

The output of Combinational circuit is depends on present inputs only.

It does not depend on past and future inputs.

for example:-

Adder

Subtractor

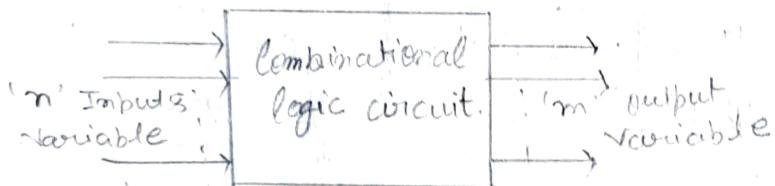
Encoder

Decoder

Multiplexer and De-multiplexer.

Characteristics of combinational circuit:

- Working speed is fast
- Time independent circuit
- There is no feedback element
- it doesn't required clock signal
- ⇒ Circuit design is not complex.



A Combinational circuit are three types which is describe below:-

1 Arithmetic and logic circuit

Adder, Subtraction, Multiplication, Comparator etc.

2. Data manipulation:-

Multiplexers, Demultiplexers, Encoder, Decoder and Priority.

3. Code converter:-

Binary to gray, gray to binary etc.

Adders :-

Adders circuit is a digital circuit that performs addition in computer. It is the basic circuit in arithmetic logic units.

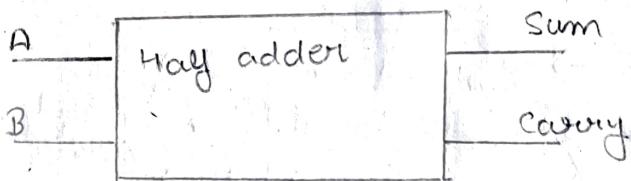
The adder is two type

1. Half adder

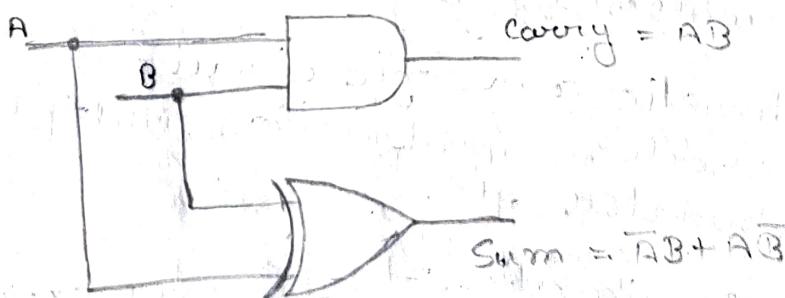
2. Full adder

Half adder :-

when we add two binary numbers, we start with the least significant column. This means that we have to add two bits with the possibility of a carry. The circuit used for this is called a half-adder.



Block diagram of half-adder

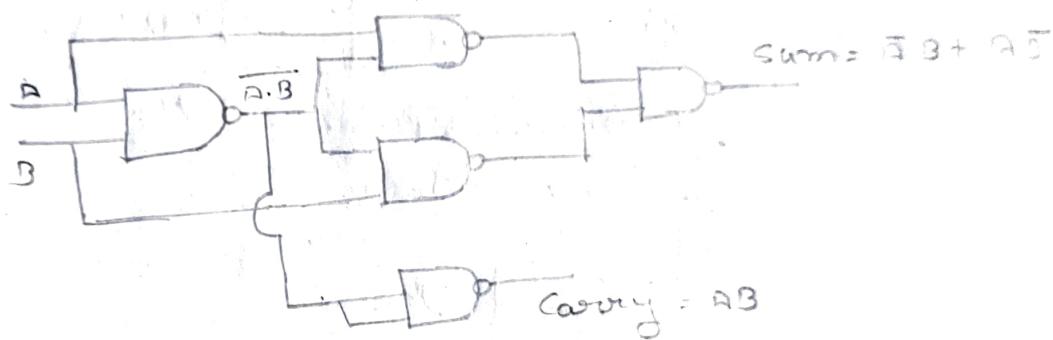


Logic of half adder

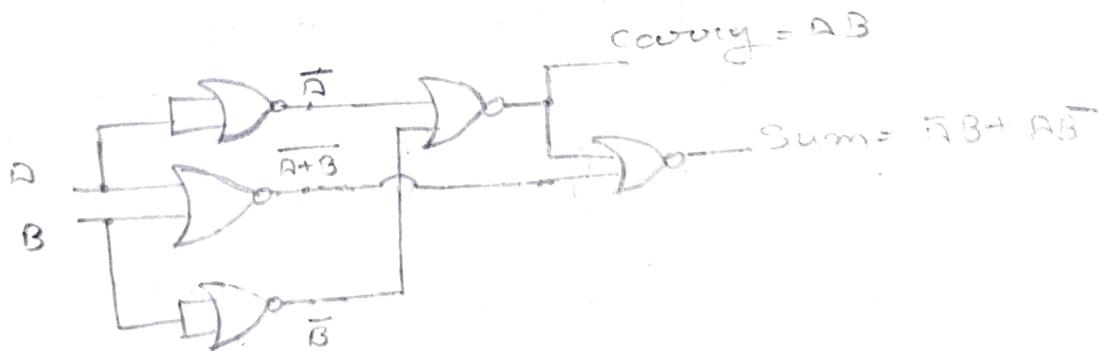
Truth table :-

A	B	Carry $\bar{A}B$	sum $\bar{A}B + A\bar{B}$
0	0	0	0
0	1	0	1
1	0	0	1
1	1	1	0

Half adder implemented by NAND gates :-



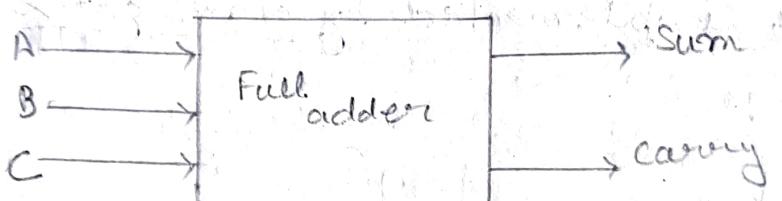
Half adder implemented by NOR gates :-



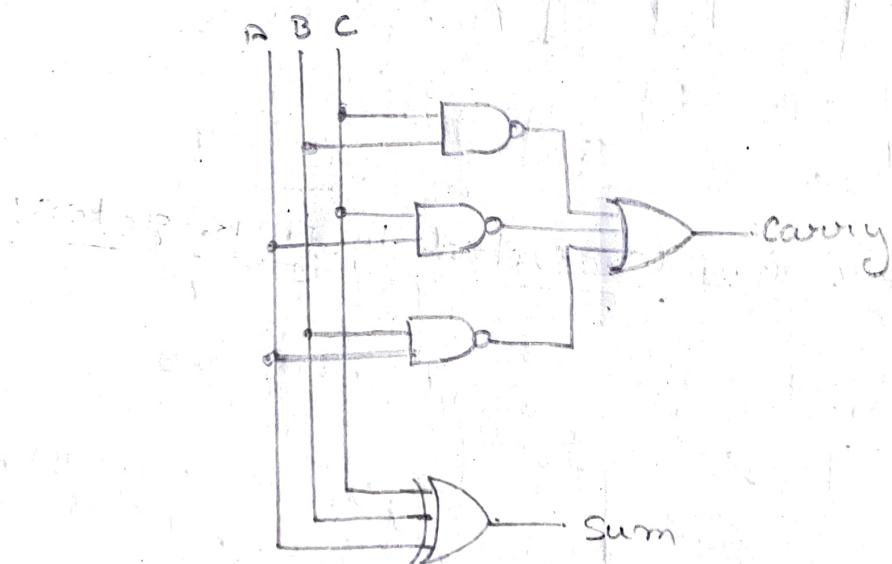
In Half adder we only add two binary bits. we can not add three binary bits. It is the major limitation of half adder.

Full adder:-

For the higher-order columns, we have to use a full-adder, a logic circuit that can add 3 bits at a time. The third bit is the carry from a lower column. This implies that we need a logic circuit with three inputs and two outputs.



Block diagram of full adder.



Logic Diagram of Full adder

K-map:-

		00	01	11	10
		0	0	1	0
C\B		0	0	1	1
0	0	0	1	1	1
1	0	1	0	1	0

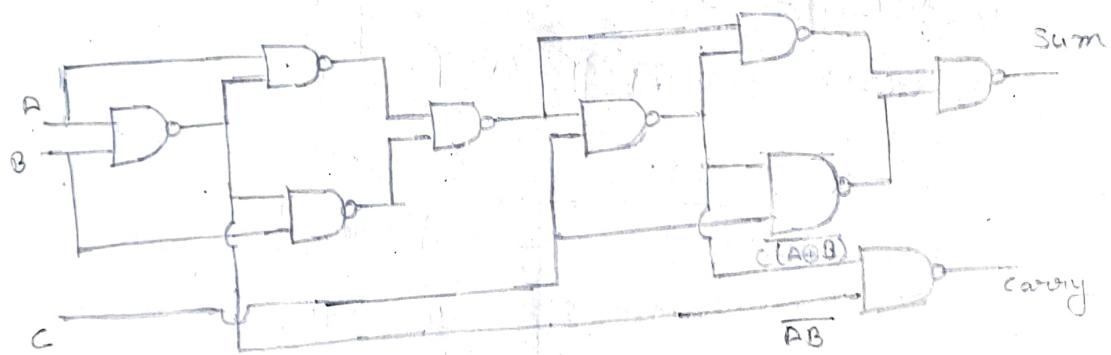
$$\text{Carry} = AB + BC + AC$$

		00	01	10	10
		0	1	0	1
C\B		0	1	0	0
0	0	0	1	0	1
1	0	1	0	1	0

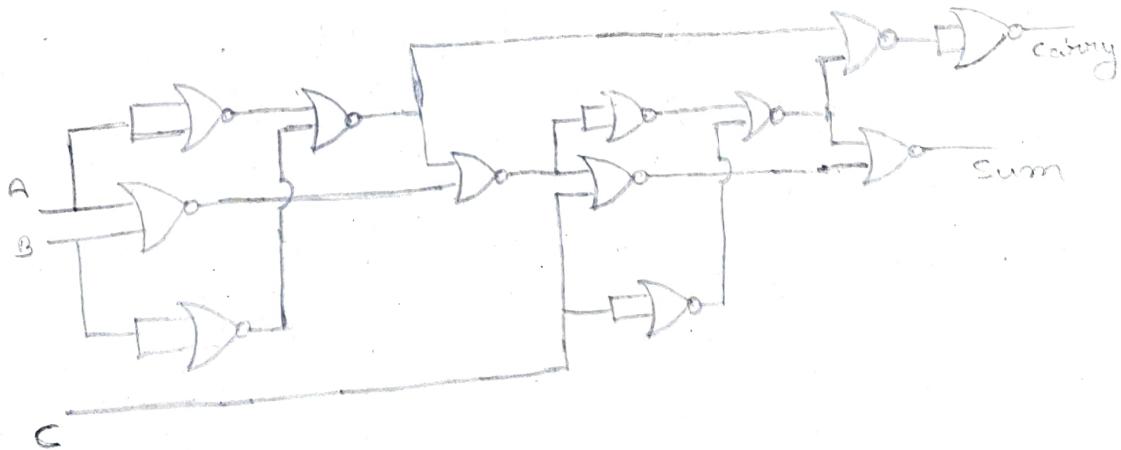
Truth table:-

A	B	C	Carry $AB + BC + AC$	Sum $A \oplus B \oplus C$
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	1	1

Full adder implemented by NAND gates:-



Full adder implemented by NOR gates:-



Subtractor circuit:-

There are two type subtractor:-

1. Half subtractor
2. full subtractor

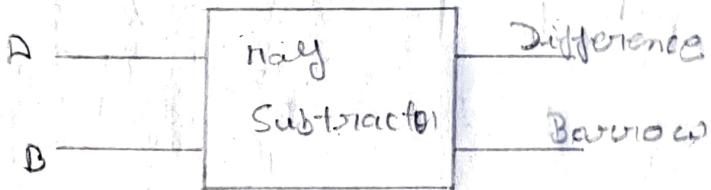
Half subtractor:-

A half subtractor is a combinational logic circuit that performs a subtraction operation of two binary digits.

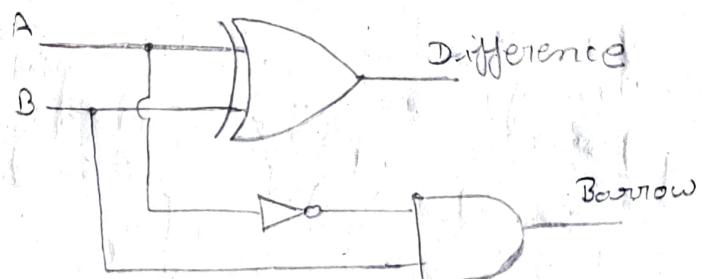
The expression of half subtractor is -

$$\text{Difference } d = A \oplus B = \overline{A}B + A\overline{B}$$

$$\text{Borrow } b = \overline{A} \cdot Y$$



Block diagram of half subtractor:-

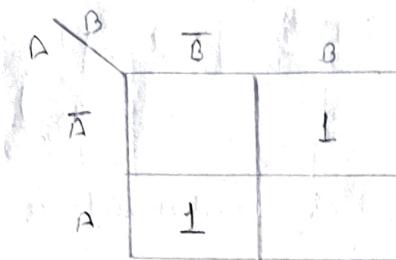


Logic Diagram of half subtractor:-

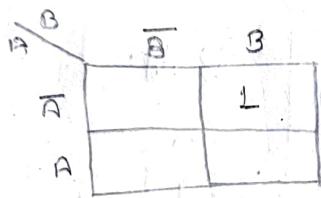
Truth table :-

A	B	Difference $\overline{A}B + A\overline{B}$	Borrow $\overline{A}B$
0	0	0	0
0	1	1	0
1	0	1	0
1	1	0	0

K - Map :-

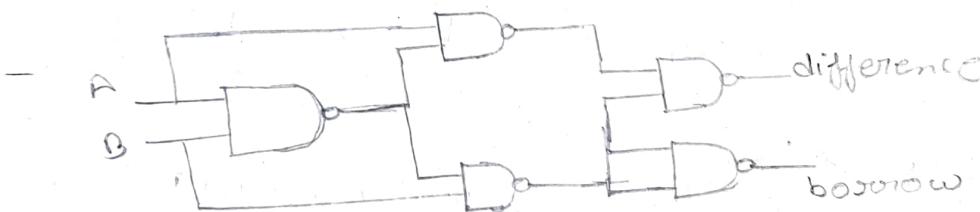


K-map of Difference



K-map of Borrow

Half subtractor using NAND gates



Full subtractor :-

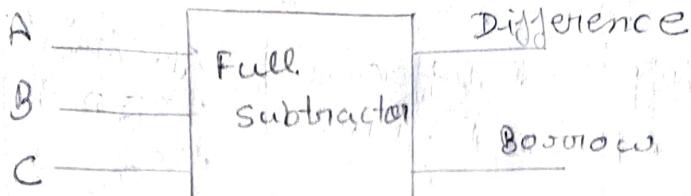
A full subtractor is a combinational logic circuit that performs a subtraction operation of three binary digits.

The third input is borrow-in.

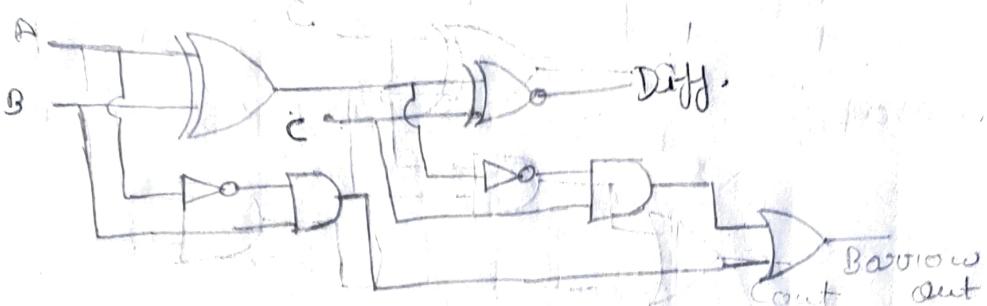
The expression of full subtractor is -

$$\text{difference } d = (A \oplus B) \oplus C$$

$$\text{Borrow } b = \overline{A}B + (\overline{A} \oplus B)$$



block diagram of Full subtractor



Logic diagram of full subtractor

Truth table:-

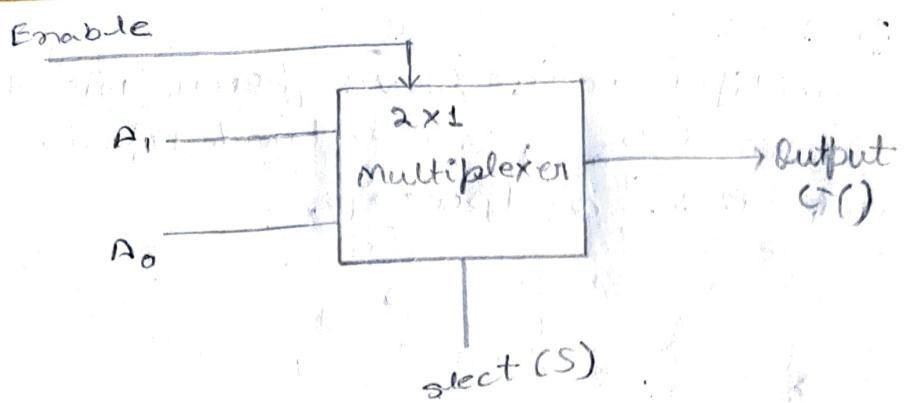
A	B	C (Borrow'in)	Diff.	Borrow
0	0	0	0	0
0	0	1	1	1
0	1	0	1	1
0	1	1	0	1
1	0	0	1	0
1	0	1	0	0
1	1	0	0	0
1	1	1	1	1

Multiplexers:-

Multiplex means many into one. A multiplexer is a circuit with many inputs but only one output. it is also called a data selector and control inputs are termed select inputs.

2×1 multiplexer:-

In 2×1 multiplexer there are only two inputs, 1 selection line and single output.



Block diagram of a 2×1 multiplexer

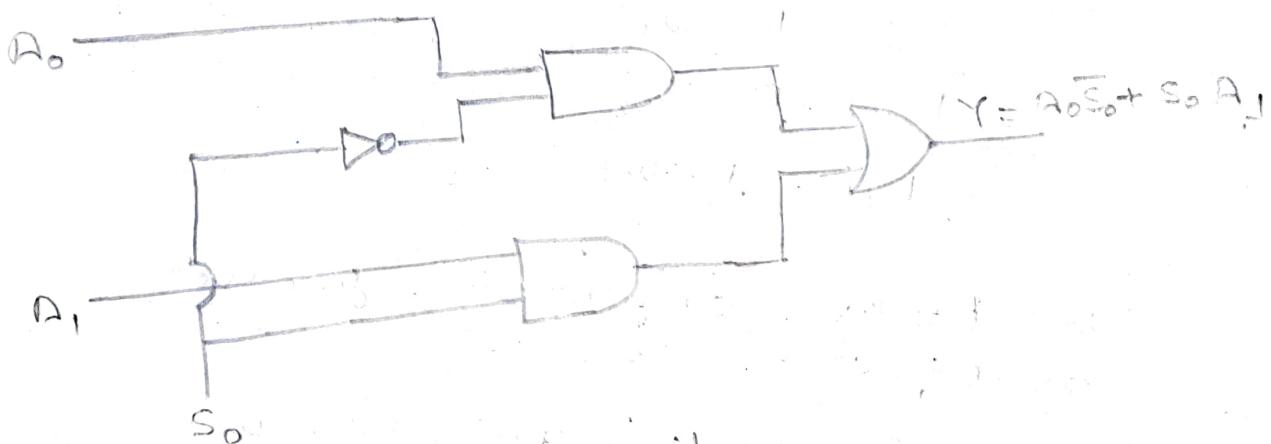
Truth table :-

S_0	Y
0	A_0
1	A_1

two input A_0, A_1
one control input S_0
and output Y

The logic expression for 2×1 multiplexer
is -

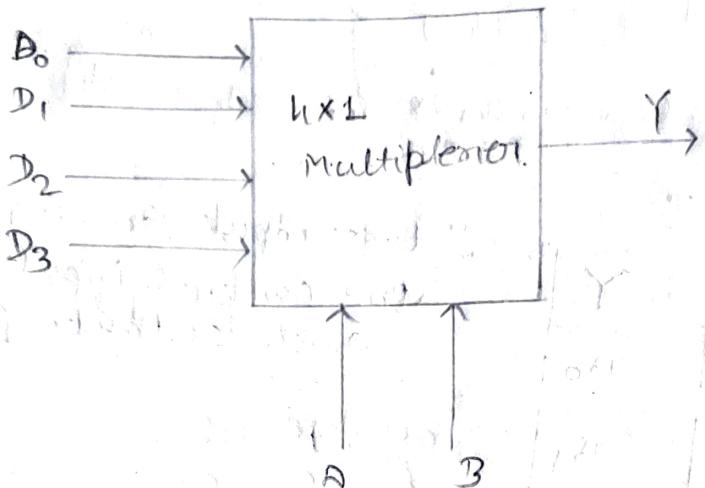
$$Y = \overline{S_0}A_0 + S_0A_1$$



Logic circuit of 2×1 multiplexer

4x1 multiplexer:-

In 4x1 multiplexers have four input
D₀, D₁, D₂ and D₃, 2 control inputs
A, B and one output Y.



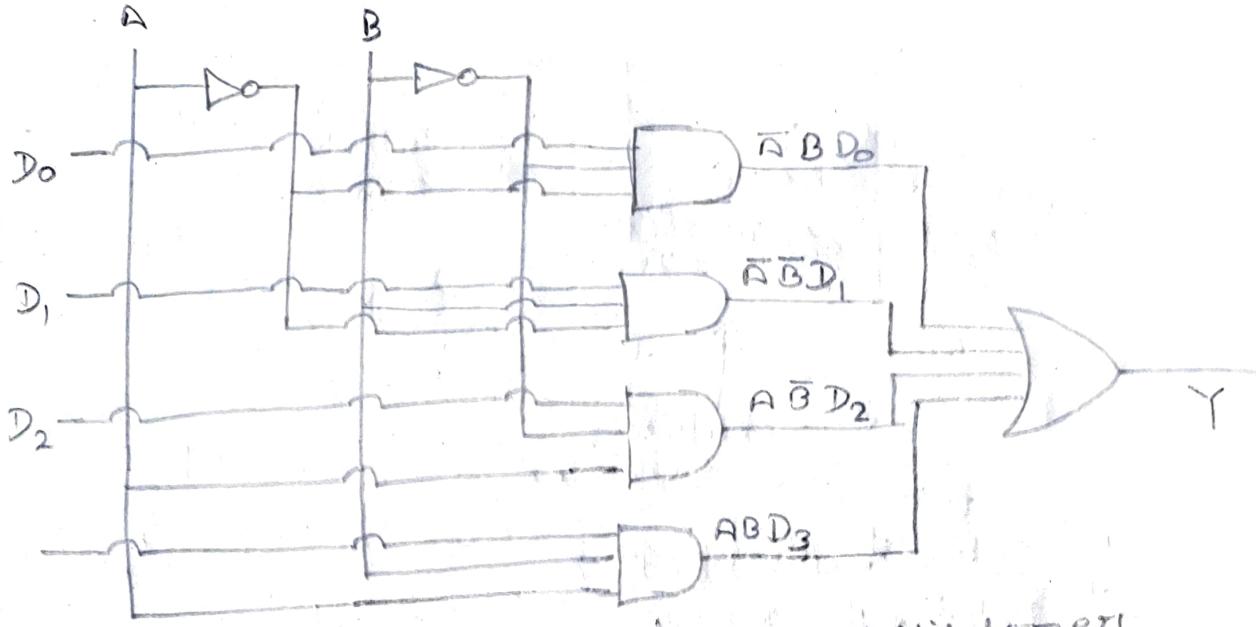
Block diagram

Truth table:-

A	B	Y
0	0	D ₀
0	1	D ₁
1	0	D ₂
1	1	D ₃

The boolean expression for 4x1 multiplexer is,

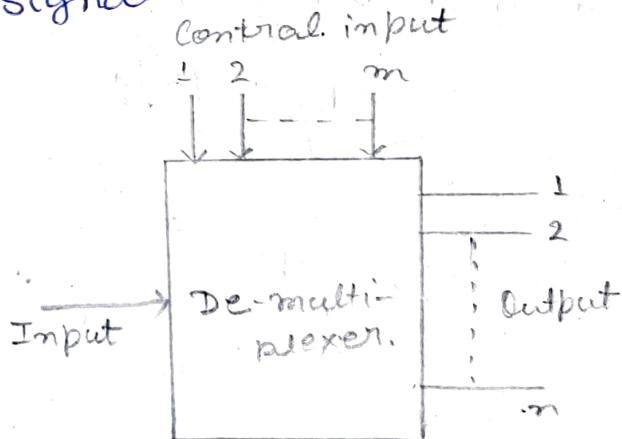
$$Y = \bar{A}\bar{B}D_0 + \bar{A}BD_1 + A\bar{B}D_2 + AB\bar{D}_3$$



Logic Diagram of 4×1 multiplexer

Demultiplexers:-

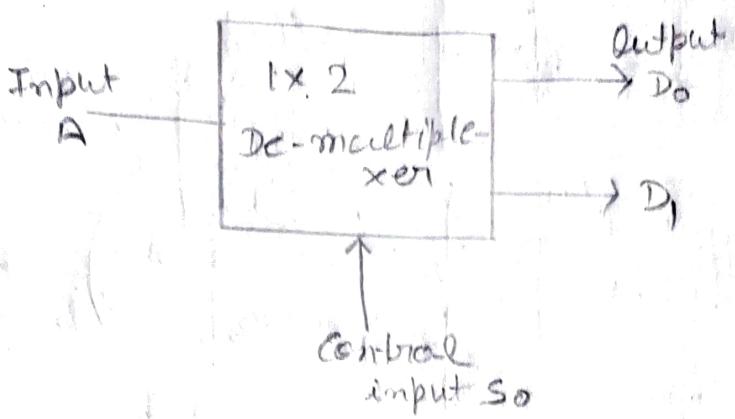
Demultiplexer means one into many. Demultiplexer is a logic circuit with one input and many outputs. By applying control signals, we can steer the input signal to one of the output lines.



Block diagram of De-multiplexer

1×2 Demultiplexer

In 1×2 De-multiplexer, there are only two outputs D_0 & D_1 , and one control input S_0 and single input A .



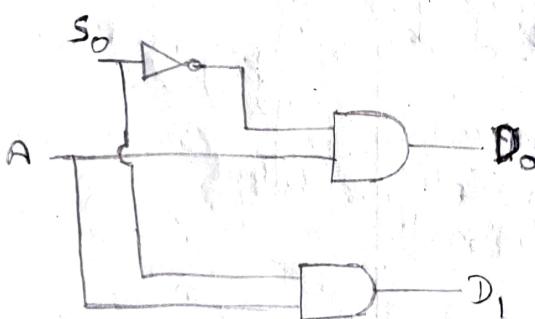
Truth table

S ₀	D ₀	D ₁
0	0	A
1	A	0

The logic expression of the term Y is as follows:-

$$Y_0 = \cancel{S_0} A \quad D_0 = \cancel{S_0} A$$

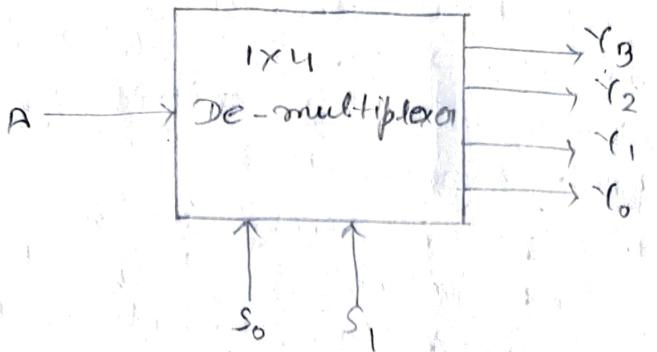
$$Y_1 = S_0 A$$



Logic circuit of 1x2 Demultiplexer

1x4 De-multiplexer:-

There are four outputs Y₀, Y₁, Y₂ and Y₃, 2 Control inputs S₀ and S₁, and single input A.



Block diagram

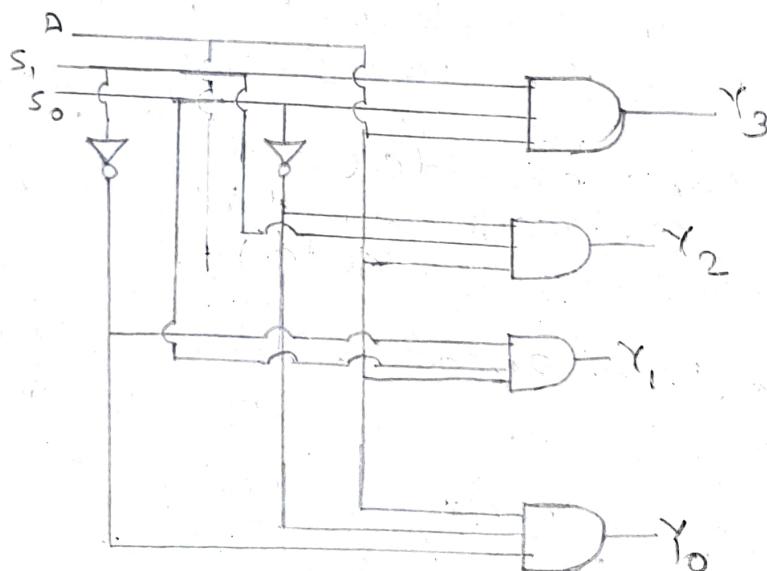
Truth table:-

Control inputs		Output			
S_0	S_1	Y_3	Y_2	Y_1	Y_0
0	0	0	0	0	A
0	1	0	0	A	0
1	0	0	A	0	0
1	1	A	0	0	0

The logic expression is.

$$Y_0 = \overline{S_0} \overline{S_1} A, \quad Y_1 = \overline{S_0} S_1 A$$

$$Y_2 = S_1 \overline{S_0} A, \quad Y_3 = S_1 S_0 A$$



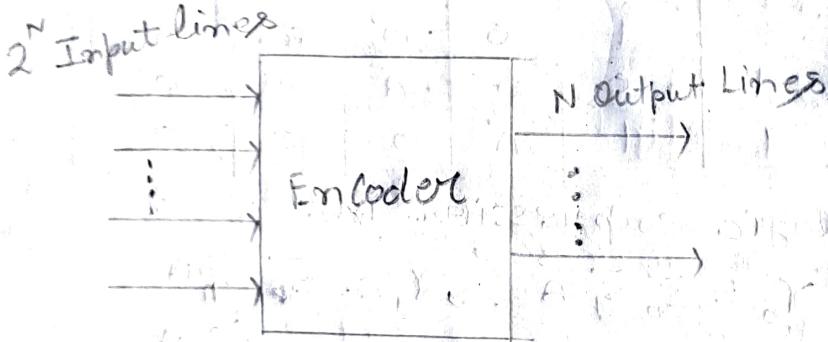
Logic circuit of 1x4 De-multiplexer

Encoder :-

An encoder converts an active input signal into a coded output signal. An encoder changes the binary information into ~~N output lines~~ ~~the binary information~~.

The binary information is passed in the form of 2^N input lines. The output lines define the N-bit code for the binary information.

The produced N-bit output code is equivalent to the binary information.



There are various types of encoders which are as follows:-

⇒ 4 to 2 line encoder

(There are total four inputs and two outputs).

⇒ 8 to 3 line encoder (Octal encoder)

(There are 8 inputs and 3 outputs).

Decimal to BCD Encoder:-

The decimal to binary encoder usually consists of 10 input lines and 4 output lines.

Each input line corresponds to the each decimal digit and 4 outputs

correspond to the BCD code.
when button 3 is pressed, the C and D OR gates have high inputs; therefore the output is.

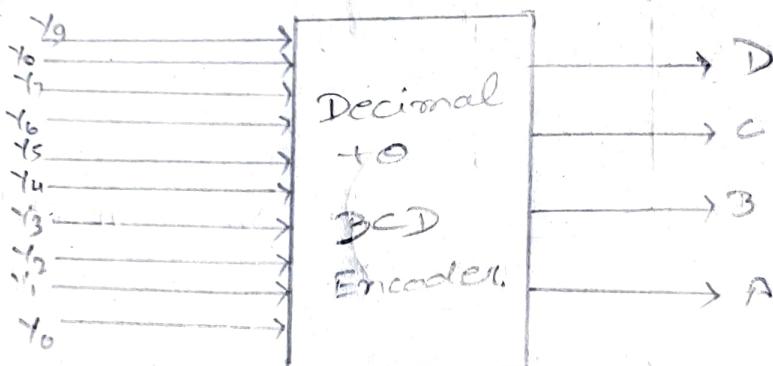
$$ABCD = 0011$$

if button 5 is pressed, the output becomes

$$ABCD = 0101$$

when switch 9 is pressed,

$$ABCD = 1001$$



The truth table for decimal to BCD converter is as follows:-

Y_9	Y_8	Y_7	Y_6	Y_5	Y_4	Y_3	Y_2	$Y_1 + Y_0$	A	B	C	D
0	0	0	0	0	0	0	0	0	1	0	0	0
0	0	0	0	0	0	0	0	1	0	0	0	1
0	0	0	0	0	0	0	1	0	0	0	0	1
0	0	0	0	0	0	1	0	0	0	0	0	1
0	0	0	0	0	0	1	0	0	0	0	1	0
0	0	0	0	0	1	0	0	0	0	0	1	0
0	0	0	0	1	0	0	0	0	0	0	1	0
0	0	0	1	0	0	0	0	0	0	1	1	0
0	0	1	0	0	0	0	0	0	0	0	1	1
0	1	0	0	0	0	0	0	0	1	0	0	0
1	0	0	0	0	0	0	0	0	0	1	0	0

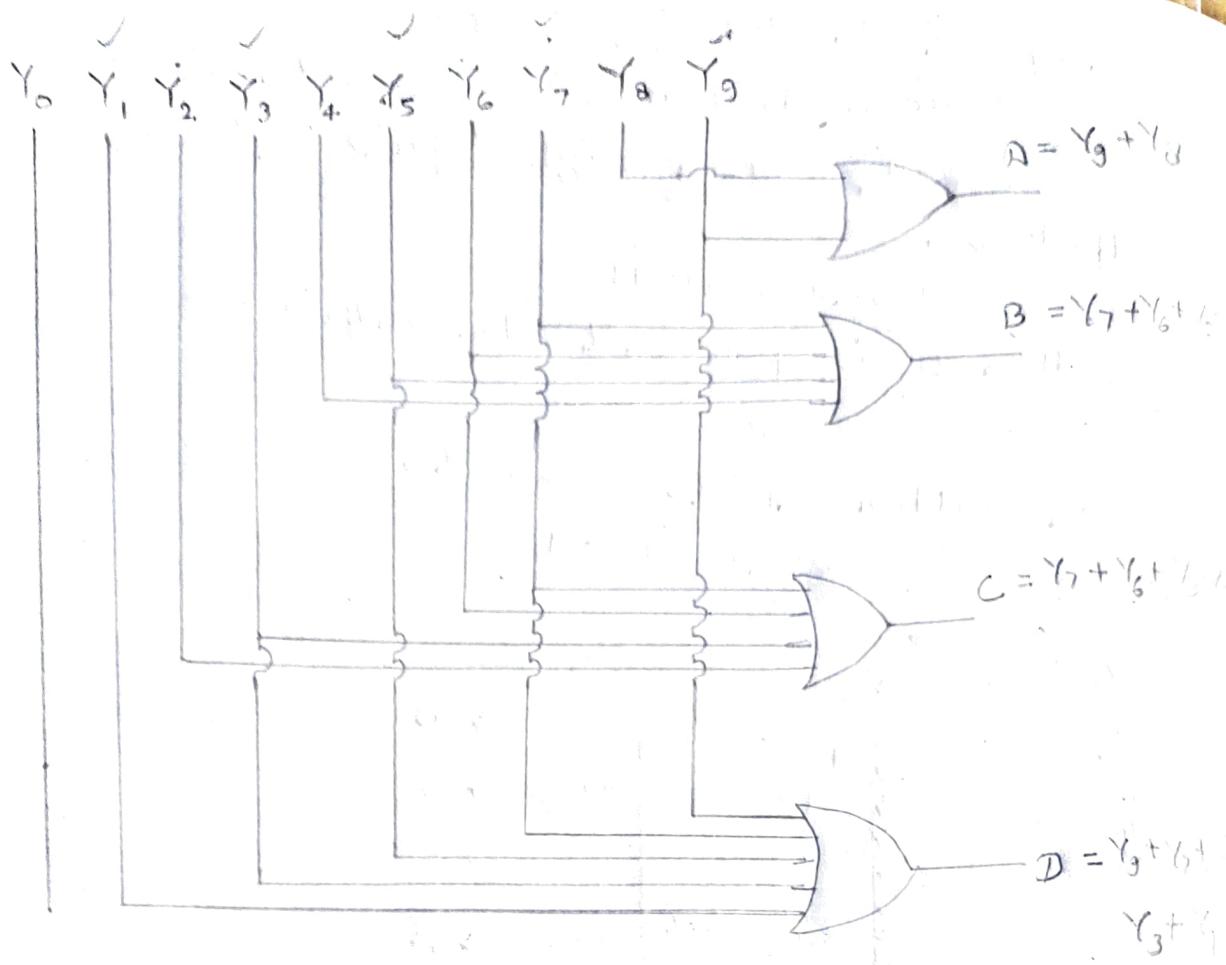
Logic expression for A,B,C,D:-

$$A = Y_9 + Y_8$$

$$B = Y_7 + Y_6 + Y_5 + Y_4$$

$$C = Y_7 + Y_6 + Y_3 + Y_2$$

$$D = Y_9 + Y_7 + Y_5 + Y_3 + Y_1$$



⇒ Priority Encoder:-

uses of Encoder:-
These system are very easy to use in all digital system.

Encoders are used to convert a decimal number into the binary number. The objective is to perform a binary operation such as addition, subtraction, multiplication, etc.

Decoder:-