

# Compiler Optimizations for Machine Learning Workloads

Bojian Zheng

CSCD70 Compiler Optimization

2023/3/20

# Announcements

- The lecture & tutorial next week (i.e., 2023/03/27) will be **cancelled**.
- Assignment 3 will be released this Friday (i.e., 2023/03/24).
  - 2 weeks will be given.
  - Covers loop invariant code motion and register allocation.

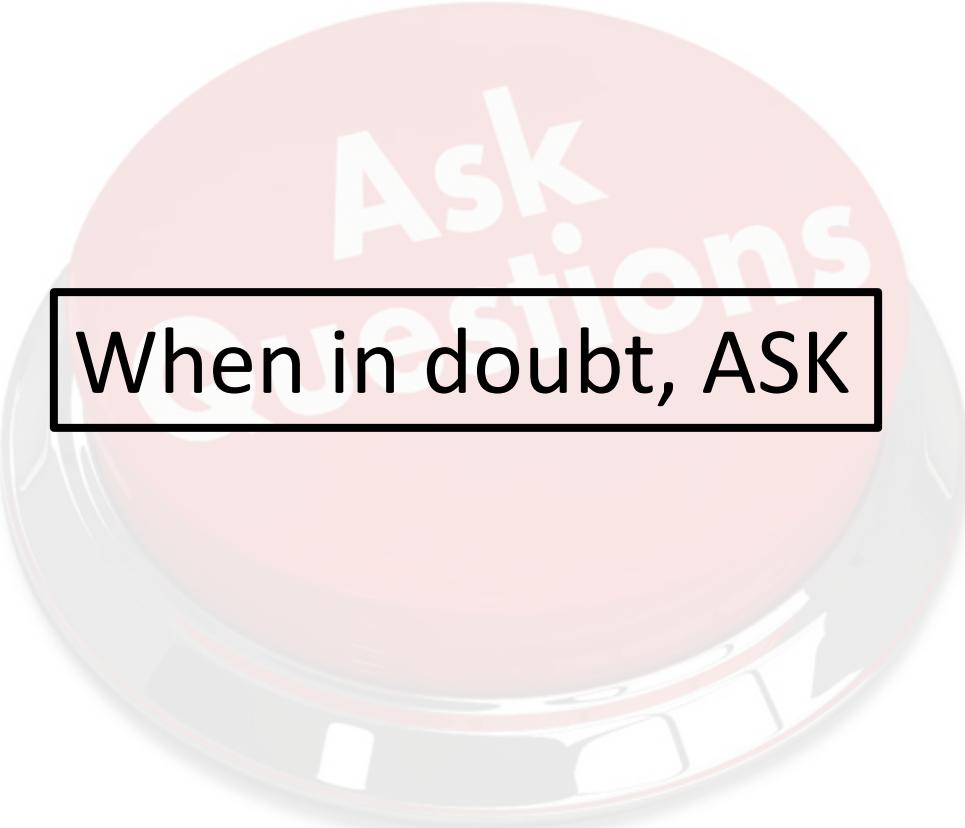


# Agenda

0. Background: Deep Neural Networks

1. Machine Learning Systems

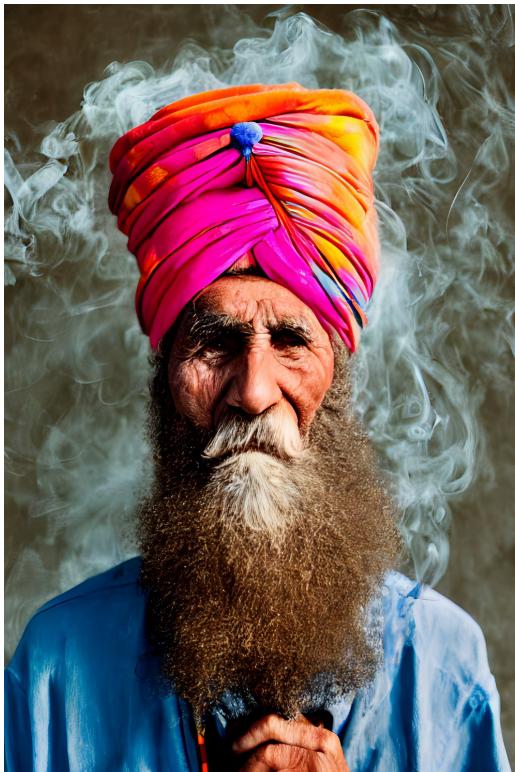
2. Memory Optimizations



**When in doubt, ASK**

# Hypes in Machine Learning

**Image Synthesis**



<https://stablediffusionweb.com/>



**Chat Bot**



<https://openai.com/blog/chatgpt>

# Deep Neural Networks

- An important class of machine learning algorithms, usually interpreted as **graphs**.

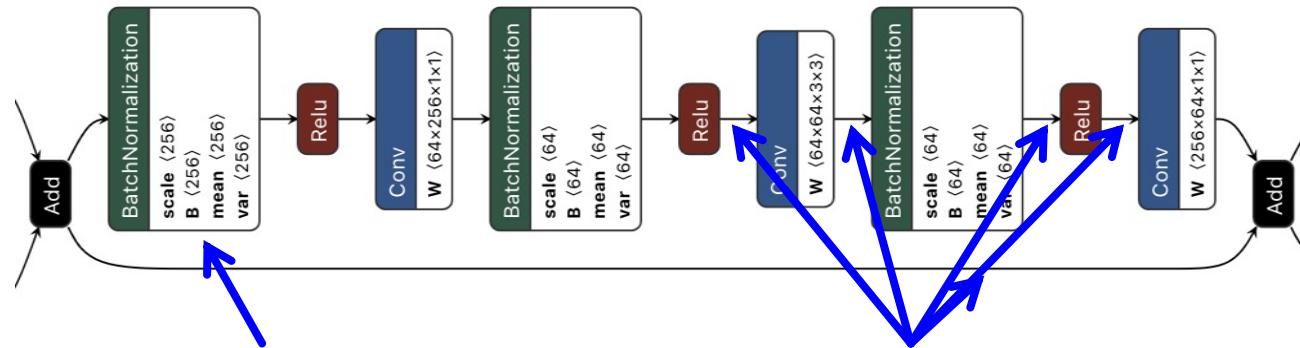
Graph visualization of ResNet-50, an image classification model



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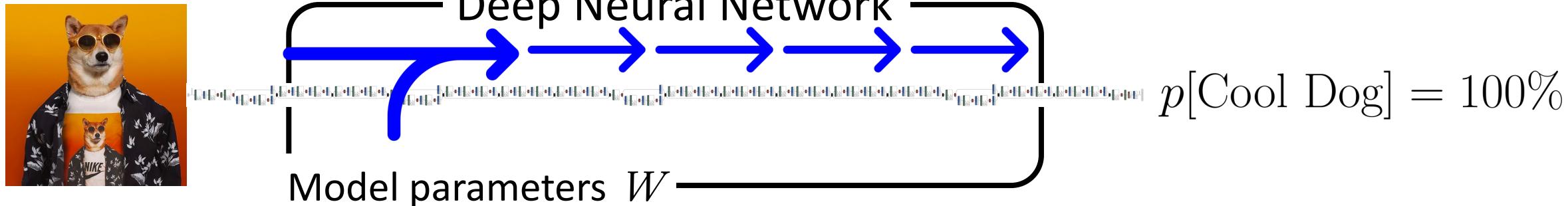
Graph visualization of ResNet-50, an image classification model



Graph = Nodes (i.e., **Operators**) + Edges (i.e., **Tensors**)  
Tensor = NDArray = Multi-dimensional array

# Deep Neural Networks

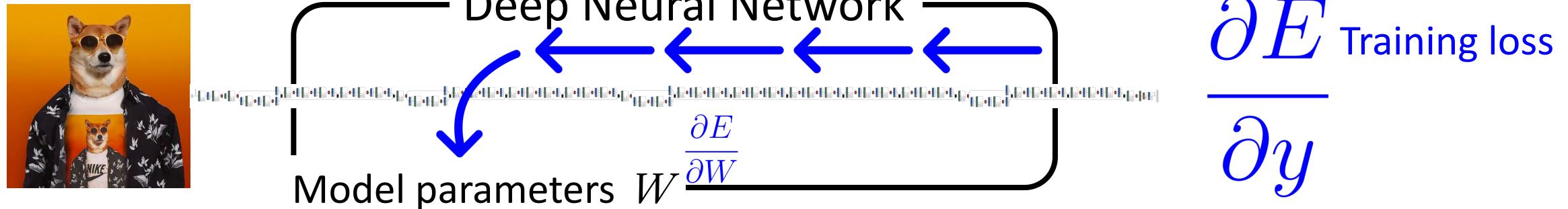
- 3 phases:



① Forward Pass

# Deep Neural Networks

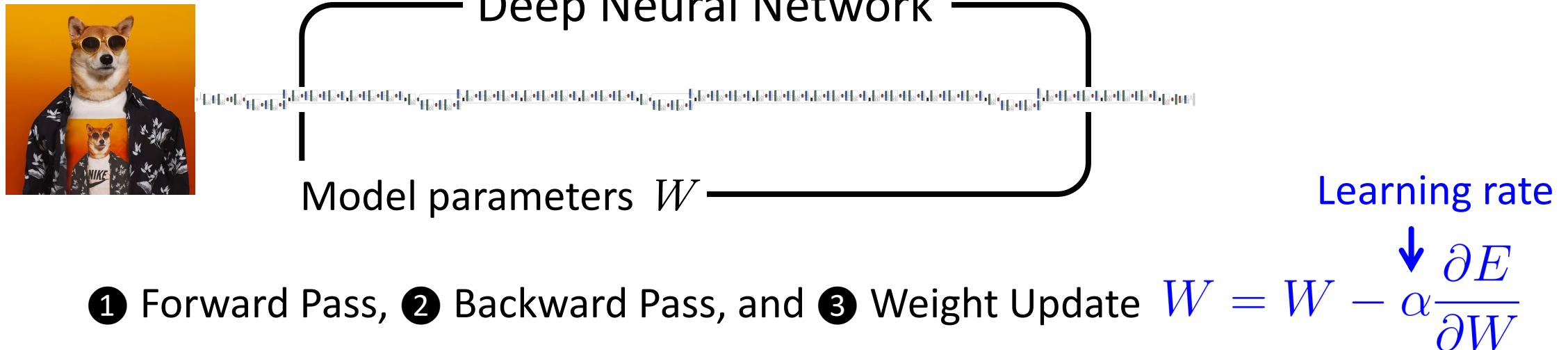
- 3 phases:



- ① Forward Pass, ② Backward Pass

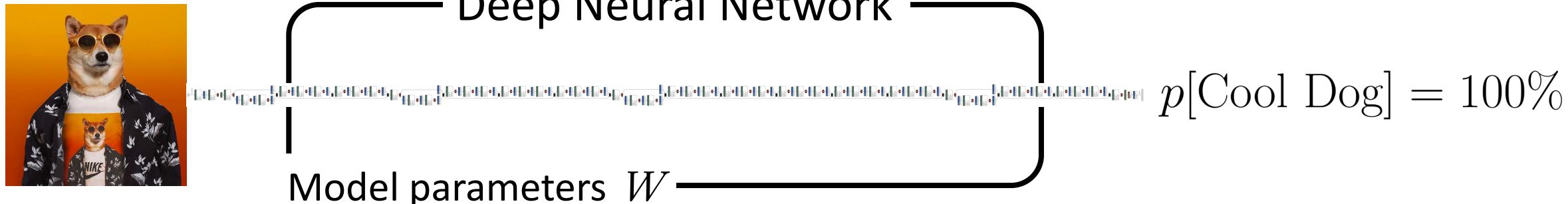
# Deep Neural Networks

- 3 phases:



# Deep Neural Networks

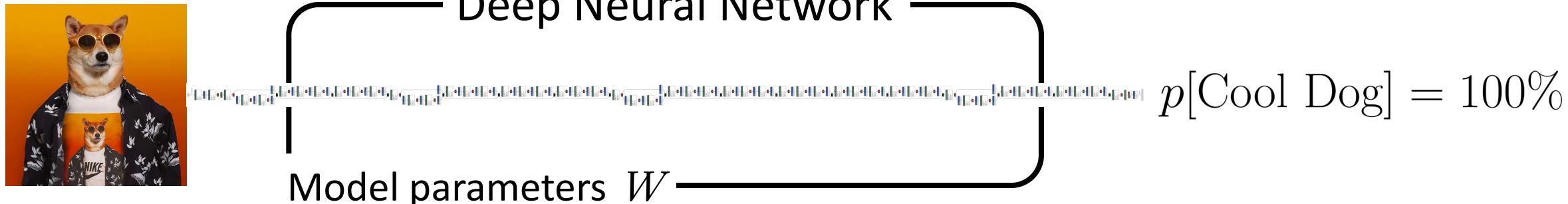
- 3 phases:



- ① Forward Pass, ② Backward Pass, and ③ Weight Update
- **Training:** Learn the model parameters.

# Deep Neural Networks

- 3 phases:



- ① Forward Pass, ② Backward Pass, and ③ Weight Update
- **Inference:** Forward only to obtain the output labels.

# Section Summary

- Deep neural networks: graphs of operators and tensors.
- 3 phases & 2 modes of operation:
  - Training: Forward, Backward, and Weight Update
  - Inference: Forward only
- These special properties call for domain-specific system design.

# Machine Learning Systems

- Machine Learning Systems Overview
- TensorFlow & PyTorch: Declarative vs. Imperative
- Evolution of PyTorch Compiler Design

# Machine Learning Systems Overview

## Application



Image Classification



Machine Translation



Speech Recognition

# Machine Learning Systems Overview

## Application

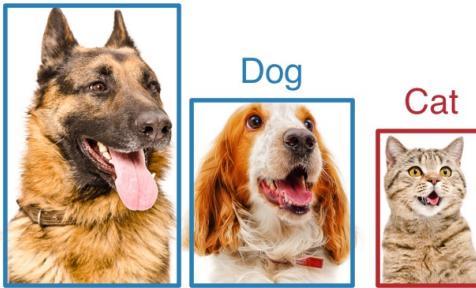
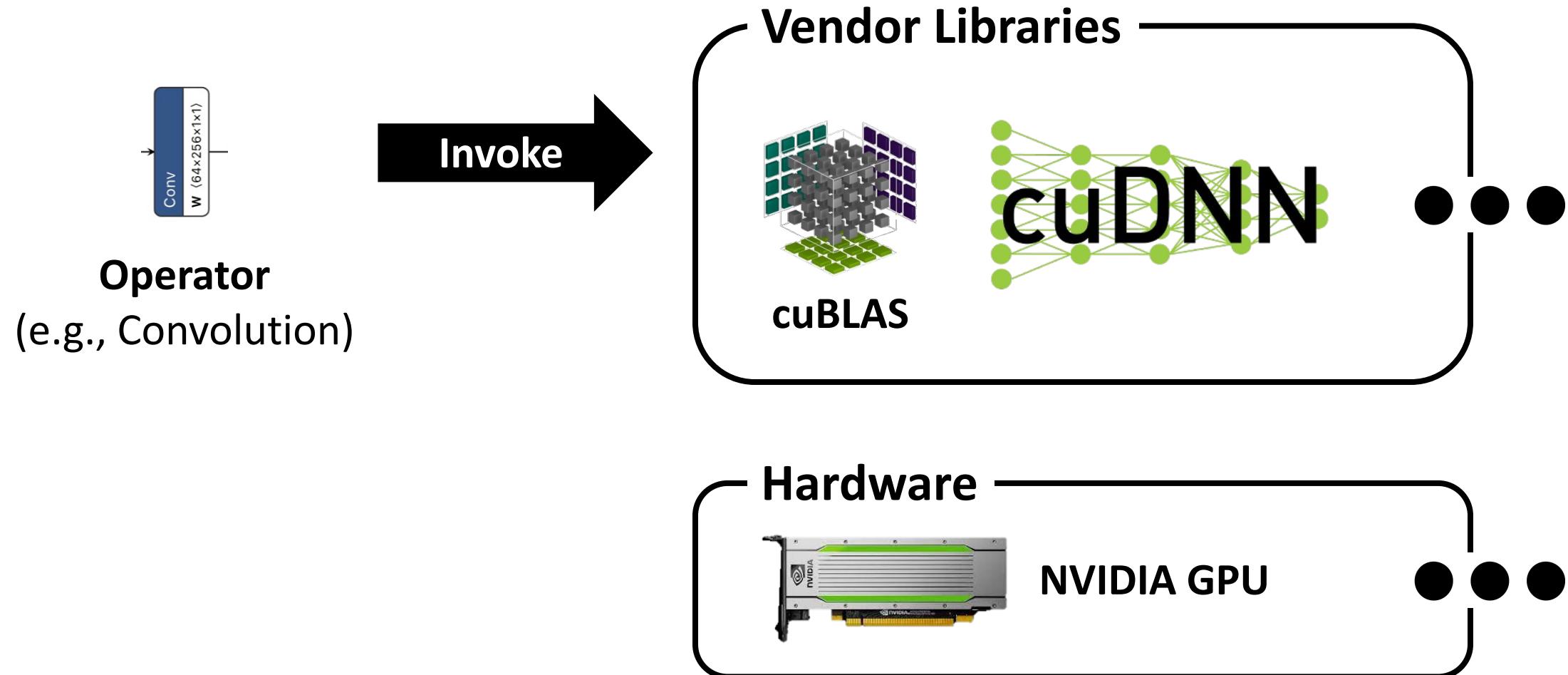


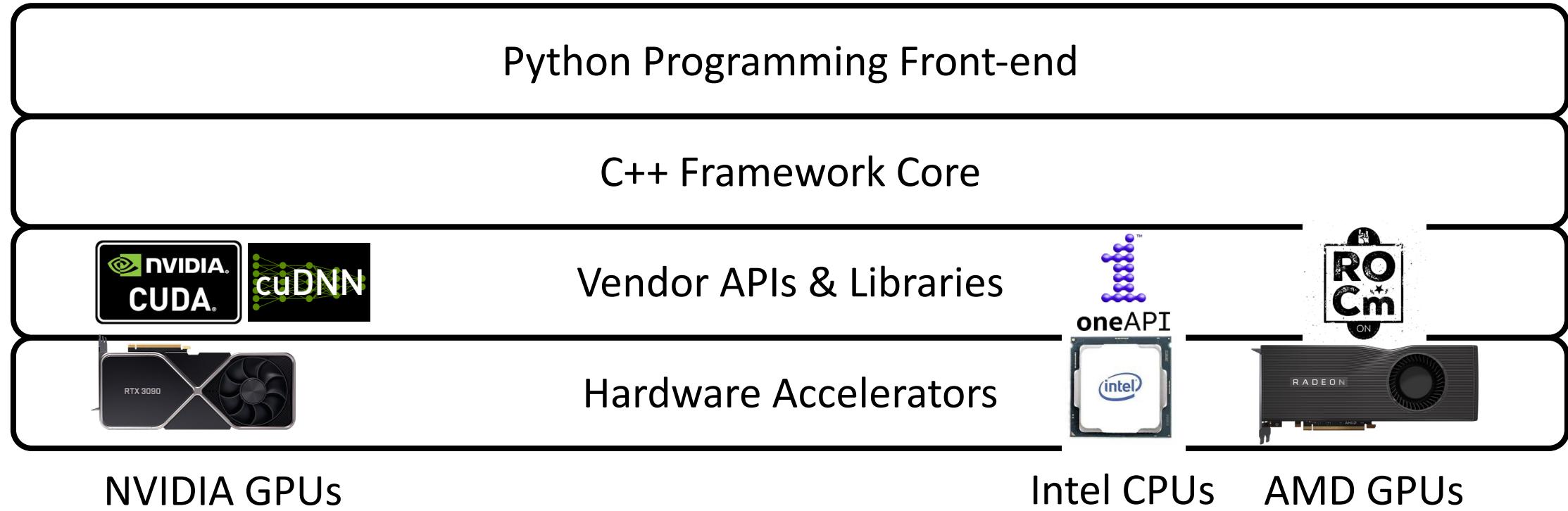
Image Classification



# Machine Learning Systems Overview

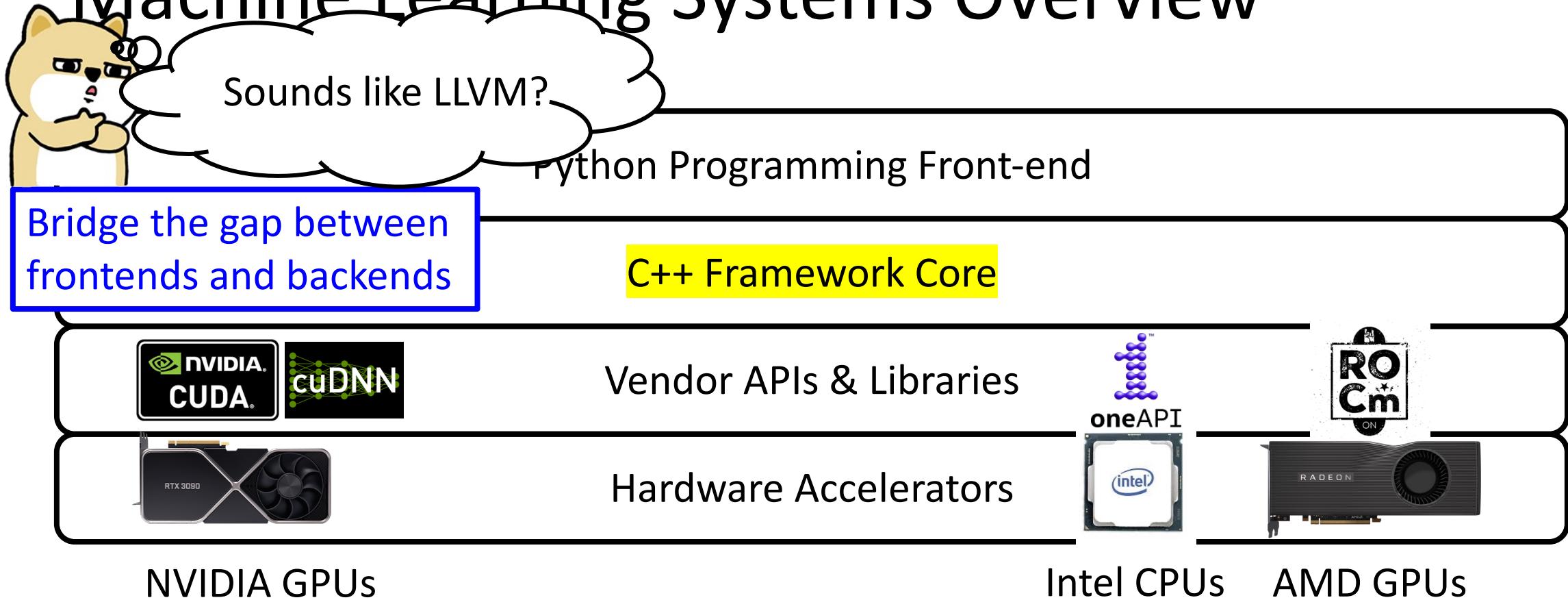


# Machine Learning Systems Overview



- Apply generically to many state-of-the-art systems.

# Machine Learning Systems Overview



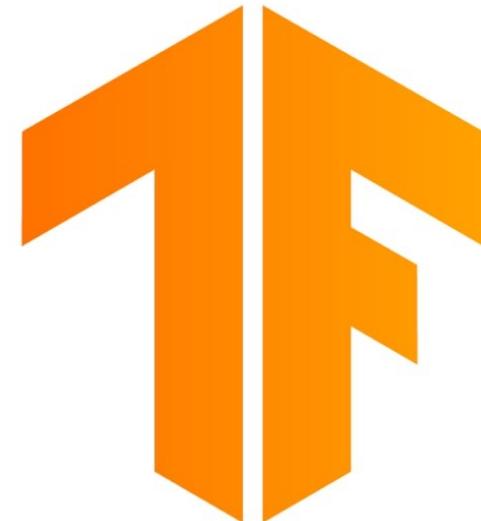
- Apply generically to many state-of-the-art systems.

# TensorFlow (V1)

- One of the first mature machine learning frameworks that support GPUs.
- Declarative programming paradigm:

```
import tensorflow as tf

a = tf.placeholder()
b = tf.placeholder()
c = a + b
with tf.Session() as sess:
    sess.run(
        c, feed_dict={a: 10, b: 32})
)
```

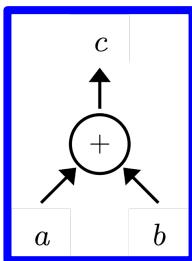


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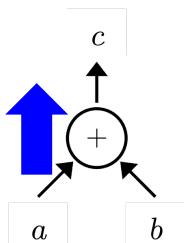


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  - **Declarative** programming paradigm
    - Key Idea: Create a **compilable** graph object in Python, an interpreter environment.
- (+) **Holistic view** of the model makes many optimizations easy to implement.
- TensorFlow **Grappler Optimizer**, responsible for
    - Arithmetic optimizations, e.g., constant folding, common subexpression elimination, dead *node* elimination, ...
    - Memory allocations
    - ...

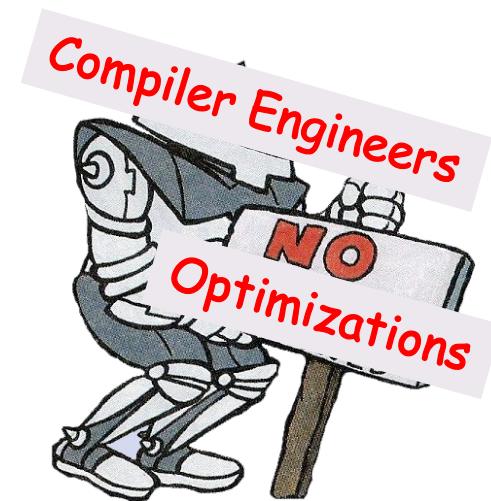
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  - **Declarative** programming paradigm
    - Key Idea: Create a **compilable** graph object in Python, an interpreter environment.
- (+) **Holistic view** of the model makes many optimizations easy to implement.
- (-) **Hard to program** models with dynamic control flows.
- (-) **Hard to debug** intermediate tensor values.

# PyTorch

- One of the prevalent machine learning frameworks that adopts **imperative** programming.

- (+) Easy to program and debug.
- (-) No graphs, ...

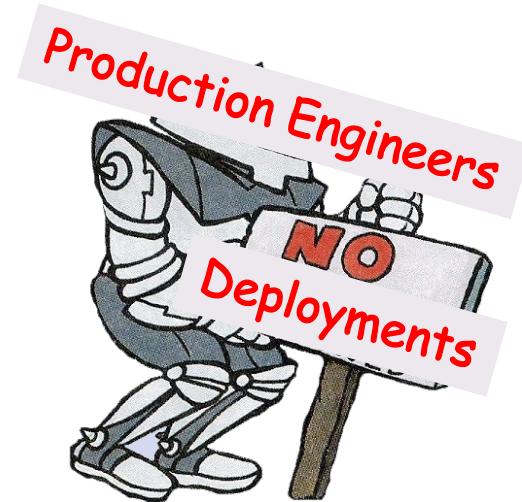


[https://chips-compilers-mlsys-22.github.io/assets/slides/PyTorch%20Compilers%20\(Compiler%20&%20Chips%20Symposium%202022\).pdf](https://chips-compilers-mlsys-22.github.io/assets/slides/PyTorch%20Compilers%20(Compiler%20&%20Chips%20Symposium%202022).pdf)

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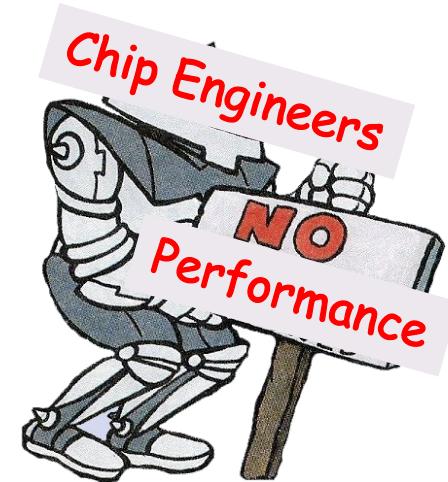


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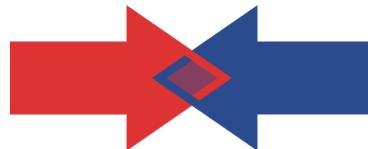
# TensorFlow & PyTorch

## TensorFlow

- TensorFlow.**Eager** switched to imperative execution in 2018.

## PyTorch

- Gen1: torch.jit.script/trace
- Gen2: torch.fx
- Gen3: torch.Dynamo



# PyTorch Gen1 Compiler

## `torch.jit.script`

- An embedded language that moves outside of Python.

```
import torch
from torch.nn import Module

class MyModel(Module):
    ...

model = MyModel()

scripted_model = \
    torch.jit.script(model)
```

## `torch.jit.trace`

- A tracer that records all the evaluated operators.

```
traced_model = torch.jit.trace(
    model, (sample_input,))
```

# PyTorch Gen1 Compiler

## `torch.jit.script`

- An embedded language that moves outside of Python.
- (+) Easy to deploy and convert to other formats.
- (-) Limited operator coverage.

```
scripted_model = \  
    torch.jit.script(model)
```

## `torch.jit.trace`

- A tracer that records all the evaluated operators
- (-) Specialized to the provided sample input.

```
traced_model = torch.jit.trace( \  
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```

# PyTorch Gen2 Compiler torch.fx

- Key Idea: Python-to-Python transformation.
- 3 main components:
  - Symbolic tracing

```
import torch
from torch.nn import Module

class MyModel(Module):
    def forward(self, x, y):
        return x + y

model = MyModel()
traced_model = \
    torch.fx.symbolic_trace(module)
```

Feed in proxy inputs and record operations on them

# PyTorch Gen2 Compiler torch.fx

- Key Idea: Python-to-Python transformation.
- 3 main components:
  - Symbolic tracing
  - Duck -typed Python IR

Operate on this representation



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import torch
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fx_model = torch.fx.symbolic_trace(model)
print(fx_model.graph)
"""

graph():
    %x : = placeholder[target=x]
    %y : = placeholder[target=y]
    %ret : = call_function[target=op.add](
        args=(%x, %y), kwargs={}
    )
"""

```

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fx_model.recompile()
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```

# PyTorch Gen2 Compiler torch.fx

- Key Idea: Python-to-Python transformation.

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(+) The Python-like IR is easy to understand and manipulate.

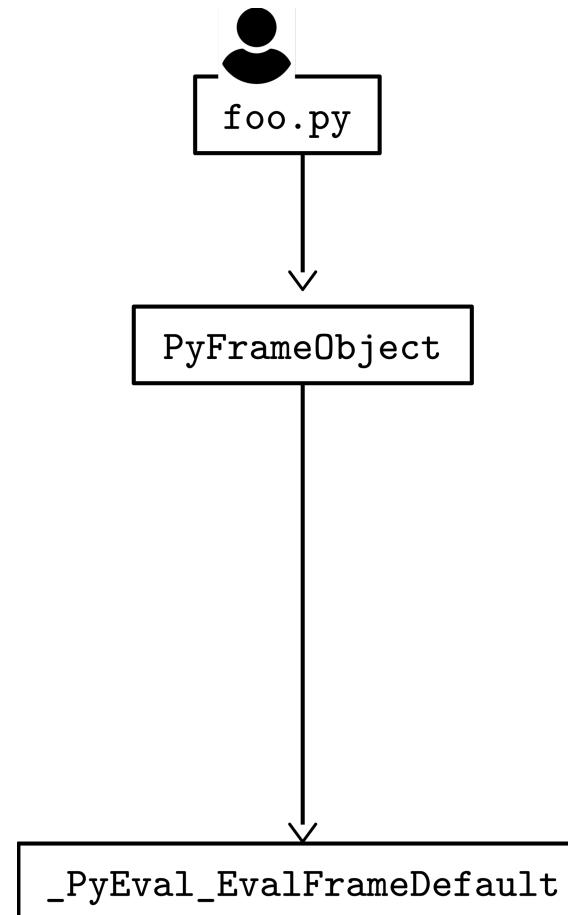
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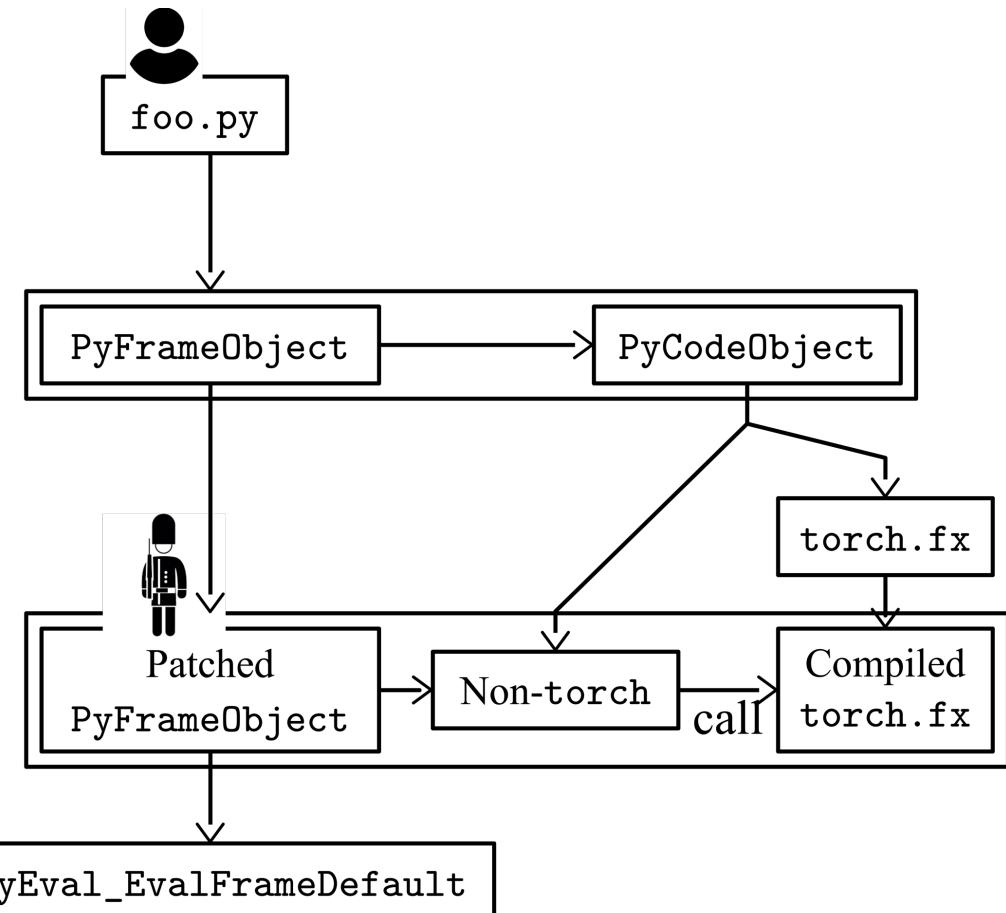
- Key Idea: torch.fx but supports partial capture.

```
import torch

def toy_example(a, b):
    x = a / (torch.abs(a) + 1)
    if b.sum() > 0:
        b = b * -1
    return x * b

def my_pass(fx_module, sample_inputs):
    pass

with torch.dynamo.optimize(toy_example,
                           sample_inputs=sample_inputs):
    toy_example(
        torch.randn(10), torch.randn(10)
    )
```



# PyTorch Gen3 Compiler torch.Dynamo

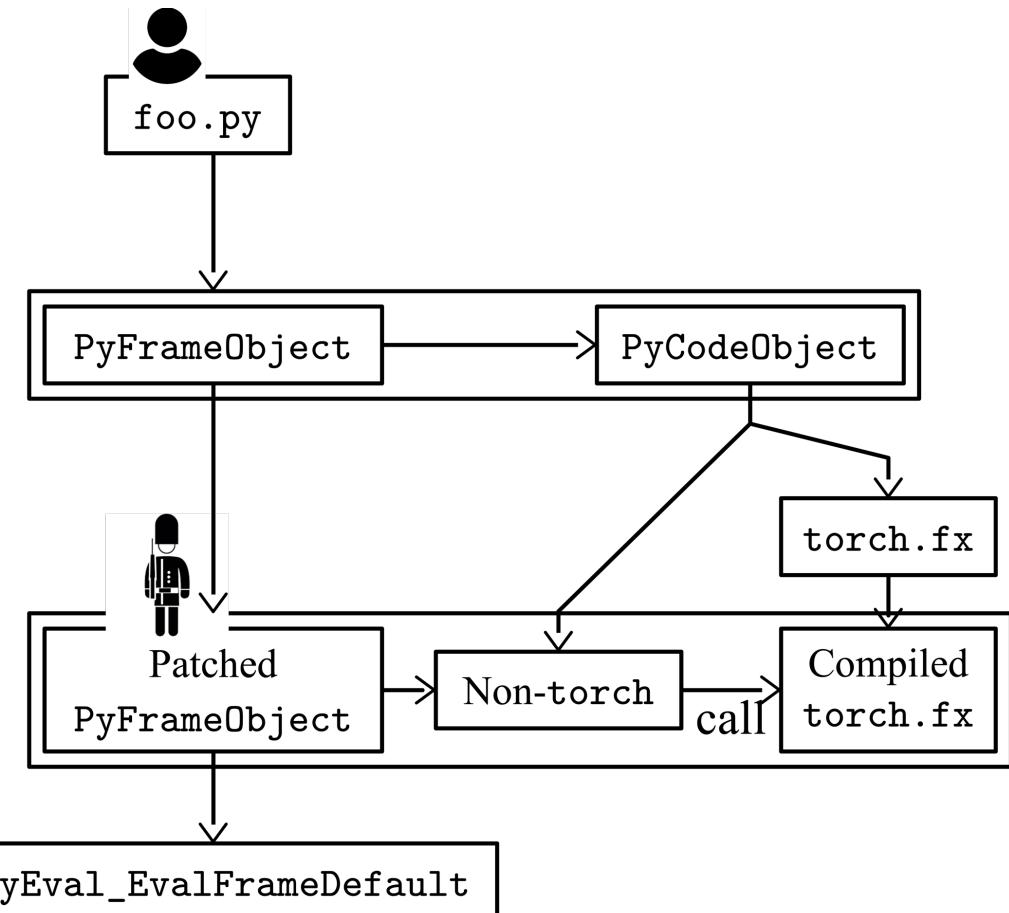
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# PyTorch Gen3 Compiler torch.Dynamo

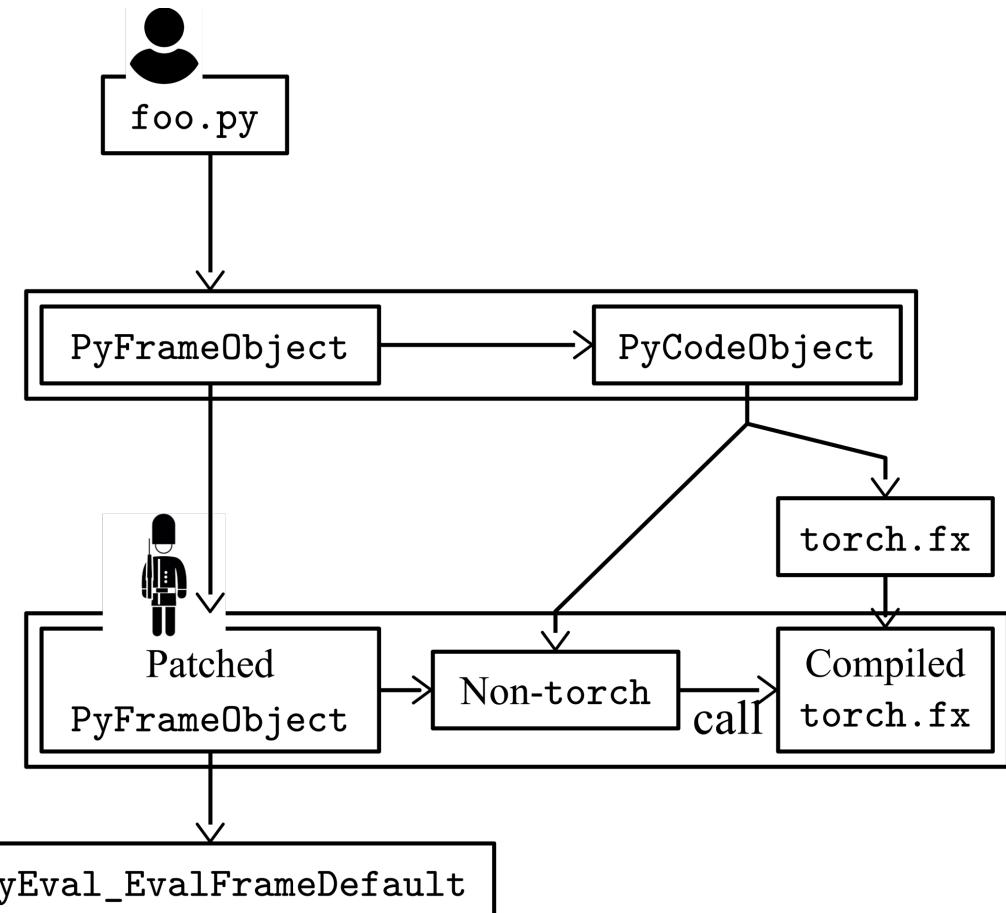
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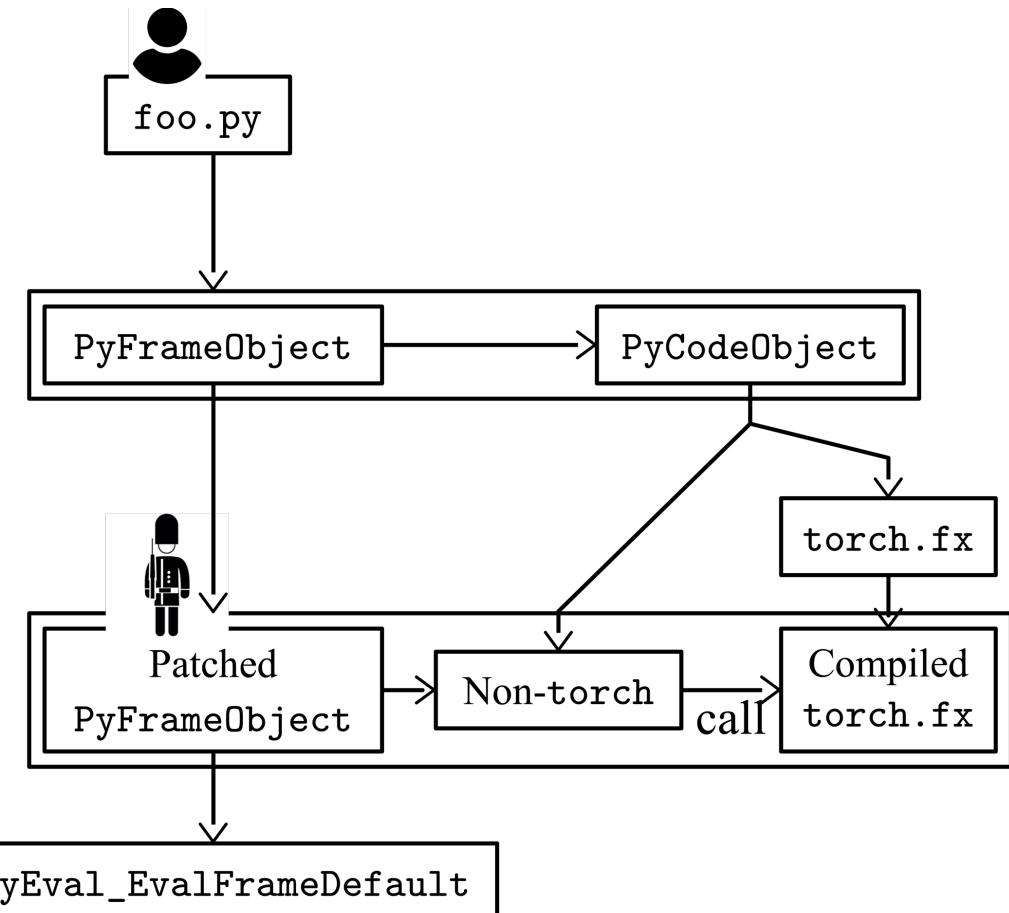
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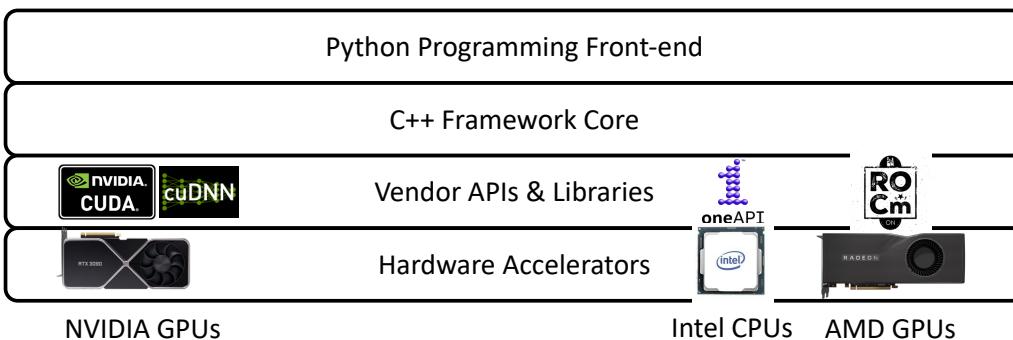
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# Section Summary

- MLSys Overview



- TensorFlow and PyTorch
  - Declarative vs. Imperative
- Please support the research work **Hidet** from my colleague Yaoyao: [www.github.com/hidet-org/hidet](https://www.github.com/hidet-org/hidet) by starring the repository.

- Evolution of PyTorch Compilers

- Gen1: Scripting and tracing
- Gen2: Ducked-type Python IR
- Gen3: Partial capture

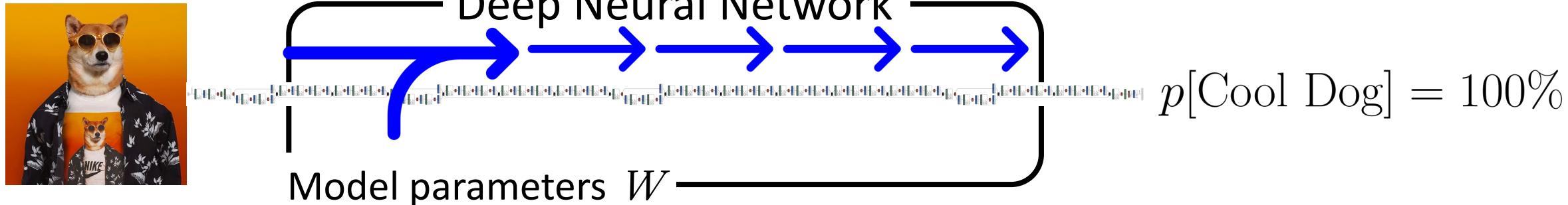
- Can jump out of those existing systems and create much more **powerful** wheels!

# Memory Optimizations

- Background: Feature Maps
- Why memory matters?
- 3 optimization strategies ⇒ Selective Recomputation
- Impact of memory optimizations

# Deep Neural Networks

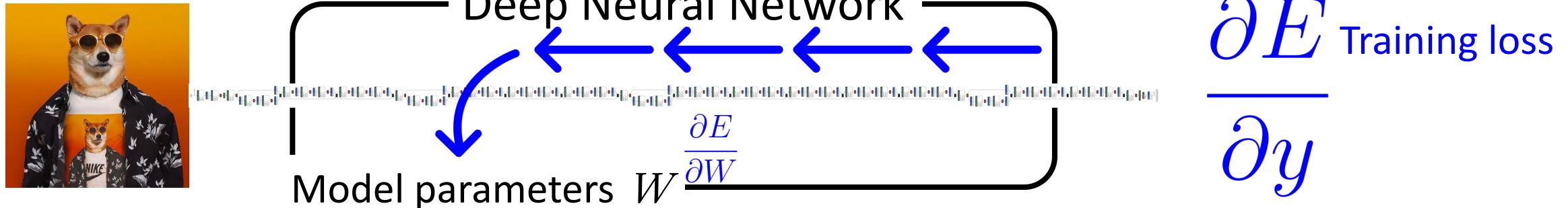
- 3 phases:



① Forward Pass

# Deep Neural Networks

- 3 phases:



① Forward Pass, ② Backward Pass

# Feature Maps

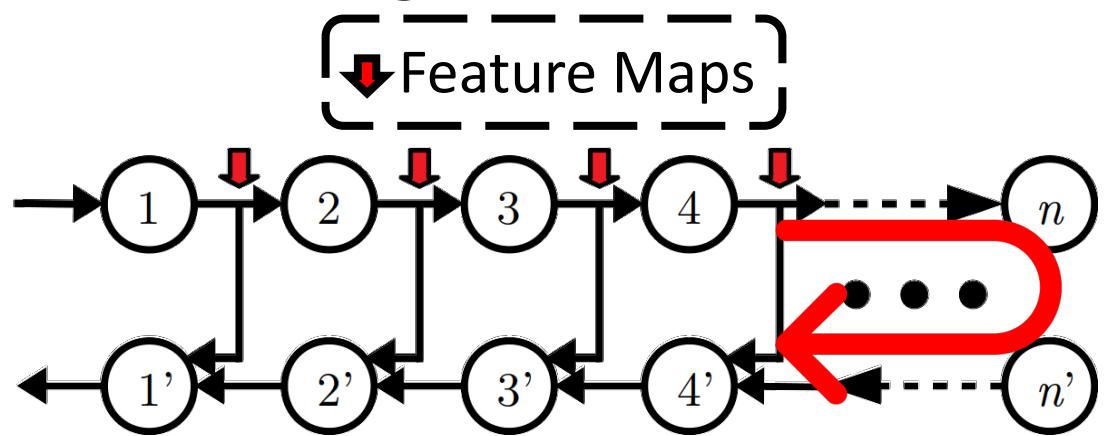
- Data entries that are stashed by the forward pass to compute the backward gradients.

$$\begin{aligned}y = \tanh x &\Rightarrow \frac{\partial E}{\partial x} = \frac{\partial E}{\partial y} \frac{dy}{dx} \\&= \frac{\partial E}{\partial y} (1 - \tanh^2 x) \\&= \frac{\partial E}{\partial y} (1 - \textcolor{blue}{y}^2)\end{aligned}$$

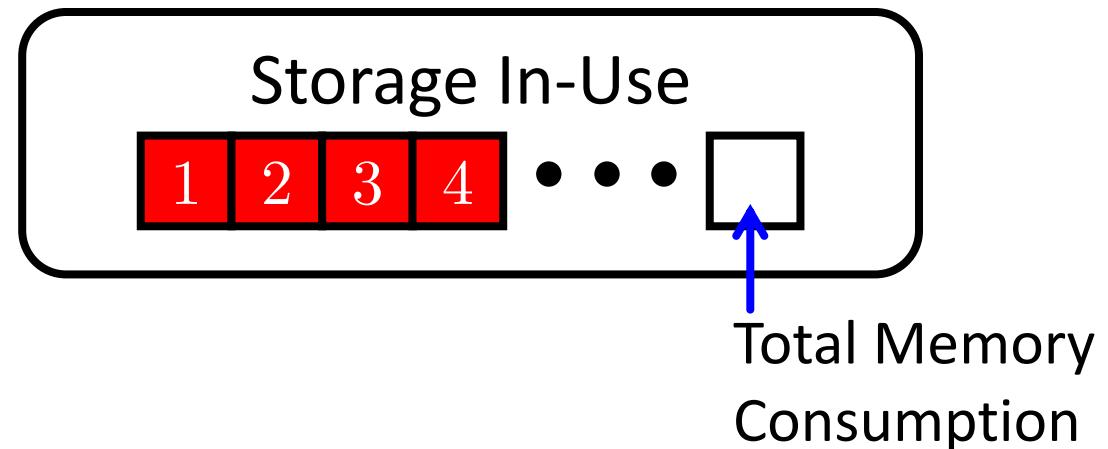


# Feature Maps

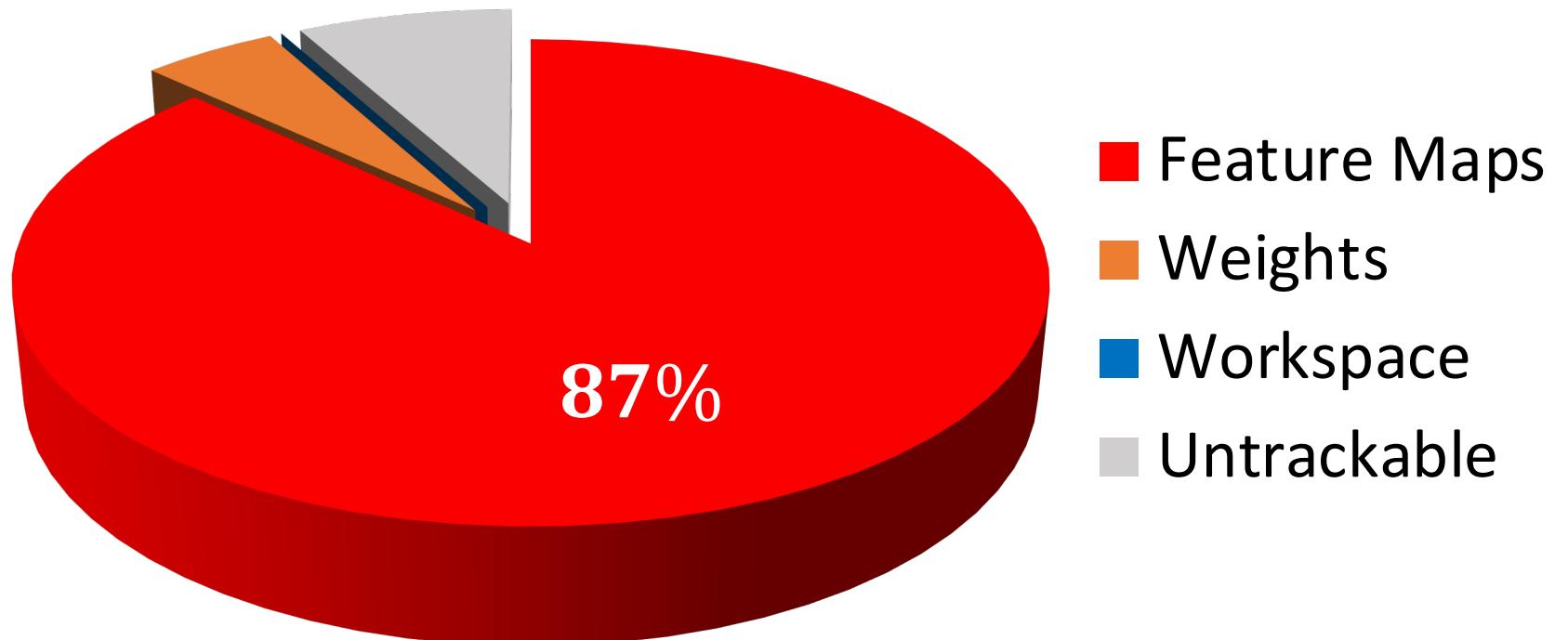
- Data entries that are stashed by the forward pass to compute the backward gradients.



Large **temporal gap** between usage



## GPU Memory Consumption Profile of A Machine Translation Workload



**Feature maps** dominate the GPU memory consumption

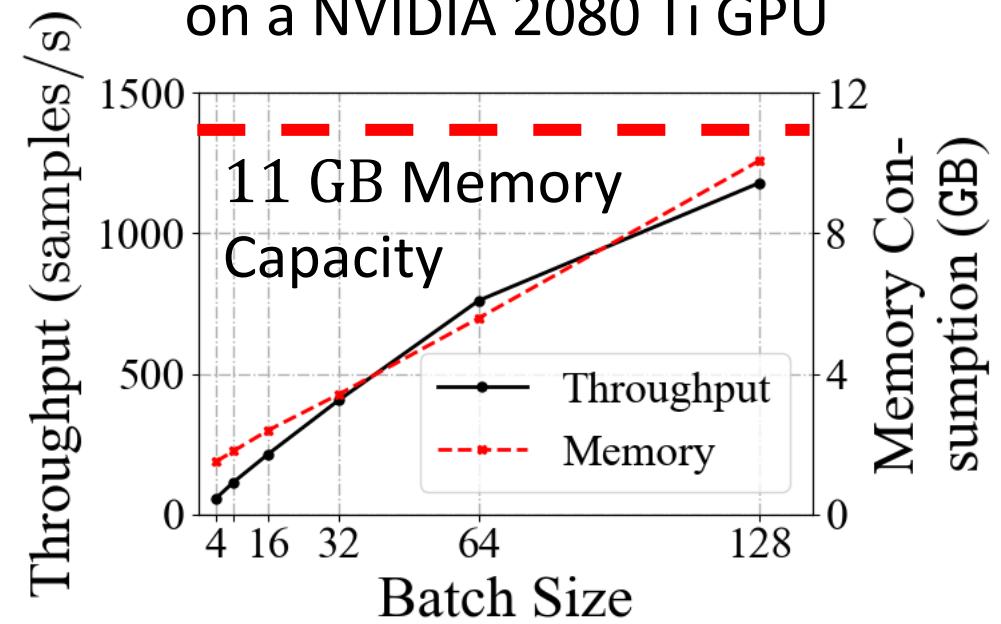
# Why memory matters?

- Hardware accelerators (e.g., NVIDIA GPUs) usually have limited memory capacity (10-40 GB).
- Memory optimizations allow for
  - Training for deeper neural networks ( $\approx$  better training quality).
  - Higher training throughputs.

# Memory → Training Throughputs

- When training, data is usually **batched** for higher throughput and faster convergence.

Throughput and memory consumption of English-Vietnamese translation on a NVIDIA 2080 Ti GPU



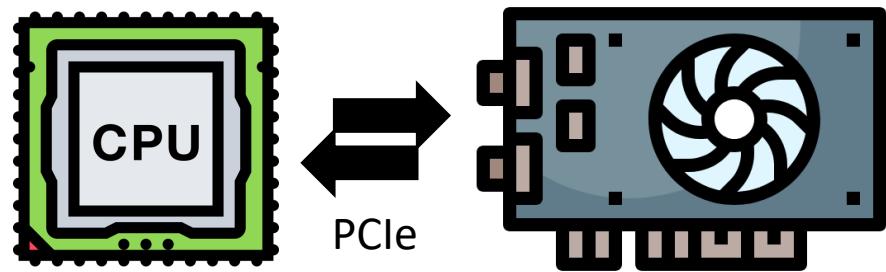
# Strategy #1. Virtualization

- Key Idea: Temporarily offload data entries to the CPU side.

(+) Generic

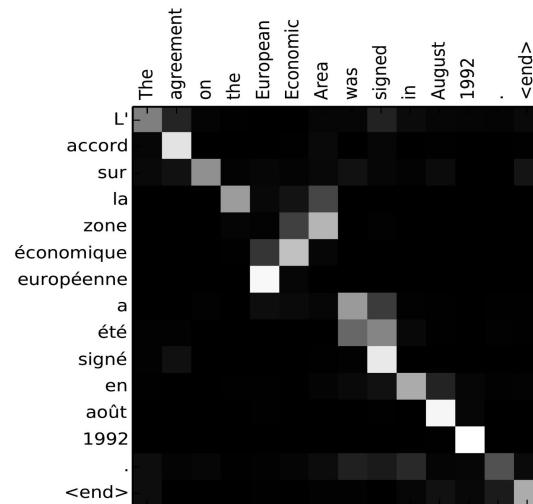
(-) Intensive use of interconnect  
(a valuable resource in distributed systems)

- Hard to control the timing.
  - Significant performance overhead if data is not fetched back on time.
  - Graph + System Information ⇒ What data to offload & When to issue the prefetch.



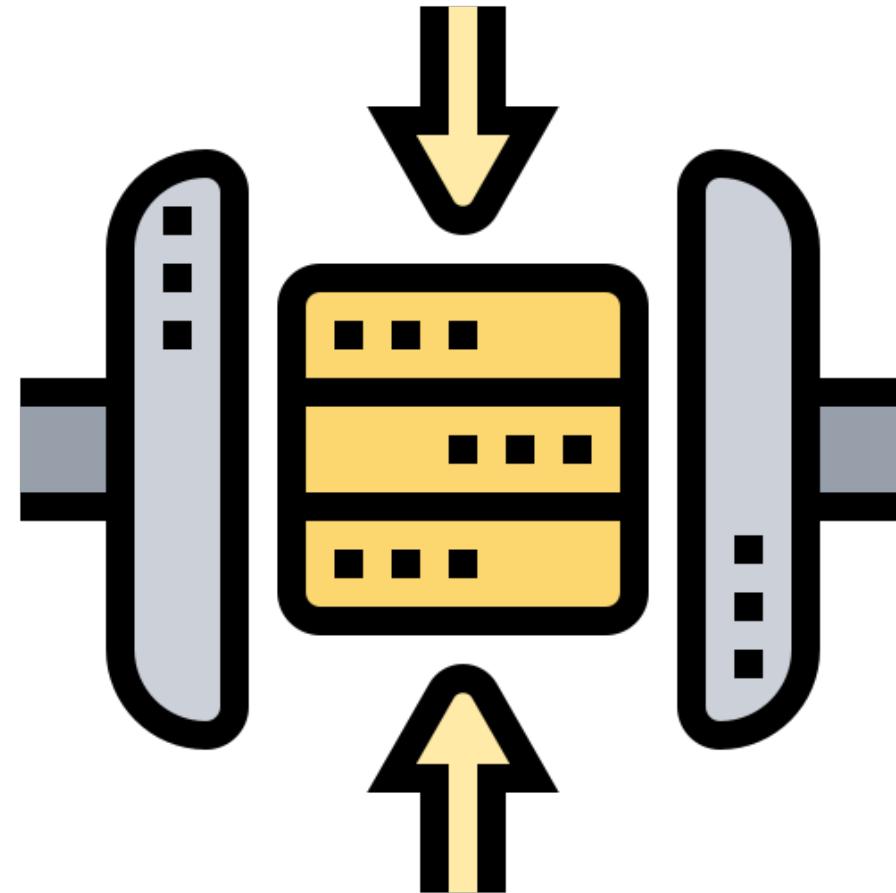
# Strategy #2. Data Encoding

- Key Idea: Compress (usually eliminate zeros).



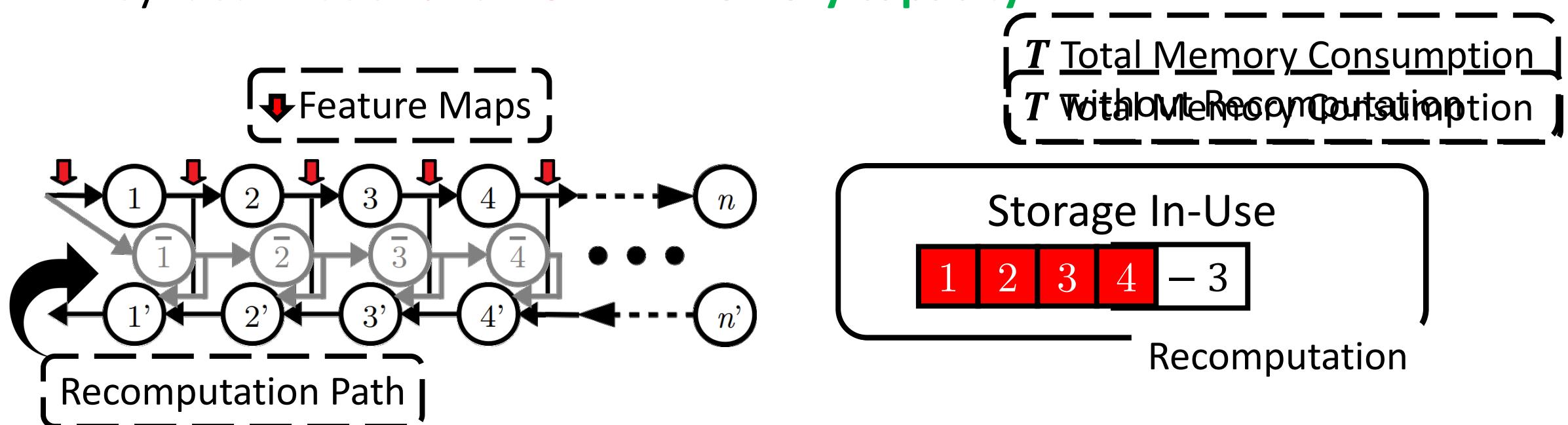
Example feature  
maps (darker  
means  $\rightarrow$  0)

- (+) Low performance overhead
- (-) Model/layer specific



# Strategy #3. Selective Recomputation

- Key Idea: Trade **runtime** with **memory capacity**.



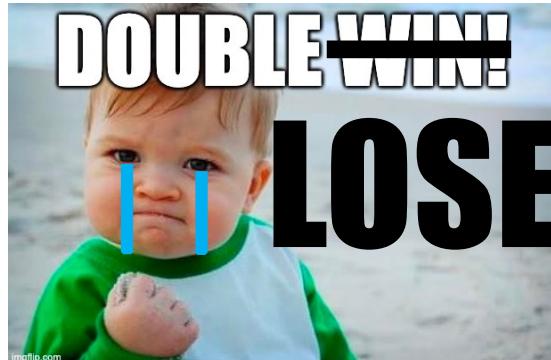
- The recomputation path should only involve **lightweight** operators.

# Strategy #3. Selective Recomputation

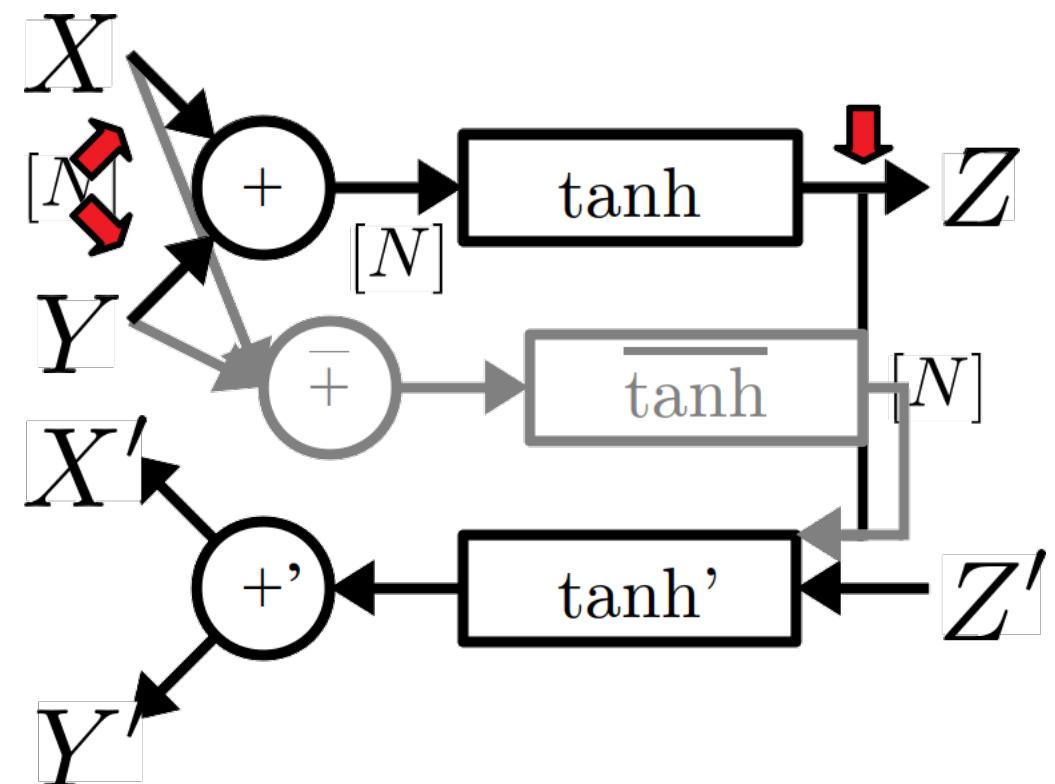
- Recomputing naively can end up with **more** memory.

(-) Feature maps  $\uparrow (N \rightarrow 2N)$

(-) Performance  $\downarrow$



$$Z = \tanh(X + Y)$$



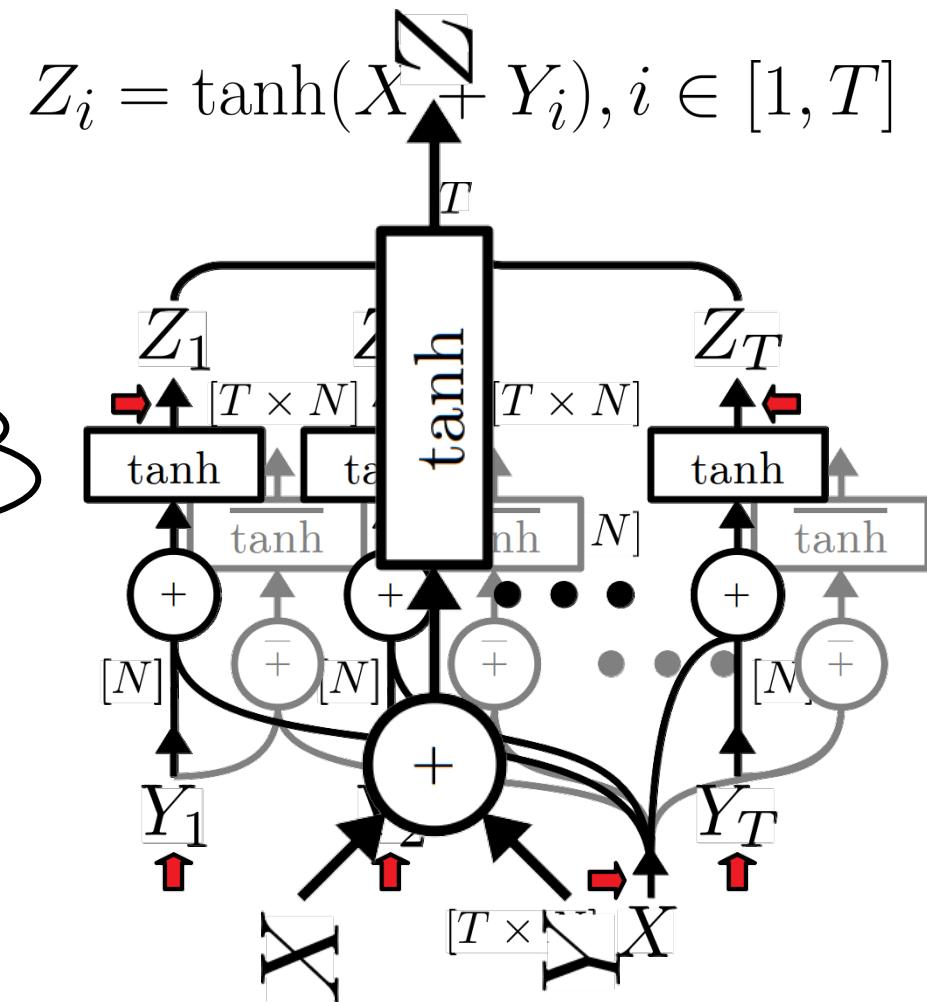
# Strategy #3. Selective Recomputation

- Not considering the **global** graph structure could have us miss key optimization opportunities.
  - E.g.,  $T^2N \rightarrow 2TN$

Want to know the **sweet spot** where doing recomputation is optimal

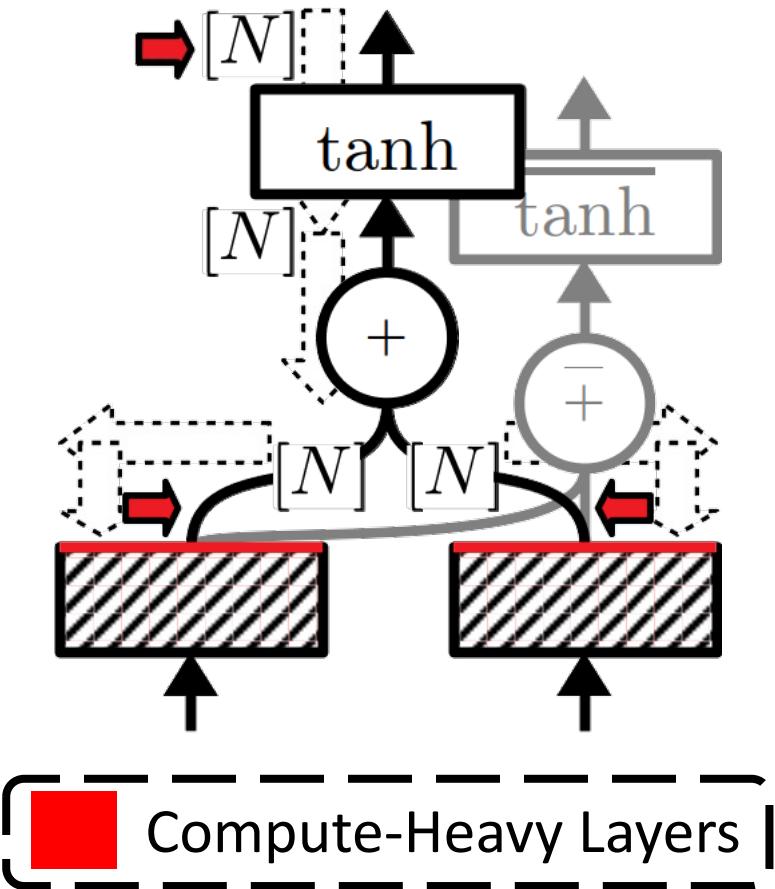


Our approach:  
Bidirectional Analysis



# Bidirectional Analysis

$$Z = \tanh(X + Y)$$

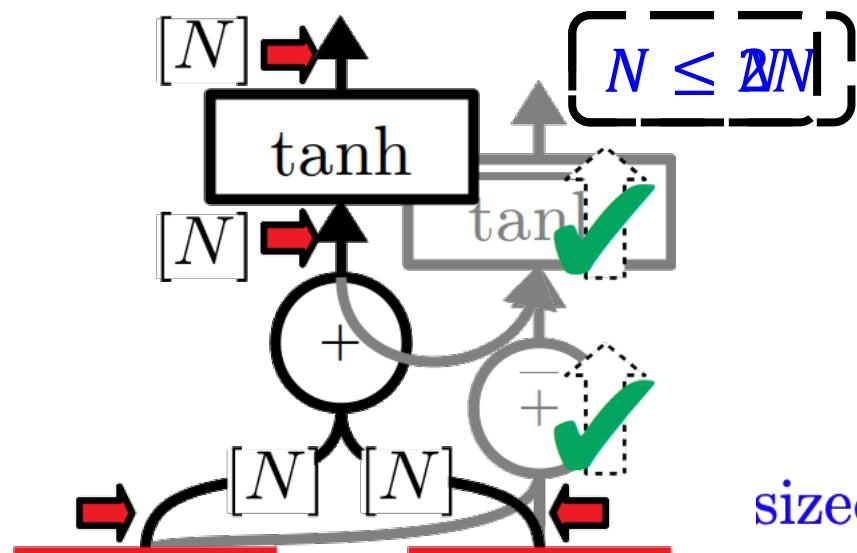


## ▼ Backward Pass

- Breaks at compute-heavy layers to partition the graph
- Constructs a recomputation path that consists of nodes visited

# Bidirectional Analysis

$$Z = \tanh(X + Y)$$



## ▼ Backward Pass

- Breaks at compute-heavy layers to partition the graph.
- Constructs a recomputation path that consists of nodes visited.

## ▲ Forward Pass

- Remove operator nodes from the recomputation path if  $\text{sizeof}(\text{FeatureMaps}_{\text{New}}) \leq \text{sizeof}(\text{FeatureMaps}_{\text{Old}})$

# Bidirectional Analysis

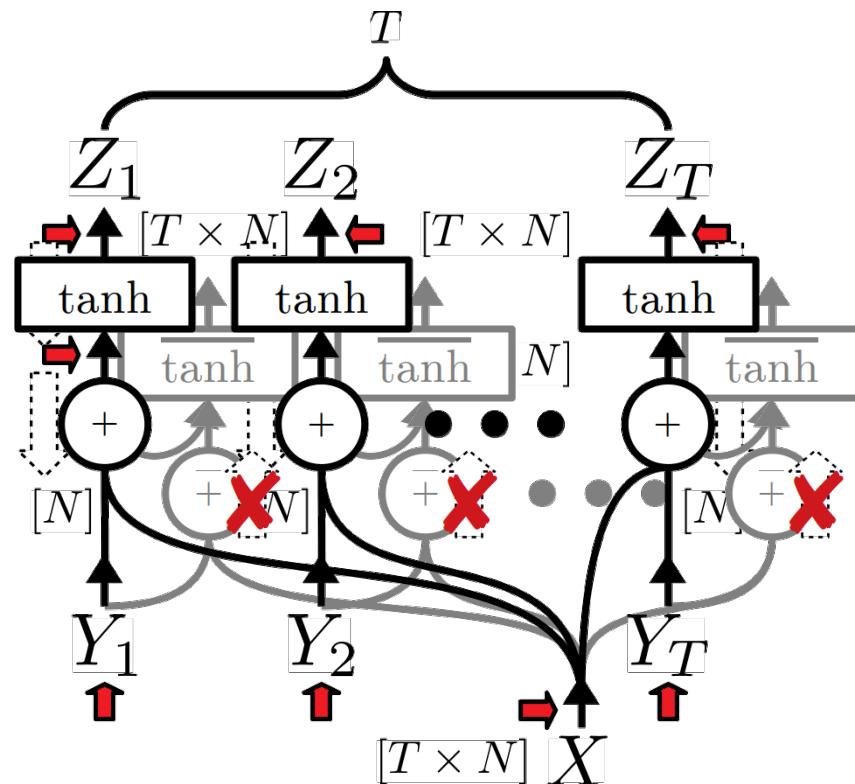
- Tensor sharing causes all the correlated operators to forward propagate simultaneously:

$$\text{sizeof} \left( \sum \text{FeatureMaps}_{\text{New}} \right) \leq$$

$$\text{sizeof} \left( \sum \text{FeatureMaps}_{\text{Old}} \right)$$

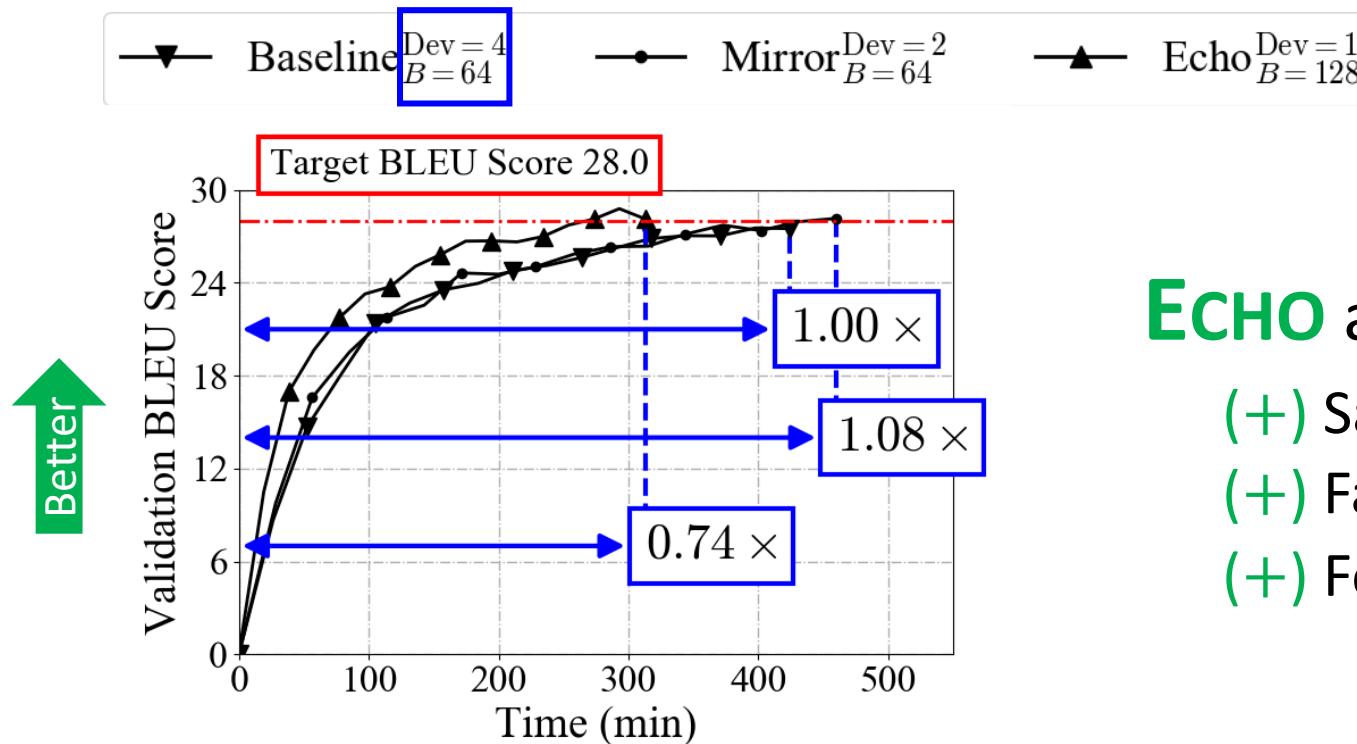
$$T^2N \leq 2TN$$

$$Z_i = \tanh(X + Y_i), i \in [1, T]$$



# Evaluation

English-German translation with the same number of training steps



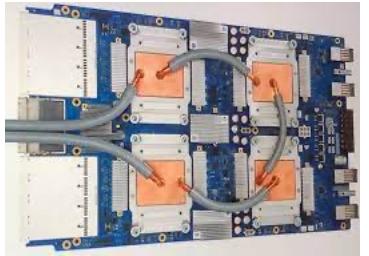
**ECHO achieves:**

- (+) Same training quality
- (+) Faster convergence
- (+) Fewer compute devices

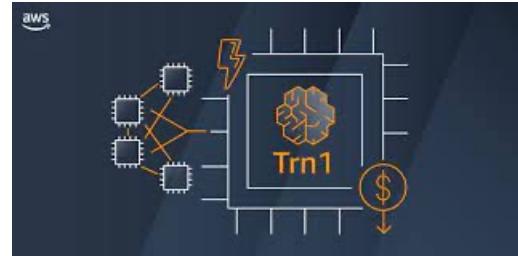
# Section Summary

- Why memory matters?
  - Deeper neural networks
  - Higher training throughputs
- Impact of memory optimizations
  - Same training quality
  - Faster convergence
  - Fewer compute devices
- 3 Optimization Strategies:
  - Virtualization
  - Data Encoding
  - Selective Recomputation  
(formulated as a bidirectional analysis)

# Future Vision



Google TPU



AWS Trainium



Qualcomm  
Cloud AI 100



SAPEON X220



Compute power cannot be exploited  
without a mighty compiler stack.

# Compiler Optimizations for Machine Learning Workloads

Bojian Zheng

CSCD70 Compiler Optimization

2023/3/20