



Master in Computer Vision | Barcelona



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Module: 3D Vision
Project: Structure from Motion

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Goal

Reconstruction from uncalibrated images with a stratified method, by designing and applying a Structure from Motion (SfM) pipeline in order to achieve a 3D reconstruction.

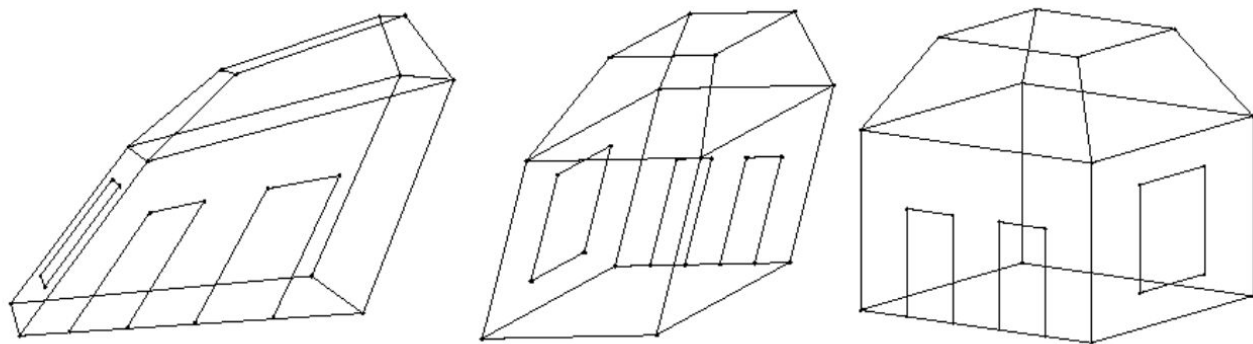
Mandatory Tasks:

• Computation of Projective cameras (for the case $n=2$)	1.0
• Affine and Metric rectification.....	4.0
○ Homography estimation	
• Estimation of reprojection error	1.0
• Bundle Adjustment.....	1.0
○ Intrinsic parameter factorization	
○ Construction and understanding of optimization formulation.....	1.0
■ Sparse Jacobian	
■ Non-Linear problem	
• Report	3.0

Optional Tasks

- Estimate affine homography from the 3 vanishing points and F (Alg.13.1 p332, result 10.3 p271) **(0.5)**
- Perform Bundle Adjustment over the estimation of the vanishing points and all available images, with PySBA. **(1.0)**
- Implement the resection method, as explained in MVG, Alg 7.1. **(2.0)**
- Implement track management for more than 2 images, with tracks structure **(1.0)**
- Investigate strategies to improve the pipeline: **(1.0)**
 - on results: number of points, reprojection error, camera poses.
 - on implementation: time of computation, resources, etc.

Affine And Metric Rectification



Affine Rectification

$$H_{a \leftarrow p} = \begin{pmatrix} I & \mathbf{0} \\ \mathbf{p}^T & 1 \end{pmatrix}$$

Projective to Affine Space.

\mathbf{p} is the plane to infinity. Which you find estimating the image vanishing points in the image.

How?

- Geometric and algebraic intuition
- Try to plot the vanishing point



Metric Rectification

$$H_{e \leftarrow a} = \begin{pmatrix} K^{-1} & \mathbf{0} \\ \mathbf{0}^T & 1 \end{pmatrix}$$

Projective to Euclidean Space.

Find the Absolute Conic Image

- **What is the Absolute Conic Image.**
- **Why is it relevant in our application?**
- **What assumptions you should make to estimate it?**
- Geometric and algebraic intuition

Metric Rectification

The key to metric reconstruction is to find the image of the absolute conic in one of the images $\omega = K^{-T} K^{-1}$

Suppose that the image of the absolute conic is known in some image to be ω , and one has an affine recons. in which the corresponding camera matrix is given by $P = [M|m]$. Then, the affine recons. may be transformed to a metric recons. by applying a 3D transformation of the form:

$$H_{e \leftarrow a} = \begin{pmatrix} A^{-1} & \mathbf{0} \\ \mathbf{0}^T & 1 \end{pmatrix}$$

where A is obtained by Cholesky factorization: $AA^T = (M^T \omega M)^{-1}$

Metric Rectification

The approach relies on identifying ω . There are various ways of doing this.

There are different kinds of constraints on ω :

- Constraints coming from scene orthogonality.
- Constraints coming from known internal parameters.
- Constraints arising from the same cameras (same matrix K) in all images.

Typically, a combination of these constraints is used.

Metric Rectification

Constraints coming from scene orthogonality

If \mathbf{v}_1 and \mathbf{v}_2 is a pair of vanishing points arising from orthogonal scene lines, then we have a linear constraint on ω :

$$\mathbf{v}_1^T \omega \mathbf{v}_2 = 0$$

Metric Rectification

Constraints coming from known internal parameters

Since

$$\omega = K^{-T} K^{-1} = \begin{pmatrix} \omega_{11} & \omega_{12} & \omega_{13} \\ \omega_{12} & \omega_{22} & \omega_{23} \\ \omega_{13} & \omega_{23} & \omega_{33} \end{pmatrix}$$

knowledge about some restrictions on the internal parameters contained in K may be used to constraint or determine the elements of ω .

If we assume the camera has zero skew, then $\omega_{12} = 0$.

If the pixels are square, that is, zero skew and $\alpha_x = \alpha_y$, then: $\omega_{11} = \omega_{22}$.

Metric Rectification

Combination of the previous constraints

Five constraints on ω :

$$\mathbf{u}^T \omega \mathbf{v} = 0$$

$$\mathbf{u}^T \omega \mathbf{z} = 0$$

$$\mathbf{v}^T \omega \mathbf{z} = 0$$

$$\omega_{11} = \omega_{22}$$

$$\omega_{12} = 0$$

In matrix form: $A\omega_V = \mathbf{0}$,

where $\omega_V = (\omega_{11}, \omega_{12}, \omega_{13}, \omega_{22}, \omega_{23}, \omega_{33})^T$

$$A = \begin{pmatrix} u_1 v_1 & u_1 v_2 + u_2 v_1 & u_1 v_3 + u_3 v_1 & u_2 v_2 & u_2 v_3 + u_3 v_2 & u_3 v_3 \\ u_1 z_1 & u_1 z_2 + u_2 z_1 & u_1 z_3 + u_3 z_1 & u_2 z_2 & u_2 z_3 + u_3 z_2 & u_3 z_3 \\ v_1 z_1 & v_1 z_2 + v_2 z_1 & v_1 z_3 + v_3 z_1 & v_2 z_2 & v_2 z_3 + v_3 z_2 & v_3 z_3 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & -1 & 0 & 0 \end{pmatrix}$$

The solution ω_V is the null vector of A .

Deliverables

- Jupyter Notebook with **all** auxiliary modules and files.
- Short report with
 - Analysis of process and results.
 - Problems, comments and conclusions.