC are returned to the borrower
- Or ETH rises above \$2,400 ( $10,000 * 1.2 / 5$ ), \$13,200 USDC are liquidated and \$1,800 USDC are returned to the borrower

# Why overcollateralized borrowing makes sense

Why taking an overcollateralized loan when you can just exchange the collateral

➔ In a nutshell : **shorting**

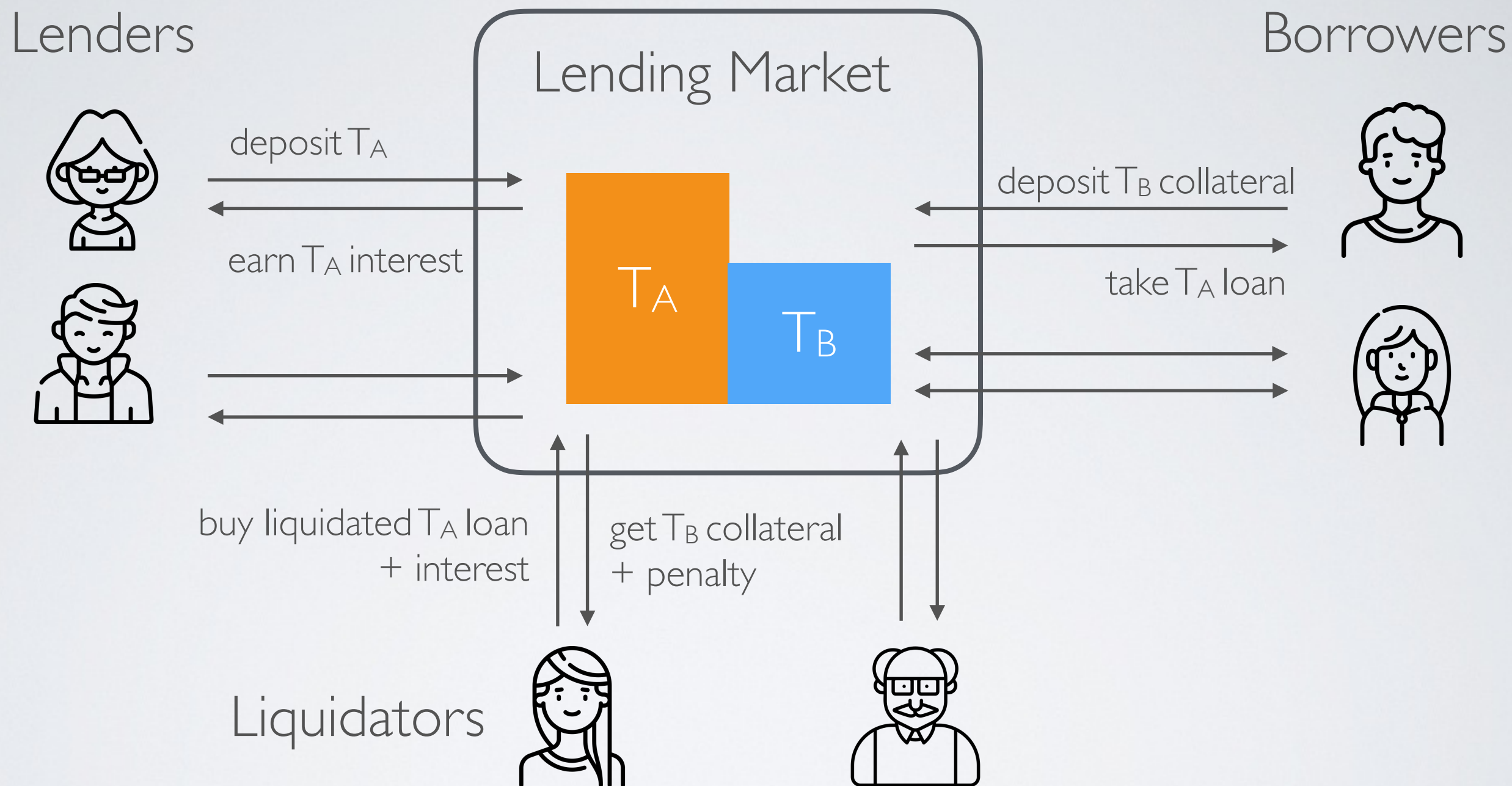
i.e betting that the value of an asset will go down

Example

1. Borrow 5 ETH (1 ETH - \$2,000) with \$15,000 collateral
2. and sell it right away to cash out \$10,000
3. Wait for ETH to decrease to \$1,500 and buy back 5.5 ETH for \$7,875
4. Repays 5.25 ETH and get the full collateral back

✓ The borrower pockets \$2,125

# Implementing a DeFi Lending Market



- ➔ The liquidators are important to make sure the  $T_A$  pool does dry up when borrowers are defaulting



# Linear Variable Interest Rate

When the **supply of  $T_A$  is low**, raise interest rate to

- decrease the demand of loans
- and increase the incentive for lenders to stake  $T_A$

➔ Have a interest rate that depends on the utilization of the  $T_A$  pool

Utilization ratio  $U = \text{totalBorrow} / \text{totalDeposit}$

Borrow rate  $R = \text{baseRate} + U$

✓ The interest rate varies on every deposit, loan and liquidation transactions

# Slopped Variable Interest Rate

Used in common DeFi Lending Markets such as AAVE and Compound

Same idea but the goal is to reach an optimal pool utilization (usually 80% by empirical model)

- ➔ The model takes into account how fast the interest rate should varies (a.k.a **slope**) to reach the optimal utilization rate
- **Slope1** defines how the borrow rate increases as utilization rises up to the optimal utilization rate (to incentivize borrowing)
  - **Slope2** Defines how sharply the borrow rate increases after the optimal utilization point (to penalize borrowing)

$$\text{Borrow Rate} = \begin{cases} \text{Base Rate} + U \times \text{Slope}_1, & \text{if } U \leq U_{opt} \\ \text{Base Rate} + \text{Slope}_1 + \frac{U - U_{opt}}{1 - U_{opt}} \times \text{Slope}_2, & \text{if } U > U_{opt} \end{cases}$$