$W_{loc}^S(p_0)$