

LAB 1

BISECTION METHOD

OBJECTIVE

To find the real root of $x e^x - 1$

TOOLS

gcc (code::blocks)

ALGORITHM/FLOWCHART:

1. Read x1, x2, e
2. e is the absolute error
3. Compute: f1 = f(x1) and f2 = f(x2)
4. If (f1*f2) > 0, then display initial guesses are wrong and goto (11).
5. $x = (x1 + x2)/2$
6. If (|(x1 - x2)/x| < e), then display x and goto (11).
7. Else, f = f(x)
8. If ((f*f1) > 0), then x1 = x and f1 = f.
9. Else, x2 = x and f2 = f. Bishal Sharma
10. Goto (5).
11. Stop

CODE:

```
#include<stdio.h>
#include<math.h>
float f(float x){
    return(x*exp(x)-1);
}
int main()
{
    float x1,x2,xm=0,flg,eps=0.0001,a,b,c;
    int count=0;
    do{
        printf("Enter Initial guess");
        scanf("%f %f", &x1,&x2);
        if(f(x1)*f(x2)>0)
            printf("\n Invalid Guess.... Type the guess again...");
    }
    while(f(x1)*f(x2)>0);
    printf("\n ITR   x1       x2       xm       F(x1)   F(x2)   F(xm)");
    do{
        flg=xm;
        xm=(x1+x2)/2.00;
        count++;
        a=f(x1);
        b=f(x2);
        c=f(xm);
        printf("\n %d    %f    %f    %f    %f    %f    %f",count,x1,x2,xm,a,b,c);
        if(f(xm)*f(x1)<0)
            x2=xm;
```

```

else
    x1=xm;
}
while(fabs(xm-flg)>eps);
printf("\n Result = %12.4f  count=%d",xm,count);
return 0;
}

```

OBSERATION AND RESULT

```

Enter Initial guess0
1

```

ITR	x1	x2	xm	F(x1)	F(x2)	F(xm)
1	0.000000	1.000000	0.500000	-1.000000	1.718282	-0.175639
2	0.500000	1.000000	0.750000	-0.175639	1.718282	0.587750
3	0.500000	0.750000	0.625000	-0.175639	0.587750	0.167654
4	0.500000	0.625000	0.562500	-0.175639	0.167654	-0.012782
5	0.562500	0.625000	0.593750	-0.012782	0.167654	0.075142
6	0.562500	0.593750	0.578125	-0.012782	0.075142	0.030619
7	0.562500	0.578125	0.570312	-0.012782	0.030619	0.008780
8	0.562500	0.570312	0.566406	-0.012782	0.008780	-0.002035
9	0.566406	0.570312	0.568359	-0.002035	0.008780	0.003364
10	0.566406	0.568359	0.567383	-0.002035	0.003364	0.000662
11	0.566406	0.567383	0.566895	-0.002035	0.000662	-0.00068
12	0.566895	0.567383	0.567139	-0.000687	0.000662	-0.00001
13	0.567139	0.567383	0.567261	-0.000013	0.000662	0.000325
14	0.567139	0.567261	0.567200	-0.000013	0.000325	0.000156

```

Result = 0.5672 count=14
Process returned 0 (0x0) execution time : 6.920 s
Press ENTER to continue.

```

CONCLUSION

hence we can use bisection method to find the real root of $x e^x - 1$

LAB 2

FALSE POSITION METHOD

OBJECTIVE

To find the real root of $x - \cos x$

TOOLS

gcc (code::blocks)

ALGORITHM/FLOWCHART:

- 1 Start
- 2 Read values of x_0 , x_1 and e
- 3 Computer function values $f(x_0)$ and $f(x_1)$
- 4 Check whether the product of $f(x_0)$ and $f(x_1)$ is negative or not.\
If it is positive take another initial guesses.
If it is negative then goto step 5.
- 5 Determine: $x = [x_0 * f(x_1) - x_1 * f(x_0)] / (f(x_1) - f(x_0))$
- 6 Check whether the product of $f(x_1)$ and $f(x)$ is negative or not.
If it is negative, then assign $x_0 = x$;
If it is positive, assign $x_1 = x$;
- 7 Check whether the value of $f(x)$ is greater than 0.00001 or not.
If yes, goto step 5.
If no, goto step 8.
*Here the value 0.00001 is the desired degree of accuracy, and hence the
- 10 stopping criteria.*
- 8 Display the root as x .
- 9 Stop

CODE:

```
#include<stdio.h>
#include<math.h>
float f(float x) {
    return(x-cos(x));
}
int main()
{
    float x0,x1,xm=0,flg,eps=0.0001,a,b,c;
    int count=0;
    do{
        printf("Enter Initial guess");
        scanf("%f %f", &x0,&x1);
        if(f(x0)*f(x1)>0)
            printf("\n Invalid Guess.... Type the guess again...");
    }
    while(f(x0)*f(x1)>0);
    printf("\n ITR   x0       x1       xm       F(x0)       F(x1)       F(xm)");
    do{
        count++;
        flg=xm;
        xm=x0-(f(x0)*(x1-x0))/(f(x1)-f(x0));
```

```

a=f(x0);
b=f(x1);
c=f(xm);
printf("\n %d %12.3f  %f  %f  %f  %f %f",count,x0,x1,xm,a,b,c);
if(f(xm)*f(x0)<0)
    x1=xm;
else
    x0=xm;

}
while(fabs(flg-xm)>eps);
printf("\n Result = %10.3f  count=%d",xm,count);
return 0;
}

```

OBSERATION AND RESULT

```

Enter Initial guess0
1

```

ITR	x0	x1	xm	F(x0)	F(x1)	F(xm)
1	0.000	1.000000	0.685073	-1.000000	0.459698	-0.089299
2	0.685	1.000000	0.736299	-0.089299	0.459698	-0.004660
3	0.736	1.000000	0.738945	-0.004660	0.459698	-0.000234
4	0.739	1.000000	0.739078	-0.000234	0.459698	-0.000012
5	0.739	1.000000	0.739085	-0.000012	0.459698	-0.000001

```

Result = 0.739  count=5
Process returned 0 (0x0)  execution time : 3.979 s
Press ENTER to continue.

```

CONCLUSION

hence we can use false position method to find the real root of $x^3+x^2-3x-3=0$

LAB 3

FIXED POINT METHOD

OBJECTIVE

To find the real root of $\frac{(x^2+2)}{3}$

TOOLS

gcc (code::blocks)

ALGORITHM/FLOWCHART:

- 1 Start
- 2 Read values of x0 and e.
 Here x0 is the initial approximation e is the absolute error or the desired degree of accuracy, also the stopping criteria
- 3 Calculate x1 = g(x0)
- 4 If $|x1 - x0| \leq e$, goto step 6.
- 5 Else, assign x0 = x1 and goto step 3.
- 6 Display x1 as the root.
- 7 Stop

CODE:

```
#include<stdio.h>
#include<math.h>

float f(float x){
    return ((pow(x,2)+2)/3);
}

int main()
{
    float x0,x1=0, flg, eps=0.0001;
    int count=0;
    printf("Enter initial guess: ");
    scanf("%f",&x0);
    do {
        flg=x1;
        x1=f(x0);
        count++;
        printf("\n%d\t%f",count,x1);
        x0=x1;
    }
    while(fabs(flg-x1)>eps);
    printf("\n\n Real root = %0.5f \n and the number of iteration is %d",x1,count);
    return 0;
}
```

OBSERATION AND RESULT

```
Enter initial guess: 0
1      0.666667
2      0.814815
3      0.887974
4      0.929500
5      0.954656
6      0.970456
7      0.980595
8      0.987189
9      0.991514
10     0.994367
11     0.996255
12     0.997508
13     0.998341
14     0.998895
15     0.999264
16     0.999509
17     0.999673
18     0.999782
19     0.999855

Real root = 0.99985
and the number of iteration is 19
Process returned 0 (0x0)   execution time : 2.985 s
Press ENTER to continue.
```

CONCLUSION

hence we can use fixed point method to find the real root of $\frac{(x^2+2)}{3}$

LAB 4

NEWTON-RAPHSON METHOD

OBJECTIVE

To find the real root of $3^x + \sin x - e^x$

TOOLS

gcc (code::blocks)

ALGORITHM/FLOWCHART:

- 1 Start
- 2 Read x, e, n, d
 x is the initial guess e is the absolute error i.e the desired degree of accuracy n is for operating loop d is for checking slope*
- 3 Do for $i = 1$ to n in step of 2
- 4 $f = f(x)$
- 5 $f1 = f'(x)$
- 6 If ($|f1| < d$), then display too small slope and goto 11.
- 7 $x1 = x - f/f1$
- 8 If ($|(x1 - x)/x1| < e$), the display the root as $x1$ and goto 11.
- 9 $x = x1$ and end loop
- 10 Display method does not converge due to oscillation.
- 11 Stop

CODE:

```
#include<stdio.h>
#include<math.h>
float f(float x){
    return(3*x+sin(x)-exp(x));
}
float g(float y){
    return(3+cos(y)-exp(y));
}
int main()
{
    float x0,x1=0,eps=0.0000001,flg;
    count=0;
    printf("      NEWTONS METHOD");
    printf("\n\n\n\n\n\n      Enter guess ");
    scanf("%f",&x0);
    printf("\n Ite   X");
    do{
        flg=x1;
        x1=x0-(f(x0)/g(x0));
        count++;
        printf("\n %d  %f   %f",count,x1,x0);
        x0=x1;
    }
    while(fabs(flg-x1)>eps);
    printf("\n\n\n The root up to 5 decimal place of the given function is%12.5f \n and the
```

```
    number of iteration is %d",x1,count);  
    return 0;  
}
```

OBSERATION AND RESULT

```
NEWTONS METHOD  
  
Enter guess 0  
  
Ite  X  
1  0.333333  0.000000  
2  0.360171  0.333333  
3  0.360422  0.360171  
4  0.360422  0.360422  
  
The root up to 5 decimal place of the given function is 0.36042  
and the number of iteration is 4  
Process returned 0 (0x0)   execution time : 6.461 s  
Press ENTER to continue.  
█
```

CONCLUSION

hence we can use newton-raphson method to find the real root of $3^x + \sin x - e^x$

LAB 5

SECANT METHOD

OBJECTIVE

To find the real root of $x^3 + x^2 + x + 7$

TOOLS

gcc (code::blocks)

ALGORITHM/FLOWCHART:

- 1 Start
- 2 Get values of x0, x1 and e
Here x0 and x1 are the two initial guesses e is the stopping criteria, absolute error or the desired degree of accuracy
- 3 Compute f(x0) and f(x1)
- 4 Compute $x2 = |x0*f(x1) - x1*f(x0)| / |f(x1) - f(x0)|$
- 5 Test for accuracy of x2
If $|x2 - x1|/x2 > e$, assign $x0 = x1$ and $x1 = x2$ goto step 4 Else, goto step 6
- 6 Display the required root as x2.
- 7 Stop

CODE:

```
#include<stdio.h>
#include<math.h>
float f(float x){
    return(3*x+sin(x)-exp(x));
}
float g(float y){
    return(3+cos(y)-exp(y));
}
int main()
{
    float x0,x1=0,eps=0.0000001,flg;
    count=0;
    printf("      NEWTONS METHOD");
    printf("\n\n\n\n\n      Enter guess ");
    scanf("%f",&x0);
    printf("\n Ite   X");
    do{
        flg=x1;
        x1=x0-(f(x0)/g(x0));
        count++;
        printf("\n %d  %f   %f",count,x1,x0);
        x0=x1;
    }
    while(fabs(flg-x1)>eps);
    printf("\n\n The root up to 5 decimal place of the given function is%12.5f \n and the
    number of iteration is %d",x1,count);
    return 0;
}
```

OBSERATION AND RESULT

```
NEWTONS METHOD

Enter guess 0

Ite  X
1  0.333333  0.000000
2  0.360171  0.333333
3  0.360422  0.360171
4  0.360422  0.360422

The root up to 5 dcimal place of the given function is 0.36042
and the number of iteration is 4
Process returned 0 (0x0)   execution time : 6.461 s
Press ENTER to continue.
```

CONCLUSION

hence we can use newton-raphson method to find the real root of $3^x + \sin x - e^x$