

Data-Driven Model Free Adaptive Sliding Mode Control For Multi DC Motors Speed Regulation

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Abstract

Here goes an Abstract

I. INTRODUCTION

IN short time ago, the field of control systems experienced significant advancements, particularly in the domain of multi-agent systems. Distributed coordination of multi-agent systems has been utilized in range of practical applications, including satellite formation, autonomous, underwater vehicules,automated highway systems, and mobile robots. These applications highlight the importance and adaptability of multi-agent systems in addressing complex real world challenges.

A critical aspect of multi-agent systems is robust speed regulation, effectively managing multi direct current (DC) motors is essential for acheiving complex machine movements. The complexity of such systems arises from the necessity to maintain synchronization and optimal performance despite parametric uncertainties and external disturbances. Conventional control methodologies, such us Proportional-Integral-Derivative (PID) control and Linear Quadratic Regulator (LQR), often fall short in these dynamic and unpredictable environments, highlighting the need for more adaptive and resilient approaches.

Firstly, this paper aims to address these challenges by representing an innovative control strategy. Moreover, the proposed method synergizes the strengths of Model Free Adaptive Control (MFAC) and Sliding Mode Control (SMC) to achieve robust and efficient speed regulation in multi-agents systems. Secondly, By leveraging the adaptability of MFAC and the robustness of SMC, this approach seeks to enhance the performance and realilbty of multi DC motors speed regulation in the presence of uncertainties and perturbations.

Model Free Adaptive Control (MFAC) is a technique that eschews the need for an explicit mathematical model of the system, making it highly adaptive to real time changes and disturbances. This adaptability ensures optimal control performance in varying conditions. On the other hand, Sliding Mode Control (SMC) is well known for its robustness and ability to handle Nonlinearities and uncertainties by enforcing high frequency switching control law. SMC ensures that the system states are driven to and maintained within a specified sliding surface.

Finally, the integration of these two methodologies facilitates a control strategy that is both adaptive and resilient. MFAC continously adjusts the control parameters based on real-time system feedback, while SMC provides a robust framework to manage system uncertainties and external disturbances. This combination is particularly well-suited for the complex dynamics and interactions inherent in multi-agent systems, offering a comprehensive solution to the challenges of robust speed control.

The following sections will outline the remaining content of this paper: section 2 provides——. Section 3 ————. Section 4 presents simulation results and performance analysis , demonstrating the efficacy of the proposed method under various operating conditions. At the end, Section 5 concludes the paper, summarizing the key findings potential points for future research, including the extension of the proposed approach to other types of multi-agent systems and exploring further enhancements to the control algorithms.

II. PRELIMINARIES AND PROBLEM FORMULATION

A. Preliminaries

The set of real numbers is denoted by \mathbb{R} . For a given matrix $A \in \mathbb{R}^{n \times n}$, $\|A\|$ represents its matrix norm. The notation $\text{diag}(\cdot)$ refers to a diagonal matrix, and I signifies an identity matrix of appropriate dimensions. In the context of multi-agent systems, graph theory serves as a powerful tool to model interaction topologies. We will now provide a brief introduction to directed graphs within algebraic graph theory. Let $G = (V, E, A)$ be a weighted directed graph, where $V = \{1, 2, \dots, N\}$ represents the set of vertices, $E \subseteq V \times V$ denotes the set of edges, and A is the adjacency matrix. Here, V also indexes the agents. If agent j can receive a message from agent i , then $(i, j) \in E$, making j the child of i and i the parent of j . The neighborhood of agent i is given by $N_i = \{j \in V \mid (j, i) \in E\}$.

The weighted adjacency matrix $A = (a_{i,j}) \in \mathbb{R}^{N \times N}$ is defined such that $a_{i,i} = 0$, $a_{i,j} = 1$ if $(j, i) \in E$; otherwise, $a_{i,j} = 0$. The Laplacian matrix of G is defined as $L = D - A$, where $D = \text{diag}(d_1^{\text{in}}, d_2^{\text{in}}, \dots, d_N^{\text{in}})$ and $d_i^{\text{in}} = \sum_{j=1}^N a_{i,j}$ is called the in-degree of vertex i . A graph is said to be strongly connected if there exists a path between any pair of vertices.

B. Problem Formulation

In this research, the speed regulation problem of DC motors is frequently examined under the assumption that all motors demonstrate identical dynamic characteristics. Nevertheless, heterogeneity is still a fundamental characteristic of systems comprising multi DC motors. Even if the motors are of the same type and have similar structural features, their parameters can never be exactly the same. This inherent variability makes achieving coordinated speed regulation across heterogeneous motors a more complex task. Let consider a multi DC motors system consisting of N motors where the interaction topology is represented by G . Assume that each motor i the following nonlinear dynamics is considered:

$$y_i(k+1) = f_i(y_i(k), u_i(k)), \quad i = 1, 2, \dots, N \quad (1)$$

Where $y_i(k) \in \mathbb{R}$ represents the output (speed of DC motor), $u_i(k) \in \mathbb{R}$ is the control input (the voltage) and $f_i(\cdot)$ is an unknown nonlinear function, respectively.

We consider a scenario where multiple agents aim to track a consensus trajectory $yd(k)$, which is exclusively accessible to a subset of agents. This trajectory is assumed to be generated by a virtual leader designated as vertex 0. To model this interaction, we construct a direct graph $G' = (V \cup \{0\}, E', A')$ where V denotes the set of agents, E' represents the edge set defining connections from agents to the virtual leader, and A' constitute a weighted adjacency matrix detailing these connections.

This analysis presupposes nonlinear dynamics governing each agent's evolution, encompassing dependencies on their respective states and inputs. These nonlinear dynamics accommodate various complexities, facilitating an investigation into how agents align with the desired trajectory $yd(k)$.

Assumption 1: The partial derivative of the nonlinear function $f_i(\cdot)$ with respect to $u_i(k)$ is continuous.

Assumption 2: The model $y_i(k+1) = f_i(y_i(k), u_i(k))$ is generalized Lipschitz, meaning that if $\Delta u_i(k) = u_i(k) - u_i(k-1) \neq 0$, then $|\Delta y_i(k+1)| \leq b|\Delta u_i(k)|$ holds for any k , where $\Delta y_i(k+1) = y_i(k+1) - y_i(k)$ and b is a positive constant.

Remark 1: The practical applicability of the aforementioned assumptions to nonlinear systems has been extensively discussed in [?], affirming their suitability for practical multi-agent systems. **Assumption 1** establishes a foundational criterion for controller design, ensuring the continuity of the partial derivative of the nonlinear function $f_i(\cdot)$ with respect to $u_i(k)$. **Assumption 2** implies that the rate of change in an agent's output in response to changes in its control input is bounded. This constraint ensures that, from an energetic perspective, finite changes in control input energy correspond to bounded changes in output energy rates, a crucial consideration for system stability and performance.

C. Linearization Technique

This paper delves into the Compact Form Dynamic Linearization (CFDL) technique, this method simplifies the dynamic of nonlinear systems into a linear form that is easier to handle and control. The CFDL is particularly useful when the control input $u_i(k) = 0$ holds, enabling the system to be described through a compact dynamic linearization model. The system under consideration is governed by the following equation:

$$\Delta y_i(k+1) = \phi_i(k) \Delta u_i(k) \quad (2)$$

Where $|\phi_i(k)| \leq b$. b is a positive constant and the variable $\phi_i(k)$ named pseudo-partial-derivative.

We define the distributed measurement output of $x_i(k)$ for i -th agents as follow:

$$\xi_i(k) = \sum_{j \in N_i} a_{i,j} (y_j(k) - y_i(k)) + d_i (y_d(k) - y_i(k)) \quad (3)$$

In this equation $x_i(k)$ represents the distributed measurement output of the i -th agent at time step k , N_i denotes the set of the neighboring agents of the i -th agent and $a_{i,j}$ are elements of the adjacency matrix representing the weights between agents i and j . For this equation, we assume that $d_i = 0$, meaning the agent i does not directly consider the desired trajectory $y_d(k)$ in the distributed measurement output. However if agent i can receive the desired trajectory, setting d_i to a non-zero value allows it to align its output with the desired trajectory, improving the control performance.

Let $e_i(k) = y_d(k) - y_i(k)$ denote the tracking error. The objective of this paper is to find a good control law using I/O data of the agents (DC motors), such that the outputs of all agents can track the reference trajectory $y_d(k)$ when only some of agents can access the desired trajectory.

Assumption 3: The communication graph \bar{G} is fixed and strongly connected, with at least one follower agent able to access the leader's trajectory.

Remark 2: This assumption ensures the solvability the tracking problem. An isolated agent, oblivious of the control objective, cannot follow the leader's reference trajectory.

Assumption 4 : The PPD $\phi_i(k) > \varsigma$, $i = 1, 2, 3 \dots N$ holds for all k , where ς is a randomly small positive constant. Without loss of generality, in this paper we assume that $\phi_i(k) \varsigma$.

Remark 3: This indicates that the agent output does not decrease with increasing control input, resembling a linear characteristic. It implies the control direction is known and unchanging. Similar assumptions are common in model-based control and are reasonable for practical systems like mobile robots and UAVs.

III. MAIN RESULTS

Considering the following PPD criterion function:

$$J(\phi_i(k)) = |\Delta y_i(k) - \hat{\phi}_i(k) \Delta u_i(k-1)|^2 + \mu |\hat{\phi}_i(k) - \hat{\phi}_i(k-1)| \quad (4)$$

Differentiating equation (4) with respect to PPD parameter $\phi_i(k)$ and make it equal to zero:

$$\frac{\partial J(\phi_i(k))}{\partial \phi_i(k)} = |\Delta y_i(k) - \hat{\phi}_i(k) \Delta u_i(k-1)|^2 + \mu |\hat{\phi}_i(k) - \hat{\phi}_i(k-1)| = 0 \quad (5)$$

And, let's compute the derivative of $J(\hat{\phi}_i(k))$, we obtain:

$$2[\Delta y_i(k) - \phi_i(k-1)] - [\Delta u_i(k-1)] + 2\mu[\phi_i(k) - \hat{\phi}_i(k-1)] = 0 \quad (6)$$

Then , the following distributed MFAC algorithms is presented:

$$\hat{\phi}_i(k) = \hat{\phi}_i(k-1) + \frac{\eta \Delta u_i(k-1)(\Delta y_i(k) - \hat{\phi}_i(k-1)\Delta u_i(k-1))}{\mu + \Delta u_i(k-1)} \quad (7)$$

$$\hat{\phi}_i(k) = \hat{\phi}_i(1), \text{ if } |\hat{\phi}_i(k)| \leq \epsilon \text{ or } \text{sign}(\hat{\phi}_i(k)) \neq \text{sign}(\hat{\phi}_i(1)) \quad (8)$$

A. Model Free Adaptive Controller Design

To design the MFAC algorithm, a performance function $J(u_i(k))$ is set a:

$$J(u_i(k)) = |\xi_i(k)|^2 + \lambda |u_i(k) - u_i(k-1)|^2 \quad (9)$$

This function used to evaluate the effectiveness of the control input $u_i(k)$ for the i -th agents in a control function, with two terms , the first one is the tracking error term $|\xi_i(k)|^2$ where $\xi_i(k)$ represents the distributed measurement output, and by minimizing $|\xi_i(k)|^2$ ensures that the agent's output closely matches the disired trajectory. The second one is control effect term $\lambda |u_i(k) - u_i(k-1)|^2$ where $u_i(k)$ is the current control input, and $u_i(k-1)$ is the previous control input, and λ is a weighted factor that balances the importance of the control effort.

Subtituting (2) and (3) into (9), then differentiating (9) with respect to $u_i(k)$, and letting it zero, gives:

$$\mathbf{u}_{\text{MFAC}}(k) = \mathbf{u}_{\text{MFAC}}(k-1) + \frac{\rho \phi_i(k)}{\lambda + |\phi_i(k)|^2} \xi_i(k) \quad (10)$$

Where $\rho \in (0,1)$ is a step-size constant, which is added to make (10) general. Using the parameter estimation algorithm (7) and the control law algorithm (10), the MFAC scheme is constructed.

B. Sliding Mode Controller Design

To design the sliding mode control (SMC) for this system, we first define the sliding mode surface, this one guides the system's behavior to ensure robust and accurate tracking of the desired trajectory.

The sliding mode surface is defined as:

$$S_i(k+1) = S_i(k) + e_i(k+1) + \alpha e_i(k) \quad (11)$$

Where $S_i(k)$ represents the sliding surface at the current time step k , $e_i(k)$ is the tracking error , α is a positive constant that influences the dynamics of the sliding surface. The error $e_i(k)$ is defined as the difference between the desired output $y_d(k)$ and the actual output $y_i(k)$.

To ensure that the systm's trajectory is driven toward and remains on the sliding surface, we define a reaching law. The reaching law dictates how quickly the system state converges to the sliding surface and is given by:

$$\Delta S_i(k+1) = -\epsilon T \text{Sign}(k) \quad (12)$$

Where,

$$y_d(k+1) - y_i(k+1) = -\alpha e_i(k) - \varepsilon T \text{Sign}(k) \quad (13)$$

In that equation, ε is a small positive constant that controls the rate of the convergence, T is the sampling period, and $\text{Sign}(k)$ indicates the direction in which the system should move to reach the sliding surface.

By combining the sliding surface definition and the reaching law, we can derive the control law that ensures the desired tracking performance while maintaining robustness.

The final sliding mode control input $\mathbf{u}_{\text{ISM}}(k)$ is designed to be :

$$\mathbf{u}_{\text{ISM}}(k) = u_i(k-1) + \frac{y_d(k+1) - y(k) + \alpha e_i(k) + \varepsilon T \text{Sign}(k)}{\phi_i(k)} \quad (14)$$

To enhance the robustness and adaptability of the control system, the Model Free Adaptive Sliding Mode Control (MFASMC) approach is employed. In this approach, the control input of the system will be:

$$u_i(k) = \mathbf{u}_{\text{MFA}}(k) + \gamma_i \mathbf{u}_{\text{ISM}} \quad (15)$$

Where the parameter γ is a gain factor that adjusts the contribution of the sliding mode control in the control effort and tunes the convergence rate.

C. Stability Analysis

The stability analysis is conducted in two primary steps. The first step focuses on establishing the bounds of the error between the actual parameter and its estimated value. The second step ensures that this error remains within acceptable limits over time, leading to a stable system.

Step 1 : The establishment of the bounds of the error between the estimated and actual values of the system's parameter, denote as $\tilde{\phi}_i(k) = \phi_i(k) - \hat{\phi}_i(k)$, starting from the foundational equation derived from the compact dynamic linearization model in equation (2) along with the PPD estimation equation (7), we have:

$$\tilde{\phi}_i(k) = \hat{\phi}_i(k+1) + \frac{\eta \Delta u_i(k-1)}{\mu + |\Delta u_i(k-1)|^2} * ((\Delta y_i(k) - \hat{\phi}_i(k-1) \Delta u_i(k-1))) - \phi_i(k) \quad (16)$$

Here we can write the following equation to facilitate the derivation:

$$\phi_i(k) = \phi_i(k-1) + (\phi_i(k) - \phi_i(k-1)) \quad (17)$$

Then by simplifying the previous equation, we have:

$$\tilde{\phi}_i(k) = (\hat{\phi}_i(k+1) - \phi_i(k-1)) + \frac{\eta \Delta u_i(k-1)}{\mu + |\Delta u_i(k-1)|^2} * ((\Delta y_i(k) - \hat{\phi}_i(k-1) \Delta u_i(k-1))) - (\phi_i(k) - \phi_i(k-1)) \quad (18)$$

$$\beta_i(k) = \frac{\eta \Delta u_i(k-1)}{\mu + |\Delta u_i(k-1)|^2} \quad (19)$$

Using equation (19) in equation (18), we get:

$$\tilde{\phi}_i(k) = \tilde{\phi}_i(k-1) + \beta_i(k) * (\Delta y_i(k) - \hat{\phi}_i(k-1) \Delta u_i(k-1) - \phi_i(k) - \phi_i(k-1)) \quad (20)$$

$$\tilde{\phi}_i(k) = (1 - \frac{\eta(\Delta u_i(k-1))^2}{\mu + |\Delta u_i(k-1)|^2}) * \tilde{\phi}_i(k-1) + \phi_i(k-1) - \phi_i(k) \quad (21)$$

$$\tilde{\phi}_i(k) = (1 - \frac{\eta(\Delta u_i(k-1))^2}{\mu + |\Delta u_i(k-1)|^2}) * \tilde{\phi}_i(k-1) - \Delta\phi_i(k) \quad (22)$$

To demonstrate the boundedness of the error, we start by taking the absolute value of both sides of the error equation (22). This is a crucial step, as it allows us to establish an inequality that provides an upper bound on the error term.

Taking the absolute value on both sides and applying the triangle inequality to the right-hand side, we have:

$$|\tilde{\phi}_i(k)| \leq \left| 1 - \frac{\eta(\Delta u_i(k-1))^2}{\mu + |\Delta u_i(k-1)|^2} \right| |\tilde{\phi}_i(k-1)| + |\Delta\phi_i(k)| \quad (23)$$

Let's define:

$$\alpha(k-1) = \frac{\eta(\Delta u_i(k-1))^2}{\mu + |\Delta u_i(k-1)|^2} \quad (24)$$

So equation (23) becomes:

$$|\tilde{\phi}_i(k)| \leq |1 - \alpha(k-1)| |\tilde{\phi}_i(k-1)| + |\Delta\phi_i(k)| \quad (25)$$

Given that $\Delta u_i(k) \neq 0$, $0 < \eta \leq 1$, and $\mu \geq 0$, it follows that $0 < \alpha(k-1) \leq q_1 < 1$.

Next, we replace $1 - \alpha(k-1)$ with its upper bound, a constant q_1 :

$$|1 - \alpha(k-1)| \leq 1 - q_1 \quad (26)$$

$$|\Delta\phi_i(k)| \leq |\phi_i(k-1) - \phi_i(k)| \leq b \quad (27)$$

By combining the inequalities and applying an iterative process, we obtain:

$$|\tilde{\phi}_i(k)| \leq |1 - q_1| |\tilde{\phi}_i(k-1)| + b \quad (28)$$

Continuing this process for previous time steps, we get:

$$|\tilde{\phi}_i(k-1)| \leq |1 - q_1| |\tilde{\phi}_i(k-2)| + b \quad (29)$$

Continuing this process back to the initial condition at $k = 0$ and summing the resulting geometric series:

$$\sum_{j=0}^{k-1} (1 - q_1)^j = \frac{1 - (1 - q_1)^k}{q_1}$$

Thus, we have:

$$|\tilde{\phi}_i(k)| \leq (1 - q_1)^k |\tilde{\phi}_i(0)| + \frac{b}{q_1} (1 - (1 - q_1)^k) \quad (30)$$

As $k \rightarrow \infty$, the term $(1 - q_1)^k$ tends to zero, simplifying the bound to:

$$|\tilde{\phi}_i(k)| \leq \frac{b}{q_1} \quad (31)$$

Therefore, $\tilde{\phi}_i(k)$ is bounded by $\frac{b}{q_1}$, proving that the error remains within this bound as k approaches infinity.

Part 2: In this part, we delve into the convergence properties of the tracking error $\xi_i(k)$. To understand this convergence, we start with the expression for $\xi_i(k)$ as given in equation (3). We aim to express $\xi_i(k)$ in terms of the individual tracking errors $e_i(k)$ and the errors associated with neighboring systems.

The expression for $\xi_i(k)$ is formulated as follows:

$$\xi_i(k) = \sum_{j \in N_i} (e_i(k) - e_j(k)) + d_i e_i(k) \quad (32)$$

In this equation, $\xi_i(k)$ represents the tracking error of the i -th system at time k , taking into account the deviations from its neighbors j in the set N_i and an additional term $d_i e_i(k)$ that depends on the specific characteristics of the i -th system. The parameter d_i is a diagonal matrix term that adjusts the impact of the individual error $e_i(k)$ on the overall error $\xi_i(k)$.

To facilitate analysis, we define the following vectors that aggregate the tracking errors, outputs, and control inputs for all systems:

$$y(k) = \begin{pmatrix} y_1 \\ y_2 \\ y_3 \\ \vdots \\ y_n \end{pmatrix}, \quad e(k) = \begin{pmatrix} e_1 \\ e_2 \\ e_3 \\ \vdots \\ e_n \end{pmatrix}, \quad \xi(k) = \begin{pmatrix} \xi_1 \\ \xi_2 \\ \xi_3 \\ \vdots \\ \xi_n \end{pmatrix}, \quad u(k) = \begin{pmatrix} u_1 \\ u_2 \\ u_3 \\ \vdots \\ u_n \end{pmatrix}$$

Using these definitions, the expression for $\xi_i(k)$ can be compactly rewritten as:

$$\xi_i(k) = (L + D)e(k) \quad (33)$$

Here, L represents the interaction matrix that describes how each system interacts with its neighbors, while D is a diagonal matrix defined by $D = \text{diag}(d_1, d_2, d_3, \dots, d_n)$. This formulation helps us to analyze how the overall system's tracking error is influenced by the individual tracking errors and the interaction structure.

Next, the control input $u(k)$ is updated according to the following rule:

$$u(k) = u(k-1) + \rho \cdot \text{diag} \left(\frac{\hat{\phi}_1(k)}{\lambda + |\hat{\phi}_1(k)|^2}, \frac{\hat{\phi}_2(k)}{\lambda + |\hat{\phi}_2(k)|^2}, \frac{\hat{\phi}_3(k)}{\lambda + |\hat{\phi}_3(k)|^2}, \dots, \frac{\hat{\phi}_n(k)}{\lambda + |\hat{\phi}_n(k)|^2} \right) (L + D)e(k)$$

This update rule accounts for the adjustment of control inputs based on the estimation $\hat{\phi}_i(k)$ of the parameters, where λ is a regularization parameter that ensures stability. This formulation leads to:

$$u(k) = u(k-1) + \rho H_1(k)(L + D)e(k) \quad (34)$$

where $H_1(k)$ is a diagonal matrix whose elements are functions of the estimated parameters $\hat{\phi}_i(k)$. The evolution of the output $y(k)$ is described by:

$$y(k+1) = y(k) + \phi(k)\Delta u(k)$$

In this context, $\Delta u(k)$ represents the change in the control input:

$$\Delta u(k) = u(k) - u(k-1)$$

and $H_\phi(k)$ is defined as:

$$H_\phi(k) = \text{diag}(\phi_1(k), \phi_2(k), \phi_3(k), \dots, \phi_n(k))$$

By substituting the expression for $u(k)$ from equation (34) into the output evolution equation, we obtain:

$$e(k+1) - e(k) = y(k) - y(k+1)$$

Rearranging the terms, we get:

$$e(k+1) = e(k) + y(k) - y(k+1)$$

Substituting the previously derived expression for $y(k+1)$, we have:

$$e(k+1) = e(k) - H_\phi(k)\rho H_1(k)(L+D)e(k)$$

This can be rewritten as:

$$e(k+1) = (I - \rho\Theta(k))e(k) \quad (35)$$

where $\Theta(k)$ is defined by:

$$\Theta(k) = \sum(k)(L+D) = H_\phi(k)H_1(k)(L+D)$$

with:

$$\sum(k) = \text{diag}\left(\frac{\hat{\phi}_1(k)}{\lambda + |\hat{\phi}_1(k)|^2}, \frac{\hat{\phi}_2(k)}{\lambda + |\hat{\phi}_2(k)|^2}, \frac{\hat{\phi}_3(k)}{\lambda + |\hat{\phi}_3(k)|^2}, \dots, \frac{\hat{\phi}_n(k)}{\lambda + |\hat{\phi}_n(k)|^2}\right)$$

which can be expressed in diagonal form as:

$$\sum(k) = \text{diag}(\mathcal{V}_1(k), \mathcal{V}_2(k), \mathcal{V}_3(k), \dots, \mathcal{V}_n(k))$$

where each $\mathcal{V}_i(k)$ is given by:

$$\mathcal{V}_i(k) = \frac{\hat{\phi}_i(k)}{\lambda + |\hat{\phi}_i(k)|^2}, \quad i = 1, 2, 3, \dots, n$$

Thus, we have:

$$\Theta(k) = \text{diag}(\mathcal{V}_1(k), \mathcal{V}_2(k), \mathcal{V}_3(k), \dots, \mathcal{V}_n(k))(L+D)$$

To ensure convergence of the tracking error, we impose the condition:

$$\|I - \rho\Theta(k)\| < 1 \quad (36)$$

This condition guarantees that the tracking error $e(k)$ will approach zero as $k \rightarrow \infty$. Consequently, we have:

$$\lim_{k \rightarrow \infty} \|e(k+1)\| = 0$$

This result indicates that the tracking error will converge to zero, demonstrating the effectiveness of the proposed control strategy in achieving desired tracking performance.

IV. QUADRIPE-FREQUENCY DATA PROCESSING METHOD FOR DC MOTORS SPEED REGULATION

To regulate the speed of DC motors accurately, we employ a sophisticated data-driven binary containment control method, which requires precise measurement and processing of encoder data. This section describes the methodology and hardware used for speed regulation, including the calculation of motor speed using the quadruple-frequency data processing (QFDP) method.

A. Hardware Implementation

The DC brushed motors have a rated voltage of 12V, an unloaded speed of 293 ± 21 RPM, and a rated current of 0.36 A. The gear ratio of 20 means that the output speed of the motor is 1/20 of the rotor speed, resulting in higher torque with a higher gear ratio. The Hall encoders used have 13 pulses per revolution (ppr), meaning each full rotation generates 13 pulse signals.

To enhance measurement accuracy, we employed a quadruple-frequency data processing method. This technique quadruples the effective resolution of the encoder by processing the output pulse signals at four times the frequency, thus increasing measurement precision by a factor of four.

B. Data Processing Method

The motor speed is measured in revolutions per second (r/s). The following equations are used to calculate the speed based on encoder measurements and sampling:

1. Calculation of Rounds:

The total number of "rounds" that the encoder measures is given by:

$$T = \text{Encoder line count} \times \text{Reduction Ratio} \times 4 \quad (37)$$

Here, the Encoder line count is 13, and the Reduction Ratio is 20. The factor of 4 accounts for the quadrature encoding, which effectively quadruples the resolution.

2. Calculation of Number of Rotations:

The number of rotations can be determined using:

$$\text{Number of Rotations} = \frac{m}{\text{Rounds Per T}} \quad (38)$$

Where m is the total count from the encoder, and Rounds Per T is the number of encoder counts per revolution, derived from Equation (37).

3. Calculation of Speed:

The speed of the motor in resolution per second (r/s) is given by:

$$v = \frac{\text{Number of Rotations}}{T} \quad (39)$$

Here, v represents the speed, calculated by dividing the number of rotations by the time T it takes to complete those rotations.

4. Combining the Equations:

Substituting Equation (38) into Equation (39), we obtain:

$$v = \frac{m}{\text{Rounds Per T} \times T} \quad (40)$$

This final equation integrates encoder measurements and the sampling period to provide an accurate speed regulation formula using the QFDP method.

In our system, the sampling period, which is set by a timer, defines how frequently speed measurements are taken. Each sampling interval triggers an interrupt where the controller samples the motor speed and updates control commands accordingly.

The quadruple-frequency method, implemented through software, is crucial for maximizing encoder measurement precision, resulting in more accurate speed control for the motor system.

V. EXTENSION TO SWITCHING TOPOLOGY

In this section, the proposed design is extended to the multiagent system with switching topology