

# Report on Backup Camera Simulation with Dynamic Trajectory

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## Introduction

This report outlines the implementation of a backup camera simulation with dynamic trajectory visualization. The simulation, based on a 10-second clip recorded from a phone's perspective, aims to overlay the trajectory of the rear wheels on the video. The project involves assumptions about steering geometry, vehicle dimensions, and the application of ADAS (Advanced Driver Assistance Systems) principles.

## Objective

The primary goal is to demonstrate proficiency in ADAS software development, understanding vehicle dynamics, and basic object classification. The simulation should accurately represent the trajectory of rear wheels during a backup maneuver.

## 1 Implementation

### 1.1 Vehicle Dimensions

The vehicle used for this project is a Toyota RAV4 with the following specifications:

- Wheelbase: 2.69 meters,
- Track Width: 1.69 meters,
- Steering Ratio: 14.3:1

### 1.2 Ackermann Steering Model

The Ackermann steering system, commonly used in car-like vehicles, minimizes tire slippage by adjusting the steering angles of the inner and outer wheels. Figure 1 illustrates this configuration, where  $w$  is the track width,  $l$  is the wheelbase,  $\phi_i$  and  $\phi_o$  are the steering angles, and  $r$  is the distance to the Instantaneous Center of Curvature (ICC).

The relationship between the Ackermann angle  $\phi$  and the steering wheel input  $\delta_{in}$  is defined by:

$$\phi = \frac{\delta_{in}}{\gamma} \quad (1)$$

Here,  $\phi$  is the Ackermann angle,  $\delta_{in}$  is the steering wheel input in radians, and  $\gamma$  is the steering ratio.

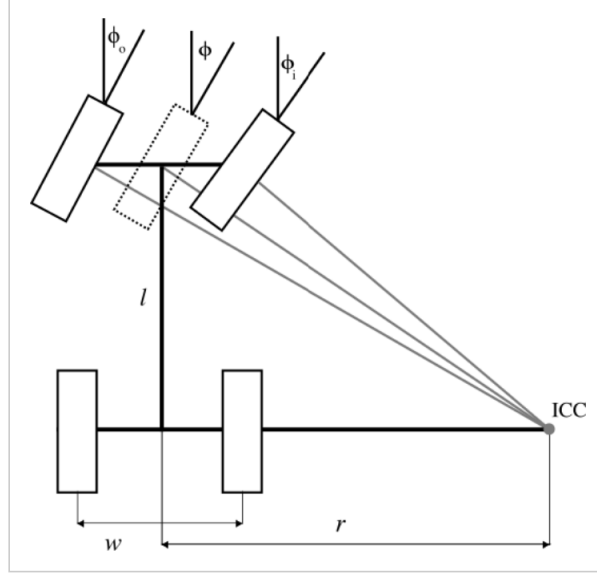


Figure 1: Simplified Ackermann Steering Model

To simulate the vehicle's trajectory, the heading direction was calculated based on the steering input over time. The forward kinematics, predicting the future state given the current configuration, is expressed as a quadruple  $(x, y, \theta, \phi)$  with  $\delta$  as the heading and  $(x, y)$  as the position. Given vehicle speed  $s$ , the angular velocity  $\omega$  is determined by:

$$\omega = \frac{s}{WB} \cdot \phi \quad (2)$$

Here,  $\omega$  is the angular velocity,  $WB$  is the wheelbase, and  $\phi$  is the Ackermann angle. Using Ackermann steering principles, the heading angle  $\theta$  was computed at each time step, capturing the vehicle's directional orientation.

The vehicle's position was determined using kinematic equations:

$$\dot{x} = s \cos \theta \quad (3)$$

$$\dot{y} = s \sin \theta \quad (4)$$

By iterating through these equations over a specified time period, a comprehensive trajectory of the rear wheels was generated.

### 1.3 3D to 2D Projection

The functions use a pinhole camera model for projecting 3D points onto the image plane, represented as:

$$sp = A[R|t]P_w$$

where:

- $P_w$  : 3D point in world coordinates
- $p$  : 2D pixel in the image plane
- $A$  : Camera intrinsic matrix
- $R$  : Rotation matrix
- $t$  : Translation vector
- $s$  : Arbitrary scaling (not part of the camera model)

For this project, 2D trajectory lines were converted to 3D by augmenting them with a constant depth, matching the camera height.

The camera intrinsic matrix  $A$  projects 3D points to 2D pixel coordinates:

$$p = AP_c, \quad A = \begin{bmatrix} f_x & 0 & c_x \\ 0 & f_y & c_y \\ 0 & 0 & 1 \end{bmatrix}$$

Calibration was performed using Zhang's Checkerboard method and OpenCV's calibration functions.

The joint rotation-translation matrix  $[R|t]$  involves a projective and homogeneous transformation:

$$Z_c \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} X_c \\ Y_c \\ Z_c \\ 1 \end{bmatrix}$$

Assuming the camera pose at the origin with a 70-degree clockwise rotation from the x-axis, the homogeneous transformation is:

$$P_c = [R|t]P_w, \quad [R|t] = \begin{bmatrix} r_{11} & r_{21} & r_{31} & t_x \\ r_{12} & r_{22} & r_{32} & t_y \\ r_{13} & r_{23} & r_{33} & t_z \end{bmatrix}$$

The overall projection is given by:

$$s \begin{bmatrix} uv \\ 1 \end{bmatrix} = \begin{bmatrix} f_x & 0 & c_x \\ 0 & f_y & c_y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} r_{11} & r_{21} & r_{31} & t_x \\ r_{12} & r_{22} & r_{32} & t_y \\ r_{13} & r_{23} & r_{33} & t_z \end{bmatrix} \begin{bmatrix} X_w \\ Y_w \\ Z_w \\ 1 \end{bmatrix}$$

Using OpenCV's `projectPoints` function, accurate estimations of points in the image plane were obtained with respect to the trajectory.

## 1.4 Video Visualization

In the final step, the trajectories are brought to life through a visual representation overlaid onto a sample reversing camera video.

This visualization dynamically adjusts the trajectories in response to the steering angle. The steering angle can remain constant, providing a straightforward view, or it can be dynamically altered using an interactive slider in a separate video interface. This real-time adjustment of the steering angle results in corresponding updates to the trajectories, enhancing the interactive and dynamic nature of the visualization.