

Algolab 2015

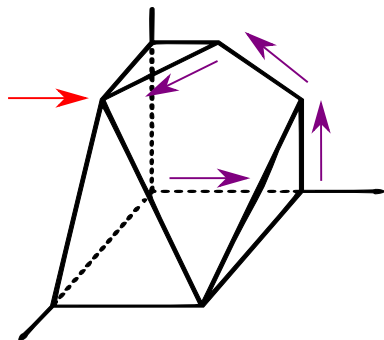
LP/QP: Some facts

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December 2, 2015

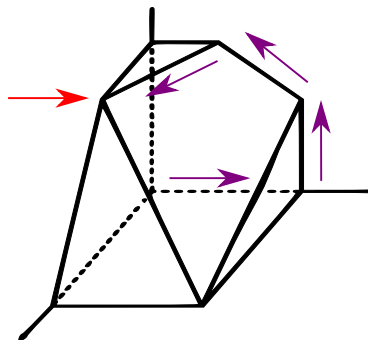
Solving Linear Programs

- The constraints define a convex polyhedron $P = \{x \mid Ax \leq b\}$
- Simplex-type algorithms walk along the edges of P to vertices with better values of the objective function until an optimum is reached.
- Decide on next edge: *pivot rule* or *pricing strategy*



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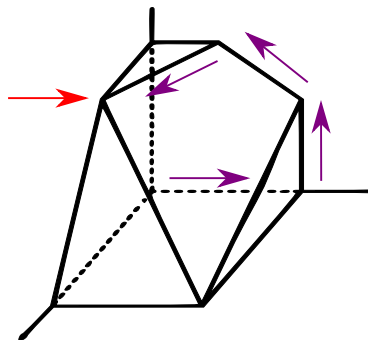


Complexity

- exponential!

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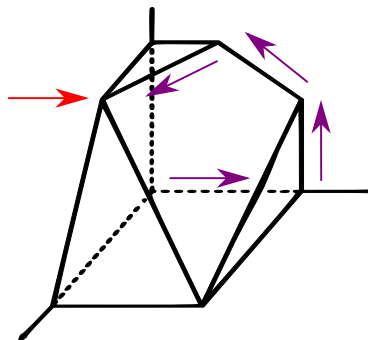


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- $O(m)$ if n is fixed (exponential in n)
(m # inequalities, n # variables)

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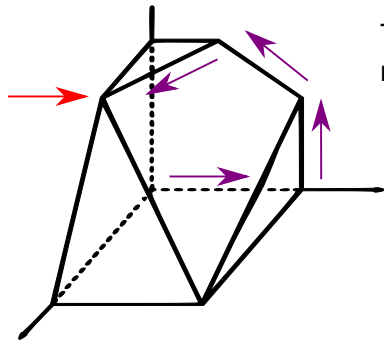
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- CGAL: for geometric applications, dimension typically $n \leq 50$ or ≤ 100

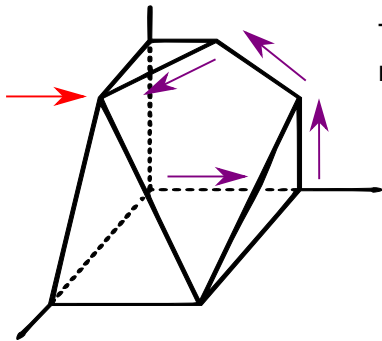
Solving Linear Programs with CGAL



The default pivot rule/pricing strategy might fail:

- it always picks the same improving edge every time it visits the same vertex
- suppose the algorithm reaches a certain vertex for the second time
 \Rightarrow infinite cycle

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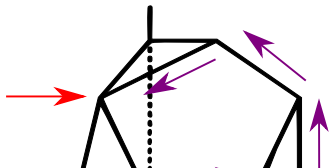
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Change the pivot rule

- Bland's pivot rule avoids cycling (but it is slower...)

```
CGAL::Quadratic_program_options options;  
options.set_pricing_strategy(CGAL::QP_BLAND);  
Solution s = CGAL::SOLVER(program, ET(), options);
```

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BUG - Don't Forget!

There is a bug in the assignment `operator=` for `Solution` objects...

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