

## Data Management and Artificial Intelligence Homework 11

### Task 1 *N-Puzzle*

Implement a class *State* for N-Puzzle, which models the game of playing a puzzle with  $N$  tiles. For instance, 8-Puzzle is played on a board with  $3 \times 3$  slots and the next larger puzzle is 15-Puzzle which is played on a board with  $4 \times 4$  slots. The number  $N$  should be passed to the constructor of *State* along with the initial configuration.

1. Implement functions for goal state judgement, legal action identification, state transition and etc. Keep in mind that your code should work for any valid  $N$ !
2. Implement the heuristic function, i.e. Manhattan distance, to evaluate the  $h$  value for a specific state.
3. Implement a function which computes an initial configuration of the N-Puzzle at most  $k$  steps away from the goal state. **Hint:** Just simulate moving the empty tile around for  $k$  steps from the goal state, avoiding previously seen states.
4. Implement three uninformed searching methods: BFS, DFS and UCS (Uniform-Cost Search) to solve the initial configuration generated in subtask 3. **Hint:** You may consider to use *heapq* package to implement priority queue.
5. Implement two informed searching methods: GBFS (Greedy best first search), and  $A^*$  to solve the initial configuration generated in subtask 3.
6. Visualize the number of expanded nodes for different values of  $N \in \{8, 15, 24, 35\}$ ,  $k \in \{3, 6, 9, 12, 15\}$  and searching method  $m \in \{BFS, UCS, GBFS, A^*\}$  using matplotlib. A possible outcome is visualized in Figure 6.
7. Visualize the runtime for different values of  $N \in \{8, 15, 24, 35\}$ ,  $k \in \{3, 6, 9, 12, 15\}$  and searching method  $m \in \{BFS, UCS, GBFS, A^*\}$  using matplotlib. A possible outcome is visualized in Figure 7.

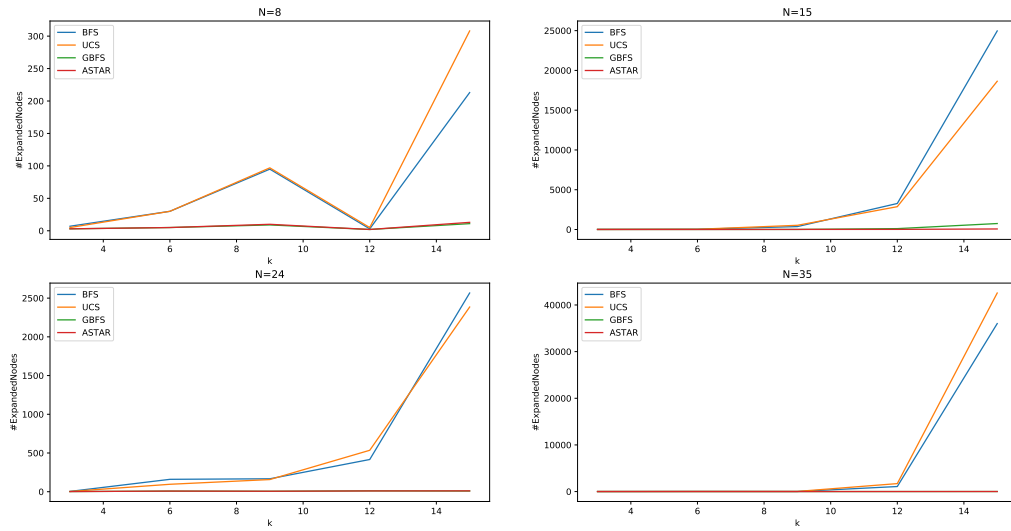


Figure 6: Task1-1

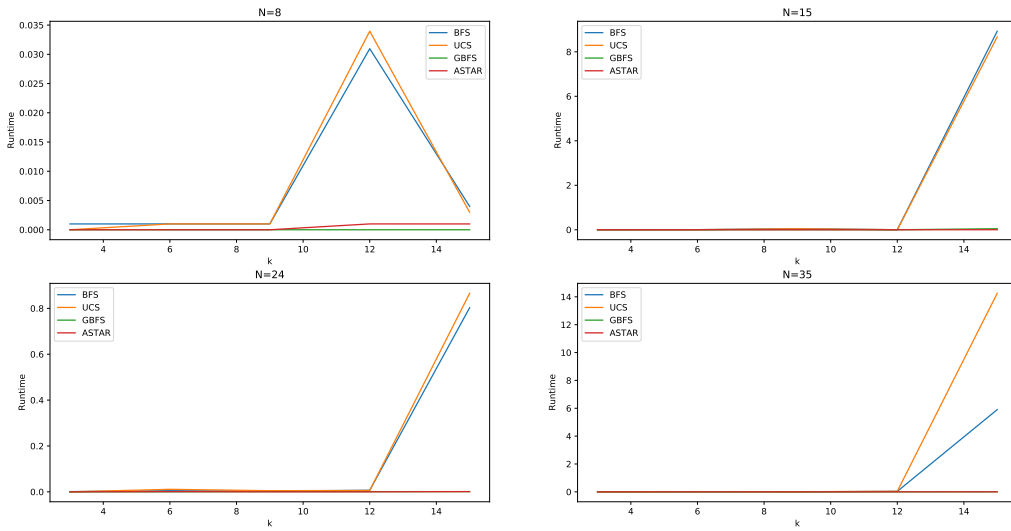


Figure 7: Task1-2