

$$mgh = \frac{1}{2}mv^2 + \frac{1}{2}I\omega^2$$

$$0.75mv^2 = mgh$$

9. $2.2 - 0.27 = 1.93 \text{ m}$

$$t_1 = \frac{1.93}{v_{i1}}$$

let the vertical distance of falling be Δx

$$\Delta x = \frac{1}{2}at^2 = \frac{1}{2}g \cdot \left(\frac{1.93}{v_{i1}}\right)^2 = \frac{18.63}{v_{i1}^2} \quad (1)$$

\therefore conservation of energy

$$\therefore \frac{1}{2}mv_{i1}^2 = \frac{1}{2}kx_1^2$$

$$v_{i1}^2 = \frac{0.011^2 \cdot k}{m}$$

substitute this into (1)

$$\Delta x = 18.63 \times \frac{m}{0.011^2 \cdot k} = \frac{153966.94 \cdot m}{k}$$

\therefore the right time need to hit the center of the box is $t_2 = \frac{2.2}{v_{i2}}$

$$\therefore \Delta x = \frac{1}{2}at^2 \Rightarrow \frac{153966.94 \cdot m}{k} = \frac{1}{2}g \cdot \frac{2.2^2}{v_{i2}^2} \Rightarrow v_{i2}^2 = \frac{k}{6362.27 \cdot m}$$

$$\therefore \frac{1}{2}kx_2^2 = \frac{1}{2}mv_{i2}^2 \Rightarrow \frac{m}{2} \cdot \frac{k}{6362.27 \cdot m} = \frac{1}{2}k \cdot x_2^2 \Rightarrow x_2 = 0.012 \text{ m} = 1.2 \text{ cm}$$

10. (a) $mgh = \frac{1}{2}mv^2 + \frac{1}{2}I\omega^2$

$$mgh = \frac{1}{2}mv^2 + \frac{1}{4}mv^2$$

$$0.75v^2 = gh$$

$$v^2 = \frac{gh}{0.75}$$

$$v^2 = \frac{30}{0.75}$$

$$v = 6.33 \text{ m/s}$$

(b) $\frac{1}{2}I\omega^2 = \frac{1}{2} \cdot \left(\frac{1}{2} \cdot m \cdot r^2\right) \cdot \left(\frac{v}{r}\right)^2$

$$= \frac{1}{4} \cdot m \cdot v^2$$

$$= \frac{1}{4} \cdot 2 \cdot 6.33^2$$

$$= 20.04 \text{ J}$$

2a. $\frac{3}{\sin 30^\circ} = v_f^2 - v_i^2 = 40$

$$6a = 20$$

$$a = 3.33 \text{ m/s}^2$$