

Computational Neuroscience Course

An Introduction to Computational Neuroscience

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A brief pre-history

Theoretical Neurophysiology

1907 Lapique:
integrate-and-fire model

1952 Hodgkin-Huxley:
theory of action potential

1960's Rall:
cable theory of dendrites

1970's Wilson-Cowan:
firing-rate population models

1980's: Biophysics of neurons &
synapses, network dynamics

Psychology & Computer Science

1949 Hebb:
learning rules

1960's Rosenblatt, Minsky:
perceptrons

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perceptrons

1970's signal detection theory

1980's Hopfield:
associative memory model



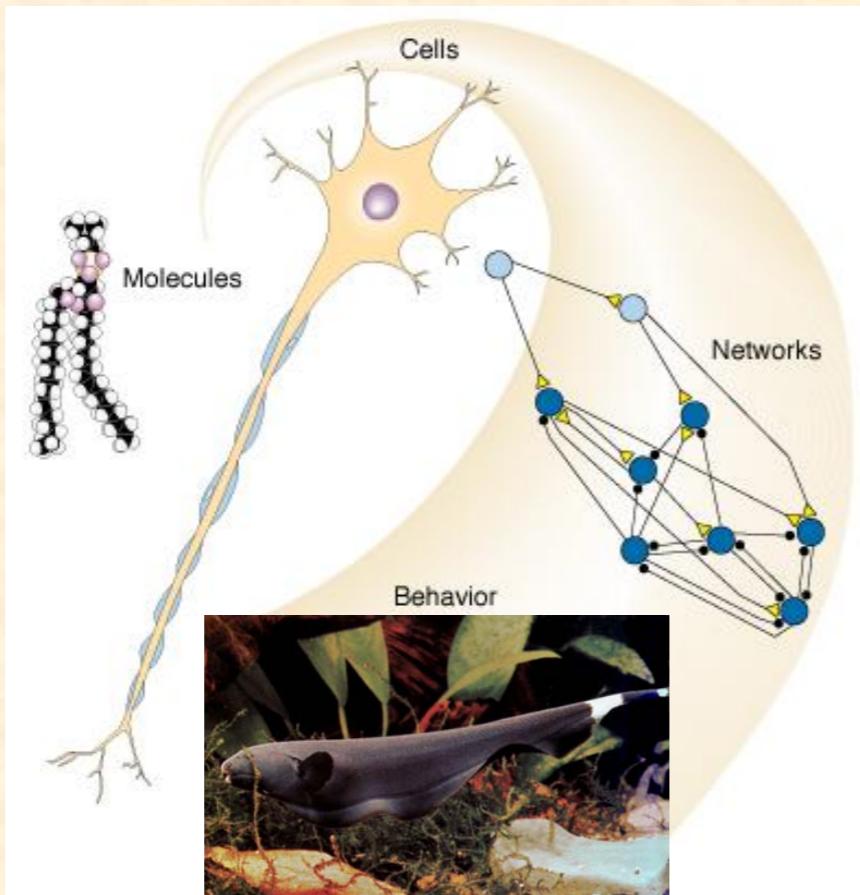
Sejnowski, Koch, Churchland, Computational neuroscience. *Science* 1988 241: 1299-1306
Methods in Computational Neuroscience Summer School, Marine Biological Laboratory

adapted from Xiaojing Wang's slide

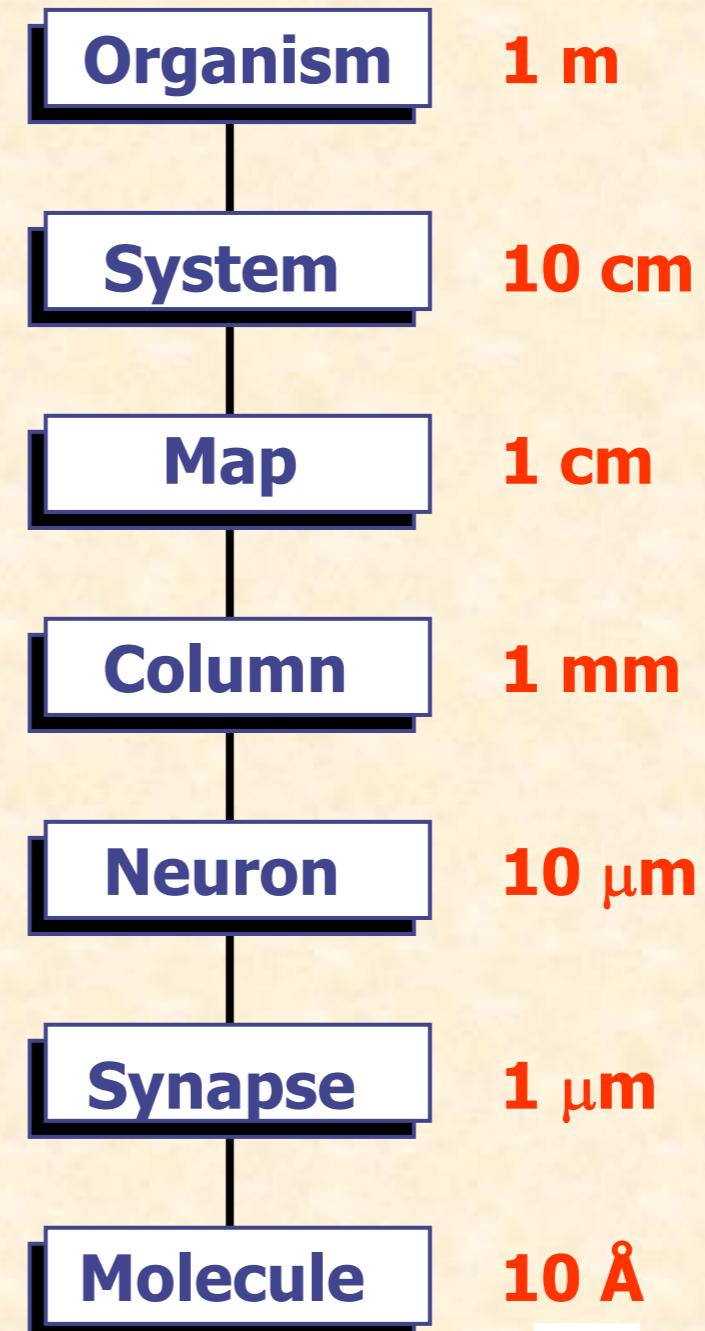
Principles of Neuroscience ?



Multiscale Organization of the Nervous System



Delcomyn 1998



“To pile speculation on speculation, I would say that the next stage could be hierarchy or specialization of function, or both.... with increasing complication at each stage, we go on up the hierarchy of sciences. We expect to encounter fascinating and, I believe, very fundamental questions at each stage in fitting together less complicated pieces into the more complicated system and understanding the basically new types of behavior which can result.”

P. W. Anderson, 1972
Nobel Laureate
condensed matter physicist

More is different

Fitzgerald: The rich are **different** from us.

Hemingway: Yes, they have **more** money.

a conversation somewhere in Paris in 1920s



David Marr
1945-1980



Henry Markram
1962 -

VISION



David Marr

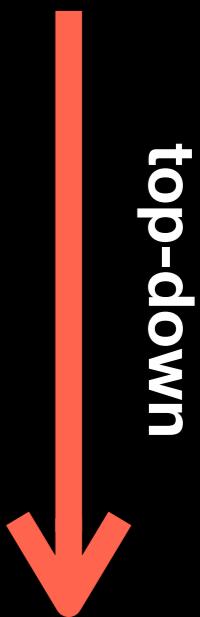
FOREWORD BY
Shimon Ullman
AFTERWORD BY
Tomaso Poggio

blue brain project



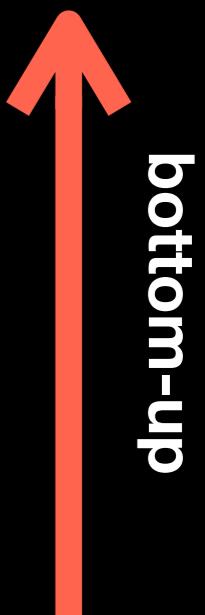
David Marr's three level theory

- **Computational level:** Identify the computational problem and task that the brain solves.
- **Algorithmic level:** Find the mathematical procedures that solve the problem.
- **Implementation level:** How the algorithms are realized by the nervous system.



Henry Markram's three level theory

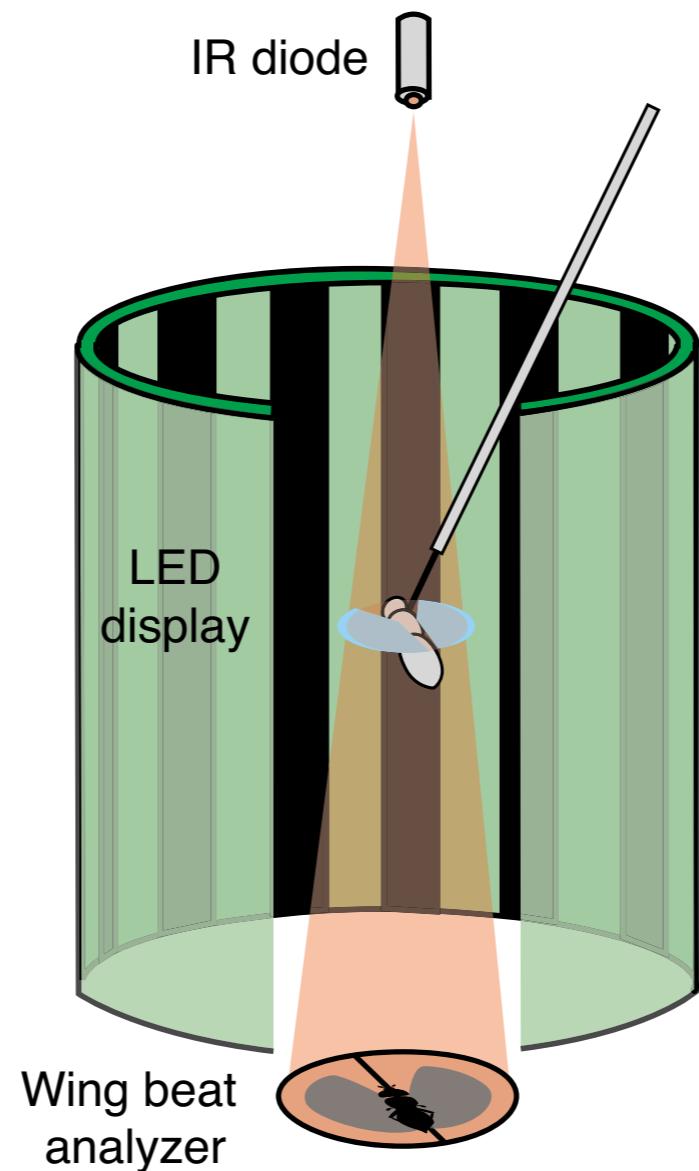
- **Systems level:** describe how population neural dynamics and behaviors emerge from ensembles of neurons.
- **Cellular level:** develop biophysically accurate models to describe input-output relationships of different cell types.
- **Structure level:** identify how neurons are statistically connected to each other in a circuit.



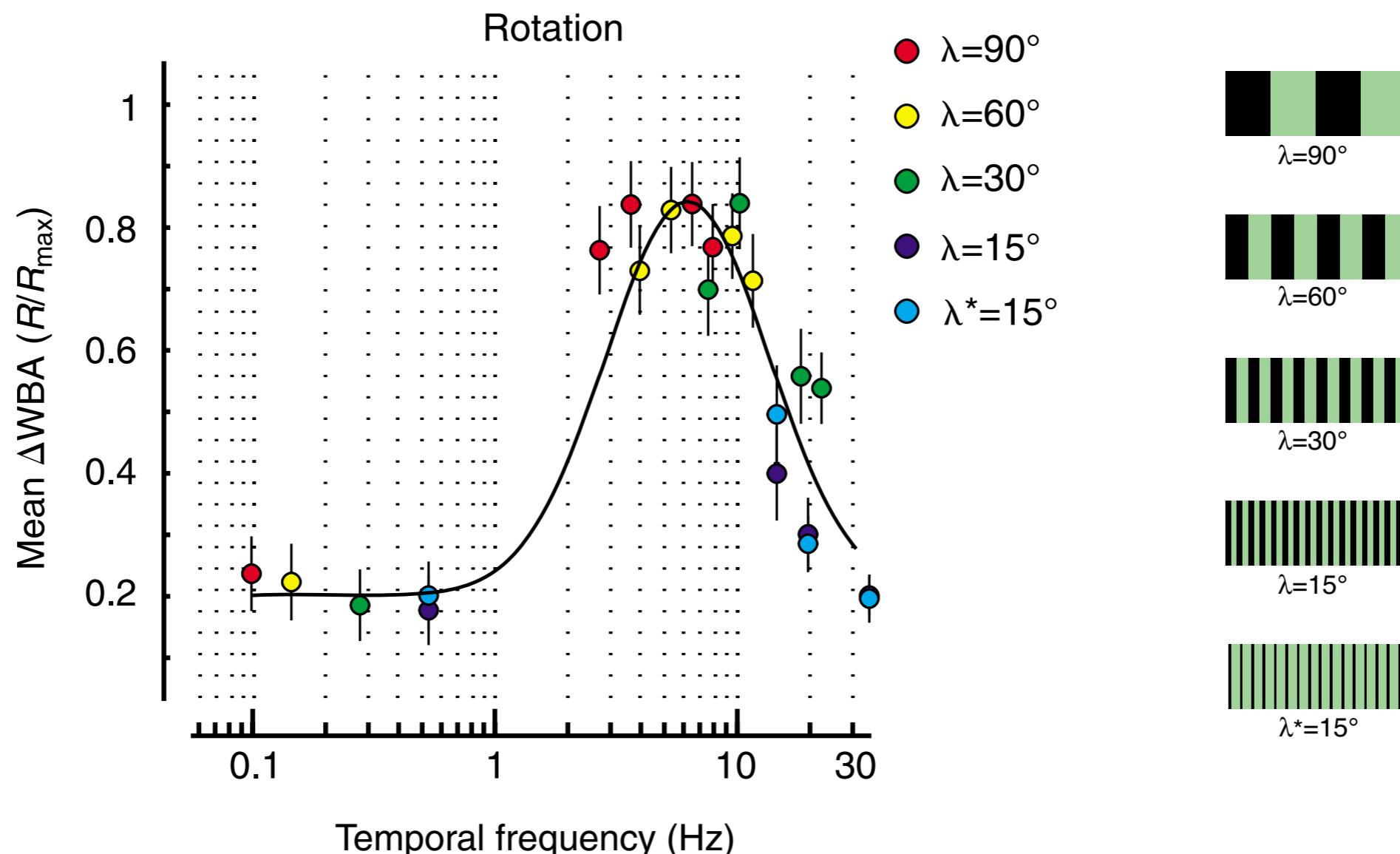
Motion detection, an example



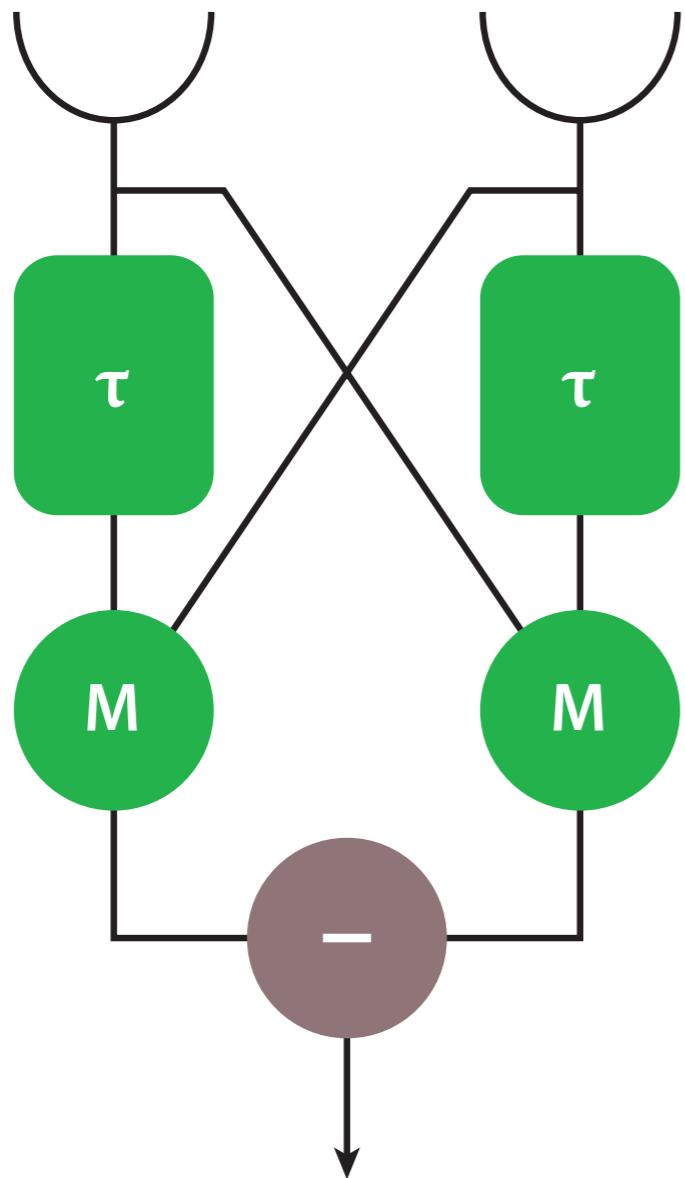
Optomotor response in fly



Optomotor response in fly

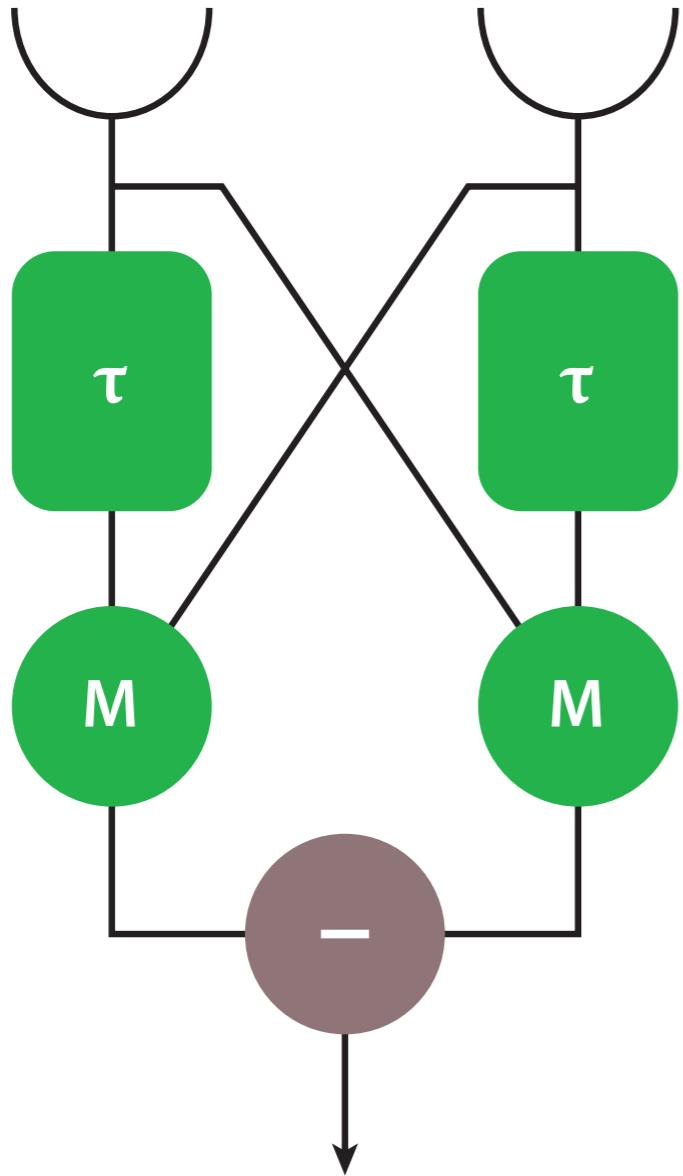


Hassenstein-Reichardt Detector Model



Werner Reichardt

Hassenstein-Reichardt Detector Model

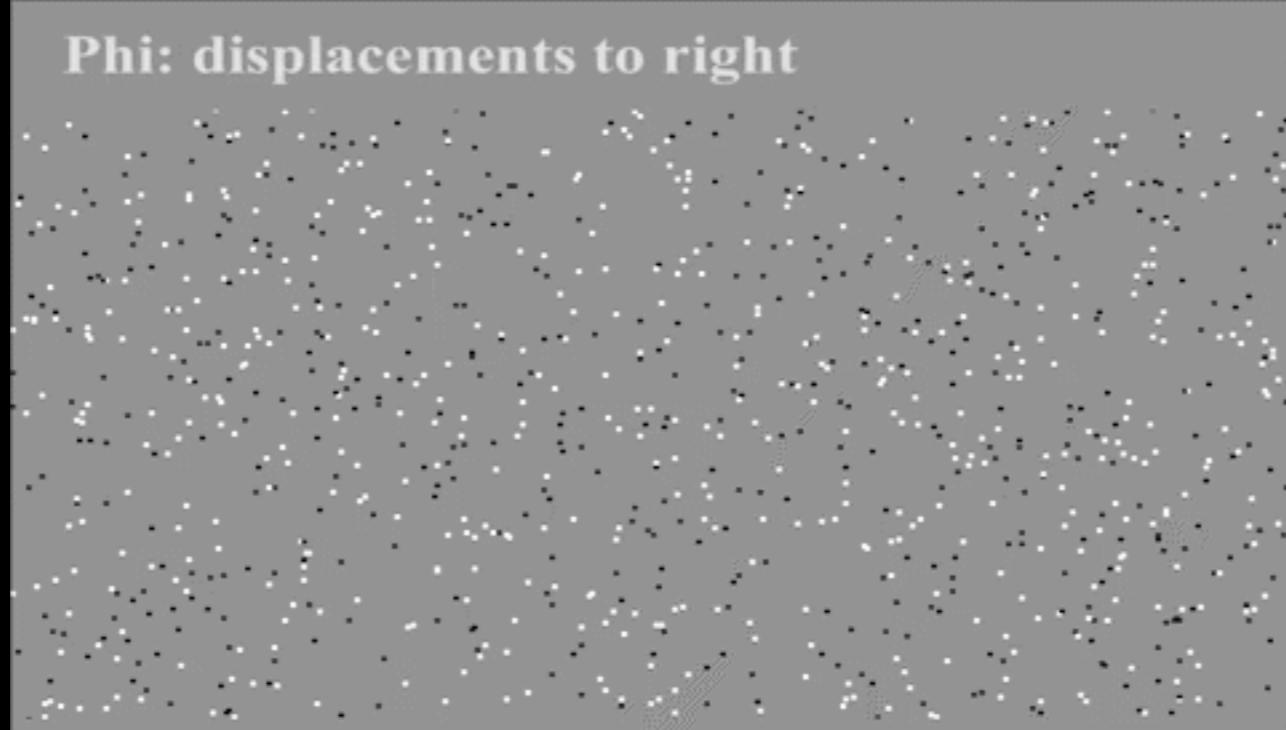


$$r_1(t) = \int_0^{\infty} s_1(t - \tau)D(\tau)d\tau; \quad r_2(t) = \int_0^{\infty} s_1(t - \tau)\delta(\tau)d\tau$$
$$r_3(t) = \int_0^{\infty} s_2(t - \tau)\delta(\tau)d\tau; \quad r_4(t) = \int_0^{\infty} s_2(t - \tau)D(\tau)d\tau;$$
$$R(t) = r_1(t)r_3(t) - r_2(t)r_4(t)$$

$$D(\tau) = \frac{1}{\tau_0} \exp(-\tau/\tau_0)$$

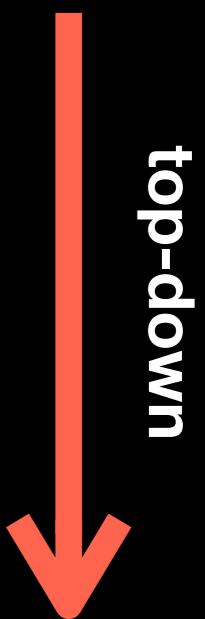
$$\langle R \rangle = \frac{\omega_0 \tau_0}{\omega_0^2 \tau_0^2 + 1}$$

Phi: displacements to right

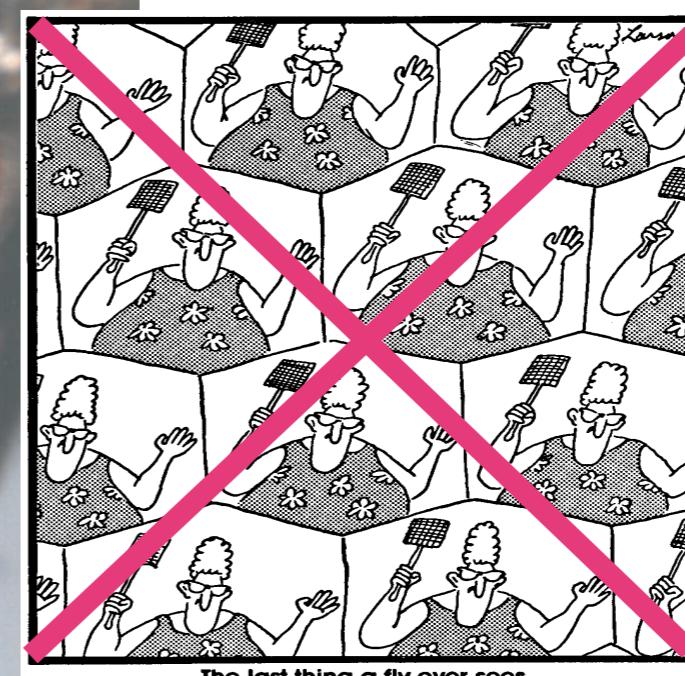
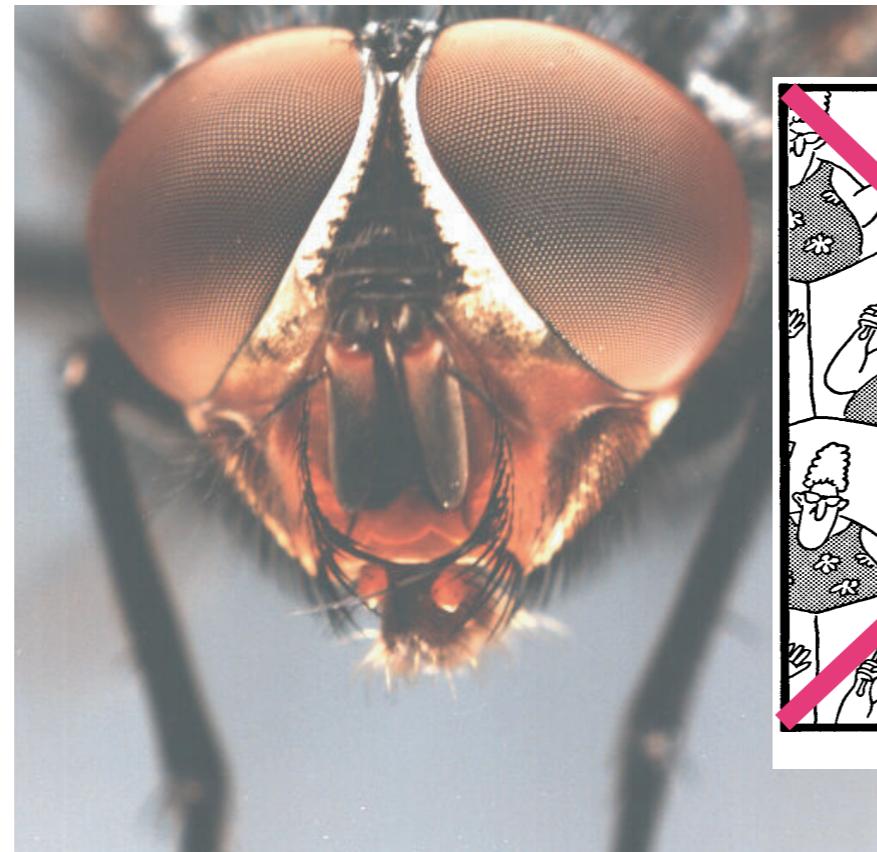


adapted from Damon Clark's slide

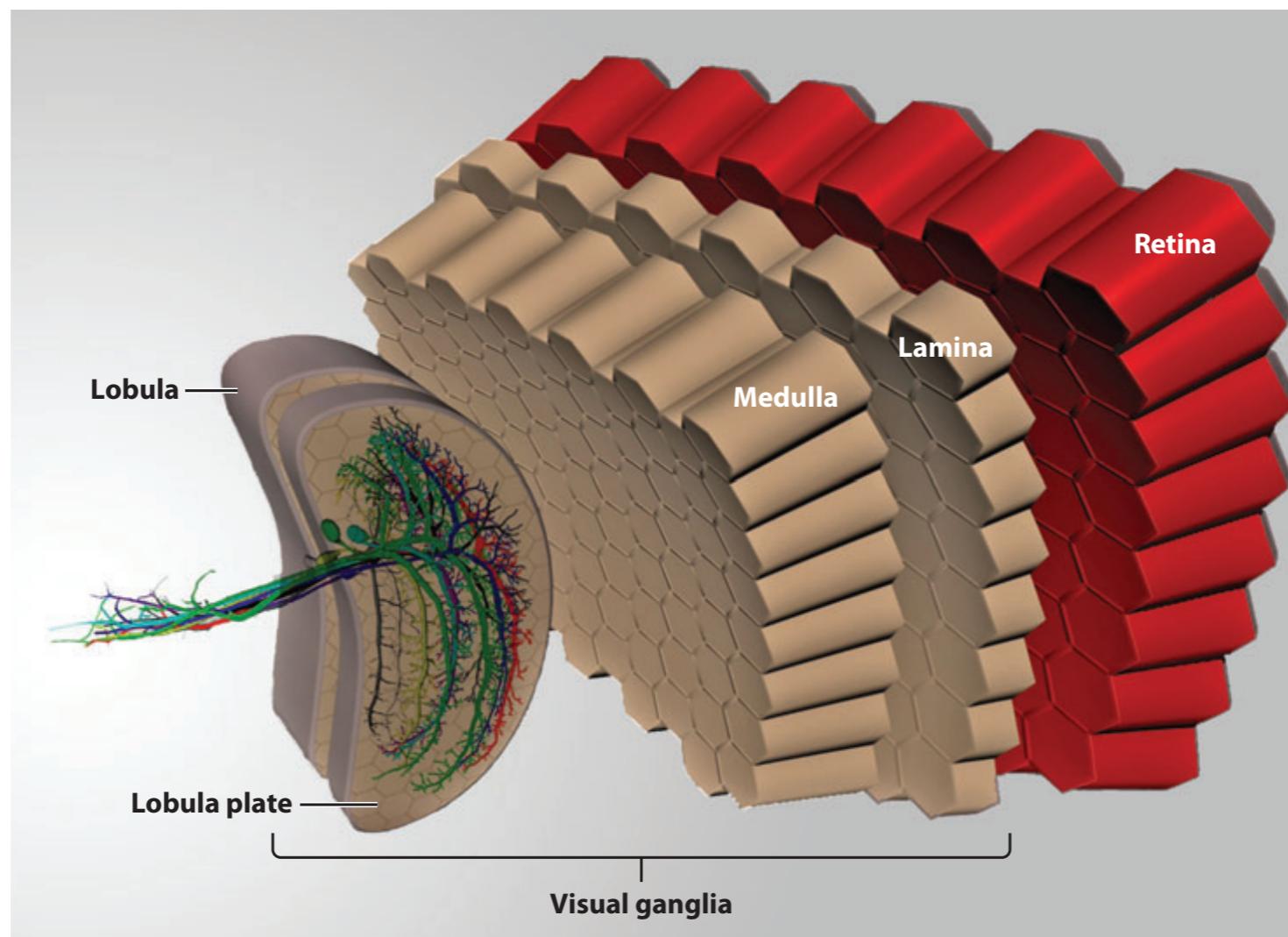
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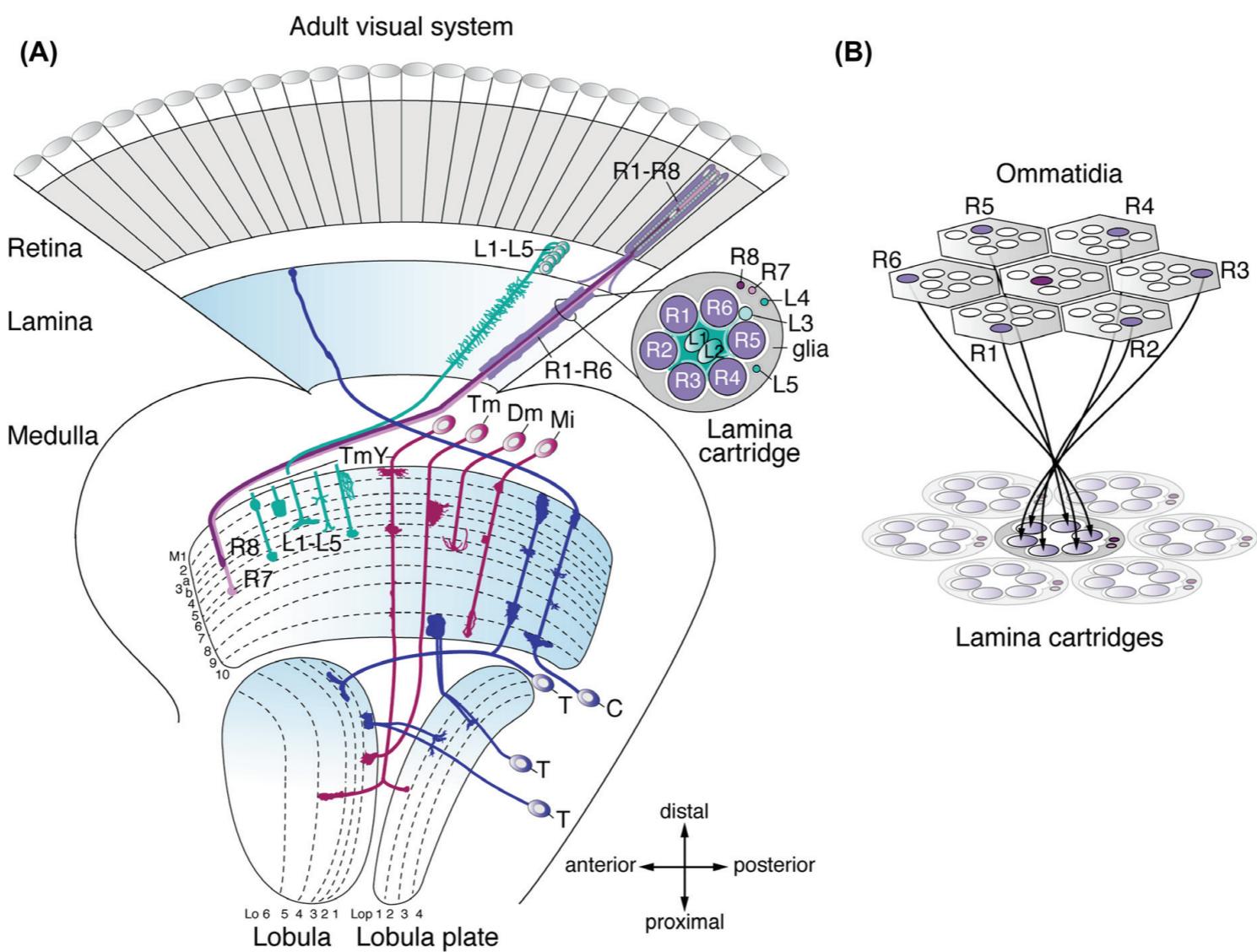
The Fly Visual System

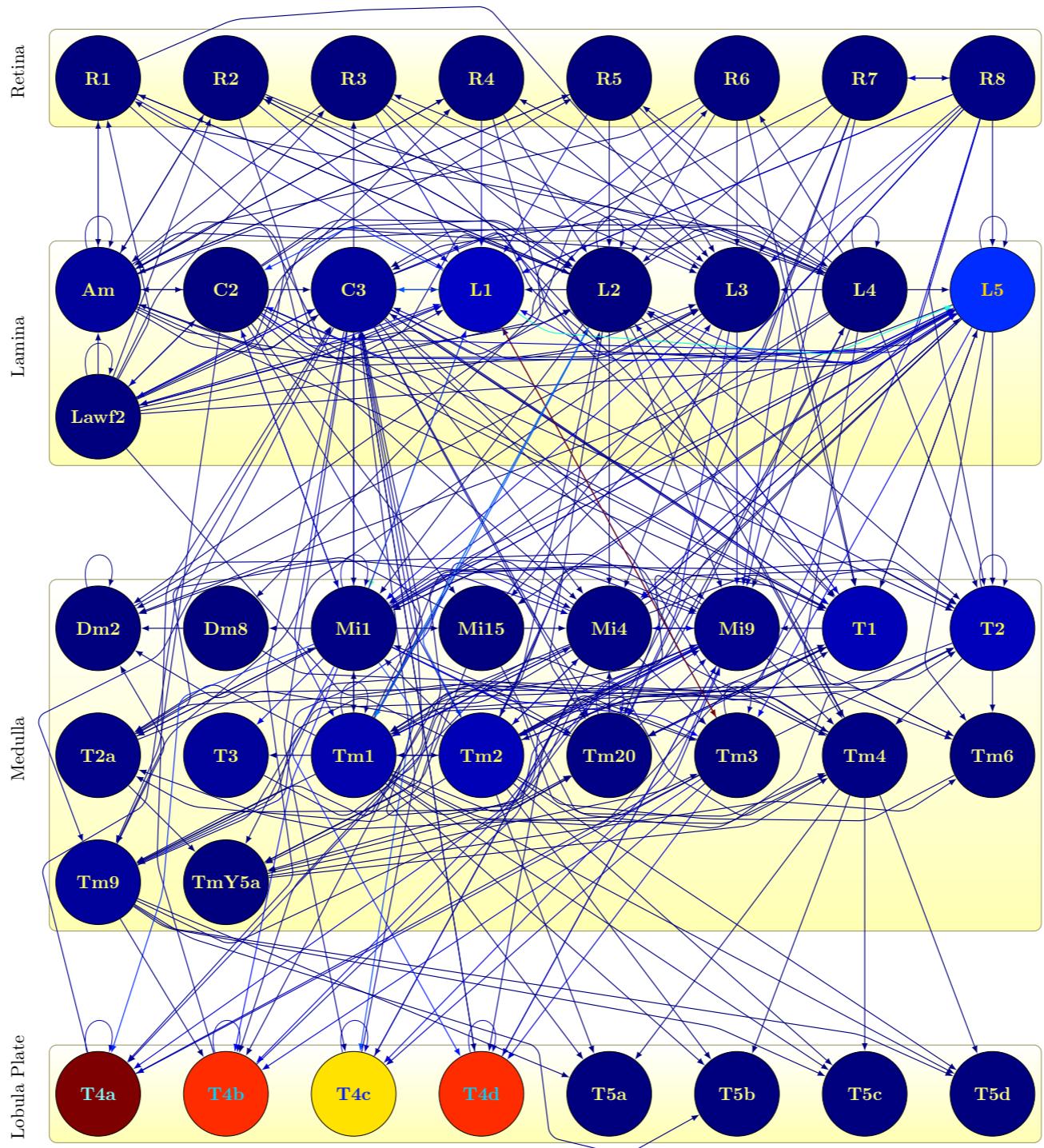


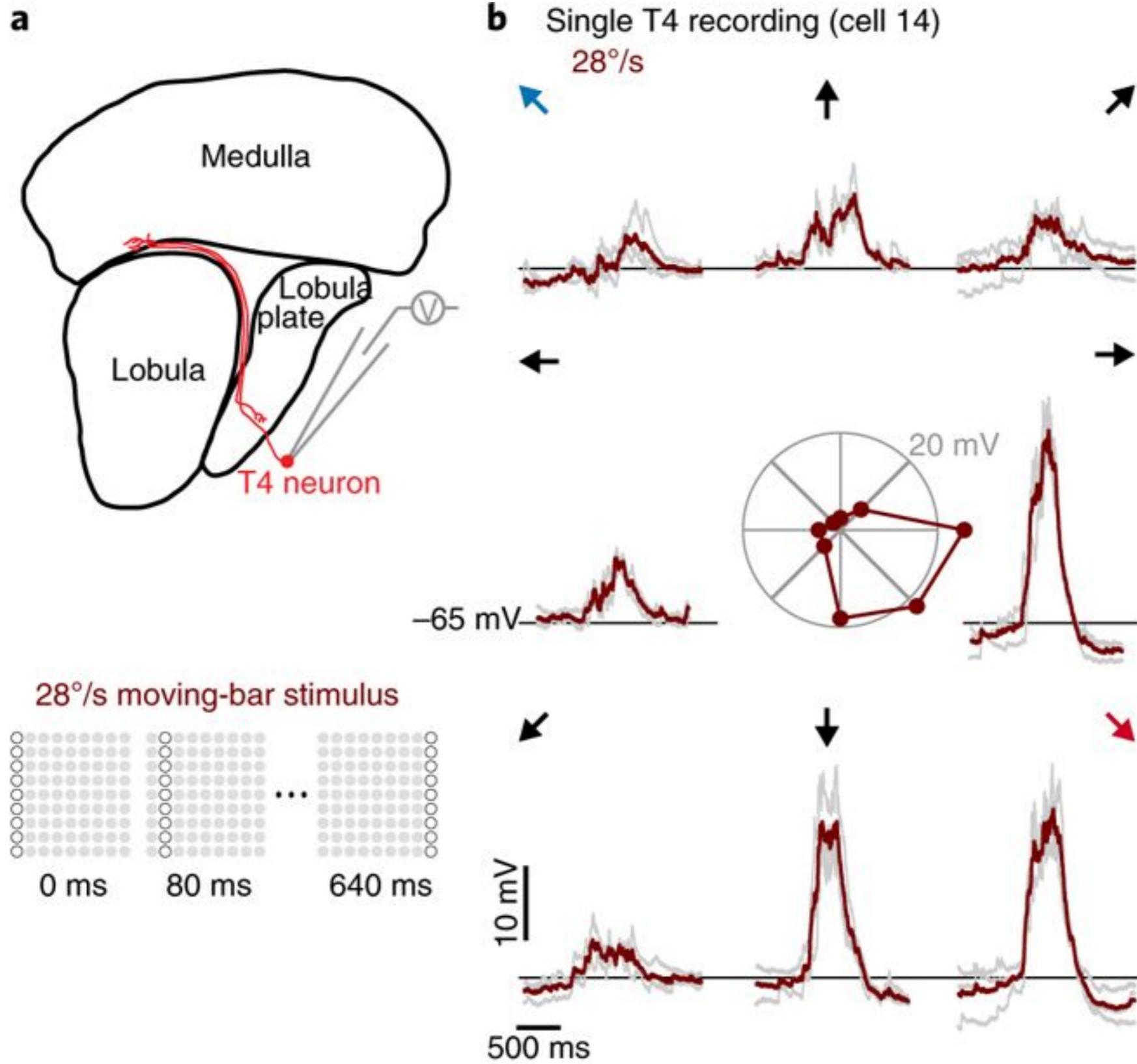
The Fly Visual System



The Fly Visual System



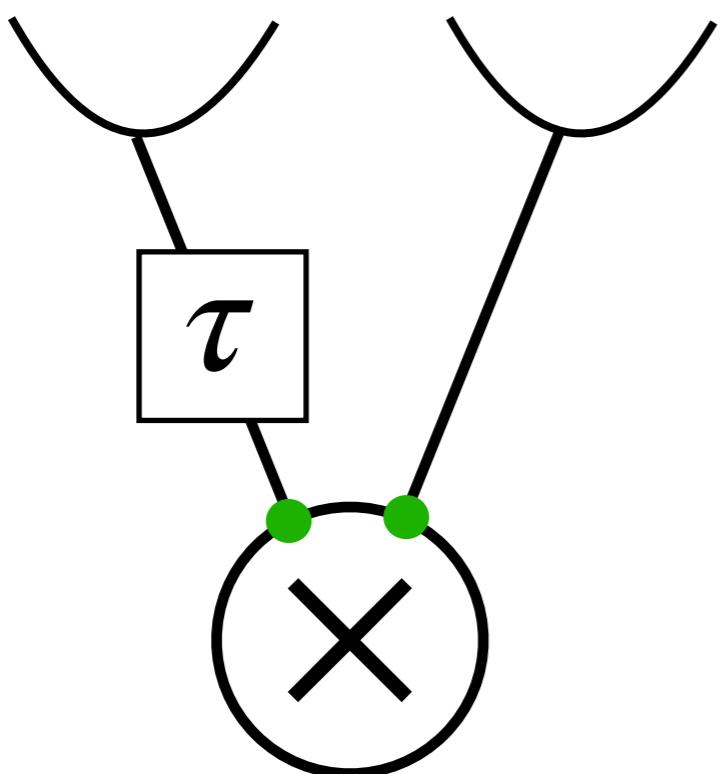




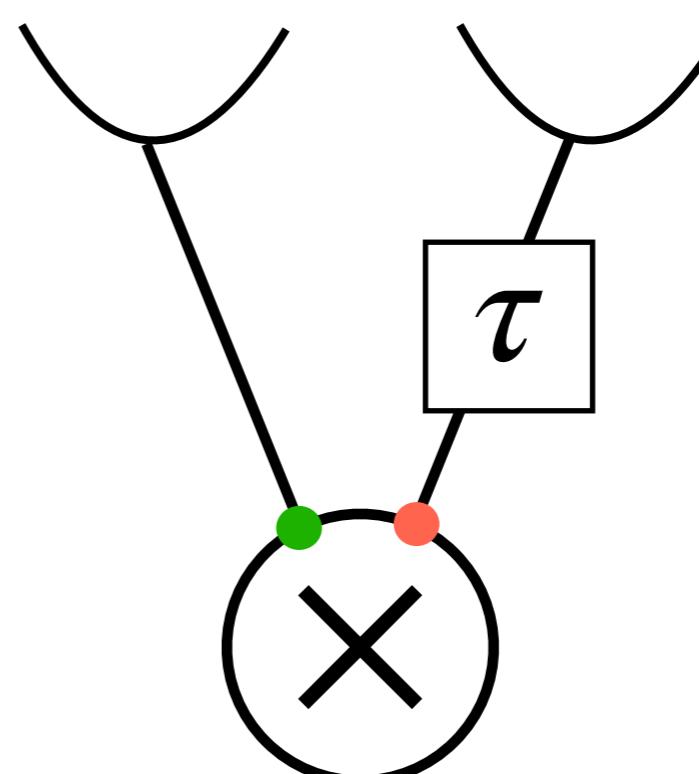
preferred
direction



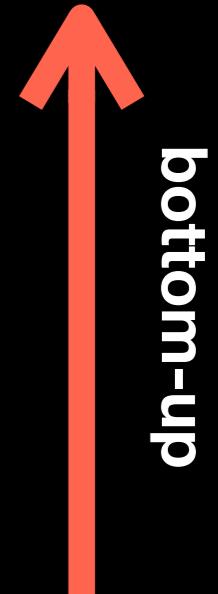
null
direction



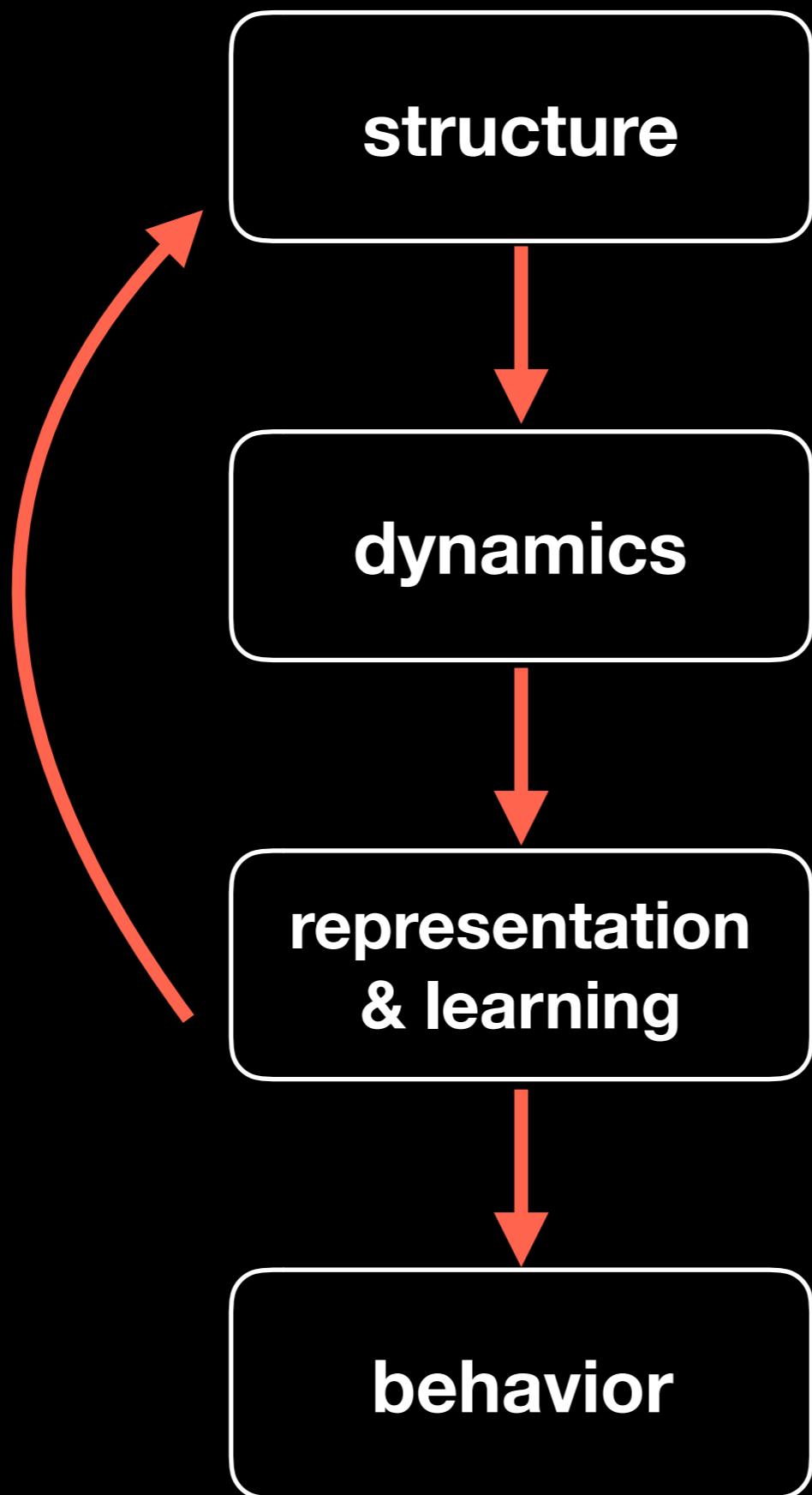
Reichardt model



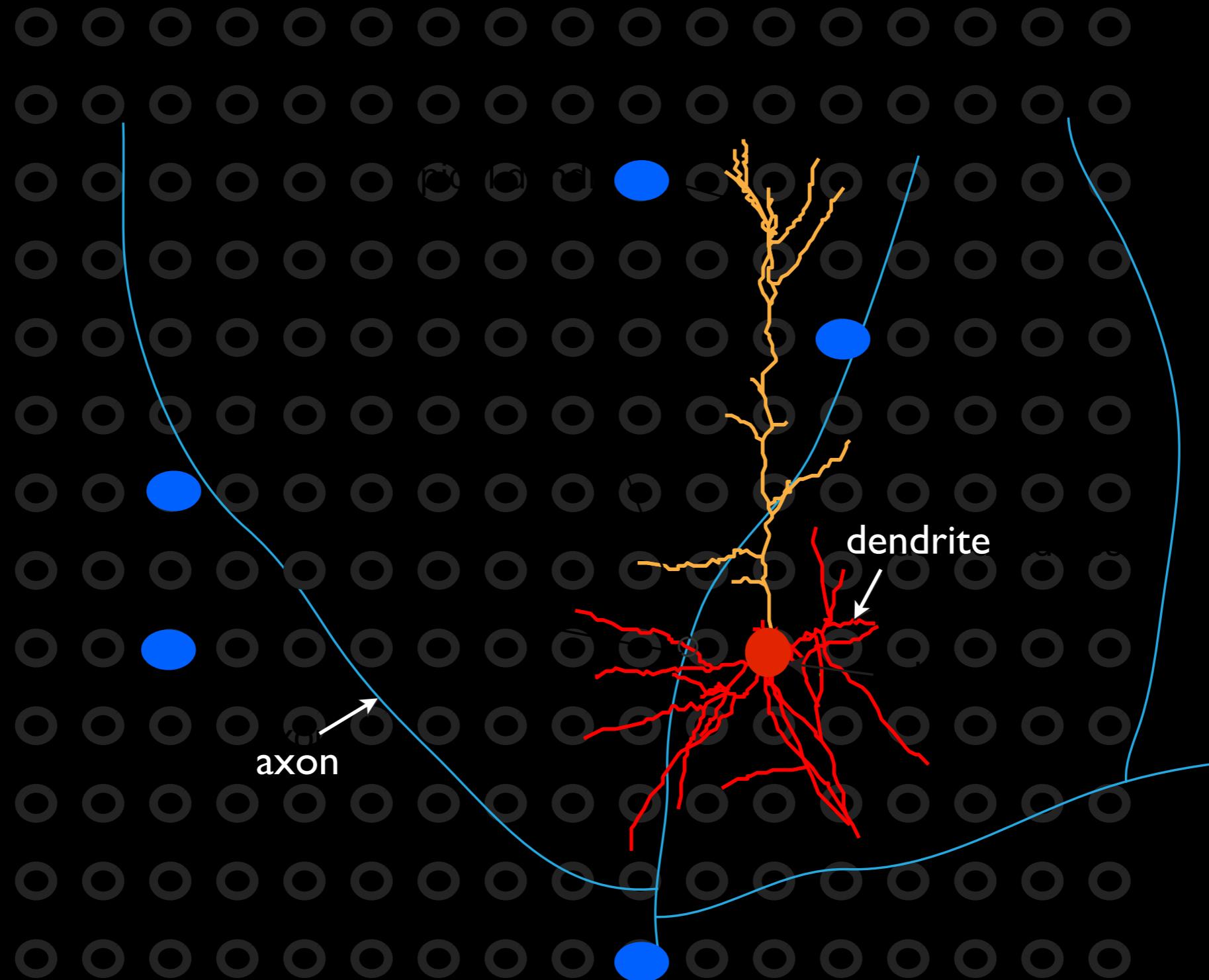
barlow-levick model

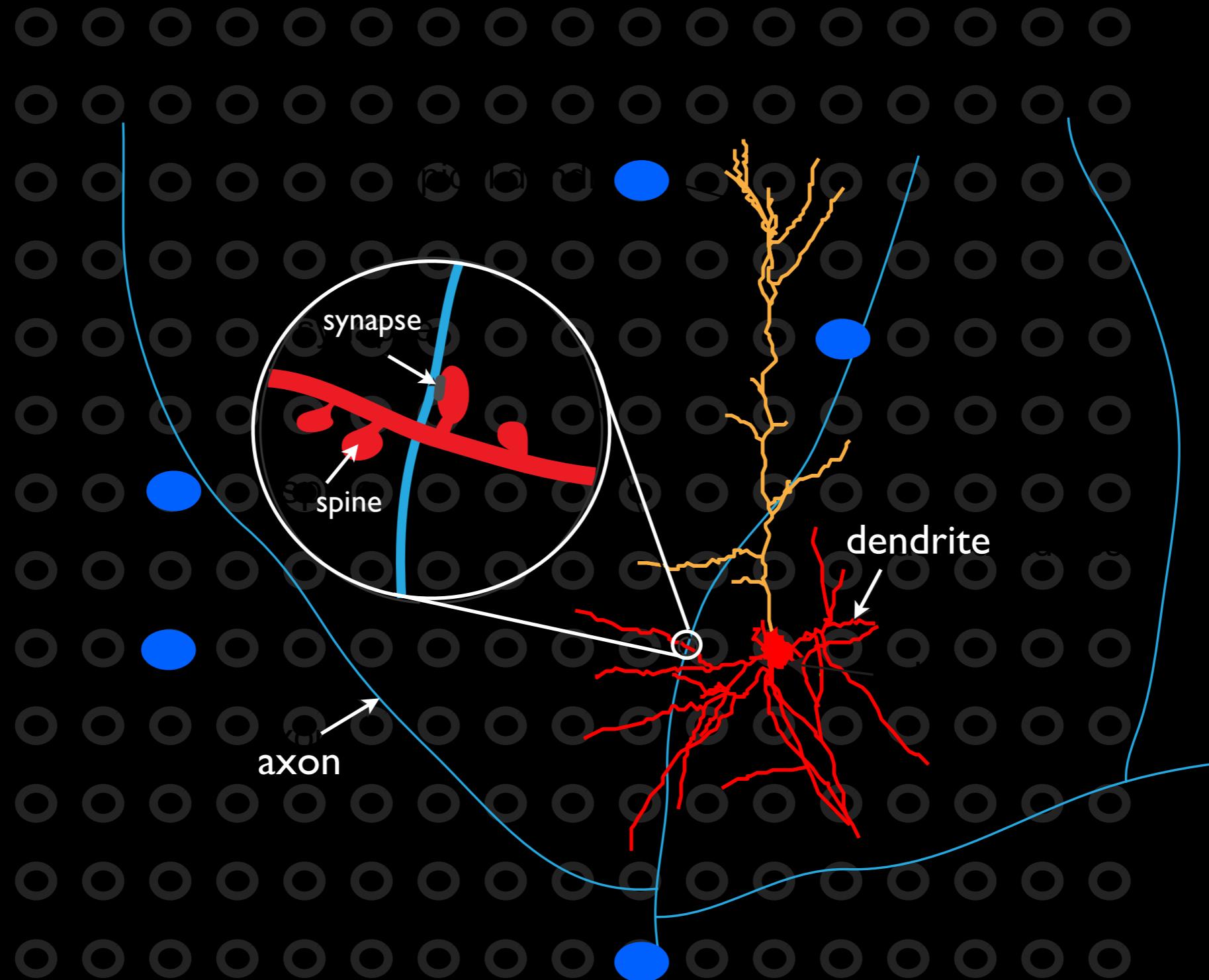
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- 

2019 Fall Course Program

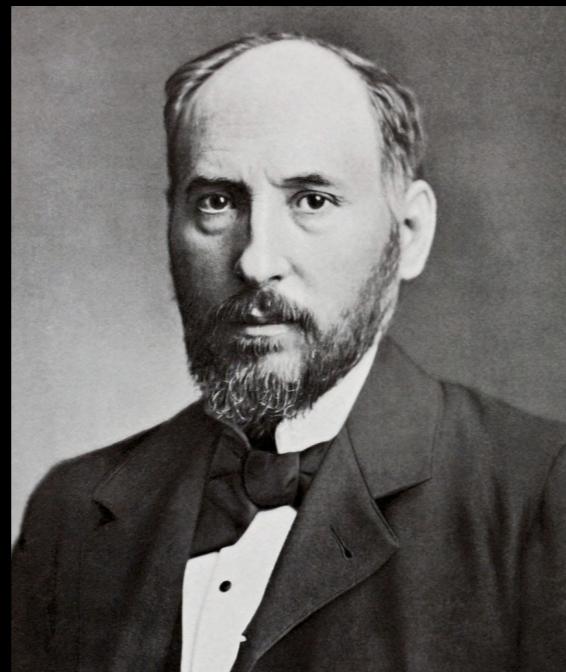


The Neuron Doctrine

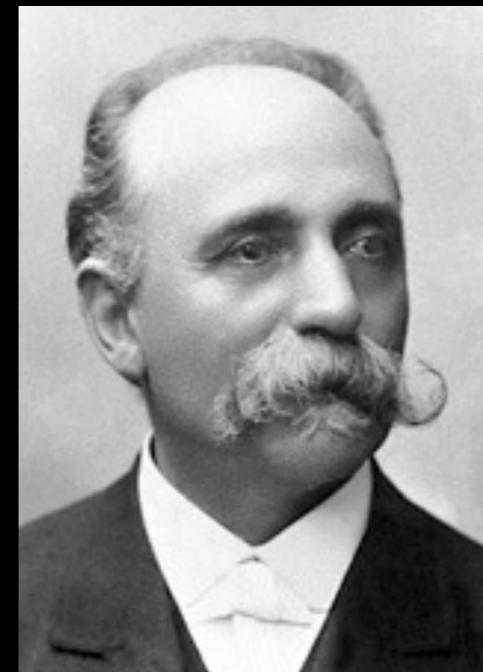




The Debate between Cajal and Golgi

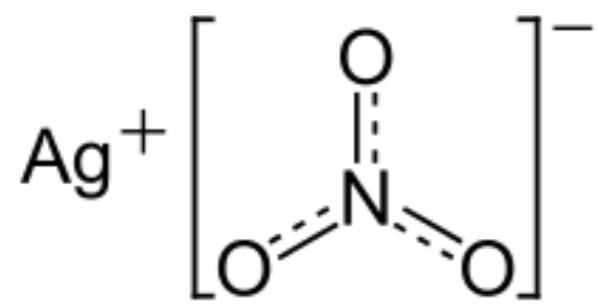


Ramon y Cajal

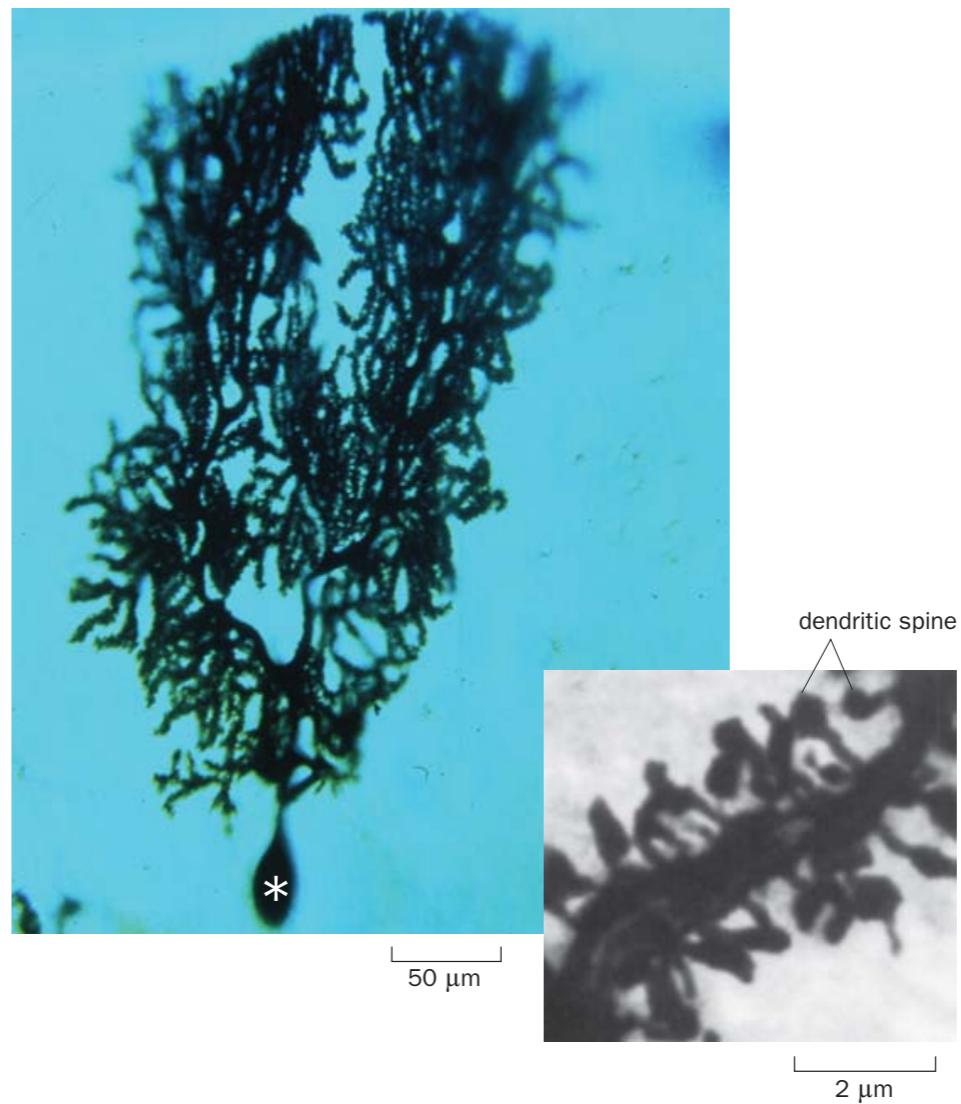


Camillo Golgi

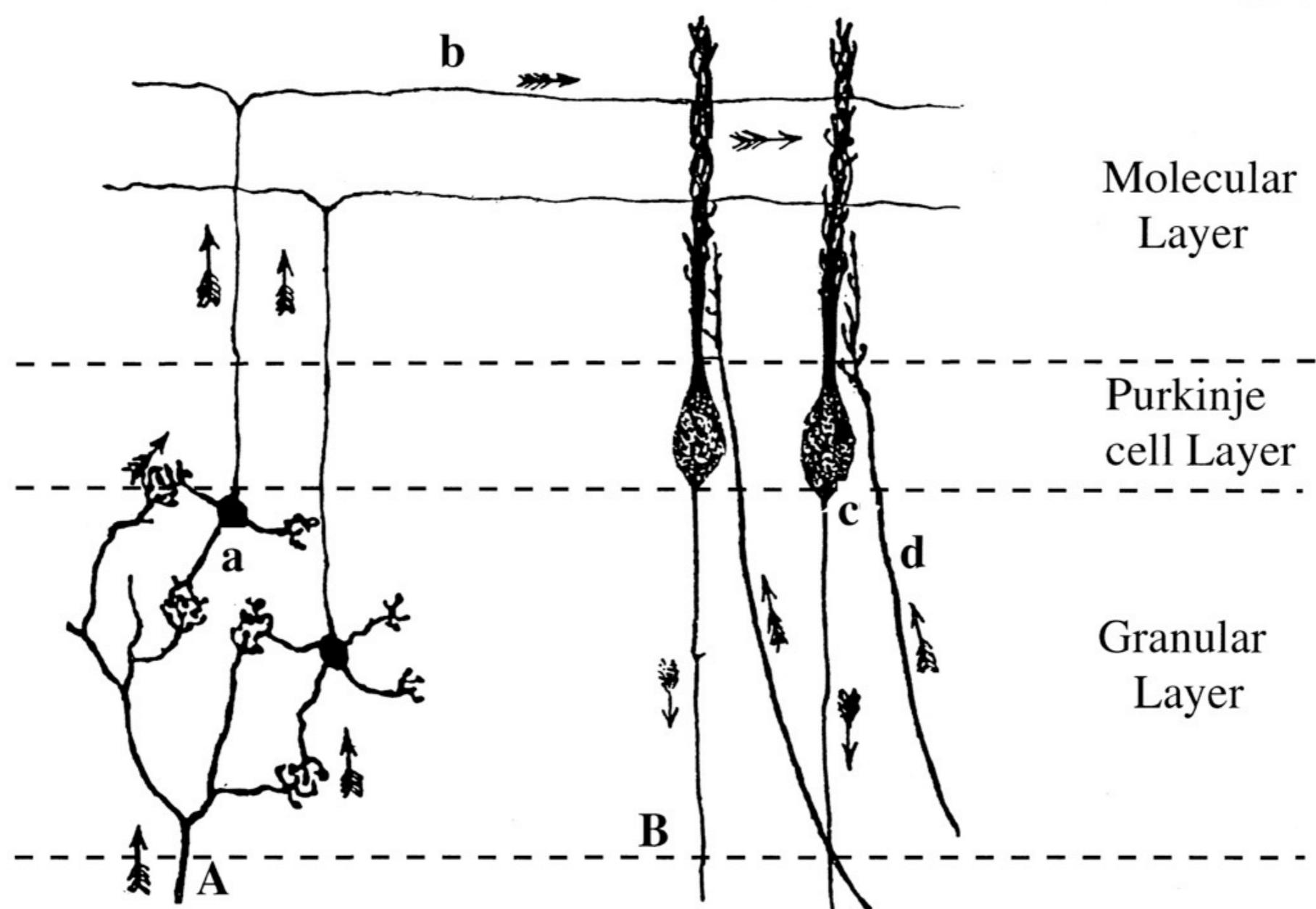
Golgi Staining method



Silver nitrate

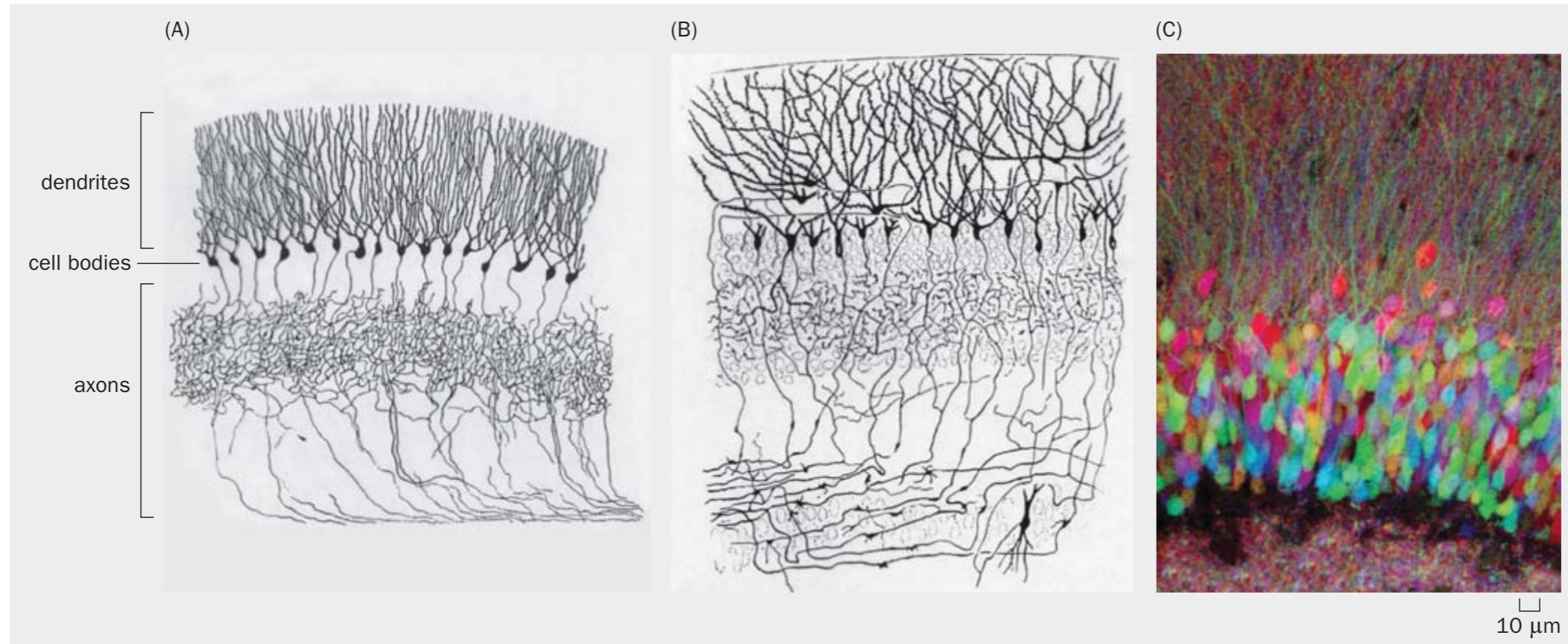


Cerebellar cortex



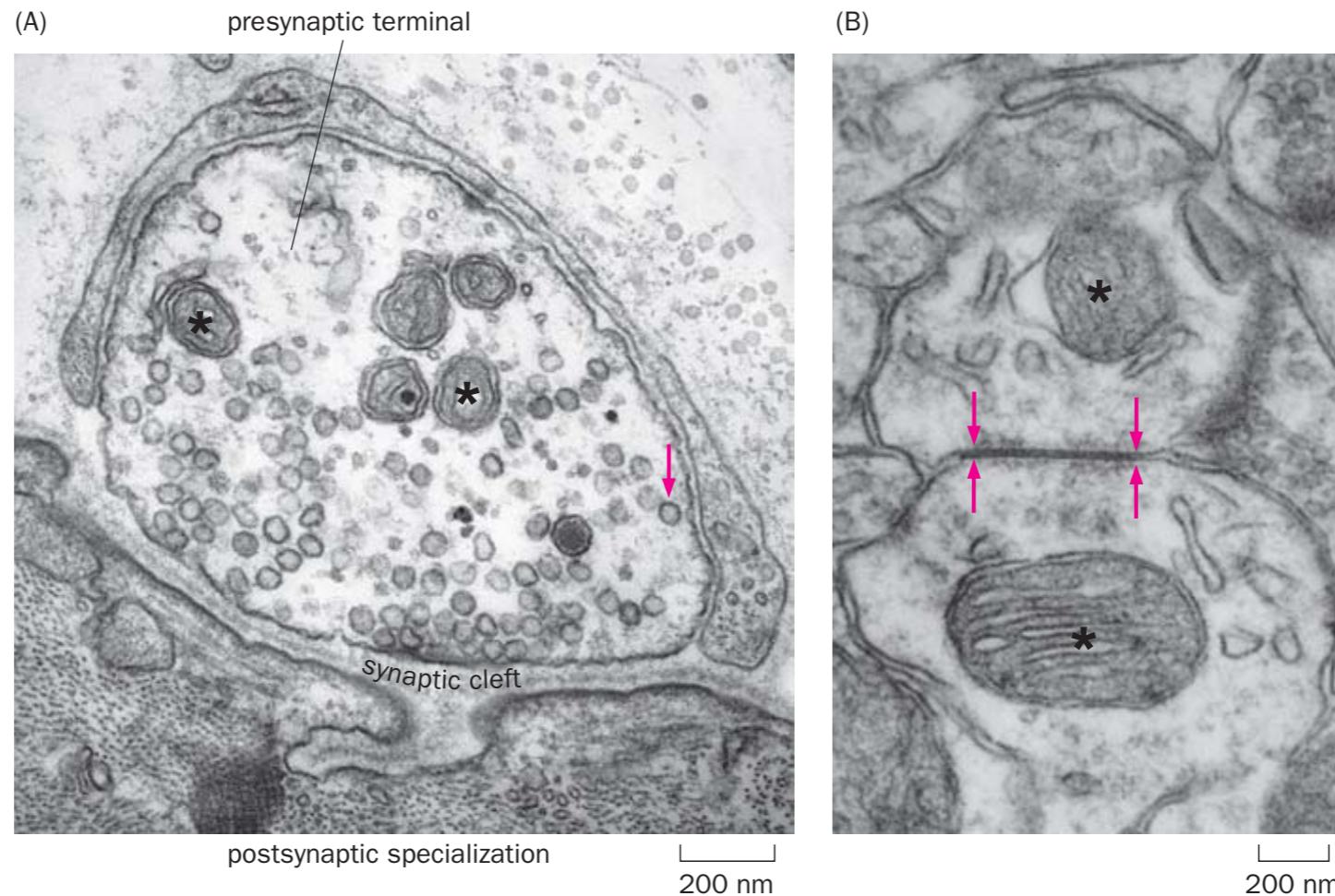
Cajal's drawing of the cerebellar cortex

Reticular Theory vs Neuron Doctrine



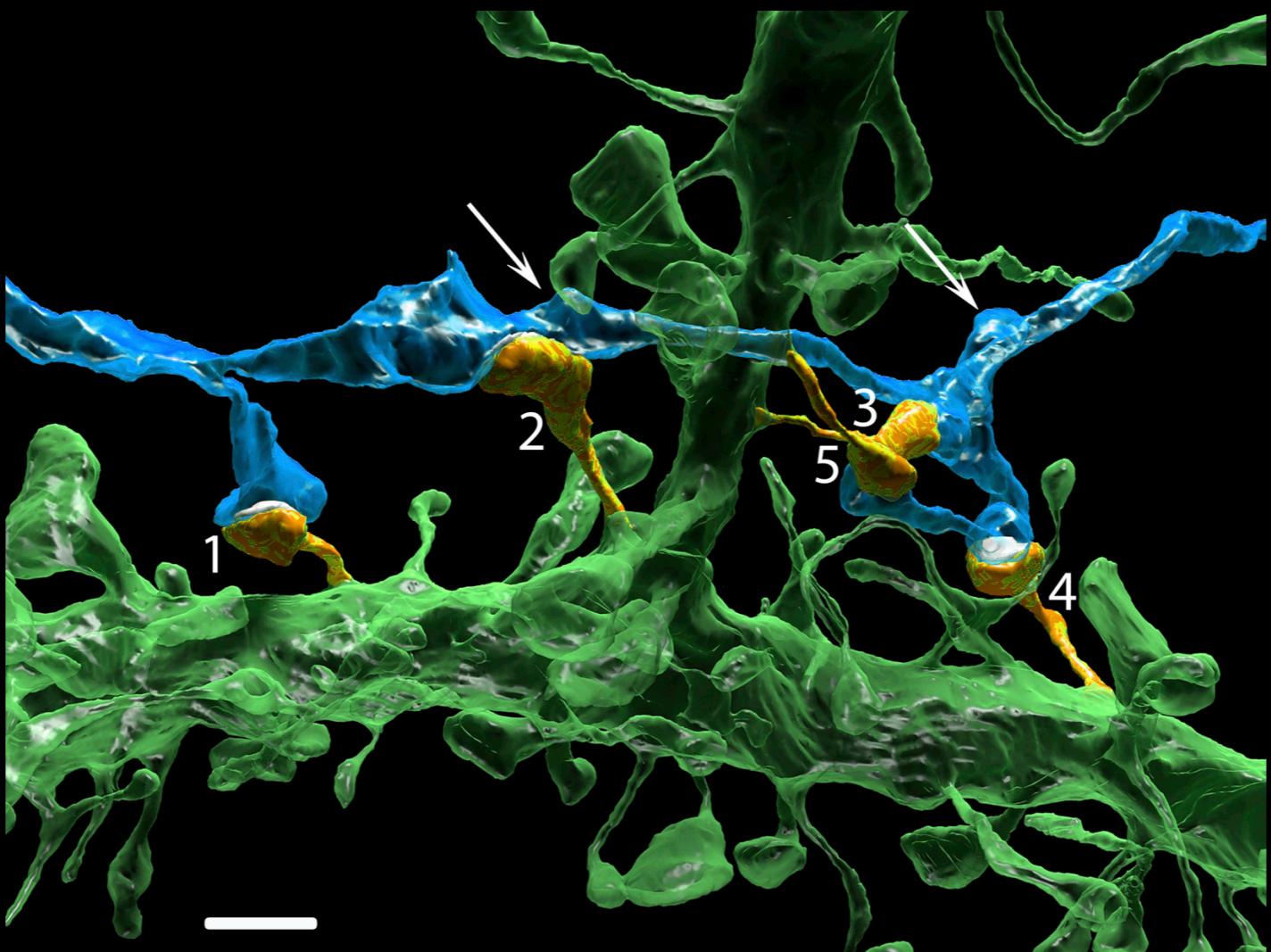
Synapse

How neurons communicate with each other?

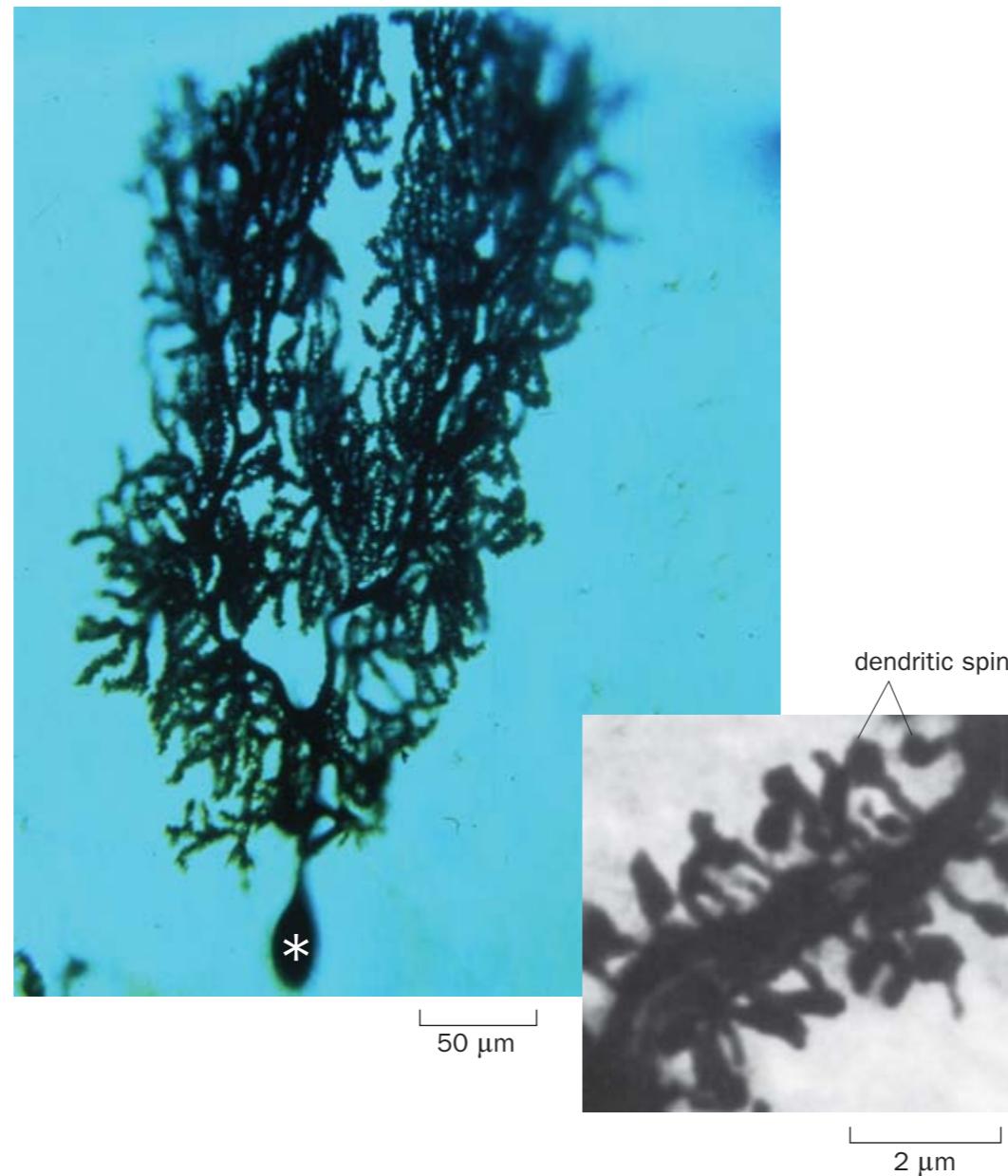


Chemical and electrical synapses

Synaptic Connectivity

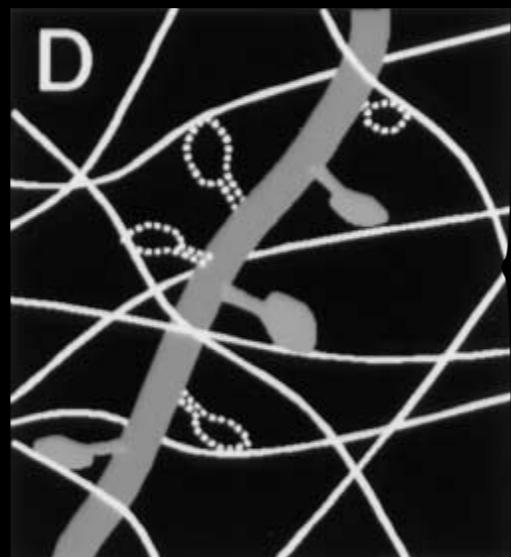
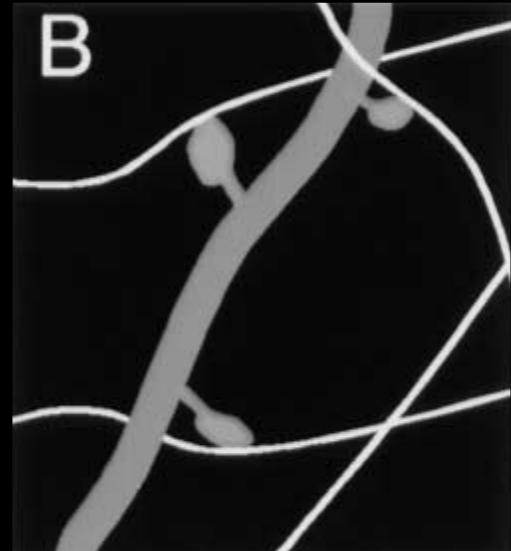
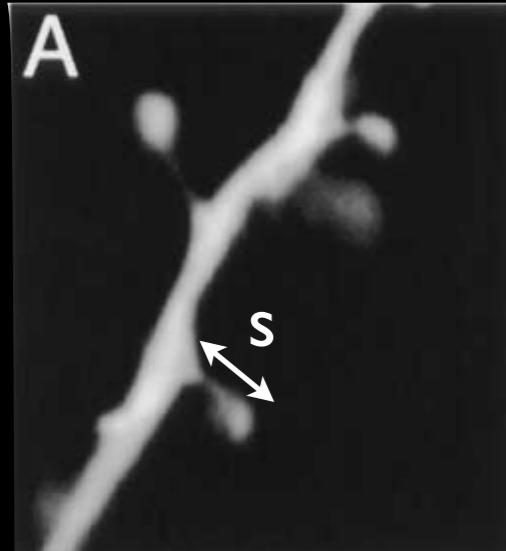


Kasthuri et. al, Cell 2015



Purkinjie cell in the cerebellum has the highest
spine density in the brain

Structural Plasticity of Synaptic Connectivity



$$f = \frac{2}{\pi s L_d b n}$$

s: spine length

L_d: total dendritic length per neuron

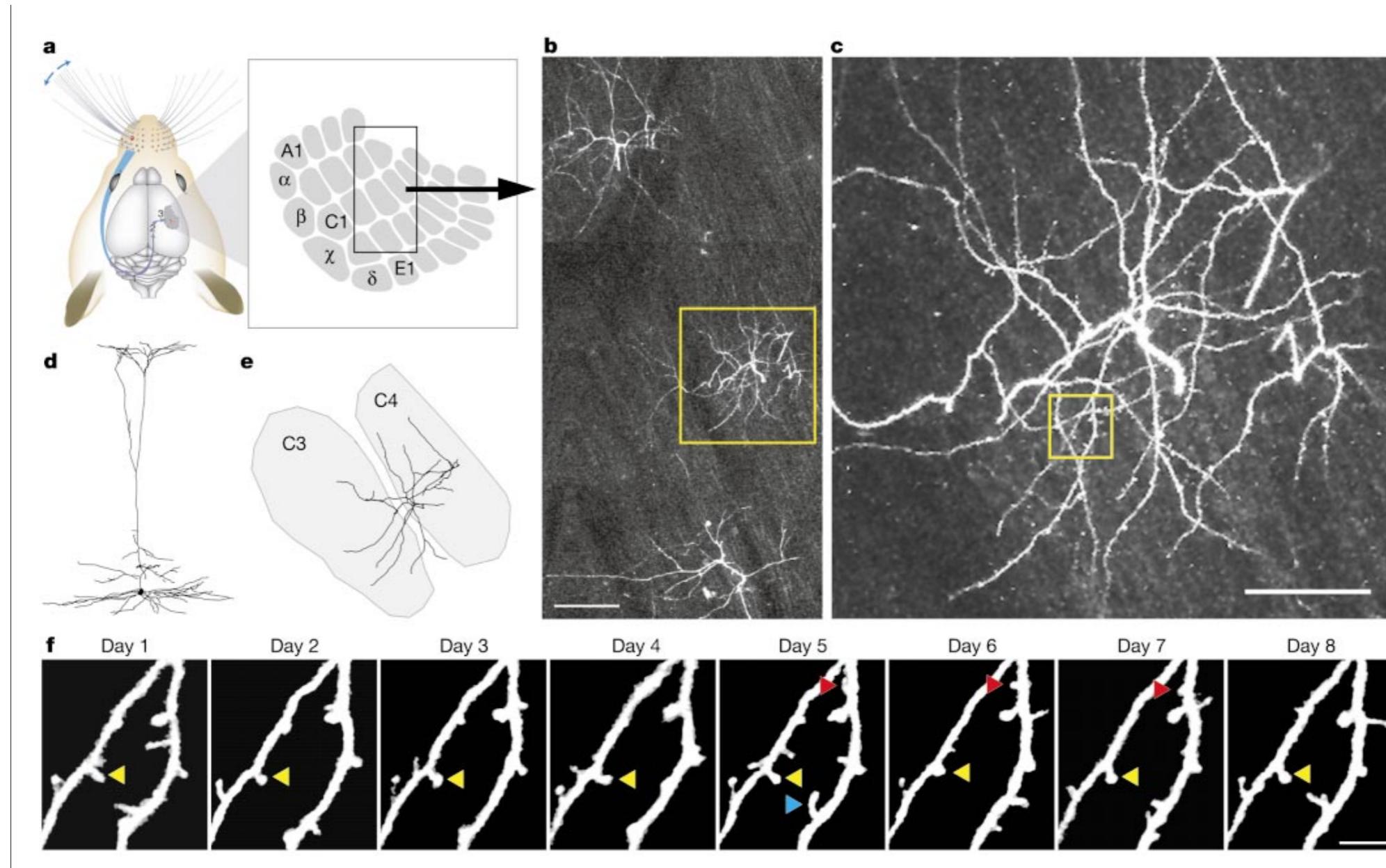
b: inter-bouton distance

n: neuronal density

filling fraction = 3/7

Stepanyants et. al., *Neuron* 2001

Structural Plasticity of Synaptic Connectivity



Trachtenberg et., al. *Nature* 2002

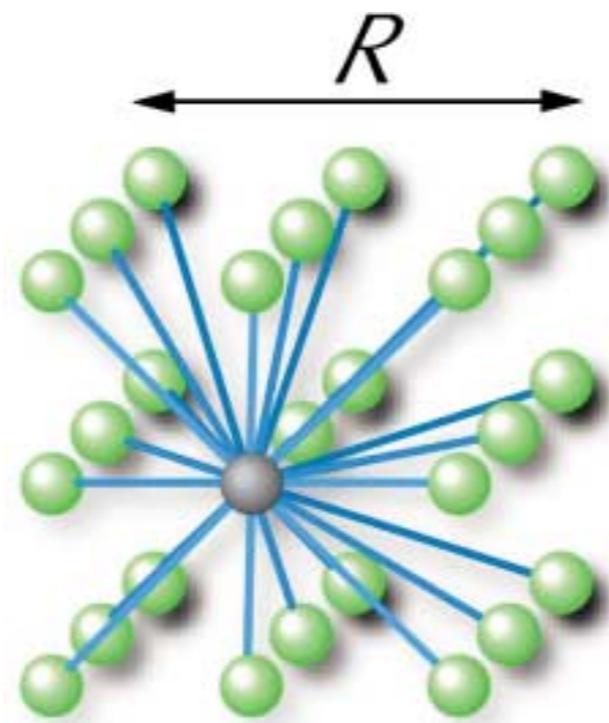
Why do we need axons and dendrites?

Wiring Optimization of Neural Circuit

“After the many shapes assumed by neurons, we are now in a position to ask whether this diversity ... has been left to chance and is insignificant, or whether it is tightly regulated and provides an advantage to the organism. ... we realized that all of the various conformations of the neuron and its various components are simply morphological adaptations governed by laws of conservation for time, space, and material.”

Ramon y Cajal

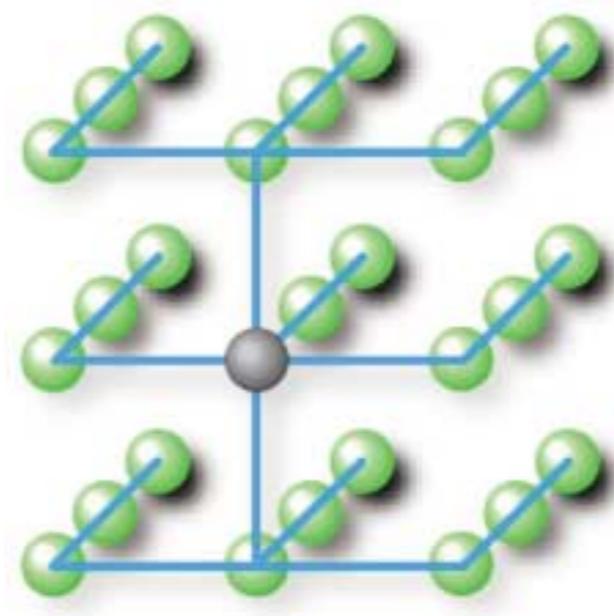
Why do we need axons and dendrites?



N : number of neurons
 d : process diameter
 R : network linear size

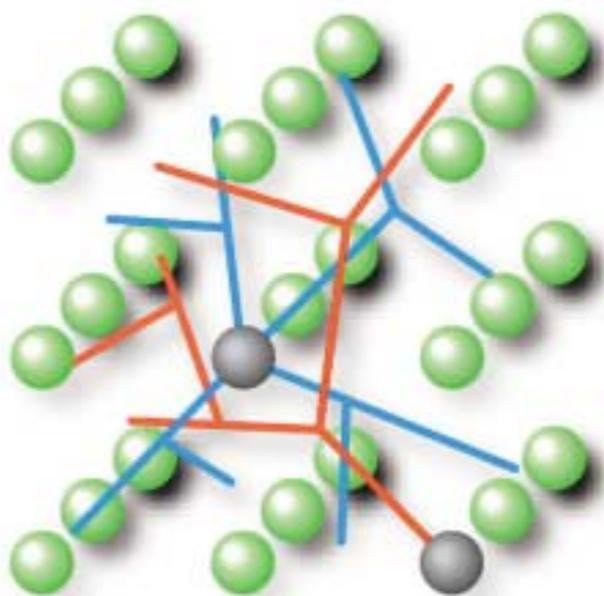
Design I

Why do we need axons and dendrites?



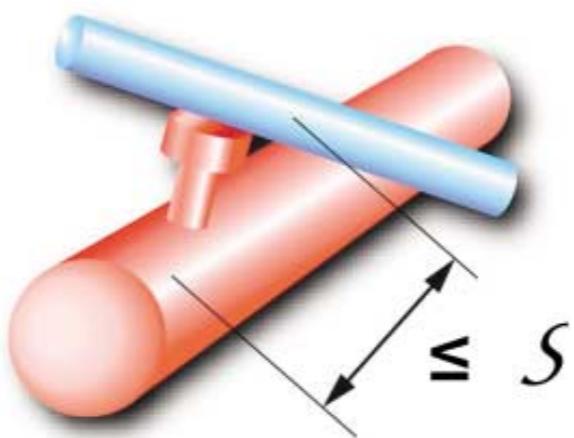
Design II

Why do we need axons and dendrites?



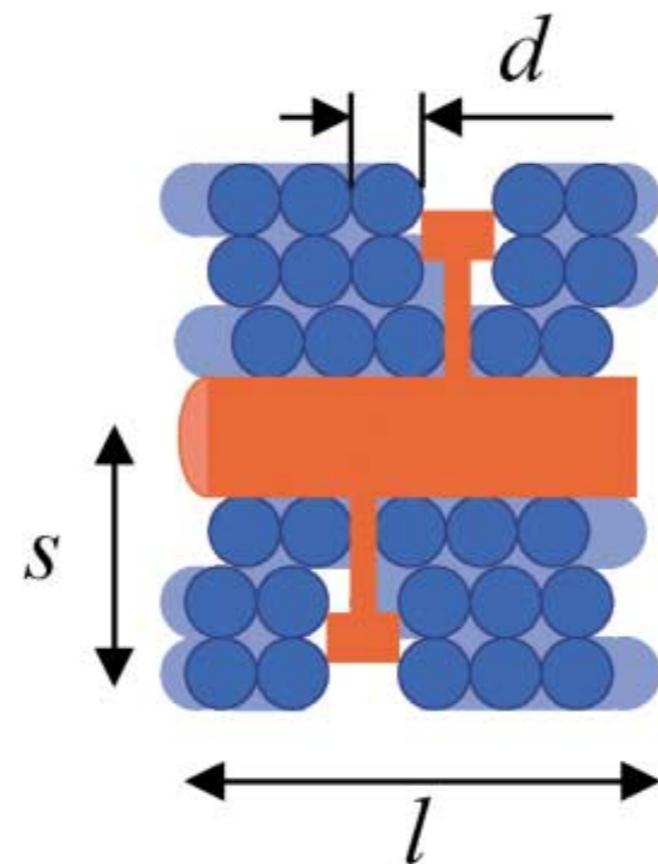
Design III

Why do we need axons and dendrites?



Design IV

Why do we need axons and dendrites?



The Optimality of the design

The cerebellar cortex

