



Design and Analysis
of Algorithms I

QuickSort

Overview

QuickSort

- Definitely a “greatest hit” algorithm
- Prevalent in practice
- Beautiful analysis
- $O(n \log n)$ time “on average”, works in place
 - i.e., minimal extra memory needed
- See course site for optional lecture notes

The Sorting Problem

Input: array of n numbers, unsorted.

3	8	2	5	1	4	7	6
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Output: Same numbers, sorted in increasing order.

1	2	3	4	5	6	7	8
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Assume: all array entries distinct.

Exercise: extend QuickSort to handle duplicate entries.

Partitioning Around a Pivot

Key idea: partition array around a pivot element.

- pick element of array

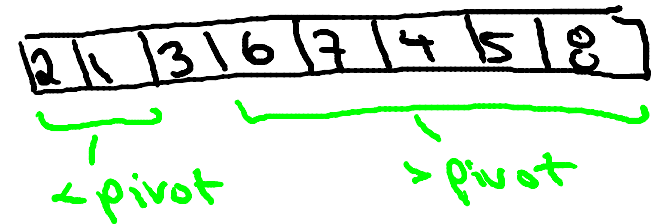
3	8	2	5	1	4	7	6
---	---	---	---	---	---	---	---

pivot

- rearrange array so that:

- left of pivot \Rightarrow less than pivot

- right of pivot \Rightarrow greater than pivot



Note: puts pivot in its "rightful position".

Two Cool Facts About Partition

① linear ($O(n)$) time, no extra memory
[see next video]

② reduces problem size

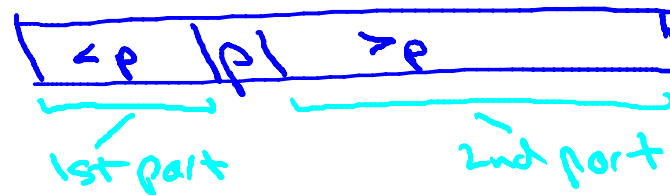
QuickSort: High-Level Description

[Hoare circa 1961]

QuickSort (array A , length n)

- if $n = 1$ return
- $p = \text{ChoosePivot}(A, n)$
- Partition A around p
- recursively sort 1st part
- recursively sort 2nd part

[currently unimplemented]



Outline of QuickSort Videos

- The Partition subroutine
- Correctness proof [optional]
- Choosing a good pivot
- Randomized QuickSort
- Analysis
 - A Decomposition Principle
 - The Key Insight
 - Final Calculations