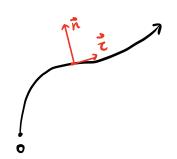
自动驾驶控制算法第三讲

运动学方程 X=νcosφ

$$\dot{\varphi} = \frac{v \tan \delta}{L}$$
 $\dot{\varphi} = \frac{v}{R} \Rightarrow \frac{1}{R} = \frac{\tan \delta}{L}$ $\tan \delta = \frac{L}{R}$

动力学方程:考虑轮胎特性

当选取 Frenet 坐标系时,可以将纵向控制与横向控制解耦



$$\vec{v} = \frac{dS}{dt}$$
 $\vec{a}_{c} = \frac{d^{2}S}{dt^{2}}$ $\vec{a}_{n} = \frac{v^{2} tanS}{L}$

$$\begin{cases}
\dot{X} = v \cos \varphi \\
\dot{Y} = v \sin \varphi \\
\dot{\varphi} = v \frac{\tan \theta}{L}
\end{cases}$$

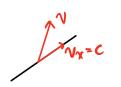
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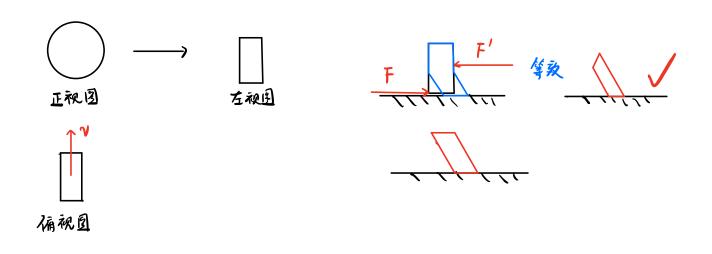
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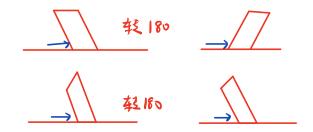
二自由度车辆动力学方程

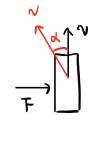
假设前轮转角S较小,假设 W=C



轮胎的侧偏特性

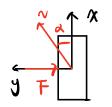






义侧偏角 定义 F=Cd C侧偏侧底侧偏侧底头侧偏侧底×侧偏角=侧向力

侧偏刚度-定是负数



负的侧偏力 ⇒ 正的侧偏角

的车模型

ar dy 都是负的

假设 δ 较小 (OS δ 与 1

ays y的关系,以及好,如的具体起式

$$N_y = \dot{y}$$
 $(\alpha_y = \ddot{y} + N_x \dot{\phi})$

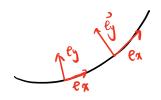
$$\vec{q} = \frac{d\vec{v}}{dt} = \frac{d(\sqrt{x}\vec{e_x} + \sqrt{y}\vec{e_y})}{dt}$$

在画生标系中 的,的为常矢量 前,的一

$$\Rightarrow \vec{a} = \frac{dv_x}{dt} \vec{e_x} + v_x \cdot \frac{de_x}{dt} + \frac{dv_y}{dt} \vec{e_y} + v_y \cdot \frac{d\vec{e_y}}{dt} \Rightarrow 0$$

在鲔生林 a= vx ex + Ny ey : ay= Ny

在车身生标 ex, in 不是常矢量 (Frenet 公式) (非惯性系)



y sip yeo

$$tandt = \frac{\dot{\varphi}b - v_y}{v_x} \approx dr$$

$$\dot{\gamma}b = V \sin \beta = \dot{\gamma}b - V y$$

$$tand_{I} = \frac{\dot{\gamma}b - v y}{v_{x}} \times dr \qquad \exists dr \notin \dot{\chi}\dot{\eta} \qquad \forall r = \frac{v y - \dot{\gamma}b}{v_{x}}$$

$$tan\theta = \frac{\dot{\varphi}a + v_y}{v_x}$$
 $ds = \theta - \delta = \frac{\dot{\varphi}a + v_y}{v_x} - \delta$

may = Cy dy + Cardr => m(
$$\mathring{v}_{y} + \mathring{v}_{x}\mathring{\phi}$$
) = Cy ($\frac{\mathring{\phi}a + \mathring{v}_{y}}{\mathring{v}_{x}} - \delta$) + Cy ($\frac{\mathring{v}_{y} - \mathring{\phi}b}{\mathring{v}_{x}}$)
$$1\mathring{\phi} = aCy dy + Cy dy => 1\mathring{\phi} = aCy \left(\frac{\mathring{\phi}a + \mathring{v}_{y}}{\mathring{v}_{x}} - \delta \right) - bCy \left(\frac{\mathring{v}_{y} - \mathring{\phi}b}{\mathring{v}_{x}} \right)$$

$$\frac{(\ddot{y})}{(\ddot{\phi})} = \begin{pmatrix} \frac{\cos f + \cos r}{m^{N}\chi} & \frac{a \cos f - b \cos r}{m^{N}\chi} - v_{\chi} \\ \frac{a \cos f - b \cos r}{1 v_{\chi}} & \frac{a^{2}\cos f + b \cos r}{1 v_{\chi}} \end{pmatrix} \begin{pmatrix} \ddot{y} \\ \ddot{\phi} \end{pmatrix} + \begin{pmatrix} -\frac{\cos f}{m} \\ -\frac{a \cos f}{1} \end{pmatrix} \begin{cases} 5 \\ -\frac{a \cos f}{1} \end{cases}$$

该
$$x = \begin{pmatrix} \dot{y} \\ \dot{\varphi} \end{pmatrix}$$

设 $X = \begin{pmatrix} \dot{y} \\ \dot{\varphi} \end{pmatrix}$ $U = \delta$ $\dot{\chi} = AX + Bu$ 通过控制 δ , 实现对 \dot{y} , $\dot{\gamma}$ 的控制