

Diodes



Linear Passive Components Resistor, inductor and Capacitor

Let us review some of their properties:



- 1. They may store energy or may convert it into heat.
- 2. They are LINEAR the current through them is proportional to applied voltage across their terminals.
- 3. Their parameter values like resistance, capacitance and inductance does not change with value of applied voltage or current passing through them. In that sense their values are STATIC.

DIODE

In comparison, a DIODE is completely different than R, L and C:



- 1. It does not store energy. A very small amount of energy is converted into heat.
- It is NON-LINEAR, i.e. current through diode is not linearly proportional to voltage across its terminals.
- 3. Its so called "resistance" is DYNAMIC in nature and its value changes based on "point of operation" on its I-V curve.

Actual DIODE Terminal Characteristics



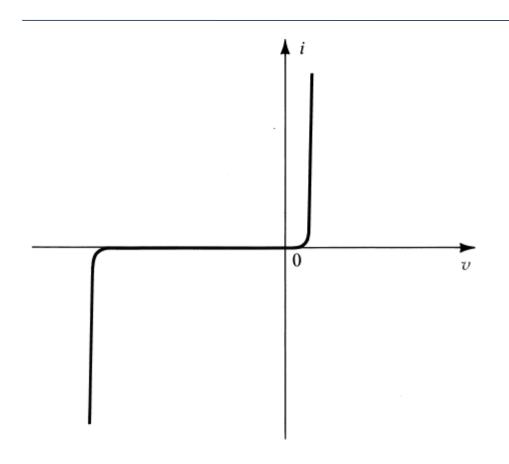


FIGURE 2.7 The i–v characteristic of a silicon junction diode.

For v> 0V, forward bias region, exponential curve

For v< 0V, reverse bias region, virtually open circuit or very high resistance.

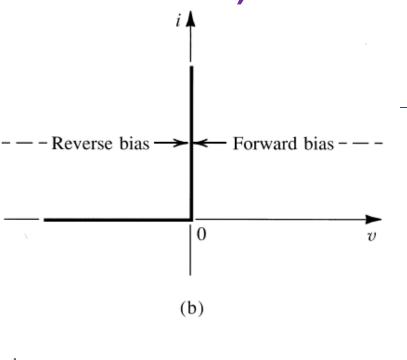
For Vi< Vzk, breakdown region, constant voltage source.

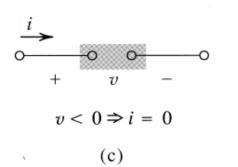
Converting Non-linear Diode Characteristics into simpler Linear Models..



- 1. There is a need for rapid analysis of diode based circuits which will quickly tell the designer whether the diode in the given circuit will be conducting or not and if yes, then approx. how much current will be there.
- 2. Such need created simpler linear models which approximated the actual diode behavior with an acceptable level of error say + or -5 %.
- 3. The designer first analyzed the circuit using approximate models. If found workable then detailed analysis was used for solving for currents.

IDEAL DIODE (behaves like a switch)





v

(a)

Cathode

Anode

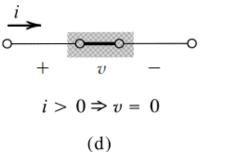


FIGURE 2.1 The ideal diode: (a) diode circuit symbol; (b) i-v characteristic; (c) equivalent circuits reverse direction; (d) equivalent circuit in the forward direction.



- In forward direction the diode behaves like a short circuit or the resistance is ZERO.
- In reverse direction it behaves like an open circuit or the resistance is INFINITY.

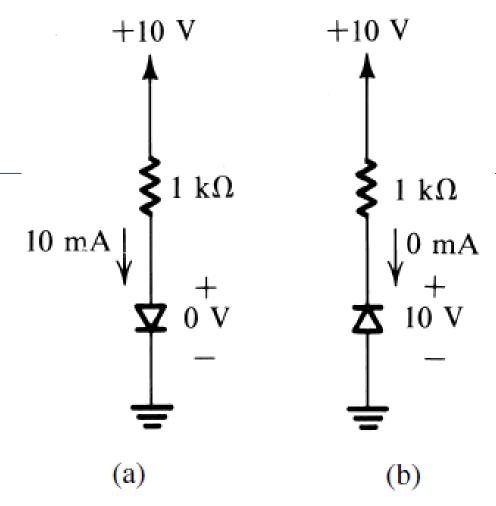


FIGURE 2.2 The two modes of operation of ideal diodes and the use of an external circuit to limit the forward current (a) and the reverse voltage (b).



- (a) In forward direction, the voltage across diode is 0 and all of 10V appears across 1K so current is 10 mA.
- (b) In reverse direction, since the resistance is infinity, all the 10V appears across diode, there is 0V across the 1K resistor and the current is ZERO.

IDEAL DIODE as a RECTIFIER (converts AC into DC)



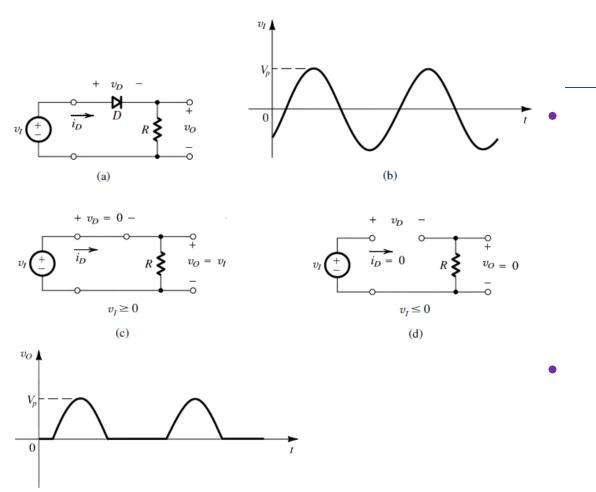


FIGURE 2.3 (a) Rectifier circuit. (b) Input waveform. (c) Equivalent circuit when $v_I \ge 0$. (d) Equivalent circuit when $v_I \le 0$. (e) Output waveform.

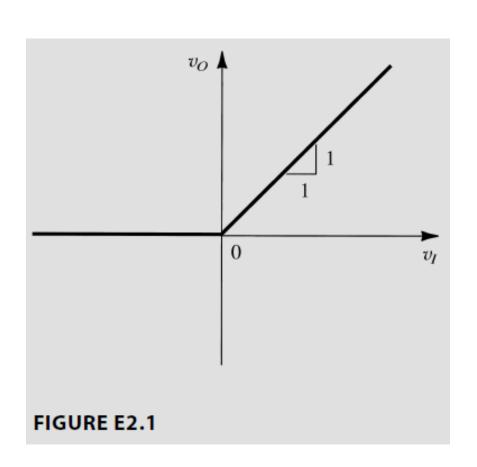
(e)

During positive half cycle, the diode is forward biased and connects load R to source. Hence all of source voltage appears across the load.

During negative half cycle, diode gets reverse biased and becomes open circuit. The load is isolated from source. The current is ZERO.

Q:For Circuit in Fig 2.3, Plot Transfer Characteristics Vo/Vi

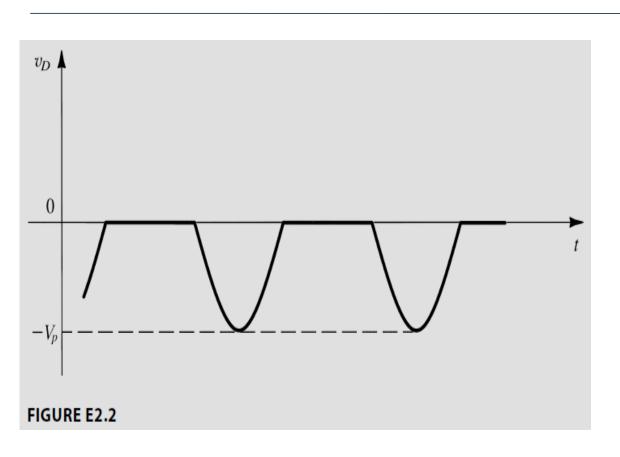




- For Vi> 0, positive half cycle, Vo= Vi and gain
 = 1. Slope = 1
- For Vi< 0, negative half cycle,
 Vo = 0 and
 Gain = Slope = 0.

Q:For Circuit in Fig 2.3, Plot voltage across diode Vd.





For Vi> 0, positive half cycle, short circuit, diode voltage

Vd = 0

For Vi< 0, negative half cycle, open circuit,
Vd = Vi-Vo = Vi- 0

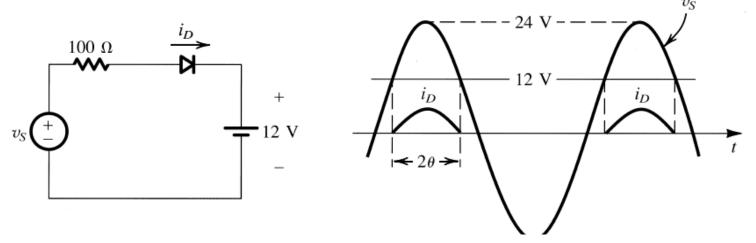
$$Vd = Vi-Vo = Vi-0$$

= Vi .

Q: Plot current Id in diode circuit

A: When (input voltage > 12V), diode shorts and current flows Id = (Vs- 12V)/ 100 otherwise diode is open and Id = 0.





The diode conducts when Vs exceeds 12 V, as shown in Fig. The conduction angle is 2Θ, given by

$$24 \cos \theta = 12$$

Thus $\theta = 60^{\circ}$ and the conduction angle is 120°, or one-third of a cycle.

The peak value of the diode current is given by

$$I_d = \frac{24 - 12}{100} = 0.12 \text{ A}$$

The maximum reverse voltage across the diode occurs when v_s is at its negative peak and is equal to 24 + 12 = 36 V.

Q:Find V and I in each case

Hint: (Find out whether diode is on or off. Use ideal diode model)



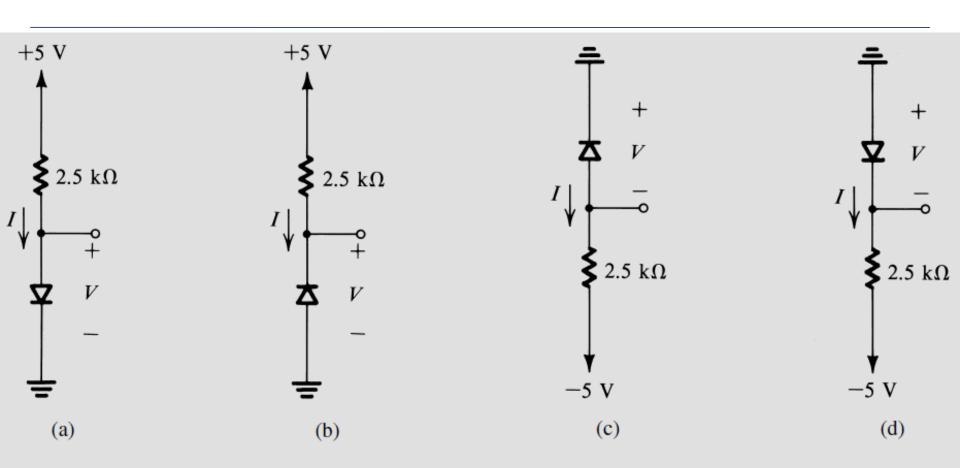


FIGURE E2.4

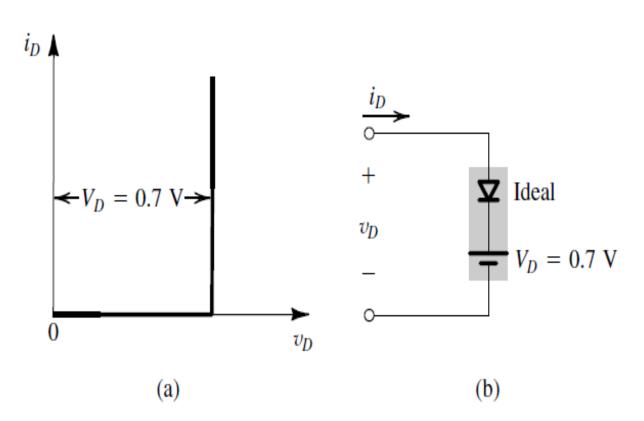


- (a) 2 mA, 0 V
- (b) 0 mA, 5 V
- (c) 0 mA, 5 V
- (d) 2 mA, 0 V

NON-IDEAL DIODE

Model – Constant Voltage Drop (behaves like a switch with offset voltage created by a battery)





For Vi> 0.7V
(Cut-in
voltage) diode
behaves like
short circuit

For Vi< 0.7V, diode behaves like open circuit.

FIGURE 2.16 The constant-voltage-drop model of the diode forward characteristics and its equivalent-circuit representation.

NON-IDEAL DIODE Model – II

Model – Piecewise Linear (behaves like a switch with battery and a small resistor)



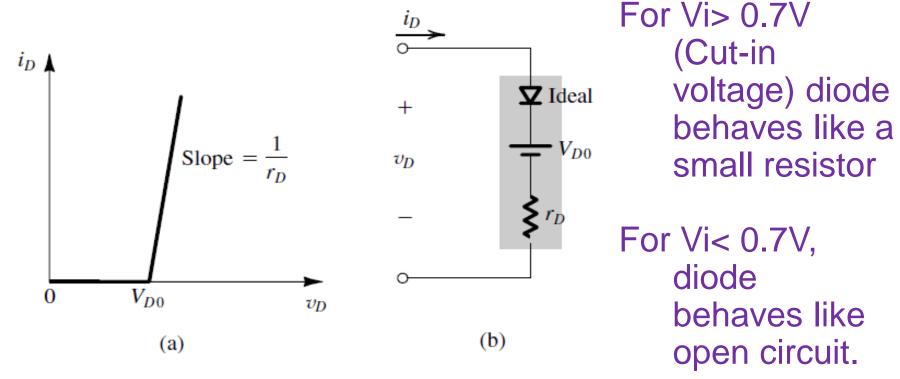


FIGURE 2.13 Piecewise-linear model of the diode forward characteristic and its equivalent circuit representation.

Actual characteristics vs. piecewise linear model



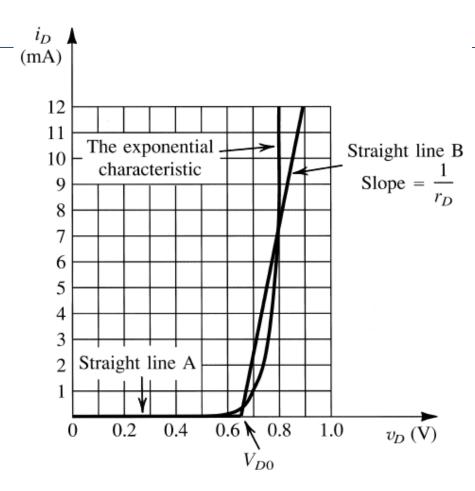
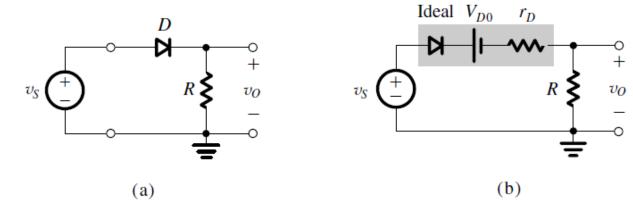
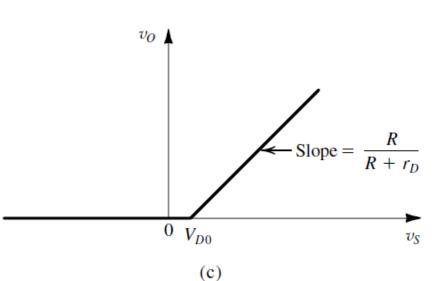


FIGURE 2.12 Approximating the diode forward characteristic with two straight lines: the piecewise-linear model.

NON- IDEAL DIODE as a RECTIFIER (converts AC into DC)







Now the source
voltage is shared
by load resistor
R and diode
resistance rd.

The transfer characteristics slope is less than 1.

Cut-in begins at Vdo and not at 0V.

NON- IDEAL DIODE as a RECTIFIER (converts AC into DC)



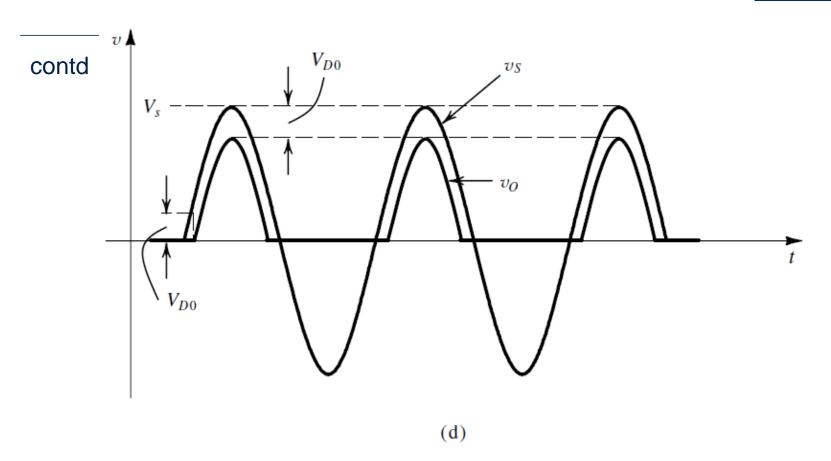


FIGURE 2.25 (a) Half-wave rectifier. (b) Equivalent circuit of the half-wave rectifier with the diode replaced with its battery-plus-resistance model. (c) Transfer characteristic of the rectifier circuit. (d) Input and output waveforms, assuming that $r_D \le R$.

Actual DIODE Terminal Characteristics (studied in detail)



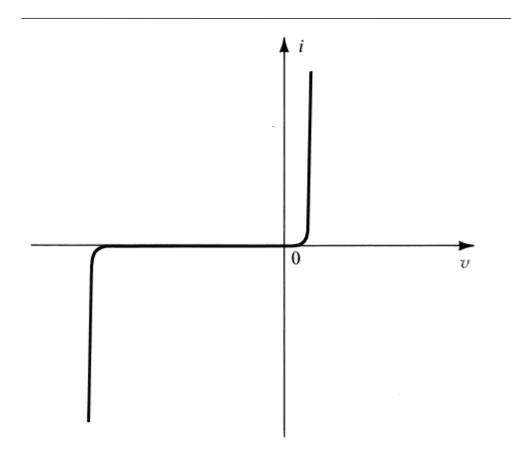


FIGURE 2.7 The i–v characteristic of a silicon junction diode.

For v> 0V, forward bias region, exponential curve

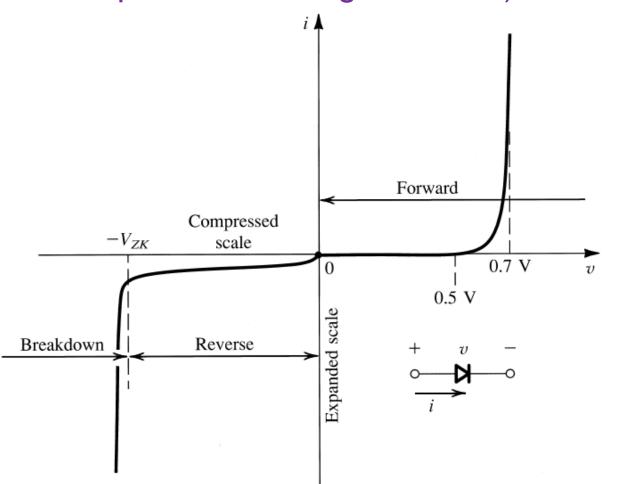
For v< 0V, reverse bias region, virtually open circuit or very high resistance.

For Vi< Vzk, breakdown region, constant voltage source.

DIODE Terminal Characteristics

(X-axis expanded on positive side and compressed on negative side)





For 0<Vi < 0.5V,
negligible current
For 0.5<Vi exponentially
rising current
For 0 > Vi > -Vzk,
reversed bias
leakage current
For Vzk >Vi, constant
terminal voltage.

FIGURE 2.8 The diode i-v relationship with some scales expanded and others compressed in order to reveal details.

DIODE Terminal Characteristics (Forward Bias Region)



When diode is forward biased i.e. anode voltage is > cathode voltage then i-v relationship is approximated by:

$$i = Is (exp(v/n*VT) -1)$$

- where **S** is called as Saturation Current which is constant for a given diode at a given temperature.
- VT = constant (kT/q) called as Thermal Voltage
- N = constant 1 or 2 depending upon construction.

DIODE Terminal Characteristics (Forward Bias Region)



- **1.** Is is of the order of 10 ^ (-15) Amps or 0.001 pico A.
- 2. S doubles every 5 deg C rise in temperature.
- 3. At room temperature 25 deg C, $V_T = 25.8 \, \text{mV}$ but we take it as 25 mV for simplicity.
- 4. For | >> | S, we can approximate it further as

$$i= Is exp(v/n*VT)$$
 or $V = n VT In (i / Is)$

DIODE Terminal Characteristics (Forward Bias Region)



1.If v1 is diode voltage and current is i1 then

$$I1 = Is exp (V1 / n * V_T)$$

2. If v2 is diode voltage and current is i2 then

$$I2 = Is exp (V2 / n * V_T)$$

3. Dividing I2 by I1 we get,

$$(12 / 11) = \exp ((V2-V1) / (n *V_T))$$
 taking log,

Temperature Dependence of DIODE Terminal characteristics (Forward Bias Region)



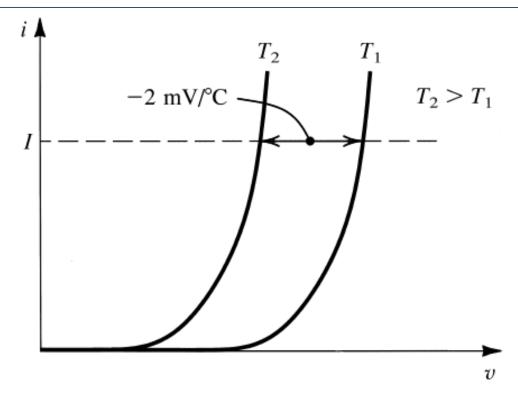


FIGURE 2.9 Illustrating the temperature dependence of the diode forward characteristic. At a constant current, the voltage drop decreases by approximately 2 mV for every 1°C increase in temperature.

DIODE Terminal Characteristics (Reverse Bias Region)



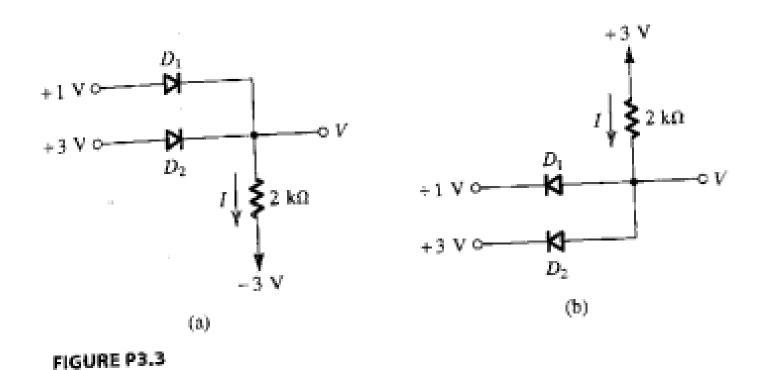
When diode is reversed biased i.e. anode voltage is < cathode voltage i.e. if v is negative and larger than V_T or 25 mV then exponential term becomes negligible and 1 predominates. Then i-v relationship is approximated by:

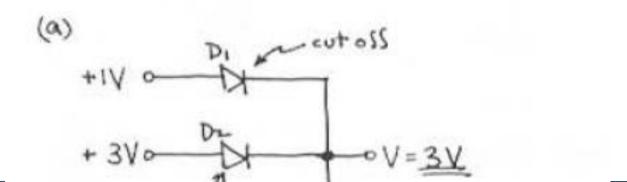
$$i = -ls$$

The current in reverse direction is constant and is called Saturation Current. It is of the order of 0.001 pico amps to 1 nA. Also called as Leakage Current.

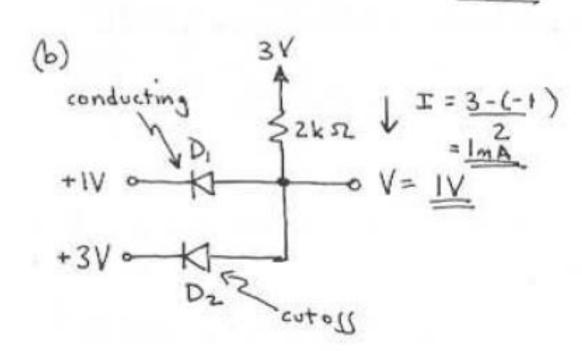
3.3 For the circuits shown in Fig. P3.3 using ideal diodes, find the values of the labeled voltages and currents.





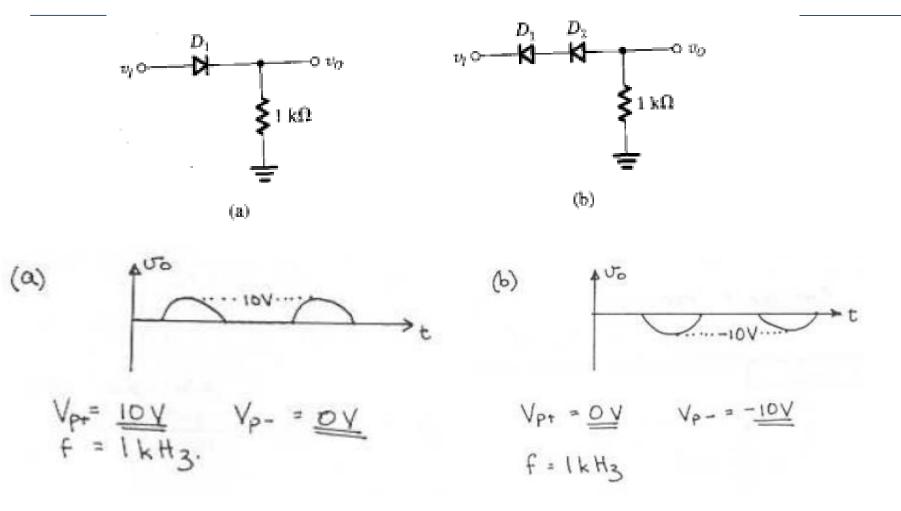


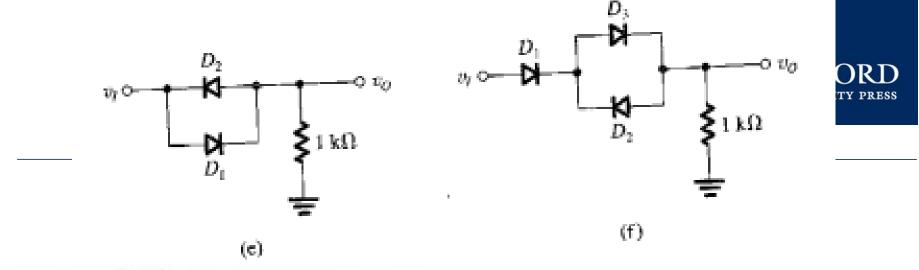


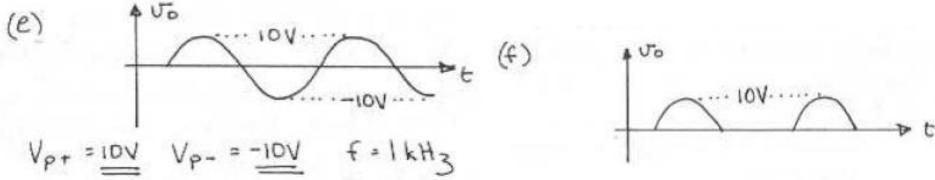


3.4 In each of the ideal-diode circuits shown in Fig. P3.4, v_t is a 1-kHz, 10-V peak sine wave. Sketch the waveform resulting at v_0 . What are its positive and negative peak values?



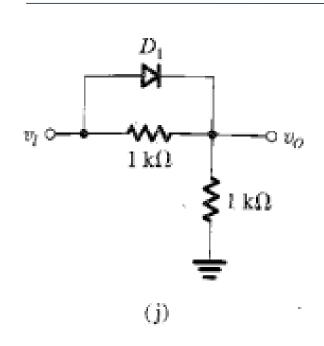


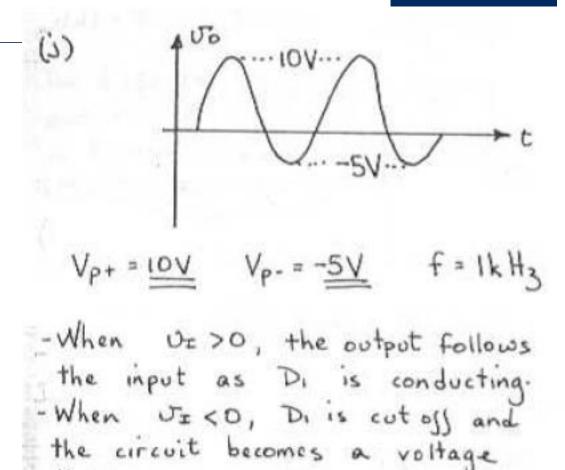




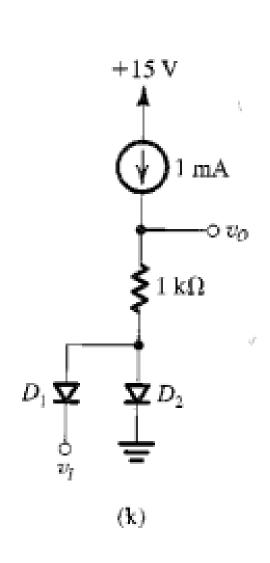
Di conducts when U=>0 and Dz conducts when U=<0. Thus the output follows the input.

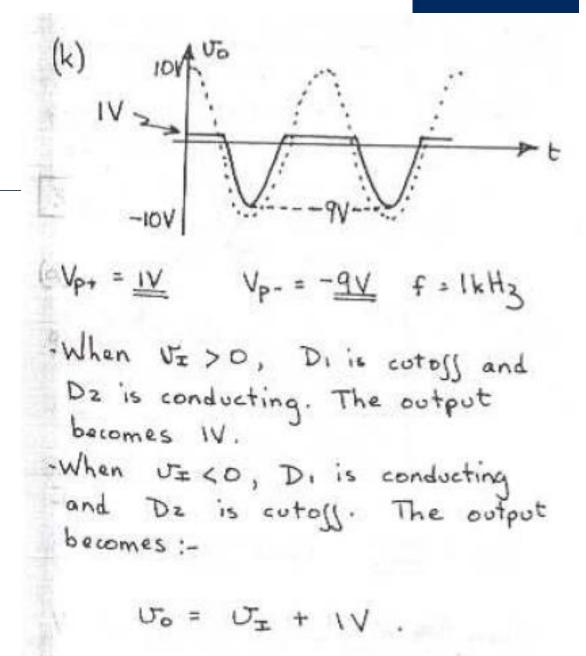






divider.





DIODE Small Signal Model



 Since Diode exhibits a non-linear characteristics, we can calculate diode "resistance" at different points of curve by calculating slope of curve as

Dynamic resistance rd = delta v / delta i which comes to

$$Rd = n VT/ID$$

 Note resistance is inversely proportional to diode current.

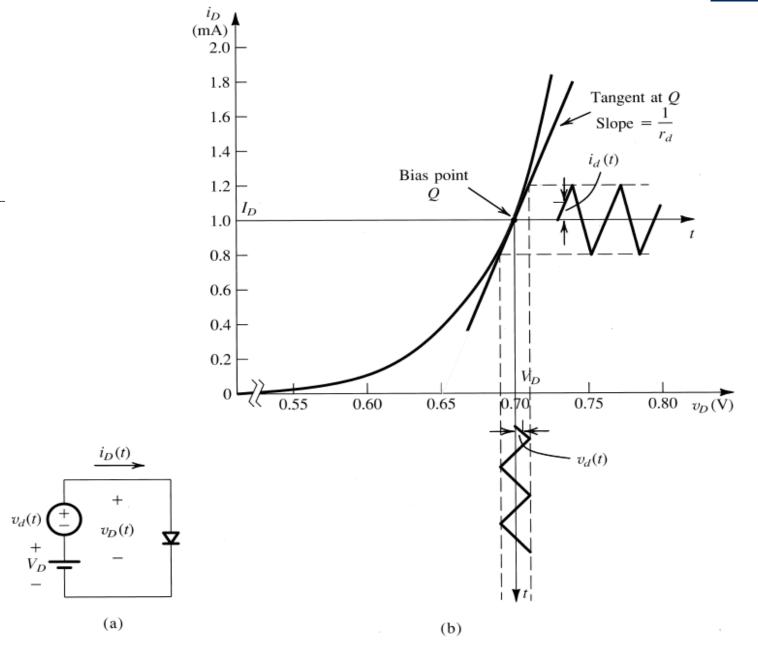


FIGURE 2.17 Development of the diode small-signal model. Note that the numerical values shown are for a diode with n = 2.

Determining Diode Current graphically



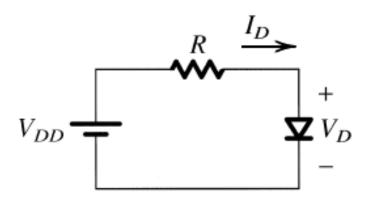


FIGURE 2.10 A simple circuit used to illustrate the analysis of circuits in which the diode is forward conducting.

$$I_D = I_S e^{V_D / nV_T}$$

$$I_D = \frac{V_{DD} - V_D}{R}$$

Determining Diode Current graphically



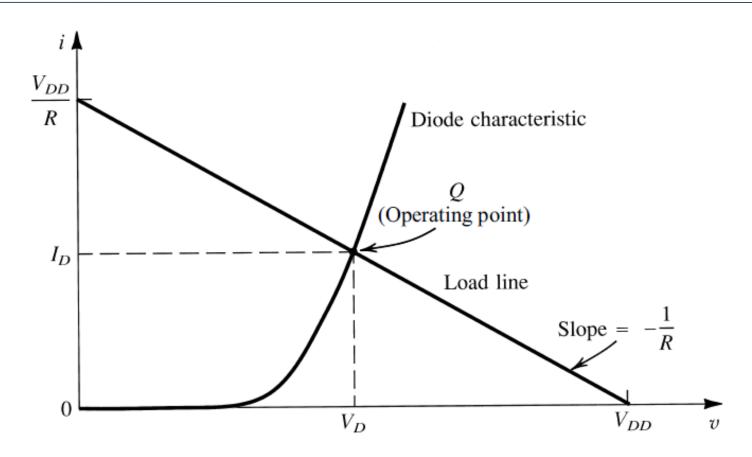


FIGURE 2.11 Graphical analysis of the circuit in Fig. 2.10 using the exponential diode model.

Zener DIODE



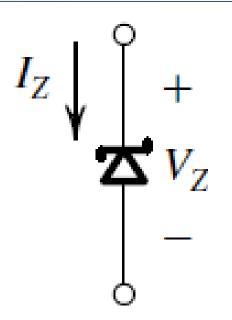


FIGURE 2.20 Circuit symbol for a Zener diode.

- In breakdown region, diode exhibits a very steep curve of i-v characteristics similar to a voltage source.
- 2. In Zener diode, current flows into Cathode and leaves Anode.
 - Manufacturer specifies
 Zener voltage at a specific test current. Say 2.7V @ 10 mA. That will define a dynamic resistance Rz of 2.7V/ 0.010 A = 270 ohms.

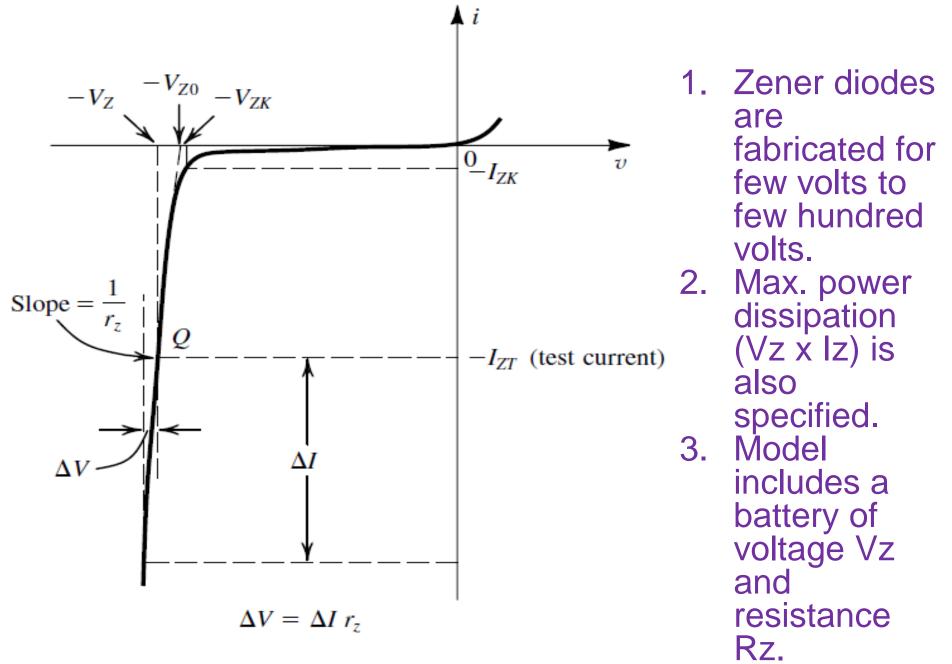


FIGURE 2.21 The diode i-v characteristic with the breakdown region shown in some detail.

Piecewise Linear Model for Zener DIODE



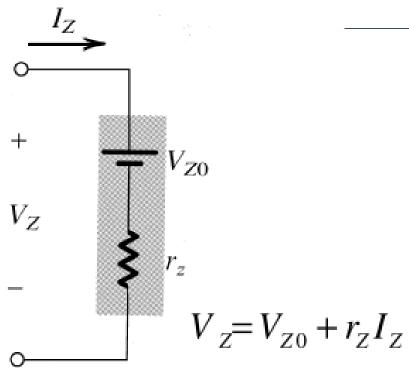


FIGURE 2.22 Model for the zener diode.

Very similar to Diode model except that:

- 1. Voltage source direction is reversed and value could be anything as manufactured.
- $V_z = V_{z_0} + r_z I_z$ 2. Resistance Rz value range very wide due to steep slope.

Application of Diodes in a Regulated Power Supply



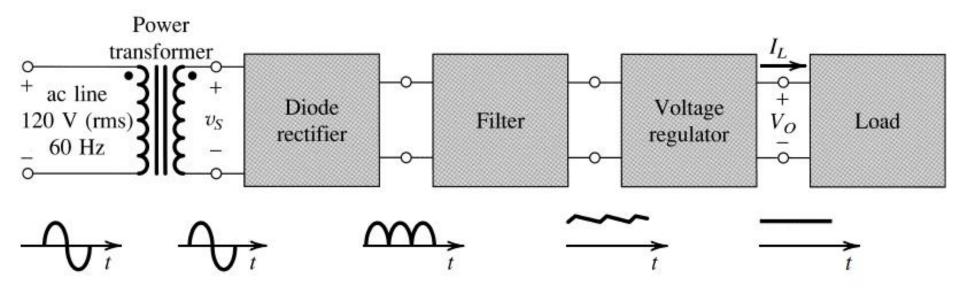


FIGURE 2.24 Block diagram of a dc power supply.

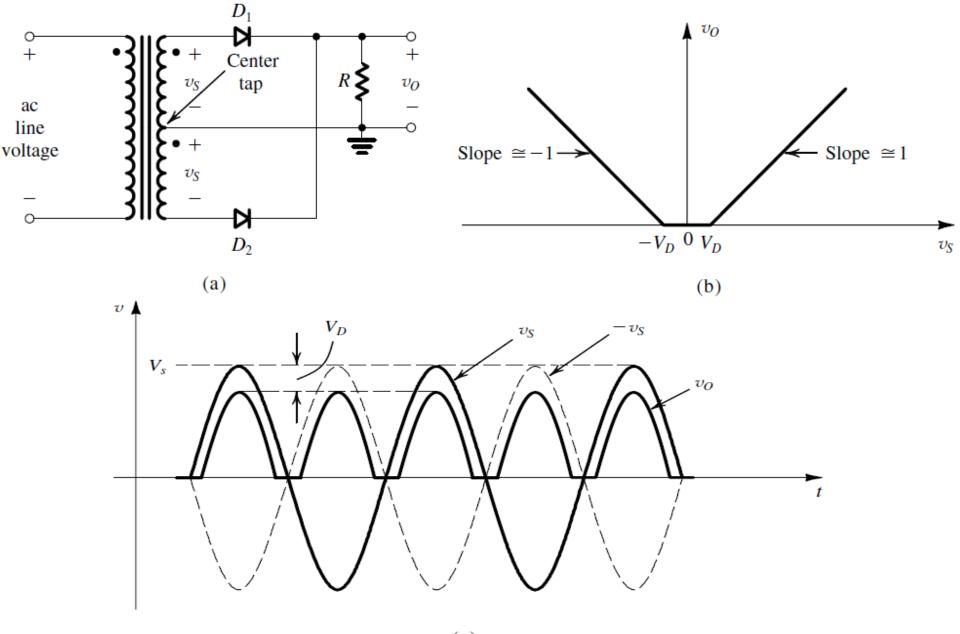


FIGURE 2.26 Full-wave rectifier utilizing a transformer with a center-tapped secondary winding: (a) circuit; (b) transfer characteristic assuming a constant-voltage-drop model for the diodes; (c) input and output waveforms.

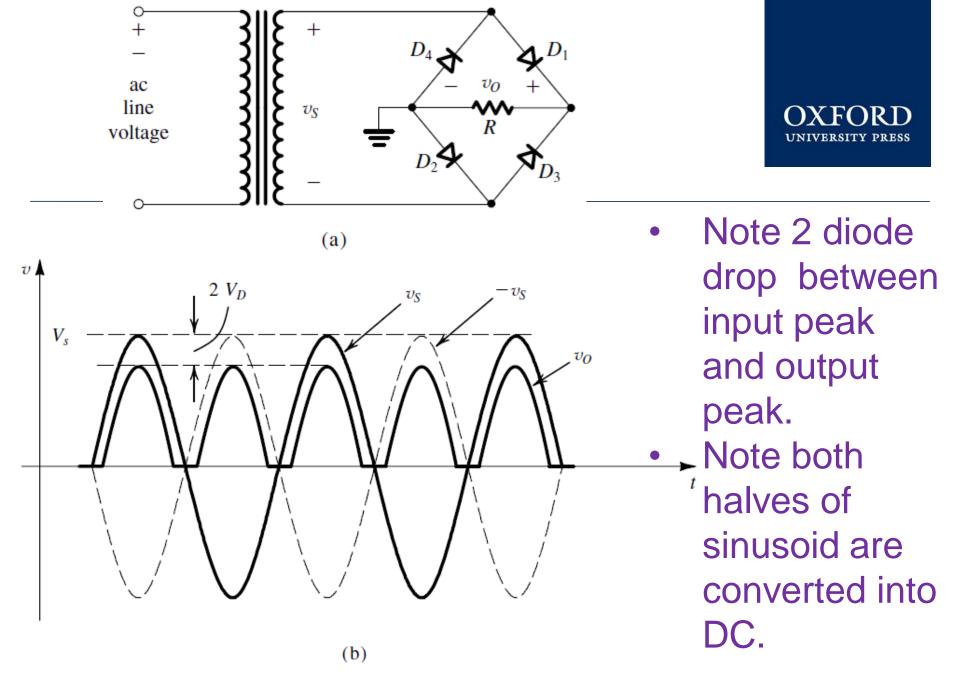
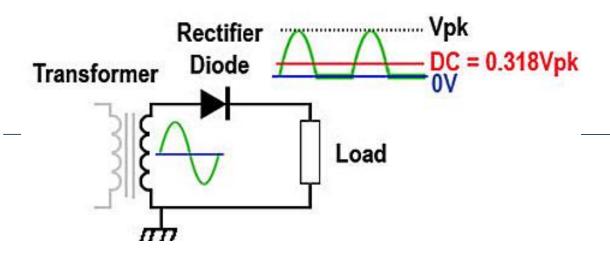


FIGURE 2.27 The bridge rectifier: (a) circuit; (b) input and output waveforms.

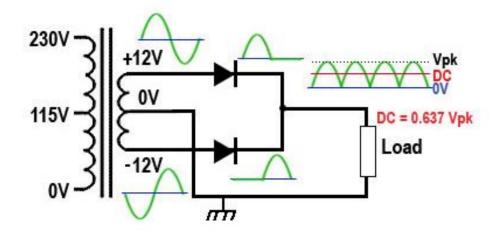
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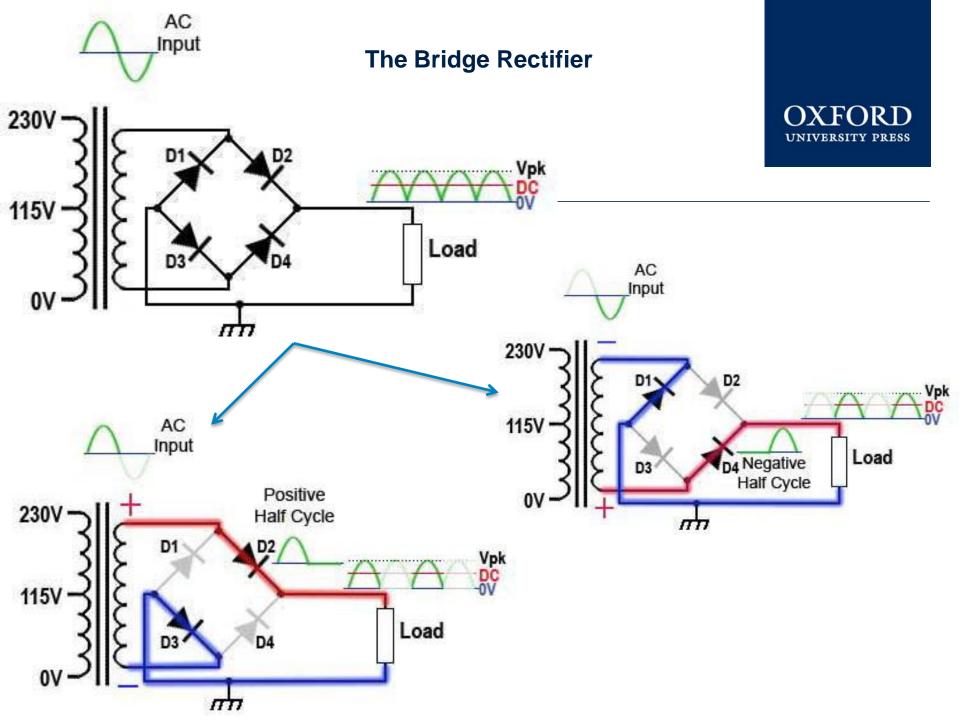
Half Wave Rectification





Full Wave Rectification





Application of Capacitor & Diode as a Peak Detector



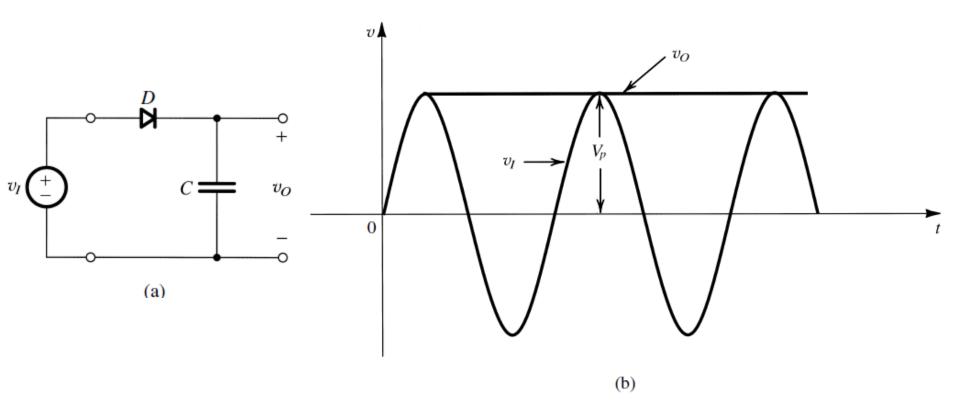
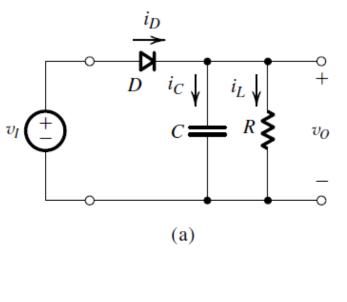


FIGURE 2.28 (a) A simple circuit used to illustrate the effect of a filter capacitor. (b) Input and output waveforms assuming an ideal diode. Note that the circuit provides a dc voltage equal to the peak of the input sine wave. The circuit is therefore known as a peak rectifier or a peak detector.

Leaky Peak Detector (Half Wave)



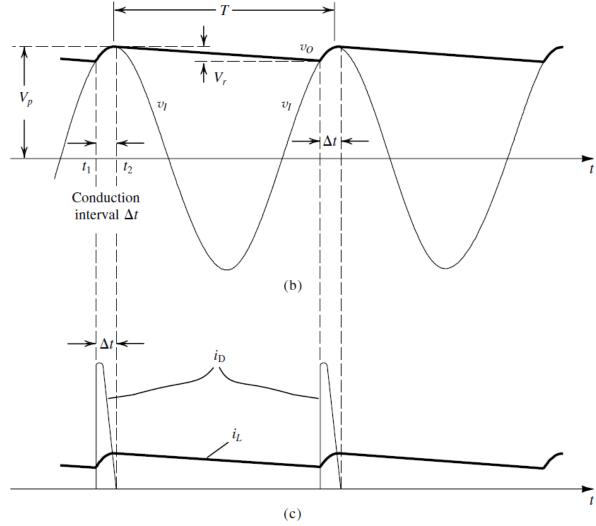


FIGURE 2.29 Voltage and current waveforms in the peak rectifier circuit with $CR \gg T$. The diode is assumed ideal.

Leaky Peak Detector (Full Wave)



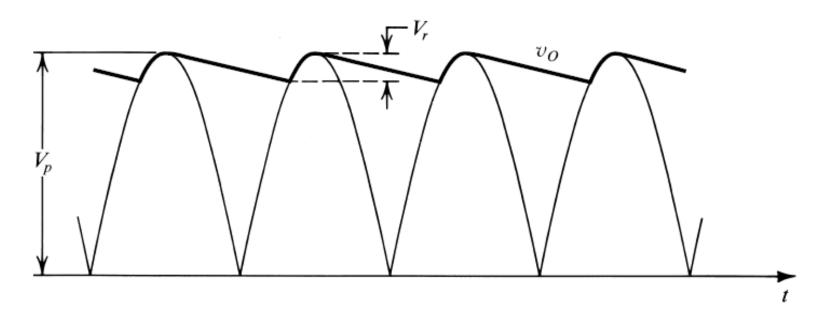
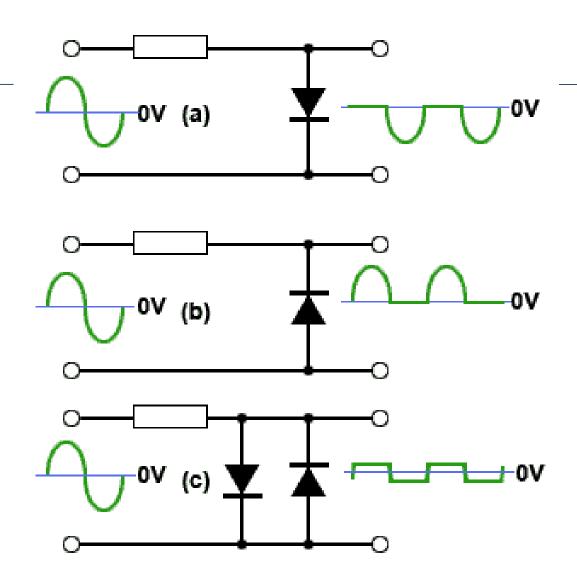


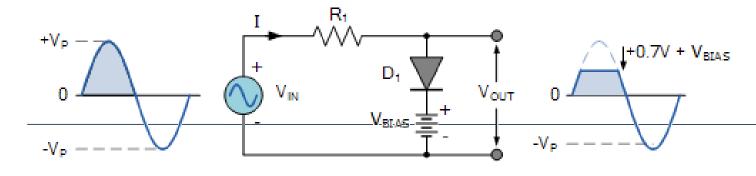
FIGURE 2.30 Waveforms in the full-wave peak rectifier.

Clipping Action



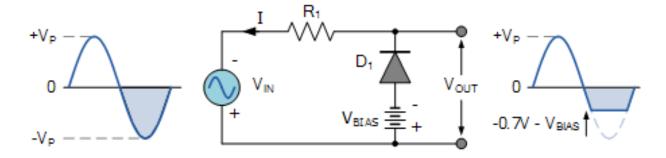


Positive Bias Diode Clipping

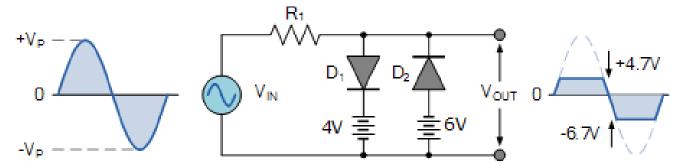




Negative Bias Diode Clipping

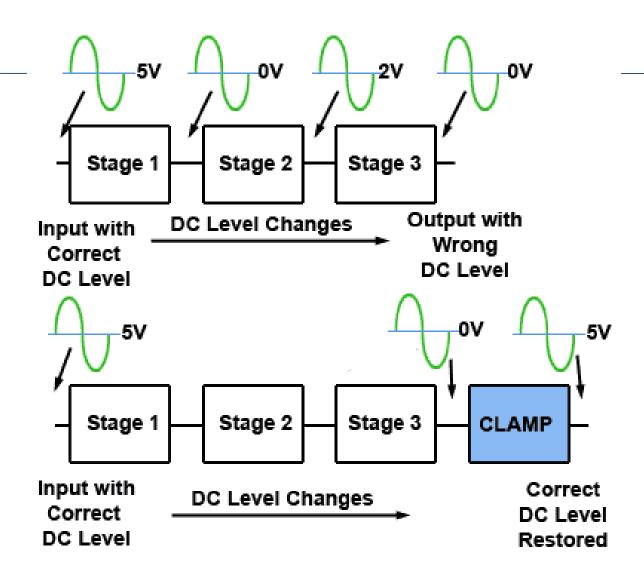


Diode Clipping of Different Bias levels

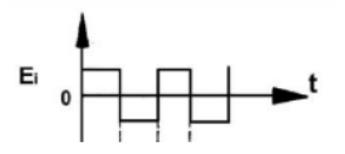


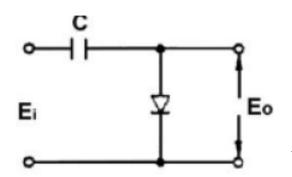
Clamping or DC Restoration





Typical clamping circuit

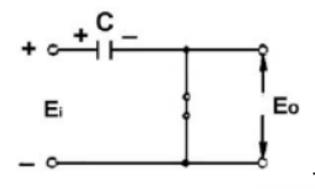


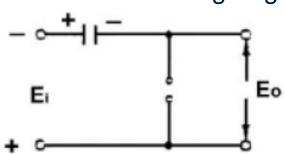


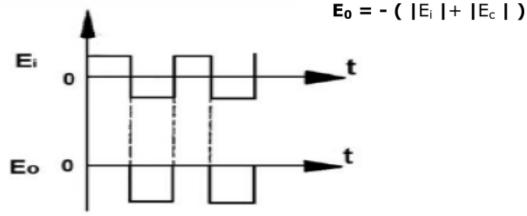


Diode conducts for positive cycle

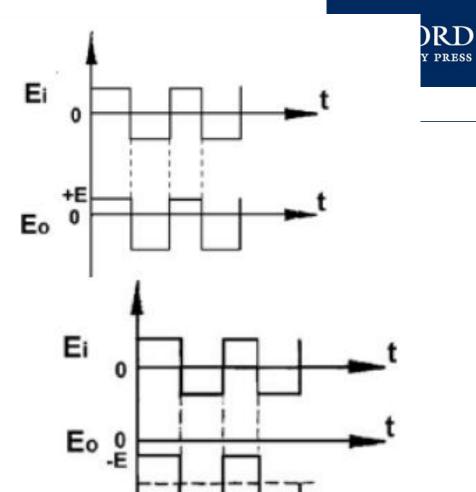
Diode is switched off during negative cycle

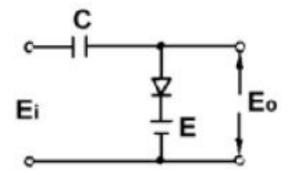


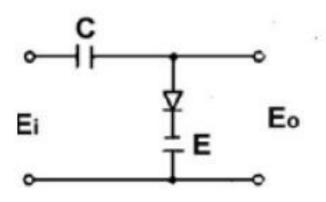




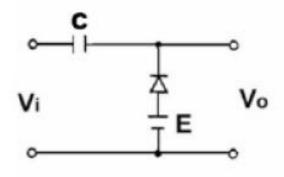
Clamping circuit in which threshold voltage is inserted

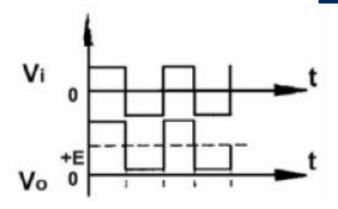




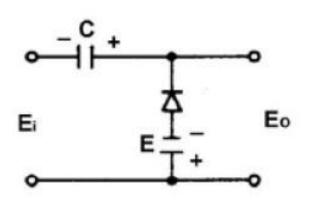


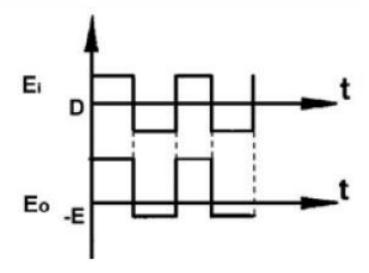
Clamping circuit in which threshold voltage is inserted





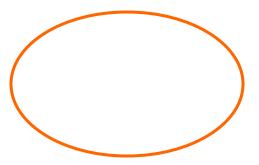






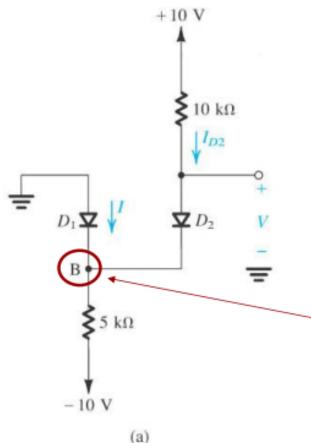
Clamping circuits (3)





Example

Assuming the diode to be ideal, Find the values of I and V in the circuit of Fig. (a) and (b)



Sol:

Asssume that both diodes are conducting

$$V_B = 0$$
 and $V = 0$

$$I_{D_2} = \frac{(10-0)V}{10k\Omega} = 1mA$$

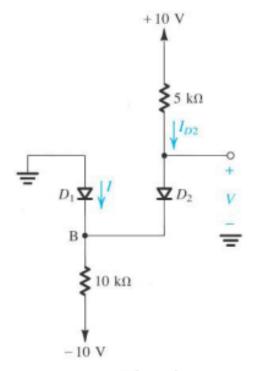
Writting a node equation at **B** (K.C.L)

$$I + 1 = \frac{0 - (-10)}{5} \Rightarrow I = 1 \text{mA}$$

Results in I = 1mA,

Thus D_1 is conducting as originally assumed and the find result is I = 1mA and V = 0V \triangle





Sol:

We assume that both diodes are conducting then $V_R = 0$ and V = 0

$$I_{D_2} = \frac{(10-0)V}{5k\Omega} = 2mA$$

The node equation at B is

$$I + 2 = \frac{0 - (-10)}{10} \Longrightarrow I = -1\text{mA}$$

(This is not possible)

Our assumption is not correct, we start again assuming that D_1 is OFF and D_2 is ON. The current I_{D_2} is given by

$$I_{D_2} = \frac{10 - (-10)}{15} = 1.33 \text{mA}$$

 $V_R = -10 + 10 \cdot 1.33 = 3.3 \text{V}$

Thus D_1 is reverse biased as assumed

$$\therefore I = 0$$
A and $V = 3.3$ V

3.3.3 Iterative analysis using the exponential model

Example 3.4 determine the current I_D and the diode voltage V_D for the circuit in Fig. 3.10 with $V_{DD} = 5$ V and R = 1k Ω , assume that the diode has a current of 1mA at voltage of 0.7V and that its voltage drop changes by 0.1V for every decade change in current.

Second

First

Sol: We assume that
$$V_D = 0.7 \text{V}$$
, $I_D = 1 \text{mA}$

$$I_D = \frac{V_{DD} - V_D}{R} = \frac{(5 - 0.7)V}{1k\Omega} = 4.3mA$$

$$V_2 - V_1 = 2.3 \cdot n \cdot V_T \cdot \log \frac{I_2}{I_1}$$

$$V_2 = V_1 + 0.1 \cdot \log \frac{I_2}{I_1} (n = 2, 2.3 \cdot n \cdot V_T \cong 0.1 \text{V})$$

$$V_2 = 0.7 + 0.1 \cdot \log \frac{4.3 \text{mA}}{1 \text{mA}} = 0.763 \text{V}$$

The first iteration are $I_D = 4.3 \text{mA}$, $V_D = 0.763 \text{V}$

Please see slide no 23 and 34.

We assume that $V_D = 0.763 \text{V}$, $I_D = 4.3 \text{mA}$

$$I_D = \frac{V_{DD} - V_D}{R} = \frac{(5 - 0.763)\text{V}}{1\text{k}\Omega} = 4.237\text{mA}$$

$$V_2 = 0.763 + 0.1 \cdot \log \frac{4.237 \text{mA}}{4.3 \text{mA}} = 0.762 \text{V}$$

The second iteration are $I_D = 4.237 \text{mA}$, $V_D = 0.762 \text{V}$

We assume that $V_D = 0.762 \text{V}$, $I_D = 4.237 \text{mA}$

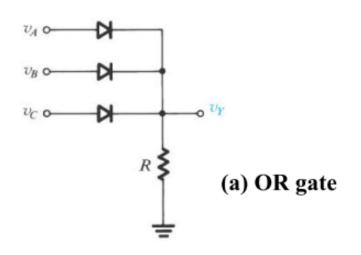
$$I_D = \frac{V_{DD} - V_D}{R} = \frac{(5 - 0.762)\text{V}}{1K\Omega} = 4.238\text{mA}$$

$$V_2 = 0.762 + 0.1 \cdot \log \frac{4.238 \text{mA}}{4.237 \text{mA}} = 0.762 \text{V}$$

Because I_D did not change by much stop here and the solution is $I_D = 4.237 \text{mA}$ and $V_D = 0.762 \text{V}$

D

3.1.3 Another Application: Diode Logic Gates



	+5 V	
<i>v</i> ₄ ◦ K	_	
<i>UB</i> ○	• υ _γ	(b) AND gate
<i>v_C</i> ∘ √		, ,

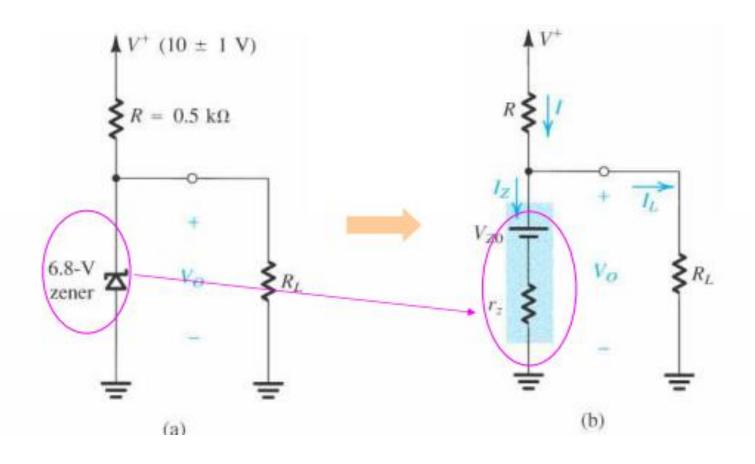
v_A	v_B	v_C	v_{Y}
0	0	0	0
0 0 0	0		1
0	1	1 0	1
0	1	1	1
:	:	:	:
1	1	0	1
1	1	1	1

v_A	v_B	v_C	v_Y
0	0	0	
0 0 0	0	1 0	0
	1	0	0
0	1	1	0 0 0 0
:	:	:	
1	1	: 0	0
1	1	1	0 1

The 6.8V Zener diode in the circuit below

is specified to have $V_Z=6.8\mathrm{V}$ at $I_Z=5\mathrm{mA}, r_z=20\Omega$ and SITY PRESS

 $I_{ZK} = 0.2 \text{mA}$, the V⁺ is $10 \text{V} \pm 1 \text{V}$.



With these ratings

or

FORD

$$V_Z = V_{Z0} + r_z I_Z \implies V_{Z0} = V_Z - r_z I_Z$$

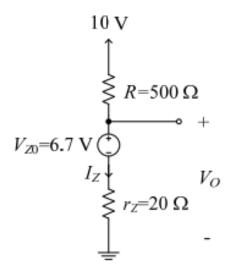
 $V_{Z0} = 6.8 - 20 \cdot 5 \times 10^{-3} = 6.7 \text{ V}$

Note that the supply voltage can fluctuate by ± 1 V. Imagine this fluctuation is a random process rather than a time periodic variation.

Determine the following quantities:

(b) Find V_O with no load and V^+ at the nominal value. The equivalent circuit for the reverse bias operation of the Zener diode is





From this circuit we calculate

$$I_Z = \frac{10 - 6.7}{500 + 20} = 6.35 \text{ mA}$$

Therefore,

$$V_0 = 10 - I_z \cdot 500 = 10 - 6.35 \times 10^{-3} \cdot 500 = 6.83 \text{ V}$$

 ${
m RD}$

Find the change in V_O resulting from a ± 1 V change in V^{\dagger} . Using the circuit above the V^+ = 11 V:

$$V_O = 11 - \frac{11 - 6.7}{500 + 20} \cdot 500 = 6.865 \text{ V}$$

Similarly, with $V^{+}=9$ V:

$$V_o = 9 - \frac{9 - 6.7}{500 + 20} \cdot 500 = 6.788 \text{ V}$$

Consequently,
$$\Delta V_o = 6.865 - 6.788 = 0.077$$
 V or $\Delta V_o = \pm 38.5$ mV.

The ratio of the change in output voltage to the change in the source voltage $(\Delta V_o/\Delta V^+)$ is called the line regulation

of the regulator circuit. It's often expressed in units of mV/V. For this example and no load attached,

Line Regulation
$$\equiv \frac{\Delta V_O}{\Delta V^+} = \frac{77}{11-9} \frac{\text{mV}}{\text{V}} = 38.5 \frac{\text{mV}}{\text{V}}$$

(d) Find the change in V_O resulting from connecting a load of $R_L = 2 \text{ k}\Omega$ with a nominal $V^+ = 10 \text{ V}$.

Assuming that the diode is operating in the breakdown region:



$$R=500 \Omega$$

$$I_{S}$$

$$I_{L}$$

$$I_{Z}$$

$$I_{L}$$

$$V_{O}$$

$$I_{L}=2 \text{ k}\Omega$$

then

$$I_L = \frac{6.8}{2000} = 3.4 \text{ mA}.$$

Is this a reasonable value? Calculate I_S :

$$I_S = \frac{10 - 6.8}{500} = 6.4 \text{ mA}.$$

So, yes, this is a reasonable value because $I_L < I_S$, as it must.

From (1), $\Delta V_O = r_z \Delta I_Z$ and since $\Delta I_Z = -3.4$ mA then



$$\Delta V_o = 20(-3.4 \times 10^{-3}) = -68 \text{ mV}$$

The ratio of the change in output voltage to the change in the load current $(\Delta V_O/\Delta I_L)$ is called the load regulation of the regulator circuit. It's often expressed in units of mV/mA. For this example,

Load Regulation
$$\equiv \frac{\Delta V_o}{\Delta I_L} = \frac{-68 \text{ mV}}{3.4 \text{ mA}} = -20 \text{ mV}$$



Home-work

From the text book find out the solutions to problems no, 3.10, 3.23, 3.26, 3.95, 3.96, 3.99, 3.105.