

**VIT**Vellore Institute of Technology
(Deemed to be University under section 3 of UGC Act, 1956)

Winter Semester – 2019~2020

Continuous Assessment Test – I

Programme Name & Branch: B.Tech. &
M.TechCourse Code & Name : MAT2001 – Statistics for Engineers
Exam Duration : 90 MinutesSlot : G2+TG2
Maximum Marks : 50**Answer ALL the Questions**Each question carries equal marks ($5 \times 10 = 50$ Marks)

S. No.	Questions	Marks																				
1.	<p>The following data relate to the frequency distribution of Intelligence Quotients (I.Q.'s) of 900 school children. Find the lower and upper quartiles, quartile deviation.</p> <table><tr><td>I.Q:</td><td>54.5-64.5</td><td>64.5-74.5</td><td>74.5-84.5</td><td>84.5-94.5</td><td>94.5-104.5</td></tr><tr><td># children :</td><td>3</td><td>21</td><td>78</td><td>182</td><td>302</td></tr></table> <table><tr><td>104.5-114.5</td><td>114.5-124.5</td><td>124.5-134.5</td><td>134.5-144.5</td></tr><tr><td>207</td><td>81</td><td>21</td><td>5</td></tr></table>	I.Q:	54.5-64.5	64.5-74.5	74.5-84.5	84.5-94.5	94.5-104.5	# children :	3	21	78	182	302	104.5-114.5	114.5-124.5	124.5-134.5	134.5-144.5	207	81	21	5	[10]
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207	81	21	5																			
2.	<p>Calculate the mean, variance and standard deviation for the following frequency distribution, and hence obtain the co-efficient of variation for the following data:</p> <table><tr><td>X:</td><td>20-25</td><td>25-30</td><td>30-35</td><td>35-40</td><td>40-45</td><td>45-50</td><td>50-55</td><td>55-60</td><td>60-65</td></tr><tr><td>f :</td><td>35</td><td>165</td><td>215</td><td>185</td><td>145</td><td>105</td><td>75</td><td>65</td><td>45</td></tr></table>	X:	20-25	25-30	30-35	35-40	40-45	45-50	50-55	55-60	60-65	f :	35	165	215	185	145	105	75	65	45	[10]
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3.	<p>If the random variable X takes the values 1, 2, 3 and 4 such that $2P(X = 1) = 3P(X = 2) = P(X = 3) = 5P(X = 4)$, find the probability distribution function and cumulative distribution function of X.</p>	[10]																				
4.	<p>If the joint density for the random variables (X, Y), where X is the unit temperature change and Y is the proportion of spectrum shift that a certain atomic particle produces, is given by</p> $f(x, y) = \begin{cases} cxy^2, & 0 < x < y < 1; \\ 0, & \text{otherwise,} \end{cases}$ <p>then find (i). the value of c, (ii). $f_{Y/X}(y/x)$, (iii). $f_X(x)$, (iv). $f_Y(y)$, (iv). $E(X)$.</p>	[10]																				
5.	<p>A random variable X has probability mass function $p(x) = P(X = x) = \frac{1}{2^x}$ for $x = 1, 2, 3, \dots$. Find the moment generating function and hence obtain the mean and the variance.</p>	[10]																				
