Assignment-3 (12th Feb) deadline: 19th Feb, 2019

Assignments must be submitted in the form of a report along with MATLAB codes (through moodle). For all the problems below, **provide graphs (from the simulation) in your report**(use "hold on" and "subplot" wherever necessary to generate the graphs). Plots/graphs must be properly labeled with proper units and right choice of axis.

For each problem: describe the model (governing mathematical equations), approximations made and conclusions based on the simulation (final data/plot). Choose realistic initial conditions, take help from google.

You can do more investigations with your program/code in addition to what have been asked in the question for a particular problem (put these investigations under "additional investigation" section in your report below each problem.)

Use Matlab ODE solver for the following problems:

1. Simple Harmonic Motion:

Computationally investigate the motion of a **pendulum** and a **spring-mass system** as discussed in the class (without any damping). Draw phase plots to explain your observations.

2. Projectile Motion: Cannon Shell/ Missile Problem

- (a) Investigate (computationally) the cannon-shell trajectories ignoring both air drag and the effect of air density. Compare your result with exact solutions. Acceleration due to gravity depends on altitude; include this effect in your computational model by making some rational assumption.
- (b) Investigate the trajectory of the canon shell including both air drag (proportional to square of velocity) and reduced air density at high altitudes. Perform your calculation for different firing angles; and determine the value of the angle that gives the maximum range.

$$F_{drag} = -B v^2$$

Density of atmosphere varies as follows:

$$\rho = \rho_0 \exp(-y/y_0)$$

y is the altitude; $y_0 = 1000$ m. Drag force with air resistance:

$$F_{\text{drag}}^* = \frac{\rho}{\rho_0} F_{\text{drag}}(y=0)$$

Take initial speed=750 m/s; B/m= 4E-5 m⁻¹.

- (c) Generalize the program so that it can deal with situations where the target is at a different altitude (higher or lower) than the canon. Investigate for both the cases. How the minimum firing velocity to hit a target varies as the altitude of the target varies.
- (d) **Optional:** Effect of wind on shell trajectory. Can you include this in your computational model and investigate the effects.

3. Bicycle problem:

(a) Rewrite the bicycle problem/code as discussed in the class. Investigate the effect of rider's power, mass and frontal area on the ultimate velocity.

Generally for a rider in the middle of a group the effective frontal area is about 30% less than the rider at the front. How much less energy does a rider in the group expend than one at the front (assuming both moving at 12.5 m/s).

(b) Run your code (<u>case (a)</u> discussed during class) with initial v=0; observe the output and give possible explanation. Explain why it is important to give a non-zero initial velocity.

- (c) As discussed in the class, we have assumed that the bicyclist maintains a constant power. What about the assumption when the bicycle has a very small velocity? (instantaneous power=product of force and velocity).
- (d) At low velocities it is more realistic to assume, that the rider is able to exert a constant force. That means for small "v" there is a constant force, which means eqn is dv/dt=F0/m

Modify your matlab code to include this term for small velocities, that means we have 2 regimes and 2 eqns one for small velocities and one for larger velocities. Make your code work automatically for both the regimes and crossover from small to large v occur when the power reaches $P(=F_0v)$. Take $F_0=P/v$ where v=5m/s.

Change different parameters and report about important observations.