

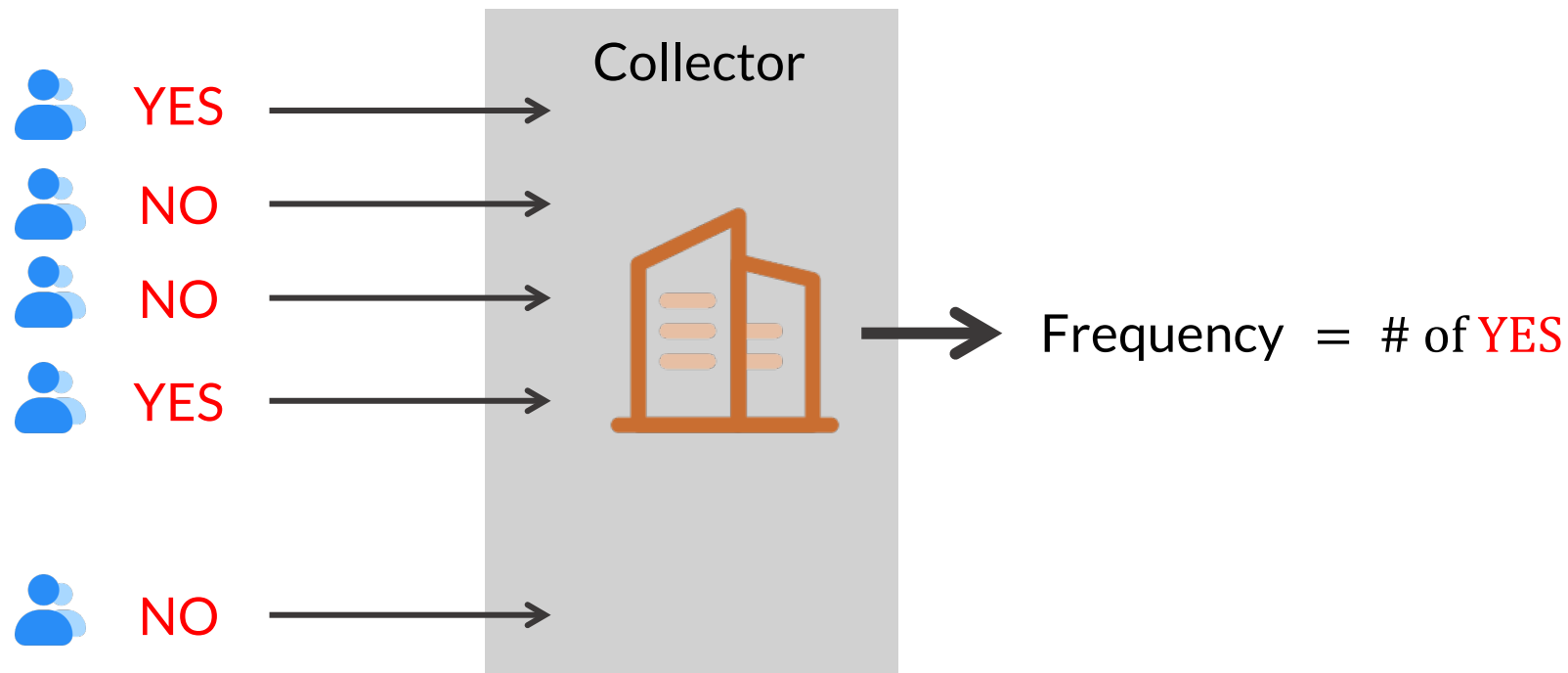
# Locally Differentially Private Frequency Estimation via Joint Randomized Response

Authors: [Ye Zheng](#), Shafizur Rahman Seeam, Yidan Hu, [Rui Zhang](#), [Yanchao Zhang](#)



# Frequency Estimation

- Social science: How many people engage in tax evasion?
  - ask one person if they had evaded tax
  - the person answers YES or NO



# Randomized Response for Privacy

- People have **privacy concerns** on sensitive/embarrassing question
  - i.e. don't want to let the collector know
- A **privacy mechanism**  $\mathcal{M}$  satisfies LDP if

For any truth  $x_1, x_2$ ,  
and randomized answer  $y$ :

$$\max \frac{\Pr[\mathcal{M}(x_1) = y]}{\Pr[\mathcal{M}(x_2) = y]} \leq e^\epsilon$$

Distinguishability of  $x_1$  (YES) and  $x_2$  (NO)  
from  $y$  (randomized answer)



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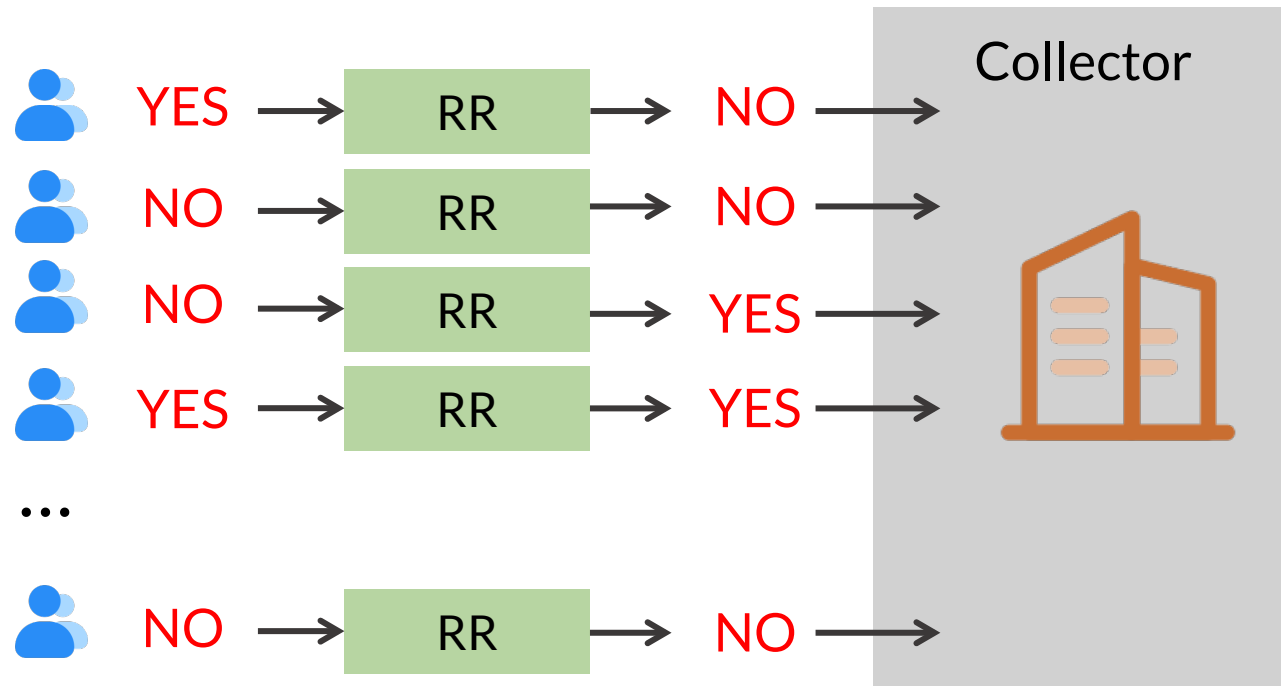
$$\max \frac{\Pr[\mathcal{M}(x_1) = y]}{\Pr[\mathcal{M}(x_2) = y]} \leq e^\epsilon$$

Distinguishability of  $x_1$  (YES) and  $x_2$  (NO)  
from  $y$  (randomized answer)

- **quantifiable hardness** to distinguish  $x_1$  (YES) and  $x_2$  (NO) from the randomized answer  $y$
- against inference from data collectors  or adversaries 

# Randomized Response for Privacy

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- Randomized Response: Randomize the truth **before answering the collector**



# Randomized Response for Privacy

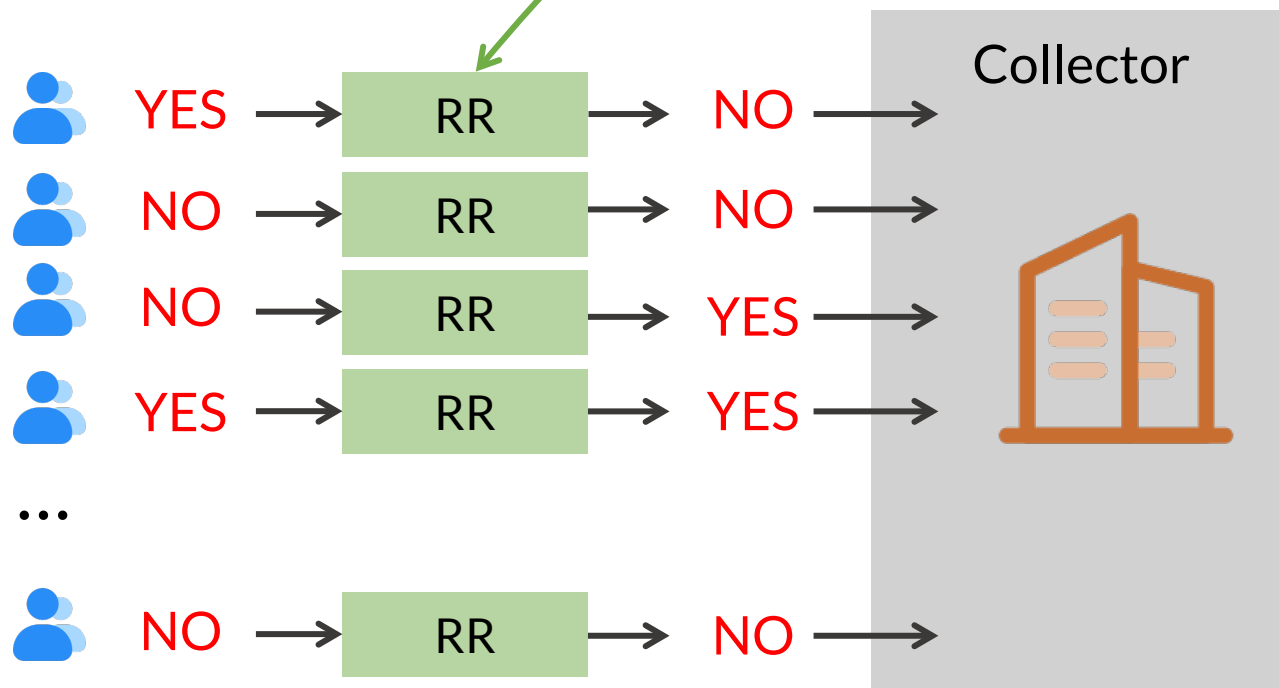
$$\max \frac{\Pr[\mathbf{RR}(x_1) = y]}{\Pr[\mathbf{RR}(x_2) = y]} \leq e^{\ln \frac{p}{1-p}}$$

- People have **privacy concerns** on sensitive/embarrassing questions - i.e. don't want to let the collector know
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Private

**RR:** [Warner, 1965]  
answer truth with probability  $p$

$$\mathbf{RR}(x) = \begin{cases} x & \text{w.p. } p \\ \neg x & \text{w.p. } 1 - p \end{cases}$$



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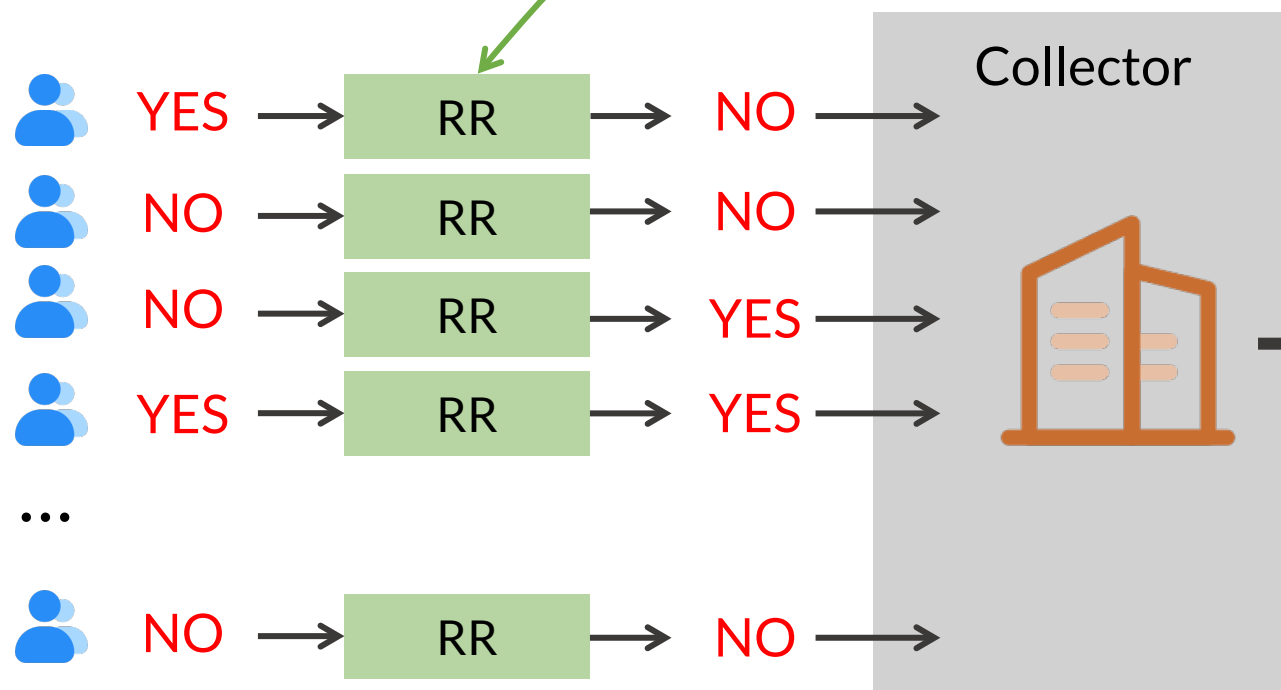
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estimated frequency

$$= \frac{\# \text{ of YES} - \# \text{ people} \times q}{p - q}$$

Unbiased:

expectation = truth

# Utility: RR's Variance

- Randomization reduces data utility

$$\text{Var}\left[\frac{\# \text{ of YES} - \# \text{ of people} \times q}{p - q}\right] = \frac{\text{Var}[\# \text{ of YES}]}{(p - q)^2} = \frac{npq}{(p - q)^2}$$

- summation of variance from  $n$  independent randomization



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- larger  $p \in (0.5, 1]$   $\rightarrow$  lower variance  $\rightarrow$  larger privacy parameter  $\epsilon$

$\uparrow$  data utility



$\downarrow$  privacy

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↓ privacy

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- Q: Can we improve this privacy-utility tradeoff?
  - yes, by correlated (joint) randomization

# This Paper: Joint RR (JRR)

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RR: Joint distribution

	$T_1 = 1$	$T_1 = 0$	Truthfulness of $x_1$
$T_2 = 1$	0.64 ( $= p^2$ )	0.16 ( $= pq$ )	
$T_2 = 0$	0.16 ( $= pq$ )	0.04 ( $= q^2$ )	

Truthfulness  
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**Independent  $T_1$  and  $T_2$**  ( $P[T_1 \cap T_2] = P[T_1] \cdot P[T_2]$ )

Joint probability =  $\Pi$  of marginal probabilities

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$T_2 = 1$	0.6 ( $= p^2 + \rho pq$ )	0.2 ( $= pq - \rho pq$ )
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$P[T_1 = 1] = 0.8$

$P[T_1 = 0 \cap T_2 = 0] = 0 \neq P[T_1 = 0] \cdot P[T_2 = 0] = 0.04$

NOT independent  $T_1$  and  $T_2$

Joint probability  $\neq$   $\Pi$  of marginal probabilities

Frequency Estimation

# Utility: JRR's Variance

- Same estimator as RR

$$\underset{\substack{\uparrow \\ \text{Expectation}}}{E[\# \text{ of YES}]} = \sum_{i=1}^{\# \text{ 👤}} P[y_i = \text{YES}] = n_{\text{YES}} \cdot p + (\# \text{ 👤} - n_{\text{YES}}) \cdot q$$

$\underset{\substack{\uparrow \\ \text{Ground truth}}}{n_{\text{YES}}}$  $\nearrow$

# Utility: JRR's Variance

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$$E[\# \text{ of YES}] = \sum_{i=1}^{\# \text{ people}} P[y_i = \text{YES}] = n_{\text{YES}} \cdot p + (\# \text{ people} - n_{\text{YES}}) \cdot q$$

→ Unbiased estimator  $\hat{n}_{\text{YES}} = \frac{\# \text{ of YES} - 2q}{p - q}$

Identical to RR

# Utility: JRR's Variance

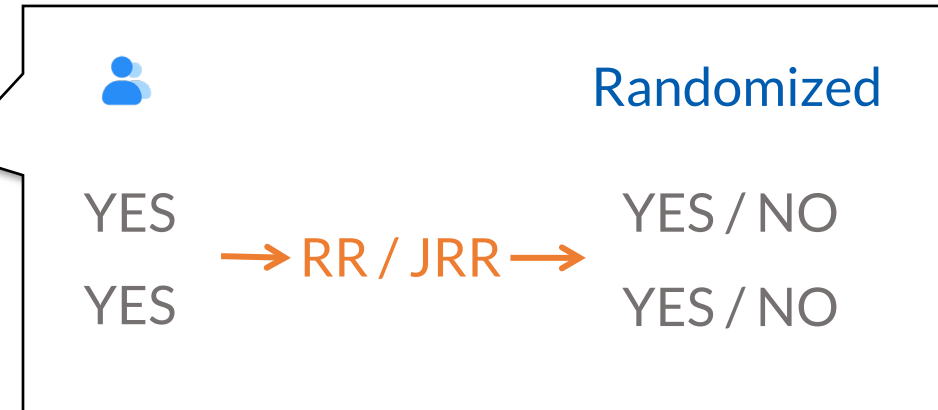
- Variance: ( $\# \text{ people} = 2, p = 0.8$ )

$$\text{Var}[\hat{n}_{\text{YES}}] = \frac{\text{Var}[\# \text{ of YES}]}{(0.8 - 0.2)^2}$$

# Utility: JRR's Variance

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- Distribution table:

RR

# of YES	0	1	2
Probability	0.04	0.16 + 0.16	0.64

$$\text{Var}[\# \text{ of YES}] = E[(X - \mu)^2] = \mathbf{0.32}$$

$$= \sum_{X=0,1,2} (X - 1.6)^2 \cdot \text{Pr}[X] \approx \mathbf{0.1 + 0.12 + 0.1}$$

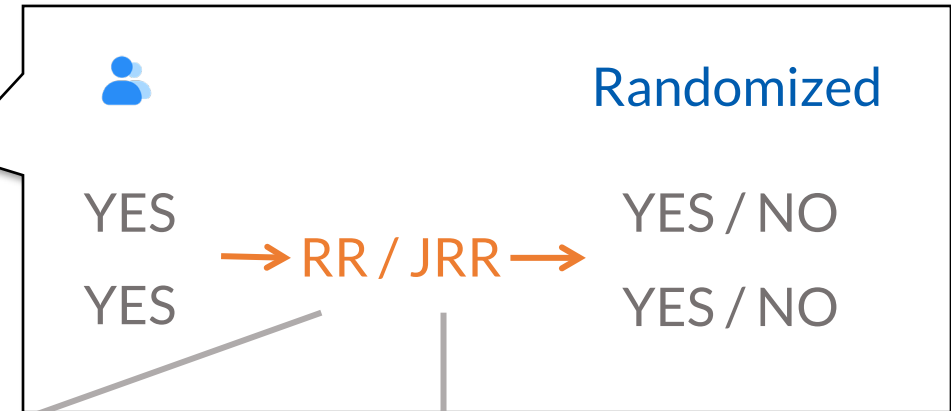
JRR

# of YES	0	1	2
Probability	0	0.2 + 0.2	0.6

$$\text{Var}[\# \text{ of YES}] = E[(X - \mu)^2] = \mathbf{0.24}$$

$$= \sum_{X=0,1,2} (X - 1.6)^2 \cdot \text{Pr}[X] = \mathbf{0 + 0.14 + 0.1}$$

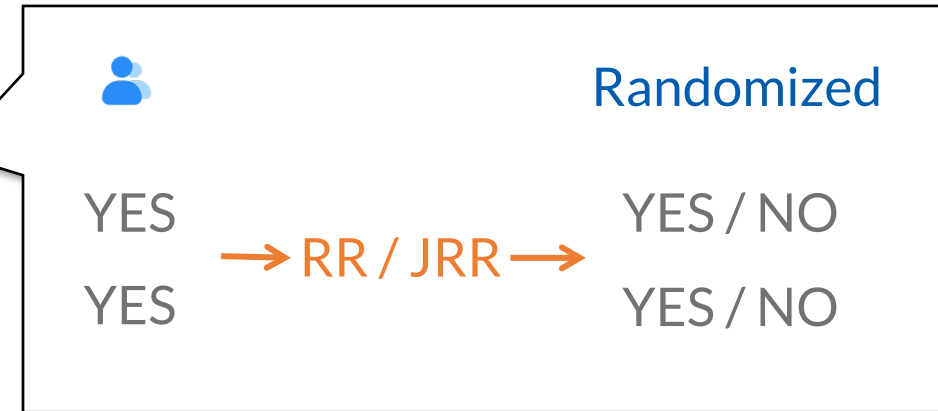
Frequency Estimation via Joint Randomization



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- Variance: (# 👤 = 2,  $p = 0.8$ )

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- Distribution table:

RR

# of YES	0	1	2
Probability	0.04	0.16 + 0.16	0.64

Better utility

JRR (near to  $\mu$ )

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Probability	0	0.2 + 0.2	0.6

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Frequency Estimation via Joint Randomized Response

# JRR's General Form

- Correlated randomization with 2 persons  $x_{2i-1}$  and  $x_{2i}$

JRR: Joint distribution

	$T_{2i-1} = 1$	$T_{2i-1} = 0$
$T_{2i} = 1$	$p^2 + \rho pq$	$(1 - \rho)pq$
$T_{2i} = 0$	$(1 - \rho)pq$	$q^2 + \rho pq$

$\rho \in [-1,1]$ :  
correlation coefficient



- RR is a special case of JRR with  $\rho = 0$  (no correlation)



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**Utility Theorem.** The variance of JRR's estimator  $\hat{n}_v$  is

$$\text{Var}[\hat{n}_v] = \frac{pq}{(p - q)^2} \cdot \left( n + \frac{\rho((2n_{\text{YES}} - n)^2 - n)}{n - 1} \right).$$

# Privacy: NOT as Simple as RR

- If any person can be an adversary

JRR: Joint distribution

	$T_1 = 1$	$T_1 = 0$
$T_2 = 1$	0.6	0.2
$T_2 = 0$	0.2	0

$T_1$ : I am an adversary 🤖

When I report untruthfully ( $T_1 = 0$ ),  
My partner will report truthfully ( $T_2 = 1$ )

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- Correlation results in privacy leakage


# JRR – Privacy Model in This Paper

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- Form random 2-person groups for correlated randomization

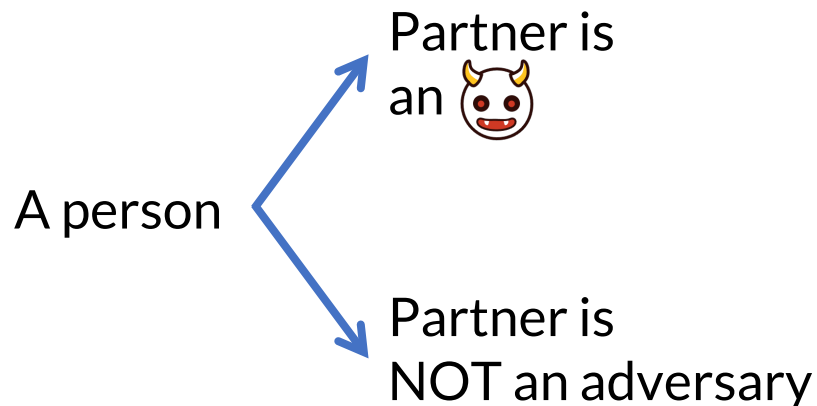
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- Form random 2-person groups for correlated randomization
- **Threat model:**
  - any person can be an adversary 
  - if a group contains an adversary, the adversary knows **who is their partner** (after random grouping)

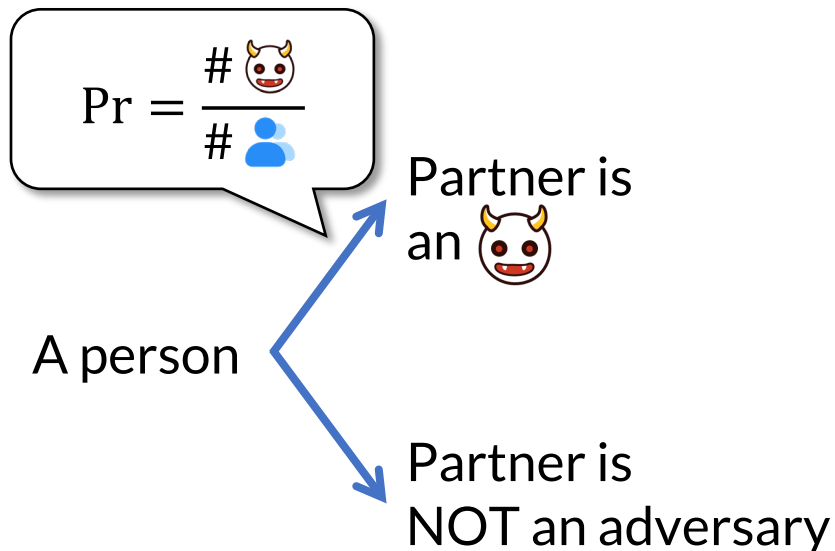
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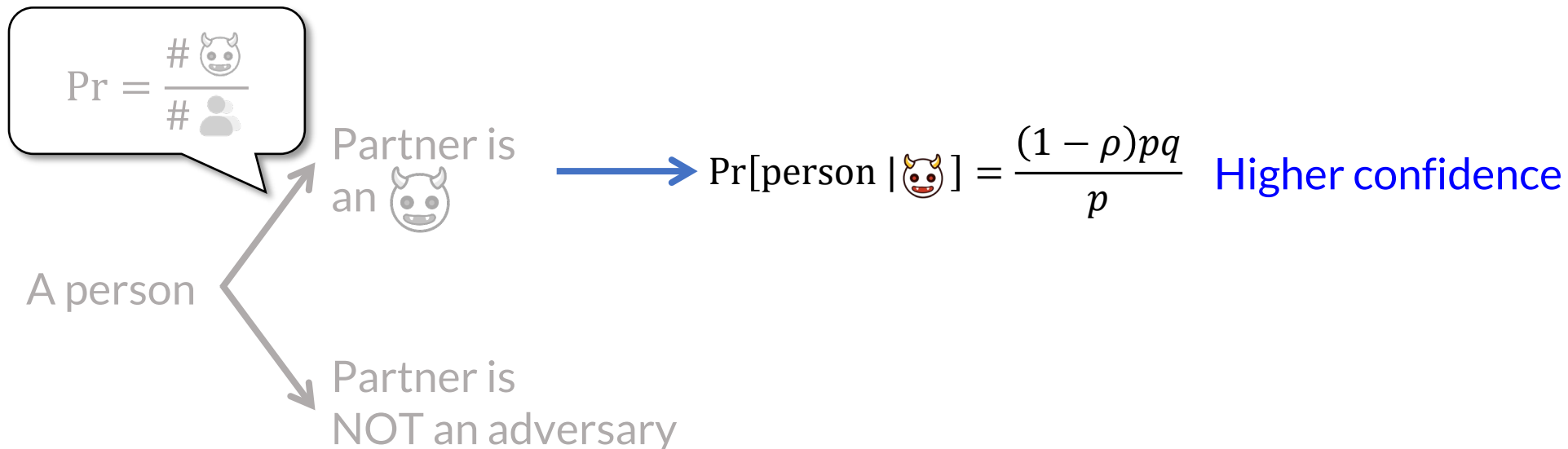
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# JRR – Privacy Model in This Paper

- Form random 2-person groups for correlated randomization
- **Threat model:**
  - if a group contains an adversary, the adversary knows who is their partner (after random grouping)
  - the adversary cannot control randomness, but can **infer their partner's**





# JRR – Formal Privacy & Utility

**Privacy Theorem.** Assume a set of data contributors  $\mathcal{T}_m$  whose reporting truthfulness is known to the adversary. For any data contributor  $i$ , the JRR mechanism satisfies:

$$\frac{\Pr[\text{JRR}(x_i) | \mathcal{T}_m]}{\Pr[\text{JRR}(x'_i) | \mathcal{T}_m]} \leq e^\varepsilon, \text{ where } \varepsilon = \ln \frac{mp_{\max} + (n - m - 1)p}{mp_{\min} + (n - m - 1)q}.$$

**Privacy affected by**

$m$	# adversaries 🐉
$n$	# of persons 👤
$\rho$	Correlated coefficient

$p_{\max} = \max\{(1 - \rho)p, p + \rho q\}$ :  
confidence of adversaries  
inferring a specific value

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**privacy constraint**

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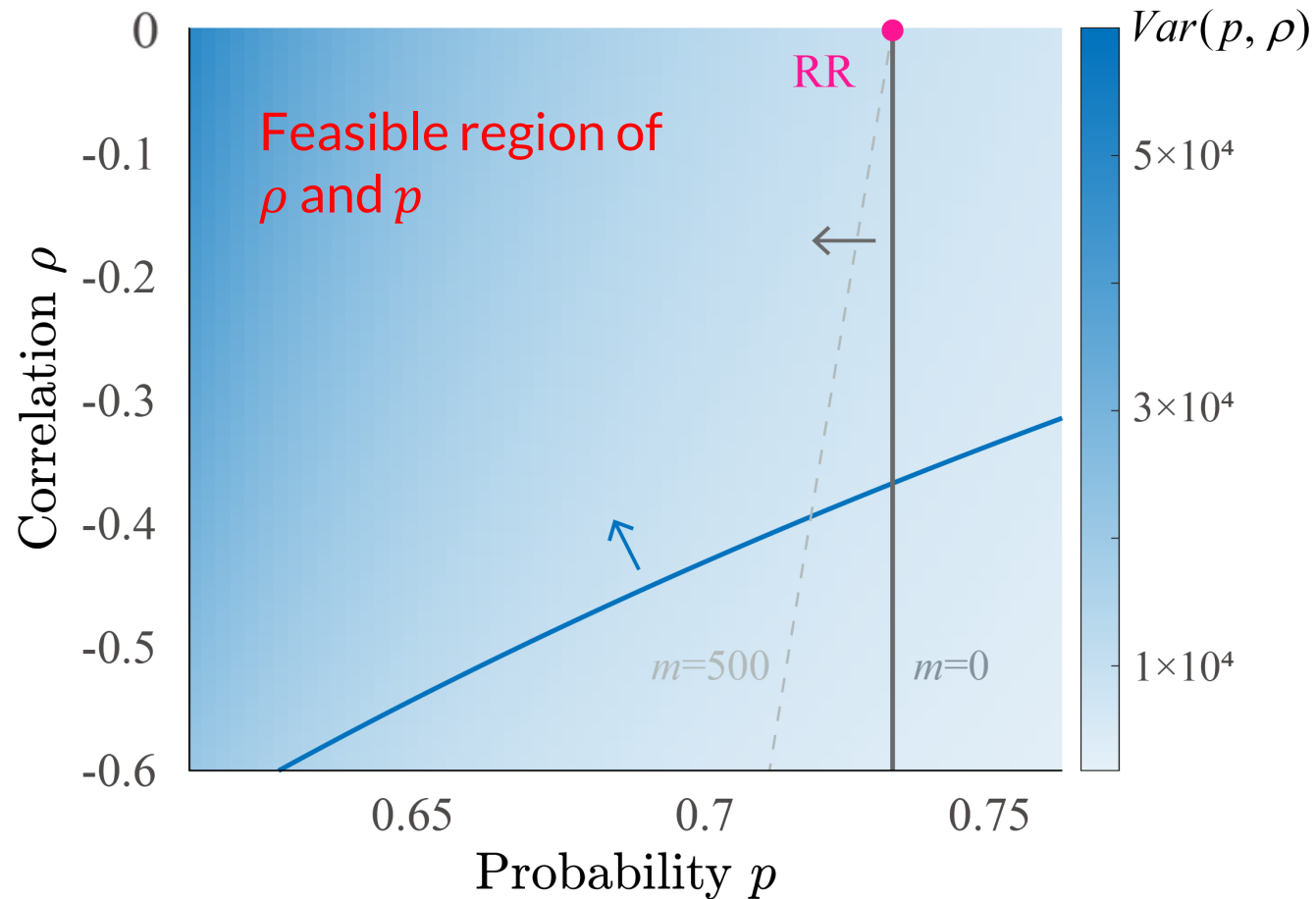
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**minimize**

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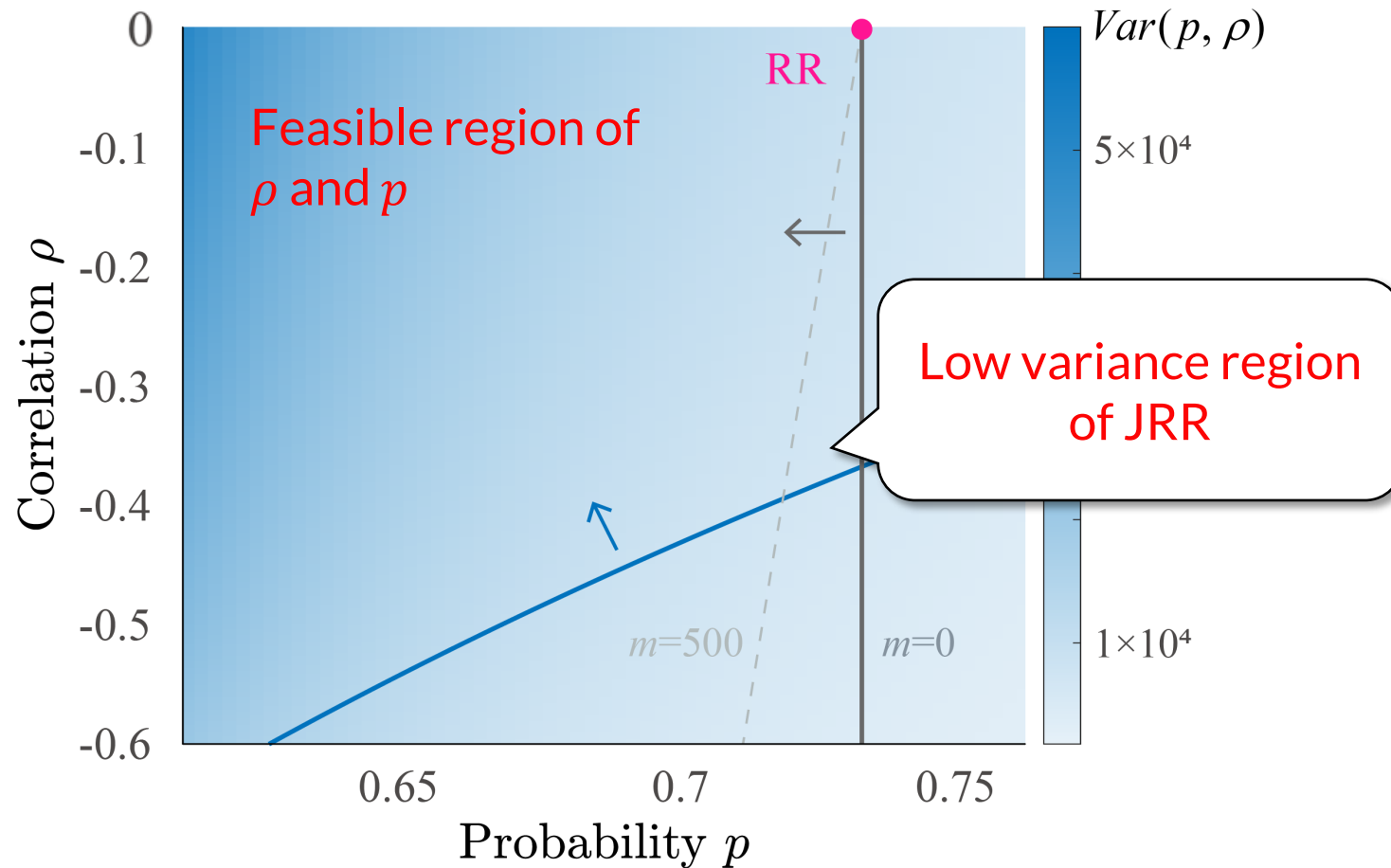
# JRR – Variance Heatmap

- Effect of  $\rho$  and  $p$  (when  $\varepsilon = 1$ ,  $n = 10^4$ ,  $n_{\text{Yes}} = 200$ , and  $m = 0$  &  $500$ )



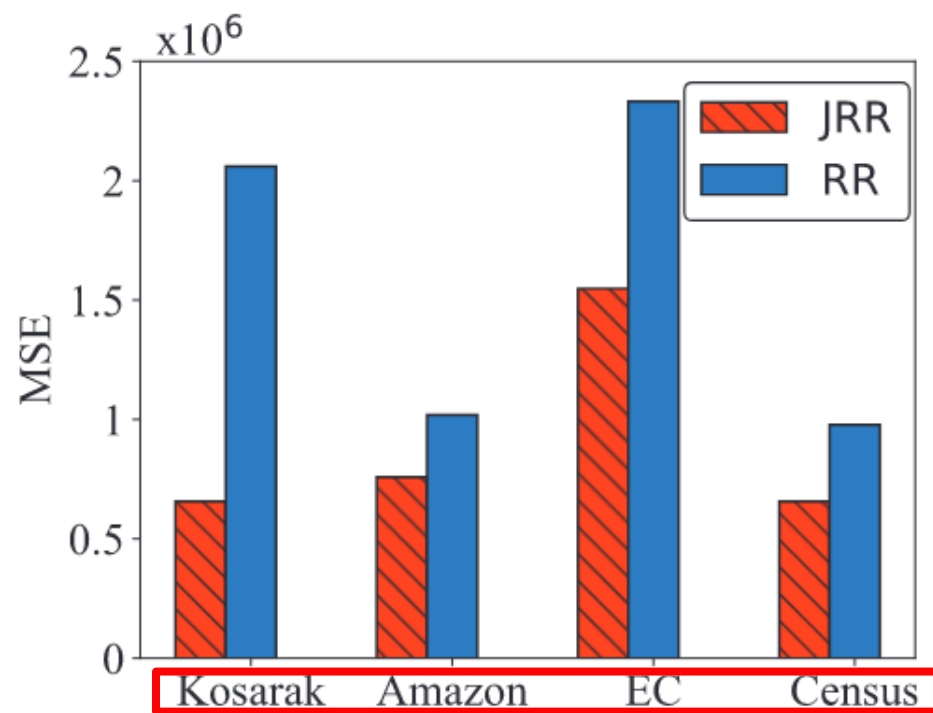
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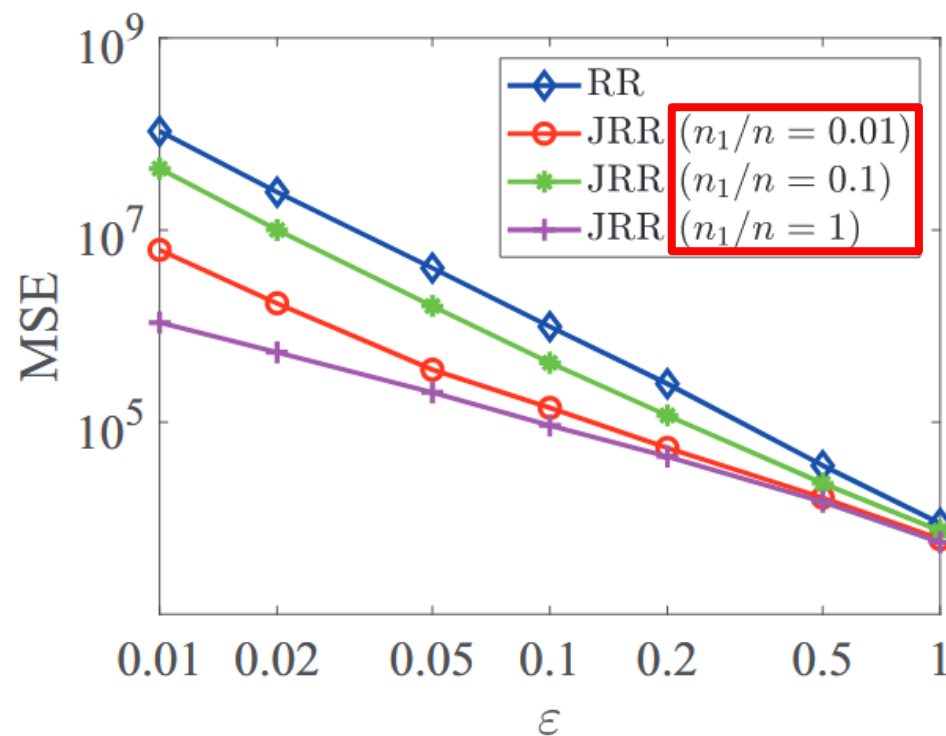


# Experiments

- Comparison with RR under the same privacy level - JRR:  $\varepsilon(n, m, \rho, p)$ , RR:  $\varepsilon(p)$



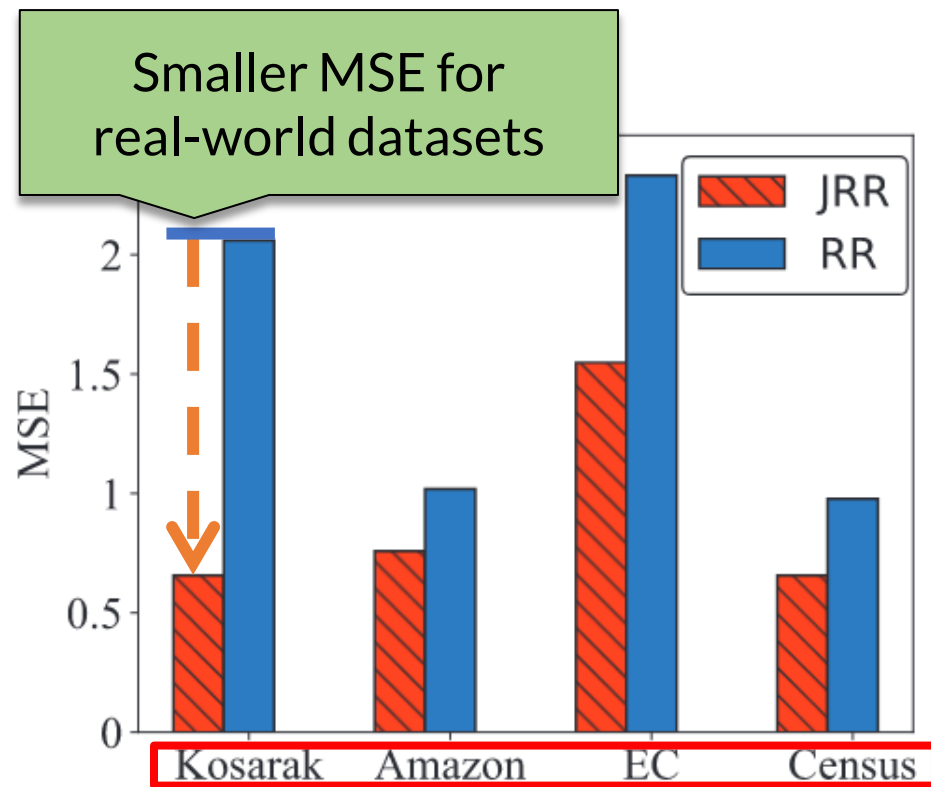
Real-world datasets ( $\varepsilon = 0.1$ )



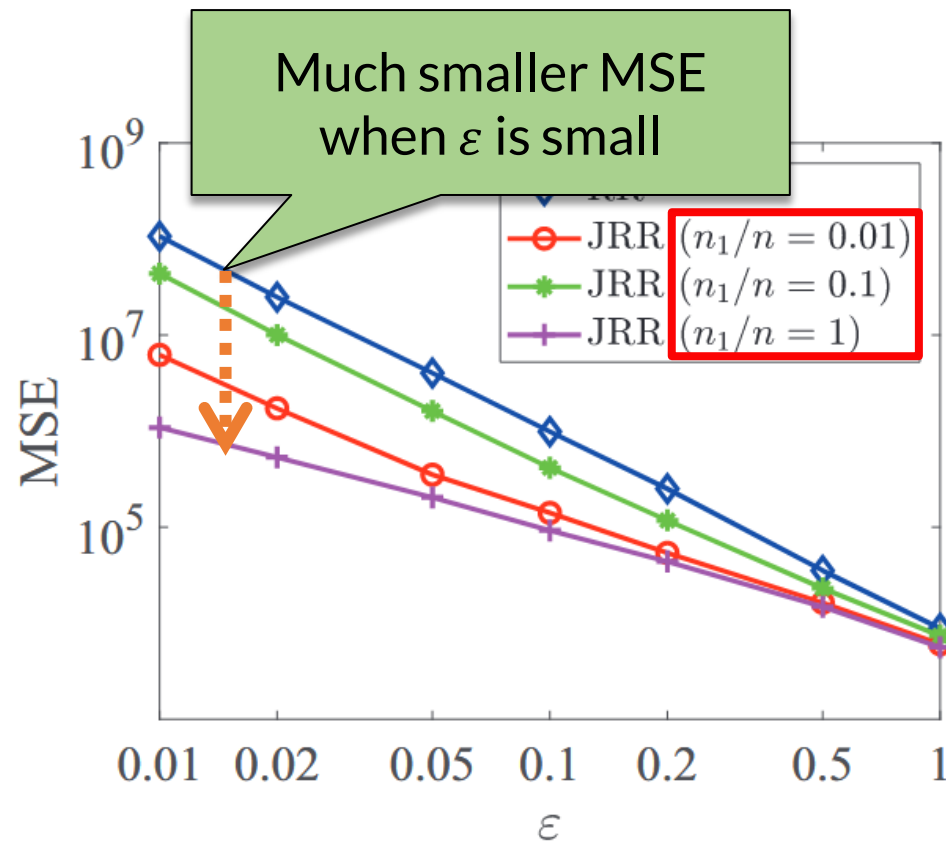
Synthetic datasets ( $n = 10^4$ )

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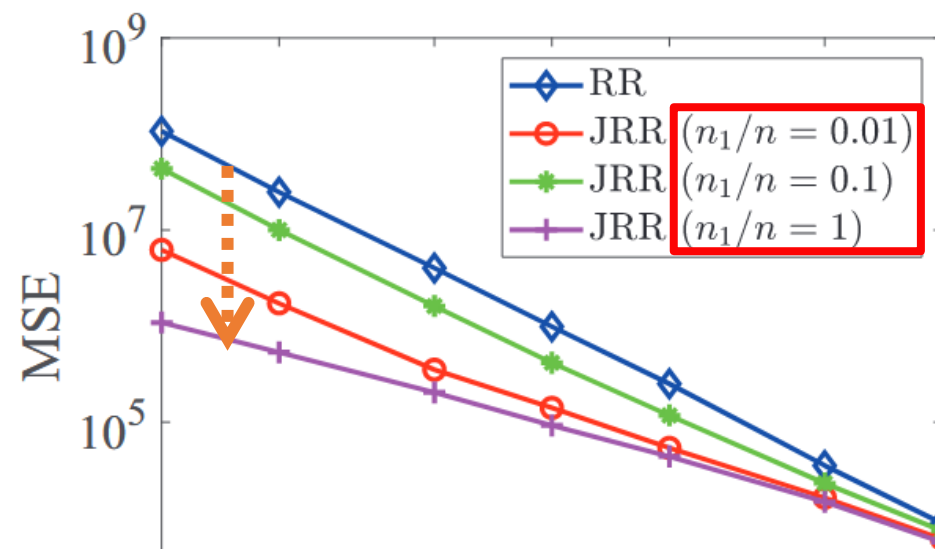
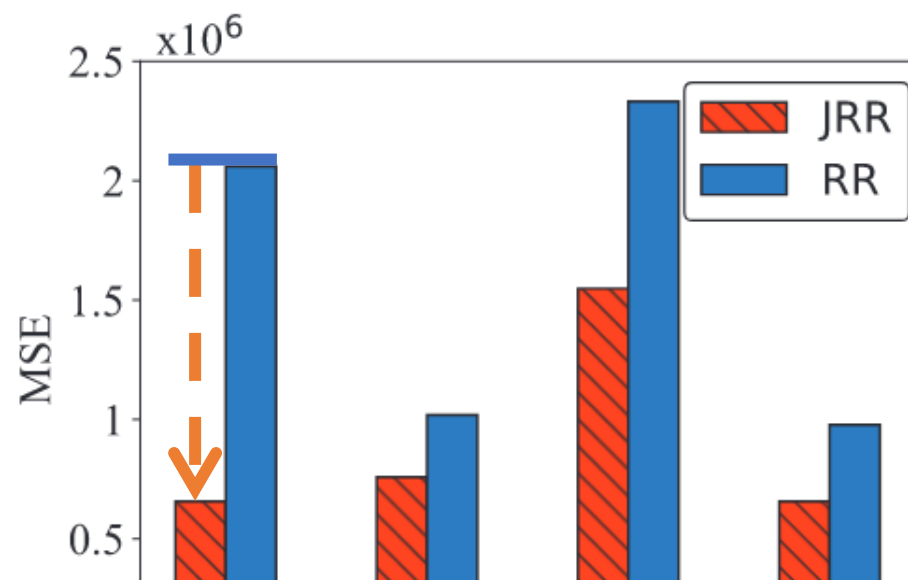
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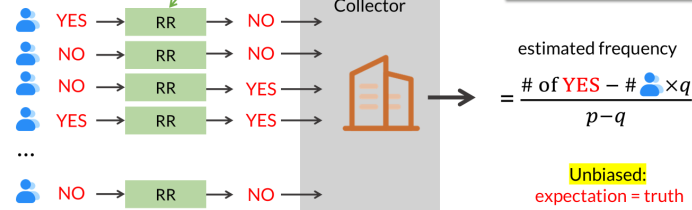
- Correlated randomization can improve the data utility of frequency estimation
- JRR: Privacy & utility model for correlated randomization**



# Locally Differentially Private Frequency Estimation via Joint Randomized Response

## Randomized Response for Privacy

- People have **privacy concerns** on sensitive/embarrassing questions - i.e. don't want to let the collector know
- Randomized Response: Randomize the truth before answering



Ye Zheng

Locally Differentially Private Frequency Estimation via Joint Randomized Response

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Locally Differentially Private Frequency Estimation via Joint Randomized Response

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## This Paper: Joint RR (JRR)

- JRR: Better data utility by joint randomization
- Example: 2-person ( $x_1 = \text{YES}$  and  $x_2 = \text{YES}$ ) with  $p = 0.8$  ( $P[T = 1] = 0.8$ )

RR: Joint distribution

	$T_1 = 1$	$T_1 = 0$
$T_2 = 1$	0.64 ( $= p^2$ )	0.16 ( $= pq$ )
$T_2 = 0$	0.16 ( $= pq$ )	0.04 ( $= q^2$ )

Truthfulness of  $x_2$

Independent  $T_1$  and  $T_2$  ( $P[T_1 \cap T_2] = P[T_1] \cdot P[T_2]$ )

Joint probability =  $\Pi$  of marginal probabilities

JRR: Joint distribution

	$T_1 = 1$	$T_1 = 0$
$T_2 = 1$	0.6 ( $= p^2 + \rho pq$ )	0.2 ( $= pq - \rho pq$ )
$T_2 = 0$	0.2 ( $= pq - \rho pq$ )	0 ( $= q^2 + \rho pq$ )

$P[T_1 = 0 \cap T_2 = 0] = 0 \neq P[T_1 = 0] \cdot P[T_2 = 0] = 0.04$

NOT independent  $T_1$  and  $T_2$

Joint probability  $\neq \Pi$  of marginal probabilities

## JRR - Privacy Model in This Paper

- Randomly groups into form 2-person groups for correlated randomization
- Threat model:**
  - if a group contains an adversary, the adversary knows who is their partner (after random grouping)
  - the adversary cannot control randomness, but can **infer their partner's**



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## Utility: JRR's Variance

- Variance: ( $\# = 2, p = 0.8$ )

$$\text{Var}[\hat{n}_{\text{YES}}] = \frac{\text{Var}[\# \text{ of YES}]}{(0.8 - 0.2)^2}$$

- Distribution table:

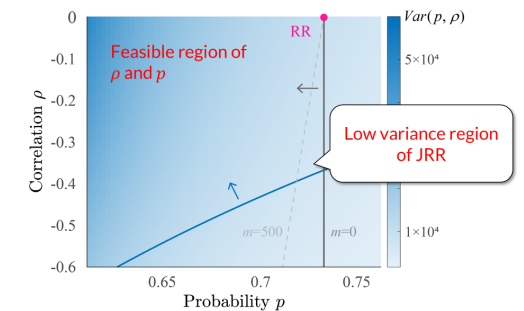
RR				JRR (near to $\mu$ )			
# of YES	0	1	2	# of YES	0	1	2
Probability	0.04	0.16 + 0.16	0.64	Probability	0	0.2 + 0.2	0.6

Var[# of YES] =  $E[(X - \mu)^2] = 0.32$

Var[# of YES] =  $E[(X - \mu)^2] = 0.24$

## JRR - Variance Heatmap

- Effect of  $\rho$  and  $p$  (when  $\epsilon = 1, n = 10^4, n_{\text{YES}} = 200$ , and  $m = 0$  & 500)



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Thank you!



# Privacy Model

- No need of random grouping:
  - when **one** person hold **multiple** items

