# Diving into Deep Learning

Deep Learning School

Radoslav Neychev

### Outline

- 1. Previous lecture recap: backpropagation, activations, intuition.
- 2. Optimizers.
- 3. Data normalization.
- 4. Regularization.
- 5. PyTorch practice.
- 6. Q & A.

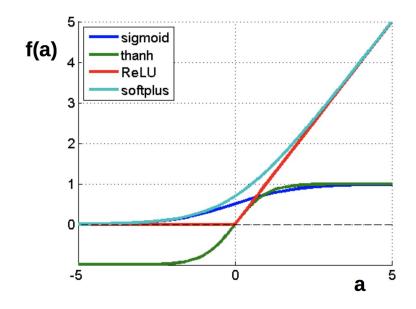
### Once more: nonlinearities

$$f(a) = \frac{1}{1 + e^a}$$

$$f(a) = \tanh(a)$$

$$f(a) = \max(0, a)$$

$$f(a) = \log(1 + e^a)$$

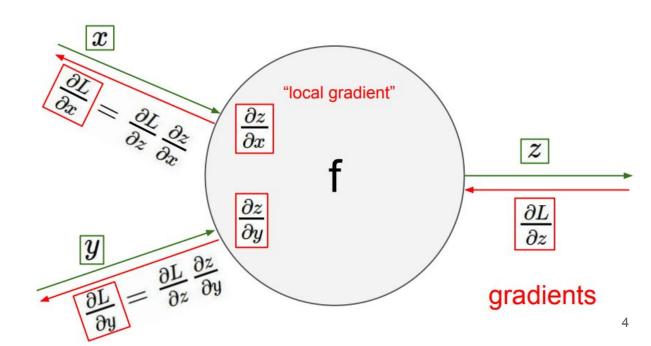


# Backpropagation and chain rule

Chain rule is just simple math:

$$\frac{\partial L}{\partial x} = \frac{\partial L}{\partial z} \frac{\partial z}{\partial x}$$

Backprop is just way to use it in NN training.



source: <a href="http://cs231n.github.io">http://cs231n.github.io</a>

# Different layers

#### Layers

- a. Dense layer (done)
- b. Convolutional layer (next lecture)
- c. Pooling layer (next lecture)
- d. Dropout layer (today)
- e. Batchnorm layer (batch normalization) (today)
- f. Embeddings (aka word2vec, GloVe) (last lecture)
- g. Recurrent layers (last lecture)

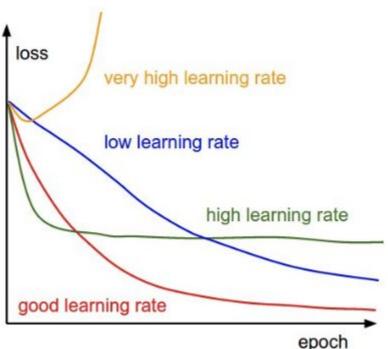
# Different layers

#### Layers

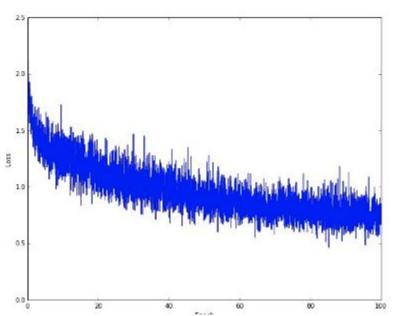
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# **Optimizers**

Stochastic gradient descent is used to optimize NN parameters.



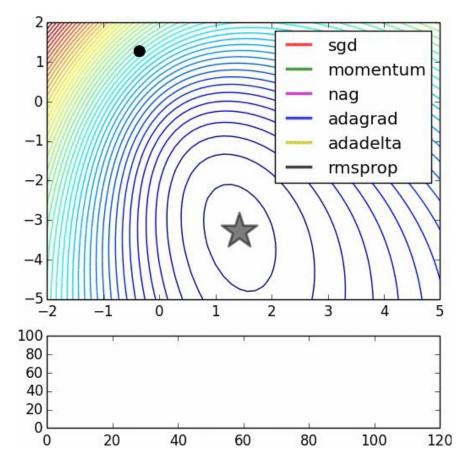
 $x_{t+1} = x_t - \text{learning rate} \cdot dx$ 



# **Optimizers**

#### There are much more optimizers:

- Momentum
- Adagrad
- Adadelta
- RMSprop
- Adam
- ...
- even other NNs

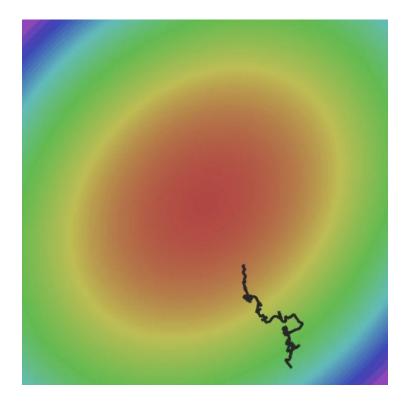


# **Optimization: SGD**

$$L(W) = \frac{1}{N} \sum_{i=1}^{N} L_i(x_i, y_i, W)$$

$$\nabla_W L(W) = \frac{1}{N} \sum_{i=1}^{N} \nabla_W L_i(x_i, y_i, W)$$

Averaging over minibatches ---> noisy gradient



### First idea: momentum

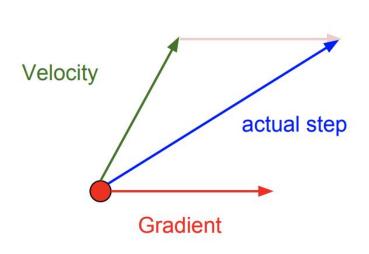
Simple SGD

$$x_{t+1} = x_t - \alpha \nabla f(x_t)$$

SGD with momentum

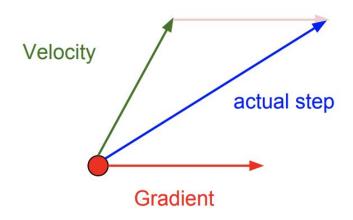
$$v_{t+1} = \rho v_t + \nabla f(x_t)$$
$$x_{t+1} = x_t - \alpha v_{t+1}$$

#### Momentum update:



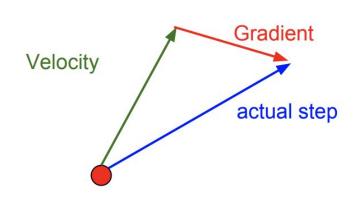
#### Nesterov momentum

#### Momentum update:



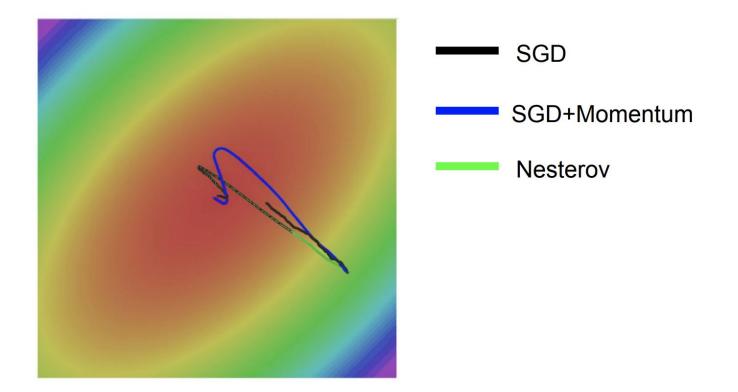
$$v_{t+1} = \rho v_t + \nabla f(x_t)$$
$$x_{t+1} = x_t - \alpha v_{t+1}$$

#### **Nesterov Momentum**



$$v_{t+1} = \rho v_t - \alpha \nabla f(x_t + \rho v_t)$$
$$x_{t+1} = x_t + v_{t+1}$$

# Comparing momentums



### Second idea: different dimensions are different

Adagrad: SGD with cache

$$\operatorname{cache}_{t+1} = \operatorname{cache}_t + (\nabla f(x_t))^2$$
$$x_{t+1} = x_t - \alpha \frac{\nabla f(x_t)}{\operatorname{cache}_{t+1} + \varepsilon}$$

### Second idea: different dimensions are different

Adagrad: SGD with cache

$$\operatorname{cache}_{t+1} = \operatorname{cache}_t + (\nabla f(x_t))^2$$
$$x_{t+1} = x_t - \alpha \frac{\nabla f(x_t)}{\operatorname{cache}_{t+1} + \varepsilon}$$

Problem: gradient fades with time

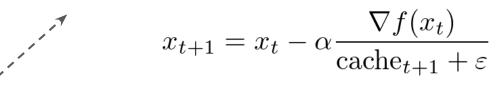
## Second idea: different dimensions are different

Adagrad: SGD with cache

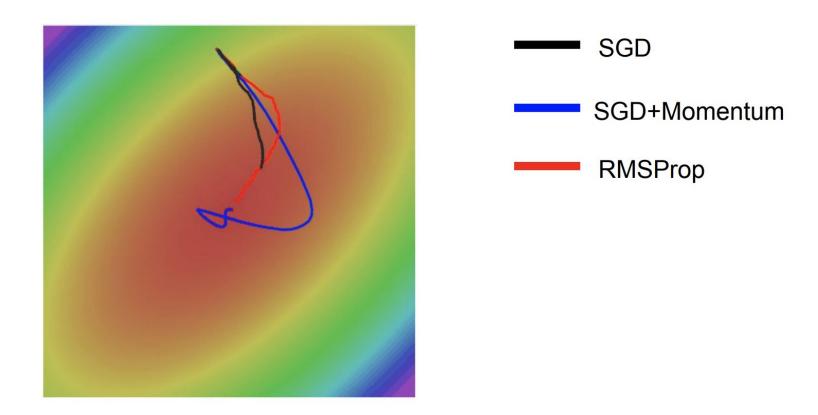
$$cache_{t+1} = cache_t + (\nabla f(x_t))^2$$
$$x_{t+1} = x_t - \alpha \frac{\nabla f(x_t)}{cache_{t+1} + \varepsilon}$$

RMSProp: SGD with cache with exp. Smoothing

$$cache_{t+1} = \beta cache_t + (1 - \beta)(\nabla f(x_t))^2$$



Slide 29 Lecture 6 of Geoff Hinton's Coursera class



# Adam

Let's combine the momentum idea and RMSProp normalization:

$$v_{t+1} = \gamma v_t + (1 - \gamma) \nabla f(x_t)$$

$$\operatorname{cache}_{t+1} = \beta \operatorname{cache}_t + (1 - \beta) (\nabla f(x_t))^2$$

$$x_{t+1} = x_t - \alpha \frac{v_{t+1}}{\operatorname{cache}_{t+1} + \varepsilon}$$

Let's combine the momentum idea and RMSProp normalization:

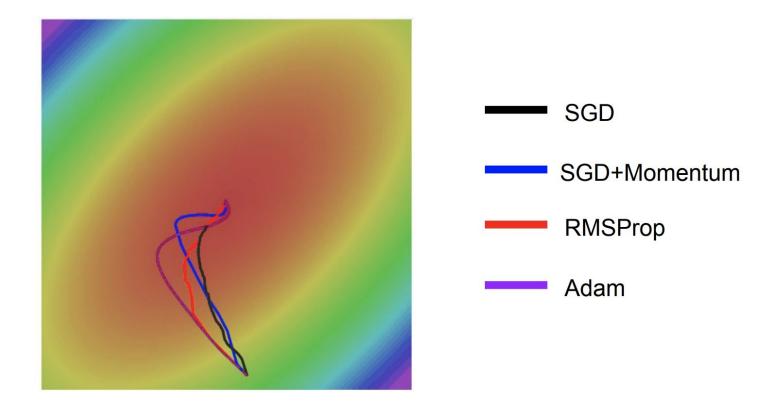
$$v_{t+1} = \gamma v_t + (1 - \gamma) \nabla f(x_t)$$

$$\operatorname{cache}_{t+1} = \beta \operatorname{cache}_t + (1 - \beta) (\nabla f(x_t))^2$$

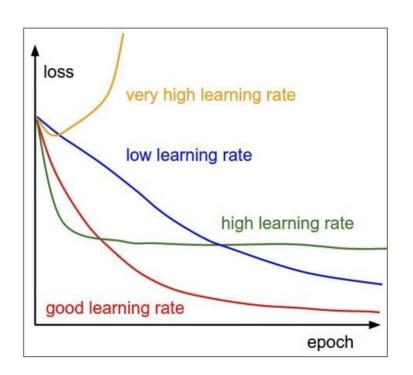
$$x_{t+1} = x_t - \alpha \frac{v_{t+1}}{\operatorname{cache}_{t+1} + \varepsilon}$$

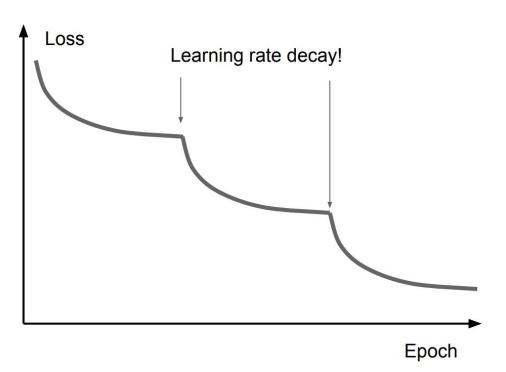
Actually, that's not quite Adam.

# Comparing optimizers



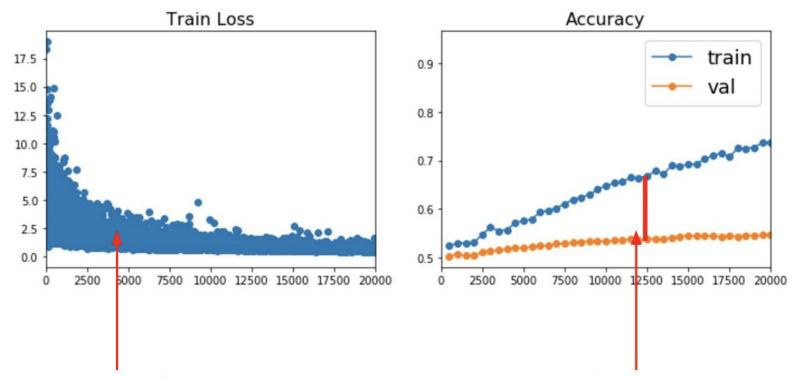
# Once more: learning rate





# Sum up: optimization

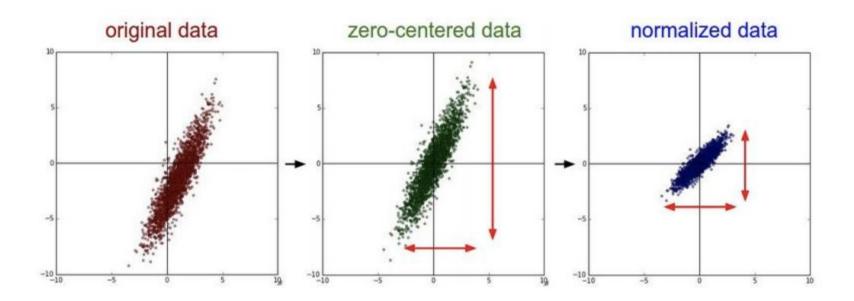
- Adam is great basic choice
- Even for Adam/RMSProp learning rate matters
- Use learning rate decay
- Monitor your model quality



Better optimization algorithms help reduce training loss

But we really care about error on new data - how to reduce the gap?

#### Data normalization



#### Data normalization

**After normalization**: less sensitive to small Before normalization: classification loss changes in weights; easier to optimize very sensitive to changes in weight matrix; hard to optimize

# Weights initialization

Pitfall: all zero initialization.

# Weights initialization

- Pitfall: all zero initialization.
- Small random numbers.

# Weights initialization

- Pitfall: all zero initialization.
- Small random numbers.
- Calibrated random numbers.

$$S = \sum_{i}^{n} w_{i}x_{i}$$

$$Var(s) = Var(\sum_{i}^{n} w_{i}x_{i})$$

$$= \sum_{i}^{n} Var(w_{i}x_{i})$$

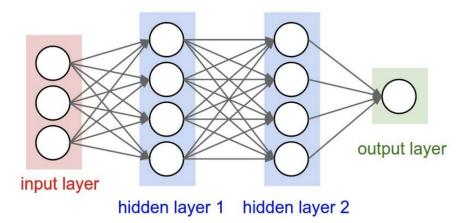
$$= \sum_{i}^{n} [E(w_{i})]^{2} Var(x_{i}) + E[(x_{i})]^{2} Var(w_{i}) + Var(x_{i}) Var(w_{i})$$

$$= \sum_{i}^{n} Var(x_{i}) Var(w_{i})$$

$$= (nVar(w)) Var(x)$$

#### Problem:

- Consider a neuron in any layer beyond first
- At each iteration we tune it's weights towards better loss function
- But we also tune it's inputs. Some of them become larger, some smaller
- Now the neuron needs to be re-tuned for it's new inputs



TL; DR:

It's usually a good idea to normalize linear model inputs

(c) Every machine learning lecturer, ever

 Normalize activation of a hidden layer (zero mean unit variance)

$$h_i = \frac{h_i - \mu_i}{\sqrt{\sigma_i^2}}$$

• Update  $\mu_i$ ,  $\sigma_i^2$  with moving average while training

$$\mu_{i} := \alpha \cdot mean_{batch} + (1 - \alpha) \cdot \mu_{i}$$

$$\sigma_{i}^{2} := \alpha \cdot variance_{batch} + (1 - \alpha) \cdot \sigma_{i}^{2}$$

Original algorithm (2015)

Input: Values of x over a mini-batch:  $\mathcal{B} = \{x_{1...m}\}$ ; Parameters to be learned:  $\gamma$ ,  $\beta$ 

Output:  $\{y_i = BN_{\gamma,\beta}(x_i)\}$ 

$$\mu_{\mathcal{B}} \leftarrow \frac{1}{m} \sum_{i=1}^{m} x_i$$
 // mini-batch mean

$$\sigma_{\mathcal{B}}^2 \leftarrow \frac{1}{m} \sum_{i=1}^m (x_i - \mu_{\mathcal{B}})^2$$
 // mini-batch variance

$$\widehat{x}_i \leftarrow \frac{x_i - \mu_{\mathcal{B}}}{\sqrt{\sigma_{\mathcal{B}}^2 + \epsilon}}$$
 // normalize

$$y_i \leftarrow \gamma \widehat{x}_i + \beta \equiv \mathrm{BN}_{\gamma,\beta}(x_i)$$
 // scale and shift

Original algorithm (2015)

What is this?

**Input:** Values of x over a mini-batch:  $\mathcal{B} = \{x_{1...m}\}$ ; Parameters to be learned:  $\gamma$ ,  $\beta$ Output:  $\{y_i = BN_{\gamma,\beta}(x_i)\}$ // mini-batch mean // mini-batch variance // normalize  $y_i \leftarrow \gamma \widehat{x}_i + \beta \equiv \mathrm{BN}_{\gamma,\beta}(x_i)$ // scale and shift

Input: Values of x over a mini-batch:  $\mathcal{B} = \{x_{1...m}\}$ ; Parameters to be learned:  $\gamma$ ,  $\beta$ 

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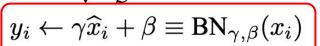
// mini-batch mean

$$\sigma_{\mathcal{B}}^2 \leftarrow \frac{1}{m} \sum_{i=1}^{m} (x_i - \mu_{\mathcal{B}})^2$$

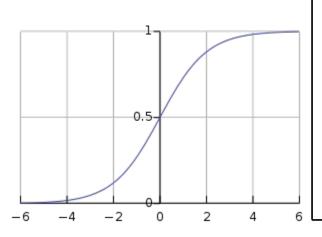
// mini-batch variance

$$\widehat{x}_i \leftarrow \frac{x_i - \mu_{\mathcal{B}}}{\sqrt{\sigma_{\mathcal{B}}^2 + \epsilon}}$$

// normalize



// scale and shift



Input: Values of x over a mini-batch:  $\mathcal{B} = \{x_{1...m}\}$ ; Parameters to be learned:  $\gamma$ ,  $\beta$ 

Output:  $\{y_i = BN_{\gamma,\beta}(x_i)\}$ 

$$\mu_{\mathcal{B}} \leftarrow \frac{1}{m} \sum_{i=1}^{m} x_i$$

// mini-batch mean

$$\sigma_{\mathcal{B}}^2 \leftarrow \frac{1}{m} \sum_{i=1}^{n} (x_i - \mu_{\mathcal{B}})^2$$

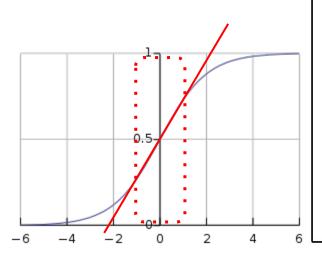
// mini-batch variance

$$\widehat{x}_i \leftarrow rac{x_i - \mu_B}{\sqrt{\sigma_B^2 + \epsilon}}$$

// normalize

$$oxed{y_i \leftarrow \gamma \widehat{x}_i + eta \equiv \mathrm{BN}_{\gamma,eta}(x_i)}$$

// scale and shift



Original algorithm (2015)

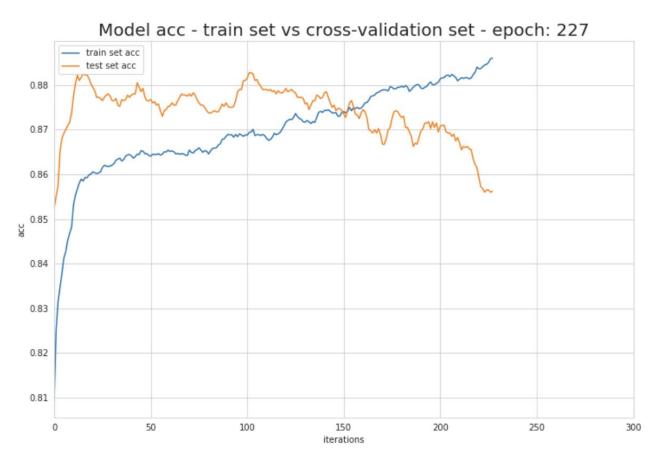
What is this?

This transformation should be able to represent the identity transform.

```
Input: Values of x over a mini-batch: \mathcal{B} = \{x_{1...m}\};
           Parameters to be learned: \gamma, \beta
Output: \{y_i = BN_{\gamma,\beta}(x_i)\}
                                                    // mini-batch mean
                                                // mini-batch variance
                                                              // normalize
    y_i \leftarrow \gamma \widehat{x}_i + \beta \equiv BN_{\gamma,\beta}(x_i)
                                                        // scale and shift
```

	Model	Steps to 72.2%	Max accuracy
	Inception	$31.0 \cdot 10^{6}$	72.2%
	BN-Baseline	$13.3\cdot 10^6$	72.7%
	BN-x5	$2.1\cdot 10^6$	73.0%
accuracy	BN-x30	$2.7\cdot 10^6$	74.8%
0.8	BN-x5-Sigmoid		69.8%
0.6			
	nception BN-Baseline		
0.5	BN-x5 BN-x30 BN-x5-Sigmoid		
	Steps to match Inception		
5M 10M 15M 20M cource: https://arxiv.org/pdf/1502.03167.pdf	<sup>25M</sup> 30M n	umber of training steps	36

## Problem: overfitting



## Regularization

$$L=rac{1}{N}\sum_{i=1}^{N}\sum_{j
eq y_i}\max(0,f(x_i;W)_j-f(x_i;W)_{y_i}+1)+\lambda R(W)$$

Adding some extra term to the loss function.

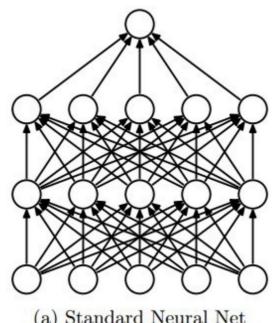
#### Common cases:

- L2 regularization:  $R(W) = \|W\|_2^2$
- L1 regularization:  $R(W) = \|W\|_1$
- Elastic Net (L1 + L2):  $R(W) = \beta ||W||_2^2 + ||W||_1$

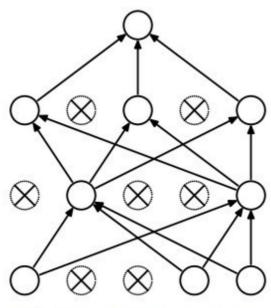
## Regularization: Dropout

Some neurons are "dropped" during training.

Prevents overfitting.



(a) Standard Neural Net

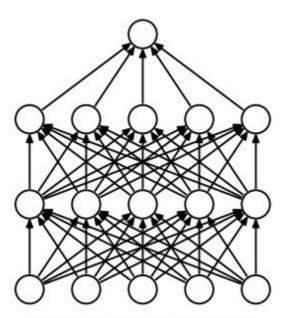


(b) After applying dropout.

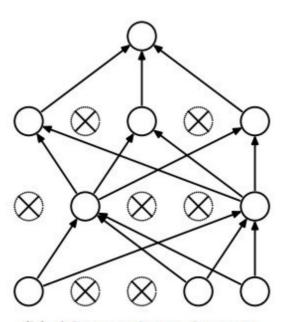
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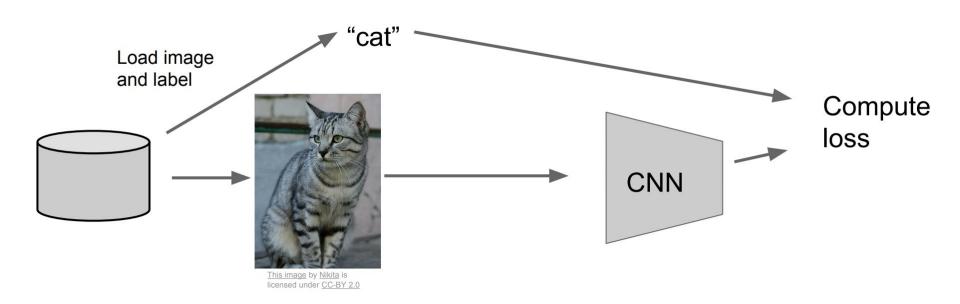
(a) Standard Neural Net



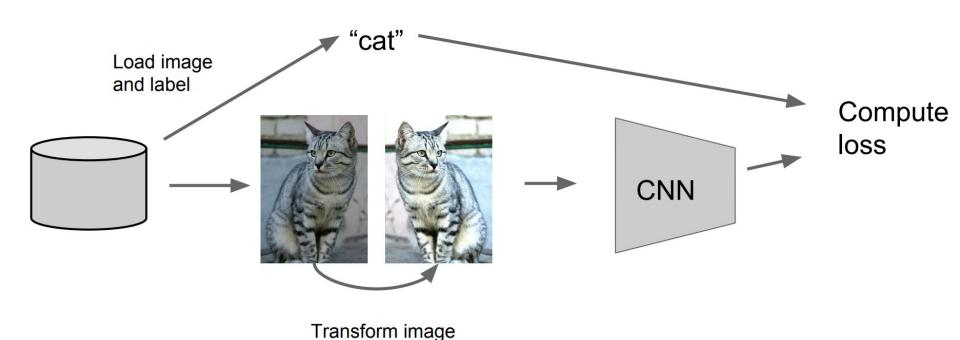
(b) After applying dropout.

Actually, on test case output should be normalized. See sources for more info.

## Regularization: data augmentation



# Regularization: data augmentation



### Sum up: regularization

#### Regularization:

- Add some weight constraints
- Add some random noise during train and marginalize it during test
- Add some prior information in appropriate form

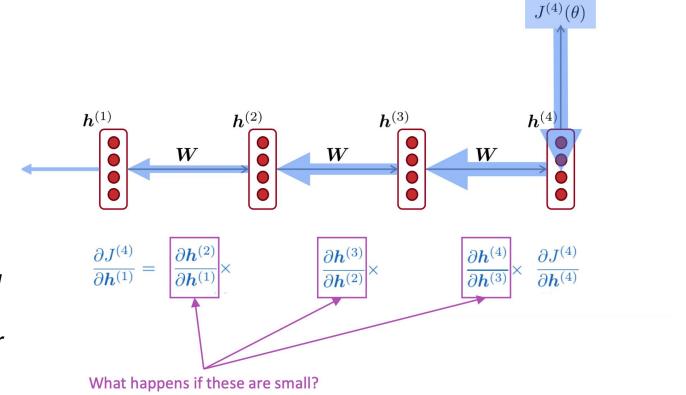
That's all. Feel free to ask any questions.

# Backup

### Vanishing gradient problem

Vanishing gradient problem:

When the derivatives are small, the gradient signal gets smaller and smaller as it backpropagates further



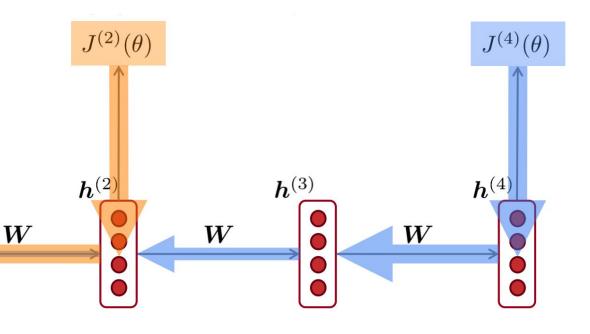
More info: "On the difficulty of training recurrent neural networks", Pascanu et al, 2013 <a href="http://proceedings.mlr.press/v28/pascanu13.pdf">http://proceedings.mlr.press/v28/pascanu13.pdf</a>

Gradient signal from far away is lost because it's much smaller than from close-by.

So model weights updates will be based only on short-term effects.

 $oldsymbol{h}^{(1)}$ 

# Vanishing gradient problem



## Exploding gradient problem

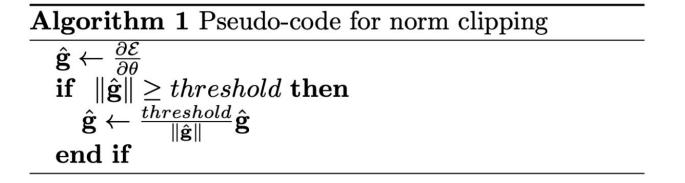
 If the gradient becomes too big, then the SGD update step becomes too big:

$$heta^{new} = heta^{old} - \overset{\text{learning rate}}{\alpha} \overset{\text{pradient}}{\nabla_{\theta} J(\theta)}$$

- This can cause bad updates: we take too large a step and reach a bad parameter configuration (with large loss)
- In the worst case, this will result in Inf or NaN in your network (then you have to restart training from an earlier checkpoint)

## Exploding gradient solution

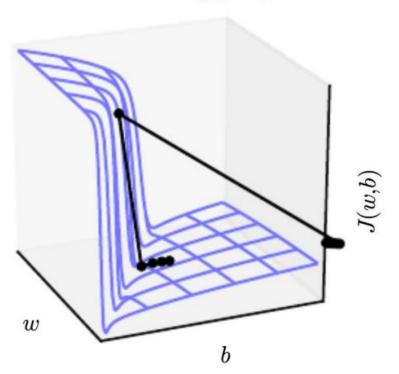
 Gradient clipping: if the norm of the gradient is greater than some threshold, scale it down before applying SGD update



 Intuition: take a step in the same direction, but a smaller step

# Exploding gradient solution

Without clipping



With clipping

