$$f(x) = \frac{1}{1 + e^{-x}} \qquad f'(x) = f(x)\,(1 - f(x))$$