$$H^k = \left\{ x \in \mathbb{R}^k : x_1 \ge 0 \right\}$$