

Section: 10

Sparse Matrix

and

Polynomial Representation

Sparse Matrix Representation -

	1	2	3	4	5	6	7	8	9
1	0	0	0	0	0	0	0	3	0
2	0	0	8	0	0	10	0	0	0
3	0	0	0	0	0	0	0	0	0
4	4	0	0	0	0	0	0	0	0
5	0	0	0	0	0	0	0	0	0
6	0	0	2	0	0	0	0	0	0
7	0	0	0	6	0	0	0	0	0
8	0	9	0	0	5	0	0	0	0

8x9 (72 element)

72x2=144 bytes

Sparse Matrix → In numerical analysis and scientific computing, a sparse matrix or sparse array is a matrix in which most of the elements are zero.

Method to store non-zero elements -

1. Coordinate list (3 column representation)
2. Compressed Sparse Row

3-Column Representation :-

Row number, Column number, value (Element)

No. of rows, no. of column →

row	column	element
8	1	8
1	8	3
2	3	8
2	6	10
4	1	4
6	3	2
7	4	6
8	2	9
8	5	5

Compressed sparse rows :-

$A[3, 8, 10, 4, 2, 6, 9, 5]$ (order wise)

~~IA~~ [0, 1, 3, 3, 7, 7, 9,]
 0 1 2 3 4 5 6
 ↓ ↓ ↓ ↓ ↓
 2+1 3+0 3+4 7+0

~~JA~~ [8, 3, 6, 1, 3, 4, 2, 5]

IA [0, 1, 3, 3, 4, 4, 5, 6, 8]
 0 1 2 3 4 5 6 7 8
 ↑
 prev + no. of element
 sum

IA [8, 3, 6, 1, 3, 4, 2, 5]

space

$$\Rightarrow 8 + 9 + 8$$

$$\Rightarrow 25 \times 2$$

$$= 50 \text{ bytes}$$

Addition of Sparse Matrices

$$A = \begin{bmatrix} 1 & 2 & 3 & 4 & 5 & 6 \\ 0 & 0 & 0 & 6 & 0 & 0 \\ 0 & 7 & 0 & 0 & 0 & 0 \\ 0 & 2 & 0 & 5 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 4 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

$$B = \begin{bmatrix} 1 & 2 & 3 & 4 & 5 & 6 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 3 & 0 & 0 & 5 & 0 \\ 0 & 0 & 2 & 0 & 0 & 7 \\ 0 & 0 & 0 & 9 & 0 & 0 \\ 8 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

$$A + B \rightarrow C = \begin{bmatrix} 1 & 2 & 3 & 4 & 5 & 6 \\ 0 & 0 & 0 & 6 & 0 & 0 \\ 0 & 10 & 0 & 0 & 5 & 0 \\ 0 & 2 & 2 & 5 & 0 & 7 \\ 0 & 0 & 0 & 9 & 0 & 0 \\ 12 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

Non-zero element $\rightarrow 9$

Adding using Coordinate

A

	0	1	2	3	4	5
	5	1	2	3	3	5
	6	4	2	4	4	1
	5	6	(7)	2	5	4

B

	0	1	2	3	4	5	6
	5	2	2	3	3	4	8
	6	2	8	3	6	4	1
	6	(3)	5	2	7	9	8

C

	0	1	2	3	4	5	6	7	8	9
	5	1	2	2	3	3	3	3	4	5
	6	4	2	5	2	3	4	6	4	1
		6	10	5	2	2	5	7	9	12

$rows[i] < rows[j]$

copy $[i]$ to c and $i++$;

$column[i] < column[j]$

copy $[i]$ to c and $i++$;

$rows[i] == rows[j] \& \& column[i] == column[j]$

Add both element

$rows[i] > rows[j]$

copy j to c and $j++$;

$column[i] > column[j]$

copy j to c and $j++$;

$rows[i] \neq rows[j]$ & $column[i] < column[j]$

copy i to c and $i++$;

$rows[i] == rows[j]$ & $column[i] > column[j]$

copy i to c and $j++$;

Array Representation of Sparse Matrix :-

$$A = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 & 5 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 0 & 0 & 7 & 0 & 0 \\ 2 & 0 & 0 & 5 & 0 \\ 9 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 4 \end{bmatrix} \end{matrix}$$

dimension and no zero element

4x5

Non-zero element = 5

	0	1	2	3	4	5
i	0	1	2	2	3	4
j	5	3	1	4	1	5
x	5	7	2	5	9	4

m x n

- How to represent
- How to create
- How to add

struct Element

{

int i;

int j;

int x;

};


```
struct sparse
{
```

```
    int m;
```

```
    int n;
```

```
    int num;
```

```
    struct Element *e; // Dynamic Array
```

```
}
```

↓
Array of element

```
void create(struct sparse *s)
{
```

```
    printf("Enter Dimensions");
```

```
    scanf("%d%d", &s->m, &s->n);
```

```
    printf("Enter no. of non-zero");
```

```
    scanf("%d", &s->num);
```

```
    s->e = new Element[s->num];
```

```
    printf("Enter all elements");
```

```
    for(int i=0; i<s->num; i++)
```

```
    {
```

```
        scanf("%d%d%d", &s->e[i].i,
```

```
              &s->e[i].j,
```

```
              &s->e[i].x);
```

```
    }
```

```
}
```

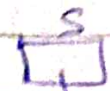
```
void main()
```

```
{
```

```
    struct sparse s;
```

```
    create(&s);
```

```
}
```



	s
m	4
n	5
min	5
0	

	0	1	2	3	4	5
i						
j						
x						

Program for Adding Sparse Matrix →

$$S_1 = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 & 5 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 0 & 0 & 3 & 0 & 0 \\ 4 & 0 & 0 & 0 & 7 \\ 0 & 0 & 5 & 0 & 8 \\ 0 & 6 & 0 & 0 & 0 \end{bmatrix} \end{matrix}$$

$$S_2 = \begin{bmatrix} 0 & 0 & 0 & 0 & 2 \\ 0 & 5 & 0 & 0 & 6 \\ 4 & 0 & 8 & 0 & 0 \\ 0 & 0 & 0 & 0 & 9 \end{bmatrix}$$

$$S_1 \rightarrow$$

m	4	0	1	2	3	4	5
n	5	1	2	2	3	3	4
num	6	3	1	5	3	5	2
e	→	3	4	7	5	8	6

$$S_2 \rightarrow$$

m	4
n	5
num	6
e	

0	1	2	3	4	5
1	2	3	3	3	4
5	2	5	1	3	5
2	5	6	4	8	9

```
void add(struct sparse *s1, struct sparse *s2)
{
```

```
    if (s1->m != s2->m || s1->n != s2->n)
    {
```

```
        return 0;
```

```
    }
```

```
    sparse *sum;
```

```
    sum = new sparse;
```

```
    sum =
```

```
    sum->m = s1->m; sum->n = s1->n;
```

$$sum$$

→ m	
n	
num	
e	

sum → e = new Element [s1 → num + s2 → num];

while (i < s1 → num & j < s2 → num)

{ if (s1 → e[i].i < s2 → e[j].i)

if (s1 → e[i].i < s2 → e[j].i)

{

sum → e[k++] = s1 → e[i++];

}

else if (s1 → e[i].i > s2 → e[j].i)

{

sum → e[k++] = s2 → e[j++];

}

else

{

if (s1 → e[i].j < s2 → e[j].j)

{

sum → e[k++] = s1 → e[i++];

}

if (s1 → e[i].j > s2 → e[j].j)

{

sum → e[k++] = s2 → e[j++];

}

else

{

sum → e[k++] = s1 → e[i++];

sum → e[k++] = s2 → e[j++];

}

}

}

Polynomial Representation

$$p(x) = \frac{1}{3}x^5 + 2x^4 + 5x^2 + 2x + 7$$

↑ coefficient
↑ exponent
↑ variable

1) Polynomial Representation

2) Evaluation of Polynomial

3) Addition of two polynomials

n=5

coeff	3	2	5	2	7
Exp	5	4	2	1	0

struct Term

{

int coeff;

int Exp;

};

struct Poly

{

int n;

struct Term *t;

};

P

n	
t	1

0	1	2	3	4	5

struct Poly P;

printf("No. of non-zero terms");

scanf("%d", &P.n);

P.t = new term[P.n]

printf("Enter Polynomial terms");

for (i=0; i<P.n; i++)

{
printf("Term no %d", i+1)

scanf("%d %d", &P.t[i].coeff,

&P.t[i].exp);

}

Polynomial Evaluation →

	P		0	1	2	3	4
n	5	coeff	3	2	5	2	7
i		exp	5	4	2	1	6

struct Poly P;

int sum=0;

for (i=0; i<P.n; i++)

{

sum += P.t[i].coeff * Pow(x, P.t[i].exp);

}

return sum;

Polynomial Addition →

$$P_1(x) = 5x^4 + 2x^2 + 5$$

$$P_2(x) = 6x^4 + 5x^3 + 9x^2 + 2x + 3$$

P ₁			0	1	2
n	3	coeff	5	2	5
t	→	Exp	4	2	0

i → i →

P ₂			0	1	2	3	4
n	5	coeff	6	5	9	2	3
t	→	Exp	4	3	2	1	0

j → j → j → j →

P ₃			0	1	2	3	4
n		coeff	11	5	11	2	8
t	→	Exp	4	3	2	1	0

k → k → k → k →

$$i = j = k = 0;$$

```
while(i < p1.n && j < p2.n)
{
```

```
    if( p1.t[i].Exp > p2.t[j].Exp)
    {
```

```
        p3.t[k++] = p1.t[i++];
```

```
    }
```

```
    else if( p2.t[j].Exp > p1.t[i].Exp)
    {
```

```
        p3.t[k++] = p2.t[j++];
```

```
    }
```

else

}

$$P3.t[k\#].Exp = P1.t[i].Exp;$$

$$P3.t[k++].coeff = P1.t[i++].coeff + P2.t[j++].coeff;$$

}

}