After going through the birthday problem paper I noticed the goal of the K-list algorithm is to find elements  $y_{k_2},\ldots,y_{k_2+k_1}$  such that  $s=y_{k_2}+\cdots+y_{k_2+k_1}\in I(-1)$