

# Chapter 3

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**Theorem 3.1 Riemann's theorem on removable singularities:**  *$f$  hol on  $\Omega - \{z_0\}$ , if  $f$  is bounded on  $\Omega - \{z_0\}$ , then  $z_0$  is a removable singularity*

**Corollary 3.2:** *Suppose that  $f$  has an isolated singularity at the point  $z_0$ , Then  $z_0$  is a pole*

$\iff |f(z)| \rightarrow \infty$  as  $z \rightarrow z_0$

Isolated singularities belong to one of three categories:

1. Removable singularities ( $f$  bounded near  $z_0$ )

2. Pole singularities ( $|f(z)| \rightarrow \infty$  as  $z \rightarrow z_0$ )

3. Essential singularities