## Supplementary Material: Robust Two-Layer Partition Clustering of Sparse Multivariate Functional Data

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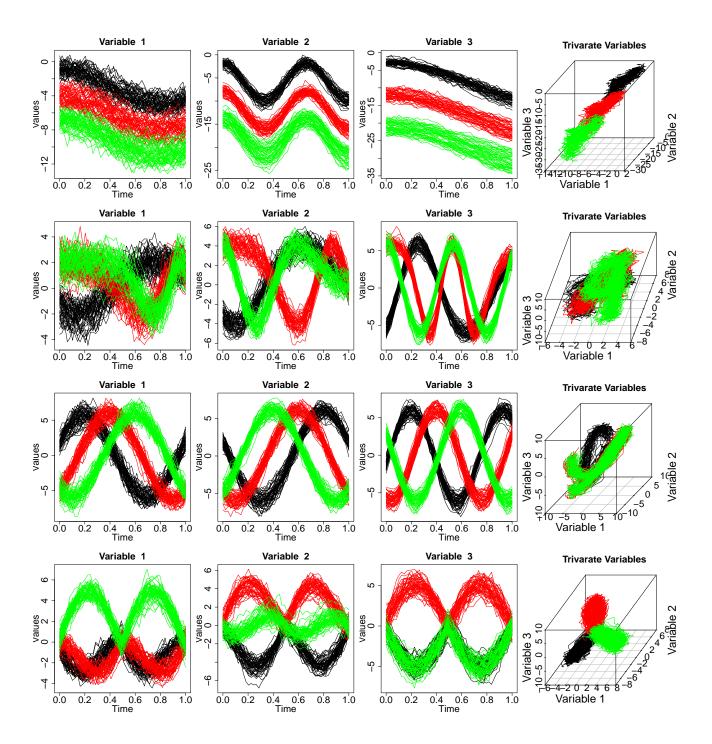
October 9, 2022

This Supplementary Material provides the results of Scenarios 1-6 in the Simulation Studies. First, we present one simulation of all the above scenarios without the outlier and sparseness corruption. Next, we display the performance of clustering for Scenarios 1-6. Then, we show the performance of outlier detection for Scenarios 1-6.

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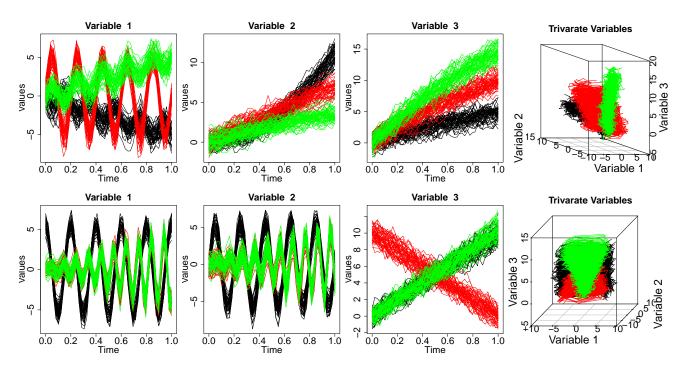


Figure S1: Rows from top to down represent samples from Scenario 1-6, respectively. Three clusters are represented in black, red, and green.

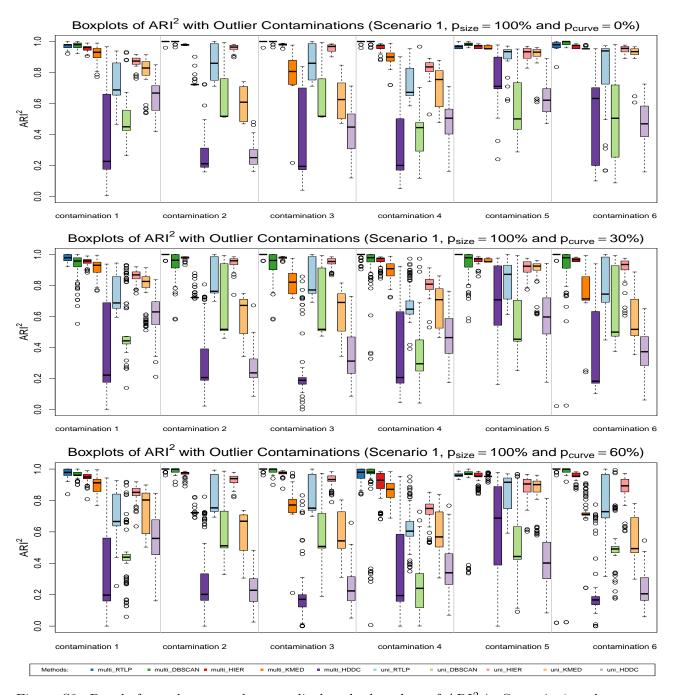


Figure S2: Panels from the top to bottom display the boxplots of ARI<sup>2</sup> in Scenario 1 under  $p_{curve} = 0,30\%$  and 60%. Ten methods are compared in all settings with six contaminations. Here, K=3 and 100 simulation replicates. The methods from left to right are the multivariate and average marginal univariate versions of RTLP, DBSCAN, agglomerative hierarchical, K-medoids, and funHDDC methods.

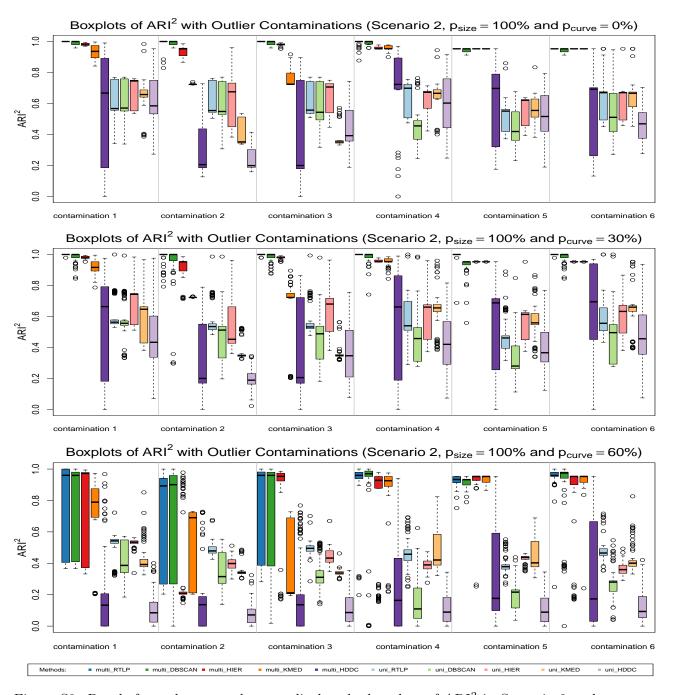


Figure S3: Panels from the top to bottom display the boxplots of ARI<sup>2</sup> in Scenario 2 under  $p_{curve} = 0,30\%$  and 60%. Ten methods are compared in all settings with six contaminations. Here, K=3 and 100 simulation replicates. The methods from left to right are the multivariate and average marginal univariate versions of RTLP, DBSCAN, agglomerative hierarchical, K-medoids, and funHDDC methods.

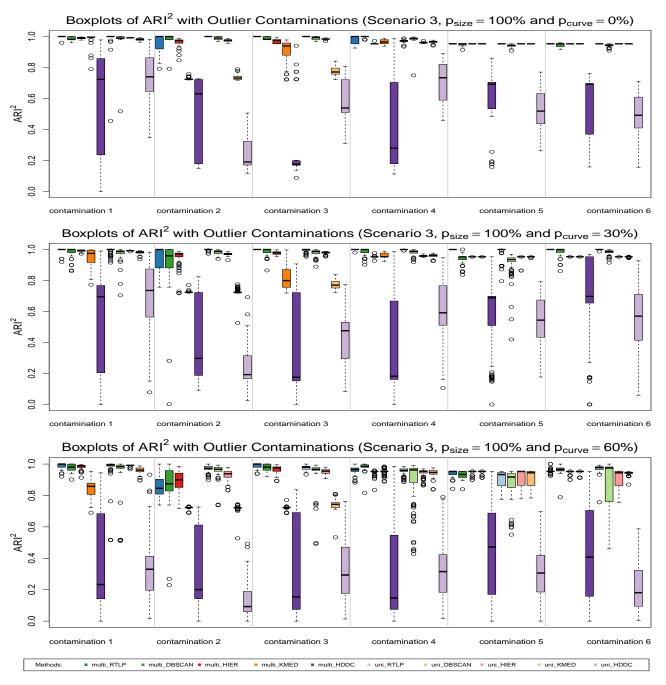


Figure S4: Panels from the top to bottom display the boxplots of ARI<sup>2</sup> in Scenario 3 under  $p_{curve} = 0,30\%$  and 60%. Ten methods are compared in all settings with six contaminations. Here, K=3 and 100 simulation replicates. The methods from left to right are the multivariate and average marginal univariate versions of RTLP, DBSCAN, agglomerative hierarchical, K-medoids, and funHDDC methods.

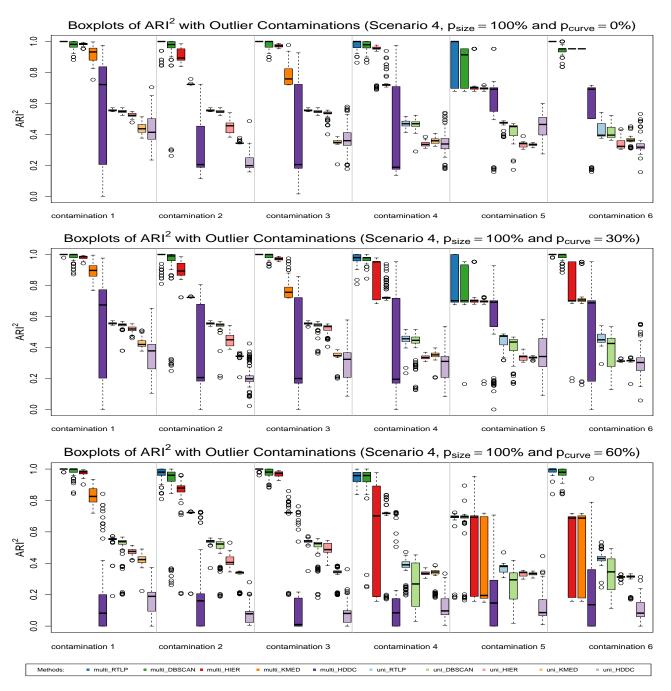


Figure S5: Panels from the top to bottom display the boxplots of ARI<sup>2</sup> in Scenario 4 under  $p_{curve} = 0,30\%$  and 60%. Ten methods are compared in all settings with six contaminations. Here, K=3 and 100 simulation replicates. The methods from left to right are the multivariate and average marginal univariate versions of RTLP, DBSCAN, agglomerative hierarchical, K-medoids, and funHDDC methods.

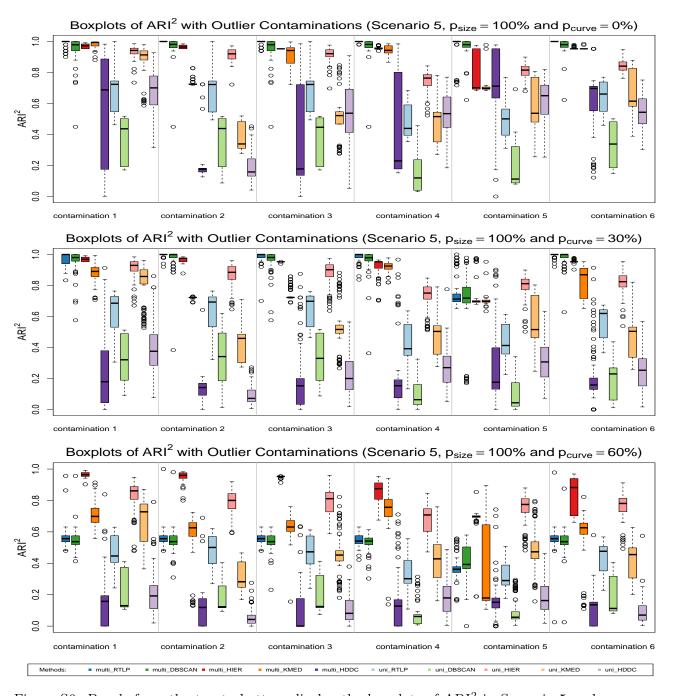


Figure S6: Panels from the top to bottom display the boxplots of ARI<sup>2</sup> in Scenario 5 under  $p_{curve} = 0,30\%$  and 60%. Ten methods are compared in all settings with six contaminations. Here, K=3 and 100 simulation replicates. The methods from left to right are the multivariate and average marginal univariate versions of RTLP, DBSCAN, agglomerative hierarchical, K-medoids, and funHDDC methods.

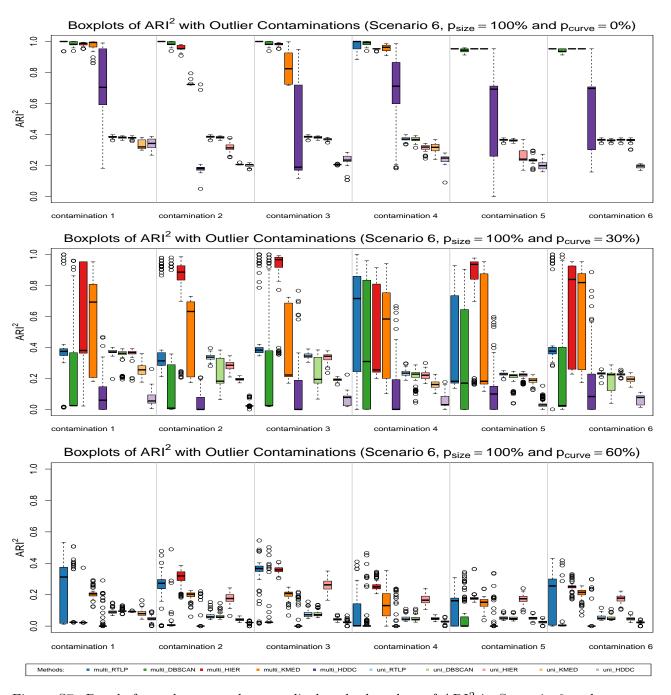


Figure S7: Panels from the top to bottom display the boxplots of ARI<sup>2</sup> in Scenario 6 under  $p_{curve} = 0,30\%$  and 60%. Ten methods are compared in all settings with six contaminations. Here, K=3 and 100 simulation replicates. The methods from left to right are the multivariate and average marginal univariate versions of RTLP, DBSCAN, agglomerative hierarchical, K-medoids, and funHDDC methods.

Table S1: Correct outlier detection percentage  $p_c$  (%) and false outlier detection percentage  $p_f$  (%) of multivariate and univariate versions of in different outlier contaminations for Scenarios 1-6. We name multi\_RTLP (uni\_RTLP) multivariate (univariate) in the Methods and write the higher  $p_c$  and the lower  $p_f$  in bold in each setting given the contamination and  $p_{curve}$ . The proportion of outliers is 10%, and  $p_{size} = 100\%$  in all settings. Simulations with 100 replicates.

		( ) (	y				
	Methods	(a) S Contamir	Scenario 1	Contamin	ation 2	Contamin	ation 3
$p_{curve}$		$p_c$	$p_f$	$p_c$			$p_f$
Peurve	7					$p_c$	
	multi_RTLP	92.0 (6.8)	<b>0.1</b> (0.3)	99.5 (1.8)	<b>0.1</b> (0.2)	99.7 (1.3)	<b>0.1</b> (0.2)
0%	multi_DBSCAN	<b>92.4</b> (6.2)	1.7 (2.3)	99.7 (1.5)	2.1 (2.9)	<b>99.7</b> (1.3)	2.1 (2.9)
	uni_RTLP	63.6 (9.6)	0.2 (0.3)	96.0 (3.2)	0.2 (0.3)	96.1 (3.0)	0.2 (0.4)
	uni_DBSCAN	65.0 (9.1)	0.5 (0.5)	96.2 (3.0)	0.7(0.9)	96.1 (3.0)	0.7(0.9)
	multi_RTLP	92.3 (6.3)	<b>0.0</b> (0.0)	99.8 (1.1)	<b>0.0</b> (0.1)	99.8 (1.1)	<b>0.0</b> (0.1)
30%	multi_DBSCAN	<b>92.4</b> (6.2)	2.0(3.5)	<b>100.0</b> (0.0)	2.5(3.7)	<b>100.0</b> (0.0)	2.5(3.7)
3070	uni_RTLP	65.9 (8.5)	0.2(0.5)	100.0 (0.3)	0.3(0.5)	99.5 (1.0)	0.2(0.5)
	uni_DBSCAN	66.3 (8.3)	0.5 (0.8)	100.0 (0.3)	0.9 (1.0)	99.5 (1.0)	0.8 (1.0)
	multi_RTLP	92.0 (6.8)	<b>0.1</b> (0.3)	<b>99.5</b> (1.8)	<b>0.1</b> (0.2)	<b>99.7</b> (1.3)	<b>0.1</b> (0.2)
60%	multi_DBSCAN	<b>92.5</b> (6.2)	1.1 (2.7)	<b>99.5</b> (1.8)	1.3 (2.9)	<b>99.7</b> (1.3)	1.4 (2.9)
0076	uni_RTLP	65.5 (8.6)	0.2 (0.3)	96.0 (3.2)	0.2 (0.3)	96.1 (3.0)	0.3(0.5)
	uni_DBSCAN	66.3 (8.2)	0.6 (0.6)	96.2 (3.0)	0.9 (1.1)	96.1 (3.0)	0.9 (0.9)
	Methods	Contamination 4		Contamin	ation 5	Contamin	ation 6
$p_{curve}$		$p_c$	$p_f$	$p_c$	$p_f$	$p_c$	$p_f$
	multi_RTLP	99.2 (2.9)	<b>0.0</b> (0.4)	98.4 (11.4)	<b>0.1</b> (0.5)	94.1 (12.1)	0.4 (1.2)
0%	multi_DBSCAN	<b>99.3</b> (2.5)	2.0 (2.9)	<b>100.0</b> (0.0)	2.4 (3.1)	<b>100.0</b> (0.0)	3.0 (3.7)
070	uni_RTLP	62.5 (14.3)	0.1 (0.4)	76.3 (14.2)	0.2(0.5)	84.3 (15.7)	<b>0.2</b> (0.3)
	uni_DBSCAN	41.7 (12.3)	0.1 (0.4)	99.1 (14.0)	0.3(0.8)	90.3 (15.8)	0.3(0.9)
	multi_RTLP	97.3 (6.4)	<b>0.0</b> (0.1)	<b>100.0</b> (0.0)	<b>0.0</b> (0.0)	99.8 (1.1)	<b>0.0</b> (0.1)
30%	multi_DBSCAN	<b>97.8</b> (5.0)	1.4 (2.9)	<b>100.0</b> (0.0)	2.6 (4.1)	<b>100.0</b> (0.0)	2.4 (3.7)
3070	uni_RTLP	55.4 (13.9)	0.1 (0.4)	76.6 (14.2)	0.2(0.4)	91.8 (9.4)	0.1 (0.2)
	uni_DBSCAN	63.8 (11.8)	0.2 (0.4)	79.6 (15.0)	0.7(0.8)	92.7 (8.1)	0.9 (1.0)
	multi_RTLP	89.4 (13.5)	<b>0.0</b> (0.2)	99.0 (10.0)	<b>0.1</b> (0.2)	99.7 (1.3)	<b>0.1</b> (0.2)
60%	multi_DBSCAN	<b>93.2</b> (11.4)	0.5 (1.3)	<b>99.8</b> (1.0)	1.1 (2.7)	<b>99.9</b> (0.7)	1.1 (2.7)
00%	uni RTLP	40.2 (16.4)	0.2 (0.5)	67.2 (18.3)	0.3 (0.4)	89.7 (8.9)	0.2 (0.3)

0.1 (0.4)

72.9 (16.5)

0.6 (0.7)

uni DBSCAN

49.5 (14.5)

		(b) S	cenario 2				
	Methods		ation 1	Contamin	ation 2	Contamin	ation 3
$p_{curve}$		$p_c$	$p_f$	$p_c$	$p_f$	$p_c$	$p_f$
	multi RTLP	<b>100.0</b> (0.0)	<b>0.0</b> (0.0)	97.0 (12.0)	<b>0.0</b> (0.0)	<b>100.0</b> (0.0)	<b>0.0</b> (0.0)
0%	$\operatorname{multi}_{\overline{D}}\operatorname{BSCAN}$	<b>100.0</b> (0.0)	0.7 (1.2)	<b>97.1</b> (11.4)	0.8 (1.3)	<b>100.0</b> (0.0)	0.8 (1.3)
070	uni_RTLP	<b>100.0</b> (0.0)	<b>0.0</b> (0.0)	93.8 (3.6)	<b>0.0</b> (0.0)	91.7 (6.4)	<b>0.0</b> (0.0)
	uni_DBSCAN	<b>100.0</b> (0.0)	0.4 (0.4)	93.3 (3.9)	0.3(0.4)	91.8 (5.9)	0.2(0.3)
	multi RTLP	<b>100.0</b> (0.0)	<b>0.0</b> (0.1)	96.0 (13.4)	<b>0.0</b> (0.1)	<b>99.9</b> (0.7)	<b>0.0</b> (0.1)
30%	$\operatorname{multi}_{\overline{D}}\operatorname{BSCAN}$	<b>100.0</b> (0.0)	0.6 (1.1)	<b>96.1</b> (13.0)	0.6 (0.9)	99.9 (0.7)	0.6 (1.0)
3070	uni_RTLP	<b>100.0</b> (0.0)	0.1 (0.1)	89.5 (6.2)	<b>0.0</b> (0.1)	89.1 (6.2)	0.0 (0.2)
	uni_DBSCAN	<b>100.0</b> (0.0)	0.4(0.5)	89.0 (6.5)	0.2(0.4)	89.2 (5.9)	0.2(0.3)
	multi RTLP	<b>100.0</b> (0.0)	0.8 (1.3)	63.6 (29.1)	0.4 (0.8)	95.2 (8.4)	0.6 (1.1)
60%	$\operatorname{multi} \overline{\operatorname{D}} \operatorname{BSCAN}$	<b>100.0</b> (0.0)	1.4 (2.1)	62.5 (30.6)	0.6 (1.2)	<b>95.4</b> (8.0)	1.0 (1.7)
00%	uni_RTLP	99.9 (0.7)	<b>0.5</b> (0.6)	<b>75.6</b> (10.3)	<b>0.4</b> (0.5)	78.2 (8.6)	<b>0.5</b> (0.6)
	uni_DBSCAN	<b>100.0</b> (0.0)	1.4 (2.1)	75.3 (10.4)	0.7(0.8)	78.9 (7.8)	0.6(0.7)
	Methods	Contamin	ation 4	Contamin	ation 5	Contamin	ation 6
$p_{curve}$		$p_c$	$p_f$	$p_c$	$p_f$	$p_c$	$p_f$
	multi_RTLP	<b>100.0</b> (0.0)	<b>0.0</b> (0.0)	<b>100.0</b> (1.4)	<b>0.0</b> (0.4)	<b>100.0</b> (0.7)	<b>0.0</b> (0.5)
0%	multi_DBSCAN	<b>100.0</b> (0.0)	0.7(1.2)	0.0 (0.0)	0.9 (1.3)	2.0 (14.3)	0.9 (1.3)
070	uni_RTLP	90.2 (9.9)	0.2(0.4)	54.8 (20.5)	0.1(0.3)	87.1 (16.4)	0.1(0.3)
	uni_DBSCAN	98.3 (8.8)	0.2(0.4)	94.7 (4.8)	0.2(0.5)	93.8 (9.2)	0.1 (0.4)
	multi_RTLP	<b>100.0</b> (0.0)	<b>0.0</b> (0.0)	<b>99.0</b> (10.0)	<b>0.0</b> (0.1)	<b>100.0</b> (0.0)	<b>0.0</b> (0.1)
30%	multi_DBSCAN	<b>100.0</b> (0.0)	0.6 (1.3)	0.0 (0.0)	0.7(1.9)	<b>100.0</b> (0.0)	0.6 (1.1)
3070	uni_RTLP	87.8 (9.8)	0.2(0.4)	55.4 (17.2)	0.2(0.5)	88.3 (15.8)	0.2(0.5)
	uni_DBSCAN	83.2 (8.1)	0.3(0.4)	0.0 (0.0)	0.4(0.6)	72.6 (12.1)	0.4 (0.6)
	multi_RTLP	<b>97.7</b> (9.3)	<b>0.9</b> (1.3)	<b>92.0</b> (27.3)	<b>0.8</b> (1.3)	<b>98.6</b> (10.1)	0.8 (1.3)
60%	multi_DBSCAN	96.0 (14.7)	1.5 (1.8)	0.0 (0.0)	1.4 (2.1)	96.7 (16.5)	1.4 (2.0)
1 0070 -	uni RTLP	77.5 (13.8)	<b>0.9</b> (1.3)	54.5 (16.4)	0.7(0.9)	77.9 (15.8)	<b>0.8</b> (0.9)
	uni DBSCAN	74.8 (12.2)	1.1 (2.2)	0.0 (0.0)	1.1 (2.5)	70.9 (12.3)	

(c) Scenario 3

Methods		Contamin	ation 1	Contamination 2		Contamination 3	
$p_{curve}$	e	$p_c$	$p_f$	$p_c$	$p_f$	$p_c$	$p_f$
	multi_RTLP	99.9 (1.0)	<b>0.0</b> (0.1)	86.9 (20.5)	<b>0.0</b> (0.0)	<b>100.0</b> (0.0)	<b>0.0</b> (0.0)
0%	multi DBSCAN	<b>100.0</b> (0.0)	1.0 (1.7)	86.9 (20.5)	0.5 (1.1)	<b>100.0</b> (0.0)	0.9 (1.7)
070	uni_RTLP	97.2 (7.3)	<b>0.0</b> (0.1)	<b>100.0</b> (0.0)	<b>0.0</b> (0.0)	99.8 (1.6)	<b>0.0</b> (0.0)
	uni_DBSCAN	98.7 (4.4)	0.7(0.5)	<b>100.0</b> (0.0)	0.7(0.5)	99.8 (1.6)	0.7(0.5)
	multi_RTLP	99.5 (2.7)	<b>0.0</b> (0.1)	78.6 (25.2)	<b>0.0</b> (0.0)	<b>100.0</b> (0.0)	<b>0.0</b> (0.0)
30%	multi_DBSCAN	<b>100.0</b> (0.0)	0.5 (1.0)	78.6 (25.3)	0.2(0.5)	<b>100.0</b> (0.0)	0.4 (0.8)
3070	uni_RTLP	98.4 (4.8)	<b>0.0</b> (0.1)	<b>99.7</b> (1.4)	<b>0.0</b> (0.0)	98.8 (2.8)	<b>0.0</b> (0.0)
	uni_DBSCAN	99.6 (2.5)	0.8 (1.1)	<b>99.7</b> (1.4)	0.6(0.5)	98.8 (2.9)	0.6 (0.7)
	multi RTLP	99.7 (2.0)	0.3 (0.5)	53.4 (27.7)	<b>0.1</b> (0.4)	<b>99.1</b> (2.6)	0.3 (0.6)
60%	multi_DBSCAN	<b>100.0</b> (0.0)	0.9 (1.2)	53.4 (27.7)	0.2(0.5)	<b>99.1</b> (2.6)	0.9 (1.0)
0070	uni RTLP	99.4 (2.1)	<b>0.2</b> (0.3)	91.9 (6.5)	0.2 (0.2)	93.8 (4.4)	<b>0.2</b> (0.3)
	uni DBSCAN	<b>100.0</b> (0.0)	0.8 (0.7)	<b>92.2</b> (6.5)	0.6 (0.6)	94.2 (4.2)	0.7 (0.7)
		. ,	\ /	\ /	\ /	. ,	\ /
	Methods	Contamin		Contamin	ation 5	Contamin	ation 6
$p_{curve}$		$p_c$		Contamin $p_c$	ation 5 $p_f$	Contamin $p_c$	ation 6 $p_f$
$p_{curve}$			ation 4			<i>p<sub>c</sub></i> <b>100.0</b> (0.0)	
	е	$p_c$	ation 4 $p_f$	$p_c$	$p_f$	$p_c$	$p_f$
$p_{curve}$	e multi_RTLP	p <sub>c</sub> 100.0 (0.0)	ation 4 $p_f$ <b>0.0</b> (0.0)	<i>p<sub>c</sub></i> <b>100.0</b> (0.0)	$p_f$ <b>0.0</b> (0.0)	<i>p<sub>c</sub></i> <b>100.0</b> (0.0)	$p_f$ 0.0 (0.0)
	multi_RTLP multi_DBSCAN	pc           100.0 (0.0)           100.0 (0.0)	ation 4 $p_f$ 0.0 (0.0) 0.9 (1.7)	$p_c$ <b>100.0</b> (0.0) 24.5 (43.4)	$p_f$ 0.0 (0.0) 0.7 (1.3)	$p_c$ <b>100.0</b> (0.0) 38.8 (49.2)	$p_f$ 0.0 (0.0) 0.7 (1.4)
	multi_RTLP multi_DBSCAN uni_RTLP	$\begin{array}{c c} p_c \\ \hline 100.0 \ (0.0) \\ 100.0 \ (0.0) \\ \hline 100.0 \ (0.0) \\ \end{array}$	ation 4 $p_f$ 0.0 (0.0) 0.9 (1.7) 0.0 (0.0)	$ \begin{array}{c} p_c \\ 100.0 \ (0.0) \\ 24.5 \ (43.4) \\ 98.6 \ (6.7) \end{array} $	$p_f$ 0.0 (0.0) 0.7 (1.3) 0.0 (0.0)	$p_c$ 100.0 (0.0) 38.8 (49.2) 98.0 (8.1)	$\begin{array}{ c c c c c }\hline p_f \\ \hline \textbf{0.0} & (0.0) \\ \hline 0.7 & (1.4) \\ \hline 0.0 & (0.1) \\ \hline \end{array}$
0%	multi_RTLP multi_DBSCAN uni_RTLP uni_DBSCAN	$\begin{array}{c c} p_c \\ \hline 100.0 & (0.0) \\ \hline \end{array}$	ation 4 $p_f$ <b>0.0</b> (0.0) $0.9 (1.7)$ <b>0.0</b> (0.0) $0.7 (0.5)$	<i>p<sub>c</sub></i> <b>100.0</b> (0.0) 24.5 (43.4) 98.6 (6.7) 12.9 (20.2)	$\begin{array}{c} p_f \\ \textbf{0.0} \ (0.0) \\ 0.7 \ (1.3) \\ \textbf{0.0} \ (0.0) \\ 0.9 \ (0.8) \\ \end{array}$	p <sub>c</sub> 100.0 (0.0) 38.8 (49.2) 98.0 (8.1) 21.1 (23.3)	$\begin{array}{c c} p_f \\ \hline \textbf{0.0 } (0.0) \\ 0.7 \ (1.4) \\ 0.0 \ (0.1) \\ 0.9 \ (0.8) \\ \end{array}$
	multi_RTLP multi_DBSCAN uni_RTLP uni_DBSCAN multi_RTLP	$\begin{array}{c c} p_c \\ \hline 100.0 & (0.0) \\ \hline \end{array}$	ation 4 $p_f$ 0.0 (0.0) 0.9 (1.7) 0.0 (0.0) 0.7 (0.5) 0.0 (0.1)	$\begin{array}{c} p_c \\ \textbf{100.0} \ (0.0) \\ 24.5 \ (43.4) \\ 98.6 \ (6.7) \\ 12.9 \ (20.2) \\ \textbf{100.0} \ (0.0) \end{array}$	$\begin{array}{c c} p_f \\ \textbf{0.0} \ (0.0) \\ 0.7 \ (1.3) \\ \textbf{0.0} \ (0.0) \\ 0.9 \ (0.8) \\ \hline \textbf{0.0} \ (0.0) \\ \end{array}$	$\begin{array}{c} p_c \\ \hline \textbf{100.0} \ (0.0) \\ 38.8 \ (49.2) \\ 98.0 \ (8.1) \\ \hline \textbf{21.1} \ (23.3) \\ \hline \textbf{100.0} \ (0.0) \end{array}$	$\begin{array}{c c} p_f \\ \hline \textbf{0.0 } (0.0) \\ 0.7 \ (1.4) \\ 0.0 \ (0.1) \\ 0.9 \ (0.8) \\ \hline \textbf{0.0 } (0.0) \\ \end{array}$
0%	multi_RTLP multi_DBSCAN uni_RTLP uni_DBSCAN multi_RTLP multi_DBSCAN	$\begin{array}{c c} p_c \\ \hline 100.0 & (0.0) \\ 100.0 & (0.0) \\ \hline \end{array}$	ation 4 $p_f$ 0.0 (0.0) 0.9 (1.7) 0.0 (0.0) 0.7 (0.5) 0.0 (0.1) 0.5 (0.8)	$\begin{array}{c} p_c \\ \hline \textbf{100.0} \ (0.0) \\ 24.5 \ (43.4) \\ 98.6 \ (6.7) \\ 12.9 \ (20.2) \\ \hline \textbf{100.0} \ (0.0) \\ 5.0 \ (21.9) \\ \end{array}$	$\begin{array}{c} p_f \\ \textbf{0.0} \ (0.0) \\ 0.7 \ (1.3) \\ \textbf{0.0} \ (0.0) \\ 0.9 \ (0.8) \\ \hline \textbf{0.0} \ (0.0) \\ 0.5 \ (0.9) \\ \end{array}$	$\begin{array}{c} p_c \\ \hline \textbf{100.0} \ (0.0) \\ 38.8 \ (49.2) \\ 98.0 \ (8.1) \\ \hline 21.1 \ (23.3) \\ \hline \textbf{100.0} \ (0.0) \\ \hline \textbf{100.0} \ (0.0) \end{array}$	$\begin{array}{ c c c c }\hline p_f \\ \hline \textbf{0.0} & (0.0) \\ 0.7 & (1.4) \\ 0.0 & (0.1) \\ 0.9 & (0.8) \\ \hline \textbf{0.0} & (0.0) \\ 0.4 & (0.9) \\ \hline \end{array}$
0%	multi_RTLP multi_DBSCAN uni_RTLP uni_DBSCAN  multi_RTLP uni_DBSCAN  multi_RTLP multi_DBSCAN uni_RTLP	$\begin{array}{c c} p_c \\ \hline 100.0 & (0.0) \\ 100.0 & (0.0) \\ \hline \end{array}$	ation 4 $p_f$ 0.0 (0.0) 0.9 (1.7) 0.0 (0.0) 0.7 (0.5) 0.0 (0.1) 0.5 (0.8) 0.0 (0.0)	$p_c$ 100.0 (0.0)  24.5 (43.4)  98.6 (6.7)  12.9 (20.2)  100.0 (0.0)  5.0 (21.9)  93.6 (14.7)	$\begin{array}{c} p_f \\ \textbf{0.0} \ (0.0) \\ 0.7 \ (1.3) \\ \textbf{0.0} \ (0.0) \\ 0.9 \ (0.8) \\ \hline \textbf{0.0} \ (0.0) \\ 0.5 \ (0.9) \\ \textbf{0.0} \ (0.0) \\ \end{array}$	$\begin{array}{c} p_c \\ \hline \textbf{100.0} \ (0.0) \\ 38.8 \ (49.2) \\ 98.0 \ (8.1) \\ 21.1 \ (23.3) \\ \hline \textbf{100.0} \ (0.0) \\ \textbf{100.0} \ (0.0) \\ \hline \textbf{100.0} \ (0.0) \\ \end{array}$	$\begin{array}{c c} p_f \\ \hline \textbf{0.0} \ (0.0) \\ 0.7 \ (1.4) \\ 0.0 \ (0.1) \\ 0.9 \ (0.8) \\ \hline \textbf{0.0} \ (0.0) \\ 0.4 \ (0.9) \\ \hline \textbf{0.0} \ (0.0) \\ \end{array}$
30%	multi_RTLP multi_DBSCAN uni_RTLP uni_DBSCAN  multi_RTLP multi_DBSCAN  uni_RTLP uni_DBSCAN uni_RTLP uni_DBSCAN	$\begin{array}{c c} p_c \\ \hline 100.0 & (0.0) \\ 100.0 & (0.0) \\ \hline \end{array}$	ation 4 $p_f$ 0.0 (0.0) 0.9 (1.7) 0.0 (0.0) 0.7 (0.5) 0.0 (0.1) 0.5 (0.8) 0.0 (0.0) 0.6 (0.6)	$\begin{array}{c} p_c \\ \hline \textbf{100.0} \ (0.0) \\ 24.5 \ (43.4) \\ 98.6 \ (6.7) \\ 12.9 \ (20.2) \\ \hline \textbf{100.0} \ (0.0) \\ 5.0 \ (21.9) \\ 93.6 \ (14.7) \\ 3.7 \ (10.5) \\ \hline \end{array}$	$\begin{array}{c} p_f \\ \textbf{0.0} \ (0.0) \\ 0.7 \ (1.3) \\ \textbf{0.0} \ (0.0) \\ 0.9 \ (0.8) \\ \hline \textbf{0.0} \ (0.0) \\ 0.5 \ (0.9) \\ \textbf{0.0} \ (0.0) \\ 0.6 \ (0.7) \\ \end{array}$	$\begin{array}{c} p_c \\ \hline \textbf{100.0} \ (0.0) \\ 38.8 \ (49.2) \\ 98.0 \ (8.1) \\ \hline 21.1 \ (23.3) \\ \hline \textbf{100.0} \ (0.0) \\ \hline \end{array}$	$\begin{array}{c c} p_f \\ \hline \textbf{0.0} \ (0.0) \\ 0.7 \ (1.4) \\ 0.0 \ (0.1) \\ 0.9 \ (0.8) \\ \hline \textbf{0.0} \ (0.0) \\ 0.4 \ (0.9) \\ \textbf{0.0} \ (0.0) \\ 0.6 \ (0.6) \\ \end{array}$
0%	multi_RTLP multi_DBSCAN uni_RTLP uni_DBSCAN  multi_RTLP multi_DBSCAN uni_RTLP uni_DBSCAN uni_RTLP uni_DBSCAN multi_RTLP	$\begin{array}{c c} p_c \\ \hline 100.0 & (0.0) \\ 100.0 & (0.0) \\ \hline \end{array}$	ation 4 $p_f$ 0.0 (0.0) 0.9 (1.7) 0.0 (0.0) 0.7 (0.5) 0.0 (0.1) 0.5 (0.8) 0.0 (0.0) 0.6 (0.6) 0.3 (0.5)	$\begin{array}{c} p_c \\ \hline \textbf{100.0} \ (0.0) \\ 24.5 \ (43.4) \\ 98.6 \ (6.7) \\ 12.9 \ (20.2) \\ \hline \textbf{100.0} \ (0.0) \\ 5.0 \ (21.9) \\ 93.6 \ (14.7) \\ 3.7 \ (10.5) \\ \hline \textbf{100.0} \ (0.0) \\ \end{array}$	$\begin{array}{c} p_f \\ \textbf{0.0} \ (0.0) \\ 0.7 \ (1.3) \\ \textbf{0.0} \ (0.0) \\ 0.9 \ (0.8) \\ \textbf{0.0} \ (0.0) \\ 0.5 \ (0.9) \\ \textbf{0.0} \ (0.0) \\ 0.6 \ (0.7) \\ \hline 0.3 \ (0.5) \\ \end{array}$	$\begin{array}{c} p_c \\ \hline \textbf{100.0} \ (0.0) \\ 38.8 \ (49.2) \\ 98.0 \ (8.1) \\ \hline \textbf{21.1} \ (23.3) \\ \hline \textbf{100.0} \ (0.0) \\ \hline \end{array}$	$\begin{array}{c c} p_f \\ \hline \textbf{0.0} \ (0.0) \\ 0.7 \ (1.4) \\ 0.0 \ (0.1) \\ 0.9 \ (0.8) \\ \hline \textbf{0.0} \ (0.0) \\ 0.4 \ (0.9) \\ \hline \textbf{0.0} \ (0.0) \\ 0.6 \ (0.6) \\ \hline \hline \textbf{0.3} \ (0.5) \\ \end{array}$

(d) Scenario 4

Methods		Contamin	ation 1	Contamination 2		Contamination 3	
$p_{curve}$	e	$p_c$	$p_f$	$p_c$	$p_f$	$p_c$	$p_f$
	multi_RTLP	<b>100.0</b> (0.0)	<b>0.0</b> (0.0)	92.4 (17.1)	<b>0.0</b> (0.0)	<b>100.0</b> (0.0)	<b>0.0</b> (0.0)
0%	$\overline{\mathrm{multi}}$ $\overline{\mathrm{D}}\mathrm{BSCAN}$	<b>100.0</b> (0.0)	0.8 (1.1)	92.4 (17.1)	0.6 (1.0)	<b>100.0</b> (0.0)	0.8 (1.1)
070	uni_RTLP	<b>100.0</b> (0.0)	0.0 (0.1)	<b>99.9</b> (0.4)	0.0 (0.1)	<b>100.0</b> (0.0)	0.0 (0.1)
	uni_DBSCAN	<b>100.0</b> (0.0)	0.5(0.4)	<b>99.9</b> (0.4)	0.5(0.4)	<b>100.0</b> (0.0)	0.5 (0.4)
	multi_RTLP	<b>100.0</b> (0.0)	<b>0.0</b> (0.1)	93.8 (15.5)	<b>0.0</b> (0.0)	<b>100.0</b> (0.0)	<b>0.0</b> (0.0)
30%	multi_DBSCAN	<b>100.0</b> (0.0)	0.7 (1.1)	93.8 (15.5)	0.5(0.9)	<b>100.0</b> (0.0)	0.5 (0.7)
3070	uni_RTLP	<b>100.0</b> (0.0)	<b>0.0</b> (0.1)	99.5 (1.2)	0.0 (0.1)	99.4 (1.3)	0.0 (0.1)
	uni_DBSCAN	<b>100.0</b> (0.0)	0.6 (0.6)	<b>99.5</b> (1.1)	0.6 (0.6)	100.0 (0.0) 100.0 (0.0) 100.0 (0.0) 100.0 (0.0) 100.0 (0.0) 99.4 (1.3) 99.4 (1.3) 99.3 (2.0) 99.4 (1.9) 94.4 (3.4) 94.9 (3.2) Contamin $p_c$ 100.0 (0.0) 18.4 (39.1)	0.6 (0.7)
	multi_RTLP	<b>100.0</b> (0.0)	<b>0.0</b> (0.1)	89.9 (14.4)	<b>0.0</b> (0.1)	99.3 (2.0)	<b>0.0</b> (0.1)
60%	multi_DBSCAN	<b>100.0</b> (0.0)	0.7 (1.1)	89.9 (14.5)	0.5 (1.1)	<b>99.4</b> (1.9)	0.8 (1.1)
00%	uni_RTLP	99.8 (1.6)	0.1 (0.2)	94.4 (3.2)	0.1 (0.2)	94.4 (3.4)	0.1 (0.2)
	uni_DBSCAN	99.9 (0.7)	1.1 (1.1)	<b>94.5</b> (3.2)	0.9 (0.9)	94.9 (3.2)	1.0 (1.0)
	Methods	Contamin	ation 4	Contamin	ation 5	Contamin	ation 6
$p_{curve}$	e	$p_c$	$p_f$	$p_c$	$p_f$	$p_c$	$p_f$
	multi RTLP	<b>92.5</b> (11.3)	<b>0.0</b> (0.0)	<b>63.3</b> (48.7)	<b>0.0</b> (0.0)	<b>100.0</b> (0.0)	<b>0.0</b> (0.0)
0%	multi_DBSCAN	93.3 (10.6)	0.4 (1.0)	0.0 (0.0)	0.4 (0.7)	18.4 (39.1)	0.8 (1.1)
070	uni_RTLP	65.5 (11.2)	0.1 (0.1)	61.8 (11.8)	0.1 (0.1)	44.0 (16.3)	0.0 (0.1)
	uni_DBSCAN	67.9 (9.0)	0.4 (0.4)	4.1 (13.0)	0.5(0.5)	7.8 (14.4)	0.2 (0.2)
	multi RTLP	91.3 (11.5)	<b>0.0</b> (0.0)	30.0 (46.1)	<b>0.0</b> (0.1)	<b>99.9</b> (0.9)	<b>0.0</b> (0.1)
30%	$\overline{\mathrm{multi}}$ $\overline{\mathrm{D}}\mathrm{BSCAN}$	92.9 (8.6)	0.2 (0.5)	0.0 (0.0)	0.2 (0.6)	<b>99.9</b> (0.9)	0.6 (1.0)
3070	uni_RTLP	59.1 (12.4)	0.1 (0.2)	<b>56.3</b> (17.4)	0.1 (0.2)	62.6 (12.4)	0.1 (0.1)
	uni_DBSCAN	61.4 (9.6)	0.4 (0.6)	3.0 (9.6)	0.7 (0.7)	64.8 (12.8)	0.4 (0.4)
	multi_RTLP	<b>82.3</b> (14.5)	<b>0.0</b> (0.2)	0.0 (0.0)	<b>0.1</b> (0.3)	97.3 (6.8)	<b>0.0</b> (0.1)
60%	multi_DBSCAN	82.3 (16.1)	0.2(0.5)	0.0 (0.0)	0.3 (0.8)	<b>97.1</b> (7.2)	0.7 (1.2)
00%	uni_RTLP	31.6 (13.2)	0.2 (0.3)	<b>22.3</b> (16.1)	0.3 (0.3)	54.3 (11.3)	0.2 (0.2)
	uni_DBSCAN	37.4 (11.3)	0.6 (0.7)	0.3 (3.3)	1.3 (1.5)	53.7 (9.4)	0.8 (1.3)

(e) Scenario 5

	Methods Contamination 1 Contamination 2 Contamination 3							
					1			
$p_{curve}$	~	$p_c$	$p_f$	$p_c$	$p_f$	$p_c$	$p_f$	
0%	multi_RTLP	97.8 (5.0)	0.2(0.5)	<b>100.0</b> (0.0)	<b>0.0</b> (0.0)	98.9 (2.5)	<b>0.2</b> (0.4)	
	multi_DBSCAN	<b>100.0</b> (0.0)	2.2(4.2)	<b>100.0</b> (0.0)	1.3 (3.6)	<b>100.0</b> (0.0)	2.2(4.2)	
070	uni_RTLP	99.9 (1.6)	$0.2\ (0.4)$	99.3 (3.1)	0.2(0.3)	<b>100.0</b> (0.0)	<b>0.2</b> (0.4)	
	uni_DBSCAN	<b>100.0</b> (0.0)	0.4 (0.6)	99.3 (3.1)	0.4(0.5)	<b>100.0</b> (0.0)	0.4 (0.6)	
	multi_RTLP	96.4 (6.7)	<b>0.5</b> (0.8)	<b>99.9</b> (0.9)	<b>0.1</b> (0.4)	98.7 (2.7)	<b>0.4</b> (1.4)	
30%	multi_DBSCAN	<b>100.0</b> (0.0)	1.6 (3.9)	<b>99.9</b> (0.9)	0.6 (1.0)	<b>100.0</b> (0.0)	1.5 (4.0)	
30%	uni_RTLP	97.8 (4.8)	0.8(2.0)	95.8 (5.3)	0.5 (1.4)	98.0 (2.4)	0.5(1.4)	
	uni_DBSCAN	99.6 (1.2)	1.2(2.2)	96.1 (5.3)	0.7 (1.3)	98.2 (2.4)	0.6 (1.2)	
	multi_RTLP	99.8 (2.0)	32.7(4.5)	<b>100.0</b> (0.0)	33.0 (3.6)	<b>99.8</b> (1.1)	33.3 (1.2)	
60%	multi_DBSCAN	<b>100.0</b> (0.0)	33.5 (4.1)	<b>100.0</b> (0.0)	33.8 (3.9)	<b>99.8</b> (1.1)	34.1 (2.2)	
0070	uni_RTLP	98.5 (4.0)	<b>11.5</b> (0.9)	95.4 (3.5)	11.4 (1.0)	96.1 (3.5)	<b>11.3</b> (1.4)	
	uni DBSCAN	<b>100.0</b> (0.2)	11.6 (0.9)	95.5 (3.4)	<b>11.4</b> (0.6)	96.2 (3.5)	11.4 (1.2)	
	_	\ /	( )	( )	( /	( )	( /	
	Methods	Contamir	nation 4	Contami	nation 5	Contamin	nation 6	
$p_{curve}$		$p_c$	nation 4 $p_f$	. ,	nation 5 $p_f$	Contamin $p_c$	nation 6 $p_f$	
$p_{curve}$				Contami				
	multi_RTLP multi_DBSCAN	$p_c$	$p_f$	$p_c$	$p_f$	$p_c$	$p_f$	
p <sub>curve</sub>	multi_RTLP multi_DBSCAN uni_RTLP	99.7 (1.3)	$p_f$ <b>0.0</b> (0.0)	Contamin $p_c$ 89.1 (28.7)	$p_f$ <b>0.0</b> (0.0)	$p_c$ <b>100.0</b> (0.0)	<i>p<sub>f</sub></i> <b>0.0</b> (0.0)	
	multi_RTLP multi_DBSCAN	<i>p<sub>c</sub></i> <b>99.7</b> (1.3) <b>99.7</b> (1.3)	$p_f$ <b>0.0</b> (0.0) 1.2 (3.6)	Contamin $p_c$ 89.1 (28.7) <b>95.6</b> (14.4)	$p_f$ 0.0 (0.0) 0.7 (2.3)	$p_c$ <b>100.0</b> (0.0) <b>100.0</b> (0.0)	$p_f$ 0.0 (0.0) 1.1 (2.4)	
	multi_RTLP multi_DBSCAN uni_RTLP	$p_c$ 99.7 (1.3) 99.7 (1.3) 37.5 (14.5)	$p_f$ 0.0 (0.0) 1.2 (3.6) 0.2 (0.5)	Contamin p <sub>c</sub> 89.1 (28.7)  95.6 (14.4)  38.2 (19.9)	$\begin{array}{c c} p_f \\ \hline \textbf{0.0} \ (0.0) \\ 0.7 \ (2.3) \\ 0.3 \ (0.4) \\ \end{array}$	$p_c$ 100.0 (0.0) 100.0 (0.0) 91.7 (14.1)	$p_f$ 0.0 (0.0) 1.1 (2.4) 0.2 (0.4)	
0%	multi_RTLP multi_DBSCAN uni_RTLP uni_DBSCAN	pc       99.7 (1.3)       99.7 (1.3)       37.5 (14.5)       44.3 (13.3)	$p_f$ 0.0 (0.0) 1.2 (3.6) 0.2 (0.5) 0.1 (0.2)	Contamin $p_c$ 89.1 (28.7) 95.6 (14.4) 38.2 (19.9) 19.3 (14.2)	$\begin{array}{c c} p_f \\ \textbf{0.0} \ (0.0) \\ 0.7 \ (2.3) \\ 0.3 \ (0.4) \\ 0.4 \ (1.0) \end{array}$	$p_c$ 100.0 (0.0) 100.0 (0.0) 91.7 (14.1) 68.7 (8.1)	$\begin{array}{c} p_f \\ \textbf{0.0} \ (0.0) \\ 1.1 \ (2.4) \\ 0.2 \ (0.4) \\ 0.5 \ (0.7) \\ \end{array}$	
	multi_RTLP multi_DBSCAN uni_RTLP uni_DBSCAN multi_RTLP	$\begin{array}{c} p_c \\ \textbf{99.7 (1.3)} \\ \textbf{99.7 (1.3)} \\ \textbf{37.5 (14.5)} \\ 44.3 (13.3) \\ \textbf{97.7 (5.4)} \end{array}$	$p_f$ 0.0 (0.0) 1.2 (3.6) 0.2 (0.5) 0.1 (0.2) 0.3 (0.8)	Contamin $p_c$ 89.1 (28.7)  95.6 (14.4)  38.2 (19.9)  19.3 (14.2)  21.0 (34.7)	$\begin{array}{c c} p_f \\ \textbf{0.0} \ (0.0) \\ 0.7 \ (2.3) \\ 0.3 \ (0.4) \\ 0.4 \ (1.0) \\ \hline \textbf{0.4} \ (0.7) \\ \end{array}$	$\begin{array}{c} p_c \\ \textbf{100.0} \ (0.0) \\ \textbf{100.0} \ (0.0) \\ \textbf{91.7} \ (14.1) \\ 68.7 \ (8.1) \\ \textbf{100.0} \ (0.0) \end{array}$	$\begin{array}{c} p_f \\ \textbf{0.0} \ (0.0) \\ 1.1 \ (2.4) \\ 0.2 \ (0.4) \\ 0.5 \ (0.7) \\ \hline \textbf{0.2} \ (0.5) \\ \end{array}$	
0%	multi_RTLP multi_DBSCAN uni_RTLP uni_DBSCAN multi_RTLP multi_DBSCAN	pc           99.7 (1.3)           99.7 (1.3)           37.5 (14.5)           44.3 (13.3)           97.7 (5.4)           97.9 (4.7)	$\begin{array}{c} p_f \\ \textbf{0.0} \ (0.0) \\ 1.2 \ (3.6) \\ 0.2 \ (0.5) \\ 0.1 \ (0.2) \\ \textbf{0.3} \ (0.8) \\ 1.0 \ (1.5) \end{array}$	Contamin $p_c$ 89.1 (28.7)  95.6 (14.4)  38.2 (19.9)  19.3 (14.2)  21.0 (34.7)  29.1 (35.4)	$\begin{array}{c c} p_f \\ \hline \textbf{0.0} \ (0.0) \\ 0.7 \ (2.3) \\ 0.3 \ (0.4) \\ 0.4 \ (1.0) \\ \hline \textbf{0.4} \ (0.7) \\ 1.1 \ (1.8) \\ \end{array}$	$\begin{array}{c} p_c \\ \textbf{100.0} \ (0.0) \\ \textbf{100.0} \ (0.0) \\ \textbf{91.7} \ (14.1) \\ 68.7 \ (8.1) \\ \textbf{100.0} \ (0.0) \\ \textbf{100.0} \ (0.0) \end{array}$	$\begin{array}{c} p_f \\ \textbf{0.0} \ (0.0) \\ 1.1 \ (2.4) \\ 0.2 \ (0.4) \\ 0.5 \ (0.7) \\ \hline \textbf{0.2} \ (0.5) \\ 0.9 \ (2.3) \\ \end{array}$	
0%	multi_RTLP multi_DBSCAN uni_RTLP uni_DBSCAN multi_RTLP multi_DBSCAN multi_RTLP multi_DBSCAN uni_RTLP	pc           99.7 (1.3)           99.7 (1.3)           37.5 (14.5)           44.3 (13.3)           97.7 (5.4)           97.9 (4.7)           36.0 (11.4)	$\begin{array}{c} p_f \\ \textbf{0.0} \ (0.0) \\ 1.2 \ (3.6) \\ 0.2 \ (0.5) \\ 0.1 \ (0.2) \\ \textbf{0.3} \ (0.8) \\ 1.0 \ (1.5) \\ 4.1 \ (4.9) \end{array}$	Contamin $p_c$ 89.1 (28.7)  95.6 (14.4)  38.2 (19.9)  19.3 (14.2)  21.0 (34.7)  29.1 (35.4)  31.4 (14.7)	$\begin{array}{c c} p_f \\ \hline \textbf{0.0} \ (0.0) \\ 0.7 \ (2.3) \\ 0.3 \ (0.4) \\ 0.4 \ (1.0) \\ \hline \textbf{0.4} \ (0.7) \\ 1.1 \ (1.8) \\ 2.2 \ (3.7) \\ \hline \end{array}$	$p_c$ 100.0 (0.0) 100.0 (0.0) 91.7 (14.1) 68.7 (8.1) 100.0 (0.0) 100.0 (0.0) 66.8 (2.3)	$\begin{array}{c} p_f \\ \hline \textbf{0.0} \ (0.0) \\ 1.1 \ (2.4) \\ 0.2 \ (0.4) \\ 0.5 \ (0.7) \\ \hline \textbf{0.2} \ (0.5) \\ 0.9 \ (2.3) \\ 0.6 \ (0.9) \\ \end{array}$	
30%	multi_RTLP multi_DBSCAN uni_RTLP uni_DBSCAN  multi_RTLP multi_DBSCAN  multi_RTLP multi_DBSCAN  uni_RTLP uni_DBSCAN  multi_RTLP uni_DBSCAN  multi_RTLP multi_DBSCAN	$p_c$ 99.7 (1.3)  99.7 (1.3)  37.5 (14.5)  44.3 (13.3)  97.7 (5.4)  97.9 (4.7)  36.0 (11.4)  39.2 (10.7)	$\begin{array}{c} p_f \\ \hline \textbf{0.0} \ (0.0) \\ 1.2 \ (3.6) \\ 0.2 \ (0.5) \\ 0.1 \ (0.2) \\ \hline \textbf{0.3} \ (0.8) \\ 1.0 \ (1.5) \\ 4.1 \ (4.9) \\ 4.8 \ (4.8) \\ \hline 33.3 \ (1.2) \\ 33.9 \ (2.2) \\ \end{array}$	Contamin $p_c$ 89.1 (28.7)  95.6 (14.4)  38.2 (19.9)  19.3 (14.2)  21.0 (34.7)  29.1 (35.4)  31.4 (14.7)  21.3 (12.2)  19.2 (31.3)  40.4 (36.7)	$\begin{array}{c c} p_f \\ \hline \textbf{0.0} \ (0.0) \\ 0.7 \ (2.3) \\ 0.3 \ (0.4) \\ 0.4 \ (1.0) \\ \hline \textbf{0.4} \ (0.7) \\ 1.1 \ (1.8) \\ 2.2 \ (3.7) \\ 3.0 \ (3.9) \\ \end{array}$	$\begin{array}{c} p_c \\ \textbf{100.0} \ (0.0) \\ \textbf{100.0} \ (0.0) \\ \textbf{91.7} \ (14.1) \\ 68.7 \ (8.1) \\ \textbf{100.0} \ (0.0) \\ \textbf{100.0} \ (0.0) \\ 66.8 \ (2.3) \\ 66.7 \ (0.0) \\ \end{array}$	$\begin{array}{c} p_f \\ \textbf{0.0} \ (0.0) \\ 1.1 \ (2.4) \\ 0.2 \ (0.4) \\ 0.5 \ (0.7) \\ \hline \textbf{0.2} \ (0.5) \\ 0.9 \ (2.3) \\ 0.6 \ (0.9) \\ 1.3 \ (1.7) \\ \end{array}$	
0%	multi_RTLP multi_DBSCAN uni_RTLP uni_DBSCAN  multi_RTLP multi_DBSCAN  uni_RTLP uni_DBSCAN uni_RTLP uni_DBSCAN multi_RTLP	$\begin{array}{c} p_c \\ \textbf{99.7} \ (1.3) \\ \textbf{99.7} \ (1.3) \\ 37.5 \ (14.5) \\ 44.3 \ (13.3) \\ 97.7 \ (5.4) \\ \textbf{97.9} \ (4.7) \\ 36.0 \ (11.4) \\ 39.2 \ (10.7) \\ \hline 96.3 \ (9.0) \\ \end{array}$	$\begin{array}{c} p_f \\ \textbf{0.0} \ (0.0) \\ 1.2 \ (3.6) \\ 0.2 \ (0.5) \\ 0.1 \ (0.2) \\ \textbf{0.3} \ (0.8) \\ 1.0 \ (1.5) \\ 4.1 \ (4.9) \\ 4.8 \ (4.8) \\ \hline 33.3 \ (1.2) \\ \end{array}$	Contamin $p_c$ 89.1 (28.7)  95.6 (14.4)  38.2 (19.9)  19.3 (14.2)  21.0 (34.7)  29.1 (35.4)  31.4 (14.7)  21.3 (12.2)  19.2 (31.3)	$\begin{array}{c c} p_f \\ \hline \textbf{0.0} \ (0.0) \\ 0.7 \ (2.3) \\ 0.3 \ (0.4) \\ 0.4 \ (1.0) \\ \hline \textbf{0.4} \ (0.7) \\ 1.1 \ (1.8) \\ 2.2 \ (3.7) \\ 3.0 \ (3.9) \\ \hline 32.3 \ (5.4) \\ \end{array}$	$\begin{array}{c} p_c \\ \textbf{100.0} \ (0.0) \\ \textbf{100.0} \ (0.0) \\ \textbf{91.7} \ (14.1) \\ 68.7 \ (8.1) \\ \textbf{100.0} \ (0.0) \\ \textbf{100.0} \ (0.0) \\ 66.8 \ (2.3) \\ 66.7 \ (0.0) \\ \textbf{100.0} \ (0.0) \\ \end{array}$	$\begin{array}{c} p_f \\ \textbf{0.0} \ (0.0) \\ 1.1 \ (2.4) \\ 0.2 \ (0.4) \\ 0.5 \ (0.7) \\ \hline \textbf{0.2} \ (0.5) \\ 0.9 \ (2.3) \\ 0.6 \ (0.9) \\ 1.3 \ (1.7) \\ \hline 32.6 \ (4.8) \\ \end{array}$	

(f) Scenario 6

Methods		Contami	nation 1	Contami	nation 2	Contamination 3	
$p_{curve}$	e	$p_c$	$p_f$	$p_c$	$p_f$	$p_c$	$p_f$
	multi RTLP	98.8 (3.8)	0.1 (0.2)	<b>100.0</b> (0.0)	<b>0.0</b> (0.0)	<b>100.0</b> (0.0)	<b>0.0</b> (0.0)
0%	$multi\_\overline{D}BSCAN$	<b>100.0</b> (0.0)	1.3 (1.6)	<b>100.0</b> (0.0)	1.1 (1.6)	<b>100.0</b> (0.0)	1.1 (1.6)
070	uni_RTLP	<b>100.0</b> (0.0)	<b>0.0</b> (0.0)	<b>100.0</b> (0.0)	<b>0.0</b> (0.0)	<b>100.0</b> (0.0)	<b>0.0</b> (0.0)
	uni_DBSCAN	<b>100.0</b> (0.0)	1.0 (0.9)	<b>100.0</b> (0.0)	1.0 (0.9)	<b>100.0</b> (0.0)	1.0 (0.9)
	multi_RTLP	94.5 (9.0)	0.5 (0.7)	61.8 (21.0)	<b>0.2</b> (0.5)	<b>99.1</b> (2.5)	0.4 (1.2)
30%	multi_DBSCAN	<b>100.0</b> (0.0)	<b>0.2</b> (0.7)	57.7 (21.2)	<b>0.2</b> (0.5)	99.0 (2.7)	0.5 (1.6)
3070	uni_RTLP	99.8 (1.7)	0.9 (0.7)	80.7 (8.9)	0.4 (0.5)	85.3 (8.1)	<b>0.4</b> (0.4)
	uni_DBSCAN	<b>100.0</b> (0.0)	1.5 (0.9)	<b>81.3</b> (8.6)	0.7 (0.6)	86.6 (7.2)	0.7(0.6)
	multi_RTLP	91.7 (9.0)	<b>2.1</b> (4.8)	49.7 (21.3)	<b>1.9</b> (5.5)	95.7 (5.7)	2.5 (6.4)
60%	multi_DBSCAN	<b>100.0</b> (0.0)	3.0 (6.6)	51.5 (22.5)	3.6 (10.4)	<b>96.9</b> (4.4)	4.4 (8.8)
0076	uni_RTLP	75.7 (8.3)	3.1 (3.2)	55.8 (10.2)	2.6 (3.4)	67.8 (11.1)	<b>2.4</b> (3.4)
	uni_DBSCAN	99.9 (0.4)	4.8 (4.7)	<b>59.8</b> (9.9)	4.2 (5.3)	74.7 (9.4)	4.1 (5.0)
	Methods	Contamination 4		Contamination 5		Contamination 6	
$p_{curve}$	e	$p_c$	$p_f$	$p_c$	$p_f$	$p_c$	$p_f$
	multi RTLP	<b>99.9</b> (1.0)	<b>0.0</b> (0.0)	<b>100.0</b> (0.0)	<b>0.0</b> (0.0)	<b>100.0</b> (0.0)	<b>0.0</b> (0.0)
0%	$multi\_\overline{D}BSCAN$	<b>99.9</b> (1.0)	1.1 (1.6)	59.2 (49.7)	1.0 (1.4)	75.5 (43.4)	1.1 (1.4)
070	uni_RTLP	95.7 (4.1)	0.0 (0.0)	<b>100.0</b> (0.0)	<b>0.0</b> (0.0)	<b>100.0</b> (0.0)	<b>0.0</b> (0.0)
	uni_DBSCAN	97.4 (2.5)	0.9 (0.9)	34.0 (17.3)	1.0 (0.8)	50.3 (21.6)	1.0 (0.8)
	multi_RTLP	42.3 (37.4)	1.4 (1.9)	26.7 (34.1)	3.8 (8.3)	91.1 (16.8)	<b>0.5</b> (0.7)
30%	multi_DBSCAN	<b>49.6</b> (30.4)	1.9 (3.3)	0.0 (0.0)	1.3 (2.4)	<b>91.1</b> (13.4)	0.7(1.5)
3070	uni_RTLP	37.6 (9.5)	<b>0.8</b> (0.6)	<b>34.1</b> (14.9)	<b>1.3</b> (1.0)	80.0 (7.0)	0.7(0.5)
	uni_DBSCAN	41.8 (6.8)	1.9 (1.2)	31.3 (8.0)	1.6 (1.0)	37.1 (6.3)	1.2 (0.9)
	multi_RTLP	16.6 (22.7)	14.2 (9.3)	0.0 (0.0)	<b>3.4</b> (5.9)	<b>100.0</b> (0.0)	<b>1.9</b> (2.4)
60%	$multi\_\overline{D}BSCAN$	18.7 (21.5)	16.7 (20.0)	0.0 (0.0)	17.3 (20.4)	50.4 (20.9)	4.3 (12.5)
0070	uni_RTLP	<b>33.1</b> (6.5)	14.9 (3.5)	12.9 (9.4)	15.1 (3.7)	51.1 (4.6)	9.0 (1.9)
	uni DBSCAN	32.5 (4.8)	9.0 (5.5)	<b>33.0</b> (3.3)	11.6 (12.4)	34.6 (5.9)	9.7 (8.2)