# Genetic Analysis of RNA-Seq Data

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# 2 Genetic Analysis of a Metazoan Pathway using Transcriptomic Phenotypes Supplementary and Extended Material

# David Angeles-Albores, Carmie Puckett Robinson, Brian Williams, Igot Antoshechkin, and Paul W Sternberg

The purpose of this notebook is to serve as an extended, interactive document for our paper.

All code in this notebook was written, documented and generated by David Angeles-Albores. In cases when code was inspired, written or shown elsewhere first, links have been provided to the source material where possible.

100% of the data, with the exception of the raw reads, is deposited in our GitHub project. If you would like to verify our analysis, you are welcome to fork the project, although we will not allow pulls into the main branches. I hope you find this useful!

#### 3 Folder Structure

The folder structure is a little bit important if you want to replicate the findings presented here. Briefly, the folder structure is contained in the following major folders:

- input contains raw FASTQ files, kallisto\_all (processed reads), genmap file, TF list, cDNA file, transcripts.idx, enrichment dictionaries and hypoxia gold standard gene files
- sleuth contains differential analysis (no fog-2 included) results
- sleuth\_batch\_adjusted contains differential analysis results with fog-2 included
- src all python scripts
- output all figures
- tex manuscript
- experimental\_docs all bioanalyzer results are placed here

# 4 Read alignment and differential expression analysis

The raw FASTQ reads are in input/rawseq/PROJECT\_NAME/. These reads are processed by running **kallisto\_bash\_generator.py**, then from terminal (in the main directory) *chmod* +*x kallisto commands.sh*; *sh kallisto\_commands.sh*. Reads were processed using a length of **180**bp, with a standard deviation of **60** basepairs, bootstrapped 200 times. The results from this analysis are then placed in input/kallisto\_all/PROJECT\_NAME/.

Sleuth analysis was performed by running diff\_exp\_analyzer.R in the sleuth\_adjusted\_all folder. This will perform the differential expression analysis. The results are stored within the sleuth\_adjusted/results/ folder.

### 4.1 Details of Differential Analysis

We used a Generalized Linear Model to simultaneously estimate batch effects and the effects of varying mutations relative to a wild-type genome. Therefore, the model we used can be written:

$$\log(y_{i,j,k}) = \beta_{0,i} + \beta_{\text{batch},i} * Y_{k,i} + \beta_{\text{genotype},i} * X_{j,i}$$
(1)

Where  $Y_{k,i}$  and  $X_{j,i}$  are indicator variables for batch and genotype respectively.

# 5 Introduction: Genetic Analysis Using Global Expression Measurements

The following sections will provide (excruciating) detail on how we performed the genetic analysis of our mutants using this data. Initially, this analysis was done blindly. For clarity, I have added all the genotype identifiers from the beginning.

To start, we should load all the python libraries that we will need:

```
In [1]: # important stuff:
        import os
        import pandas as pd
        import numpy as np
        from IPython.core.display import HTML
        # stats
        import sklearn.decomposition
        from scipy import stats as sts
        from sklearn.cluster import AgglomerativeClustering
        from scipy.cluster import hierarchy
        import statsmodels.api as sm
        # TEA and morgan
        import tissue_enrichment_analysis as tea
        import morgan as morgan
        # network graphics
        import networkx as nx
        # Graphics
        import matplotlib as mpl
        import matplotlib.ticker as plticker
        import matplotlib.pyplot as plt
        import seaborn as sns
        import matplotlib.patheffects as path_effects
        from matplotlib import rc
        rc('text', usetex=True)
        # bokeh
        import bokeh.charts
```

```
import bokeh.charts.utils
import bokeh.io
import bokeh.models
import bokeh.palettes
import bokeh.plotting
from bokeh.plotting import figure
from bokeh.resources import CDN
from bokeh.embed import file_html
# bayes and mcmc
import pymc3 as pm
import theano
# Display graphics in this notebook
bokeh.io.output_notebook()
# Magic function to make matplotlib inline;
# other style specs must come AFTER
%matplotlib inline
# This enables SVG graphics inline.
# There is a bug, so uncomment if it works.
%config InlineBackend.figure_formats = {'png', 'retina'}
# JB's favorite Seaborn settings for notebooks
rc = {'lines.linewidth': 2,
      'axes.labelsize': 18,
      'axes.titlesize': 18,
      'axes.facecolor': 'DFDFE5'}
sns.set_context('notebook', rc=rc)
sns.set_style("dark")
ft = 35 \#title fontsize
import genpy
```

Next, I need to load the **phenotype\_df** (please don't use this file without permission for publication purposes. This tool is unpublished [I am actively working on a paper with this] and will be available soon. I provide it here for clarity, even though it was not part of our paper), the **tissue\_df** and the **tf\_df**. These files contains a phenotype-gene dictionary, a tissue-gene dictionary (downloaded from TEA) and a transcription factor list (from Chris Grove).

Additionally, I will initialize several variables whose purpose will mainly be to prettify the tables and substitute in the correct names.

```
hypoxia_gold = pd.read_csv('.../input/hypoxia_gold_standard.csv',
                            sep=',')
genotype_mapping = {'a': r'\emph{egl-9; vhl-1}',
                    'f': r'\emph{eql-9; hif-1}',
                     'b': r'\emph{eql-9}',
                     'c': r'\emph{hif-1}',
                     'd': r'\emph{vhl-1}',
                     'e': r'\emph{rhy-1}',
                     'g': r'\emph{fog-2}'
                     }
sort_pairs = {'eb': 1, 'be': 1,
              'ed': 2, 'de': 2,
              'ec': 3,'ce': 3,
              'eq': 4, 'ge': 4,
              'bd': 5, 'db': 5,
              'cb': 6, 'bc': 6,
              'bg': 7, 'gb': 7,
              'cd': 8,'dc': 8,
              'dq': 9, 'qd': 9,
              'cq': 10,'qc': 10
decode_pairs = {'eb': '\emph{rhy-1}, \emph{egl-9}',
                 'be': '\emph{rhy-1}, \emph{eql-9}',
                 'ed': '\emph{rhy-1}, \emph{vhl-1}',
                 'de': '\emph{rhy-1}, \emph{vhl-1}',
                 'ec': '\emph{rhy-1}, \emph{hif-1}',
                 'ce': '\emph{rhy-1}, \emph{hif-1}',
                 'eg': '\emph{rhy-1}, \emph{fog-2}',
                 'ge': '\emph{rhy-1}, \emph{fog-2}',
                 'bd': '\emph{egl-9}, \emph{vhl-1}',
                 'db': '\emph{egl-9}, \emph{vhl-1}',
                 'cb': '\emph{eql-9}, \emph{hif-1}',
                 'bc': '\emph{egl-9}, \emph{hif-1}',
                 'bg': '\emph{eql-9}, \emph{foq-2}',
                 'gb': '\emph{egl-9}, \emph{fog-2}',
                 'cd': '\emph{vhl-1}, \emph{hif-1}',
                 'dc': '\emph{vhl-1}, \emph{hif-1}',
                 'dg': '\emph{vhl-1}, \emph{fog-2}',
                 'qd': '\emph{vhl-1}, \emph{foq-2}',
                 'cg': '\emph{hif-1}, \emph{fog-2}',
                 'gc': '\emph{hif-1}, \emph{fog-2}'
```

Next, we will load up all of our files. These files will be placed within a class called morgan.hunt (funny!). All of the classes that are referenced in this tutorial are in the file morgan.py,

which you are welcome to use for your own analysis. The classes are relatively well-documented and should be usable if you are careful. That said, I am not a computer scientist, so some pathologies or bugs may pop up – if they do, please perform a pull-request on our github with a fix for the bug. Alternatively, please email me a sufficiently detailed script so I can reconstruct the failure event and correct the bug.

```
In [3]: # Specify the genotypes to refer to:
        single_mutants = ['b', 'c', 'd', 'e', 'g']
        # Specify which genotypes are double mutants
        # and of what single mutants:
        double_mutants = {'a' : 'bd', 'f':'bc'}
        # initialize the morgan.hunt object:
        # target_id is the column with isoform specific names
        # b is the name of the column with the GLM regression coefficients
        # tpm is the name of the column with the TPM numbers
        # qval is the name of the column with the FDR corrected q-values
        thomas = morgan.hunt('target_id', 'b', 'tpm', 'qval')
        # input the genmap file:
        thomas.add_genmap('../input/library_genotype_mapping.txt', comment='#')
        # add the names of the single mutants
        thomas.add_single_mutant(single_mutants)
        # add the names of the double mutants
        thomas.add double mutants(['a', 'f'], ['bd', 'bc'])
        # set the q-value threshold for significance to its default value, 0.1
        thomas.set_qval()
        # Add the tpm files:
        kallisto_loc = '../input/kallisto_all/'
        thomas.add_tpm(kallisto_loc, '/kallisto/abundance.tsv', '')
        # Make all possible combinations of WT, X
        combs = {}
        for gene in thomas.genmap.genotype.unique():
            if gene != 'wt':
                combs[gene] = 'WT '+gene+'/'
        # # load all the beta values for each genotype:
        # sleuth loc = '../sleuth/'
        # thomas.add_betas(sleuth_loc, 'betas.csv', combs)
        # load all the beta values for each genotype:
        sleuth_loc = '../sleuth_all_adjusted/kallisto/'
        for file in os.listdir("../sleuth_all_adjusted/kallisto"):
```

```
if file[:4] == 'beta':
    letter = file[-5:-4].lower()
    thomas.add_beta(sleuth_loc + file, letter)
    thomas.beta[letter].sort_values('target_id', inplace=True)
    thomas.beta[letter].reset_index(inplace=True)
```

Next, I will filter the data, removing any genes that don't show up in all the files and removing the bottom 10% of the genes by expression level. This is an aggressive cutoff, I know.

```
In [4]: thomas.filter_data(0, 0.1)
Number of na genes: 232
```

### 6 Figure 1. Dendrogram Clustering

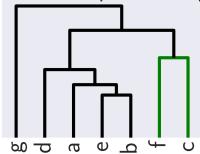
Having performed the above analysis, let's go ahead and make the (almost finished) dendrogram figure in the paper. The only post-processing this will undergo is manually changing the letters to gene names and removing some of the labels for clarity.

```
In [5]: # find the set of all genes that are DE in any category
        max_overlap = np.array([])
        for df in thomas.beta_filtered.values():
            ind = df.qval < thomas.q</pre>
            if len(max_overlap) == 0:
                max_overlap = df[ind].target_id.values
            else:
                max_overlap = np.concatenate((max_overlap,
                                df[ind].target_id.values))
        max_overlap = max_overlap.tolist()
        max_overlap = list(set(max_overlap))
        print(len(max_overlap))
       bvals = np.array([])
        for df in thomas.beta_filtered.values():
            temp = df[df.target_id.isin(max_overlap)].b.values
            temp = (temp - temp.mean())/temp.std()
            if len(bvals) == 0:
                bvals = temp
            else:
                bvals = np.vstack((bvals, temp))
        # Perform agglomerative clustering
        sklearn_pca, n = genpy.pca(bvals)
        model = hierarchy.linkage(sklearn_pca.transform(bvals), 'ward')
        # extract the labels:
        labels = list(thomas.beta filtered.keys())
```

```
for i, label in enumerate(labels):
            if label in double mutants:
                labels[i] = double mutants[label]
        # Linewidth parameter, temporarily set to 7
        plt.rcParams['lines.linewidth'] = 7
        # set colors (black; blue)
        hierarchy.set_link_color_palette(['k', 'g', 'b'])
        # draw the dendrogram
        hierarchy.dendrogram(
            model,
            truncate_mode='level', # show only the last p merged clusters
            labels=list(thomas.beta_filtered.keys()),
            p=21, # show only the last p merged clusters
            show_leaf_counts=False, # otherwise numbers in brackets are counts
            leaf rotation=90.,
            leaf font size=12.,
            show_contracted=True,
            above threshold color='k'
        )
        # get the current axis
        ax = plt.gca()
        # add in the orange and green boxes
        height = ax.get_ylim()[1]*.36
        plt.xticks(fontsize=55)
        plt.gca().yaxis.set_major_locator(plt.NullLocator())
        title = 'Clustering by Expression Recapitulates Epistatic Interactions'
        plt.title(title, fontsize=ft*1.5)
        plt.savefig('../output/tpm dendrogram.pdf', bbox inches='tight')
        # return linewidth to a reasonable setting
        plt.rcParams['lines.linewidth'] = 2
4674
The first 2 principal components explain >=90% of the data
```

# rename the double mutant labels (i.e. instead of 'a' --> 'bd')

Clustering by Expression Recapitulates Epistatic Interactions



### 7 Bayesian versus Spearman Regressions

Ok! Having verified that we still have plenty of power to identify these mutants, we need to go ahead and perform some statistics. Next, I will define some useful functions to make plotting easier. After that, I will begin a detailed analysis of the different prediction methods, specifically attempting to compare Spearman rank regression with a Bayesian linear regression of ranked data.

```
In [51]: def pathify(title, xlabel, ylabel, xticks=True, yticks=True, **kwargs):
             A function to pathify the labels, titles and ticks in a plot.
             labelsize = kwargs.pop('labelsize', 20)
             titlesize = kwargs.pop('titlesize', 25)
             # make the labels and title into paths
             effect = [path_effects.Normal()]
             plt.ylabel(ylabel,
                        fontsize=labelsize).set_path_effects(effect)
             plt.xlabel(xlabel,
                        fontsize=labelsize).set_path_effects(effect)
             plt.title(title,
                       fontsize=titlesize).set_path_effects(effect)
             ax = plt.qca()
             # go through each xtick or ytick and make
             # it a path if user specified to do so.
             if xticks == True:
                 for i, label in enumerate(ax.get_xticklabels()):
                     ax.get_xticklabels()[i].set_path_effects(effect)
             if yticks == True:
                 for i, label in enumerate(ax.get_yticklabels()):
                     ax.get_yticklabels()[i].set_path_effects(effect)
```

### 7.1 Spearman Regression Method

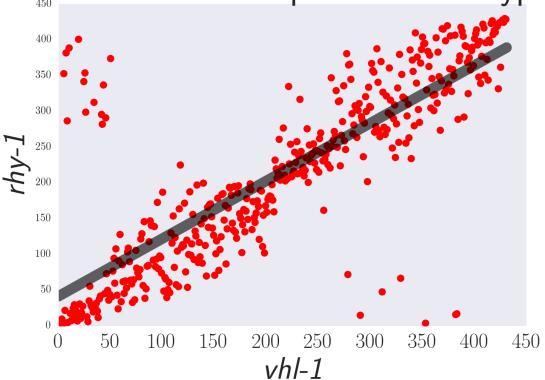
In order to perform the Spearman regression, this is what I will do:

- Extract the pertinent datasets for the two genotypes I want to convert.
- Find the genes that are altered between both conditions, regardless of direction
- After finding this overlap, rank the genes by their  $\beta$  coefficient in each dataset
- Perform Least Squares on the ranked data, which is the Spearman Regression
- Plot the results

```
In [7]: # lambda index function:
        lind = lambda x: (x.qval < 0.1)
        # As an example, let me show you what a
        # good spearman correlation looks like:
        # name of the column that contains the
        # isoform names:
        genes = 'target_id'
        # the genotypes to compare
        letters = ['d', 'e']
        # extract the dataframes from the morgan.hunt object
        x = thomas.beta_filtered[letters[0]]
        y = thomas.beta_filtered[letters[1]]
        # boolean logic to find the stat. sig. diff.
        # genes that appear in both x and y
        ovx = x[lind(x)]
        ovy = y[lind(y) \& y[genes].isin(ovx[genes])].copy()
        ovx = x[lind(x) & x[genes].isin(ovy[genes])].copy()
        # a function to rank order the data
        def find rank(df):
            """A function to find the rank values of a variable."""
            # make a copy of the dataframe, then sort it inplace
            d = df.copy()
            d.sort_values('b', inplace=True)
            # make a rank vector and append it to the sorted dataframe
            rank = np.linspace(0, len(d)-1, len(d))
            d['r'] = rank
            # sort by isoform name again and return the modified df
            d.sort_values('target_id', inplace=True)
            return d
        # apply said function
        ovx = find_rank(ovx)
        ovy = find_rank(ovy)
```

```
# calculate a linear regression on ranked data,
# which is equivalent to Spearman Ranked Regression
slope, intercept, r_value, p_value, std_err = sts.linregress(ovx.r,ovy.r)
# We make two vectors in order to draw the best fit line on a plot
X = np.linspace(0, len(ovx.r))
Y = slope*X + intercept
# Plot the genes that are significantly altered in both X and Y
plt.plot(ovx.r, ovy.r, 'ro',
         alpha=1, label='Overlapped Diff. Exp. Genes')
# Plot the best fit line
plt.plot(X, Y, k-1, alpha=0.6,
         lw=10, label= 'Best Fit')
# prettify the plot
plt.title('Linear Pathways Share a\nCommon Transcriptomic Phenotype',
          fontsize=ft).\
            set_path_effects([path_effects.Normal()])
plt.xlabel(genotype_mapping[letters[0]],
           fontsize=30).set_path_effects([path_effects.Normal()])
plt.ylabel(genotype_mapping[letters[1]],
           fontsize=30).set_path_effects([path_effects.Normal()])
plt.xticks(fontsize=20)
plt.savefig('../output/spearmanr_b_and_c.pdf')
```





Spearman R predicts a trend, but the best fit we found doesn't agree with the one I would predict with my eye. We can probably do better if we use a Bayesian regression that minimizes least squares but using a Student-T distribution, NOT a Gaussian.

### 7.2 Bayesian Robust Regression

In order to perform the Spearman regression, this is what I will do:

- Extract the pertinent datasets for the two genotypes I want to convert.
- Find the genes that are altered between both conditions, regardless of direction
- After finding this overlap, rank the genes by their  $\beta$  coefficient in each dataset
- Perform Least Squares on the ranked data, but use a Student-T instead of a Gaussian prior.
- The regression in this case is sampled using a full Monte Carlo Simulation.
- Identify outliers to this regression, and run a second regression on outliers to see if there are complex regulatory relationships between these genes.
- Plot the results

In other words, given ranked data, I will find the line that is likeliest to explain the data by finding:

$$P(D|\mu,\sigma) \propto \prod_{i} \text{StudentT}(D_i(x) - \mu(x), \sigma)$$
 (2)

The Student-T distribution has considerably heavier tails than a Gaussian distribution, so it will not consider the evidence provided by outliers as informative as a Gaussian would.

In order to perform this simulation, we will use the **pymc3** package to specify the model. This model was inspired and successfully deployed thanks to Thomas Wiecki; specifically thanks to this blog entry by him. Thanks Tom!

#### 7.3 Figure 4. Complex Regulation Generates Detectable Patterns in Transcriptomes

The code that we will run below was used to generate the bottom panel of figure 4 in our paper. The figure as is output here was only subjected to very minor aesthetic modifications postgeneration (such as moving the title a little above where it appears here).

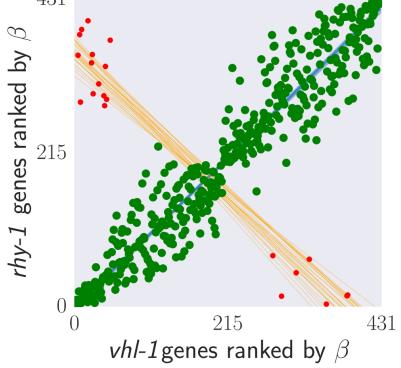
```
In [8]: def robust_regress(data):
            """A robust regression using a StudentT distribution instead of a Gauss
            with pm.Model() as model_robust:
                # set the model. pymc is nice because
                # it will automatically choose
                # appropriate priors for us once we
                # specify our likelihood is StudentT
                family = pm.glm.families.StudentT()
                # specify we want a generalized linear
                # model with a Student T distribution
                pm.glm.glm('y \sim x', data, family=family)
                # find the MAP as a good starting point
                start = pm.find_MAP()
                # do the simulation and return the results
                step = pm.NUTS(scaling=start)
                trace_robust = pm.sample(2000, step, progressbar=True)
                return trace_robust
In [9]: # Take the data from the Spearman example and put it
        # into a dictionary to feed into the robust regression
        data = dict(x=ovx.r, y=ovy.r)
        x = np.linspace(ovx.r.min(), ovx.r.max())
        # perform the simulation
        trace_robust = robust_regress(data)
        # draw a figure
        plt.figure(figsize=(5, 5))
        # some statistics.
        \# normalize everything so that all points are centered around 0
        # by taking the y-coordinates and subtracting
```

```
# the value of the model at the point we calculated
intercept = trace_robust.Intercept.mean()
slope = trace_robust.x.mean()
distribution = ovy.r - intercept - ovx.r*slope
# find the mean and stdev of the distribution
# (even though mean should be 0 now)
mean = distribution.mean()
std = distribution.std()
# find inliers and outliers (see text description below)
def find_inliers(distribution, mean, trace):
    """A function to identify inliers and outliers in a distribution"""
    # find the outliers:
    sel = np.abs(distribution - mean)/(trace_robust.x.std()
                 + trace_robust.Intercept.std()+ std) < 1.5
    # get the outliers and inliers
   distribution_inliers = distribution[sel]
    distribution_outliers = distribution[~sel]
    # get the gene names of the outliers
    inverse = distribution outliers + \
                          intercept + ovx.r*slope
    outliers = ovy[ovy.r.isin(inverse)].target id
    return distribution_inliers, distribution_outliers, outliers
# call the function
results = find_inliers(distribution, mean, trace_robust)
distribution_inliers, distribution_outliers, outliers = results
# run a secondary regression on the outliers
data2 = dict(x=ovx[ovx.target_id.isin(outliers)].r,
             y=ovy[ovy.target_id.isin(outliers)].r)
# run the second trace
trace robust2 = robust regress(data2)
# get the y-coordinate of the inliers and outliers
yri = distribution_inliers + intercept + ovx.r*slope
yro = distribution_outliers + intercept + ovx.r*slope
# plot the regression lines
label = 'posterior predictive regression lines'
pm.glm.plot_posterior_predictive(trace_robust, eval=x,
                                 label=label,
                                 color='#357EC7')
pm.glm.plot_posterior_predictive(trace_robust2, eval=x,
                                 label=label,
```

```
# plot the data. Inliers are plotted as
       #large green dots, outliers as small red dots
       plt.plot(ovx.r, yri, 'go', ms = 7.5, alpha=0.7)
       plt.plot(ovx[yro > 0].r, yro[yro > 0], 'ro', ms = 5)
       # prettify plot
       plt.xlim(0, len(ovx))
       plt.ylim(0, len(ovy))
       plt.yticks([0, np.floor(len(ovx)/2), len(ovx)], fontsize=20)
       plt.xticks([0, np.floor(len(ovx)/2), len(ovx)], fontsize=20)
       pathify('Transcriptome Reflects Multiple Interaction Modes',
              genotype_mapping[letters[0]] + r'genes ranked by $\beta$',
              genotype_mapping[letters[1]] + r' genes ranked by $\beta$',
              labelsize=24)
       comp = letters[0] + letters[1]
       plt.savefig('../output/multiple_modes_{0}.pdf'.format(comp)
Applied log-transform to lam and added transformed lam_log_ to model.
 [-----] 2000 of 2000 complete in 1.5 secApplied
 [-----] 2000 of 2000 complete in 2.0 sec
```

color='#FFA500')

# Transcriptome Reflects Multiple Interaction Modes



There, much better! Penalizing outliers allows us to estimate the primary regression slope really well (blue lines). Here, each blue line is the result of a simulation, and we can see that they are all clustered together. Having estimated the first regression, we can proceed to identify outliers.

Now, there are multiple ways to identify outliers, and this is the point where I am going to cheat just a little bit. If we pretend that the model is gaussian (it isn't), then we can identify outliers (fairly aggressively) via the following method. Thus, if

$$z(i) = \frac{D_i(x) - \mu(x)}{\sigma_{\mu} + \sigma_{\text{Intercept}} + \sigma_{\text{Data}}} > 1$$
(3)

then z(i) is an outlier.

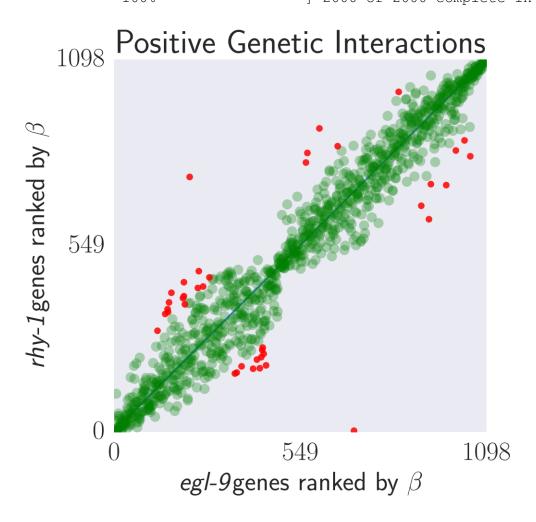
After identifying these outliers, I can then pool them and run a second regression on them (orange lines). These lines are also quite clustered, and the slope is practically 1! Wow!

# 7.4 Figure 2. Positive Regulatory Relationships Can Be Identified By Transcriptomic Correlation

In the above example, we saw that *rhy-1* and *hif-1* share a complex regulatory relationship as exhibited by the cross-pattern. However, an important point is whether or not this cross pattern appears in all datasets. While we cannot generalize yet (this kind of analysis is very new) we should definitely make sure that not all of our genes are exhibiting this cross pattern. Below, I show some a pair of genes that don't exhibit a cross pattern.

```
In [10]: genes = 'target_id'
         letters = ['b', 'e']
         # datasets
         x = thomas.beta_filtered[letters[0]]
         y = thomas.beta_filtered[letters[1]]
         # overlap
         ovx = x[lind(x)]
         ovy = y[lind(y) & y[genes].isin(ovx[genes])].copy()
         ovx = x[lind(x) & x[genes].isin(ovy[genes])].copy()
         # find rank
         ovx = find_rank(ovx)
         ovy = find_rank(ovy)
         # Take the data and place it
         # into a dictionary to feed into the robust regression
         data = dict(x=ovx.r, y=ovy.r)
         x = np.linspace(ovx.r.min(), ovx.r.max())
         # perform the simulation
         trace_robust = robust_regress(data)
```

```
# draw a figure
plt.figure(figsize=(5, 5))
# some statistics.
# normalize everything so that all points are centered around 0
# by taking the y-coordinates and subtracting
# the value of the model at the point we calculated
intercept = trace robust.Intercept.mean()
slope = trace_robust.x.mean()
distribution = ovy.r - intercept - ovx.r*slope
# find the mean and stdev of the distribution
# (even though mean should be 0 now)
mean = distribution.mean()
std = distribution.std()
# find inliers
results = find_inliers(distribution, mean, trace_robust)
distribution inliers, distribution outliers, outliers = results
# y-coordinate of outliers
yri = distribution_inliers + intercept + ovx.r*slope
yro = distribution_outliers + intercept + ovx.r*slope
# plot the regression lines
label = 'posterior predictive regression lines'
pm.glm.plot_posterior_predictive(trace_robust, eval=x,
                                 label=label,
                                 color='#357EC7')
pm.glm.plot_posterior_predictive(trace_robust2, eval=x,
                                 label=label,
                                 color='#FFA500')
# plot the data. Inliers are plotted as
#large green dots, outliers as small red dots
plt.plot(ovx.r, yri, 'go', ms = 7.5, alpha=0.7)
plt.plot(ovx[yro > 0].r, yro[yro > 0], 'ro', ms = 5)
# prettify plot
plt.xlim(0, len(ovx))
plt.ylim(0, len(ovy))
plt.yticks([0, np.floor(len(ovx)/2), len(ovx)], fontsize=20)
plt.xticks([0, np.floor(len(ovx)/2), len(ovx)], fontsize=20)
pathify('Transcriptome Reflects Multiple Interaction Modes',
        genotype_mapping[letters[0]] + r'genes ranked by $\beta$',
        genotype_mapping[letters[1]] + r' genes ranked by $\beta$',
        labelsize=24)
```



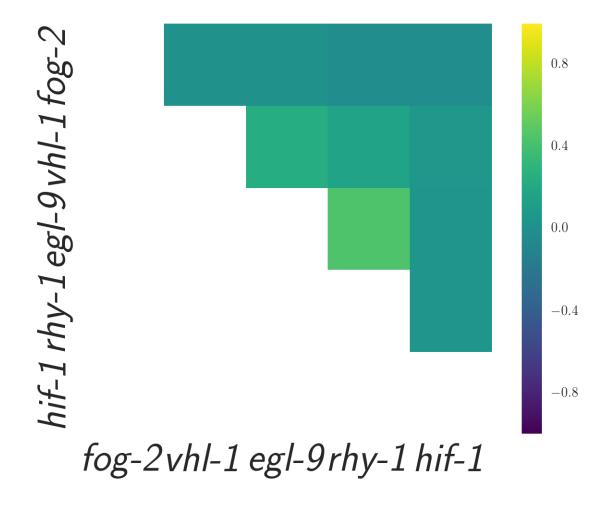
# 8 Pairwise Analysis of All Genes Using Spearman Correlation

Given what we found above, we know that the spearman analysis is good to use to get a rough fast idea of how our data looks. Let's go ahead and run the analysis for all pairwise comparisons that can be made using this dataset.

Spearman correlations and hypergeometric tests can be performed using the class morgan.brenner.

Once I calculate the quantities of interest, I will plot them on a heatmap. However, reader beware. Do NOT **EVER** use jet. The red and blue heatmaps? Awful. They have very serious pathologies that have been well described, and they generate patterns via optical illusions. Instead, we will use the *viridis* colormap, which was used by scientists in LIGO.

```
In [11]: # Define a 'genes' variable that will be used
         # for labelling every plot from here on out:
         genes = [genotype_mapping[x] for x in thomas.single_mutants]
         # Define a plotting function to plot only a triangular heat map
         def tri_plot(matrix, xlabels, ylabels=[]):
             """Given a matrix, draw a triangle plot."""
             # Minimum and maximum for colormap
             vmin= matrix.min().min()
             vmax= np.max(matrix).max()
             # if user didn't specify xlabels, assume ylabels
             # are the same as xlabels
             if len(ylabels) == 0:
                 ylabels = xlabels
             # make the lower triangle of the matrix,
             # since we are only dealing with
             # symmetric matrices. Also, remove the diagonal
             mask = np.zeros like(matrix)
             mask[np.tril_indices_from(mask)] = True
             # draw and adjust xtick size
             with sns.axes style("white"):
                 ax = sns.heatmap(matrix, xticklabels=xlabels
                                  yticklabels=ylabels, cmap='viridis',
                                  mask=mask, square=True, vmin=vmin,
                                  vmax=vmax)
             plt.xticks(fontsize=30)
             plt.yticks(fontsize=30)
         # Perform Correlation Analysis
         sydney = morgan.brenner('spearman', thomas)
         # Plot
         tri plot(sydney.rho.as matrix(columns=thomas.single mutants),
                  genes)
```



So maybe *egl-9* and *rhy-1* interact? Let's wait for the full Bayesian treatment.

# 9 Hypergeometric Analysis:

Another method to query whether there are interactions between genes is perform an urn test of enrichment. We ask: What is the probability that the DE genes in a gene B are the same as those in A? This probability should intuitively be 1 if A and B have exactly the same DE genes; it should be 0 (or close to) if they share no genes in common.

I approached this problem by assuming that the urn to be drawn from is exactly gene A in the above example. We define one of the two genes in the comparison to be the 'urn' (specifically, I always select the one which has more DE genes). Then, the question can be rephrased as follows: What is the probability that the DE genes in B were drawn from A? In other words, we want to calculate:

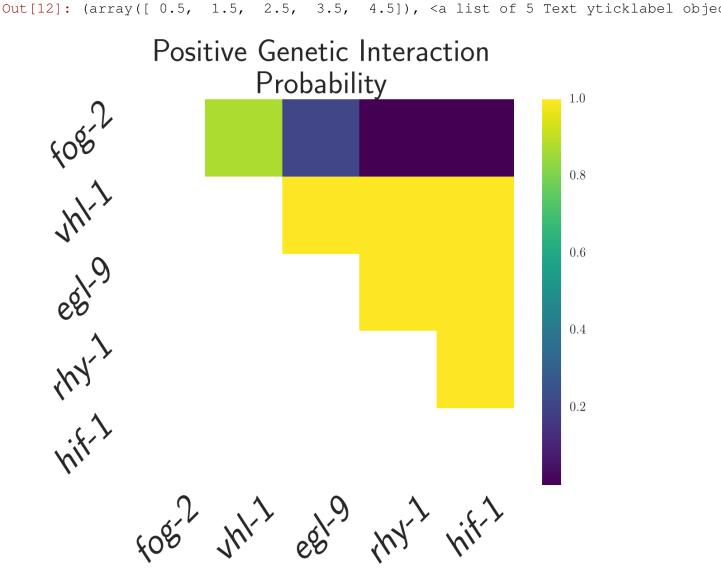
$$P(A \text{ and } B \text{ are in a pathway}|B,A) \propto P(A|B) = \text{Hypergeom}(A,B,A\cap B,\text{ genome})$$
 (4)

In reality this approach has an incredibly low threshold for activation. Biological networks are not random, and therefore my suspicion is that this test is biased towards positive results. This

would be the case particularly if networks are dense (everything interacts with everything). Part of the problem with the hypergeometric is that it saturates very rapidly, so the dynamic range is low. In effect, the answers become largely binary (....great for an SVM?). However, this means that we can't use the hypergeometric probabilities to gauge functional distance (these probabilities cannot be weighted intuitively).

```
In [12]: # Perform a test for positive interaction, put them in a matrix
    mat = sydney.hyper_plus.as_matrix(columns=thomas.single_mutants)
    genes = [genotype_mapping[x] for x in thomas.single_mutants]

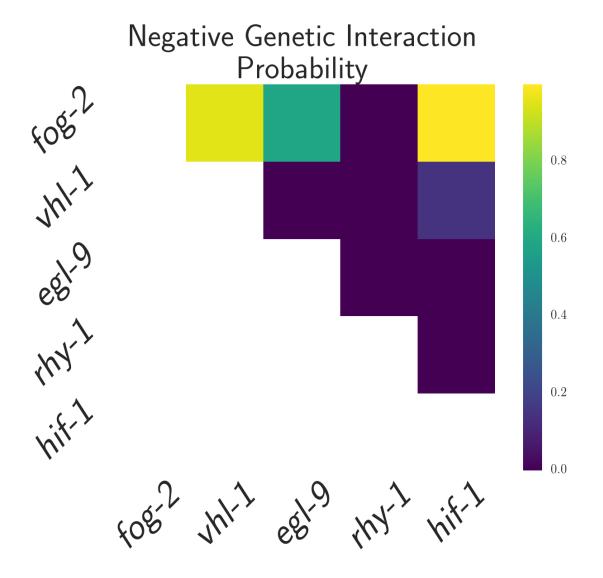
# plot the results
    tri_plot(mat, genes)
    pathify('Positive Genetic Interaction\nProbability', '', '')
    plt.xticks(rotation=45)
    plt.yticks(rotation=45)
```



*fog-*2 has a weak probability of interacting with any genes in this pathway. It would be most likely that *vhl-*1 and *fog-*2 share a positive interaction according to this diagram. Moreover, notice that all the hypoxia genes are predicted to interact; however, the saturation makes it hard to gauge exactly what kind of interaction is occurring.

#### 9.0.1 Probability of Negative Regulatory Interaction

Next, we can repeat our query, but we modify it slightly to ask about the possibility of a negative regulatory interaction:



```
\emph{vhl-1} \emph{egl-9} 15
\emph{rhy-1} \emph{fog-2} 255
\emph{hif-1} \emph{fog-2} 113
\emph{fog-2} \emph{rhy-1} 255
\emph{egl-9} \emph{hif-1} 39
\emph{fog-2} \emph{egl-9} 248
\emph{rhy-1} \emph{hif-1} 38
\emph{vhl-1} \emph{hif-1} 18
\emph{egl-9} \emph{rhy-1} 3
\emph{hif-1} \emph{rhy-1} 3
```

We see that this time *fog-2* has a real probability of negative interaction with the hypoxia pathway. Interesting.

Aside from that, there is a small probability (20%) that *hif-1* and *egl-9* are interacting in a negative manner. Incidentally, that is the **correct** mode of interaction, according to the canonical literature.

### 10 Analysis Using Robust Regression

What I do here is try to identify trends. Namely, for two genotypes X and Y, I fit a line using a Bayesian robust regression (see methods) thru the rank-ordered regression coefficients that are statistically significantly different from 0 and that are present in both X and Y. Next, I use this Bayesian framework to identify any and all outliers to the regression.

In order to test for alternative modes of interaction in this dataset, I take the outliers and I run the same regression again *on the outliers*. If this second interaction has an opposite sign to the first, then we predict that there are two modes of interaction, subject to the following caveats:

- Both the primary and secondary regressions yield strong correlations (>0.7)
- The first regression results in many outliers

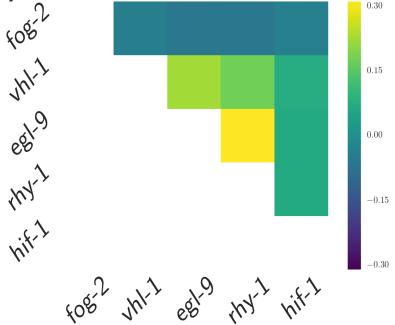
Finally, because of the approach I used, I can also predict which genes are under what mode of regulation. Super cool!

```
[-----] 2000 of 2000 complete in 1.7 sec
starting comparison of d, b
Applied log-transform to lam and added transformed lam_log_ to model.
[-----] 2000 of 2000 complete in 1.6 sec
starting comparison of d, e
Applied log-transform to lam and added transformed lam_log_ to model.
[-----] 2000 of 2000 complete in 1.8 sec
starting comparison of d, c
Applied log-transform to lam and added transformed lam_log_ to model.
 [-----] 2000 of 2000 complete in 1.3 sec
starting comparison of b, e
Applied log-transform to lam and added transformed lam_log_ to model.
[-----] 2000 of 2000 complete in 1.9 sec
starting comparison of b, c
Applied log-transform to lam and added transformed lam_log_ to model.
[-----] 2000 of 2000 complete in 1.3 sec
starting comparison of e, c
Applied log-transform to lam and added transformed lam_log_ to model.
[-----] 2000 of 2000 complete in 1.5 secg g
q d
Applied log-transform to lam and added transformed lam_log_ to model.
 [-----] 2000 of 2000 complete in 1.3 secq b
Applied log-transform to lam and added transformed lam_log_ to model.
 [-----] 2000 of 2000 complete in 1.3 secg e
Applied log-transform to lam and added transformed lam_log_ to model.
 [-----] 2000 of 2000 complete in 1.3 secq c
Applied log-transform to lam and added transformed lam_log_ to model.
[-----] 2000 of 2000 complete in 1.5 secd d
Applied log-transform to lam and added transformed lam_log_ to model.
 [-----] 2000 of 2000 complete in 1.3 secd e
Applied log-transform to lam and added transformed lam_log_ to model.
 [-----] 2000 of 2000 complete in 1.5 secd c
b b
Applied log-transform to lam and added transformed lam_log_ to model.
[-----] 2000 of 2000 complete in 1.5 secb c
Applied log-transform to lam and added transformed lam_log_ to model.
[-----] 2000 of 2000 complete in 1.3 sece e
Applied log-transform to lam and added transformed lam_log_ to model.
 [-----] 2000 of 2000 complete in 1.5 secc c
```

The simulation has finished, and now I should make the heat map showing the primary correlations.

### 10.1 Figure 3. Pairwise regression values between all single mutants

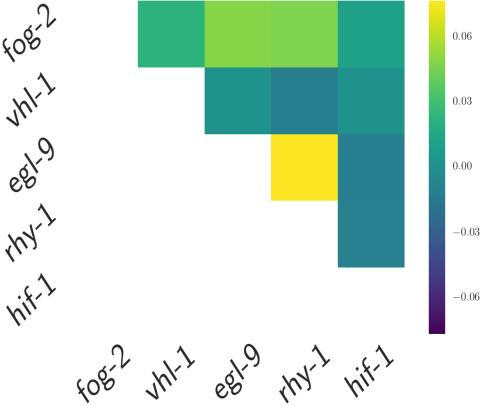
### Robust Bayesian Correlations Predict Interaction Between Genes



Notice the correlation values. They are very small, less than 0.30 in magnitude. This is fine though: While you weren't looking, I weighted the correlation by the fraction of DE genes that two mutant transcriptomes share divided by the total number of DE genes in either transcriptome. Since this fraction is usually << 1, our correlations have all shifted down, but that's OK! Remember the hypergeometric test suggested that every single on of the hypoxia interactions is non-random (for positive interactions) so we can freely interpret these correlation coefficients.

We can also plot the secondary correlations and see what comes out of them





# 11 Extracting functional relationships between genes

Another way to plot the results from the regression above is to make scatterplots. For that, it's best to work with tidy dataframes. What I will do next is the following:

Take the square correlation matrix I calculated above. Place it in a tidy dataframe. Concatenate this dataframe to include both primary and secondary relationships. Add a column that contains an indicator variable specifying whether the primary and the secondary regressions have different sign. If they don't have different signs, then add the correlations together. The reasoning for this is that:

$$w_1 \rho + w_2 \rho = (w_1 + w_2) \rho \tag{5}$$

In other words, we expect the correlation coefficient to be the same between the primary and secondary correlation and performing this is heuristically the same as adding the weights together. I know there's a better way to do this, and I am actively working on implementing this is in a proper manner. In the future, the weights will be added, and the secondary regression wil be discarded.

Finally, I order the pairs of genes to reflect decreasing functional distance and plot.

# 11.1 Decorrelation due to branching pathways generates monotonically decreasing plots

If we consider a pathway, A  $\rightarrow$  B  $\rightarrow$  C, then we can imagine the following thought process, granted that at each point of the pathway there are branches (i.e., A controls more genes than just B, but B is entirely controlled by A; etc...): \* The mutant  $A^-$  should lose the transcriptomes associated with all proteins, since it is equivalent to  $A^-B^-C^-$  \* The mutant  $B^-$  is equivalent to losing only  $B^-C^-$ , since the off-pathway transcriptome associated with A is intact \* The mutant  $C^-$  is equivalent to losing only  $C^-$ 

Therefore, if the mutants for A and B ought to share a fraction equal to:

$$\frac{A \cap B}{A \cup B} = \frac{|B^-| + |C^-|}{|A^-| + |B^-| + |C^-|},\tag{6}$$

Where |x| signifies 'the number of elements in X'. Moreover, here we consider the set of genes associated with loss of a gene to be only those genes that are differentially expressed relative to wild-type, NOT the entire genome.

And the mutants for A and C should share a fraction equal to:

$$\frac{A \cap C}{A \cup C} = \frac{|C^-|}{|A^-| + |B^-| + |C^-|}.$$
 (7)

Therefore, it follows that the fraction of genes that A and B share should be larger than the fraction that A and C share.

Moreover, if we relax the assumption that A, B and C should be entirely under control of this chain, we can imagine that the correlation between a LOF allele of A and a mutant B or C will necessarily be < 1. We can combine both assumptions by generating a weighted correlation coefficient:

$$\hat{\rho_{i,j}} = \frac{|i \cap j|}{|i \cup j|} \rho_{i,j} \tag{8}$$

if 'corr\_with' not in df:

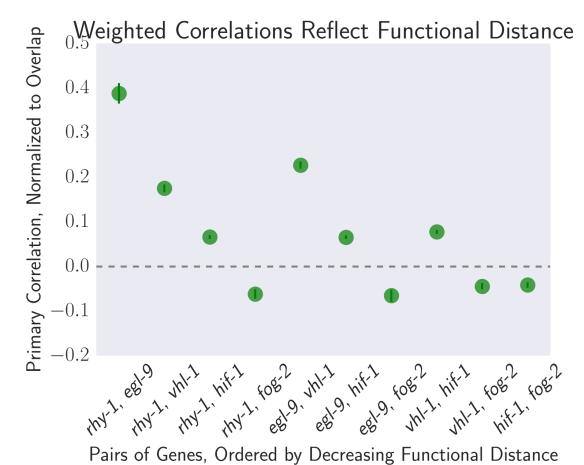
```
df['corr_with'] = morgan_obj.single_mutants
    # melt it so that each row has a single correlation
    df = pd.melt(df, id_vars='corr_with')
    # drop any observations where the correlated letters are the same
    df = df[df.corr with != df.variable]
    def calculate fraction(x, fraction='corr'):
        """Fraction of genes that participate in a given interaction."""
        if (x.corr_with, x.variable) in barbara.correlated_genes.keys():
            dd = barbara.correlated_genes[(x.corr_with, x.variable)]
            outliers = len(dd['outliers'])
            corr = len(dd['corr'])
            total = outliers + corr
            if fraction == 'corr':
                return corr/total
            else:
                return outliers/total
        else:
            return np.nan
    # calculate the fraction of genes participating in any interaction
    df['fraction'] = df.apply(calculate fraction, args=(corr,), axis=1)
    # generate a new variable 'pair' that is
    # the sum of the correlated genotypes (i.e. 'a', 'b' --> 'ab')
    df['pair'] = df.variable + df.corr_with
    # return the damned thing:
    return df
def different(x, d):
    Returns an indicator variable if the primary regression
    is different in sign from the secondary.
    n n n
    # extract the pair in question:
    p = x.pair
    # search for the primary interaction in the dataframe
   primary = d[(d.pair == p) &
                (d.regression == 'primary')].value.values[0]
    # search for the secondary
    secondary = d[(d.pair == p) &
                  (d.regression == 'secondary')].value.values[0]
    # if the interactions are 0, return 0
    if primary == 0 or secondary == 0:
        return 0
    # if they have the same sign, return -1
    elif (primary*secondary > 0):
        return -1
```

```
# otherwise return 1
    else:
        return 1
def special add(x):
    If the primary and secondary have the same sign,
    returns the addition of both.
    # if the current row is a secondary row
    # and the primary and secondary rows are the same
    # then return np.nan since we will want to ignore
    # the secondary correlation
    # if they are different in sign, return the current value
    if x.regression == 'secondary':
        if x.different == -1:
            return np.nan
        else:
            return x.value
    # if the regression is primary,
    # then add the values if the correlations have the same sign
    # otherwise just return the current value:
    check = d[(d.regression=='secondary') & \
         (d.pair == x.pair)].different.values
    if check == -1:
        to_add = d[(d.regression=='secondary') &
                   (d.pair == x.pair)].value.values[0]
        return x.value + to add
    else:
        return x.value
# tidy up the dataframe w/bayesian primary interactions:
d_pos = tidy_df(barbara.robust_slope)
# add a label specifying these are the primary regressions
d_pos['regression'] = 'primary'
# tidy up the secondary interactions
d_minus = tidy_df(barbara.secondary_slope, corr='outliers')
# add a label specifying these are the secondary regressions
d_minus['regression'] = 'secondary'
# concatenate the dataframes
frames = [d_pos, d_minus]
d = pd.concat(frames)
# identify whether primary and secondary
# interactions have different signs
d['different'] = d.apply(different, args=(d,), axis=1)
```

```
# drop any fractions that are NAN
         d.dropna(subset=['fraction'], inplace=True)
         # calculate corrected coefficients
         d['corrected'] = d.apply(special_add, axis=1)
         # drop any NAN corrected columns
         d.dropna(subset=['corrected'], inplace=True)
         # sort the pairs according to functional distance
         d['sort_pairs'] = d.pair.map(sort_pairs)
         d.sort('sort_pairs', inplace=True)
         # add the labels for plotting:
         d['genes'] = d.pair.map(decode_pairs)
In [38]: # extract the standard error for each correlation
         e_plus = tidy_df(barbara.errors_primary)
         e_plus['sort_pairs'] = e_plus.pair.map(sort_pairs)
         e_plus['genes'] = e_plus.pair.map(decode_pairs)
         e_plus.sort('sort_pairs', inplace=True)
         e_plus.dropna(inplace=True)
         e_minus = tidy_df(barbara.errors_secondary)
         e_minus['sort_pairs'] = e_minus.pair.map(sort_pairs)
         e_minus['genes'] = e_minus.pair.map(decode_pairs)
         e minus.sort('sort pairs', inplace=True)
         e_minus.dropna(inplace=True)
```

### 11.2 Figure 4. Weighted Correlations Reflect Functional Distance

Now we can plot the weighted correlations, making sure that they are ordered by functional distance.



### 11.3 hif-1 has negative interactions with rhy-1, and egl-9

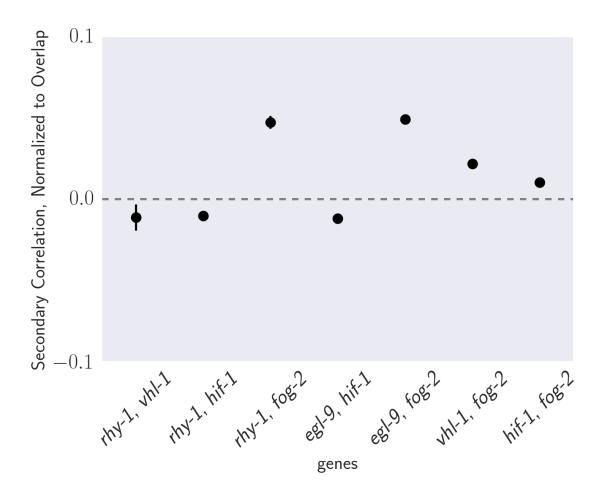
If we look at the secondary, what picture emerges? The most striking picture is that there are two modes of interaction between *rhy-1* and *vhl-1*, *hif-1* and *fog-2*. In every case, the secondary interaction is considerably less than 10% of the total overlap. I will make the claim that these interactions are stronger and more important than we may believe at first sight, but I won't push it. We will wait until we have more datasets to show this.

Regardless, let's think about what this entails. In theory, *rhy-1*, *egl-9* and *vhl-1* should have exclusively positive relationships. However, we see that these genes share at least some other secondary interactions.

In particular, I find the fact that *rhy-1* and *egl-9* both have negative secondary interactions interesting. In theory, we would have expected this to be the primary mode of interaction (negative), but the data did not bear it out. The fact that these genes have two modes of interaction with *hif-1* is therefore (strongly) suggestive of a cyclic pathway, or other types of homeostasis. Moreover, the presence of this cycle promises to be explicatory: If *hif-1* has a cycle with *rhy-1* that constitutes a positive feedback loop (the primary observed mode of interaction), then *vhl-1* should have a positive primary relationship with *rhy-1*, in which case we wouldn't observe a negative interaction. However, if *hif-1* has a negative feedback loop with *rhy-1*, then *vhl-1* should have a negative secondary relationship with *rhy-1*, which we can observe.

Therefore, a parsimonious model that can explain these interactions is one that suggests that *hif-1* is interacting in a negative feedback loop with *rhy-1* in a *vhl-1* independent manner. This should lead to both positive and negative transcriptomic interactions between *hif-1* and *rhy-1* and also between *rhy-1* and *vhl-1* and *egl-9* and *hif-1*.

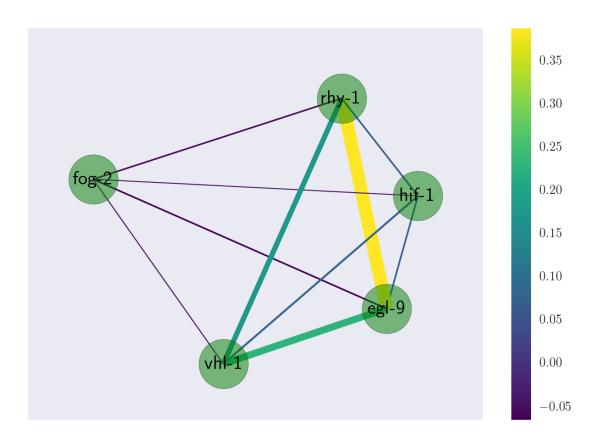
```
In [41]: sns.stripplot(x='genes', y='corrected',
                       data=d[(d.regression=='secondary') &
                              (d.different == 1)],
                       size=10, color='k')
         # add errorbars:
         for x, xlabel in zip(plt.gca().get_xticks(),
                              plt.gca().get xticklabels()):
             temp = d[d.regression=='secondary']
             f = temp.genes == xlabel.get_text()
             f2 = e_minus.genes == xlabel.get_text()
             plt.qca().errorbar(np.ones_like(temp[f].corrected.values)*x,
                                temp[f].corrected.values,
                                yerr=e_minus[f2].value.values,
                                ls='none', color='k')
         plt.axhline(0, ls='--', color='0.5')
         plt.xticks(rotation=45, fontsize=20)
         plt.yticks([-0.1, 0, 0.1], fontsize=20)
         plt.axhline(0, lw=2, ls='--', color='gray')
         plt.ylabel('Secondary Correlation, Normalized to Overlap')
Out[41]: <matplotlib.text.Text at 0x17482db00>
```



# 12 Figure 3 (Bottom) Correlation Graph

Now that I have estimated the primary correlation accurately, we can draw a network using these. This code will generate the bottom part of figure 3.

```
for i, key in enumerate(thomas.single_mutants):
    # and through each mutant:
    for j, key2 in enumerate(thomas.single_mutants):
        # extract the correlation coefficient
        r = d[(d.variable == key) & (d.corr with == key2) &
              (d.regression == 'primary')].corrected.values
        # only add an edge if a correlation coefficient exists:
        if r:
            # add the edge
            G.add_edge(mutant_dict[key],
                       mutant_dict[key2], weight=r[0])
# parameterize the edge and width and color of the graphs
# extract the edges:
elarge=[(u,v) for (u,v,d) in G.edges(data=True)]
# set the width -- I will use a slightly supra-linear function to
# make the widths easier to discern to human eyes:
width=[30*np.abs(d['weight'])**1.15]
       for (u, v, d) in G.edges(data=True)]
# extract the weights (keep these exact!)
weights=[d['weight'] for (u,v,d) in G.edges(data=True)]
# paint the canvas:
fig, ax = plt.subplots()
pos=nx.spring_layout(G) # positions for all nodes
# draw the nodes:
nx.draw_networkx_nodes(G, pos, node_size=1500,
                       node_color='g', alpha=.5)
# draw the edges:
edges = nx.draw_networkx_edges(G, pos, edgelist=elarge,
                               width=width, edge_color=weights,
                               edge_cmap=plt.cm.viridis)
# add the labels:
nx.draw_networkx_labels(G, pos, font_size=15,
                        font_family='sans-serif')
# add a colorbar:
fig.colorbar(edges)
# de-tick and save
plt.xticks([])
plt.yticks([])
plt.savefig("../output/weighted_graph.pdf") # save as png
plt.show() # display
```



# 13 Double Mutant Analysis

With double mutants, the analysis gets slightly more complicated. Now we're getting into full pathways!

A first approach is to inspect the double mutants by Spearman correlation analysis to the single mutants that make them up. A quick visualization will show us any epistasis and the extent of it:

plt.yticks([-0.2, 0.5, 1], fontsize=20)

```
In [ ]: sns.stripplot(x='double mutant', y='correlation',
                      hue='corr with', data=alfred.epistasis,
                      size=15, jitter=True)
        plt.xticks(fontsize=20)
        plt.axhline(0, ls='--', color='0.5')
        plt.yticks([-0.1, 0.2, 0.4], fontsize=20)
In [ ]: alfred.epistasis_secondary['unweighted'] = alfred.epistasis_secondary.corre
        alfred.epistasis_secondary['fractional corr'] = alfred.epistasis_secondary
        alfred.epistasis_secondary['double mutant'] = alfred.epistasis_secondary.do
        alfred.epistasis_secondary['corr with'] = alfred.epistasis_secondary.corr_v
        sns.stripplot(x='double mutant', y='unweighted',
                      hue='corr with', data=alfred.epistasis_secondary,
                      size=15, jitter=True)
        plt.xticks(fontsize=20)
        # plt.ylim(-1.1, 1.1)
        # plt.axhline(0, ls='--', color='0.5')
        # plt.yticks([-1, 0, 1], fontsize=20)
```

## 14 Table 1. Epistasis Can Be Quantified Via Linear Regression Models

Previously we have observed that correlations between double and single mutants might be informative. However, raw correlations alone are not the most informative in this situation. The reason is that the robust comparison (ranked genes) between single mutants and double mutants is not likely to be highly variable between single and double mutants under an additive model or even certain epistatic models.

However, it is illustrative to look at a double mutant under an additive model. Consider that a double mutant ought to have extensive overlap with both single mutants that make it up. If the individual genes are interacting, then it makes sense that the double mutant should exhibit a perturbation proportional to the kind of relationship these genes share. Specifically, the genes that are involved in *both* genes will be the ones that will exhibit the expected perturbation.

Therefore, the plan of attack should be as follows: \* Identify the genes that appear in each single mutant and the double mutant \* Run a linear regression on the regression coefficients between the single and the double mutant (these are two correlations).

If the mutants are additive, as would be expected if they both interact via a branched third party (i.e.  $A \rightarrow X$ ;  $B \rightarrow X$ ;  $X \rightarrow O$ utput), then the double mutant should show worsening (a linear regression with slope > 1). If they are interacting via a linear pathway, then the double mutant should have a linear slope with value of unity. If they share an inhibitory relationship, then the double mutant ought to have a slope < 1.

In the next steps, I will calculate these linear regressions. However, I will plot something slightly different. I will plot  $\Delta$  versus the single mutant, where  $\Delta = \beta_{Double} - \beta_{Single}$ , and run the regression on the resulting values. The slopes that I will obtain will be trivially related to the ones I have described above by a scalar.

First, I will define a few functions, then plot the results.

```
In [43]: def quadrature(x):
```

```
"""Variance of sums is sum of the variances."""
    def square(x):
        return x**2
    return np.sqrt(np.sum(x.apply(square)))
def identify(pair, df0, df1, double):
    identify the genes that are altered
    in all of these mutant dataframes
    Params:
    pair =
    m m m
    # predictions, single mutants
    df_pred0 = df0.copy()
    df_pred1 = df1.copy()
    # identify single mutants DE genes
    df_pred0 = df_pred0[df_pred0.qval < thomas.q]</pre>
    df pred1 = df pred1[df pred1.gval < thomas.g]</pre>
    # find the predicted genes
    pred_genes = df_pred0[ind].target_id
    # get the double mutant
    df_test = thomas.beta[double]
    # find the predicted genes that show up in the double,
    # these constitute the final overlap
    df_test = df_test[df_test.target_id.isin(pred_genes) &
                       (df_test.qval< 0.1)].copy()</pre>
    # select only the overlapping genes
    df_pred0 = df_pred0[df_pred0.target_id.isin(df_test.target_id)]
    df_pred1 = df_pred1[df_pred1.target_id.isin(df_test.target_id)]
    # drop anything that is NA... hopefully that means dropping nothing...
    df_pred0 = df_pred0.dropna(subset=['b'])
    df_pred1 = df_pred1.dropna(subset=['b'])
    df_test = df_test.dropna(subset=['b'])
    # return the damned thing
    return df_pred0, df_pred1, df_test
def plot_delta(prediction, test, fmt, label):
    11 11 11
    Given a prediction, calculates the delta between
```

```
the prediction and the test, and plots the result.
    # variance of the sum is sum of the variances:
    yerr = np.sqrt(test.se_b.values**2 +
                   prediction.se b.values**2)
    # calculate the delta
    delta = test.b.values - prediction.b.values
    # plot the errorbar
    plt.errorbar(prediction.b, delta,
                 xerr=prediction.se_b,
                 yerr=yerr, fmt=fmt,
                 alpha=0.2, ms=4,
                 label=label)
    plt.legend()
def weighted_regression_delta(prediction, test):
    Given a prediction and a test,
    find the weighted least squares regression between them.
    # fit a WLS
    wls = sm.WLS(test.b.values - prediction.b.values,
                  prediction.b.values,
                 weights=1./prediction.se_b.values**2)
    res_wls = wls.fit()
    return res_wls
def plot_epistasis_regression(prediction0, prediction1,
                              double, slope0, slope1):
    """Plot the WLS line."""
    # find the xmin and xmax:
    xmin = np.min([prediction0.b.min(),
                   prediction1.b.min()])
    xmax = np.max([prediction0.b.max(),
                   prediction1.b.max()])
    # make a linear array for x
    x = np.linspace(xmin - 0.1, xmax + 0.1, 1000)
    # make the models
    y0 = x*slope0
    y1 = x * slope1
    # plot the models
    plt.plot(x, y0, 'g-', lw=2)
    plt.plot(x, y1, 'b-', 1w=2)
```

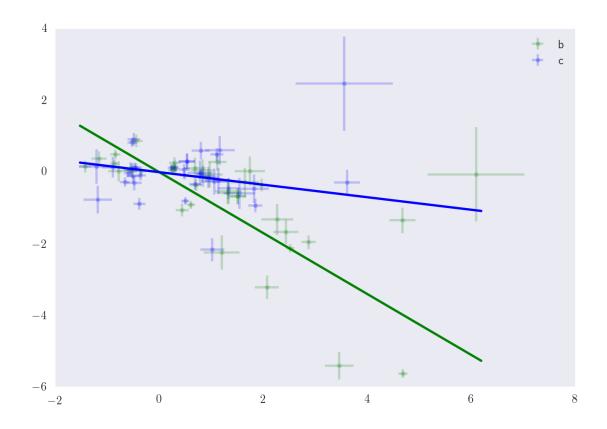
### 14.1 Double Mutant hif-1; egl-9 WLS epistatic analysis

```
In [48]: double = 'f'
         pair = thomas.double_muts[double]
         results = identify(pair, thomas.beta_filtered[pair[0]],
                            thomas.beta_filtered[pair[1]], double)
         df_pred0, df_pred1, df_test = results
         # plot the prediction versus the delta:
         plot_delta(df_pred0, df_test, 'go', pair[0])
         plot_delta(df_pred1, df_test, 'bo', pair[1])
         # perform the WLS
         res wls0 = weighted regression delta(df pred0, df test)
         res_wls1 = weighted_regression_delta(df_pred1, df_test)
         # get the slopes out:
         slope0 = res_wls0.params[0]
         slope1 = res_wls1.params[0]
         # print a summary of the results
         print_WLS_summary(pair, [slope0, slope1],
                           res_wls0, res_wls1)
         # plot
         plot_epistasis_regression(df_pred0, df_pred1,
                                    df_test, slope0, slope1)
         # print out basic stats about the 'fold change'
         # which should agree with WLS
         def print_b_summary(pair, p1, p2, test):
             adj_p1 = np.sqrt(quadrature(p1.se_b)/len(p1)**2
             adj_p2 = np.sqrt(quadrature(p2.se_b)/len(p2)**2
             adj_test = np.sqrt(quadrature(test.se_b)/len(test)**2
             string = """
         \{0\}: mean b = \{3:.2q\} +/- \{6:.2q\}
         \{1\}: mean b = \{4:.2g\} +/- \{7:.2g\}
```

print\_b\_summary(pair, df\_pred0, df\_pred1, df\_test)

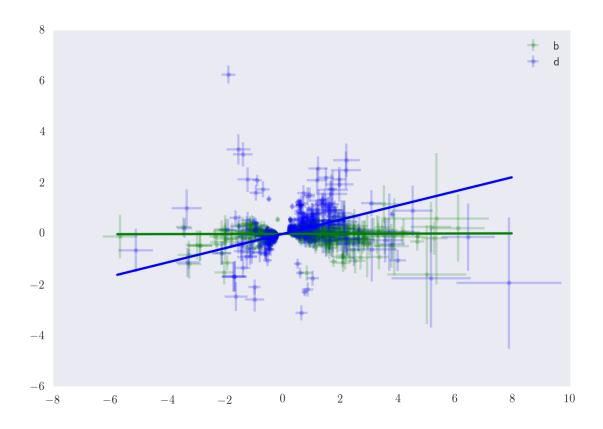
```
mutant b slope: -0.85 +/- 0.074, pvalue=1e-13 mutant c slope: -0.18 +/- 0.1, pvalue=0.097
```

b: mean b = 1.5 + /- 0.22c: mean b = 0.95 + /- 0.13bc: mean b = 1 + /- 0.17



#### 14.2 Double Mutant egl-9; vhl-1 WLS epistatic analysis

```
In [49]: double = 'a'
         pair = thomas.double_muts[double]
         results = identify(pair, thomas.beta_filtered[pair[0]],
                            thomas.beta filtered[pair[1]], double)
         df_pred0, df_pred1, df_test = results
         # plot the prediction versus the delta:
         plot_delta(df_pred0, df_test,
                    'go', pair[0])
         plot_delta(df_pred1, df_test,
                    'bo', pair[1])
         # perform the WLS
         res_wls0 = weighted_regression_delta(df_pred0, df_test)
         res_wls1 = weighted_regression_delta(df_pred1, df_test)
         # get the slopes out:
         slope0 = res_wls0.params[0]
         slope1 = res_wls1.params[0]
         # print a summary of the results
         print_WLS_summary(pair, [slope0, slope1],
                           res_wls0, res_wls1)
         # plot
         plot_epistasis_regression(df_pred0, df_pred1,
                                   df_test, slope0, slope1)
         # print out basic stats about the 'fold change',
         # which should agree with WLS
         print_b_summary(pair, df_pred0, df_pred1, df_test)
mutant b slope: 0.0023 +/- 0.0098, pvalue=0.81
mutant d slope: 0.28 +/- 0.033, pvalue=3.7e-16
b: mean b = 1.2 + /- 0.05
d: mean b = 0.9 + /- 0.041
bd: mean b = 1.2 + /- 0.05
```



# 15 Double Mutants exhibit more than additive perturbations

```
In []: for key, value in thomas.double_muts.items():
    x = thomas.beta_filtered[key]
    y = thomas.beta_filtered[value[0]]
    z = thomas.beta_filtered[value[1]]

    x = x[x.qval < thomas.q]
    y = y[y.qval < thomas.q]
    z = z[z.qval < thomas.q]

    yANDz = len(y[y.target_id.isin(z)])
    yORz = len(y) + len(z)
    expected = yORz - yANDz

    pred1 = x[(x.target_id.isin(z.target_id))]
    pred2 = x[x.target_id.isin(y.target_id)]

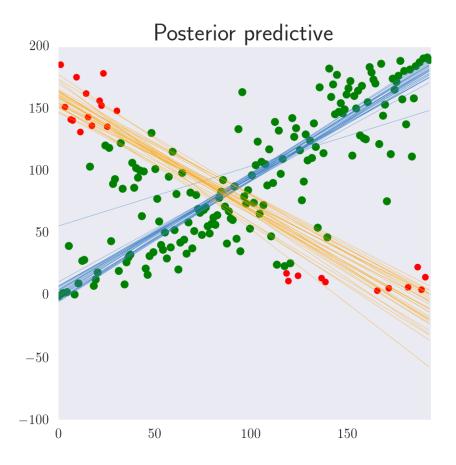
    pred = len(list(set(pred1.target_id.tolist())))</pre>
```

```
print('Expected: ', expected)
print('Observed: ', len(x))
print('Predicted: ', pred)
print('Observed/Expected: {0:.2g}'.format(len(x)/expected))
print('Predicted/Expected: {0:.2g}'.format(pred/expected))
print('Surprise factor: {0:.2g}'.format(pred/len(x)))
```

## 16 Double Mutants Exhibit Complex Interactions

```
In [50]: letters = ['a', 'c']
         x = thomas.beta_filtered[letters[0]]
         y = thomas.beta_filtered[letters[1]]
         ovx = x[lind(x)]
         ovy = y[lind(y) &
                 y.target_id.isin(ovx.target_id)].copy()
         ovx = x[lind(x) &
                 x.target_id.isin(ovy.target_id)].copy()
         ovx = find_rank(ovx)
         ovy = find_rank(ovy)
         data = dict(x=ovx.r, y=ovy.r)
         x = np.linspace(ovx.r.min(), ovx.r.max())
         trace_robust = robust_regress(data)
         plt.figure(figsize=(5, 5))
         intercept = trace_robust.Intercept.mean()
         slope = trace_robust.x.mean()
         distribution =ovy.r - intercept - ovx.r*slope
         mean = distribution.mean()
         std = distribution.std()
         # find the inliers and outliers
         _ = find_inliers(distribution, mean, trace_robust)
         distribution_inliers, distribution_outliers, outliers = _
         data2 = dict(x=ovx[ovx.target_id.isin(outliers)].r,
                      y=ovy[ovy.target_id.isin(outliers)].r)
         trace robust2 = robust regress(data2)
         intercept = trace_robust2.Intercept.mean()
         slope = trace_robust2.x.mean()
```

```
yri = distribution_inliers + intercept + ovx.r*slope
        yro = distribution_outliers + intercept + ovx.r*slope
        plt.plot(ovx.r, yri, 'go', ms = 6)
        plt.plot(ovx.r, yro, 'ro', ms = 5)
        label = 'posterior predictive regression lines'
        pm.glm.plot_posterior_predictive(trace_robust, eval=x,
                                       label=label,
                                       color='#357EC7')
        pm.glm.plot_posterior_predictive(trace_robust2, eval=x,
                                       label=label,
                                       color='#FFA500')
        plt.xlim(0, len(ovx))
        # plt.legend()
        if np.abs(slope) > 0.6 and np.abs(slope2) > 0.6:
            t1 = slope/np.abs(slope)
            t2 = slope2/np.abs(slope2)
            if t1 == -t2:
               print('Complex Regulation at Work')
Applied log-transform to lam and added transformed lam_log_ to model.
[-----] 2000 of 2000 complete in 1.7 secApplied
 [-----] 2000 of 2000 complete in 1.3 secComplex H
```



# 17 Quality Control

Load up the hypoxia gold standard Carmie gave me. These genes are expected to go up in everything except in Hif-1.

By this point, I have solved the network, I guessed which gene was Hif-1 and I have been told the identities of the genes.

```
C = Hif-1
B = egl-9
D = vhl-1
E = rhy-1
```

nhr-57 is an important gene for hypoxia. WBID is WBGene00003647

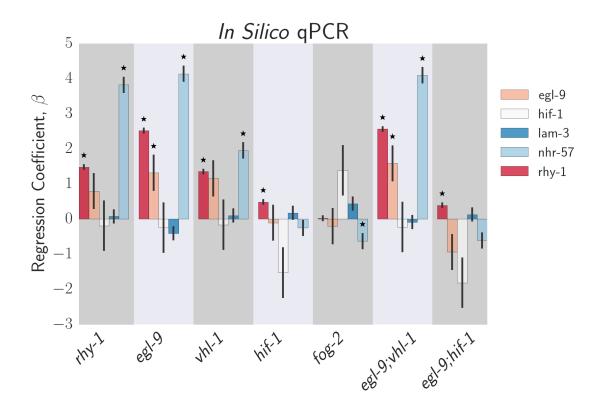
```
pval = sts.hypergeom.sf(len(found),
                                    len(df),
                                    len(hypoxia_gold),
                                    len(sig))
            print('genotype: ', sm)
             print('found: ', len(found),
                  ' Mean b: {0:.2g}'.format(found.b.mean()))
             print('pval: {0:.2g}'.format(pval))
             print('Maximum change was:')
             print(found[found.b == found.b.max()].ext_gene.values[0])
            print(np.exp(found[found.b == found.b.max()].b.values)[0],
                   ' fold change')
             if 'WBGene00003647' in found.ens_gene.values:
                 ind = found.ens_gene == 'WBGene00003647'
                 nhr57 = np.exp(found[ind].b.values[0])
                 print('nhr-57 is in', sm,
                       'and its fold change was {0:.2g}'.format(nhr57))
            print('----')
genotype: g
found: 4 Mean b: -1.4
pval: 0.22
Maximum change was:
nhr-57
0.534489095703 fold change
nhr-57 is in q and its fold change was 0.53
_____
genotype: d
found: 7 Mean b: 2.2
pval: 2.7e-06
Maximum change was:
dod-3
44.7574873949 fold change
nhr-57 is in d and its fold change was 7.1
_____
genotype: b
found: 9 Mean b: 2.6
pval: 5.7e-05
Maximum change was:
oac-54
66.7297848473 fold change
nhr-57 is in b and its fold change was 63
genotype: e
found: 10 Mean b: 2.4
```

## 18 An *in silico* qPCR experiment:

```
In [53]: sorter = {'a': 6,
                   'f': 7,
                   'b': 2,
                   'c': 4,
                   'd':3,
                   'e': 1,
                   'q': 5
                  }
         x = ['WBGene00001851',
              'WBGene00012324',
              'WBGene00001178',
              'WBGene00006922',
              'WBGene00003647',
              'WBGene00002248'
             1
         # run the experiment!
         def qPCR_prep(morgan, genelist):
             q = []
             data = np.array([])
             i = 0
             for genotype, df in thomas.beta.items():
                 for j, xi in enumerate(genelist):
                     geno = genotype_mapping[genotype]
                     cols = ['ens_gene', 'ext_gene', 'b', 'se_b', 'qval']
                     y = df[(df.ens_gene == xi)][cols].values
                     if len(y) == 0:
                          continue
                      # hif has two isoforms, so take F38A6.3c
```

```
if y.shape[0] > 1:
                         y = df[(df.target_id == 'F38A6.3c')][cols].values
                     if len(data) == 0:
                         data = y
                     else:
                         data = np.vstack((data, y))
                     g += [genotype]
                 i += 1
             d = pd.DataFrame(data, columns=cols)
             d['code'] = q
             d['genotype'] = d.code.map(genotype_mapping)
             d['order'] = d.code.map(sorter)
             d.sort_values('order', inplace=True)
             d.reset_index(inplace=True)
             return d
         d = qPCR\_prep(thomas, x)
In [54]: # a qPCR barplot
         temp = d
         index = np.linspace(0, temp.genotype.unique().shape[0]-1,
                              temp.genotype.unique().shape[0])
         alpha = 0.7
         error_config = {'ecolor': '0.2'}
         plotting = {'rhy-1': 0,
                     'egl-9': 1,
                     'hif-1': 2,
                     }
         color = { 'rhy-1': "#ca0020", }
                  'egl-9': '#f4a582',
                  'hif-1': '#f7f7f7',
                  'nhr-57': '#92c5de',
                  'lam-3': '#0571b0'
                 }
         grouped = temp.groupby('ext_gene')
         bar_width = 1/(len(grouped)+1)
         for name, group in grouped:
             if name not in plotting.keys():
                 where = max(plotting.keys(),
                              key=lambda k: plotting[k])
                 val = plotting[where]
                 plotting[name] = val + 1
```

```
add = plotting[name] *bar_width
    if name in color.keys():
        barlist = plt.bar(index + add, group.b.values,
                          bar width, alpha=alpha,
                          yerr=group.se_b,
                          error_kw=error_config, label=name,
                          color=color[name])
    else:
        barlist = plt.bar(index + add, group.b.values,
                          bar_width, alpha=alpha,
                          yerr=group.se_b,
                          error_kw=error_config, label=name)
    sig = group.qval < 0.1</pre>
    k = group[sig].order -1
    plt.plot(k + add + bar_width/2,
             group[sig].b.values + group[sig].se_b.values + 0.25,
             r'*', color='k')
grouped2 = temp.groupby('genotype')
k = 0
col = '#CFCFCF'
for name, group in grouped2:
    if k % 2 == 0:
        xmin = k - bar_width *0.5
        xmax = k + bar_width*(len(grouped) + 0.5)
        ymin, ymax = plt.gca().get_ylim()
        plt.fill_between([xmin, xmax], ymax, color=col)
        plt.fill_between([xmin, xmax], ymin, color=col)
    k += 1
plt.xlim(0, plt.gca().get_xlim()[1] - bar_width)
plt.tick_params(axis='y',
                which='major', labelsize=18)
plt.xticks(index + bar width,
           temp.genotype.unique(), rotation=45, fontsize=20)
pathify(r'\emph{In Silico} gPCR', '',
        r'Regression Coefficient, $\beta$', )
plt.legend(loc=(1.02, 0.5), fontsize=15)
plt.savefig('../output/pathwaygenes_qPCR.pdf',
            bbox_inches='tight')
```



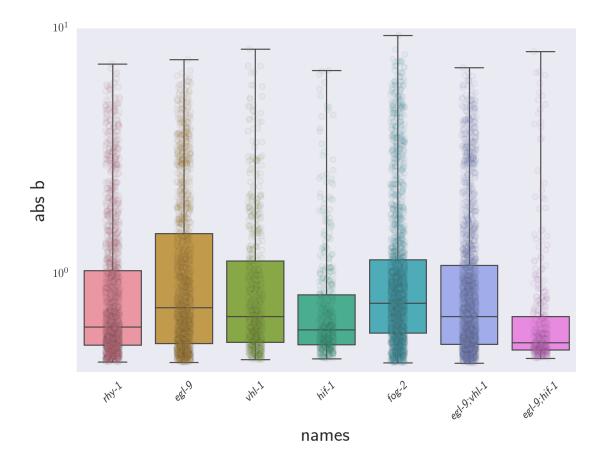
# 19 Searching for a TF that is activated by both egl-9 and hif-1

And possibly regulates rhy-1 as a result

```
In [55]: # Figure out how many hits we get and if the pvalue is significant!
         tfs = {}
         for sm in thomas.single_mutants:
             df = thomas.beta_filtered[sm]
             ind = (genpy.find(df, tf_df.target_id,
                               col='target id'))
             found = df[ind & (df.qval < 0.1)]
             sig = df[df.qval < 0.1]
             pval = sts.hypergeom.sf(len(found),
                                     len(df),
                                     len(hypoxia_gold),
                                     len(sig))
             print('genotype: ', sm)
             print('found: ', len(found),
                   ' Mean b: {0:.2g}'.format(found.b.mean()))
             print('pval: {0:.2g}'.format(pval))
             tfs[sm] = found.copy()
             print('----')
```

```
genotype: g
found: 44 Mean b: 0.15
pval: 0
_____
genotype: d
found: 10 Mean b: 0.64
pval: 5.4e-10
_____
genotype: b
found: 21 Mean b: 0.6
pval: 0
_____
genotype: e
found: 31 Mean b: 0.49
pval: 0
_____
genotype: c
found: 15 Mean b: 0.19
pval: 2.3e-19
_____
In [56]: def add_b(x):
            vals = tfs['c'][tfs['c'].target_id == x]
            if len(vals):
               return vals.b.values[0]
            else:
               return np.nan
        temp = tfs['b']
        temp['b_c'] = temp.target_id.apply(add_b)
In [57]: temp[(temp.b_c < 0) &
             (temp.b < 0)][['ext_gene','b_c','b', 'qval']]</pre>
            ext_gene b_c
Out [57]:
        5522 mxl-3 -0.89506 -0.781183 0.002857
In [58]: # mxl-3 should be down in the egl, hif double:
        temp = thomas.beta_filtered['f']
        temp[(temp.ext_gene == 'mxl-3')][['ext_gene', 'b', 'qval']]
            ext_gene
Out [58]:
                           b
                                   qval
        5522 mxl-3 -0.757522 0.020871
In [59]: temp = thomas.beta filtered['a']
        temp[(temp.ext_gene == 'mx1-3')][['ext_gene', 'b', 'qval']]
Out[59]: ext_gene b
                                   qval
        5522 mxl-3 -0.319002 0.404185
```

```
In [60]: temp = thomas.beta_filtered['e']
         temp[(temp.ext_gene == 'mxl-3')][['ext_gene', 'b', 'qval']]
Out [60]:
              ext gene
                                       qval
                 mx1-3 -0.343135 0.388758
         5522
In [61]: temp = thomas.beta_filtered['d']
         temp[(temp.ext gene == 'mx1-3')][['ext gene', 'b', 'qval']]
Out [61]:
              ext_gene
         5522
                mx1-3 - 0.383277 0.465043
In [62]: bs = np.array([])
         for key in thomas.beta.keys():
             df = thomas.beta_filtered[key]
             if len(bs) == 0:
                 bs = df.b.values
                 qs = df.qval.values
             else:
                 bs = np.vstack((bs, df.b.values))
                 qs = np.vstack((qs, df.qval.values))
In [63]: b_df = pd.DataFrame(np.transpose(bs),
                             columns = thomas.beta.keys())
         q_df = pd.DataFrame(np.transpose(qs),
                             columns = thomas.beta.keys())
         b_df = pd.melt(b_df, var_name='genotype',
                        value name='b')
         q_df = pd.melt(q_df, var_name='genotype',
                        value name='q')
         b_df['abs b'] = b_df.b.abs()
         b_df['sorter'] = b_df.genotype.map(sorter)
         q_df['sorter'] = q_df.genotype.map(sorter)
         b df.sort values('sorter', inplace=True)
         q_df.sort_values('sorter', inplace=True)
         b_df['names'] = b_df.genotype.map(genotype_mapping)
In [64]: sns.boxplot(x="names", y="abs b",
                     data=b_df[q_df.q < 0.1],
                     whis=np.inf, linewidth=1)
         sns.stripplot('names', 'abs b',
                       data=b_df[q_df.q < 0.1],
                       linewidth=1, jitter=True,
                       alpha=0.05)
         plt.xticks(rotation=45)
         plt.ylim(10 * * -1, 10)
         plt.yscale('symlog')
```



# 20 Finding direct targets of hif-1, vhl-1, egl-9 and rhy-1

## 20.1 Hydroxylated hif-1 direct targets

Knocking out *hif-1* should decrease levels of hydroxylated and non-hydroxylated *hif-1* Knocking out *vhl-1* should increase levels of both forms.

Knocking out *egl-9* or *rhy-1* should decrease the hydroxylated form and increase the non-hydroxylated form.

Knocking out *egl-9;hif-1* should decrease levels of hydroxylated and non-hydroxylated *hif-1*Therefore: Overlap *hif-1*, *egl-9* and *rhy-1* mutants with coexpression and find only targets that

go DOWN. Next, overlap *vhl-1* with anti-expression. These are the hydroxylated targets of *hif-1* and possibly some other stuff

```
In [66]: df1 = thomas.beta['f'].copy()
         df2 = thomas.beta['c']
         df3 = thomas.beta['e']
         df4 = thomas.beta['b']
         df5 = thomas.beta['a']
         df6 = thomas.beta['d']
         df1['b_c'] = df2.b
         df1['b_e'] = df3.b
         df1['b_b'] = df4.b
         df1['b_a'] = df5.b
         df1['b_d'] = df6.b
         df1['se_b_c'] = df2.b
         df1['se_b_e'] = df3.b
         df1['se_b_b'] = df4.b
         df1['se_b_a'] = df5.b
         df1['se b d'] = df6.b
         df1['q_c'] = df2.qval
         df1['q_e'] = df3.qval
         df1['q_b'] = df4.qval
         df1['q_a'] = df5.qval
         df1['q_d'] = df6.qval
         ind = (df1.qval < 0.1) & (df1.q_c < 0.1) & (df1.q_e < 0.1) & \)
               (df1.q_b < 0.1) & (df1.q_a < 0.1) & (df1.q_d < 0.1)
         ind2 = (df1.b < 0) & (df1.b_c < 0) & \
                (df1.b_e < 0) & (df1.b_b < 0) & (df1.b_a < 0)
         ind3 = (df1.b d > 0)
         df1[ind & ind2 & ind3][['ext gene', 'b d', 'g d']]
Out [66]:
                ext_gene
                               b_d
                                              q_d
                F20D6.11 0.589394 3.392273e-03
         9850
         11479
                   cat-4 0.751071 1.325726e-08
```

We find two genes. . It's possible that we just couldn't measure the hydroxylated *hif-1* targets properly because A less stringent filter would be to just anti-overlap the *vhl-1* with the (*egl-9* and *rhy-1*) mutants and see what comes up. This means we are no longer measuring *hif-1* directly,

rather, we are inferring it and hoping that the noise from other stuff that these genes have in common gets drowned out.

```
In [67]: # significant in all relevant depts.
         ind = (df1.q_e < 0.1) & (df1.q_b < 0.1) & (
               (df1.q_a < 0.1) & (df1.q_d < 0.1)
         # loss of egl causes hif-OH to go down
         ind2 = (df1.b_e < 0) & (df1.b_b < 0) & (df1.b_a < 0)
         ind3 = (df1.b_d > 0) # vhl causes hif-OH to go UP
         hydroxylated hif = df1[ind & ind2 & ind3]
         cols = ['ext_gene', 'b_d', 'q_d', 'b_e']
        hydroxylated hif[cols].sort values('q d').head()
Out [67]:
                              b_d
                ext_gene
                                             q_d
                  cat-4 0.751071 1.325726e-08 -0.763864
         11479
               F55G11.2 0.854800 1.708696e-03 -0.587116
         15045
         9850 F20D6.11 0.589394 3.392273e-03 -0.554782
        15953
                  asp-8 0.646281 6.687030e-02 -1.769170
```

Nope! It looks that even our less stringen filter yields quite the small list of targets!

#### 20.2 Non-hydroxylated hif-1 targets

Let's find the genes associated with non-hydroxylated hypoxia factor next.

Knocking out hif-1 should decrease levels of hydroxylated and non-hydroxylated hif-1

Knocking out *vhl-1* should increase levels of both forms.

Knocking out egl-9 or rhy-1 should decrease the hydroxylated form and increase the non-hydroxylated form.

Knocking out egl-9;hif-1 should decrease levels of hydroxylated and non-hydroxylated hif-1

Therefore: Overlap *vhl-1*, *egl-9* and *rhy-1* mutants with coexpression and find only targets that go UP. Next, overlap *hif-1* with anti-expression. These are targets of non-hydroxylated *hif-1* and possibly some other stuff

Again, we observe only very few genes. Let's try to remove the *hif-1;egl-9* double mutant to increase our sample size:

```
In [69]: ind = ((df1.q_c < 0.1) & (df1.q_e < 0.1) &
                (df1.q_b < 0.1) & (df1.q_a < 0.1) &
                (df1.q_d < 0.1)
        ind2 = ((df1.b_e > 0) & (df1.b_b > 0) &
                (df1.b_a > 0) & (df1.b_d > 0))
        ind3 = (df1.b_c < 0)
        df1[ind & ind2 & ind3][['ext_gene', 'b_e', 'q_e']].sort_values('q_e')
Out [69]:
               ext_gene
                              b_e
               R08E5.3 4.577666 0.000000e+00
        19626
        26372 Y37A1B.5 2.590956 1.489199e-70
                  nit-1 3.369282 4.598481e-32
        31611
        20101 R12C12.5 0.488469 3.239911e-06
        12288 hsp-12.3 1.473647 2.173847e-05
```

We can definitely say that these are the best candidates for direct control by *hif-1*. However, the list could probably still be larger.

Let's weaken the conditions a little bit. Now, we will only require that whatever our candidate genes are, they should not be **significantly upregulated in response to loss of hif-1**.

```
In [70]: ind = ((df1.q_e < 0.1) & (df1.q_b < 0.1) &
                 (df1.q_a < 0.1) & (df1.q_d < 0.1))
         ind2 = ((df1.b_e > 0) & (df1.b_b > 0) &
                 (df1.b_a > 0) & (df1.b_d > 0))
         ind3 = (\sim ((df1.q_c < 0.1) & (df1.b_c > 0)) &
                 \sim ((df1.qval < 0.1) & (df1.b > 0)))
         hypoxia_direct_targets = df1[ind & ind2 & ind3]
         print (hypoxia_direct_targets.shape[0])
         hypoxia_direct_targets[['ext_gene', 'b_e', 'q_e']].sort_values('q_e').head
133
Out [70]:
              ext_gene
                              b_e
                                             q_e
         19626
               R08E5.3 4.577666 0.000000e+00
         4509
               C31C9.2 2.469312 1.688359e-99
         10774 F26H9.5 1.599513 9.709034e-91
         26372 Y37A1B.5 2.590956 1.489199e-70
         21073
                 nhr-57 3.821550 1.190906e-57
```

Now we're talking! We can definitely say that these are the best candidates for direct control by *hif-1*.

If we are willing to let go of the difference between hydroxylated and non-hydroxylated *hif-1*, we could remove the *hif-1* filters entirely. However, I think these 167 genes are probably enough for now. Let's take a moment now to verify that this result matches what is known in the literature:

```
In [71]: ids = hypoxia_direct_targets.ens_gene.unique()
    _ = tea.enrichment_analysis(ids, tissue_df, show=True)
    _ = tea.enrichment_analysis(ids, phenotype_df, show=True)
```

```
Executing script

Analysis returned no enriched tissues.

Executing script

Tissue Expected Observed

O neuron development variant WBPhenotype:0000816 0.374431 4

Enrichment Fold Change P value Q value

O 10.68287 0.000033 0.007724
```

#### 20.3 Quality control on identified genes:

Before we call these *hif-1* targets, we should make sure that at least some known targets are contained in this set. In order to do this, we have curated a list of 20 or so genes that have been published before as *hif-1* targets.

That being said though, we need to be aware of 1 major issue with this dataset.

hif-1 and rhy-1 form an incredibly tight loop. There is a LOT of feedback between hif-1 and rhy-1. Given the kind of logic we are using, we are probably excluding a number of targets as a result. In fact, the logic we have used to develop this list excludes rhy-1 itself, a known hif-1 target! I could do better, but not without a lot more lines of code, and it just doesn't seem reasonable to do this.

This result is statistically significant with a p-value of 4.2e-08 using a hyperged

Very nice! We are actually sampling from the hif-1 pool! Fantastic!

### 20.4 Identifying rhy-1 targets

Next, let's identify rhy-1 associated genes. We will also insist that rhy-1 genes NOT be associated with hif-1 (they really shouldn't be, the logic between these two sets is mutually exclusive, I think, but it's best to make sure; let's hit stuff with a hammer):

```
In [73]: ind = ((df1.q_e < 0.1) & (df1.q_b < 0.1) & (df1.q_a < 0.1) & (df1.q_c < 0.1))
```

```
ind2 = ((df1.b_e*df1.b_b > 0) & (df1.b_e*df1.b_a > 0) &
                 (df1.b_c*df1.b_e > 0) & (df1.b_c*df1.b_b > 0))
        ind3 = (~df1.target_id.isin(hypoxia_direct_targets.target_id))
        rhy1_targets = df1[ind & ind2 & ind3]
        print (rhy1_targets.shape)
        rhy1_targets[['ext_gene', 'b_e', 'q_e']].sort_values('q_e').head()
(74, 30)
Out [73]:
              ext_gene
                              b_e
                                            q_e
         24825
                 rhy-1 1.482076 9.672920e-71
                ZC317.7 2.144840 9.204531e-63
         31240
        3949
                C26B9.3 2.686908 2.936705e-40
        20836 T04A11.1 2.014769 5.957883e-35
         20843 T04A11.4 2.014769 5.957883e-35
In [74]: rhy1_targets[(rhy1_targets.b_e <= rhy1_targets.b_e.min() + 1.5)][['ext_ger</pre>
Out [74]:
              ext_gene
                              b_e
        1082
               C01G10.8 -0.505152
             C05C10.3 -0.378379
        1581
         6216
               C47G2.4 0.290649
         6981
                  dnj-7 -0.620841
                acdh-1 -0.476948
        6992
        8936
                  ldh-1 0.308663
        9850 F20D6.11 -0.554782
        11192
                unc-45 -0.416793
        11479
                 cat-4 - 0.763864
        11703
                 pfn-2 0.278972
        12331
                dnj-12 -0.529155
        12385 F39G3.3 -0.446410
        13120
                    NaN - 0.348950
        14513
                 cct-3 -0.397977
        14659 F54D5.12 -0.626779
        16687
                  ran-1 -0.325141
        18340
                  tra-3 -0.307254
        20316
                  pfd-5 -0.517453
        20809
                 lis-1 -0.341856
        21101
                  cct-1 - 0.371549
        21106
                dnj-19 -0.403246
                 ech-6 -0.575509
        21205
        21867
                 cct-7 -0.420124
        22384 T15B7.1 -0.876063
        22391
                 lgc-54 -1.190153
        26108 Y23H5B.5 -0.380572
        26660 Y38F1A.6 -0.573424
        29202
                 arl-8 -0.263515
```

## 20.5 Identifying egl-9 targets

OK! We found 'em. Let's find the egl-9 related genes next.

```
In [75]: ind = ((df1.q_e < 0.1) & (df1.q_b < 0.1) &
                (df1.q_a < 0.1) & (df1.q_d > 0.1) &
                (df1.q_c > 0.1))
        ind2 = ((df1.b_e*df1.b_b > 0) &
                (df1.b_e*df1.b_a > 0) &
                (df1.b b*df1.b a > 0))
                  & (df1.b_c*df1.b_e < 0) & (df1.b_c*df1.b_b < 0) \
                  & (df1.b_b*df1.b_d > 0) & (df1.b_e*df1.b_d > 0)
        ind3 = True
        # remember ids contains the hypoxia_direct_targets
        ind4 = (~df1.target_id.isin(ids))
        egl_targets = df1[ind & ind2 & ind3 & ind4]
        print(egl_targets.ens_gene.unique().shape[0])
        egl_targets[['ext_gene', 'b_b', 'q_b']].sort_values('q_b').head(10)
464
Out [75]:
              ext_gene
                            b_b
                                           q_b
        3558
               C18H9.6 -3.021398 1.269703e-72
        17056
                nas-33 3.102550 4.313509e-38
        25104 W10G11.3 -2.330393 8.491660e-34
                 far-3 4.401688 3.042296e-33
        9265
        15295
                  cdo-1 2.171999 6.303173e-32
        18213 nas-11 1.521469 7.037006e-32
        18219 K11G12.5 0.937802 9.660511e-32
        22260 T13F3.6 -3.477438 3.973725e-28
        1197
                 tyr-1 1.606652 3.979676e-28
        17862 cyp-35A3 -2.002178 4.214261e-23
In [76]: egl_ids = egl_targets.ens_gene.unique()
        _ = tea.enrichment_analysis(egl_ids,
                                    tissue_df, show=True)
        _ = tea.enrichment_analysis(egl_ids,
                                   phenotype_df, show=False)
        [0].head(10)
Executing script
                              Tissue
                                     Expected Observed \
O anal depressor muscle WBbt:0004292 13.798814
                                                      30
  Enrichment Fold Change P value
                                   Q value
                  2.1741 0.000011 0.002962
Executing script
```

```
Out [76]:
                                                                  Expected
                                                                             Observed
                                                         Tissue
         8
                 neuron morphology variant WBPhenotype:0000905
                                                                  12.309859
                                                                                   56
             vulval cell induction reduced WBPhenotype:0000219
                                                                                   8
         11
                                                                  29.154930
         42
                serotonin response variant WBPhenotype:0001232
                                                                  7.690141
                                                                                   4
                                                                  12.985915
         5
                         mid larval arrest WBPhenotype:0001019
                                                                                   56
         9
             intestinal cell development variant WBPhenotyp...
                                                                  4.225352
                                                                                   3:
         54
                       early larval lethal WBPhenotype:0000057
                                                                 18.112676
                                                                                   61
                    RNA expression variant WBPhenotype:0000113
         28
                                                                  20.591549
                                                                                   61
         10
                           coiling variant WBPhenotype:0002297
                                                                  60.619718
                                                                                  111
             embryonic cell morphology variant WBPhenotype:...
                                                                  39.774648
         36
                                                                                   84
              transgene expression reduced WBPhenotype:0001278
                                                                  58.394366
                                                                                  10
         55
             Enrichment Fold Change
                                           P value
                                                         Q value
         8
                           4.549199
                                     2.342003e-23
                                                    5.433448e-21
         11
                           2.984058
                                     5.636866e-23
                                                    6.538764e-21
         42
                           5.721612 1.234956e-22
                                                    9.550330e-21
         5
                           4.312364 3.505868e-22 2.033404e-20
                                     9.227203e-20
         9
                           7.336667
                                                   4.281422e-18
         54
                           3.367807 1.724677e-18 6.668751e-17
         28
                           2.962380 9.503627e-16 3.149773e-14
         10
                           1.831087
                                     7.114180e-13 2.063112e-11
                           2.111898 9.361201e-13 2.413110e-11
         36
         55
                           1.832369 2.407076e-12 5.584415e-11
```

#### 20.6 Identifying *vhl-1* targets

24756

6937

11228

hgo-1

mboa-3

psf-2

Next, let's find the vhl-related genes.

```
In [77]: ind = (df1.q_a < 0.1) & (df1.q_d < 0.1)
         ind2 = (df1.b_d > 0) & (df1.b_a > 0)
         ind4 = ((df1.q_e > 0.1) & (df1.q_b > 0.1) &
                 (df1.q_b > 0.1))
         vhl_targets = df1[ind & ind2 & ind4]
         print(vhl_targets.shape[0])
         vhl_targets[['ext_gene', 'b_d', 'q_d', 'b_b', 'b_e']].sort_values('q_d').h
30
Out [77]:
               ext_gene
                              b_d
                                            q_d
                                                      b_b
         11227 F31C3.4
                        0.556422
                                  1.653782e-08 -0.039171
                                                           0.069805
         11226 F31C3.3
                        0.509236
                                   5.936751e-07 0.108664
                                                          0.062222
```

3.375891e-06

3.954259e-03

0.099012 -0.092270

0.164309 -0.127737

4.516616e-03 0.224087 0.094825

0.500935

0.506001

0.592778

```
5991
               C46C2.2 0.455548 4.771579e-03 0.255569 -0.016089
         11606 F33H2.6 0.390757 6.374993e-03 -0.127979 -0.199501
         31155
               duxl-1 0.382592 6.407984e-03 0.136819 0.063909
        11229 F31C3.6 0.576217 7.482708e-03 0.005797
                                                          0.059090
         1132
                 cam-1 0.393836 1.444158e-02 0.201850
                                                          0.268705
In [78]: vhl_ids = vhl_targets.ens_gene.unique()
        _ = tea.enrichment_analysis(vhl_ids,
                                    tissue_df, show=True)
         _ = tea.enrichment_analysis(vhl_ids,
                                    phenotype_df, show=False)
        [0].head(10)
Executing script
            Tissue Expected Observed Enrichment Fold Change P value \
 ADE WBbt:0005415 0.084783
                                     2
                                                     23.589744 0.000069
   Q value
0 0.017912
Executing script
Out [78]:
                                            Tissue Expected Observed \
         0 early larval arrest WBPhenotype:0000055
                                                    0.107692
                                                                     2.
           Enrichment Fold Change
                                    P value
                                              O value
         0
                        18.571429
                                   0.000149
                                             0.034665
    Identifying New Biology - understanding the role of rhy-1 and egl-9 in the hif-1
     dependent response
In [79]: df1.head()
            index Unnamed: 0 target id
Out [79]:
                                            pval
                                                       qval
         1
            11089
                        11090
                              2RSSE.1a 0.645621
```

```
se b '
                                         1.000000 0.325045 0.706845
                        AC3.10 0.284737 0.941480 -0.422590 0.395040
13
    5648
                5649
17
     225
                 226
                        AC3.2 0.000395 0.032654 -0.390064 0.110081
               11094 AC3.5a.1 0.692645 1.000000 0.271445 0.686737
20 11093
                2239 AC3.5a.2 0.077470 0.645159 -2.343688 1.327448
21
   2238
   mean_obs
            var_obs tech_var
                                                      se_b_e
                                            se_b_c
                                                               se_b_b
   2.553185 1.452565 0.481532
                                         -0.014713 0.778026 0.112480
13 3.090031 2.466209 0.056133
                                          0.235891 0.057975 - 0.267943
                                  . . .
17 5.625880 0.054498 0.004335
                                          0.005548 0.082966 -0.223640
                                  . . .
20 5.133816 7.740471 0.686008
                                  . . .
                                          0.232033 0.153005 -0.164163
21 4.484407 2.582413 1.790455
                                         -1.880010 -0.670477 -0.473572
                                  . . .
```

```
se_b_a se_b_d
                                                               q_b
                                         q_c
                                                    q_e
                                                                          q_a
              0.713097 \quad 0.090601 \quad 1.000000 \quad 0.697366 \quad 0.994068 \quad 0.683970 \quad 1.000000
         13 \ -0.458696 \ -0.008479 \ \ 0.942580 \ \ 0.998112 \ \ 0.872448 \ \ 0.608039 \ \ 1.000000
         17 - 0.057873 \quad 0.065041 \quad 1.000000 \quad 0.844141 \quad 0.259769 \quad 0.887128 \quad 0.988684
         20 - 0.004266 - 0.078161 \quad 0.989014 \quad 0.993105 \quad 0.983249 \quad 0.999848 \quad 1.000000
         21 - 0.290185 - 0.418795 0.683965 0.929625 0.962053 0.974710 1.000000
         [5 rows x 30 columns]
In [91]: ind = ((df1.q c < 0.1) & (df1.q e < 0.1) &
                (df1.q_b < 0.1) & (df1.q_a < 0.1) &
                 (df1.q d < 0.1))
         y = df1[ind]
         y.shape
Out[91]: (55, 30)
In [80]: y_bs = df1[ind][['b_e', 'b_b', 'b_d', 'b_c', 'b', 'b_a']]
         all_down = y_bs[y_bs<0].dropna().index</pre>
         all_down.shape
Out[80]: (103,)
In [86]: cols = ['ext_gene', 'ens_gene',
                  'b_e', 'b_b', 'b_d', 'b_c', 'b_a',
                  'q_e', 'q_b', 'q_d', 'q_c', 'q_a']
         sel = df1.index.isin(y_bs[y_bs<0].index)</pre>
         all_down = df1[sel][cols].sort_values('q_a')
         all_down.to_csv('.../output/all_down.csv', index=False)
In [87]: all_up = y_bs[y_bs>0].dropna().index
         print (all_up.shape)
         all_up = df1[df1.index.isin(all_up)][cols].sort_values('q_a')
         all_up.to_csv('../output/all_up.csv', index=False)
(127,)
In [92]: # What pops up on hover?
         tooltips = [('ext_gene', '@ext_gene'),
                        ('egl_qval', '@q_b')]
         # Make the hover tool
         hover = bokeh.models.HoverTool(tooltips=tooltips, names=['circles'])
         # Create figure
         p = bokeh.plotting.figure(plot_width=650,
                                      plot height=450)
```

 $q_d$ 

```
p.xgrid.grid_line_color = 'white'
p.ygrid.grid_line_color = 'white'
p.xaxis.axis_label = 'eql-9'
p.yaxis.axis label = r'Delta'
# Add the hover tool
p.add_tools(hover)
# Define colors in a dictionary to access them with
# the key from the pandas groupby funciton.
source1 = bokeh.models.ColumnDataSource(y)
transformed_q = np.sqrt(-y.q_c.apply(np.log))
cols = [
    "#%02x%02x%02x" % (int(r), int(g), int(b))
    for r, g, b, _ in
    255*mpl.cm.viridis(mpl.colors.Normalize()(transformed_q))
1
# Specify data source
p.circle(x='b_b', y=y.b_a -y.b_b, size=7,
         alpha=0.4, source=source1, color=cols, name='circles')
p.circle(x='b_b', y=y.b_a -y.b_b, size=7,
         alpha=1, fill_color=None, color='black', source=source1)
# create the coordinates for the errorbars
errx xs = []
errx_ys = []
for x, z, xerr in zip(y.b_b, y.b_a - y.b_b, y.se_b_b):
    errx_xs.append((x - xerr, x + xerr))
    errx_ys.append((z, z))
erry_xs = []
erry_ys = []
for x, z, yerr in zip(y.b_b, y.b_a - y.b_b,
                      np.sqrt(y.se_b_a**2 + y.se_b_b**2)):
    erry_xs.append((x, x))
    erry_ys.append((z - yerr, z + yerr))
# plot them
p.multi_line(errx_xs, errx_ys,color=cols, alpha=0.4)
p.multi_line(erry_xs, erry_ys, color=cols, alpha=0.4)
p.line([-10, 10], [0, 0], line_width=2, color='black')
```

```
p.background_fill_color = "#DFDFE5"
         p.background_fill_alpha = 0.5
         html = file_html(p, CDN, "my plot")
         HTML (html)
Out [92]: <IPython.core.display.HTML object>
In [ ]: from bokeh.plotting import figure
        from bokeh.resources import CDN
        from bokeh.embed import file_html
        # Display graphics in this notebook
       bokeh.io.output_notebook()
In [93]: # What pops up on hover?
         tooltips = [('ext_gene', '@ext_gene'),
                      ('hif_qval', '@q_c')]
         # Make the hover tool
         hover = bokeh.models.HoverTool(tooltips=tooltips, names=['circles'])
         # Create figure
         title = 'eql-9 is suppressed by the eql-9; hif-1 double mutant'
         p = bokeh.plotting.figure(title=title, plot_width=650,
                                   plot_height=450)
         p.xgrid.grid_line_color = 'white'
         p.ygrid.grid_line_color = 'white'
         p.xaxis.axis_label = 'eql-9'
         p.yaxis.axis_label = r'Delta'
         # Add the hover tool
         p.add_tools(hover)
         # Define colors in a dictionary to access them with
         # the key from the pandas groupby funciton.
         source1 = bokeh.models.ColumnDataSource(y)
         transformed_q = np.sqrt(-y.q_c.apply(np.log))
         cols = [
             "#%02x%02x%02x" % (int(r), int(g), int(b))
             for r, q, b, _ in
             255*mpl.cm.viridis(mpl.colors.Normalize()(transformed_q))
         1
         # Specify data source
         p.circle(x='b_b', y=y.b -y.b_b, size=7,
```

```
alpha=0.4, source=source1,
                  color=cols, name='circles')
         p.circle(x='b_b', y=y.b -y.b_b, size=7,
                  alpha=1, fill_color=None,
                  color='black', source=source1)
         # create the coordinates for the errorbars
         errx_xs = []
         errx_ys = []
         for x, z, xerr in zip(y.b_b, y.b - y.b_b, y.se_b_b):
             errx_xs.append((x - xerr, x + xerr))
             errx_ys.append((z, z))
         erry_xs = []
         erry_ys = []
         for x, z, yerr in zip(y.b_b, y.b - y.b_b,
                               np.sqrt(y.se_b\star2 + y.se_b_\star2)):
             erry_xs.append((x, x))
             erry_ys.append((z - yerr, z + yerr))
         # plot them
         p.multi_line(errx_xs, errx_ys, color=cols, alpha=0.4)
         p.multi_line(erry_xs, erry_ys, color=cols, alpha=0.4)
         p.line([-10, 10], [0, 0], line_width=2, color='black')
         p.line([-10, 10], [10, -10], line_width=1,
                line_dash=(4, 4), color='red')
         # p.circle(x='avg_b', y='logq', size=7,
                    alpha=0.2, source=source2, color='red')
         p.background_fill_color = "#DFDFE5"
         p.background_fill_alpha = 0.5
         html = file_html(p, CDN, "my plot")
         HTML (html)
Out [93]: <IPython.core.display.HTML object>
```