## STAT 201

Week 6

• In some situations we are not mainly interested on what is the specific value of a population parameter.

• Instead, we might be mostly interested in checking if the parameter is above/below/different of a specific value/threshold.

• Or, to compare the parameters of two different populations. Let us see a few examples.

 Suppose Apple claims that the new Macbook Pro can work for more than 20 hours without a recharge. We could test multiple Macbooks and check how long they hold up without a recharge. Is Apple lying to its consumers?



Source: apple.com

• Some people receive a medical treatment and die. Other receive a medical treatment and live. Does the treatment increase the chance of survival?



Source: fraserinstitute.org

# The hypotheses

#### <u>Hypotheses</u>

- A hypothesis is a statement about the population.
- In general, we have two hypothesis  $H_0$ , called the <u>null hypothesis</u>, and  $H_1$  (or  $H_A$ ), the alternative hypothesis.

In the Macbook example, we want to test

$$H_0$$
:  $\mu = 20 hours$ 

**VS** 

$$H_1$$
:  $\mu > 20$  hours

where  $\mu$  is the true mean of the battery life of the new Macbook Pro.

In the medical treatment example, we might want to test

$$H_0: p_1 = p_2$$
 $VS$ 
 $H_1: p_1 > p_2$ 

where  $p_1$  and  $p_2$  are the proportions of patients that survive with and without the treatment, respectively.

#### Null Hypotheses

• The null hypothesis is the status quo, what you should conclude if there's no evidence to say otherwise.

#### • For example:

- unless we see "strong" evidence that a new, untested drug works, we are going to assume that it does not.
- unless there is evidence showing otherwise, we are going to assume that men and women have the same average speed.
- The Macbook example is more interesting. If you trust Apple, you could say that unless you see evidence showing that Apple is wrong, you assume that the Macbook's battery life is 20 hours or more. Or, alternatively, you could say that unless there is evidence showing that the battery life is 20 hours or more, you assume Apple is wrong.

### Alternative Hypotheses

• The alternative hypothesis is the complement of the Null Hypothesis. The conclusion we want to make only if there's evidence supporting it.

• For example:

• In the Macbook example, you could use  $H_1$ :  $\mu > 20$ , in which case you are looking for evidence that Apple is **not** wrong (you don't trust Apple). Or you could set  $H_1$ :  $\mu < 20$ , you will only conclude Apple is wrong if there is evidence supporting that.

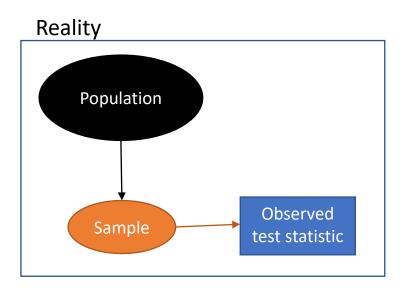
## What to do?

- Our test will be based on a sample. So we start by collecting a sample.
- Calculate the statistic that we are going to use for the test.
  - This statistic is called <u>test statistic</u>;
- As usual, everything revolves around the distribution of our statistic (remember the sampling distribution?).
  - But this time, there is a tweak!

## The null model

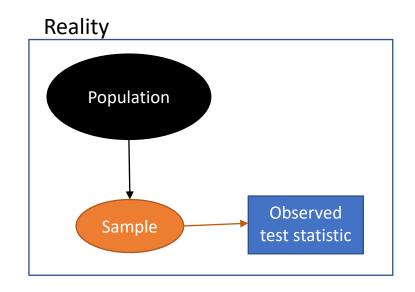
### Null model

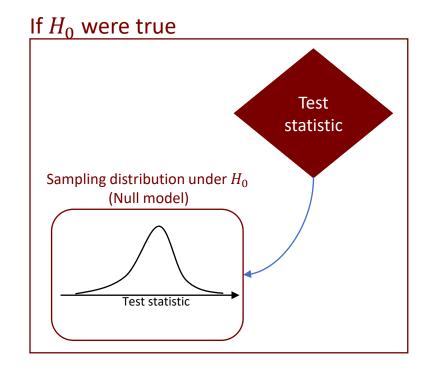
• Hypothesis test is like an argument by *contradiction*.



#### Null model

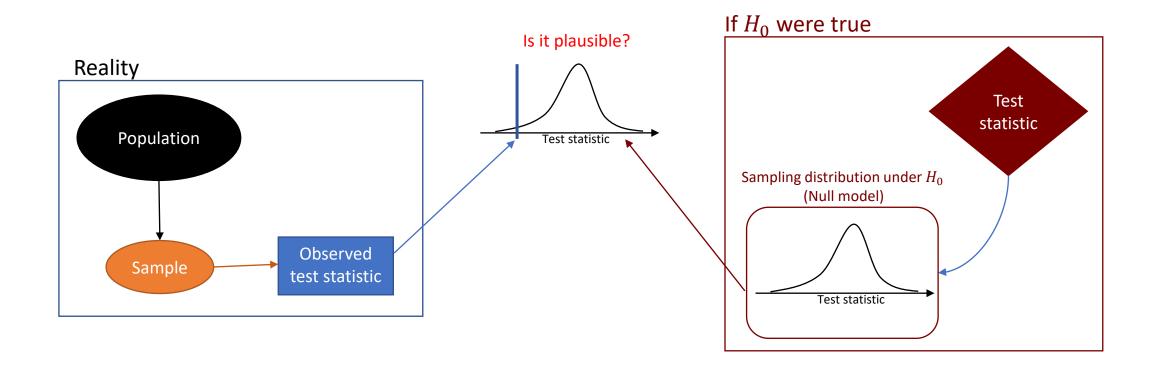
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#### Null model

• Hypothesis test is like an argument by *contradiction*.

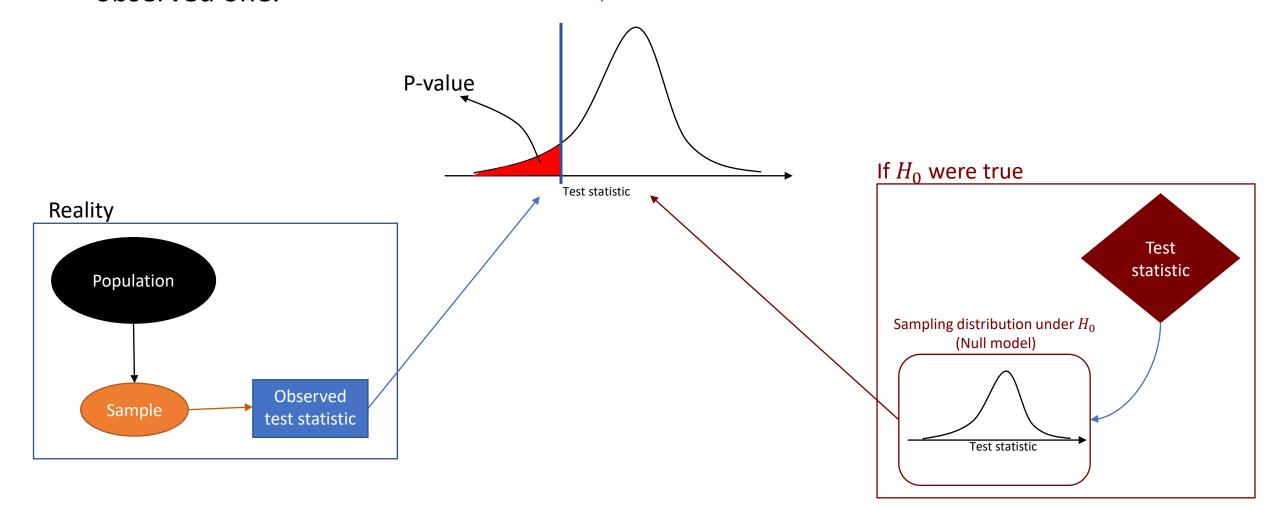


## P-Value

#### P-value

• The probability of getting a value at least as "extreme" as the observed one.

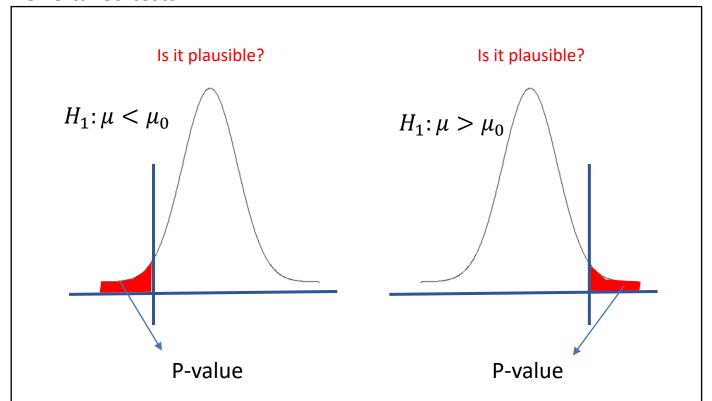
Is it plausible?



#### P-value

• But what is "extreme"? That depends on the alternative hypothesis.

#### One-tailed tests



#### Two-tailed test

