

Queues

Linear Queue is a structure in which new elements are added at one end (Rear end) & the existing elements are deleted from other end (front end).

It is a FIFO type of list

Array Representation :-

$$R=1 \quad F=1$$

							↑
	0	1	2	3	4	5	6
FR							7

1st step

Empty Queue

$$R=0 \quad F=0$$

							↑
	0	1	2	3	4	5	6
FR							7

One element Queue

2nd step

$$R=1 \quad F=0$$

10	20						
0	1	2	3	4	5	6	7
F	↑						R

Two element Queue

$$R=2 \quad F=0$$

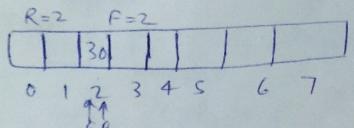
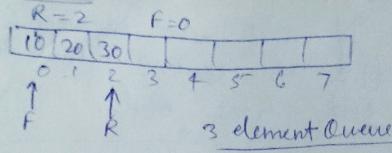
10	20	30					
0	1	2	3	4	5	6	7
F	↑	R					

Three element Queue

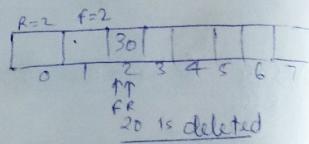
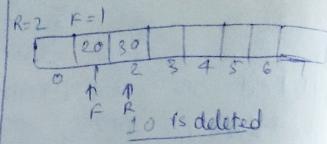
When an element is inserted in the Queue, the value of rear is incremented by one.

During the insertion of the 1st element in the front is always incremented by one. After that the front will not be changed.

(Solution)



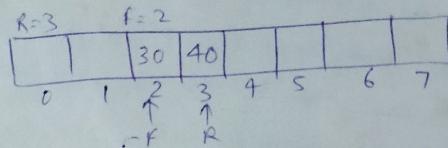
Two elements (10, 20) deleted from front



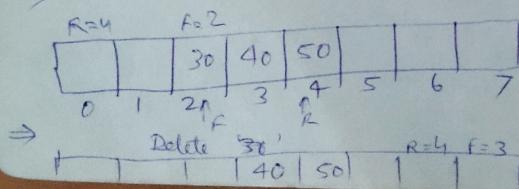
when an element is removed from the Queue
the value of Front is incremented by one

Suppose that if we insert any element the
above obtained Queue, then it will go the
next position of the previous inserted element

⇒ Insert '40'



⇒ Insert '50'



Dynamically

Implementation of Queue -

It can also be implemented in 2 ways as other lists -

1. static (Using arrays)
2. Dynamic (using pointers)

static - size of array is declared at design time or before the processing starts, i.e. exact no. of elements to be stored in Queue should be known.

In this case -

(front) = Beginning of the array = LB

(Rear) = Last location of array = UB

So, Total no of elements present in Queue = $R - f + 1$

If $R < f$ then there will be no element in Q
when R & f are +ve integers.

$$\begin{aligned} \text{Total} &= R - f + 1 \\ 0 &= 2 - 3 + 1 \quad (R=2 \quad f=3) \\ &= 1 - 2 + 1 \quad (R=1 \quad f=2) \\ &= 0 - 1 + 1 \quad (R=0 \quad f=1) \end{aligned}$$

and if $R=f$ then 'Empty Queue'

Dynamic -

size of Queue may be decided at run time. It is implemented using pointers

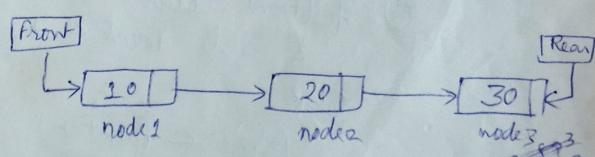


Fig: A Queue implemented using pointers

Operations on Queue :-

① Insertion.

Algo:-

QINSERT (MAXSIZE, ITEM)

① Initialize front $\leftarrow 0$ and rear $\leftarrow 1$.

② If Rear \geq MAXSIZE.

Print Q Overflow and return // check cond

else

Set Rear \leftarrow rear + 1

// At new val
of rear

③ Queue[rear] \leftarrow item

End

② Deletion.

Algo:-

QDELETE (MAXSIZE, ITEM)

① If front < 0

Print Queue is empty & return // check cond

else

item \leftarrow Queue [Front]

② If front = rear

set front \leftarrow + 1

// find new val
of front
rear \leftarrow -1

else

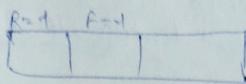
front \leftarrow front + 1

End

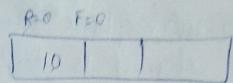
③ Create

create \leftarrow create Q as an empty queue
= declare Q(1:n) & front \leftarrow rear \leftarrow 0

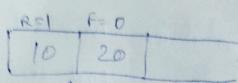
Limitation of a simple Queue



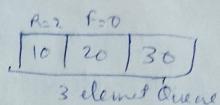
Queue Initially ✓



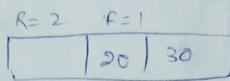
one element Queue



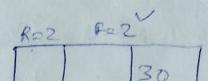
2 element Queue



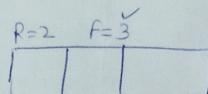
3 element Queue



on deleting an element



on deleting an element



on deleting next element

~~Rear end = last location of array~~

If we want to insert an element, it should be inserted to the rear end. But ~~now~~ now, element can't be added because ~~rear~~ (Rear end = last location of array)

To remove this problem, CIRCULAR QUEUE will be used.

↙ // check condition
at new value of front

↑ memory needed

Circular Queue -

A Circular queue is a queue in which insertion of a new element is done at the very first location, if the last location of the queue is full.

It is possible to insert new elements, if any of those locations are empty.

i.e. A circular Queue is a Queue in which the first element comes just after the last element it appears as a loop of wire, whose both ends are connected together.

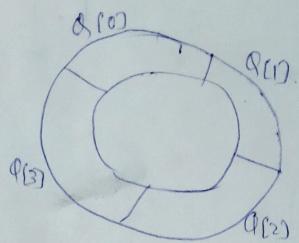


fig: A circular Queue (4 elements can be added at a time)
& INSERT (Q[MAXSIZE], ITEM)

```

if (F == (R+1) % MAXSIZE)
    write Overflow & exit
else if (F == -1)
    set F ← 0
    R ← 0
else R ← ((R+1) % MAXSIZE)
    Q[R] ← ITEM

```

③ Exit

QDELETE (Q[MAXSIZE], ITEM)

```

if (F == -1)
    write Underflow & exit
else ITEM ← Q[F]

```

② if F = R

set F ← 1

R ← -1

else F ← ((F+1) % MAXSIZE)

Alg for Q

- ①
- ②
- ③
- ④

②

Double Ended Queue (D-Queue/ Deque)

It is Queue in which both Insertion & Deletion are performed at the either end.

There are 2 types of D-Queue, due to the restrictions put to perform either the Insert "or" deletion only at one end.

1. Input-restricted DQ

2. Output-restricted DQ

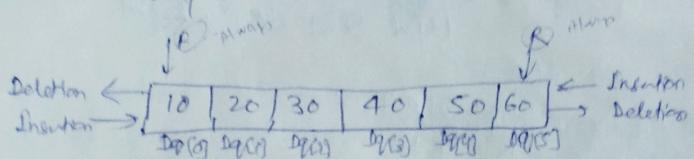


fig. A D-Queue with 6 elements

In a D-Q 4 types of operations can be performed

- ① Insertion of an element at the Rear end -
Front _____
- ② _____
Front _____
- ③ Deletion _____
Front _____
- ④ _____
Rear _____

\times [Input restricted DQ : All operations are valid]
Output _____ ; ①②③ are valid

Algo's for above operations -

① DQ(Q(MAX), ITEM)

If $R = (\text{MAX} + 1)$

Print Q is full & exit

else

$R \leftarrow R + 1$

$Q[R] \leftarrow \text{ITEM}$

End

② DQ(Q(MAX), ITEM)

If $(F = 0)$

Print Q is full & exit

else $F \leftarrow F + 1$

$Q[F] \leftarrow \text{ITEM}$

End

{ needed } \downarrow

③ DQ (Q(MAX), ITEM)

if $F < Q$
else
Print Q is empty & exit
~~ITEM ← Q[F]~~
ITEM ← Q[F]
F ← F+1
end

④ DQ (Q(MAX), ITEM)

if $R >= MAX$
Print Q is empty & exit
else
ITEM ← Q[R]
R ← R+1
end

Binary
the
d.p.s.
the

on
upw

Priority Queues -

The elements are inserted/deleted according to their priority.

In stack or simple queue the operations are performed according to their insertion time. The key matching but here Priority is taken into consideration.

In priority Queue, elements are sorted by priority & proceeded from Top to Bottom, maintaining a pointer. We have following basic priority Queue choices -

① sorted array or list - Elements are sorted out according to priority.
Deletion of the smallest element from the sorted list is very easy, but insertion of a new element in a sorted list is a little bit difficult.

Apt

① In C

② All

(+
qu

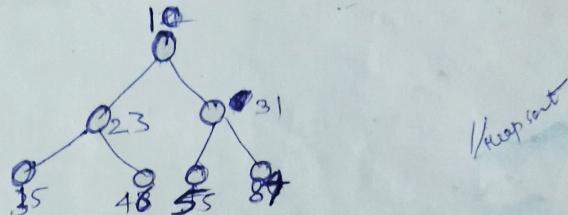
③ P

④

⑤ P

Thus sorted arrays are suitable when a few insertions occur into the priority queue.

② Binary Heaps -



Binary Heaps form a structure in which key of the root of any subtree is less than all its descendants. Thus min key is always at the root of the tree.
If a new element is inserted, it is placed on the leaf node first. Then element is relocated upward until it gets its proper location.

Application of Queues: —

- ① In CPU scheduling priority Queue is used
- ② All type of customer service center S/W's (for railway reservation) are designed using queues to store customer info
- ③ Printers are working on the concept of Q
- ④ Printer driver routines are also working on this principle.

