

p210.

$$3. \iint_D xy \, dx \, dy = \lim_{n \rightarrow \infty} \frac{1}{n^2} \sum_{k=1}^n \sum_{j=1}^n \left(\frac{k}{n} \cdot \frac{j}{n} \right) = \lim_{n \rightarrow \infty} \frac{1}{n^4} \cdot \sum_{j=1}^n kj = \lim_{n \rightarrow \infty} \frac{1}{n^4} \left(\frac{1+n}{2} n \right)^2$$

$$= \lim_{n \rightarrow \infty} \frac{(n+1)^2}{4n^2} = \frac{1}{4}$$

$$\text{故 } \iint_D xy \, dx \, dy = \frac{1}{4}$$