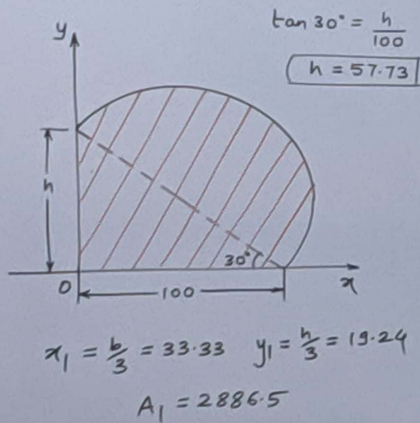


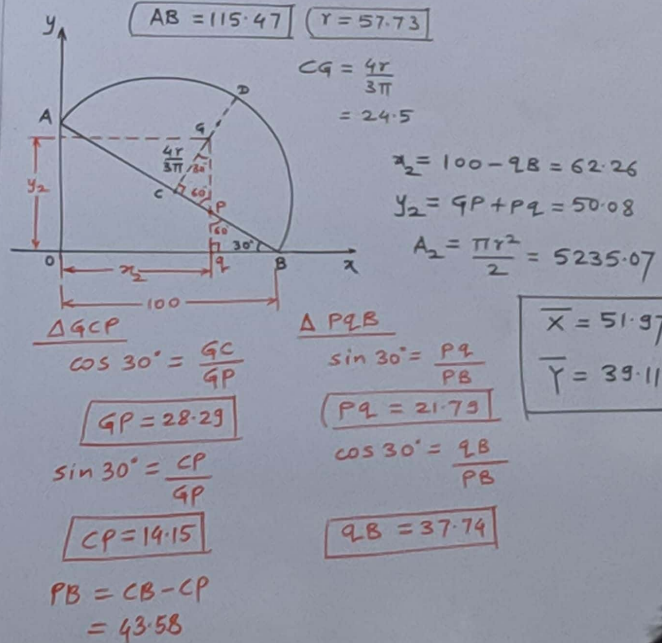
$$\frac{-A_2x_2 - A_3x_3}{-A_2 - A_3}$$

$$(91.74, 69.35)$$



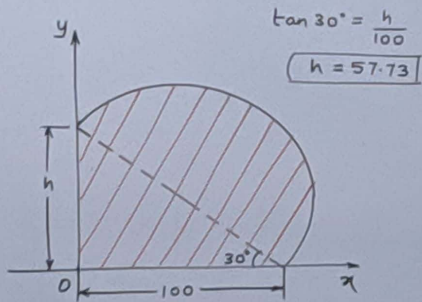
$$\cos 30^\circ = \frac{100}{AB}$$

$$AB = 115.47 \quad Y = 57.73$$



$$\frac{-A_2x_2 - A_3x_3}{1 - A_2 - A_3}$$

$$(91.74, 69.35)$$



$$x_1 = \frac{b}{3} = 33.33 \quad y_1 = \frac{h}{3} = 19.24$$

$$A_1 = 2886.5$$

$$\tan 30^\circ = \frac{h}{100}$$

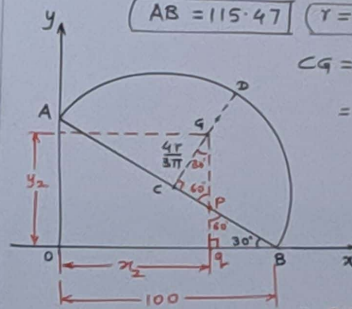
$$h = 57.73$$

$$\cos 30^\circ = \frac{100}{AB}$$

$$AB = 115.47 \quad Y = 57.73$$

$$CQ = \frac{4r}{3\pi}$$

$$= 24.5$$



$$x_2 = 100 - 9.8 = 62.26$$

$$y_2 = 9P + 9Q = 50.08$$

$$A_2 = \frac{\pi r^2}{2} = 5235.07$$

$$\Delta GCP$$

$$\cos 30^\circ = \frac{GC}{GP}$$

$$GP = 28.29$$

$$\sin 30^\circ = \frac{CP}{GP}$$

$$CP = 14.15$$

$$PB = CB - CP$$

$$= 43.58$$

$$\Delta PQB$$

$$\sin 30^\circ = \frac{PQ}{PB}$$

$$PQ = 21.79$$

$$\cos 30^\circ = \frac{QB}{PB}$$

$$QB = 37.74$$

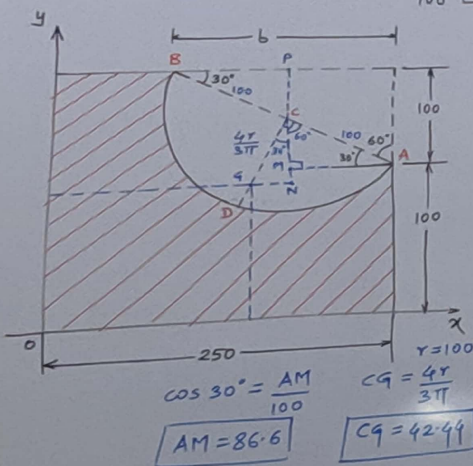
$$\bar{X} = 51.97$$

$$\bar{Y} = 39.11$$

Centroid (8M)

$$\cos 60^\circ = \frac{100}{\text{dia}} \quad (\text{dia} = 200)$$

$$\tan 60^\circ = \frac{b}{100} \quad (b = 173.2)$$



$$\begin{aligned} x_1 &= \frac{b}{2} = 125 \\ y_1 &= \frac{h}{2} = 100 \\ A_1 &= b \times h = 50000 \end{aligned}$$

$$\begin{aligned} \sin 30^\circ &= \frac{GN}{CQ} \\ GN &= 21.22 \\ \cos 30^\circ &= \frac{CN}{CQ} \\ CN &= 36.75 \end{aligned}$$

$$\begin{aligned} b &= 173.2 \quad h = 100 \\ x_2 &= 250 - \frac{b}{3} = 192.27 \\ y_2 &= 200 - \frac{h}{3} = 166.66 \\ A_2 &= 8660 \end{aligned}$$

$$\begin{aligned} \sin 30^\circ &= \frac{CP}{100} \\ CP &= 50 \end{aligned}$$

Semi-Circle

$$\begin{aligned} x_3 &= 250 - GN - AM \\ &= 250 - 21.22 - 86.6 \\ x_3 &= 142.18 \\ y_3 &= 200 - CN - CP \\ &= 200 - 36.75 - 50 \\ y_3 &= 113.25 \\ A_3 &= \frac{\pi r^2}{2} = 15707.96 \end{aligned}$$

$$\bar{x} = \frac{A_1 x_1 - A_2 x_2 - A_3 x_3}{A_1 - A_2 - A_3}$$

$$\bar{x} = 91.74$$

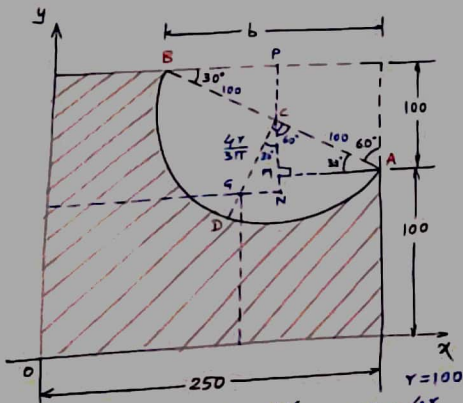
$$\bar{y} = 69.35$$

$$(\bar{x}, \bar{y}) = (91.74, 69.35)$$

Centroid (8M)

$$\cos 60^\circ = \frac{100}{\text{dia}} \quad \boxed{\text{dia} = 200}$$

$$\tan 60^\circ = \frac{b}{100} \quad \boxed{b = 173.2}$$



$$\cos 30^\circ = \frac{AM}{100}$$

$$\boxed{AM = 86.6}$$

$$CQ = \frac{4r}{3\pi}$$

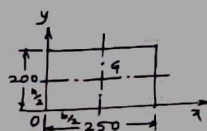
$$\boxed{CQ = 42.44}$$

$$\sin 30^\circ = \frac{GN}{CQ}$$

$$\boxed{GN = 21.22}$$

$$\cos 30^\circ = \frac{CN}{CQ}$$

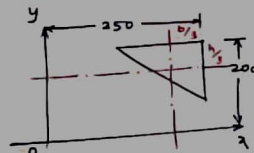
$$\boxed{CN = 36.75}$$



$$x_1 = b/2 = 125$$

$$y_1 = h/2 = 100$$

$$A_1 = b \times h = 50000$$



$$b = 173.2 \quad h = 100$$

$$x_2 = 250 - b/3 = 192.27$$

$$y_2 = 200 - h/3 = 166.66$$

$$A_2 = 8660$$

$$\sin 30^\circ = \frac{CP}{100}$$

$$\boxed{CP = 50}$$

Semi-Circle

$$x_3 = 250 - GN - AM$$

$$= 250 - 21.22 - 86.6$$

$$\boxed{x_3 = 142.18}$$

$$y_3 = 200 - CN - CP$$

$$= 200 - 36.75 - 50$$

$$\boxed{y_3 = 113.25}$$

$$A_3 = \frac{\pi r^2}{2} = 15707.96$$

$$\bar{x} = \frac{A_1 x_1 - A_2 x_2 - A_3 x_3}{A_1 - A_2 - A_3}$$

$$\bar{x} = 91.74$$

$$\bar{y} = 69.35$$

$$\boxed{(\bar{x}, \bar{y}) = (91.74, 69.35)}$$

Centroid (8M)

$$\cos 60^\circ = \frac{100}{\text{dia}} \quad \boxed{\text{dia} = 200}$$

$$\tan 60^\circ = \frac{b}{100} \quad \boxed{b = 173.2}$$



$$\cos 30^\circ = \frac{AM}{100}$$

$$\boxed{AM = 86.6}$$

$$CQ = \frac{4r}{3\pi}$$

$$\boxed{CQ = 42.44}$$

$$\sin 30^\circ = \frac{GN}{CQ}$$

$$\boxed{GN = 21.22}$$

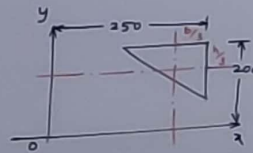
$$\cos 30^\circ = \frac{CN}{CQ}$$

$$\boxed{CN = 36.75}$$

$$x_1 = x_2 = 125$$

$$y_1 = y_2 = 100$$

$$A_1 = b \times h = 50000$$



$$b = 173.2 \quad h = 100$$

$$x_2 = 250 - \frac{b}{3} = 192.27$$

$$y_2 = 200 - \frac{h}{3} = 166.66$$

$$A_2 = 8660$$

Semi-Circle

$$x_3 = 250 - GN - AM$$

$$= 250 - 21.22 - 86.6$$

$$\boxed{x_3 = 142.18}$$

$$y_3 = 200 - CN - CP$$

$$= 200 - 36.75 - 50$$

$$\boxed{y_3 = 113.25}$$

$$A_3 = \frac{\pi r^2}{2} = 15707.96$$

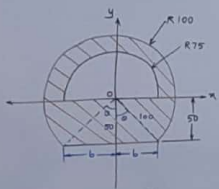
$$\bar{x} = \frac{A_1 x_1 - A_2 x_2 - A_3 x_3}{A_1 - A_2 - A_3}$$

$$\bar{x} = 91.74$$

$$\bar{y} = 69.35$$

$$\boxed{(\bar{x}, \bar{y}) = (91.74, 69.35)}$$

Centroid (8M)



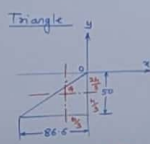
$$\cos \theta = \frac{50}{100}$$

$$\theta = 60^\circ$$

$$\tan \theta = \frac{b}{50}$$

$$b = 50 \tan 60^\circ$$

$$b = 86.6$$



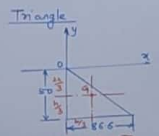
$$b = 86.6 \quad h = 50$$

$$x_1 = -\frac{b}{3} = -28.86$$

$$y_1 = -\frac{2h}{3} = -33.33$$

$$A_1 = \frac{1}{2} \times b \times h$$

$$= 2165$$



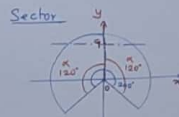
$$b = 86.6 \quad h = 50$$

$$x_2 = \frac{b}{3} = 28.86$$

$$y_2 = -\frac{2h}{3} = -33.33$$

$$A_2 = \frac{1}{2} \times b \times h$$

$$= 2165$$



$$R = 100 \quad \theta = 120^\circ$$

$$OG = \frac{2R \sin \frac{\theta}{2}}{3\theta}$$

$$= \frac{2 \times 100 \sin 60^\circ}{3 \times 120^\circ \times \frac{\pi}{180^\circ}}$$

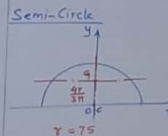
$$OG = 27.57$$

$$x_3 = 0$$

$$y_3 = OG = 27.57$$

$$A_3 = \frac{1}{2} R^2 \theta = \frac{100^2 \times 120^\circ \times \pi}{180^\circ}$$

$$A_3 = 20943.95$$



$$R = 75$$

$$x_4 = 0$$

$$y_4 = \frac{4R}{3\pi} = 31.83$$

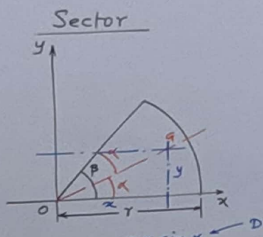
$$A_4 = \frac{\pi R^2}{2} = 8835.72$$

$$\bar{x} = 0$$

$$\bar{y} =$$

Centroid (8M)

Sector



$$OQ = \frac{2r \sin \alpha}{3\alpha}$$

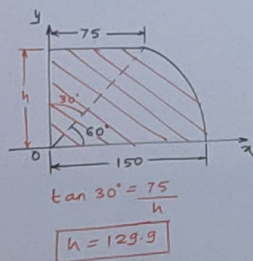
$$\sin \alpha = \frac{y}{OQ}$$

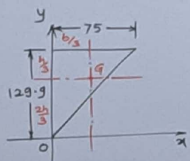
$$y = OQ \sin \alpha$$

$$\cos \alpha = \frac{x}{OQ}$$

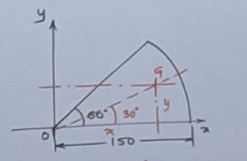
$$x = OQ \cos \alpha$$

$$A = r^2 \alpha$$





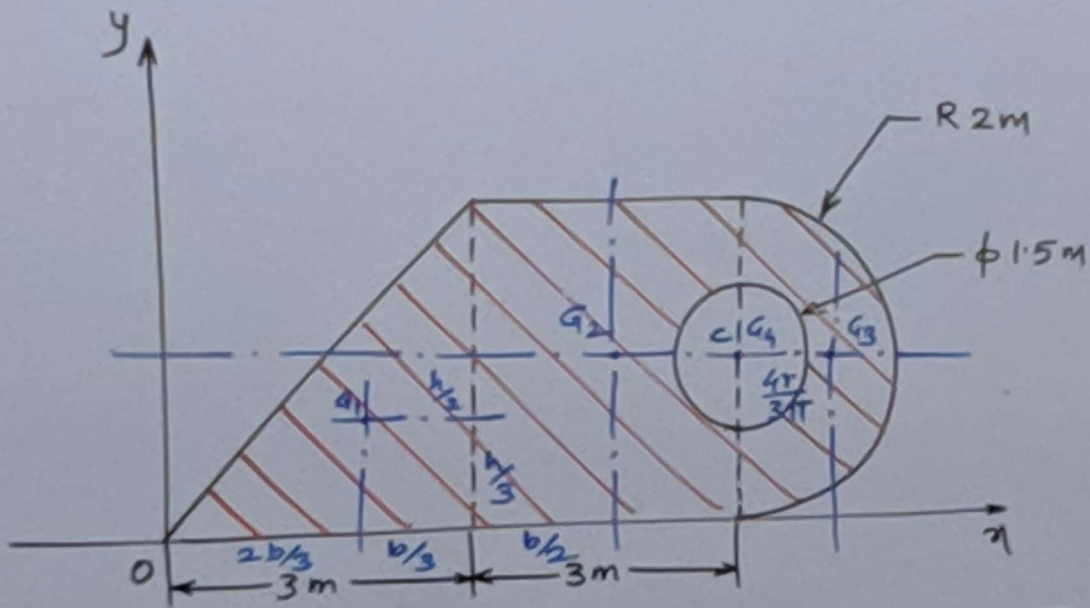
$b = 75$ $h = 129.9$
 $\alpha_1 = \frac{b}{3} = 25$
 $y_1 = \frac{2h}{3} = 86.6$
 $A_1 = \frac{1}{2} \times b \times h$
 $= 4871.25$



$\alpha = 30^\circ$
 $OQ = \frac{2r \sin \alpha}{3\alpha}$
 $= \frac{2 \times 150 \times \sin 30^\circ}{3 \times 30^\circ \times \frac{\pi}{180^\circ}}$
 $OQ = 95.49$

$\sin 30^\circ = \frac{y}{OQ}$
 $y = 95.49 \sin 30^\circ$
 $y_2 = 47.74$
 $\cos 30^\circ = \frac{x}{OQ}$
 $x = 95.49 \cos 30^\circ$
 $x_2 = 82.69$
 $A_2 = r^2 \alpha$
 $= 150^2 \times 30^\circ \times \frac{\pi}{180^\circ}$
 $A_2 = 11780.97$
 $\bar{x} = 65.81$
 $\bar{y} = 59.1$

Q-17, Pg-10)

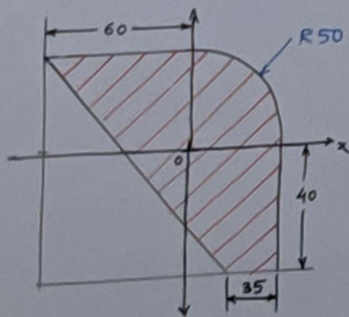


$x_1 = 2$	$y_1 = 1.33$	$A_1 = 6$	$\bar{x} = 4.37$
$x_2 = 4.5$	$y_2 = 2$	$A_2 = 12$	$\bar{y} = 1.82$
$x_3 = 6.84$	$y_3 = 2$	$A_3 = 6.28$	
$x_4 = 6$	$y_4 = 2$	$A_4 = 1.76$	

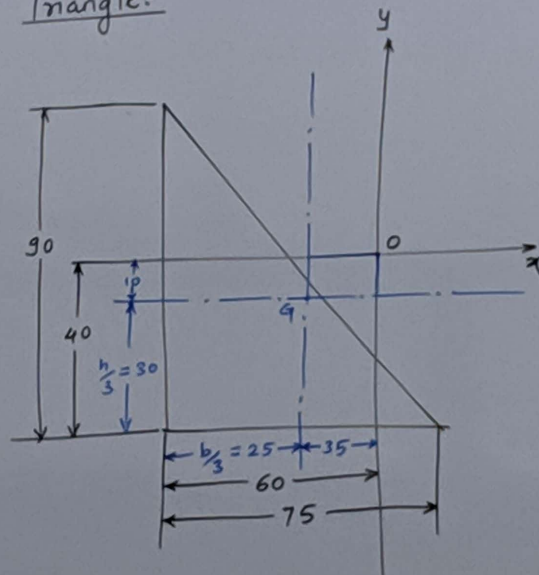
Centroid (8M)

Pg-9)

9.7) Find Centroid of shaded portion



Triangle:



$$b = 75 \quad h = 90$$

$$x_5 = -35$$

$$y_5 = -10$$

$$A_5 = \frac{1}{2} \times b \times h$$

$$= 3375$$

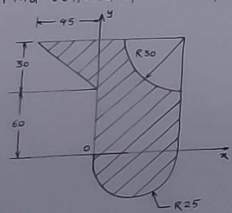
$$\bar{x} =$$

$$\bar{y} =$$

Centroid (8M)

Fig-3)
Q.4)

Find Centroid of shaded portion



Triangle:-

$b = 45, h = 30$
 $x_1 = -\frac{b}{3} = -15$
 $y_1 = 60 + \frac{2h}{3} = 80$
 $A_1 = \frac{1}{2} \times b \times h = \frac{1}{2} \times 45 \times 30$
 $A_1 = 675$

Rectangle

$b = 50, h = 90$
 $x_2 = \frac{b}{2} = 25$
 $y_2 = \frac{h}{2} = 45$
 $A_2 = b \times h = 50 \times 90$
 $A_2 = 4500$

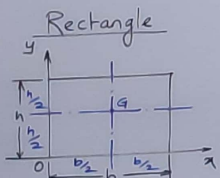
Semi-Circle:-

$r = 25$
 $x_3 = r = 25$
 $y_3 = -\frac{4r}{3\pi} = -10.61$
 $A_3 = \frac{\pi r^2}{2} = 981.74$

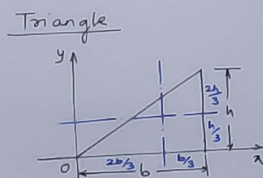
Quarter Circle:-

$r = 30$
 $x_4 = 50 - \frac{4r}{3\pi} = 37.26$
 $y_4 = 90 - \frac{4r}{3\pi} = 77.26$
 $A_4 = \frac{\pi r^2}{4} = 706.85$
 $\bar{x} = \frac{A_1 x_1 + A_2 x_2 + A_3 x_3 - A_4 x_4}{A_1 + A_2 + A_3 - A_4} = 18.45$
 $\bar{y} = 35.13$
 $(\bar{x}, \bar{y}) = (18.45, 35.13)$

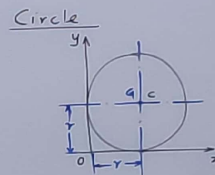
Centroid (8M)



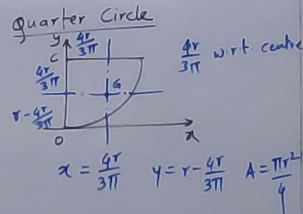
$\frac{b}{2}$ & $\frac{h}{2}$ w.r.t. 90° corner
 x & y w.r.t. origin
 $x = \frac{b}{2}$
 $y = \frac{h}{2}$
 $A = b \times h$



$\frac{b}{3}$ & $\frac{h}{3}$ w.r.t. 90° corner
 x & y w.r.t. origin
 $x = \frac{2b}{3}$
 $y = \frac{h}{3}$
 $A = \frac{1}{2} \times b \times h$

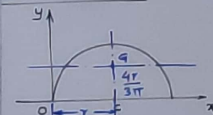


$x = r$
 $y = r$
 $A = \pi r^2$



$x = \frac{4r}{3\pi}$ $y = \frac{4r}{3\pi}$ $A = \frac{\pi r^2}{4}$

Semi-Circle



$\frac{4r}{3\pi}$ w.r.t. centre.
 x & y w.r.t. origin
 $x = r$
 $y = \frac{4r}{3\pi}$
 $A = \frac{\pi r^2}{2}$