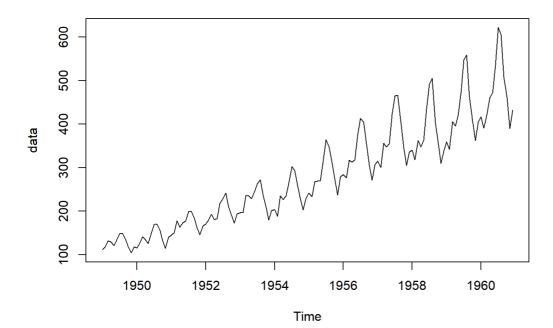
1 R

1

plot(data)

```
library(itsmr)
 library(MASS)
 ## Attaching package: 'MASS'
 ## The following object is masked from 'package:itsmr':
 ##
 ##
      deaths
 library(tseries)
 ## Warning: package 'tseries' was built under R version 4.0.4
 ## Registered S3 method overwritten by 'quantmod':
 ## method
                   from
 ## as.zoo.data.frame zoo
 ## Attaching package: 'tseries'
 ## The following object is masked from 'package:itsmr':
 ##
 ##
      arma
 library(nortest)
 library(forecast)
 ## Warning: package 'forecast' was built under R version 4.0.4
 ## Attaching package: 'forecast'
 ## The following object is masked from 'package:itsmr':
 ##
 ##
      forecast
2.
AirPassengers
                         (1949 - 1960) 3
       (trend) ; 1949
        (heteroscedasticity)
        (seasonality); 12
 data = AirPassengers
```

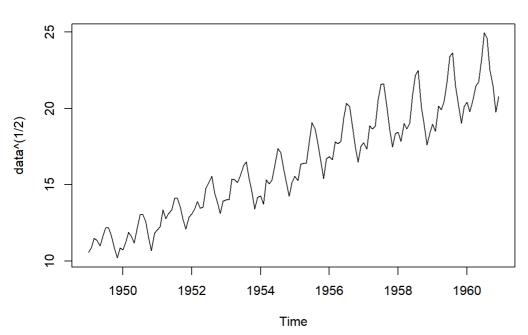


3.

, , Box-Cox .

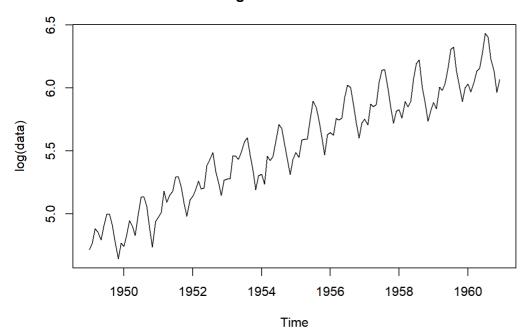
plot(data^(1/2)); title('root - transformation')

root - transformation



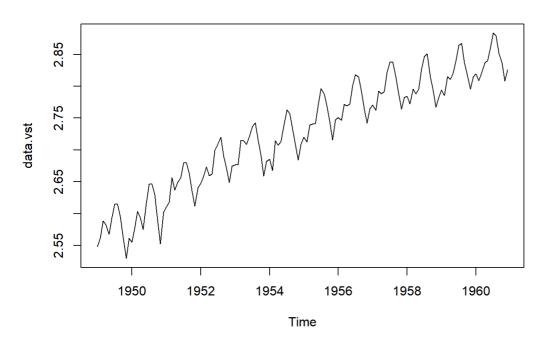
plot(log(data)); title('log - transformation')

log - transformation



lambda <- BoxCox.lambda(data)
data.vst<-BoxCox(data,lambda)
plot(data.vst);title("Box Cox transformation")

Box Cox transformation



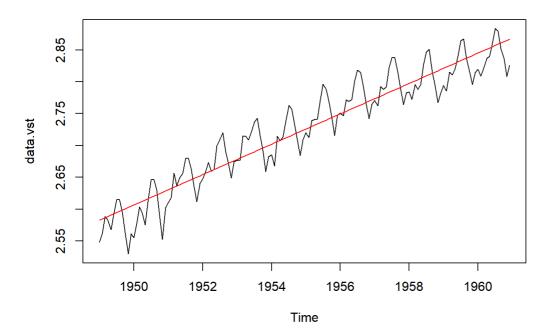
4.

1 .

```
n = length(data.vst)
x = seq(1,n,1)
Tt = lm(data.vst~1+x)

plot.ts(data.vst)
title('regression')
xa = as.vector(time(data.vst))
lines(xa, Tt$fitted.values,col='red')
```

regression



dtrend <- data.vst - Tt\$fitted.values

5.

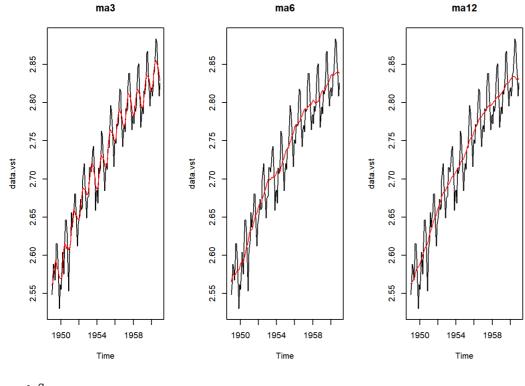
```
smooth.ma ,
```

```
ma3 = smooth.ma(data.vst, q=3)
ma6 = smooth.ma(data.vst, q=6)
ma12 = smooth.ma(data.vst, q=12)

par(mfrow = c(1,3))
plot.ts(data.vst)
title('ma3')
lines(xa,ma3,col = 'red')

plot.ts(data.vst)
title('ma6')
lines(xa,ma6,col = 'red')

plot.ts(data.vst)
title('ma12')
lines(xa,ma12,col = 'red')
```



• q . . . smooth.exp . .

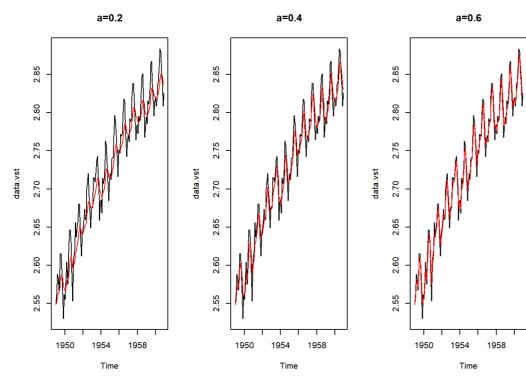
```
ex2 = smooth.exp(data.vst,.2)
ex4 = smooth.exp(data.vst,.4)
ex6 = smooth.exp(data.vst,.6)

par(mfrow = c(1,3))

plot.ts(data.vst)
lines(xa,ex2,col = 'red');title("a=0.2")

plot.ts(data.vst)
lines(xa,ex4,col = 'red');title("a=0.4")

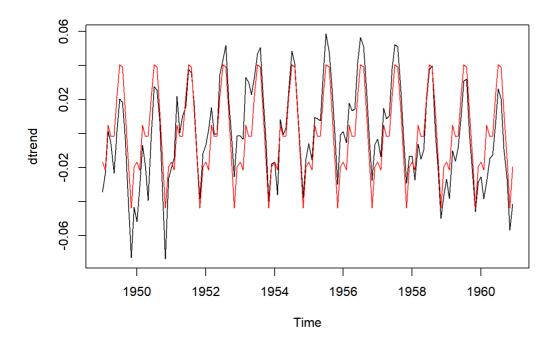
plot.ts(data.vst)
lines(xa,ex4,col = 'red');title("a=0.6")
```



• a .

season

```
season.avg = season(dtrend, d=12)
plot.ts(dtrend)
lines(xa,season.avg,col = 'red')
```



6.

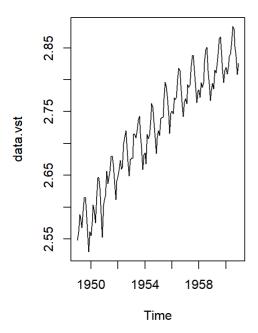
. diff .

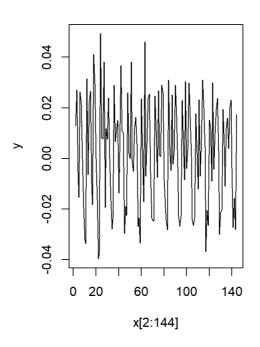
```
y = diff(data.vst)

par(mfrow = c(1,2))

plot.ts(data.vst)

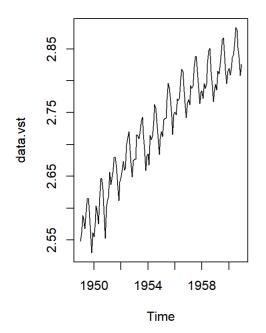
plot(x[2:144],y,type = 'l')
```

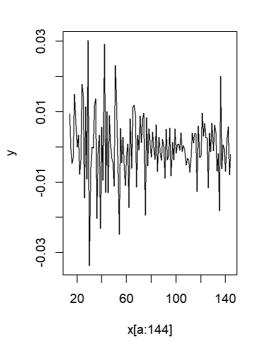




diff lag .

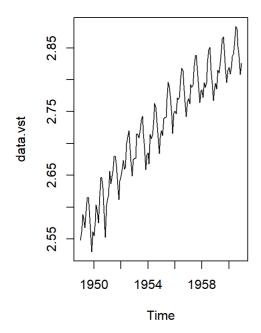
```
\begin{aligned} & \text{diff} 12 = \text{diff}(\text{data.vst}, \, \text{lag} = 12) \\ & y = \text{diff}(\text{diff} 12) \\ & \text{par}(\text{mfrow} = \text{c}(1,2)) \\ & \text{plot.ts}(\text{data.vst}) \\ & \text{a} < -145\text{-length}(y) \end{aligned}
```

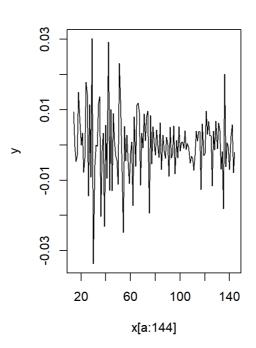




```
\begin{aligned} & \text{diff12} = \text{diff(data.vst, lag} = 12) \\ & y = \text{diff(diff12)} \\ & a <- 145\text{-length(y)} \end{aligned} & \text{par(mfrow} = c(1,2)) \\ & \text{plot.ts(data.vst)} \\ & \text{plot(x[a:144],y,type} = 'I') \end{aligned}
```

1



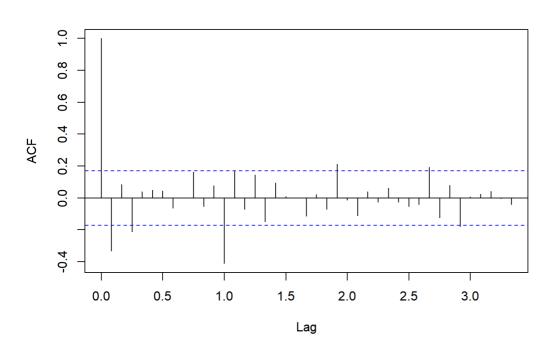


ACF

ACF

```
dat.wn <- y
acf(dat.wn,lag.max = 40)
```

Series dat.wn



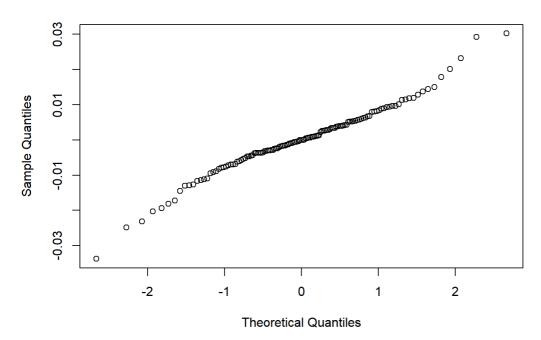
,

```
Box.test(dat.wn,lag=10,type="Ljung-Box")\\
```

```
##
## Box-Ljung test
##
## data: dat.wn
## X-squared = 27.347, df = 10, p-value = 0.002294
```

qqnorm(dat.wn)

Normal Q-Q Plot



```
jarque.bera.test(dat.wn)
```

```
##
## Jarque Bera Test
##
## data: dat.wn
## X-squared = 17.246, df = 2, p-value = 0.0001799
```

adf

- : .
- : .

adf.test(dat.wn)

Warning in adf.test(dat.wn): p-value smaller than printed p-value

```
##
## Augmented Dickey-Fuller Test
##
## data: dat.wn
## Dickey-Fuller = -5.2679, Lag order = 5, p-value = 0.01
## alternative hypothesis: stationary
```

kpss

- : .
- : .

kpss.test(dat.wn)

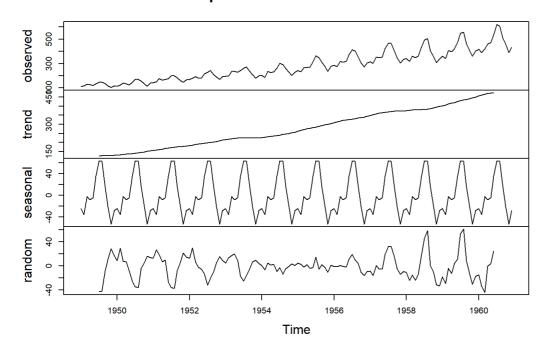
Warning in kpss.test(dat.wn): p-value greater than printed p-value

```
##
## KPSS Test for Level Stationarity
##
## data: dat.wn
## KPSS Level = 0.086789, Truncation lag parameter = 4, p-value = 0.1
```

8. Classical Deomposition

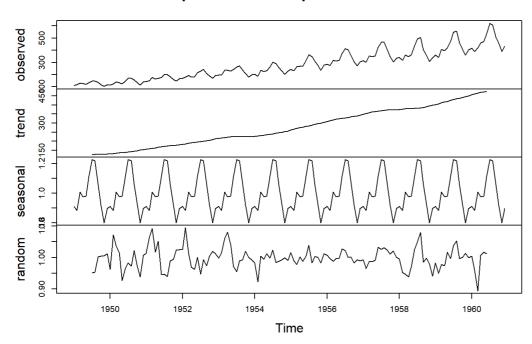
 ${\sf decompose} \qquad \quad , \quad , \quad , \qquad \quad .$

Decomposition of additive time series



plot(decompose(data, type="multiplicative"))

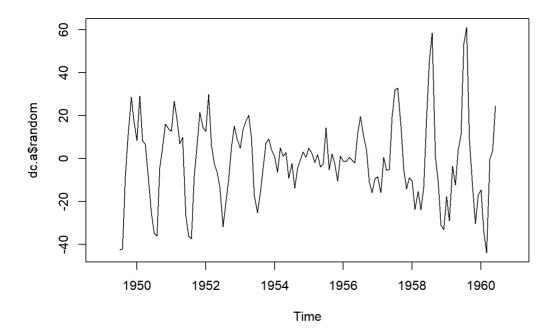
Decomposition of multiplicative time series



dc.m <- decompose(data, type="multiplicative")
dc.a <- decompose(data)

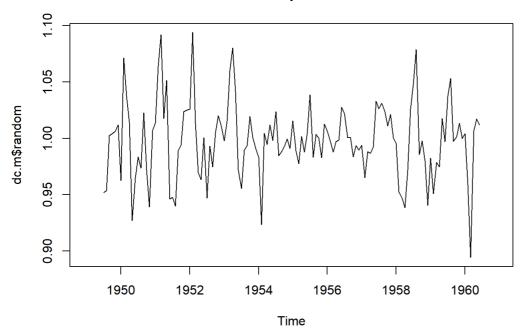
plot(dc.a\$random);title("random - addictive model")

random - addictive model



plot(dc.m\$random);title("random - multiplicative model")

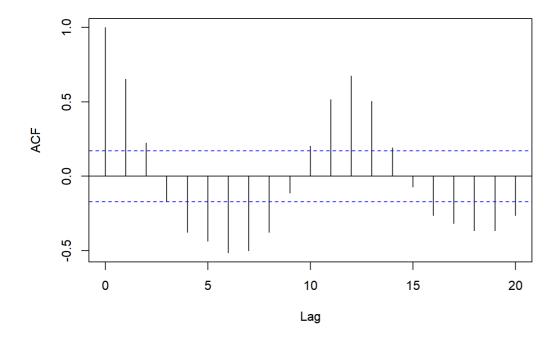
random - multiplicative model



acf

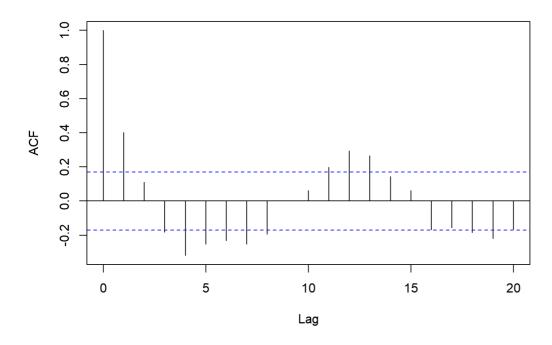
acf(dc.a\$random[complete.cases(dc.a\$random)],lag.max = 20)

Series dc.a\$random[complete.cases(dc.a\$random)]



acf(dc.m\$random[complete.cases(dc.m\$random)],lag.max = 20)

Series dc.m\$random[complete.cases(dc.m\$random)]



• !!