

# Genetic Analysis of a Metazoan Pathway using Transcriptomic Phenotypes

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**RNA-seq is commonly used to identify genetic modules that respond to a perturbation. Although transcriptomes have been mainly used for target gene discovery, the quantitative nature of these measurements makes them attractive structures with which to study genetic interactions. To understand whether whole-organism RNA-seq was suitable for genetic pathway reconstruction, we sequenced the transcriptome of four single mutants and two double mutants of the hypoxia pathway in *C. elegans*. Using principal component analysis or correlational analysis, we show that whole-organism transcriptomes contain sufficient information to identify genetic interactions. By comparing the expression levels of double mutants with their corresponding single mutants, we were able to determine, on a genome-wide level, that EGL-9 acts along VHL-1-dependent and independent branches to inhibit HIF-1. We were also able to observe genome-wide suppression of the *egl-9(lf)* phenotype in an *egl-9;hif-1(lf)* double mutant. We show that genes along a pathway tend to decorrelate as a result of alternative regulatory modes and crosstalk; and that this decorrelation accurately reflects functional distance between genes. As a by-product of our analysis, we predict 196 genes under the regulation of *hif-1*, and 44 genes under the regulation of *vhl-1*. Finally, we are able to identify 31 genes that exhibit non-canonical epistasis: for these genes, *vhl-1(lf)* mutants show opposing effects to *egl-9(lf)* mutants, but the *egl-9;vhl-1(lf)* exhibits the *egl-9(lf)* phenotype. We suggest that this non-canonical epistasis reflects unexplored aspects of the hypoxia pathway.**

genetics | RNA-seq | epistasis | hypoxia | transcriptomics | systems biology

**G**enetic analysis of molecular pathways has traditionally been performed through epistasis analysis. Epistasis indicates that two genes interact functionally; such interaction can involve the direct interaction of their products or the interaction of any consequence of their function (small molecules, physiological or behavioral effects) [1]. If two genes interact, and the mutants of these genes have a quantifiable phenotype, the double mutant of interacting genes will have a phenotype that is not the sum of the phenotypes of the single mutants that make up its genotype. Epistasis analysis remains a cornerstone of genetics today [2].

Recent developments in biology shifted in focus from studying single genes to studying all genes in parallel. In particular, RNA-seq [3] enables biologists to identify genes that change expression in response to a perturbation. Recent developments have improved the power and resolution of this technique by enabling deeper and more frequent sequencing due to lower sequencing costs [4]; better and faster abundance quantification [5–7]; as well as improved differential expression analysis methods [8, 9]. RNA-seq has been successfully used to identify genetic modules involved in a variety of processes, including T-cell regulation [10, 11], the *C. elegans* linker cell migration [12], or planarian stem cell maintenance [13, 14]. For

the most part, the role of transcriptional profiling has been restricted to target gene identification.

Although transcriptional profiling has been primarily used for descriptive purposes, transcriptomic phenotypes have been used to make genetic inferences previously. Microarray analyses in *S. cerevisiae* and *D. discoideum* showed that transcriptomes can be used to infer genetic relationships in simple eukaryotes [15, 16]. Also, eQTL studies in many organisms, including yeast, maize, *Caenorhabditis elegans*, *Drosophila melanogaster*, mice and humans have established the usefulness of transcriptomic phenotypes for population genetics studies [17–20]. In cell culture, single-cell RNA-seq has seen significant progress towards using transcriptomes as phenotypes with which to test genetic interactions [21, 22]. More recently, we have identified a new developmental state of *C. elegans* using whole-organism transcriptome profiling [23]. To investigate the ability of whole-organism transcriptomes to serve as quantitative phenotypes for epistasis analysis in metazoans, we sequenced the transcriptomes of four well-characterized loss of function mutants in the *C. elegans* hypoxia pathway [24–27].

Metazoans depend on the presence of oxygen in sufficient

## Significance Statement

Measurements of global gene expression are often used as descriptive tools capable of identifying genes that are downstream a perturbation. In theory, there is no reason why measurements of global transcriptomes could not be used as a quantitative phenotype for genetic analysis in multicellular organisms. In fact, qPCR measurements of single or a few reporter genes are already used to perform genetic network analysis. Here, we show that transcriptomes can be used for epistasis analysis in a metazoan, and that transcriptomes afford far more information per experiment than classic genetic analysis. By using transcriptomes as quantitative phenotypes, we can accurately predict interactions between genes, while at the same time identifying genes common to a pathway. When pathways branch, it is also possible to identify gene batteries that are associated with each end of the branch point. Finally, genes that would result in invisible visible phenotypes in an animal are not likely to be invisible at the transcriptome phenotype due to the exquisite granularity present in these structures, which represents an important advance towards studying small effect genes that make up the majority of animals' genetic repertoire.

DA, CPR and PWS designed the experiments. CPR selected the genes and extracted mRNA from all mutants. BW made the libraries. DA developed the genetic theory. DA wrote all computer code and performed all analyses. DA, CPR and PWS wrote the manuscript.

The authors declare no conflict of interest.

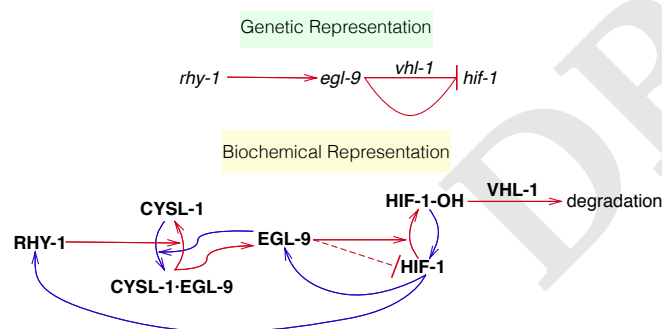
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concentrations to support aerobic metabolism. Genetic pathways evolved to rapidly respond to any acute or chronic changes in oxygen levels at the cellular or organismal level. These oxygen sensitive pathways are involved in a broad range of human pathologies and they have been subject to investigation biochemical and genetic approaches [28] that identified the Hypoxia Inducible Factors (HIFs) as an important group of oxygen responsive genes.

Hypoxia Inducible Factors are highly conserved in metazoans [29]. A common mechanism for hypoxia-response induction is heterodimerization between a HIF $\alpha$  and a HIF $\beta$  subunit. The heterodimer then initiates transcription of target genes [30]. The number and complexity of HIFs varies throughout metazoans, with humans having three HIF $\alpha$  subunits and two HIF $\beta$  subunits, whereas in the roundworm *Caenorhabditis elegans* (*C. elegans*) there is a single HIF $\alpha$  gene, *hif-1* [27] and a single HIF $\beta$  gene, *ahr-1* [31]. HIF target genes have been implicated in a wide variety of cellular and extracellular processes such as glycolysis, extracellular matrix modification, autophagy and immunity [28, 32–35].

Levels of HIF $\alpha$  proteins tend to be tightly regulated. Under conditions of normoxia, HIF-1 $\alpha$  exists in the cytoplasm and partakes in a futile cycle of continuous protein production and rapid degradation [36]. HIF-1 $\alpha$  is hydroxylated by three proline hydroxylases in humans (PHD1, PHD2 and PHD3) but is only hydroxylated by one proline hydroxylase (*egl-9*) in *C. elegans* [37]. HIF-1 hydroxylation increases its binding affinity to Von Hippel Lindau Tumor Suppressor 1 (VHL-1), which allows ubiquitination of HIF-1 leading to its subsequent degradation. In *C. elegans*, EGL-9 activity is inhibited by binding of CYSL-1, and CYSL-1 activity is in turn inhibited at the protein level by RHY-1, possibly by post-translational modifications to CYSL-1 [38] (see Fig. 1).



**Fig. 1.** Genetic and biochemical representation of the hypoxia pathway in *C. elegans*. Red arrows are arrows that lead to inhibition of HIF-1, and blue arrows are arrows that increase HIF-1 activity or are the result of HIF-1 activity. EGL-9 is known to exert *vhl-1*-dependent and independent repression on HIF-1 as shown in the genetic diagram. The *vhl-1*-independent repression of HIF-1 by EGL-9 is denoted by a dashed line and is not dependent on the hydroxylating activity of EGL-9.

Here, we show that transcriptomes contain robust signals that can be used to infer relationships between genes in complex metazoans by reconstructing the hypoxia pathway in *C. elegans* using RNA-seq. Furthermore, we show that the phenomenon of phenotypic epistasis, a hallmark of genetic interaction, holds at the molecular systems level. We also demonstrate that transcriptomes contain sufficient information, under certain circumstances, to order genes in a pathway using only single mutants. Finally, we were able to identify genes that appear to be downstream of *egl-9* and *vhl-1*, but do

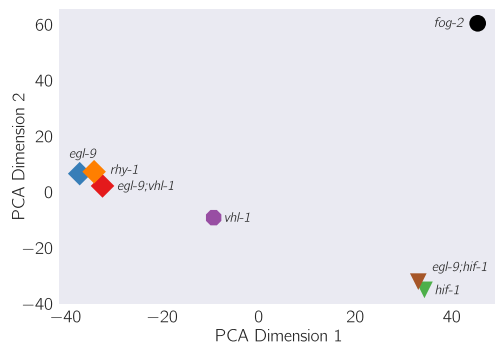
not appear to be targets of *hif-1*. Using a single set of genome-wide measurements, we were able to observe and quantitatively assess significant fraction of the known transcriptional effects of *hif-1* in *C. elegans*. A complete, interactive version of the analysis is also available at [www.wormlabcaltech.github.io/mpsq](http://www.wormlabcaltech.github.io/mpsq).

## Results

**The hypoxia pathway controls thousands of genes in *C. elegans*.** We performed whole-organism RNA-seq of the hypoxia pathway at a moderate sequencing depth ( $\sim 7$  million mapped reads for each individual replicate) under normoxic conditions. For single samples, we identified around 22,000 different isoforms per sample, which allowed us to measure differential expression of 18,685 isoforms across all replicates and genotypes (this constitutes  $\sim 80\%$  of the protein coding isoforms in *C. elegans*). We analyzed our data using a general linear model (see 1) on logarithm-transformed counts. Changes in gene expression are quantified via a regression coefficient,  $\beta$  which is specific to each isoform within a genotype. Statistical significance is achieved when the q-values for each  $\beta$  (p-values adjusted for multiple testing) are less than 0.1. Genes that are significantly altered between wild-type and a given mutant have  $\beta$  values that are statistically significantly different from 0. These coefficients are not equal to the average log-fold change per gene, although they are loosely related to this quantity. Larger magnitudes of  $\beta$  correspond to larger perturbations. These coefficients can be used to study the RNA-seq data in question.

In spite of the moderate sequencing depth, transcriptome profiling of the hypoxia pathway revealed that this pathway controls thousands of genes in *C. elegans*. The *egl-9(lf)* transcriptome showed differential expression of 1,807 genes, similarly to the 2,104 genes differentially expressed in *rhy-1(lf)* mutants. The *vhl-1(lf)* transcriptome showed considerably fewer differentially expressed genes (690), possibly reflecting the known fact that it is a weaker controller of *hif-1(lf)* than *egl-9(lf)* [26]. The *egl-9(lf);vhl-1(lf)* double mutant transcriptome showed 2,377 differentially expressed genes. The *hif-1(lf)* mutant also showed a transcriptomic phenotype involving 547 genes. The *egl-9;hif-1(lf)* double mutant showed a similar number of genes with altered expression (405).

**Principal Component Analysis visualizes epistatic relationships between genotypes.** Principal Component Analysis (PCA) is a well-known technique in bioinformatics that is used to identify relationships between high dimensional data points [39]. We performed PCA on our data to examine whether each genotype clustered in a biologically relevant manner. We expected *hif-1(lf)* to cluster near *egl-9;hif-1(lf)*, because *hif-1(lf)* exhibits no obvious phenotypes under normoxic conditions, in contrast to *egl-9(lf)*, which exhibits an egg-laying (Egl) phenotype in the same environment. *egl-9;hif-1(lf)* mutants suppress the Egl phenotype and exhibit the *hif-1(lf)* (wild-type) phenotype instead. On the other hand, we expected *egl-9(lf)*, *rhy-1(lf)*, *vhl-1(lf)* and *egl-9;vhl-1(lf)* to form a separate cluster since each of these genotypes is Egl and has a constitutive hypoxic response. Finally, we included as a negative control a *fog-2(lf)* mutant we have analyzed previously [23]. Since *fog-2* has not been described to interact with the hypoxia pathway, we expected that it should appear far away from either cluster.



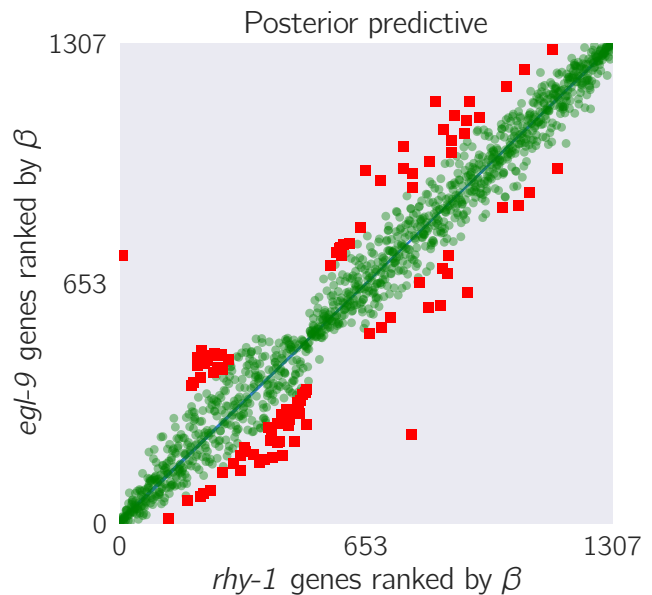
**Fig. 2.** Principal component analysis of various *C. elegans* mutants. Genotypes that have an activated hypoxia response (i.e., *egl-9(lf)*, *vhl-1(lf)*, and *rhy-1(lf)*) cluster far from *hif-1(lf)*. *hif-1(lf)* clusters with the suppressed *egl-9;hif-1(lf)* double mutant. The *fog-2(lf)* transcriptome, used as an outgroup, is far away from either cluster.

The first dimension of the PCA analysis was able to discriminate between HIF-1 positive and negative animals, whereas the second dimension was able to discriminate between mutants within the hypoxia pathway and outside the hypoxia pathway. Therefore expression profiling measures enough signal to cluster genes in a meaningful manner in complex metazoans.

**Reconstruction of the hypoxia pathway from first genetic principles.** Having shown that the signal in the mutants we selected was strong enough to cluster mutants using the regression coefficients, we set out to reconstruct the hypoxia pathway from first genetic principles. In general, to reconstruct a pathway, we must assess whether two genes act on the same phenotype (independence); then we must measure whether these genes act additively or epistatically on the measured phenotype; and if there is epistasis we must measure whether it is positive or negative, in order to assess whether the epistatic relationship is a genetic suppression or a synthetic interaction. As a first step towards reconstructing a pathway, we defined transcriptomic phenotypes as a set of genes or isoforms that are shared between two genes when these become mutated. Importantly, transcriptomic phenotypes are not directional—genes that are commonly altered between mutants need not be regulated in the same direction.

**Genes in the hypoxia mutant act on the same transcriptional phenotype.** We observed that all the hypoxia mutants had significant overlap between their differentially expressed transcriptomes relative to a wild-type control (fraction of shared transcriptomes ranged from a minimum of 78 genes shared between *hif-1(lf)* and *egl-9;hif-1(lf)* to a maximum of 1,468 shared genes between *egl-9(lf)* and *egl-9;vhl-1(lf)*). For comparison, we also analyzed a previously published *fog-2(lf)* transcriptome [23]. The *fog-2* gene is involved in masculinization of the *C. elegans* germline, which enables sperm formation, and is not known to be involved in the hypoxia pathway. The hypoxia pathway transcriptomes and the *fog-2(lf)* transcriptome overlapped (141–795 genes), but correlations between expression level changes were considerably weaker (see below), suggesting that there is at most only minor cross-talk between these pathways.

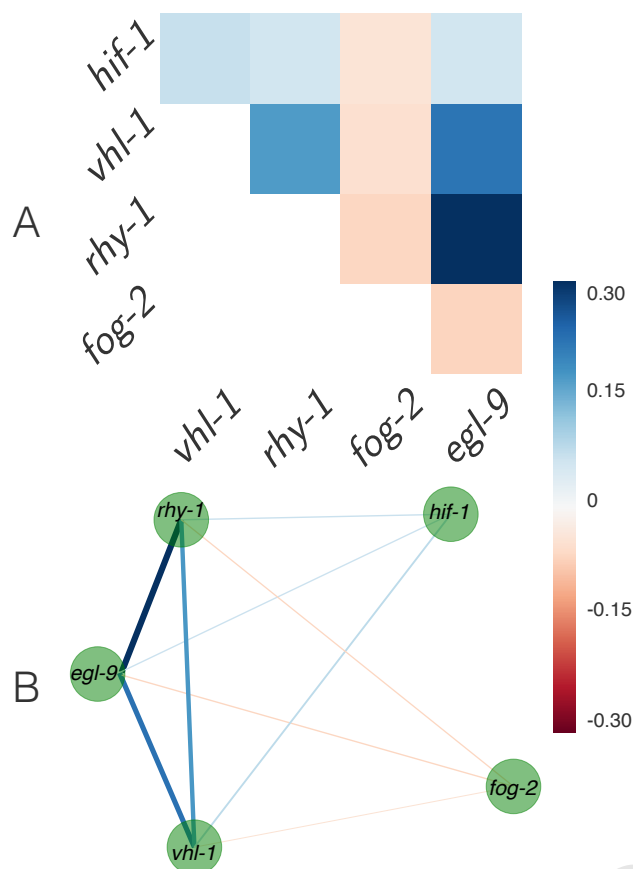
Although overlapping transcriptomes may be enough to conclude that a set of mutants share a phenotype, we wanted to know whether it was informative to look at quantitative agreement between perturbations. We rank-transformed the regression coefficients  $\beta$  for each transcriptome, and calculated



**Fig. 3.** Strong transcriptional correlations can be identified between genes that share a positive regulatory connection. We took the *egl-9(lf)* and the *rhy-1(lf)* transcriptomes, identified differentially expressed genes common to both transcriptomes and ranked each gene according to its differential expression coefficient  $\beta$ . We plotted the rank of each gene in *rhy-1(lf)* versus the rank of the same gene in the *egl-9(lf)* transcriptome. The result is an almost perfect correlation. Green, transparent large points mark inliers to the primary regressions (blue lines); red squares mark outliers to the primary regressions.

lines of best fit using bayesian regression with a Student-T distribution to mitigate noise from outliers (see Fig 3). For transcriptomes associated with the hypoxia pathway, we found that these correlations tended to have values higher than 0.9 with a tight distribution around the line of best fit. The correlations for mutants from the hypoxia pathway with the *fog-2(lf)* mutant were considerably weaker, with magnitudes between 0.6–0.85 and a greater variance around the line of best fit. Although *hif-1* is known to be genetically repressed by *egl-9*, *rhy-1* and *vhl-1* [24, 25], all the correlations between mutants of these genes and *hif-1(lf)* were positive. The overlap between *hif-1(lf)* and all other mutants was small, and each overlap involved different sets of genes, which suggests that we did not sequence deeply enough to identify the nature of these positive interactions. After we calculated the pairwise correlation between each transcriptome, we weighted the result of each regression by the number of differentially expressed isoforms shared by two transcriptomes and divided by the total number of differentially expressed isoforms present in the two transcriptomes,  $N_{\text{overlap}}/N_{g1 \cup g2}$ . The weighted regressions recapitulated a network with three ‘modules’: A control module, a responder module and an uncorrelated module (see Fig. 4). We identified a strong positive interaction between *egl-9(lf)* and *rhy-1(lf)*. The magnitude of this weighted correlation derives from the magnitude of the transcriptomes for these mutants (1,807 and 2,104 differentially expressed genes respectively) and the overlap between both genes was extensive, which makes the weighting factor considerably larger than other pairs. The weak correlation between *hif-1(lf)* and *egl-9(lf)* results from the small size of the *hif-1(lf)* transcriptome and the small overlap between the transcriptomes. The

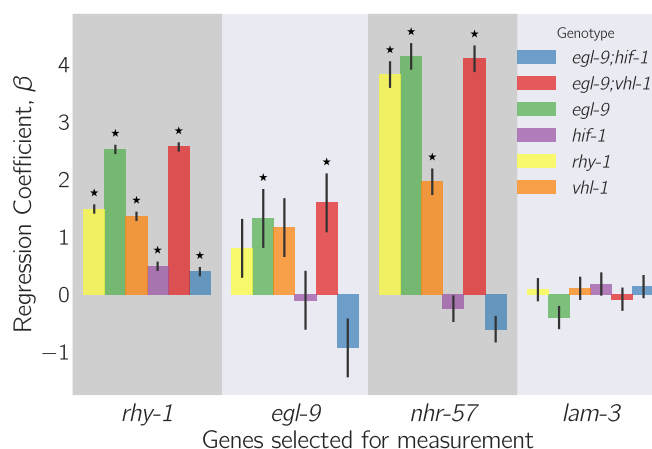
fine-grained nature of transcriptional phenotypes means that these weighted correlations between transcriptomes of single mutants are predictive of genetic interaction.



**Fig. 4. A:** Heatmap showing pairwise regression values between all single mutants. **B:** Correlation network drawn from the diagram. Edge width is proportional to the logarithm of the magnitude of the weighted correlation between two nodes divided by absolute value of the weighted correlation value of smallest magnitude. Edges are also colored according to the heatmap in A.

**A quality check of the transcriptomic data reveals excellent agreement with the literature.** One way to establish whether genes are acting additively or epistatically to each other is to perform qPCR of a reporter gene in the single and double mutants. This approach was used to successfully map the relationships within the hypoxia pathway (see, for example [25, 26]). A commonly used reporter is *nhr-57*, which is known to exhibit a several-fold increase in mRNA expression when HIF-1 accumulates [25, 34, 40, 41]. Likewise, HIF-1 is known to increase transcription of *rhy-1* and *egl-9* [42].

Our dataset enables us to perform an equivalent computational experiment to qPCR by selectively looking at expression of a few genes at a time. Therefore, we queried the changes in expression of *rhy-1*, *egl-9*, *nhr-57*. We included *lam-3* as a representative negative control. In our dataset, *nhr-57* is upregulated in *egl-9(lf)*, *rhy-1(lf)* and *vhl-1(lf)*, but remains unchanged in *hif-1(lf)*. *egl-9;vhl-1(lf)* had an expression level similar to *egl-9(lf)*; whereas the *egl-9;hif-1(lf)* mutant showed wild-type levels of the reporter expression, as reported previously [25].



**Fig. 5. Top:** *In silico* qPCR. We extracted four genes (*rhy-1*, *egl-9*, *nhr-57* and *lam-3*, shown on the x-axis) and plotted their regression coefficients,  $\beta$ , as measured for every genotype (represented by one of six colors) to study the epistatic relationships between each gene. Stars above a bar represent a regression coefficient statistically significantly different from 0, meaning that expression is altered relative to a wild-type control. Error bars show standard error of the mean value of  $\beta$ . *nhr-57* is an expression reporter that has been used previously to identify *hif-1* regulators [25, 26]. The *nhr-57* mRNA levels replicate what is observed in the literature. *lam-3* is shown here as a negative control that should not be altered by mutations in this pathway. The increases in the levels of *egl-9* and *rhy-1* when repressors of *hif-1* are knocked out are in agreement with previous literature [42]. We measured modest increases in the levels of *rhy-1* mRNA when *hif-1(lf)* is knocked out. The mechanism behind this is unclear. Negative and positive feedback loops from *hif-1* into its inhibiting genes could be a homeostatic mechanism.

We also performed *in silico* qPCR of every gene under scrutiny to get a clearer idea of the relationships between them (see Fig. 5). We observed changes in *rhy-1(lf)* expression consistent with previous literature [25] when HIF-1 accumulates. We also observed changes in *egl-9* expression in *egl-9(lf)*. *egl-9* is known as a hypoxia responsive gene [42]. Although changes in *egl-9* expression were not statistically significantly different from the wild-type in *rhy-1(lf)* and *vhl-1(lf)* mutants, the mRNA levels of *egl-9* still trended towards increased expression in these genotypes. As with *nhr-57*, *egl-9* and *rhy-1* expression was wild-type in *egl-9;hif-1(lf)*; whereas *egl-9;vhl-1(lf)* mutant showed expression phenotypes identical to *egl-9(lf)*. This dataset also showed that knockout of *hif-1* resulted in a modest increase in the levels of *rhy-1*. This suggests that *hif-1*, in addition to being a positive regulator of *rhy-1*, also inhibits it, which constitutes a novel observation. Taken together, these results indicate that RNA-seq data is equivalent to qPCR for purposes of comparing gene expression of a reporter between genotypes. Using a single reporter we would have been able to reconstruct an important fraction of the genetic relationships between the genes in the hypoxia pathway.

**Genome-wide epistasis.** Although it may be sufficient to extract the regression coefficients of a known reporter gene and use it to rebuild a genetic pathway, we felt that by relying on just a single gene, or even a handful of genes to rebuild the pathway we discarded most of the valuable information present in RNA-seq datasets. Therefore, we decided to explore a new epistasis metric—genome-wide epistasis.

Ideally, any measurement of genome-wide epistasis should conform to certain expectations. First, it should make use



of the regression coefficients of as many genes as possible. Second, it should be summarizable in a single, well-defined number. Third, it should have an intuitive behavior, such that the special values of the statistic (maximum, minimum, zero) should have an unambiguous interpretation.

One way of defining genome-wide epistasis is to plot transcriptome data onto an epistasis plot. In an epistasis plot, the X-axis represents the expected expression of a double mutant  $X^-Y^-$  if  $X$  and  $Y$  interact additively. In other words, it is the sum of the regression coefficients for an isoform calculated from the single mutants  $X^-$  and  $Y^-$ . The Y-axis represents the deviations from the additive (null) model, and can be calculated as the difference between the observed regression coefficient and the predicted regression coefficient. Only genes that are differentially expressed in all three genotypes are plotted.

Epistasis plots can be understood intuitively for simple cases of genetic interactions. If two genes act additively on the same set of differentially expressed isoforms then all the plotted points will fall along the line  $y = 0$ . If two genes interact in a single, unbranched pathway, then  $X^-$  and  $Y^-$  should have identical phenotypes for  $X^-$ ,  $Y^-$  and  $X^-Y^-$ , if all the genotypes are homozygous for complete loss of function mutations [1]. It follows that the data points should fall along a line with slope equal to  $-\frac{1}{2}$ . On the other hand, in the limit of complete inhibition of  $Y$  by  $X$ , the plots should show a line of best fit with slope equal to  $-1$ <sup>1</sup>. Genes that have a synthetic interaction between them will fall along lines with slopes  $> 0$ . When there is epistasis of one gene over another, the points will fall along a line of best fit with slope  $s_{XY=Y}$  or  $s_{XY=X}$ . This slope must be determined from the single-mutant data. From this information, we can use the single mutant data to predict the distribution of slopes that results for each case stated above, as well as for each epistatic combination ( $X^-Y^- = X^-$  or  $X^-Y^- = Y^-$ ). Given the biological relevance of the slope of the lines of best fit to the biological relationship between the genes under study, we refer to it as the genome-wide epistasis coefficient ( $s_{X,Y}$ ), because it integrates information from many different genes into a single number (see Fig. 6).

In our experiment, we studied two double mutants, *egl-9;hif-1(lf)* and *egl-9;vhl-1(lf)*. We wanted to understand how well the global epistasis agreed with the literature based on qPCR of single reporters. Therefore, we performed orthogonal distance regression on to the two gene combinations we studied (*egl-9* and *vhl-1*; and *egl-9* and *hif-1*) to determine the epistasis coefficient for each gene pair. We also generated models for the epistasis cases mentioned above using the single mutant data. For every simulation, as well as for the observed data, we used bootstraps to generate probability distributions of the epistasis coefficients.

When we compared the predictions for the genome-wide epistasis coefficient,  $s_{egl-9,vhl-1}$  under different assumptions with the observed slope ( $-0.42$ ). We observed that the predicted slope matched the simulated slope for the case where *egl-9* is epistatic over *vhl-1* ( $egl-9(lf) = egl-9;vhl-1(lf)$ , see Fig. 6) and did not overlap with any other prediction. Next, we predicted the distribution of  $s_{egl-9,hif-1}$  for different pathways and contrasted with the observed slope. In this case,

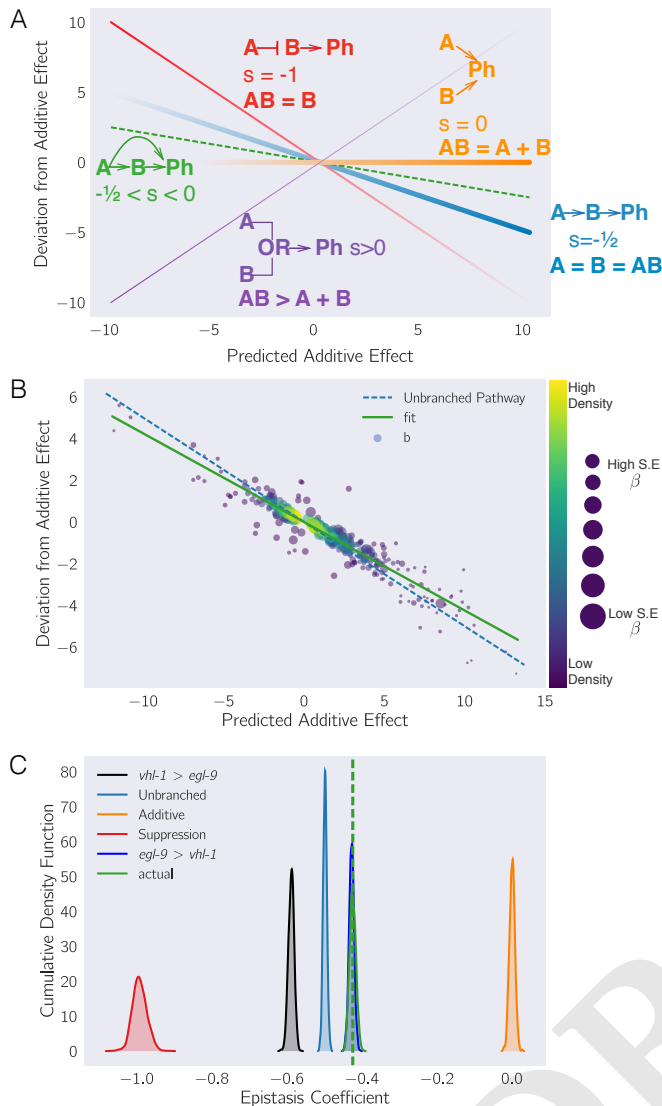
we saw that the uncertainty in the observed coefficient overlapped significantly with the strong suppression model, where EGL-9 strongly suppresses HIF-1, and also with the model where  $hif-1(lf) = egl-9;hif-1(lf)$ . In this case, both models are reasonable—HIF-1 is strongly suppressed by EGL-9, and we know from previous literature that the epistatic relationship,  $hif-1(lf) = egl-9;hif-1(lf)$ , is true for these mutants. In fact, as the repression of HIF-1 by EGL-9 becomes stronger, the epistatic model should converge on the limit of strong repression.

Another way to test which model best explains the epistatic relationship between *egl-9* and *vhl-1* is to use bayesian model selection to calculate an odds ratio between two models to explain the observed data. Models can be placed into two categories: parameter-free and fit. Parameter free models are ‘simpler’ because their parameter space is smaller (0 parameters) than the fit models ( $n$  parameters). By Occam’s razor, simpler models should be preferred to more complicated models. However, simple models suffer from the drawback that systematic deviations from them cannot be explained or accommodated, whereas more complicated models can alter the fit values to maximize their explanatory power. In this sense, more complicated models should be preferred when the data shows systematic deviations from the simple model. Odds-ratio selection gives us a way to quantify the trade-off between simplicity and explanatory power.

We reasoned that comparing a fit model ( $y = \alpha \cdot x$ , where  $\alpha$  is the slope of best fit) against a parameter-free model ( $y = \gamma \cdot x$ , where  $\gamma$  is a single number) constituted a conservative approach towards selecting which theoretical model (if any) best explained the data. In particular, this approach will tend to strongly favor the line of best fit over simpler model for all but very small, non-systematic deviations. We decided that we would reject the theoretical models only if the line of best-fit was  $10^3$  times more likely than the theoretical models (odds ratio,  $OR > 10^3$ ). Comparing the odds-ratio between the line of best fit and the different pathway models for *egl-9* and *vhl-1* showed similar results to the simulation. Only the theoretical model  $egl-9(lf) = egl-9;vhl-1(lf)$  could not be rejected ( $OR = 0.46$ ), whereas all other models were significantly less likely than the line of best fit ( $OR > 10^{44}$ ). Therefore, *egl-9* is epistatic to *vhl-1*. Moreover, since  $s_{egl-9,vhl-1}$  is strictly between and not equal to 0 and  $-0.5$ , we conclude that *egl-9* acts on its transcriptomic phenotype in *vhl-1*-dependent and independent manners. A branched pathway that can lead to epistasis coefficients in this range is a pathway where *egl-9* interacts with its transcriptomic phenotype via branches that have the same valence (both positive or both negative) [26]. When we performed a similar analysis to establish the epistatic relationship between *egl-9* and *hif-1*, we observed that the best alternative to a free-fit model was a model where *hif-1* is epistatic over *egl-9* ( $OR = 2551$ ), but the free-fit model was still preferred. All other models were strongly rejected ( $OR > 10^{25}$ ).

**Epistasis can be predicted.** Given our success in measuring epistasis coefficients, we wanted to know whether we could predict the epistasis coefficient between *egl-9* and *vhl-1* in the absence of the *egl-9(lf)* genotype. Since RHY-1 activates EGL-9, the *rhy-1(lf)* transcriptome should contain more or less equivalent information to the *egl-9(lf)* transcriptome. Therefore, we generated predictions of the epistasis coefficient between *egl-9*

<sup>1</sup>Specifically, this follows from assuming that  $Y^-$  is wild-type under the conditions assayed; and  $X^-Y^- = Y^- = \text{wild-type}$



**Fig. 6. (A)** Schematic diagram of an epistasis plot. The X-axis on an epistasis plot is the expected coefficient for a double mutant under an additive model (null model). The Y-axis plots deviations from this model. Double mutants that deviate in a systematic manner from the null model exhibit genome-wide epistasis ( $s$ ). To measure  $s$ , we perform a linear regression on the data. The slope of the line of best fit is  $s$ . This coefficient is related to genetic architectures. Genes that act additively on a phenotype (**Ph**) will have  $s = 0$ ; whereas genes that act along a single unbranched pathway will have  $s = -1/2$ . Strong repression is reflected by  $s = -1$ . Cases where  $s > 0$  correspond to synthetic interactions, and in the limit as  $s \rightarrow \infty$ , the synthetic interaction must be an OR-gate. Cases where  $0 < s < -1/2$  correspond to circuits that have multiple positive branches; whereas cases where  $-1/2 < s < -1$  correspond to cases where the branches have different valence. Cases where  $s < -1$  represent inhibitory branches. **(B)** Epistasis plot showing that the *egl-9;vhl-1(lf)* transcriptome deviates significantly from a null additive. Points are colored qualitatively according to density (purple—low, yellow—high) and size is inversely proportional to the standard error of the y-axis (larger points, higher accuracy). The purple line is the line of best fit from an orthogonal distance regression. **(C)** Comparison of simulated epistatic coefficients against the observed coefficient. Green curve shows the bootstrapped observed genome-wide epistasis coefficient for *egl-9* and *vhl-1*. Dashed green line shows the mean value of the data. Using the single mutants, we simulated coefficient distributions for a linear model (light blue, centered at  $-0.5$ ); an additive model (orange, centered at  $0$ ); a model where either *egl-9* or *vhl-1* masks the other phenotype (dark blue and black, respectively) and a complete suppression model (red, centered at  $-1$ ). The observed coefficient overlaps the predicted epistasis curve for *egl-9;vhl-1(lf) = egl-9(lf)* (green and dark blue).

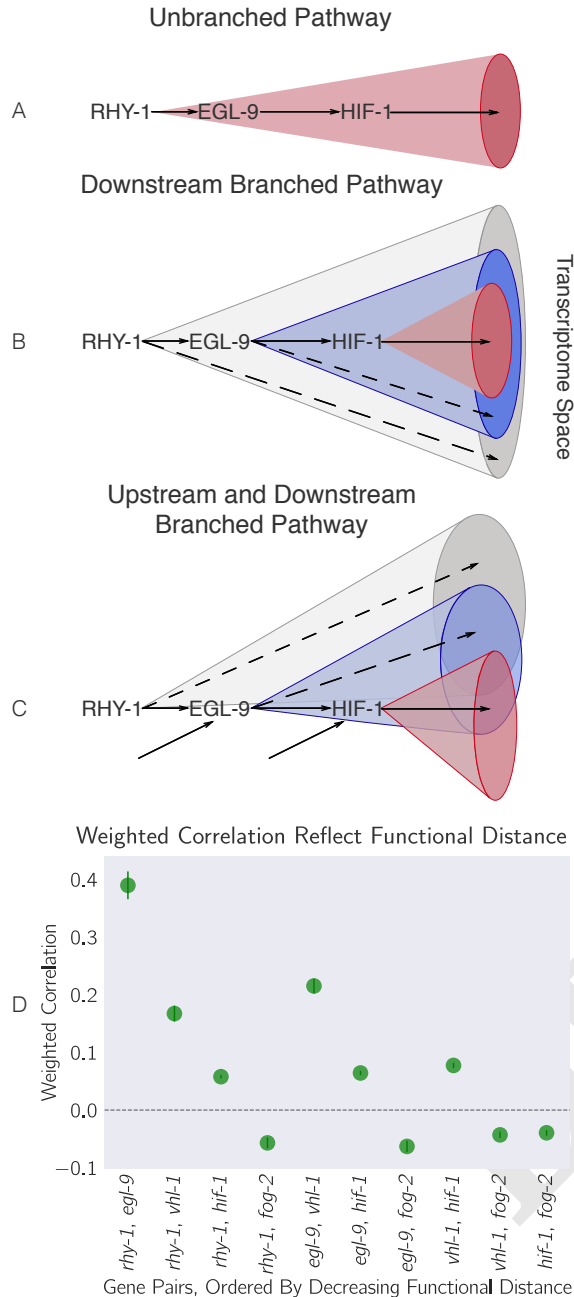
and *vhl-1* by substituting in the *rhy-1(lf)* data. We predicted  $s_{rhy-1,vhl-1} = -0.45$ . Similarly, we used the *egl-9;vhl-1(lf)* double mutant to measure the epistasis coefficient while replacing the *egl-9(lf)* dataset with the *rhy-1(lf)* dataset. We found that the epistasis coefficient using this substitution was  $-0.40$ . This coefficient was different from  $-0.50$  ( $OR > 10^{62}$ ), reflecting the same qualitative conclusion that the hypoxia pathway is branched. In conclusion, we were able to obtain a quantitatively close prediction of the epistasis coefficient for two mutants using the transcriptome of a related, upstream mutant. Finally, we showed that in the absence of a single mutant, an upstream locus can under some circumstances be used to estimate epistasis between two genes.

**Transcriptomic decorrelation can be used to infer functional distance.** Can RNA-seq be used to identify functional interactions within a genetic pathway? Although there is no *a priori* reason why global gene expression should reflect functional interactions, the strength of the unweighted correlations between genes in the hypoxia pathway made us wonder how much information can be extracted from this dataset. Single genes are often regulated by multiple independent sources. The connection between two nodes can in theory be characterized by the strength of the edges connecting them (the thickness of the edge); the fraction of sources that regulate both nodes (the fraction of common inputs); and the fraction of genes that are regulated by both nodes (the fraction of common outputs). In other words we expected that expression profiles associated with a pathway would respond quantitatively to quantitative changes in activity of the pathway. Targeting a pathway at multiple points would lead to expression profile divergence as we compare nodes that are separated by more degrees of freedom, reflecting the flux in information between them.

We investigated the possibility that transcriptomic signals do in fact contain relevant information about the degrees of separation by weighting the robust bayesian regression between each pair of genotypes by  $N_{Intersection}/N_{Union}$ . We plotted the weighted correlation of each gene pair, ordered by increasing functional distance (see Fig. 7). In every case, we see that the weighted correlation decreases monotonically due mainly, but not exclusively, to decreasing  $N_{Overlap}$ . We believe that this result is not due to random noise or insufficiently deep sequencing. Instead, we propose a framework in which every gene is regulated by multiple different molecular species, which induces progressive decorrelation. This decorrelation in turn has two consequences. First, decorrelation within a pathway implies that two nodes may be almost independent of each other if the functional distance between them is large. Second, it may be possible to use decorrelation dynamics to infer gene order in a pathway, as we have done with the hypoxia pathway<sup>2</sup>.

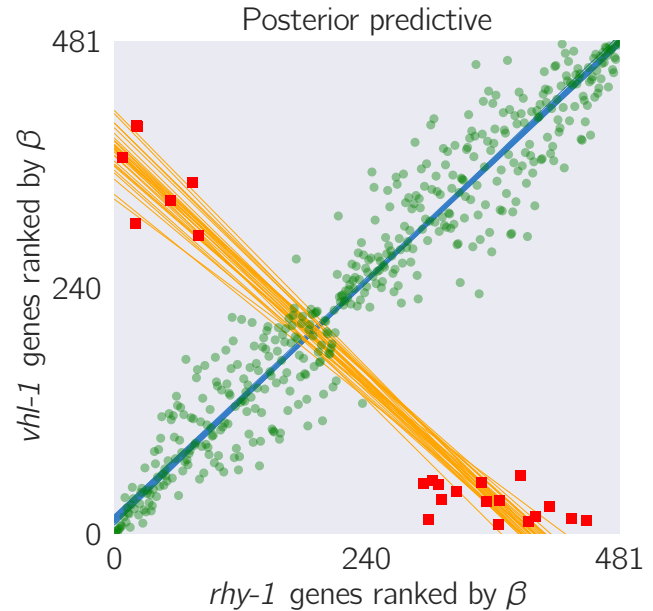
**The circuit topology of the hypoxia pathway explains patterns in the data.** We noticed that while some of the rank-plots contained a clear positive correlation (see Fig. 3), some of the other rank-plots showed a discernible cross-pattern (see Fig. 8). In particular, this cross-pattern emerged between *vhl-1(lf)* and *rhy-1(lf)* or between *vhl-1(lf)* and *egl-9(lf)*, even

<sup>2</sup>An important question is whether a looped circuit like the hypoxia pathway can be ordered in the way we have ordered it in Fig. 7 since a loop does not technically have a beginning. One explanation is that we studied the hypoxia pathway under normoxic conditions, and therefore the control of *hif-1* over *rhy-1* and *egl-9* is weak, effectively turning the looped pathway into a linear one. Probably, under hypoxic conditions the pathway would effectively be reversed.



**Fig. 7.** Theoretically, transcriptomes can be used to order genes in a pathway under certain assumptions. Arrows in the diagrams above are intended to show the direction of flow, and do not indicate valence. **A** A linear pathway in which *rhy-1* is the only gene controlling *egl-9*, which in turn controls *hif-1* does not contain information to infer the order between genes. **B** If *rhy-1* and *egl-9* have transcriptomic effects that are separable from *hif-1*, then the *rhy-1* transcriptome should contain contributions from *egl-9*, *hif-1* and *egl-9*- and *hif-1*-independent pathways. This pathway contains enough information to infer order. **C** If a pathway is branched both upstream and downstream, transcriptomes will show even faster decorrelation. Nodes that are separated by many edges may begin to behave almost independently of each other with marginal transcriptomic overlap or correlation. **D** The hypoxia pathway can be ordered according to functional distance. We hypothesize the rapid decay in correlation is due to a mixture of upstream and downstream branching that happens along this pathway. Bars show the standard error of the weighted coefficient from the Monte Carlo Markov Chain computations.

though genetically *vhl-1*, *rhy-1* and *egl-9* are all inhibitors of *hif-1(lf)*. We reasoned that it could be possible that these cross-patterns reflected multiple interaction modes between genes. Therefore, we hypothesized that patterns in the rank-plots contained valuable information for decoding more interactions in our circuit.



**Fig. 8.** **Top:** A feedback loop can generate transcriptomes that are both correlated and anti-correlated. **Bottom:** *hif-1(lf)* transcriptome correlated to the *rhy-1(lf)* transcriptome. Green large points are inliers to the first regression. Red squares are outliers to the first regression. Only the red small points were used for the secondary regression. Blue lines are representative samples of the primary bootstrapped regression lines. Orange lines are representative samples of the secondary bootstrapped regression lines.

If the logic above is correct, then it should be possible to decouple transcriptomes in a logically consistent way. Currently, transcriptomes are decoupled via subtractive logic. In other words, to identify the *rhy-1*-specific transcriptome (the effects of *rhy-1* not dependent on *egl-9*), subtractive logic might suggest to find the overlap between the two transcriptomes. The genes that are differentially expressed but are not in the overlap would then be considered *rhy-1*-specific transcriptomes. Such a gene set would consider of almost 700 genes. However, this approach suffers from a number of drawbacks, principally that it does not take into account the relationship between the two genes in question. Moreover, these genes have no testable properties: i.e., a gene might not be in the overlap because it was not identified due to chance in one of the two transcriptomes. In aggregate, there is no pattern that is present in these genes that can be used to identify them beyond overlapping the two transcriptomes.

*rhy-1* and *egl-9* share a well-defined relationship. RHY-1 inhibits CYSL-1, which in turn inhibits EGL-9 [38]. Therefore, loss of RHY-1 leads to inactivation of EGL-9, which leads to increase in the cellular levels of HIF-1. HIF-1 in turn causes the mRNA levels of *rhy-1* and *egl-9* to increase, as they are involved in the *hif-1*-dependent hypoxia response. However, since *rhy-1* has been mutated, the observed transcriptome is RHY-1 ‘null’; EGL-9 ‘null’; HIF-1 ‘on’. The situation is similar

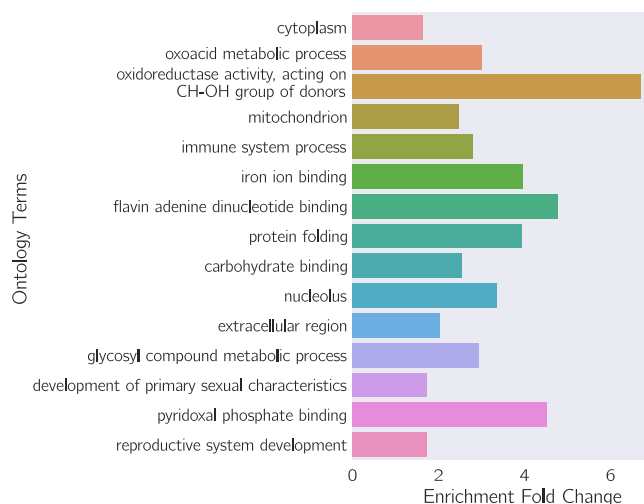
for *egl-9(lf)*, except that RHY-1 is not inactive, and therefore the observed transcriptome is the result of RHY-1 ‘up’; EGL-9 ‘null’; and HIF-1 ‘on’. From this pattern, we conclude that the *egl-9(lf)* and *rhy-1(lf)* transcriptomes should exhibit a cross-pattern when plotted against each other: The positive arm of the cross is the result of the EGL-9 ‘null’; HIF-1 ‘on’ dynamics; and the negative arm reflects the different direction of RHY-1 activity between transcriptomes. No negative arm is visible (with the exception of two outliers, which are annotated as pseudogenes in WormBase). Therefore, it is likely that a large portion or possibly all the transcriptomic effects of RHY-1 in this dataset are downstream of *egl-9(lf)*.

Using this approach, we identified a main hypoxia response induced by disinhibiting *hif-1* (356 genes). Although the hypoxic response is likely to involve between three and seven times more genes, this is a conservative estimate that minimizes false negative results, since these changes were identified in four different genotypes with three replicates each. This response included six transcription factors (*F17C11.1*, *nhr-57*, *ztf-18*, *W02D7.6* and *dmd-9*).

*hif-1*-independent effects of *egl-9* have been reported previously [41], which led us to question whether we could identify similar effects in our dataset. We have observed that *hif-1(lf)* leads to a modest increase in the transcription of *rhy-1*, from which we speculated that EGL-9 would have increased activity in the *hif-1(lf)* mutant than in the wild-type. Therefore, we searched for genes that were regulated in an opposite manner between *hif-1(lf)* and *egl-9;hif-1(lf)*, and that were regulated in the same direction between the *egl-9;hif-1(lf)* and *egl-9(lf)* (and *rhy-1(lf)*) mutants. We were able to find 126 genes that obeyed this pattern (see Supplementary Information). We also identified a *vhl-1*-specific response, comprising 44 genes. We searched for candidates directly regulated by *hif-1*. Initially, we generated this list using the most stringent pattern matching, but this revealed only three genes (*R08E5.3*, *R08E5.1.1* and *nit-1*). A relaxed set of conditions (target genes should go up in all mutants that induce HIF-1, and should not be up in *hif-1(lf)*) identified 196 candidate genes for direct regulation.

**Enrichment analysis of the hypoxia response.** In order to validate that our transcriptomes were correct, and to understand how functionalities may vary between them, we subjected each decoupled response to enrichment analysis using the WormBase Enrichment Suite [43, 44].

We used gene ontology enrichment analysis (GEA) on the main hypoxia response program. This showed that the terms ‘oxoacid metabolic process’ ( $q < 10^{-4}$ , 3.0 fold-change, 24 genes), ‘iron ion binding’ ( $q < 10^{-2}$ , 3.8 fold-change, 10 genes), and ‘immune system process’ ( $q < 10^{-3}$ , 2.9 fold-change, 20 genes) were significantly enriched. GEA also showed enrichment of the term ‘mitochondrion’ ( $q < 10^{-3}$ , 2.5 fold-change, 29 genes) (see Fig. 9). Indeed, *hif-1(lf)* has been implicated in all of these biological and molecular functions [40, 45–47]. As benchmark on the quality of our data, we selected a set of 22 genes known to be responsive to HIF-1 levels from the literature and asked whether these genes were present in our hypoxia response list. We found 8/22 known genes, which constitutes a statistically significant result ( $p < 10^{10}$ ). The small number of reporters found in this list probably reflects the conservative nature of our estimates. We also analyzed the list of predicted HIF-1 direct targets. GEA revealed that this list was significantly enriched in ‘immune system pro-



**Fig. 9.** Gene ontology enrichment analysis of genes associated with the main hypoxia response. A number of terms reflecting catabolism and bioenergetics are enriched.

cess’ ( $q < 10^{-5}$ , 5.7 fold-change, 15 genes) and ‘carbohydrate binding’ ( $q < 10^{-4}$ , 13 genes). Multiple terms involving enzymatic activities were enriched ( $q < 10^{-1}$ ) as well as ‘oxoacid metabolic process’ ( $q < 10^{-1}$ , 3 genes), suggesting that this gene list is enriched for enzymes. When we analyzed the *hif-1*-independent, *egl-9*-dependent transcriptome, we found genes that were enriched in programmed cell death, as well as ribosomal constituents. Phenotype enrichment analysis suggested that germline defects were enriched in this gene list, and tissue enrichment analysis singled out the P<sub>1</sub> and P<sub>3</sub> cells as significantly enriched. We studied the *hif-1*-independent, *vhl-1*-dependent gene set using enrichment analysis terms were significantly enriched.

**Identification of non-classical epistatic interactions.** *hif-1(lf)* has traditionally been viewed as existing in a genetic OFF state under normoxic conditions. However, our dataset indicates that 547 genes show altered expression when it is removed in normoxic conditions. Moreover, we observed positive genome-wide expression correlations between *hif-1(lf)* expression levels and *egl-9(lf)*, *vhl-1(lf)* and *rhy-1(lf)* expression levels in spite of the negative regulatory relationships between these genes and *hif-1*. Such positive relationships could indicate a different relationship between these genes than has previously been reported. We wanted to explore whether these genome-wide positive correlations were substantiated by epistasis analyses.

To perform epistasis analyses, we first identified genes that exhibited violations of the canonical genetic model of the hypoxia pathway. To this end, we searched for genes that exhibited different behaviors between *egl-9(lf)* and *vhl-1(lf)*, or between *rhy-1(lf)* and *vhl-1(lf)* (we assume that all results from the *rhy-1(lf)* transcriptome reflect a complete loss of *egl-9* activity). We found 31 that satisfied this condition (see Fig. 10). Additionally, many of these genes exhibited new kinds of epistasis. Namely, *egl-9* was epistatic over *vhl-1*. Identification of a set of genes that have a consistent set of relationships with between themselves suggests that we have identified a new aspect of the hypoxia pathway.

In particular, we focused on three genes, *nlp-31*, *ftn-1* and *ftn-2*, which epistasis patterns that we felt reflected the popu-





of the hypoxia response. *fum-1* catalyses the reaction of fumarate into malate, and complex II catalyses the reaction of succinate into fumarate. Complex II has been identified as a source of reserve respiratory capacity in neonatal rat cardiomyocytes previously [49]. We found two energy reserve genes that were down-regulated by HIF-1. *aagr-1* and *aagr-2*, which are predicted to function in glycogen catabolism [50] were both down-regulated in all the relevant mutants. Three distinct genes involved in energy reserve were up-regulated. These genes were *ogt-1*, an O-linked GlcNAc Transferase; *T04A8.7*, an ortholog of human glucosidase acid beta (GBA); and *T22F3.3*, an ortholog of human glycogen phosphorylase isozymes.

**Protein synthesis and degradation.** *hif-1(lf)* is also known to inhibit protein synthesis and translation in varied ways. HIF-1 is known to control the translational machinery indirectly via inhibition of mTOR [51]. However, most reported effects of HIF-1 on the translation machinery are posttranslational, and no reports to date show decreases in transcription of the ribosomal machinery in *C. elegans*. We used the WormBase Enrichment Suite Gene Ontology dictionary [44] to extract 143 protein-coding genes annotated as ‘structural constituents of the ribosome’ and we queried whether they were differentially expressed in our mutants. *egl-9(lf)*, *vhl-1(lf)*, *rhy-1(lf)* and *egl-9(lf);vhl-1(lf)* showed differential expression of 91 distinct ribosomal constituents (not all constituents were detected in all genotypes). For every one of these genotypes, these genes were always down-regulated. In contrast, *hif-1(lf)* showed up-regulation of a single ribosomal constituent.

Next, we asked whether HIF-1 has any transcriptional effects on the proteasomal constituents, because no such effects of HIF-1 on the proteasome have been reported in *C. elegans*. Out of 40 WormBase annotated proteasomal constituents, we found 31 constituents that were differentially expressed in at least one of the four genotypes that induce a hypoxic response. Every gene we found was down-regulated in at least two out of the four genotypes we studied, although in each case the down-regulation was minor.

## Discussion

**The *C. elegans* hypoxia pathway can be reconstructed entirely from RNA-seq data.** In this paper, we have shown that transcriptomic phenotypes using whole-organism RNA-seq can be used to reconstruct genetic pathways. We reconstructed the pathway to first- and second- order interaction between genes in the pathway. We inferred order of action (*rhy-1* activates *egl-9*, *egl-9* and *vhl-1* inhibit *hif-1*), and we were able to infer from genome-wide epistasis measurements that *egl-9* exerts *vhl-1*-dependent and independent inhibition on *hif-1*.

**HIF-1 and the cellular environment.** In addition to reconstructing the pathway, our dataset allowed us to observe a wide variety of physiologic changes that occur as a result of the HIF-1-dependent hypoxia response. In particular, we observed down-regulation of most components of the TCA cycle and the mitochondrial electron transport chain with the exceptions of *fum-1* and the mitochondrial complex II. The mitochondrial complex II catalyses the reaction of succinate into fumarate. Complex II is known to be important for hypoxic survival in rat cardiomyocyte cells [49]. Complex II may play a similar role in *C. elegans*. However, the product of complex II activity is fumarate. In mouse embryonic fibroblasts, fumarate has

been shown to antagonize HIF-1 prolyl hydroxylase domain (PHD) enzymes, which are orthologs of EGL-9 [52]. Upregulation of complex II by HIF-1 during hypoxia may therefore result in increased intracellular levels of fumarate, which in turn could lead to artificially high levels of HIF-1 (if the inhibitory role of fumarate is conserved in *C. elegans*) even after normoxia resumes. The increase in fumarate produced by the complex could be compensated by increasing expression of *fum-1*. Increased fumarate degradation allows *C. elegans* to maintain plasticity in the hypoxia pathway, keeping the pathway sensitive to oxygen levels.

**Interpretation of the non-classical epistasis in the hypoxia pathway.** The observation of almost 30 genes that exhibit a specific pattern of non-classical epistasis suggests new aspects of the hypoxia pathway. Some of these non-classical epistases had been observed previously, but no satisfactory mechanism has been proposed to explain this biology. [46] and [40] suggest that HIF-1 integrates information on iron concentration in the cell to bind to the *ftn-1* promoter, but could not definitively establish a mechanism. It is unclear why deletion of *hif-1* induces *ftn-1* expression, deletion of *egl-9* also causes induction of *ftn-1* expression, but deletion of *vhl-1* removes this inhibition. Moreover, [45] have previously reported that certain genes important for the *C. elegans* immune response against pathogens reflect similar expression patterns. Their interpretation was that *swan-1*, which encodes a binding partner to EGL-9 [53], is important for modulating HIF-1 activity in some manner. The lack of a conclusive double mutant analysis in this work means the role of SWAN-1 in modulation of HIF-1 activity remains to be demonstrated. At any rate, mechanisms that call for additional transcriptional modulators become less likely given the number of genes with different biological functions that exhibit the same pattern.

Genotype	Interpretation
wt	HIF-1 $\rightarrow$ <i>ftn-1</i> $\leftarrow$ HIF-1-OH
<i>egl-9</i>	HIF-1 $\Rightarrow$ <i>ftn-1</i> HIF-1 activates/ HIF-1-OH represses
<i>vhl-1</i>	HIF-1 $\Rightarrow$ <i>ftn-1</i> $\Leftarrow$ HIF-1-OH HIF-1-OH represses
<i>hif-1</i>	<i>ftn-1</i> Depends on specific activities/ concentrations at S.S.
<i>egl-9; hif-1</i>	<i>ftn-1</i> Depends on specific activities/ concentrations at S.S.
<i>egl-9; vhl-1</i>	HIF-1 $\Rightarrow$ <i>ftn-1</i> HIF-1 activates/ HIF-1-OH represses

**Fig. 12.** A hypothetical model showing a mechanism where HIF-1-hydroxyl antagonises HIF-1. Such a mechanism can potentially explain how genes that exhibit non-canonical epistasis are regulated. S.S = Steady-state.

One way to resolve this problem without invoking additional genes is to consider HIF-1 as a protein with both activating and inhibiting states. In fact, HIF-1 already exists in two states in *C. elegans*: unmodified HIF-1 and HIF-1-hydroxyl (HIF-1-OH). Under this model, HIF-1-hydroxyl antagonizes the effects of HIF-1 for certain genes like *ftn-1* or *nlp-31*. Loss of *vhl-1* stabilizes HIF-1-hydroxyl. A subset of genes that are sensitive to HIF-1-hydroxyl will be inhibited as a result of the increase in the amount of this species, in spite of the increased levels of HIF-1. On the other hand, *egl-9(lf)* selectively removes all HIF-1-hydroxyl, stimulating accumulation of HIF-1 and

promoting gene activity. Whether deletion of *hif-1(lf)* is overall activating or inhibiting will depend on the relative activity of each protein state under normoxia (see Fig. 12).

Multiple lines of circumstantial evidence that HIF-1-hydroxyl plays a role in the functionality of the hypoxia pathway. First, HIF-1-hydroxyl is challenging to study genetically because no mimetic mutations are available with which to study the pure hydroxylated HIF-1 species. Second, although mutations in the Von-Hippel Landau gene stabilize the hydroxyl species, they also increase the quantity of HIF-1 by mass action. Third, although deletion of *vhl-1* and *egl-9* lead to similar HIF-1 expression levels, the Egl phenotype of *vhl-1(lf)* is considerably attenuated—in fact, *vhl-1* is not annotated with an egg-laying defective phenotype in WormBase (version WS256). Finally, since HIF-1 is detected low levels in cells under normoxic conditions [54], total HIF-1 protein (unmodified HIF-1 plus HIF-1-hydroxyl) is often tacitly assumed to be vanishingly rare and therefore biologically inactive.

Our data show hundreds of genes that change expression in response to loss of *hif-1* under normoxic conditions. This establishes that there is sufficient total HIF-1 protein to be biologically active. Our analyses also revealed that *hif-1(lf)* shares positive correlations with *egl-9(lf)*, *rhy-1(lf)* and *vhl-1(lf)*, and that each of these genotypes also shows a secondary negative rank-ordered expression correlation with each other. These cross-patterns between all loss of function of inhibitors of HIF-1 and *hif-1(lf)* can be most easily explained if HIF-1-hydroxyl is biologically active.

A homeostatic argument can be made in favor of the activity of HIF-1-hydroxyl. At any point in time, the cell must measure the levels of multiple metabolites at once. The *hif-1*-dependent hypoxia response integrates information from O<sub>2</sub>,  $\alpha$ -ketoglutarate (2-oxoglutarate) and iron concentrations in the cell. One way to integrate this information is by encoding it only in the effective hydroxylation rate of HIF-1 by EGL-9. Then the dynamics in this system will evolve exclusively as a result of the total amount of HIF-1 in the cell. Such a system can be sensitive to fluctuations in the absolute concentration of HIF-1 [55]. When the system is in normoxic conditions, when absolute levels of HIF-1 are low, small fluctuations in copy-number could lead to partial activation of the hypoxic response due to random change for genes that are under strong control by HIF-1. On the other hand, genes that have a low affinity for HIF-1 will not be affected by these small fluctuations.

For yet other set of genes that must change expression in response to the hypoxia pathway, it may not make as much sense to integrate metabolite information exclusively via EGL-9-dependent hydroxylation of HIF-1. In particular, genes that may increase survival in mild hypoxia may benefit from regulatory mechanisms that are robust to transient changes in protein copy number. Likewise, genes that are involved in iron or  $\alpha$ -ketoglutarate metabolism (such as *ftn-1*) may benefit from being able to sense, accurately, small and consistent deviations from basal concentrations of these metabolites. For these genes, the information may be better encoded by using HIF-1 and HIF-1-hydroxyl as an activator/repressor pair. Such paradoxical circuits are known to possess distinct advantages for controlling output in a manner that is robust to transient fluctuations in the levels of their components [56, 57].

Our RNA-seq data suggests that one of the targets that HIF-1 may target paradoxically is RHY-1. Although *rhy-1* does

not exhibit non-classical epistasis, *hif-1(lf)* and *egl-9;hif-1(lf)* both had increased expression levels of *rhy-1*. We speculate that if *rhy-1* is controlled by both HIF-1 and HIF-1-hydroxyl, then this might imply that HIF-1 regulates the expression of its pathway (and therefore itself) in a manner that is robust to total HIF-1 levels.

## Materials and Methods

**Nematode strains and culture.** Strains used were N2 wild-type Bristol, CB5602 *vhl-1(lf)* (ok161), CB6088 *egl-9(lf)* (sa307) *hif-1(lf)* (ia4), CB6116 *egl-9(lf)* (sa307) *vhl-1(lf)* (ok161), JT307 *egl-9(lf)* (sa307), ZG31 *hif-1(lf)* (ia4), RB1297 *rhy-1(lf)* (ok1402). ZG31 *hif-1(lf)* (ia4) is a null mutant of *hif-1(lf)* which deletes 1231 bp of the second, third and fourth exons. JT307 contains the null mutant *egl-9(lf)* (sa307) which is a 243 bp deletion. RB1297 contains null mutation *rhy-1(lf)* (ok1402) with an estimated 700 bp deletion constructed by the OMRF Knockout Group. CB5602 contains the deletion mutation of *vhl-1(lf)* (ok161). CB6088 contains *egl-9(lf)* (sa307); *hif-1(lf)* (ia4). CB6116 contains *egl-9(lf)* (sa307) *vhl-1(lf)* (ok161). All strains were provided by the CGC, which is funded by NIH Office of Research Infrastructure Programs (P40 OD010440). All lines were grown on standard nematode growth media (NGM) plates with seeded with OP50 *E. coli* at 20°C (Brenner 1974).

**RNA Isolation.** Unsynchronized lines were grown on NGM plates at 20°C and eggs harvested by sodium hypochlorite treatment. Eggs were plated on 6 to 9 small 5cm NGM plates with ample OP50 *E. coli* at a density chosen to avoid starvation and grown at 20°C. Worms were staged and harvested based on the time after plating, vulva morphology and the absence of eggs. Approximately 30–50 non-gravid young adults (YA) were picked and placed in 100 $\mu$ L of TE pH 8.0 at 4°C in 0.2mL PCR tubes. After settling and a brief spin in microfuge approximately 80 $\mu$ L of TE was removed from the top of the sample and individual replicates were snap frozen in liquid N<sub>2</sub>. These replicate samples were then digested with Proteinase K for 15min at 60° in the presence of 1% SDS and 1.25 $\mu$ L RNA Secure (Ambion AM 7005). RNA samples were then taken up in 5 Volumes of Trizol (Tri Reagent Zymo Research) and processed and treated with DNase I using Zymo MicroPrep RNA Kit (Zymo Research Quick-RNA MicroPrep R1050). RNA was eluted in dH<sub>2</sub>O and divided into aliquots and stored at -80°C. One aliquot of each replicate was analyzed by both NanoDrop for impurities, Qubit for concentration and then analyzed on an Agilent 2100 BioAnalyzer. Replicates were selected that had RNA integrity numbers (RIN) equal or greater than 9.0 and showed no evidence of bacterial ribosomal bands, except for the ZG31 mutant where one of three replicates had a RIN of 8.3.

**Library Preparation and Sequencing.** 10 ngs of quality checked (RIN > 9.0), total RNA from each sample were reverse-transcribed into cDNA using the Clontech SMARTer Ultra Low Input RNA for Sequencing v3 kit reagents (catalog #634848) in the SMARTSeq2 protocol [58]. RNA was denatured at 70°C for 3 minutes in the presence of dNTPs, oligo dT primer and spiked-in quantitation standards (NIST/ERCC from Ambion, catalog #4456740). After chilling to 4°C, the first strand reaction was assembled using the LNA TSO primer described in [58], and run at 42°C for 90 minutes, followed by denaturation at 70°C for 10 minutes. The entire first strand reaction was then used as template for 13 cycles of PCR using the Clontech v3 kit. Reactions were cleaned up with 1.8X volume of Ampure XP SPRI beads (catalog #A63880) according to the manufacturer's protocol. After quantification using the Qubit High Sensitivity DNA assay, a 3ng aliquot of the amplified cDNA was run on the Agilent HS DNA chip to confirm the length distribution of the amplified fragments. The median value for the average cDNA lengths from all length distributions was 1076bp. Tagmentation of the full length cDNA for sequencing was performed using the Illumina/Nextera DNA library prep kit (catalog #FC-121-1030). Following Qubit quantitation and Agilent BioAnalyzer profiling, the tagged libraries were sequenced. Libraries were sequenced on Illumina HiSeq2500 in single read mode with the read length of



50 nt to an average depth of 15 million reads per sample following manufacturer's instructions. Base calls were performed with RTA 1.13.48.0 followed by conversion to FASTQ with bcl2fastq 1.8.4. Spearman correlation of the transcripts per million (TPM) for each genotype showed that every pairwise correlation within genotype was  $> 0.9$ .

**Read Alignment and Differential Expression Analysis.** We used Kallisto to perform read pseudo-alignment and performed differential analysis using Sleuth. We fit a generalized linear model for a transcript  $t$  in sample  $i$ :

$$y_{t,i} = \beta_{t,0} + \beta_{t,genotype} \cdot X_{t,i} + \beta_{t,batch} \cdot Y_{t,i} + \epsilon_{t,i} \quad [1]$$

where  $y_{t,i}$  are the logarithm transformed counts;  $\beta_{t,genotype}$  and  $\beta_{t,batch}$  are parameters of the model, and which can be interpreted as biased estimators of the log-fold change;  $X_{t,i}, Y_{t,i}$  are indicator variables describing the conditions of the sample; and  $\epsilon_{t,i}$  is the noise associated with a particular measurement.

**Genetic Analysis, Overview.** Genetic analysis of the processed data was performed in Python 3.5. Our scripts made extensive use of the Pandas, Matplotlib, Scipy, Seaborn, Sklearn, Networkx, Bokeh, PyMC3, and TEA libraries [43, 59–66]. Our analysis is available in a Jupyter Notebook [67]. All code and required data (except the raw reads) are available at <https://github.com/WormLabCaltech/mpsq> along with version-control information. Our Jupyter Notebook and interactive graphs for this project can be found at <https://wormlabcaltech.github.io/mpsq/>. Raw reads were deposited at XXXXXXXXXXXX

**Weighted Correlations.** Pairwise correlations between transcriptomes where calculated by first identifying the set of differentially expressed genes (DEGs) common to both transcriptomes under analysis. DEGs were then rank-ordered according to their regression coefficient,  $\beta$ . Bayesian robust regressions were performed using a Student-T distribution. Bayesian analysis was performed using the PyMC3 library [63] (`pm.glm.families.StudentT` in Python). If the correlation has an average value  $> 1$ , the correlation coefficient was set to 1.

Weights were calculated as the proportion of genes that were  $< 1.5$  standard deviations away from the primary regression out of the entire set of shared DEGs for each transcriptome.

**Epistasis Analysis.** For a double mutant  $X^-Y^-$ , we used the single mutants  $X^-$  and  $Y^-$  to find expected value of the coefficient for a double mutant under an additive model for each isoform  $i$ . Specifically,

$$\beta_{Exp,i} = \beta_{X,i} + \beta_{Y,i}. \quad [2]$$

Next, we found the deviation of the double mutant from the additive model ( $\delta$ ) for each isoform  $i$ :

$$\Delta_i = \beta_{XY,i} - \beta_{Exp,i} \quad [3]$$

To calculate the genome-wide epistasis coefficient, we plotted ( $\beta_{Exp,i}, \Delta_i$ ) and found the line of best fit using orthogonal distance regression using the `scipy.odr` package. We performed non-parametric bootstrap sampling of the ordered tuples with replacement using 5,000 iterations to generate a probability distribution of slopes of best fit.

To understand the epistatic relationships completely, we needed to simulate the possible relationships. There are as many models as epistatic relationships. The epistatic relationships are such that:

$$X^-Y^- = Z, \quad [4]$$

where  $Z$  is some combination of  $X^-$  and  $Y^-$ . Specifically,  $Z$  can take on the values  $X^-$  ( $X$  is epistatic to  $Y$ );  $Y^-$  ( $Y$  is epistatic to  $X$ );  $X^- + Y^-$  (additive);  $k^-, k^- = X^- = Y^-$  (unbranched pathway) and  $X^-, Y^- = WT$  (strong repression, where  $Y^-$  is wild-type). For each case, we modified equation 3:

$$\Delta_{Z,i} = \beta_{Z,i} - \beta_{Exp,i}. \quad [5]$$

In each case,  $\Delta_{Z,i}$  reduces to a linear combination of  $-\beta_{X,i}$  and  $-\beta_{Y,i}$ .

To select between theoretical models, we implemented an approximate Bayesian Odds Ratio. We defined a free-fit model,  $M_1$ ,

$$P(\alpha | M_1, D) \propto \prod_{(x_i, y_i, \sigma_i) \in D} \exp \frac{(y_i - \alpha \cdot x_i)^2}{2\sigma_i^2} \cdot (1 + \alpha^2)^{-3/2}, \quad [6]$$

where  $\alpha$  is the slope of the model to be determined,  $x_i, y_i$  were the  $x$ - and  $y$ -coordinates of each point respectively, and  $\sigma_i$  was the standard error associated with each coordinate (obtained from Sleuth). We minimized the negative logarithm of 6 to obtain the most likely slope given the data,  $D$  (`scipy.optimize.minimize` in Python). Finally, we approximated the computed odds ratio as:

$$OR = \frac{P(D | \alpha^*, M_1) \cdot (2\pi)^{1/2} \sigma_{\alpha^*}}{P(D | M_i)}, \quad [7]$$

where  $\alpha^*$  is the slope found after minimization,  $\sigma_{\alpha^*}$  is the standard deviation of the parameter at the point  $\alpha^*$  and  $P(D | M_i)$  is the probability of the data given the parameter-free model,  $M_i$ .

**Enrichment Analysis.** Tissue, Phenotype and Gene Ontology Enrichment Analysis were carried out using the WormBase Enrichment Suite for Python [43, 44].

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