$$\widetilde{E}_0 < E_0$$