

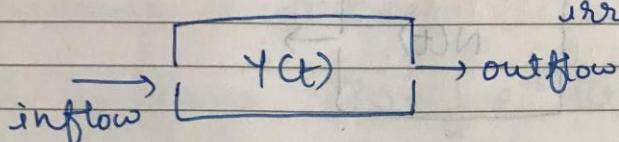
6/1/2020 Modelling & Simulation

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Compartment models

- Systems evolve with time.
- System as a compartment

Treat system as whole
irrespective of inner particles



- Interested in change of quantity wrt time

$$\text{Rate of change} = \text{Rate of inflow} - \text{Rate of outflow}$$

$$\text{Avg. change} \frac{y(t+\Delta t) - y(t)}{\Delta t}$$

$$\lim_{\Delta t \rightarrow 0} \frac{y(t+\Delta t) - y(t)}{\Delta t} = \frac{dy}{dt}$$

(i) growth (ii) decay (iii) no change

- In order to model a system by differential equation look if the system can be represented as compartments.
- Differential equations are mostly Balance equation. (e.g. $\frac{\partial f}{\partial t} = -\nabla \cdot J$)

Radioactive Decay
population of species
pollutants in water bodies
Drug delivery / dosage

} we can think in terms of compartments

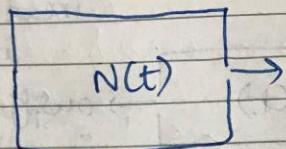
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We just consider change with time
not space.

* Things are homogeneously mixed

- (i) No. is large (no. of examples)
- (ii) Independent

Compartment (Don't look any individually)



$$\rightarrow N(t + \Delta t) - N(t)$$

- (i) Diff is negative as loss is happening
- (ii) What is loss?

$$\frac{dN}{dt} = -kN$$

Assume: \downarrow is linear & \propto # present

$$\therefore N(t + \Delta t) - N(t) = -kN(t)$$

(for 1 time unit)

$$\therefore N(t + \Delta t) - N(t) = -kN(t) \Delta t$$

(for Δt time unit)

$$(i) N(t + \Delta t) = (1 - k\Delta t)N(t)$$

$$\text{Let } \Delta t = 1,$$

$$N(t+1) = (1 - k)N(t)$$

$$\frac{N(t+1)}{N(t=0)} = (1-k)^t$$

(i) $\frac{dN}{dt} = -kN$

-A $\frac{N(t)}{N(t=0)} = e^{-kt}$

H ** No model is correct **

Laplace Transforme $f(s) = \int_0^\infty e^{-st} f(t) dt$

$\mathcal{L}\left[\frac{dy}{dt}\right] = \int_0^\infty e^{-st} \frac{dy}{dt} dt$

$\frac{d}{dt}(e^{-st} y) = -se^{-st} y + e^{-st} \frac{dy}{dt}$

i $\mathcal{L}\left[\frac{dy}{dt}\right] = s \tilde{y} - y(0)$

ii $\mathcal{L}\left[\frac{d^2y}{dt^2}\right] = s \mathcal{L}\left[\frac{dy}{dt}\right] - y'(0)$

iii $= s^2 \tilde{y} - y(0) - y'(0)$

Eg. $\frac{dy}{dt} = ay + by \Rightarrow s\tilde{y} - y(0) = \frac{a}{s} + b\tilde{y}$

∴ $(s-b)\tilde{y} = y(0) + \frac{a}{s}$

∴ $\tilde{y} = \frac{y(0)}{s-b} + \frac{a}{s(s-b)}$

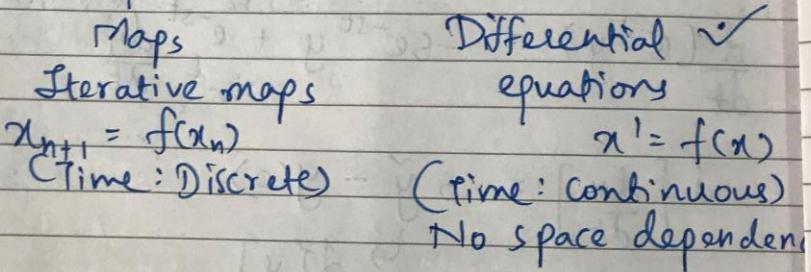
$$y(t) = y(0) e^{bt} + \frac{a}{b} [e^{bt} - 1]$$

(Laplace Transformations)

- (i) Partial fractions
- (ii) Roles & residues
- (iii) Convolution

~~7/01/2020~~ NLS (9-10)

Dynamical systems



Differential equations:

→ Dimension: order of derivative

$$m \frac{d^2x}{dt^2} + b \frac{dx}{dt} + kx = 0$$

$$\frac{dx}{dt} = v$$

$$\frac{dv}{dt} = -\frac{b}{m}v - \frac{k}{m}x$$

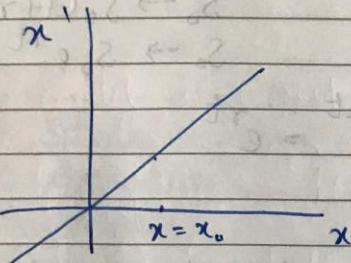
} Though 'y' not present but two dimension

→ Explicit dependence on time: Consider time as a s var. Dimension ↑

$$\rightarrow x' = \alpha x$$

$$\therefore \frac{dx}{dt} = \alpha x$$

Given $\alpha \neq 0$ & x_0 , determine $x(t)$.



$$f(x) > 0$$

$$\frac{dx}{dt} > 0$$

$x \uparrow$

$f(x) = 0$ ($x' = 0$) \rightarrow do not move

fixed points

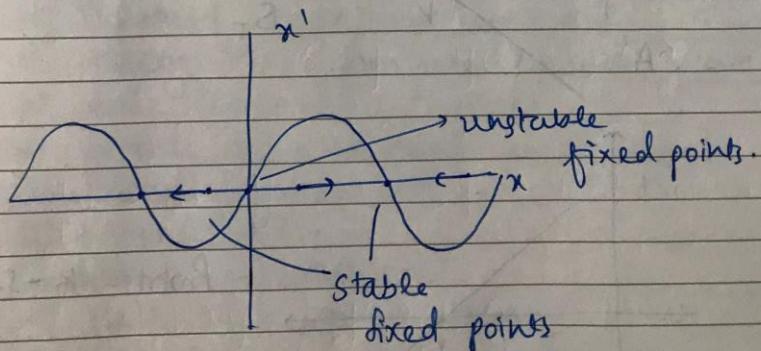
Stable (any change results to fixed point)

Unstable

(any change results to divergence from fixed point)

$$\textcircled{1} \quad \frac{dx}{dt} = x' = \sin x$$

$$t_{\text{max}} = \ln \left(\frac{\csc x_0 + \cot x_0}{\csc x_0 - \cot x_0} \right)$$



Required : "Graph of various functions"

Comp. Finance (10-11)

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Risky asset

- Equity (stock)
- Commodities
- Currency

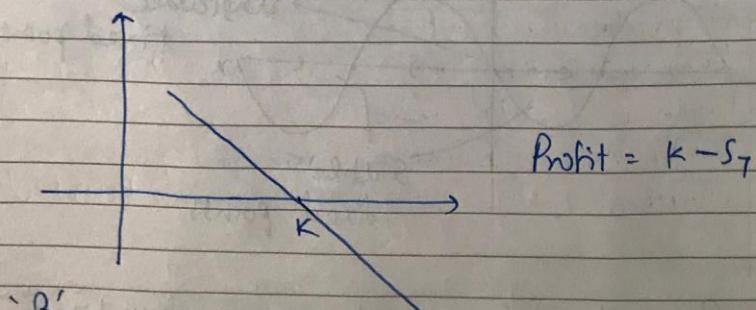
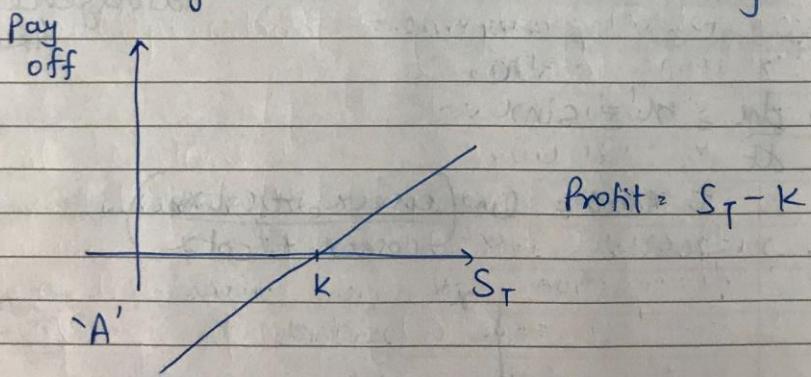
Risk free

- Bank
- $$S_0 \rightarrow S_0(1+r)$$
- $$S_0 \rightarrow S_0 e^{rt}$$

$$\lim_{n \rightarrow \infty} \left(1 + \frac{r}{n}\right)^{nt} = e^{rt}$$

Derivative : is a contract whose price depends on an underlying risky asset.
Eg - forward contract

A — B
bys sells K - strike price
 t - maturity date



- Hedging & Speculation

- Arbitrage (risk-free profit)

HM

- Stock options
- Ambience
- Salary
- allowances
- work-life balance
- lot of fields that one can switch

15 points in good organization

- (i) Competent Boss
- (ii) Friendly supervisor
- (iii) Good salary
- (iv) Interesting work
- (v) Job security
- (vi) Chance to learn & keep growing
- (vii) Pleasant working conditions
- (viii) Recognition for good work
- (ix) Fair personal policies
- (x) Good advancement in prospects
- (xi) Friendly coworkers
- (xii) Responsibility
- (xiii) Chance to achieve
- (xiv) Help each other, rewards
- (xv) Participation & decision making

OS (12-1)

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exec() - returns only when failure

fork() - fails then returns 'once'
or returns twice if call is successful

Threads → Different local variables

HCP (3-4)

Goal: Achieve max possible performance from a computing system for a particular problem.

- Real system
- Theoretical system

Matrix multiplication → complexity (Deterministic)
 $\hookrightarrow O(n^3)$ Result

Real systems

- Non-deterministic system
 - Because of hardware or software
- Non-terminating
- Real (Opp. of abstract)

Theoretical systems

- Deterministic system
- Terminating
- Abstract

Let's HPC

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System's perspective

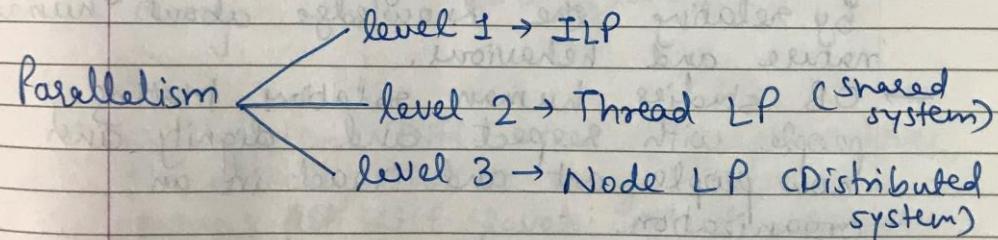
- Hardware or Architecture
- Algorithm
- Software environment

Analysis

- input
- methodology of measurement
- software environment
- Run-time environment

Power wall + Memory wall + ILP wall

↳ Instruction Level Parallelism



→ Data access is limited so ↑ freq. will not help until data access is improved in speed.

Two points for parallel programming:

(i) Hardware is parallel (we can't get a single transistor)

(ii) Real time application [accurate time constraint]

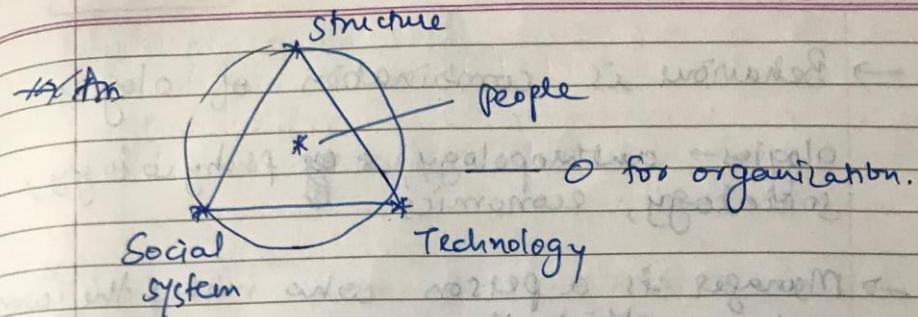
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294 21st

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H M

- OB is study of the application of knowledge about human behaviour in an organization.
- Organization is the study of structure & functioning and performance of an organization as individual, as a group and the individual & group in the organization.
- OB is defined (individuals (people's)) as optimum utilization of human resources for attainment of organizational goals by relating the knowledge about human nature and behaviour.
- OB studies human relations treating people with respect and dignity and how people act and react in an organization.
- OB is studied under two levels:
 - (i) Individual (job satisfaction, motivation, empowerment, ethics, values, attitude)
 - (ii) Group (working with other people (team), group dynamics & at organizational level it sees the challenges the organization faces to improve customer satisfaction, service, sees to change in technology, innovation & resistance to change.)



- Earlier managers were field specific (BTech + MBA)
- Now, managers are people-oriented, try to increase productivity of people.

- (i) Responsibility
 - (ii) Commitment
 - (iii) Growth
 - (iv) Money
- People continued in same organization.

→ Social system: Diff. kind of people, culture, the diversity that is brought into the system, diff. levels of education & knowledge, the value system individuals have, customs, traditions, all these are responsible in an organization to make a social system.

→ Technology: How people respond to changes, to new technology, how much of resistance is there in organization, how managers deal with these resistance to change.

→ Behavior is combination of ologies.

ologies → anthropology, psychology, sociology, economics.

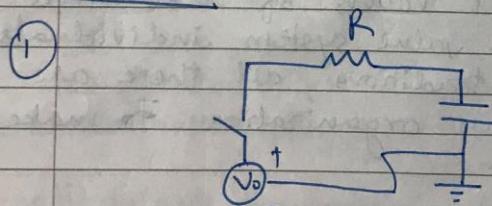
→ Manager is a person who makes the work done efficiently.

→ management is doing the work efficiently using all the given or efficient resources.

→ Organization means when two or more people come together under one roof in the system to achieve the desired goal.

→ Technical skills, human skills, conceptual skills,

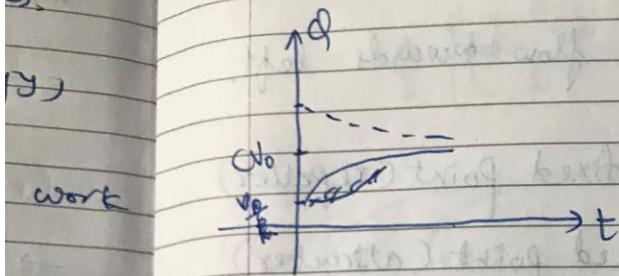
11-12 (NLD)



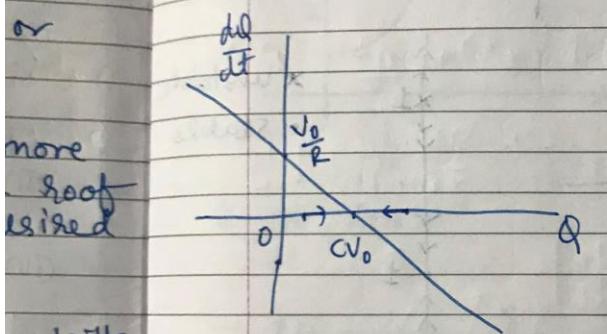
$$-V_o + IR + \frac{Q}{C} = 0$$

$$-V_o + \frac{dI}{dt}R + \frac{Q}{C} = 0$$

$$\frac{dq}{dt} = \frac{V_0}{R} - \frac{q}{RC}$$



or



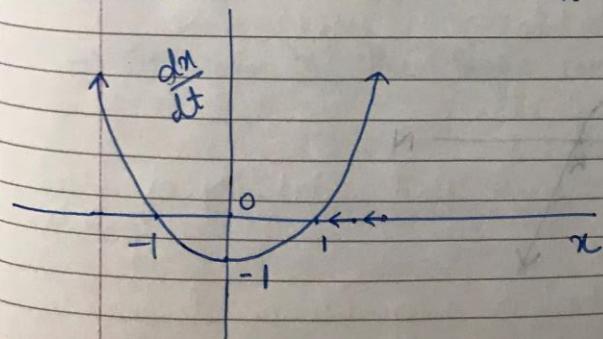
skills,

$$\rightarrow \text{For fixed point, } f(Q) = \frac{dq}{dt} = 0.$$

$$\therefore Q = CV_0 \text{ (fixed point)}$$

$$(2) \quad \frac{dx}{dt} = x^2 - 1$$

$$x = \pm 1 \text{ (fixed points)}$$

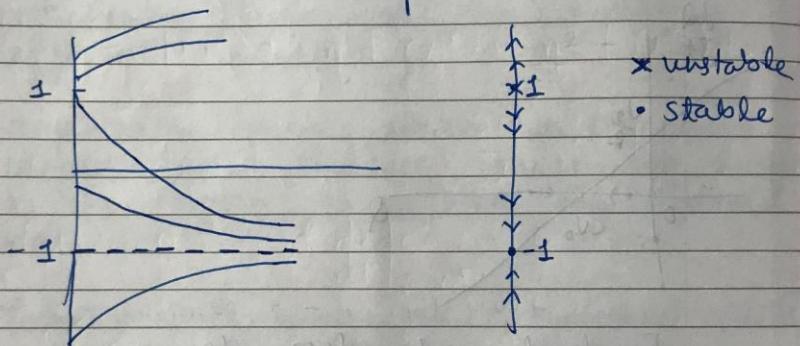


→ If $\frac{dx}{dt} > 0$ then flow towards right.

→ If $\frac{dx}{dt} < 0$ then flow towards left.

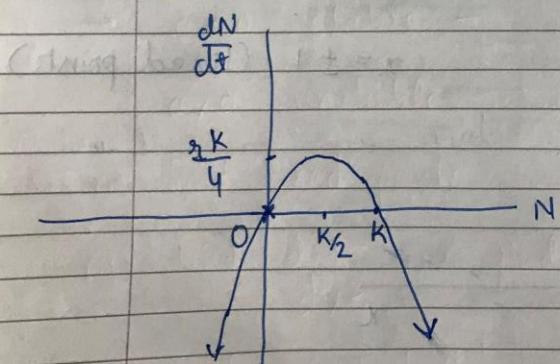
'1' → unstable fixed point (repeller)

'-1' → stable fixed point (attractor)



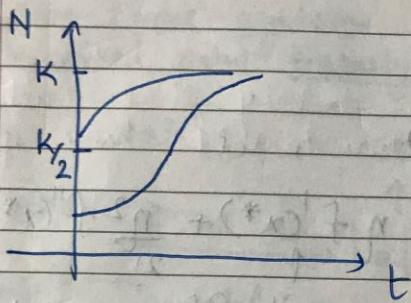
③

$$\frac{dN}{dt} = r_N N \left(1 - \frac{N}{K}\right) ; \quad r, K > 0$$



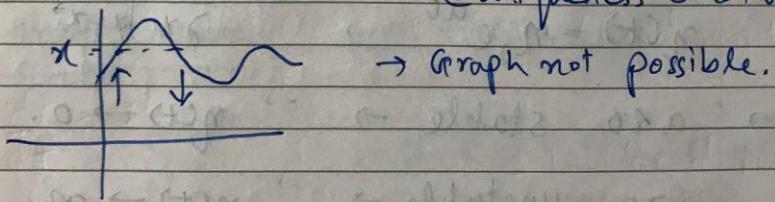
$$\frac{dN}{dt} = -\frac{r}{K} [N^2 - KN]$$

$$= -\frac{r}{K} \left[\left(N - \frac{K}{2} \right)^2 - \frac{K^2}{4} \right]$$



* $\frac{dx}{dt} = f(x)$

→ 1D system does not depending upon 't' explicitly won't show oscillations.
(uniqueness cond. violated)



→ At same 'x', the slope can either ↑ or ↓.

$x = x^* \rightarrow$ fixed point

→ Perturbations from fixed points:

$$x' = f(x)$$

$$x = x^* + \eta$$

$$x' = f(x^* + \eta)$$

$$= f(x^*) + \underset{1}{\eta} f'(x^*) + \underset{2!}{\frac{\eta^2}{2!}} f''(x^*) + \dots$$

conite $\frac{\partial f}{\partial x}$ for safety.

$$f(x^*) = 0 \quad \therefore \left. \frac{dx}{dt} \right|_{x=x^*} = 0.$$

$$\eta' \approx a\eta$$

$$\eta(t) = \eta_0 e^{at}$$

$$a = \left. \frac{\partial f}{\partial x} \right|_{x=x^*}$$

→ $a < 0$ stable $\rightarrow \because \eta(t) \rightarrow 0$.

$a > 0$ unstable $\rightarrow \because \eta(t) \rightarrow \infty$

method II:

(i) Find fixed points

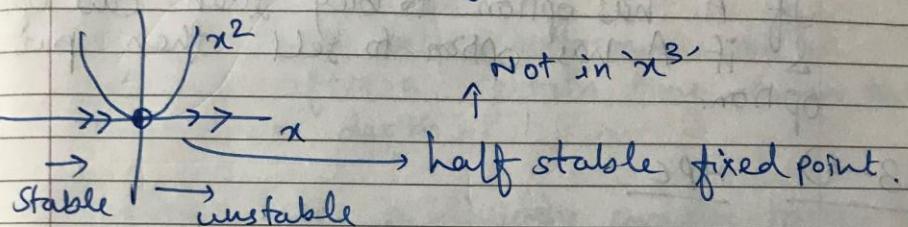
(ii) Find $\frac{d^2 f}{dx^2}$ and find stability of fixed points.

(iii) Find perturbations grows or decays towards fixed point.

Method II: Known as linearization. (we can't tell about trajectory)

If $\frac{\partial f}{\partial x} = 0$ then going to higher terms will make the problem non-linear.

→ "Non-linear systems grow away or converges to fixed point linearly."



$\frac{dx}{dt} = ax$ [change in parameter 'a', the stability changes and the graph changes drastically]

Bifurcation

↳ (Phase transition)

(12-1) Comp. Finance

$$F_0 = S_0 e^{rT}$$

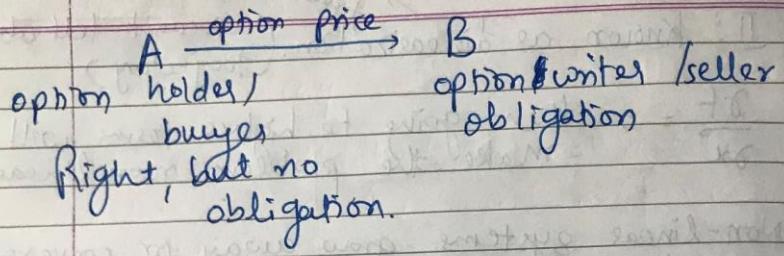
Forward price Strike price Spot price

if $F > S_0 e^{rT}$ or $F < S_0 e^{rT}$
and earn profit.
So, $F = S_0 e^{rT}$ only.

$r \rightarrow$ risk free interest rate

$T \rightarrow$ time remaining to mature.

$$F_0 = S_0 (1+r)$$



If A has option to buy then call option
 & if A has option to sell then put option.

(3-4) HPC

ILP (Instruction level parallelism) Pipeline

Complex process → Divide sub tasks

→ n (no. of instruction)

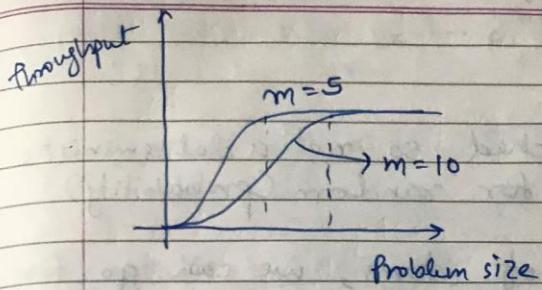
↓ m depth of pipeline

$$\text{Speedup} = \frac{nm}{n+m-1} \begin{matrix} \text{(without pipeline)} \\ \text{(with pipeline)} \end{matrix}$$

$$= \frac{m}{\frac{m}{N} - \frac{1}{N} + 1}$$

if $N \gg m$

$$\therefore \text{speedup} = \frac{m}{1} \quad (\text{Not if } m \leq n)$$



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Depth ↑ then better performance can be obtained after a certain time. (more time than ↓er depth).

→ Pipeline helps in dividing complex tasks into smaller tasks (helping in concurrency) and its Speed is directly prop. to depth of pipeline.

Throughput = $\frac{\text{Total no. of operations}}{\text{Total time}}$

$$= \frac{\text{Flops}}{s}$$

$$\text{Node performance in GFlops} = (\text{CPU speed (GHz)} \times (\text{no. of CPU cores}) \times (\text{CPU inst. per cycle}) \times (\text{no. of CPUs per node}))$$

$$\text{Performance} = \frac{\text{cycles}}{\text{sec}} \times \frac{\text{Flops}}{\text{cycles}} \times \text{No. of cores.} \rightarrow 4 \text{ nodes with } 16 \text{ cores each}$$

↑

$\frac{\text{flops}}{\text{cycles}} = 4$ (Typically)

19/01/2020

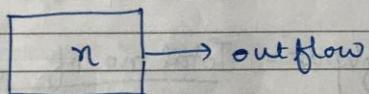
M & S (9-10)

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Radioactive Decay

- No clock attached, so not a deterministic system so go for random (probability) system.
 - For large no. of atoms, we can go for differential eqn's as average can be taken.
- (i) Number is large
- Large is large enough that any statistical variations are insignificant.

(ii) Independent



$$\frac{dn}{dt} = -kn \quad \begin{array}{l} \text{(first take only } -k\text{' , then} \\ \text{if it doesn't match with} \\ \text{results then use } -kn' \end{array}$$

-ve because only outflow.

→ Why not probabilistic model & why deterministic model?

$$n(t) = n_0 e^{-kt}$$

$$\frac{n(t)}{n_0} = e^{-kt} \quad \begin{array}{l} \text{(Prob. of no. of atoms} \\ \text{present)} \end{array}$$

$$1 - \frac{n(t)}{n_0} = 1 - e^{-kt} \quad \begin{array}{l} \text{(Prob. of no. of atoms} \\ \text{decay)} \end{array}$$

$$F(t) = \frac{1 - n(t)}{n_0} = 1 - e^{-kt}$$

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$$f(t) = \frac{dF}{dt} = ke^{-kt}$$

for taken.

Expectation = $\int_0^\infty t f(t) dt = k \int_0^\infty t e^{-kt} dt$

of time taken to move out of compartment.

$$k \left[- \int_0^\infty \frac{d}{dk} e^{-kt} dt \right]$$

$$= -k \frac{d}{dk} \int_0^\infty e^{-kt} dt$$

$$= -k \frac{d}{dk} \left(\frac{e^{-kt}}{k} \right)_0^\infty$$

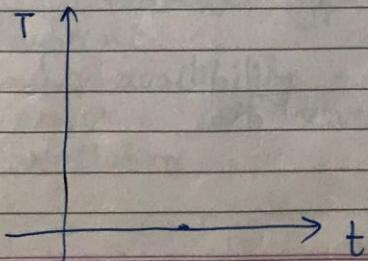
$$= -k \left(-\frac{1}{k^2} \right) = \frac{k}{k^2} = \frac{1}{k}$$

then
atch with
 $= km'$)

Cup of Coffee problem:

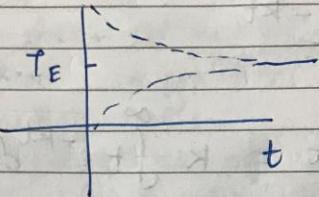
T_E : Environment temperature

T : Temperature of coffee



- (i) Treat as compartment
- (ii) $\frac{dT}{dt}$

$$\frac{dT}{dt} \propto (T - T_E) \quad (\text{Is sign + or - relevant here?})$$

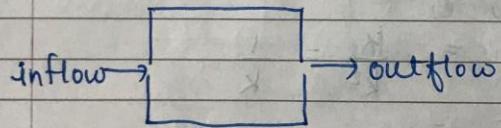


→ When gain = loss then in most linear systems modeled by balance equation then

$$\frac{dT}{dt} \rightarrow 0$$

→ In divergent systems like $\frac{dT}{dt} = kT$,

$$\frac{dT}{dt} \rightarrow \infty. \text{ No equilibrium is achieved.}$$

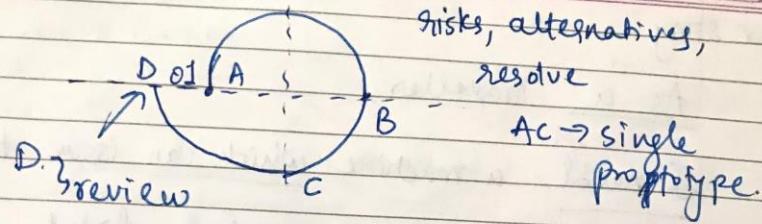


① Lake Pollution

② Drug Dosage

(p-11) Software Eng.

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Risks, alternatives,
resolve

AC → single
prototype.

CD → plan for next objectives

AB → risk analysis

→ After all objectives, when we have operational prototype we start using main 5 types to build product.

Two imp points

- (i) Order of activities
- (ii) Transition between them.

functionalities of Ticket Distributer system:

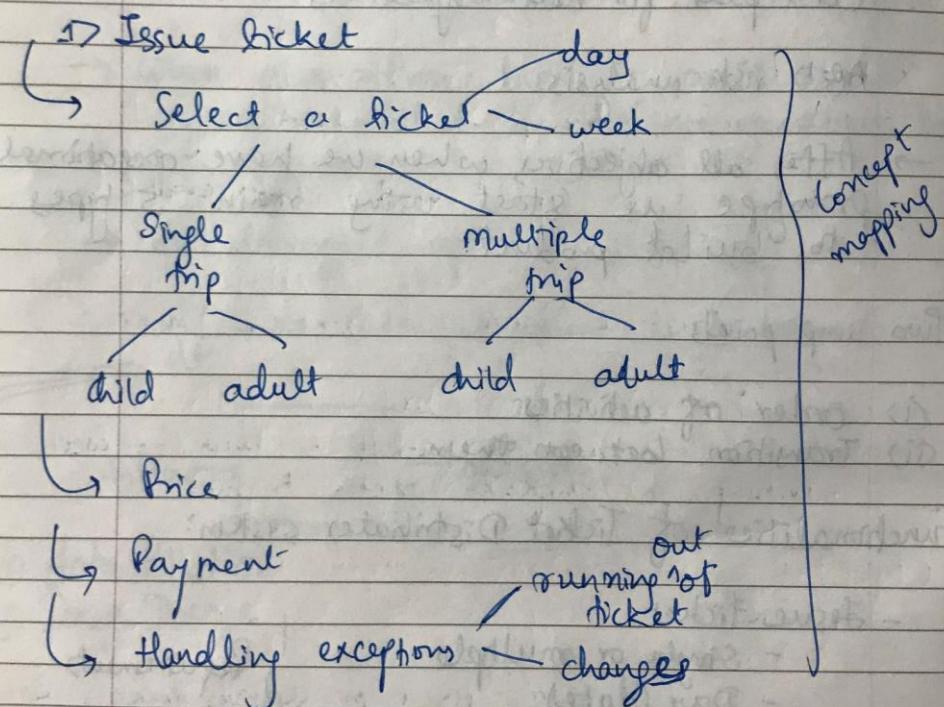
- Issue Ticket
 - Single or multiple
 - Day (date)
 - Price (total price also)
 - Traveller type
 - Payment
 - Count availability
 - Connection with server
 - Cancellation
- Requirements
for ticket

User story

As a traveller,

I need a machine which can issue ticket

such that I can purchase ticket.



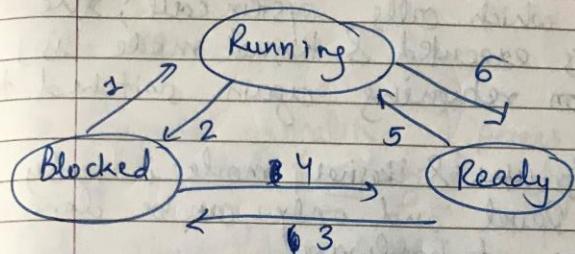
→ These requirements are not independent.

① Requirement Engineering

② Concept Mapping.

(b) C2-1)

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(a) Transition 3 : Ready to Blocked

- Not legal
- Only running processes are blocked.
- Blocked state is meant for stopping a running process to wait for an event.

(b) Transition 1 : Blocked to Running

- from Blocked state a process goes to ready state first.
- So, it is not legal.
- Because some other process would be already running so scheduler needs to decide which process to run from ready state.

System call

- There are some resources in system which are shared by processes like memory, CPU etc.
- We don't want to have a process an uncontrolled access to hard drive or processor.
- System calls allow a process to allow a resource to restricted use of it.
- At hardware level : i) User mode ii) Kernel mode
- Certain instructions can only be executed if CPU is in Kernel mode. (for accessing certain resources).

- The instructions which calls system call; the system call is executed & Kernel mode is entered & on returning again switched to user mode.
- This checking of user & kernel mode is only at hardware level and only can be done with the use of hardware.
- System call is the only way to switch from user mode to Kernel mode.
- In Kernel mode, OS routines are called & they cannot be tampered.

Assembly instruction { trap, return-from-trap }

- System calls → Kernel stack
- normal funcs → User stack.

* How functions work at machine levels?

Book - Bryant & Hildebrand

Computer System: Programmers perspective.

- A timer is kept in hardware (Time Interrupt). So, on timer being completed control is regained and again it is decided who to give the control of hardware.

Scheduling decision made

- (i) System call invoked by process
- (ii) Timer interrupt happens.

MLFQ → successful scheduling approach.

* xv6 → An OS

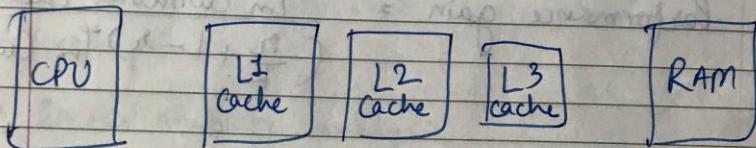
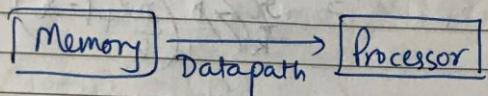
(3-4) HCP

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Cache / Memory

- * Temporal Locality
 - * Spatial Locality
- } Access pattern of algorithm

Cache reuse & hit (Diff.)



→ Cache is 'k' times faster than RAM.

→ ~~Set - r~~ ^{is} the reuse ratio.

RAM [Bandwidth Processor → Frequency
Latency]

→ Cache has better bandwidth & latency than RAM.

→ r is fraction of load/store that can be satisfied from cache.

Access time to main memory (T_m)

Access time to cache (one level) (T_c)

$$T_c = \frac{T_m}{K}$$

$$\rightarrow \text{Average access time} = \frac{r}{k} T_c + T_m(1-r)$$

$$= \frac{r}{k} T_m + T_m - rT_m$$

$$= \frac{r}{k} \left(\frac{r}{k} + 1 - r \right) T_m$$

$$\rightarrow \text{Performance gain} = \frac{T_m \text{ (without cache)}}{\left(\frac{r}{k} + 1 - r \right) T_m \text{ (with cache)}}$$

$$= \frac{1}{\left(\frac{r}{k} + 1 - r \right)}$$

$$= \frac{k}{r + (1-r)k}$$

$$\rightarrow r=0$$

$$P_{GF} = 1$$

$$\rightarrow r=1$$

$$P_{GF} = k$$

(Cache line C For Spatial Locality & hit)

\rightarrow To increase the Cache hit ($k_c \geq 16$)

$$\text{Hit Ratio} = 15/16$$

Von Neumann bottleneck

→ The rate of computation is increasing but data access rate is not being able to cope up. This diff is Von Neumann bottleneck.

Also
called

Memory wall / DRAM gap

10/01/2022

(10-11) NLD.

th
ache)

→ fixed points

→ linear stability analysis.

$$\frac{\partial f}{\partial x} \Big|_{x=x^*} \begin{cases} > 0 & \text{unstable} \\ < 0 & \text{stable} \end{cases}$$

$$\text{eg} - x' = 1 - x^2 = f(x)$$

$$f'(x) = -2x$$

$$x^* = \pm 1$$

$$f'(1) = -2 \quad (\text{stable})$$

$$f'(-1) = 2 \quad (\text{unstable})$$

$$\text{Newton's eqn} \rightarrow mx'' = -\frac{\partial V}{\partial x} = f(x)$$

$$\text{Pendulum} \rightarrow mx'' + m\gamma x' + mw^2x = 0$$

(i) Overdamped → No influence of 2nd order term.

(ii) Underdamped

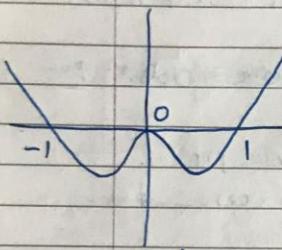
(iii) Critically damped

Eg - $x' = x - x^3 = f(x)$

$x^* = \pm 1, 0$

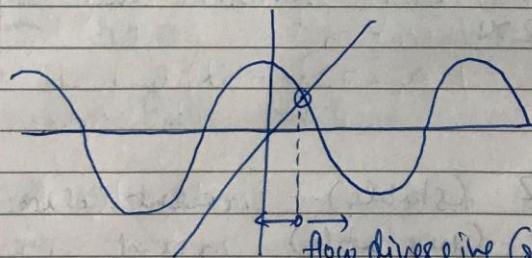
$-1, 1 \rightarrow \text{stable}$
 $0 \rightarrow \text{unstable}$

$$V = - \int f(x) dx = -\frac{x^2}{2} + \frac{x^4}{4} + C$$



Eg - $x' = x - \cos x = f(x)$

For fixed points, $f(x) = 0$
 $\therefore x = \cos x$

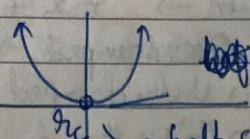


→ Solution using numerical methods like bisection, newton-raphson etc.

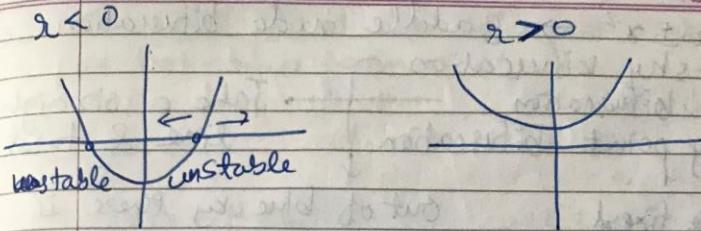
Eg - $x' = r + x^2$

if $r > 0$

Bifurcation point $r_c = \boxed{r_c = 0}$



half stable



- For $r > 0$ the system is just diverging, on \downarrow (r coming close to zero) then it becomes a half stable fixed points.
- On $\uparrow r$ further, the half stable point is divided into two fixed points i.e. one stable & one unstable fixed point.
- There can never be two adjacent & stable or unstable fixed points.
- On changing the value of constant, the behaviour of the system also changes drastically.
- Any physical system showing such property is called "Bifurcation"
 ↗ only by non-linear not by linear systems.
- Something which wasn't present, suddenly appears or something was present, suddenly disappears. → (Water to Ice) (Suddenly)
- In large systems, self-organization takes place; called phase transition same as bifurcation.

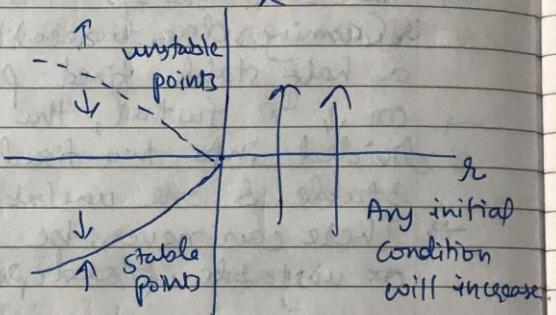
- Date to fixed
point can be
reduced to this form
called "normal form"
- $x' = r + x^2 \rightarrow$ Saddle node bifurcation
- blue-sky bifurcation
- fold bifurcation
- turning point bifurcation.
- Take a straight
line & fold

↙ a stable fixed point turns around & becomes unstable

out of blue sky there is a fixed point.

$$x' = r + x^2$$

$$x^* = \pm \sqrt{-r}$$



To ↓ show how system changes

Objective: Given an initial condition, we want to know what happens to sol^{\pm} .

If x_0 & r is given, what happens to sol^{\pm} .

$x(t) = f(x_0, r, t)$ [Not trajectory but dynamics.]

Types of Bifurcation:

- (i) Saddle node → [sudden appearance or sudden disappearance of fixed points in pair]
- (ii) Pitchfork
- (iii) Transcritical

Two new stable fixed points appear.

(along the time change their stability)

not single

* In Non-linear partial diff eq's, still research going on for normal form.

(11-12) Hm

(i) Technical Skills

(ii) Human skills

(iii) Conceptual skills

→ Aim for higher posts like decision making, problem solving, critical thinking.

• Group & Group Dynamics.

→ How team together works & achieves goal.
Working on a particular project.

• Leadership

→ Influence on other people & translate the vision into reality.

• Motivation

→ Influencing people i.e. pushing button at right time

→ Give rewards, awards, appreciation in intrinsic or extrinsic way.

• Industrial Relation

→ Relation between manager & management.

→ Relation betⁿ employee & employee.

→ If industrial relation is good then the lockouts, strike, grievances will be lesser in organization.

- Conflict Management.

→ Difference of opinion in logical thinking which leads to disturbance in work or politics in the organization.

- Change management.

→ In an organization, there is always an option to change but people are in their comfort zone & don't want change.

Z Managers (William Ouchi)

→ Combination of American & Japanese type of working.

→ American companies like IBM, Intel, HP, Kodak is combination of Theory Z.

Japanese → They have high productivity & loyal workforce because they believe in lifetime employment to their employees until they retire at the age of 55.

→ They do not fire an employee unless committed a crime.

→ The promotions are slow and are awarded only after they have served the organization for a considerable period of time.

→ Employees are trained in all aspects of the organizational functioning not just a specified area.

→ Japanese organizations take collective decision & collective responsibility to carry out the work.

- Employees, customers, suppliers ; they have the trust & goodwill (relation b/w them).
- They are not only concerned about the performers of the employees but also about the family life and social life.
- They are the people working, are loyal & committed to the organization. (Don't leave in 6 mon to 1 year)
- Growth in this company is slow.

American

- Short term employment.
- Downsizing is there if the performance is not good.
- They believe in going fast track i.e. award promotion to people, employees for extraordinary performance.
- If people are good then they can climb the ladder very fast. & If they are not good they are out.
- Career path of the employees are specialised in particular area.
- Well defined rules & policies to regulate the employee behaviour.
- Focus on individual only; not concerned about family; only concerned about the professional life of the people.

The 2 type of organization : They practice in job rotation, moderate career specialisation. The employees are acquainted with the various functioning of department.

→ Process of promotion is slow which ensures people or employees understand the culture, belief, value culture of the organization before joining or thinking of responsibilities.

→ Decisions are made collectively by managers.

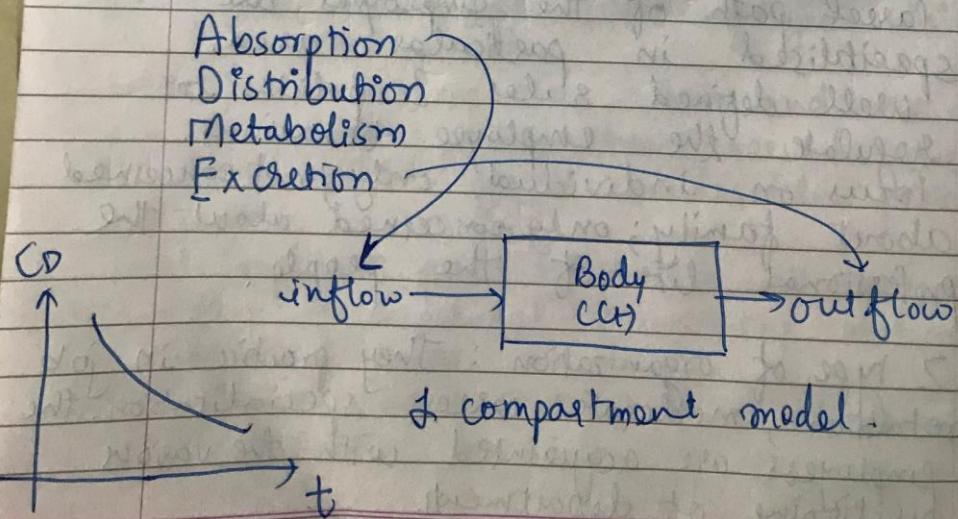
The Z type of organization have less of supervision & control.
Such organizations do not have

as they offer good working conditions and attractive pay backs.

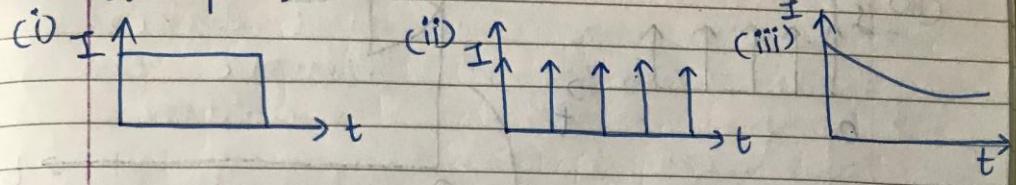
→ The demerit part is they are not open to diverse views & conflicts occur for personal goals in the organization.

→ People who are culturally dissimilar may find themselves isolated.

M&S (12-1)



Three assumptions:



$$\frac{dc}{dt} = I(t) - Kc \Rightarrow Kc(t) \downarrow \text{exponentially.}$$

Consider, (i), (ii) & (iii)

$$\Rightarrow s \tilde{c} - c(0) = \tilde{I} - k \tilde{c}$$

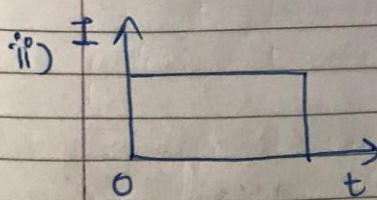
$$(s+k) \tilde{c} = c(0) + \tilde{I}$$

$$\tilde{c} = \frac{c(0)}{s+k} + \frac{\tilde{I}}{s+k}$$

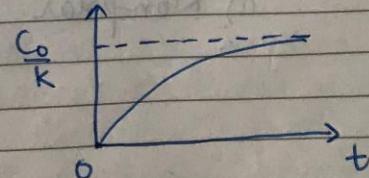
$$\mathcal{L}^{-1}[f(s)g(s)] = (f*g)(t)$$

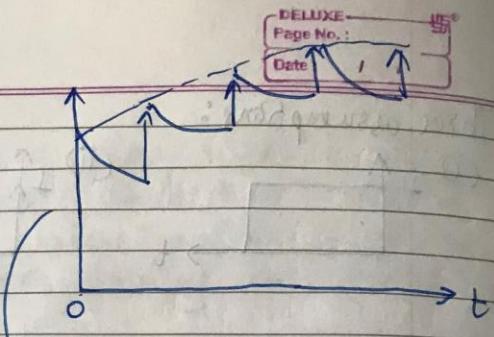
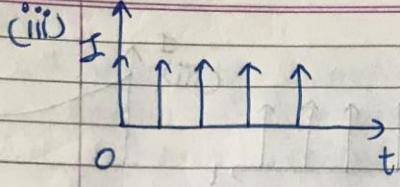
$$\therefore c(t) = c(0)e^{-kt} + \int_0^t e^{-k(t-t')} I(t') dt'$$

$$\stackrel{i)}{\Rightarrow} c_0 \int_0^t e^{-k(t-t')} g(t') dt$$



$$\frac{c_0}{K} (1 - e^{-kt})$$





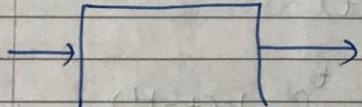
$$\rightarrow C(t=T^*) = C_0 e^{-kT} + C_0$$

Stabilizes approximately
near $\frac{C_0}{K}$.

$$\begin{aligned} C(t=2T^*) &= (C_0 e^{-kT} + C_0) e^{-kT} + C_0 \\ &= C_0 [1 + e^{-kT} + e^{-2kT} + \dots] \end{aligned}$$

$$C(t=nT^*) = C_0 \left(\frac{1 - e^{-nkT}}{1 - e^{-kT}} \right); C_{mc} \ll C_{mc}$$

Eg -



Take of constant
volume

V_L

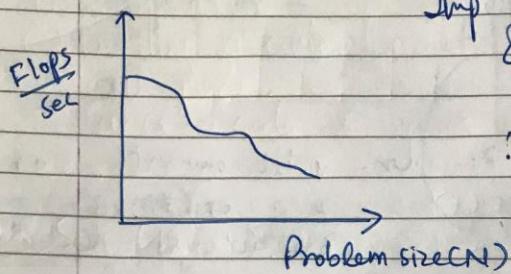
$$\frac{dc}{dt} = 0 - k_1 c_p - k_2 c_n$$

polar non-polar

Pollutants: i) Polar
ii) Non-polar

DELUXE
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HCP (3-4)

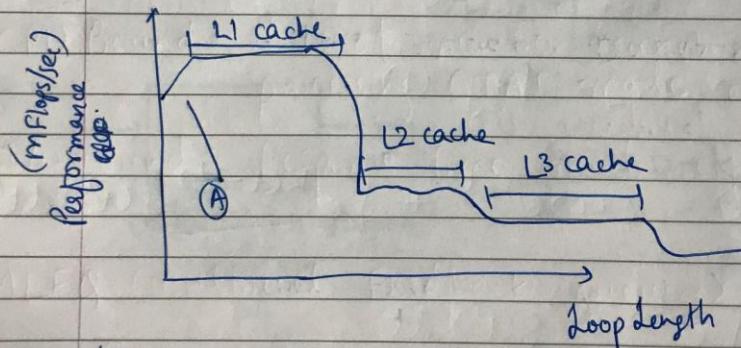


Imp : start = clock();
& other time measuring
functions.

: Out of order execution.

$$\text{Throughput} = \frac{n * \text{NITER} * 2}{(\text{End time} - \text{start time})} \quad \rightarrow \because (\text{one} + 8 \text{ one} \times)$$

- vector triad
- compiler optimization.



\$ lscpu

- Ⓐ → Because as the problem size is smaller, the pipeline is not utilized properly.
- Pipeline is efficient only for large problem size.
- No. of arrays also a factor considered.
- Diff. between malloc & realloc wrt place of memory allocation.

Block matrix multiplication & other types of optimal techn. for matrix multiplication.

Balance analysis of loops:

(i) Machine Balance = $\frac{\text{memory bandwidth}}{\text{peak performance}} \frac{\text{Bytes}}{\text{Flops}}$

(ii) Code Balance = $\frac{\text{data traffic unit}}{\text{floating pt. ops}}$
 ↳ also: $\frac{\text{Bytes}}{\text{Flops}}$

In slide q- CB = $\frac{4 \times 8 \text{ (4 doubles)}}{2 \text{ (Because 2 ops)}} = \frac{16}{2}$

→ CMA (Compute to memory access) = $\frac{\text{Flops}}{\text{Bytes}}$

↳ In GPU's, this ratio is high.

$$\text{CMA} = \frac{1}{\text{CB}}$$

→ Good performance = load some data & lot of operations.

CMA = Computational Intensity

→ Machine Balance cannot be changed. Thus, only changing the architecture we can change m.b.

→ They, for some architecture we need to play with Code balance.

Optimizing a code → Performance modelling

i) Profiling a code (gprof from GNU)

→ Takes a code & gives locations of compute/mem ratio is low.

~~M&S (part 2)~~

[13/10/20] OS (9-10).

TAT (Turnaround Time): Time between i) Job enters ii) Job gets completed.

RT (Response Time): Time between i) Job enters ii) Job scheduled for first time.

CPU Bound: Lots of number crunching & processing CTAT made efficient i.e. ↓

I/O Bound: Response time made efficient i.e. ↓

MLFQ (Multilevel Feedback queuing).

- Ready queue is divided into many no. of queues.
- No. of queue is a metric which is determined on the basis of hit & trial or practicality.
- No. of queues are fixed. Their priority levels are different.
- Within the queue RR (Round Robin)

scheduling is used. All queues can have diff. time slices.

- Scheduler doesn't know if the job is CPU bound or I/O bound
- Jobs ~~each~~ can change their behaviour in the coarse of time.
- I/O bound jobs does not exhaust time slices completely while CPU bound jobs frequently exhaust time slices.

Rules of MLFQ:

- i) If Priority(A) > Priority(B) then A runs & B doesn't.
- ii) If Priority(A) = Priority(B), A & B run in Round Robin.
- iii) When a job enters a system we don't know anything so I/O bound assumed and placed at highest priority queue.
- iv) If entire time slice is used up, priority of job is reduced.
- v) If entire time slice is not used, priority of job is kept at same level.

Problems:

(i) Starvation: Too many interactive jobs & so long running jobs will never receive CPU time.

(ii) Game the scheduler: (Assume that processes are not malicious) Doing something to trick the scheduler into giving more than fair share of resources.

Time slice: 10 ms

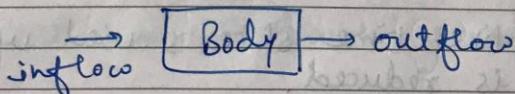
then a process will voluntarily give CPU after 9 ms (cheat)

(iii) No mechanism to go up the queue.
(what if CPU bound changes to I/O bound?)

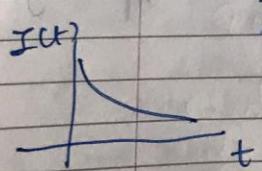
→ boosting priority → After some fixed time 's', all jobs are moved to topmost queue.

So problems (i) & (iii) solved.

(2-1) M&S



$$\frac{dc}{dt} = I(t) - kC$$



$$C(t) = C_0 e^{-kt} + \int e^{-k(t-t')} I(t') dt'$$

$$I(t') = \delta(t)$$

ignore this term.

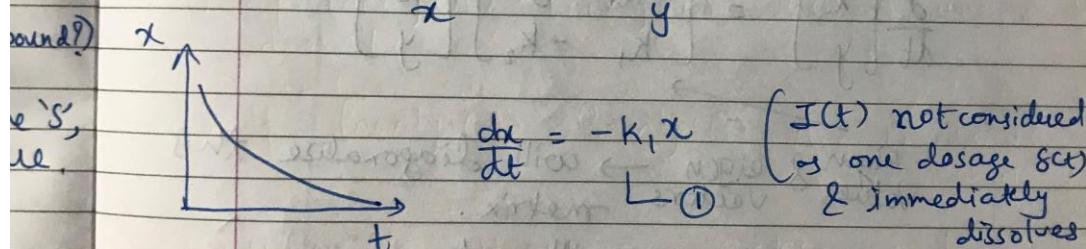
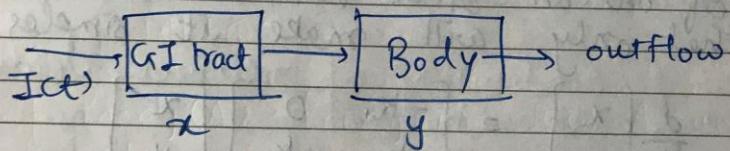
first assumed:

8 i) Pill taken instantaneously & distributed uniformly instantaneously.

Now, we are breaking the assumption that it is not merged instantaneously.

thing

→ Body is still considered a compartment; just there is a channel GI-tract through which the pill goes to the body.



$$\frac{dy}{dt} = k_1 x - k_2 y \quad ②$$

Using Laplace transform:

$$s\tilde{x} - x(0) = -k_1 \tilde{x}$$

$$\tilde{x} = \frac{x(0)}{s + k_1}$$

$$s\tilde{y} = k_1 \tilde{x} - k_2 \tilde{y} \quad (\text{Initial for } y = 0)$$

$$\therefore \tilde{y} = \frac{k_1}{(s+k_2)(s+k_1)}$$

$$\therefore \tilde{y} = \frac{k_1 x(0)}{k_1 - k_2} \left[\frac{1}{s+k_2} - \frac{1}{s+k_1} \right]$$

$$y = \frac{k_1}{k_1 - k_2} x(0) \left[e^{-k_2 t} - e^{-k_1 t} \right]$$

→ In this coupled ① & ② eqn's the dependence of one on other variable can be removed that only will make it simpler.

$$\frac{d}{dt} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} -k_1 & 0 \\ k_1 & -k_2 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

eigen values & eigen vectors → will diagonalize this matrix.

so, we will get

$$\frac{dx}{dt} \propto f(x)$$

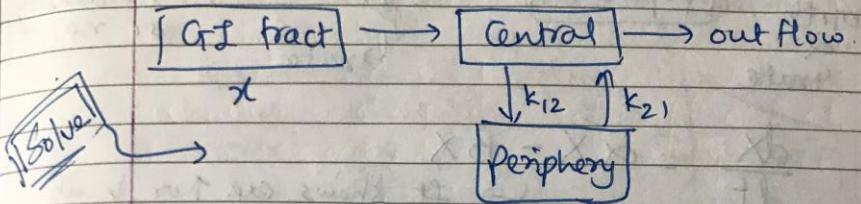
$$\frac{dy}{dt} \propto f(y)$$

→ We can solve that afterwards.

$$\bar{x}(t) = c_1 e^{\lambda_1 t} \bar{v}_1 + c_2 e^{\lambda_2 t} \bar{v}_2$$

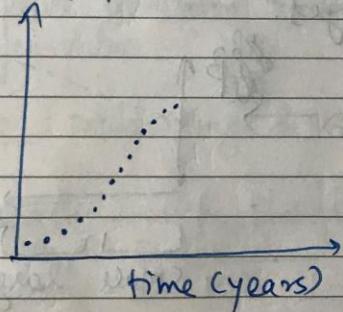
→ The decay will be in the direction of eigen vectors and the amt. of decomposition will depend on eigen values.

→ Body can be considered as two compartments.



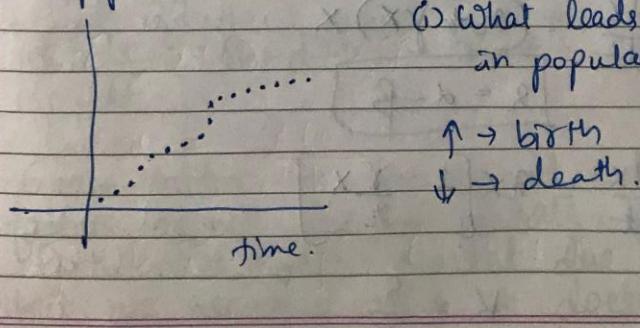
→ For multiple compartment problems write all the eqn's in matrix form and diagonalize the matrix.

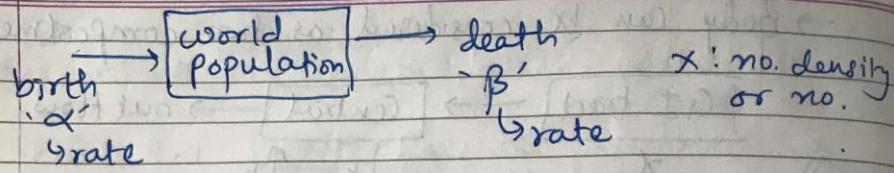
World population



How population changes with time? (Main ques.)

Bacteria population





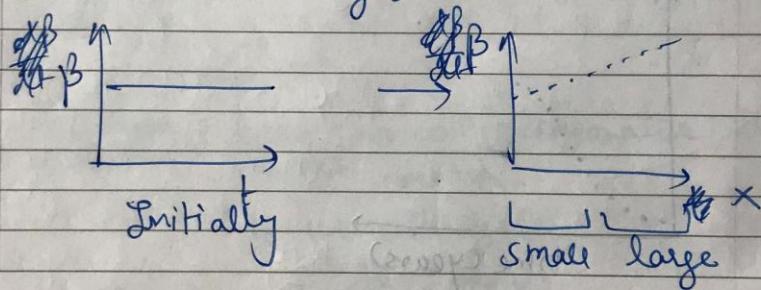
$$\frac{dx}{dt} = \alpha X - \beta X$$

It shows exp. ↑ or ↓ in small ranges but in larger ranges it saturates.

→ This won't work :: $\alpha > \beta$ then divergence but never like that.

↳ Discovered by Malthusian Explosion.

→ Due to availability of resource, death rate should be changes.



~~$\beta \rightarrow (\beta + \gamma x)$~~

$$\frac{dx}{dt} = (r - \gamma x)x$$

$$r = d - \beta$$

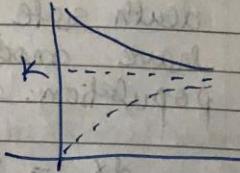
$$\frac{dx}{dt} = rx \left[1 - \frac{\gamma}{r} x \right]$$

$$K = \frac{r}{\gamma}$$

$$\frac{dx}{dt} = r x \left(1 - \frac{x}{K}\right) \rightarrow \text{logistic Equation.}$$

$$K < x \quad \frac{dx}{dt} \uparrow$$

$$K > x \quad \frac{dx}{dt} \downarrow$$



→ Constraint imposed by resources which affects the death rate which is directly linearly prop. to 'x' & shows saturation in population.

- (i) Laplace transform } Solution of Diff. equations.
- (ii) Eigen-value

16/1/2020 Modelling & Simulation (9-10)

$$\begin{array}{c} \text{birth} \\ b \end{array} \xrightarrow{\text{population}} \boxed{\text{population}} \xrightarrow{\text{death}} \begin{array}{c} d \\ d \end{array}$$

$$\frac{dx}{dt} = (b-d)x \quad \hookrightarrow d \rightarrow d + \gamma x$$

$$\frac{dx}{dt} = (b-d)x - \gamma x^2$$

- Space factor for yeast and such many factors affect the death rate
- Birth rate gets affected due to loneliness but we assumed that it doesn't.

- Also, we assumed all are identical
- Due to development in medical science, death rate should decrease but we have modelled death to increase with population.

$$\frac{dx}{dt} = \alpha x \left(1 - \frac{x}{K}\right) \rightarrow K(t)$$

- K should also be function of time because along the time due to advancements, value of K increases.

(12-1) OS

PALFQ (P) midium & problem access

- Time allotment used. If time slice is of 30 ms. Once it gives after 20 ms. then after 10 ms of second slice it will be demoted.
- * → But system call was made only when the time slice completed so now after end of time allotment, system call is made.

Lower priority queues → longer time slices
 Becoz mostly long running jobs & time of context switching saved)

Higher priority queues → Small time slices.

Q. How many queues used?

Q. How long time slice at highest & lowest priority queue?

al.
ience,
we

with

File Systems

- File descriptor table stored in Kernel memory.
- If same file opened twice, they would have diff. file descriptors & diff. file table entry.
- File data entry is removed (on calling close) only if any file descriptor is not pointing to it.

(4-5) HPC

Case 1: 99% hit

Avg. acc.

to 30 ms.

10 ms

d.

then the
end

e.

lives

long
& time

switching
d)

Case 2: 97% hit

Avg. acc.

time = 2 cycles

Case 3: 80% hit

~~0.80 + 0.20~~

Avg. acc.

time = 4 cycles

Avg. acc.

time = 20 cycles

→ latency of main memory is 100 times more than the latency of cache.

Consider, for cache = 2 cycle

then for mm = 100 cycle.

Computation Throughput

Memory access Throughput.

64 bit DDRAM

Processor
↳ Cores
↳ frequency
↳ Flops/sec.

Memory
↳ Frequency of memory system
↳ channels
↳ Bytes/sec.

$$\hookrightarrow \frac{\text{Flops}}{\text{cycles}} \times \frac{\text{cycles}}{\text{second}} \times \text{No. of cores.}$$

Peak memory access throughput

$$\text{DDRAM} \rightarrow = \left(\frac{\text{No. of bytes per transfer}}{8} \right) \times \left(\frac{\text{Transfers per channel}}{2 \text{ cycle}} \right) \times \text{No. of channels} \times (\text{Frequency})$$

(Transfers/channel)
per cycle

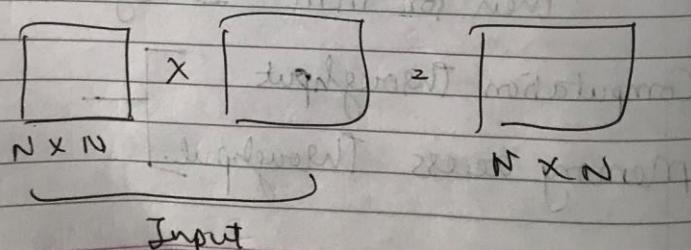
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(8-9) HPC

Optimizations of serial code.

Revision → Cache

Matrix multiplication



Patterns → (i) Temporal locality (Future use) (Cont. access)
 (ii) Spacial locality (Reuse)

$O(n^3) \rightarrow$ Time } $O(3N^2) \rightarrow$ Memory

Compute to
 Memory access (CMA) = $\frac{2N}{2N+1} \approx 1$
 (Cache ratio)
 ↳ Maybe $\frac{2N}{2N+1}$?

No. of
channels
y)

Two types of code: (i) memory bound code
 (ii) Compute bound code
 (iii) Intermediate

second.

$CMA \approx 1$ (then intermediate)
 ↳ Most linear algebra algos.

$CMA < 1$ (memory bound)

$CMA > 1$ (compute bound)

Block size → 32 or 64 byte (Together 32 or 64 bytes
 ↳ Cache lines are accessed)

Cache size << N (One row does not fit into cache)

first iteration

↳ Total no. of misses = $\frac{N}{8} + N = \frac{9N}{8}$

for column ←
 (Because stored in row major)

Date :

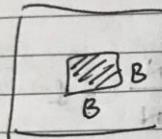
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output

$$\text{Total no. of misses} = \frac{9N}{8} \times N^2$$

Block matrix multiplication.



Block $\rightarrow B \times B$

Assume $(3B^2 < C) \& (C < N)$

First iteration

$$\hookrightarrow \frac{B^2}{8} \times \frac{2N}{B} = \frac{NB}{4}$$

$$\text{Total no. of blocks} = \left(\frac{N}{B}\right)^2$$

$$\text{Total no. of misses} = \frac{NB}{4} \times \frac{N^3}{B^2} = \frac{N^3}{4B}$$

misses	Type
$\frac{9N^3}{8}$	No blocking
$\frac{NB}{4B}$	Blocking

$$\text{Speedup} = \frac{9N^3}{8} \times \frac{4B}{NB} = \frac{9B}{2}$$

suppose,
 $B=8$

$$\text{speedup} = 36$$

$$B=16 \text{ or speedup} = 72$$

Output

Comp Finance

(9-10) Binomial Model

$$S_0 \xrightarrow{\begin{array}{l} H \\ T \end{array}} S_1(H) = uS_0 \quad S_1(T) = dS_0$$

$\boxed{K=5}$

$\rightarrow r \sim \text{risk free rate is given. } [1 \rightarrow 1+r]$

$$e.g. S_0 = 4, u = 2, d = \frac{1}{2}, r = 1\%$$

\rightarrow Let V_0 be the worth of the call option at $t=0$.

$$V_1(H) = S_1(H) - K = 3$$

$$V_1(T) = 0$$

Replication: Consider a hypothetical portfolio (x, y)

$x \rightarrow$ amt. of stock

$y \rightarrow$ amt. of money in bank

at time $t=0$

$$xS_1(H) + y^{(1+r)} = V_1(H)$$

$$xS_1(T) + y^{(1+r)} = V_1(T)$$

$$x(S_1(H) - S_1(T)) = V_1(H) - V_1(T)$$

$$x = \frac{V_1(H) - V_1(T)}{S_1(H) - S_1(T)}$$

$$y = \frac{V_1(T)u - V_1(H)d}{(u-d)(1+r)}$$

$$V_0 = xS_0 + y \\ = \frac{V_u(H) - V_d(T)}{S_u(H) - S_d(T)} \cdot S_0 + \frac{V_d(T)u - V_u(H)d}{(u-d)(1+r)}$$

$$V_0 = \frac{1}{1+r} \left[\frac{V_u(H)(1+r-d)}{u-d} + \frac{V_d(T)(u-1-r)}{u-d} \right]$$

Consider $\frac{1+r-d}{u-d}$, $\frac{u-1-r}{u-d}$ as probabilities.

→ Suppose option was worth CH. 21
→ 0.01 aside

$$t=0 \rightarrow 1.2$$

$$\text{Borrow } \rightarrow \frac{0.8}{2.0}$$

Buy $\frac{1}{2}$ stock.

	Stock	Bank	option
S_0	4	-1	-3
T	1	-1	0

→ Now, suppose option price was 1.19

	Stock	Bank	option
$t=1(H)$	4	-1.19(S_{1H})	3
$t=1(T)$	1	-1.19(S_{1T})	

~~$t=1(H)$~~ $\rightarrow 4 - 1.19(S_{1H}) = 3$

(10-11) NLD.

$$x' = rx - x^2 = - \left[x^2 - \frac{2rx}{2} + \frac{r^2}{4} - \frac{r^2}{4} \right] \\ x^* = 0, r = \frac{r^2}{4} - \left(x - \frac{r}{2} \right)^2$$

$$f'(r) = \frac{\partial f}{\partial x} = r - 2rx$$

$$f'(0) = r$$

$$f'(r) = -r$$

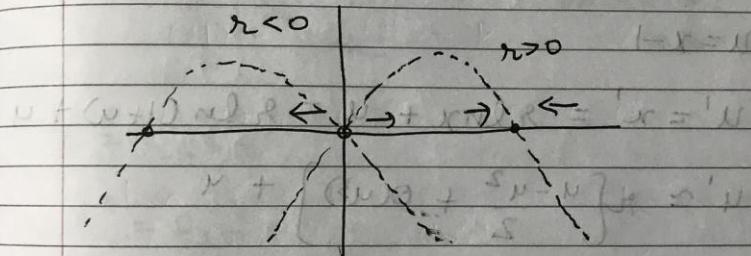
$r > 0$ unstable

$r > 0$ stable

$r \leq 0$ stable

$r < 0$ unstable

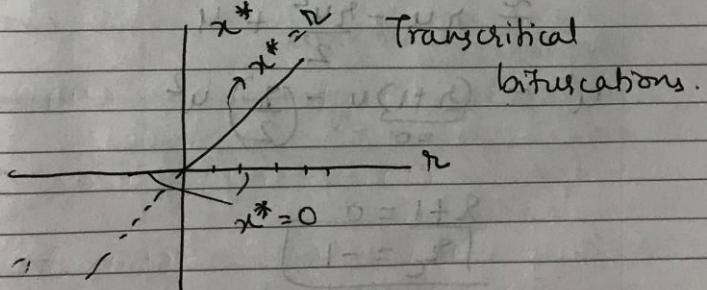
0.1 aside



option

-3

0



Transcritical bifurcations \rightarrow For $r > 0$ x stable y unstable $r = 0$ x & y half stable & $r < 0$ x unstable y stable

$$x' = rx - x^2$$

$$(x-r)(x-x^*) \leftarrow x - x^* = 'x'$$

LASER \rightarrow self organization.*

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$$\frac{dn}{dt} = \alpha((N_0 - \alpha n)^n - kn)$$

$$= (\alpha N_0 - k)n - \alpha n^2$$

$$\frac{dn}{dt} = c_1 n - c_2 n^2$$

$$n^* = 0, \frac{c_1}{c_2}$$

$$n = (c_1 t)^{-1}$$

$$\text{Eq. } x' = r \ln x + u \quad x^* = 1$$

$$u = x - 1$$

$$u' = x' = r \ln x + u = r \ln(1+u) + u$$

$$u' \approx r \left[u - \frac{u^2}{2} + O(u^3) \right] + u$$

$$\approx ru - \frac{ru^2}{2} + u$$

$$u' \approx \underbrace{(r+1)u}_{\approx 0} - \left(\frac{r}{2}\right) u^2$$

$$\begin{aligned} r+1 &= 0 \\ u_c &= -1 \end{aligned}$$

$$x' = r + x^2$$

$$x' = rx - x^2$$

$$x' = rx - x^3 \rightarrow x = -x \text{ (Symmetric)}$$

$x' = rx - x^3 \rightarrow$ supercritical pitchfork bifurcation

$$x^* = 0, \pm \sqrt{r}$$

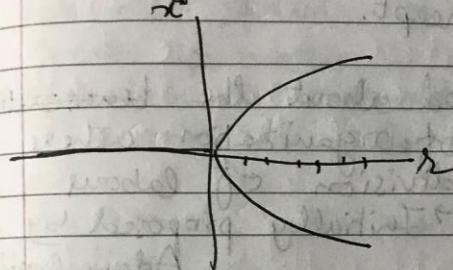
$$f'(x) = r - 3x^2$$

$$f'(0) = r$$

$$, f'(\pm\sqrt{r}) = -2r$$

x^*

Just for $r > 0$ as \sqrt{r} .

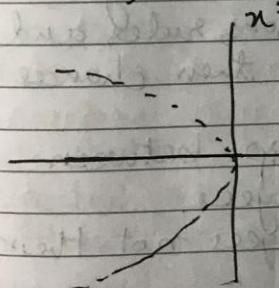


Pitchfork bifurcation.

+ 4

$$x' = rx + x^3$$

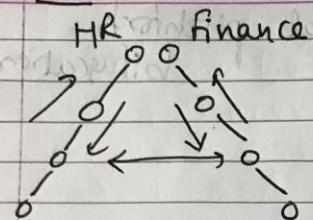
$$x^* = 0, \pm \sqrt{-r}$$



Subcritical pitchfork bifurcation.

(11-12) OB

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Henry Fyol. in diff.
↑ department
people of same level can
talk to each other
Gangplank concept

→ Gangplank concept.

Max Weber explained about the ~~bureaucratic~~ bureaucratic type of organization where

(i) Imp to have division of labour

→ Initially proposed by

Adam Smith

(ii) Imp to have well defined hierarchy.
(who is reporting to whom). (Chain of command)

(iii) Rules & regulations of the organization.

→ If in an organization, rules and roles are properly defined then chances of conflict are less.

(iv) Impersonal relationship between managers and employees.

(Know only employees not their families)

→ They have rational decision making process rather than being influenced by favouritism & personal prejudice.

(v) Competency

→ Promotions, assignments, hiring all is based on competency. If people are competent they are rewarded, awarded.

(v) Records.

→ Believe in keeping all records.

Fredrick Taylor's contribution.

→ exp. about type of payment & work done.

→ Depending on the hours of work, the salary is fixed. No. of hours more, the salary is more.

→ They have framework in org. Comb. of diff. theories adopted in org's.

→ Situational questions based on topics studied

(i) Happy workers need not be productive. Explain

(ii) How does humankind help managers to get desired goals with example?

(iii) Employees at Flash technologies felt constantly demotivated by the behaviour of their new boss Narendra Reddy. Reddy was fond of giving instructions and directing his staff on how to do their work. He expected them to follow his instructions without questioning him. He hated receiving any kind of suggestions from the subordinates. His staff considered him to be a one way communicator. Which type of manager is Reddy? Discuss typical characteristics this type of people have.

20/01/2012

- (i) Happy workers need not be productive.
- There can be two type of workers.
First the ones who are happy because they are working in their field of interest and so they would be happy because of their progress in their work. They will be happy achieving.
- Only those workers who are happy because they are working in their field of interest and they have the proper skillset to work in their field and will always try to achieve the required work will be productive.
- Those workers who are happy because they don't need to complete their work due to any of the reasons like some other worker might be in his team who does the work or there is very less amount of work in his field or maybe he is not inclined for working more in that field then he won't be productive.

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OS (9-10)

→ I/O redirection

→ Normally, output is ~~goes~~ to stdout But if we want to store the output in file named abc then write func() > abc
somepgm > abc (Not displayed just written on file)

→ dup() allows to make changes to file descriptor table.

→ dup() allocates smallest unused file descriptor on passing an oldfd. Copied the pointer.

→ On calling dup(), the file descriptor pointing to a struct. dup() returns fd pointing to same struct. So, we can use any of them.

→ The flags are respective to the file descriptor.

→ Commands for creating opening file with diff. flags.

close(1) → closing stdout
↳ fd for stdout

→ On closing fd 1 we do dup(3).

↳ newfile at 3.
dup finds '1' as the lowest unused fd. So, copies index 3 pointer to 1 fd.

→ So, now fd of stdout points to our file. So, the output will be written in the file.

→ Now, fd 3 pointing to new file will close on close(fd). Only closes the passed fd.

- On calling exec(), the file descriptors will be intact because it is in kernel memory
- So, on system calls for replacing process memory, the things in kernel memory will remain intact.
- We do this everything in child process because otherwise whole shell will get wiped out. So, not to flush out all processes (master process) child processes are cleared ch.40 & work is done.

Inode file system metadata to be stored in the disk only.

64 Blocks → 8 blocks metadata (inode) →
 ↘ 56 blocks data (Data region)
 ↘ 5 blocks inode (file name not stored here)

→ No. of files we can have is equal to the no. of inodes in the memory.

$$\text{inode size} \rightarrow 5 \text{ blocks} = 80 \text{ inodes}$$

↳ if 1 inode = 256 bytes

∴ Max no. of files = 80 files

→ For keeping track of these data blocks & inodes we require two pointers ↘ called

bitmap.

→ One bit per node & one bit per datablock required originally.

→ Block of nodes is called super block. It stores metadata for whole filesystem.

model & Sim (12-1)

will be
l memory
process
memory will
decrease

process
will get
all process
are cleared

red in the

(a region)
name not
stored here)

equal to the
nodes
↳ if 1 node
= 256 bytes

blocks &
trees
called
bitmap.
datablock
lock. St
system.

$$\frac{dx}{dt} = rx \left(1 - \frac{x}{k}\right) \quad (i) \text{ Model for } k$$

(ii) Quantitative

(iii) why fig ①?

(iv) what if system is discrete?

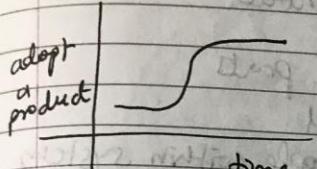
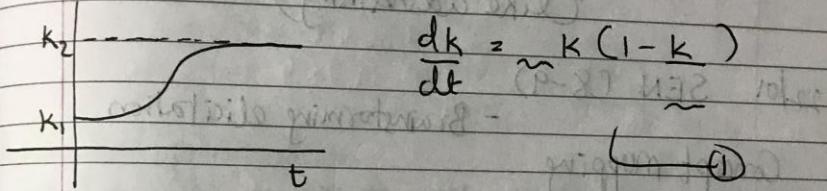


fig ①

$$\frac{dk}{dt} = r k (1 - k) \quad (1)$$

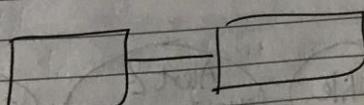


→ $\frac{dx}{dt} = rx \left(1 - \frac{x}{k}\right) \rightarrow$ In this eqⁿ we find two points using

$$\frac{dx}{dt} = 0 \quad x = 0, k$$

So, here we want $x = k_1, k_2$
eqⁿ ①

→ finding the constants, we can change one eqⁿ into two coupled eqⁿ and can be considered as two compartments.



$$\frac{dk}{dt} = r(k - k_1)(1 - \frac{k}{k_2}) \quad \frac{dx}{dt} = rx \left(1 - \frac{x}{k}\right)$$

↳ shouldn't there be $[k - k_1]$?

$$N(t + \Delta t) = N(t) + N \times f(C) \frac{(C - N) \times \Delta t}{C}$$

$$\frac{dN}{dt} = f(N) \frac{(C - N)}{C} \quad \left. \begin{array}{l} \text{Bass} \\ \text{Model} \end{array} \right.$$

Splits problem into 2 parts

(i) External (ii) Internal

↳ Any

external influence

(like advertising)

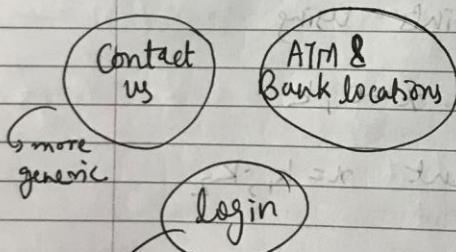
Δt

22/01 SEN (8-9)

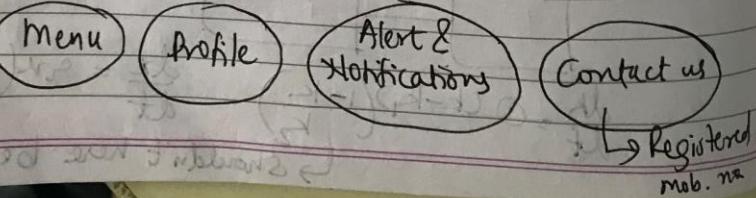
- Brainstorming elicitation

Concept mapping

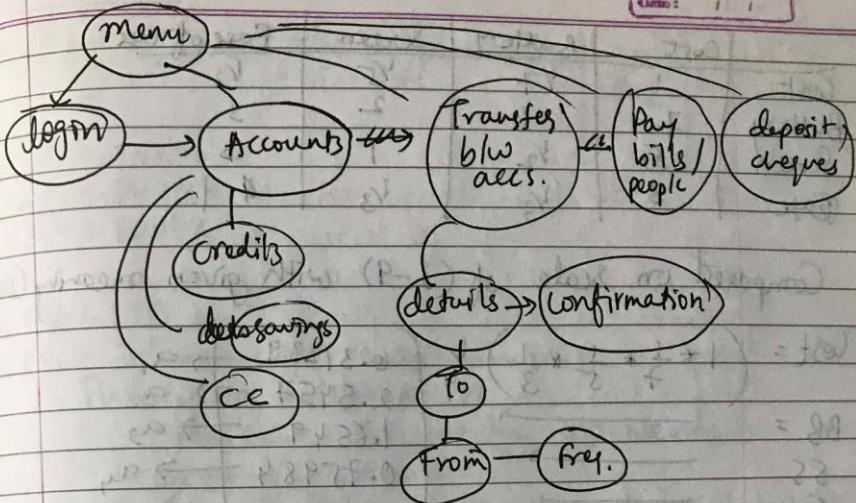
Logout and login



Should be generic/compatible to update for sec
After login



* Concept Mapping



Requirements prioritization

Why? → Can't go through all requirements in single code.

1. Ranking (Individual)

2. Numerical assessment (Grouping) [Ranking to groups]

3. MoSCoW

must have should have could have won't have would

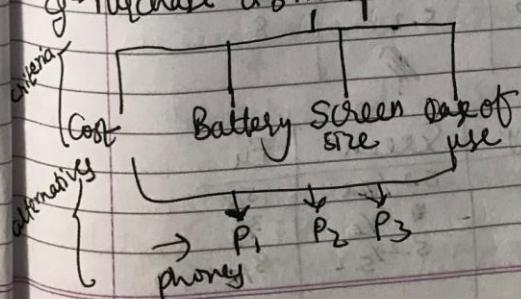
4. Bubbles sort [Compare two ref. & prioritize]

(largest no. in array give to stakeholders & prioritize)

5. Hundred Dollar method [prioritize based on their investments in the requirements]

6. Analytical hierarchy process

Eg - Purchase a smartphone



	Cost	Battery	Screen	Ease of use
Cost	1	4/7	1/5	1/3
Battery	7	1	2	3
Screen	5	1/2	1	3
Base	3	1/3	1/3	1/1

Compared on scale of (1-9) with given meaning (Aides)

$$\text{Cost} = \left(1 * \frac{1}{7} * \frac{1}{5} * \frac{1}{3} \right)^{1/4} \quad \left[\begin{array}{l} 0.31239 \\ 2.5457 \\ 1.6549 \\ 0.75984 \end{array} \right] \rightarrow a_1, a_2, a_3, a_4$$

$$BB = \xrightarrow{\quad}$$

$$SS = \xrightarrow{\quad}$$

$$EU = \xrightarrow{\quad}$$

normalize by dividing by 5.2728

sum all of them = 5.2728

weights $\rightarrow A_2 = \left[\begin{array}{l} a_1/s \\ a_2/s \\ a_3/s \\ a_4/s \end{array} \right]$

Cost Battery Screen EU

sum should be 1.

	Cost	Battery	Screen	EU
P ₁	18000	4000	5.6	5
P ₂	11000	3000	6	3
P ₃	16000	25000	5.2	8

	Cost	Battery	Screen	EU
P ₁	11/15	4/4	5.2/5.6	5/8
P ₂	11/11	3/4	6/6	3/8
P ₃	11/16	2.5/4	5.2/5.2	8/8

$$P_1 = \left(\frac{11}{15} + \frac{4}{14} + \frac{5.2}{6} + \frac{5}{8} \right) \times 0.0592 \quad [A_2]$$

$$P_1 = 0.90774$$

$$P_2 = 0.7474$$

$$P_3 = 0.80043$$

why (slides)

OB (10-11)

last lec - Human skills help managers.

- Theory of Motivation

↳ Maslow's Hierarchy of Needs

↳ Iceberg metaphor

↳ Henry Fayol's theory

↳ Henry Herzberg's managerial roles

↳ OB model

- Cognitive Dissonance

↳ We keep on procrastinating

Communication

↳ Inconsistency in people

↳ Body Meaning?

↳ about belief systems

→ Maslow's Hierarchy of Needs

Self actualization (personal growth)

↑
Esteem needs (status, achievement, responsibility)

↑
Love needs (family)

↑
Safety needs (Security, Investment, LTC)

Biological & Physiological needs

→ must for everyone (Roti, Kapda, Matka)

- Henry Fayol's Traditional theory of management
- Henry Herdsberg : key managerial roles.

OB Model:

This model explains structure of functioning style & working, performance & people dependent on structure, functioning performance how people are at work.

- Style & func. is what in OB model depending on it, understanding human behaviour.

4 OB models

→ Autocratic

- Eg - Based on power, money, authority
- Based on hire & fire policy
- Don't try to act smart.
- Always dictating manager
- Dependence on boss (Boss is right)
- Employee needs are subsistence
- Performance is minimum.
- I will not show creativity not happy in organization

Custodial

- It is based on economic resources i.e. money oriented.
- I throw money & you have to work
- Security & benefits
- Dependency is on the organization.
- I have money i.e. more than expectation
- passive cooperation (Jata hai ne sir)

Supportive

- I will help you let form good team.
- Support
- I am allow to show creativity.
- I participate in organization.
- I am happy in organization
- I am having status, recognition.
- My initiative to work in organization
(Not push to go to office)
- Doing work happily (Awakened drives)
~~& moderate~~

Collegial

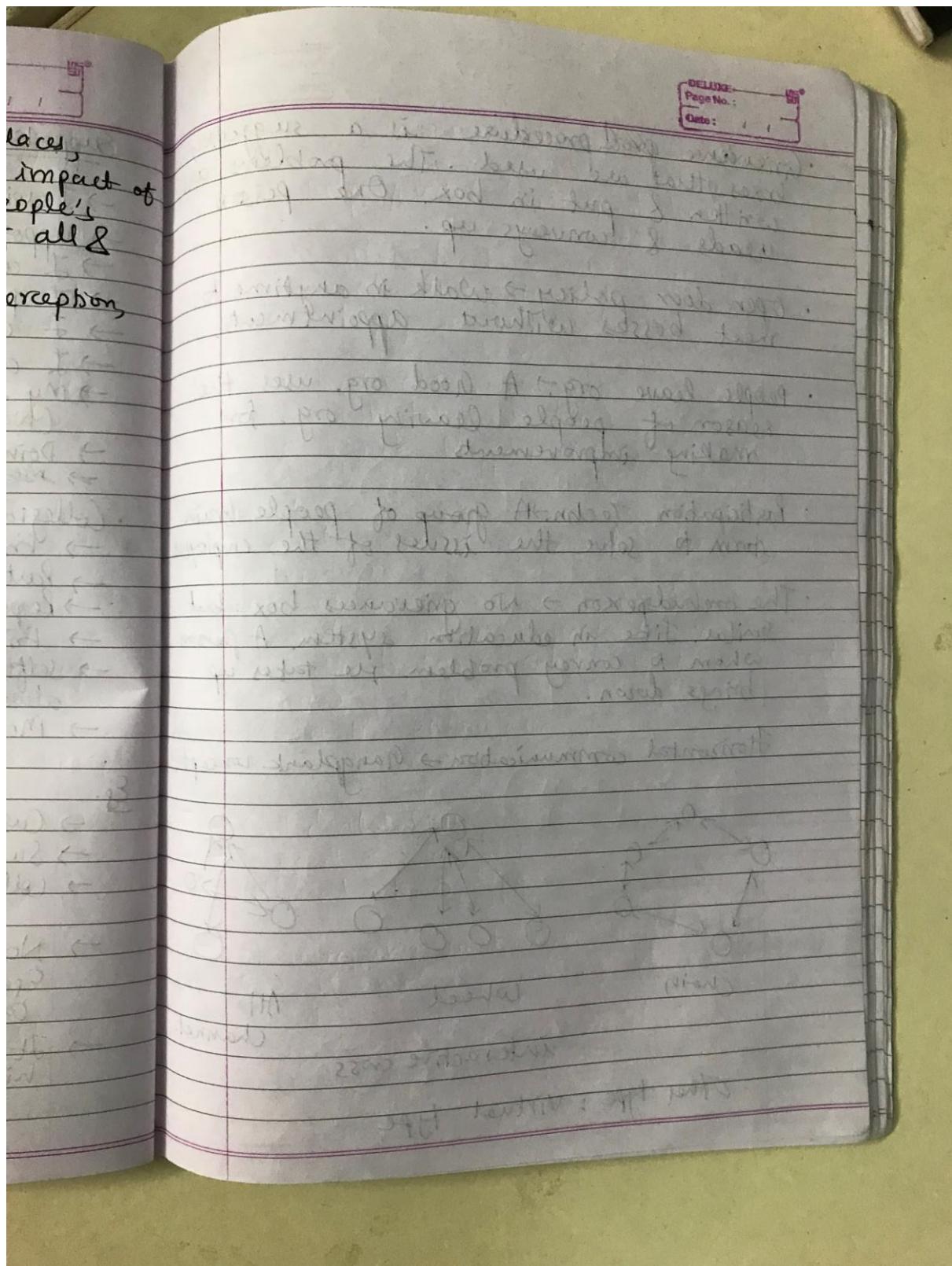
- Friend in need is friend indeed.
- Partnership
- Responsible behaviour
- Friendship plays important role.
- Self actualization (Friend doesn't hold hand always)
- Moderate enthusiasm

Eg.

- Custodial : IBM
- Supportive : Tata, HP
- Collegial : R&D type

- No company works on single model.
Eg - Finance dept. works as custodial, HR
works as supportive.
- It is mixture of these models. This is a
hidden aspect of OB.

- According to diff. situations, diff. places, people to people, behavioral diff., impact of the model is dependent on people's behavior. So, it is combination of all & not single way of functioning.
- Understanding people's behavior, perception,



(11-12)

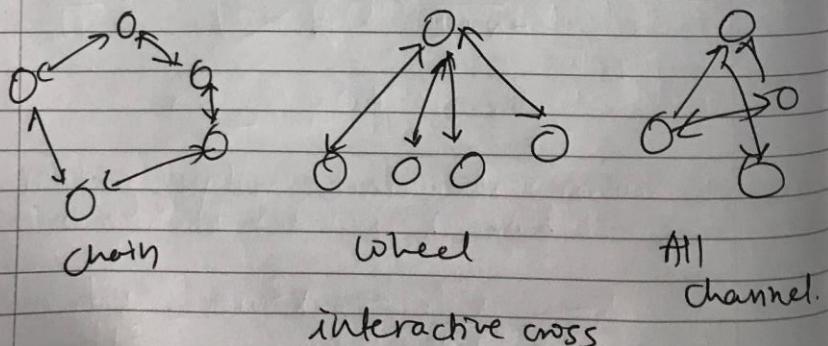
Question

Ch.3

Grievance procedure is a suggestion boxes that are used. The problems are written & put in box. One person reads & conveys up.

- Open door policy → Walk in anytime to meet bosses without appointments.
- People leave org. → A good org. uses the season of people leaving org. for making improvements
- Participation Techn. → A group of people brain storm to solve the issues of the employees.
- The ombudsman → No grievances box but similar like in education system. A person whom to convey problem. He takes up brings down.

Horizontal communication → Gangplank concept.



Other type : Virtual type

(11-12) NLD & Chaos Steven Strogatz.

Questions for exam Ch.2 Flow on a line

$$2.2.1 - 2.2.7$$

$$2.2.12, 2.2.13$$

$$2.3.1 - 2.3.4$$

$$2.4.1 - 2.4.8$$

Also, plotting functions

Ch.3

Bifurcation

$$3.1.1 - 3.1.5$$

$$3.2.1 - 3.2.4$$

$$3.3.1 \leftarrow$$

$$3.4.1 - 3.4.10$$

$$3.4.11 \leftarrow$$

$$3.4.15$$

$$3.6.2^*$$

$$3.7.3$$

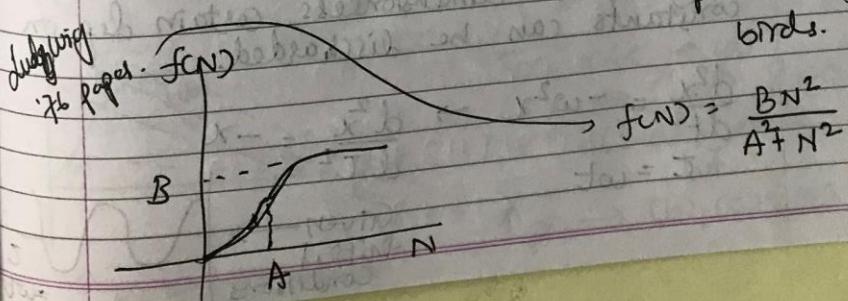
$$3.7.6$$

Insect outbreak problem -

Spruce budworm
N - Number density of insect.

$$\frac{dN}{dt} = r_2 N \left(1 - \frac{N}{K}\right) - f(N)$$

due to predation by birds.



$$f(N) = \frac{BN^2}{A + N^2}$$

n^* vs. γ phase-space diagram
Bifurcation diagram

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$$\frac{dN}{dt} = rN\left(1 - \frac{N}{K}\right) - \frac{BN^2}{A^2 + N^2}$$

- Two variables: N & t
- "make these two dimensionless. In the procedure hope that no. of parameters come down."

Take: $n = \frac{N}{N_0}$ $\tau = \frac{t}{t_0}$

$$\frac{N_0}{t_0} \frac{dn}{d\tau} = rN_0 n \left(1 - \frac{nN_0}{K}\right) - \frac{BN_0^2 n^2}{A^2 + N_0^2 n^2}$$

$$\frac{dn}{d\tau} = r t_0 n \left(1 - \frac{n}{K/N_0}\right) - \frac{B t_0}{N_0} \left[\frac{n^2}{A^2 + \frac{N_0^2}{n^2}} \right]$$

Let $N_0 = A$, $t_0 = \frac{A}{B}$, $r = \frac{rA}{B}$, $k = \frac{k}{A}$

$$\frac{dn}{d\tau} = rn \left(1 - \frac{n}{k}\right) - \frac{n^2}{1+n^2}$$

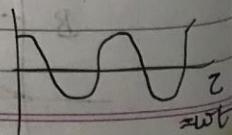
γ & k to worry.

→ Making system dimensionless, certain dep. on constants can be discarded.

$$\frac{d^2x}{dt^2} = -\omega^2 x \rightarrow \frac{d^2x}{d\tau^2} = -x$$

$$\tau = \omega t$$

Given
Initial
Conditions



$$\frac{dn}{dt} = rn\left(1 - \frac{n}{k}\right) - \frac{n^2}{1+n^2}$$

(i) Fixed points $n^* = 0$,

$$rn\left(1 - \frac{n}{k}\right) - \frac{n^2}{1+n^2} = 0.$$

$$\text{or } r\left(1 - \frac{n}{k}\right) - \frac{n}{1+n^2} = 0 \text{ and } n=0.$$

$\frac{r^2 n^2}{1+n^2}$

$+ N^2 n^2$

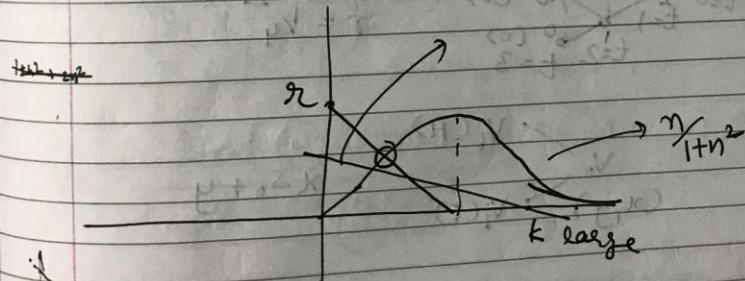
$$\begin{bmatrix} n^2 \\ A\frac{N^2}{n^2} + n^2 \end{bmatrix}$$

$$, k = \frac{A}{N}$$

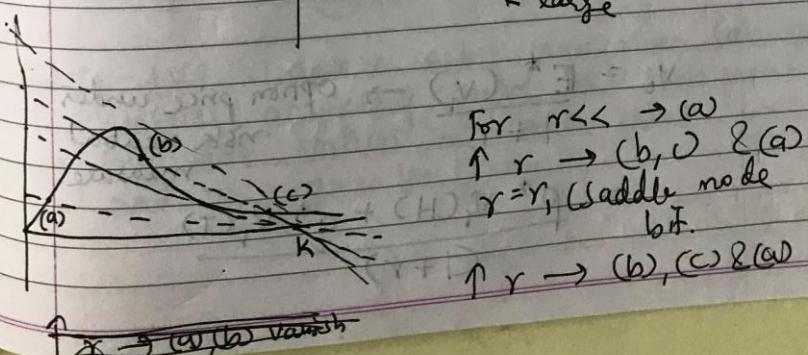
$n^* \neq 0 \rightarrow$ unstable as close to zero 'rn',
So exponentially diverging.

$$r\left(1 - \frac{n}{k}\right) = \frac{n}{1+n^2} \quad n \ll 1$$

$$n \gg 1$$

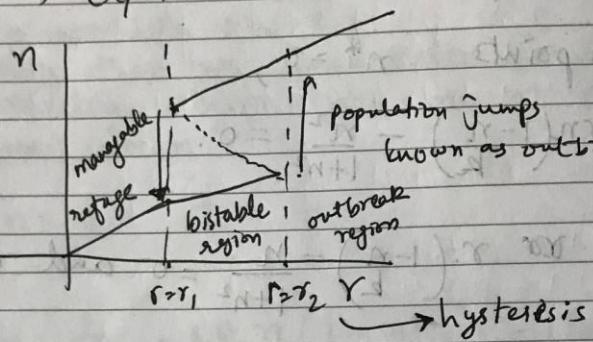


dep. on



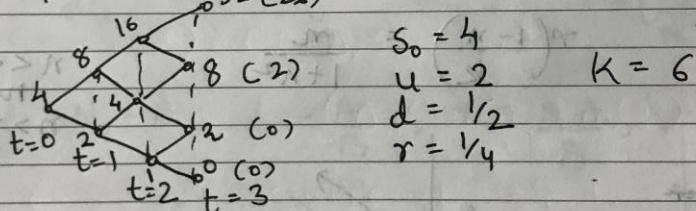
$$r = r_2 \rightarrow (a, b) \text{ & } (c)$$

$\uparrow r \rightarrow (a, b) \text{ vanishes } \& (c)$

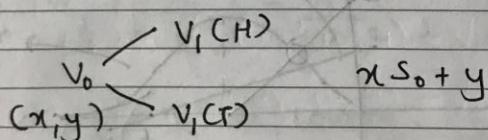


(12-1) Comp. Finance

multi period binomial model



$$\begin{aligned} S_0 &= 4 \\ u &= 2 \\ d &= 1/2 \\ r &= 1/4 \end{aligned}$$



$$V_0 = \frac{E^*(V_1)}{1+r} \rightarrow \text{option price under risk neutral measure.}$$

$$= \frac{p^* V_1(H) + q^* V_1(T)}{(1+r)}$$

$$p^*, q^* = \frac{1}{2} \quad \frac{1+r-d}{u-d} \text{ (risk neutral measure)}$$

$$V_2(HH) = p^* V_3(HH) + q^* V_3(HT)$$

$$V_2(HH) = \frac{p^* V_3(HH) + q^* V_3(HT)}{1+r}$$

break.

$$V_2(HT) = V_2(TH)$$

$$= \frac{p^* V_3(TH) + q^* V_3(HT)}{1+r}$$

is

$$(r+1) = \frac{1/2(2) + 1/2(0)}{5/4}$$

$$= 4/5$$

$$k = 6$$

$$* V_0 = \frac{\mathbb{E}^*(V_6)}{(1+r)^6}$$

$$V_0 = \frac{26 \cdot \left(\frac{1}{2}\right)^3 + 2 \cdot \left(\frac{1}{2}\right)^3 \cdot 3}{\left(\frac{4}{5}\right)^3}$$

under
neutral
measure.

→ If diff. interest rates are given. Calculate values according to r at each point.

→ Also, diff. values at each level for r , and ' u ' can be given.

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Multiperiod model

$$V_{n+1} = (V_n - \Delta_n S_n)(1+r) + \Delta_n S_{n+1} \quad] \text{Hedging argument}$$

Δ_n = amt. of stock at time n

$\Delta_n S_n$ = Total value of stock

V_n = Option price at time n

$V_n - \Delta_n S_n \rightarrow$ put in bank

$$V_{n+1}(\omega_1, \omega_2, \dots, \omega_n H) = (V_n - \Delta_n S_n)(1+r)$$

$$+ \Delta_n S_{n+1}(\omega_1, \omega_2, \dots, \omega_n H) \quad \boxed{1}$$

$$V_{n+1}(\omega_1, \omega_2, \dots, \omega_n T) = (V_n - \Delta_n S_n)(1+r)$$

$$+ \Delta_n S_{n+1}(\omega_1, \dots, \omega_n T) \quad \boxed{2}$$

where ω_i are sequence of H & T .

$$\Delta_n(\omega_1, \dots, \omega_n) = \frac{V_{n+1}(\omega_1, \dots, \omega_n H) - V_{n+1}(\omega_1, \dots, \omega_n T)}{S_{n+1}(\omega_1, \dots, \omega_n H) - S_{n+1}(\omega_1, \dots, \omega_n T)}$$

$$\text{where } \gamma = \frac{V_1(H) - V_1(T)}{S_1(H) - S_1(T)}$$

Stock holding at time n :

$$\rightarrow \text{eq } \boxed{1} \times p^* + \text{eq } \boxed{2} \times q^*$$

edging
argument
~~arg~~ (1)

$$\begin{aligned} & p^* V_{n+1}(w_1, w_2, w_3, \dots, w_n, H) + q^* V_{n+1}(w_1, \dots, w_n, T) \\ &= (V_n - \Delta_n S_n)(1+r) + p^* \Delta_n S_{n+1}(w_1, \dots, w_n, H) \\ &\quad + q^* \Delta_n S_{n+1}(w_1, \dots, w_n, T) \\ &= V_n(1+r) - \Delta_n S_n(1+r) + \Delta_n [p^* S_{n+1}(w_1, \dots, w_n, H) \\ &\quad + q^* S_{n+1}(w_1, \dots, w_n, T)] \\ &\rightarrow p^* S_{n+1}(w_1, \dots, w_n, H) + q^* S_{n+1}(w_1, \dots, w_n, T) = \frac{S_n(1+r)}{\square} \end{aligned}$$

) Arg.-return from stock market

\simeq Money obtained by investing
in bank

Risk-Neutral defⁿ.

$$\therefore V_n = \underline{p^* V_{n+1}(w_1, w_2, \dots, w_n, H) + q^* V_{n+1}(w_1, \dots, w_n, T)}$$

\downarrow spent in H $|+r$

\downarrow $V_n = V_n(w_1, w_2, \dots, w_n)$ [Random variable]

V_0 only is not a RV. (fixed value paid)

$$E^*(S_1) = S_0(1+r)$$

$$E^*(S_{n+1}) = S_n(1+r)$$

23/1/20

(9-10) Modelling & Sim.

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$$\frac{dN}{dt} = \left(p + \frac{qN}{c} \right) (C - N(t))$$

↓
Total pop.

$q = 0 \rightarrow$ No interaction &

with time $N(t) \rightarrow C$.

$p = 0 \rightarrow$ Logistic system

\rightarrow External → Anything that motivates an individual to adopt.

$q \rightarrow$ Internal.

Epidemiology (Spread of virus) (SIR)

↳ comp. virus also

↳ rumours spread.

S → Susceptible

I → Infected

R → Recovered

N is large [Incubation period]

$S \rightarrow I \rightarrow R$

No death &

No birth

So, $N = S + I + R$ const.

[Latent period]

[Not consider]

$$\frac{dS}{dt} = CPS \frac{I}{N}$$

$$\frac{dI}{dt} = CPS \frac{I}{N} - \gamma I$$

$$\frac{dR}{dt} = \gamma I$$

Jit Ho
Gaffe
that i
will
cont. ↓

$C \rightarrow$ No. of contacts each individual made per unit time

$$\rightarrow C \times S \times p \times I$$

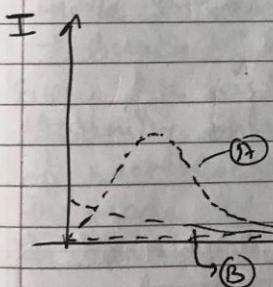
\hookrightarrow prob. with which a susceptible takes virus

$$\rightarrow \beta_f = C p, \quad \beta = \frac{\beta_f}{N}$$

$$\therefore \frac{dS}{dt} = -\beta S I$$

$$\frac{dI}{dt} = \beta S I - \gamma I$$

$$\frac{dR}{dt} = \gamma I$$



(Can show any behaviours like (A) & (B).)

There exists a critical value for which we see the behaviour changing from (B) to (A).

$$\frac{dI}{dt} = \gamma I \left(\frac{\beta_f S_0}{\gamma} - 1 \right)$$

Initially

Gaffer
that it
will
cont. ↓

$$\frac{\beta_f S_0}{\gamma} \geq 1$$

Initially most of the pop. will be susceptible. So, can be considered ≈ 1 .

$$R_0 = \frac{\beta_f}{\gamma} \quad (\text{Basic Reproduction Number})$$

$\frac{S}{N} \beta t \rightarrow R_0 = \text{effective reproduction number}$

Isolate \rightarrow wash hands.

\rightarrow vaccine

\rightarrow medicine

$\frac{1}{\tau} = \text{avg. time individual remains infected.}$

How many susceptibles will be infected by an infected individual over the time the individual remains infected.

SEN (10-11)

Actors

- Cashier
- Customer
- Store
- Catalogue system
- Inventory system

Customer → stakeholder

Use cases:

- Handle sales
- Pay in cash, Credit card or cheque
- Issue gift coupons
- Handle returns

Cashier

Print

Gift
coupons

Actions →
Use case de

(2-1) OS

→ Inc

→ Ever

→ Ass

of

→ Fun

for

→ In

of

inc

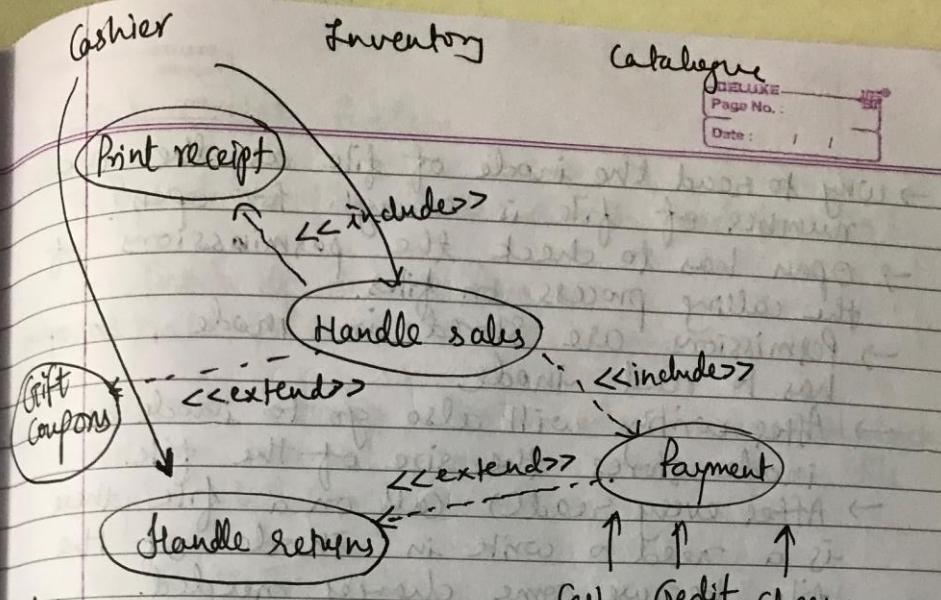
→ Inc

the

→ Rea

c

→ Ope



Actors → Use cases → diagrams Cash Credit Cheque

Device description ←

(b-1) 09

- Inode for root is fixed.
 - ↳ Bunch of location pointers of all datablocks
 - Every file has exactly one inode. datablock of root
 - Assuming only one block, read one block of root located using direct pointer present in inode of root.
 - In datablock of root there will be a pointer to inode of foo(directory)
 - In datablock of root, we find directory of foo. The directory file of foo will tell inode no. for bar.
 - Inode no. for foo is determined from the datablock of root
 - Read inode for foo → corresponding data block
 - entry for inode of bar.
 - Open also reads the inode of bar. (?)

- Why to read the inode of file as the inode number of file is enough for open?
- Open has to check the permissions of the calling process on files.
- Permissions are stored in inode, so open has to read inode.
- After writing will also go to inode as inode stores the size of the file.
- After every read() call on a file there is a need to write in inode of the file because some changes needed.
 - ↳ last time accessed.
- timestamps of the files called the dugh system calls are only updated.
- What happens when we write 0 bytes?
 - ↳ Try this, play with inode.

LFS, FFS (Book chapters)

Issues: Write a file. How to know which block to be allocated. Allocation policies

(Create) → read inode bitmap → which inode free →
allocate → write inode bitmap

Allocate a new block → need to update inode
 Space in available block → no need to update
 But size is stored in inode. So, we need to always change
 size of inode of B.

consistent Update Problem

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→ Appending a file, what blocks need to write?

Inode of file → filesize

Allocate Data-block → Data Bitmap

• data bitmap, file's inode, new datablock.
Ordering can be done in any way by file system. We can't do anything!

24/01/20 NLD (10-11).

$$\frac{dn}{dt} = \frac{rn}{R} \left(1 - \frac{n}{R}\right) = \frac{n^2}{1+n^2}$$

$$r = \frac{rA}{B}, R = \frac{k}{A}, n = \frac{N}{A}, t = \frac{tA}{B}$$

$n^* = 0 \rightarrow$ unstable.

$$r \left(1 - \frac{n^*}{R}\right) = \frac{n^*}{1+n^*}$$

$$(i) r \left(1 - \frac{n^*}{R}\right) = \frac{n^*}{1+n^*} \quad \begin{matrix} \text{solve} \\ \text{buffer}^n \end{matrix}$$

$$(ii) -\frac{r}{R} = \frac{(1+n^*) - 2n^*}{(1+n^*)^2} \quad \begin{matrix} \text{become} \\ \text{tangent} \end{matrix}$$

↳ so slopes equal.

Solving for r

$$r = \frac{2n^{*3}}{(1+n^{*2})^2} \quad R = \frac{2n^{*3}}{n^{*2}-1}$$

r

outbreak → $r \downarrow \rightarrow$ one fixed point refuge
 $r \uparrow \rightarrow$ outbreak

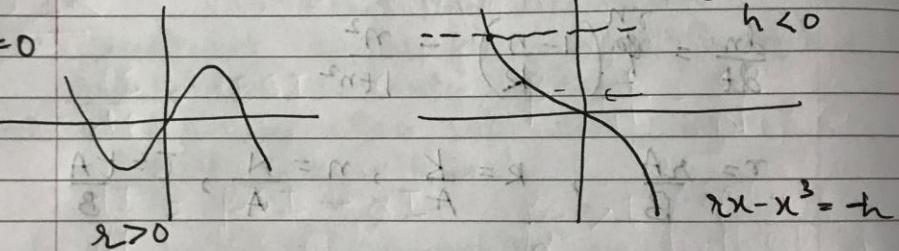
Boundaries → value of r & k
for which we get saddle node
bifurcation.

→ In parameter space, we can know the behaviour.

Imperfect Bifurcation

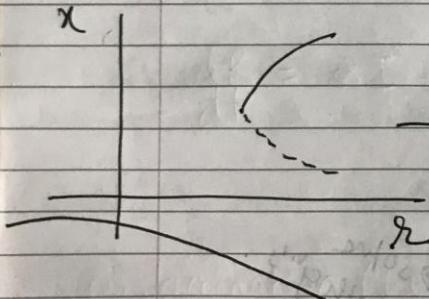
$$x' = h + rx - x^3$$

$$h=0$$



$$r < 0$$

$$h < 0$$



Such bifurcations are called
imperfect bifurcation.

happens when there is
symmetry breaking.

$$x' = rx - x^2 - h$$

$$- \beta x$$

$$- \beta x^2$$

- (i) Fixed points
- (ii) Stability
- (iii) Trajectory

- (iv) Bifurcation
→ No imperfect bif.

OB (11-12)

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Grapevine Characteristics

→ Finding out-of-information (through some trusted students) is known as Grapevine.

Rumours

(i) Spontaneous rumours

→ Rumours which spread during times of stress & are action oriented.

(ii) Predominated rumours

→ These rumours are deliberately created.
highly competitive. Create disturbance among people.

(iii) Wish fulfillment or pipe dream rumours

→ Unfulfilled desires in terms of rumors

(iv) Anxiety or bogey rumours → due to fear

→ Reallocation, change transfers, work assignment.

(v) Wedge drivers

→ Negative rumours and because of hatred, aggression towards people or work.

→ They can easily go away when the management addresses the people properly.

(vi) Home stretchers

→ Rumours are from ambiguity.

→ Delay from management to pass the information.

→ Not clear information, one right decision

✓ → dangerous rumours.

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vii) Curiosity rumours

→ originated due to curiosity among people.

How to deal with rumours?

(i) Communicating with people addressing them

(ii) Grapevine to find source

(iii) Deal with source

(iv) Pay attention to type of rumour

ModSim C12-1D

SIR - (China Kala virus)

$$\frac{dS}{dt} = -\beta SI$$

$$\beta = \frac{\beta_f S}{N} = \frac{\beta_f}{N}$$

$$\frac{dI}{dt} = \beta SI - \alpha I$$

$$\frac{\beta_s}{\alpha} > 1 \quad (\text{epidemic threshold})$$

$$\frac{dR}{dt} = \alpha I$$

$$\frac{\beta_f S}{\alpha N} > 1$$

$$R_0 = \frac{\beta_f}{\alpha} \quad (\text{Basic repr. no.})$$

(i) Vaccination (herd immunisation)

Trying to move certain fraction of

susceptibles & moves them to recovered.

ρ : fraction of susceptibles that are vaccinated.

$$\frac{R_0}{N} (1-\rho) S(0) < 1 \quad (\text{vaccinate much people so that epidemic doesn't happen})$$

we want to bring down below threshold.

$$(1-\beta) < \frac{N}{R_0 S(0)}$$

$$1-\beta < \frac{1}{R_0} \quad (\because S(0) \approx N \text{ (since } N \text{ very large)})$$

$$\beta > 1 - \frac{1}{R_0}$$

Suppose, $R_0 = \frac{3}{2} \rightarrow \beta > \frac{1}{3}$ (more than $\frac{1}{3}$ pop. should be vaccinated) (But, vaccination expensive)

$\rightarrow \alpha$ calculated using data available for time required for diff. people to recover.

\rightarrow Expected value of time distribution is $1/\alpha$.

$$\frac{ds}{dt} = -\beta SI ; \frac{dI}{dt} = \beta SI - \alpha I ; \frac{dR}{dt} = \alpha I$$

$$\frac{ds}{dt} = -\frac{\beta s}{\alpha} = -\frac{R_0}{N} s$$

$$\ln \frac{s(t)}{s(0)} = -\frac{R_0}{N} [t - t(0)]$$

$$\frac{s(t)}{s(0)} = e^{-\frac{R_0}{N} [t - t(0)]}$$

$$\lim_{t \rightarrow \infty} \frac{s(t)}{s(0)} = \frac{s(\infty)}{s(0)} = e^{-\frac{R_0}{N} [\infty - t(0)]}$$

Assume, initially all are susceptibles $s(0) = 1$

$$\frac{S(\infty)}{N} = e^{-\frac{R_0 R(\infty)}{N}}$$

$$N = S + I + R$$

$t \rightarrow \infty \quad N \approx S + R$ (No infected)

$$\frac{N - R(\infty)}{N} = e^{-\frac{R_0 R(\infty)}{N}}$$

$$\text{Let } \frac{R(\infty)}{N} = r$$

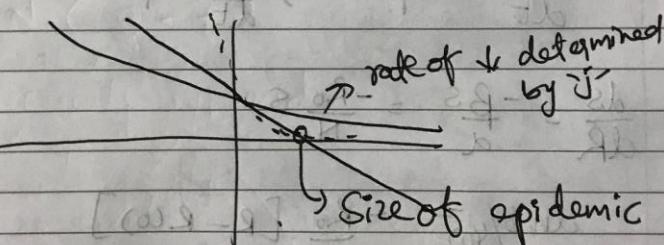
$$1 - r = e^{-R_0 r(\infty)}$$

\rightarrow At $t = \infty$ everybody infected will be recovered.
So, $r(\infty) = \text{Size of epidemic}$

$$1 - r(\infty) = e^{-R_0 r(\infty)}$$

Given $R_0 \rightarrow$ we can find $r(\infty)$ (Size of epidemic)

$$1 - r = e^{-jx}$$



$$S + I + R = 1 \quad (S = \frac{S}{N} \text{ soon})$$

$$t \rightarrow \infty \quad I(t) \rightarrow 0$$

$$S(\infty) + R(\infty) = 1$$

\rightarrow All the susceptibles will not be infected. But after a time all $I \rightarrow R$ so no longer infected people not absence of susceptibles

$$\frac{dS}{dI} = \frac{\beta SI}{\alpha I - \beta SI} = \frac{\beta S}{\alpha - \beta S} = \frac{\frac{\beta}{\alpha} S}{1 - \frac{\beta}{\alpha} S}$$

$$\frac{\beta}{\alpha} = \frac{R_0}{N}$$

$$\int ds \left(1 - \frac{R_0}{N} S \right) = \frac{R_0}{N} \int dI$$

$$\ln S - \frac{R_0}{N} (S + I) = \text{Const.}$$

$$= \ln(S(0)) - \frac{R_0}{N} [S(0) + I(0)]$$

\rightarrow conserved quantity

$$S(\infty) > N$$

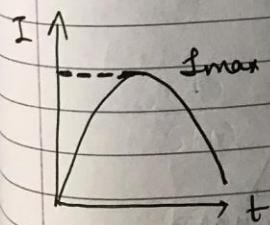
$$I(\infty) = 0.$$

$$\ln(S(\infty)) - \frac{R_0}{N} (S(\infty) + I(\infty)) = \ln S(0)$$

$$I(\infty) = 0$$

$$\ln \left(\frac{S(\infty)}{S(0)} \right) = R_0 \left(\frac{S(\infty)}{N} - 1 \right)$$

$$R_0 = \frac{\ln \frac{S(\infty)}{S(0)}}{\frac{S(\infty)}{N} - 1} \quad R_0 = \frac{\beta f}{\alpha}$$

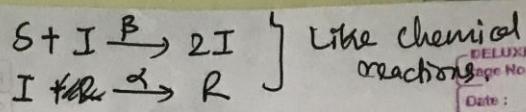


$$\left. \frac{dI}{dt} \right|_{I_{\max}} = 0$$

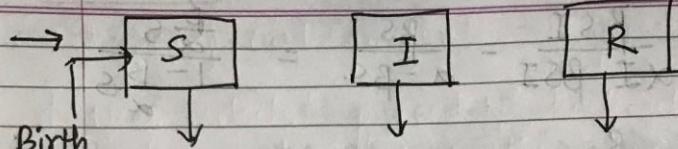
$$\beta SI - \alpha I = 0$$

$$S = \frac{\alpha}{\beta} = \frac{N}{R_0}$$

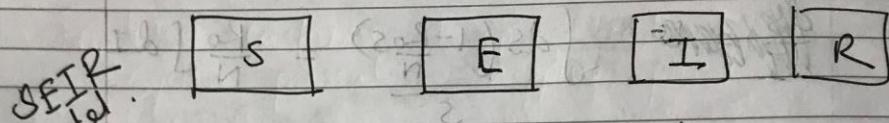
But
ger
reptibles



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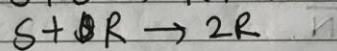
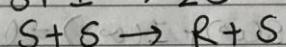
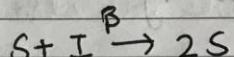


→ More the no. more the birth & more the death.



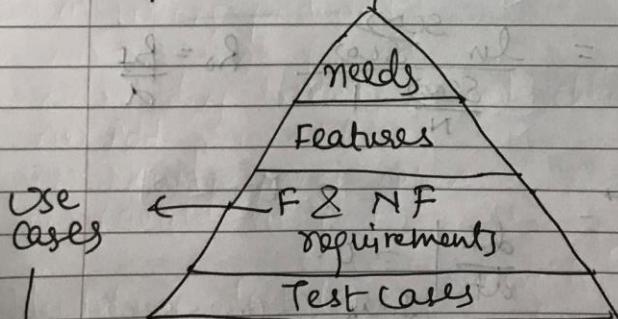
$I + S \rightarrow S$ becomes Exposed.
Time gap between S & I. Exposed.

$I \rightarrow$ Ignorant, $S \rightarrow$ spreader, $R \rightarrow$ stifles



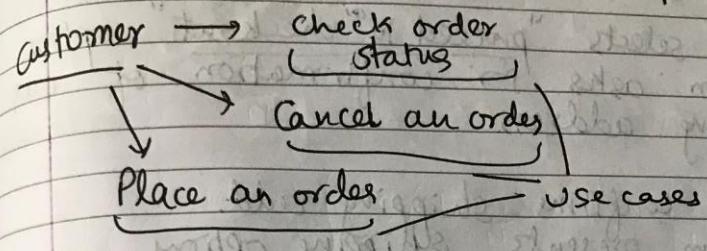
~~SEN (5-7)~~

Requirements Pyramid



Differentiate between Scenario & functionality
(entire pin) (validation of pin)

→ Testers have access to requirements/specification only.



Use case Name: Place an order
Actor: Customer / User

basic flow: → 1, 2, 3, 4... are scenario's.

- 1. User enters website address in the browser.

System displays login page.

2. User enters an email address and a password. [email, password]

System confirms correct login, presents main page, prompts for a search string.

3. User enters search string (partial name of the book) [Book-name searched]
System returns all books matching search string.

4. User selects a book.
System presents detailed information about the book. [Book-name-selected]

5. User adds the book to a shopping cart.

Shopping cart contents is presented to user.

6. User selects "proceed to checkout" option.
System asks for confirmation of user shipping address.
7. User confirms shipping add.
System presents shipping options.
→ Normal, fast, single day
8. User selects shipping options and system asks which credit card to use.
9. User confirms credit card info.
System asks for final confirmation to place an order.
10. User places and order.
System returns a confirmation number.

Many alternative flows

- (i) Wrong password
- (ii) No book found
- (iii) Adding to cart doesn't checkout
- (iv) Add new address
- (v) New payment option
- (vi) Cancels at end

Identifying test cases [System level test cases]

- (i) Identify variable name for each use case step. (Steps of basic flow)

user.
ID Identify significantly different options for each variable.

Steps	Variables	options to be tested
1	website	Actual website
2	Email password	Regular → Blank? → Char reg (max 8 min) Regular → @ reg. → check from requirements Blank → Char min & max
3	Search string	Regular → Blank Char reg. One more allowed
4	Selection	First Selection Different selections
5	Action selection	Add to cart Check for checkboxes.
6	Action selection	Proceed to checkout

One more allowed] → Maximum errors are at boundaries.
So we need to check boundaries.
(corner cases)
→ Errors for '1' instead of '0' etc.

7. Shipping address → confirm address

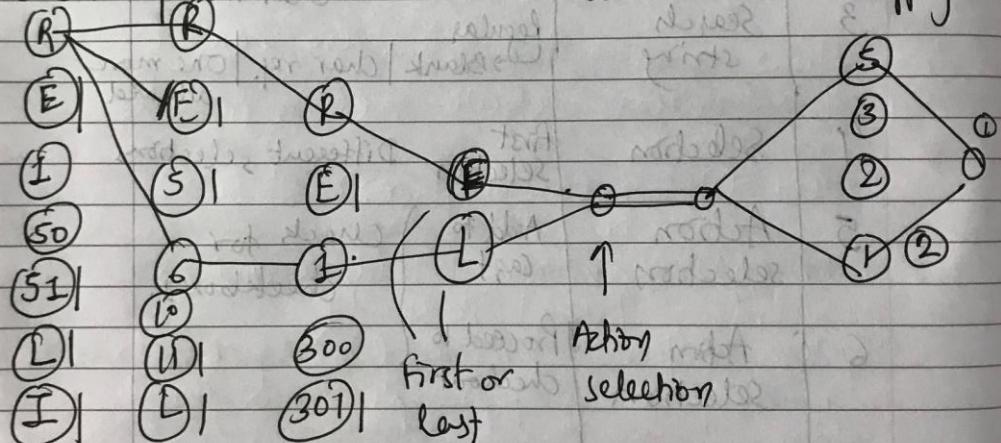
8. Shipping method → 5 days, 3 days, 2 days, 1 day

9. Payment method → CC in a file

10. Final selection → Place an order.

(iii) Combine options to be tested into testcases.

email pass. search book add. checkout shipping ord.



Check for

a → Invalid

Testcase: Test I/P + Test scenario

If stopped at a point. Till then is called a test case

(iv) Assign values to the variables.

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Step no.	Variable Selection	Value	Expected result	Actual result	Pass / fail comments
1	website	url	login screen		
2	email	isparel @gmail.com			
3	password	xyz123	main screen		

Agile → (i) Pupil
 (ii) Test early
 (iii) Code early User stories
 As a —, I need —
 so that —

front of card → user story (requirement)
 back of the card → Acceptance scenario.

Agile Process Model → Important

1) Concept mapping	"Easy" Practical well closed open
2) User stories	
3) Use cases	
4) Elicitation technique	