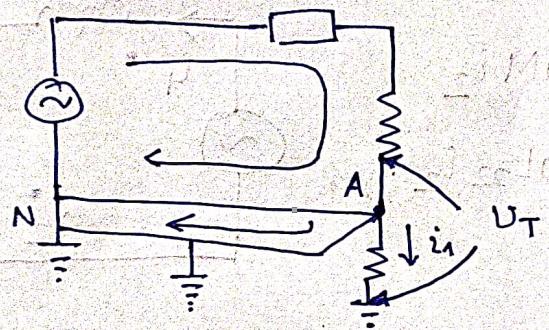


1. A. True.  
 B. False.  
 C. There is voltage drop due to loop inductance as well.  
 D. Region - I.

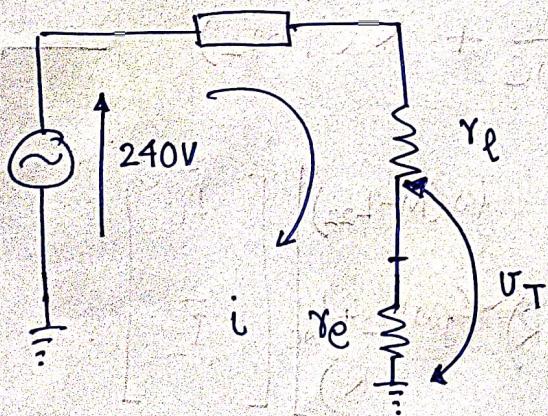
2. Subjective.

3. (a).



$$i_1 = 0. \text{ So, } V_A = V_N. \text{ So, } U_T = V_A - V_N = 0.$$

(b).



$$\begin{aligned} \text{Lamp rating} &= 2 \times 400\text{W} \\ &= 800\text{W}. \end{aligned}$$

So, lamp resistance  
( $r_L$ )

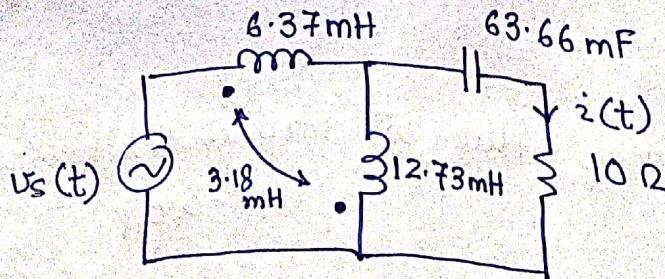
$$= \frac{V^2}{P} = \frac{240^2}{800}$$

$$= 72\Omega.$$

$$\text{Electrode resistance } r_e = 25\Omega.$$

$$\therefore U_T = 240 \times \frac{r_e}{r_e + r_L} = 240 \times \frac{25}{97} \text{ V} = \underline{61.86 \text{ V.}}$$

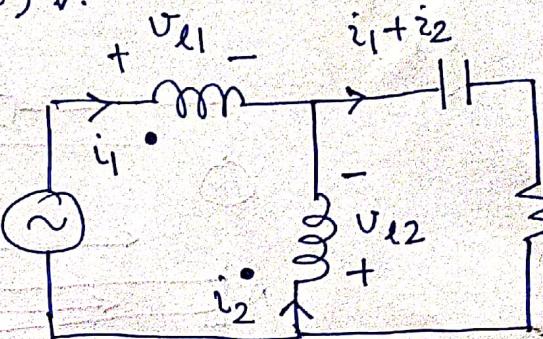
4.



$$v_s(t) = \sqrt{2} \times 100 \sin(2\pi \times 50t) \text{ V.}$$

$$v_{L1} = j\omega L_{11} i_1 + j\omega M i_2$$

$$v_{L2} = j\omega M i_1 + j\omega L_{22} i_2$$



$$\text{Now, } v_s = v_{L1} - v_{L2}$$

$$100 \angle 0^\circ = j\omega [(L_{11} - M)i_1 + (M - L_{22})i_2]. \quad \text{(1.)}$$

$$-v_{L2} = (i_1 + i_2) \cdot \frac{1}{j\omega C} + R(i_1 + i_2) \quad \text{(2.)}$$

$$\begin{bmatrix} 100 \angle 0 \\ 0 \end{bmatrix} = \begin{bmatrix} j\omega(L_{11} - M) & j\omega(M - L_{22}) \\ (j\omega M + \frac{1}{j\omega C} + R) & (j\omega L_{22} + \frac{1}{j\omega C} + R) \end{bmatrix} \begin{bmatrix} \bar{I}_1 \\ \bar{I}_2 \end{bmatrix}.$$

$$\text{Solving, } \bar{I}_1 = 26.48 \angle -78.1^\circ \text{ A, } \bar{I}_2 = 24.742 \angle 85.77^\circ$$

$$\therefore \bar{I}_R = \bar{I}_1 + \bar{I}_2 = 7.39 \angle -9.649^\circ \text{ A.}$$

$$i_R(t) = \sqrt{2} \times 7.39 \sin(2\pi \times 50t - 9.649^\circ) \text{ A.}$$

Now,  
Solu

S. (a) Ideal transformer:

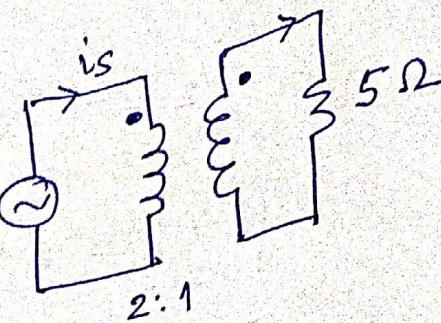
$$v_s(t) = \sqrt{2} \times 100 \sin(2\pi \times 50t + 45^\circ) \text{ V.}$$

$$\bar{V}_s = 100 \angle 45^\circ \text{ V.}$$

$$\bar{V}_R = \bar{V}_s / 2 = 50 \angle 45^\circ \text{ V.}$$

$$\bar{I}_R = \bar{V}_R / 5 = 10 \angle 45^\circ \text{ A.}$$

$$\bar{I}_S = \frac{N_2}{N_1} \bar{I}_R = \frac{1}{2} \times 10 \angle 45^\circ = 5 \angle 45^\circ \text{ A.}$$



(b) Non-ideal transformer:

Under open-circuit conditions,

$$\bar{V}_s = j\omega L_{11} \bar{I}_{oc}$$

$$\therefore j\omega L_{11} = \frac{\bar{V}_s}{\bar{I}_{oc}} \Rightarrow L_{11} = 795.8 \text{ mH.}$$

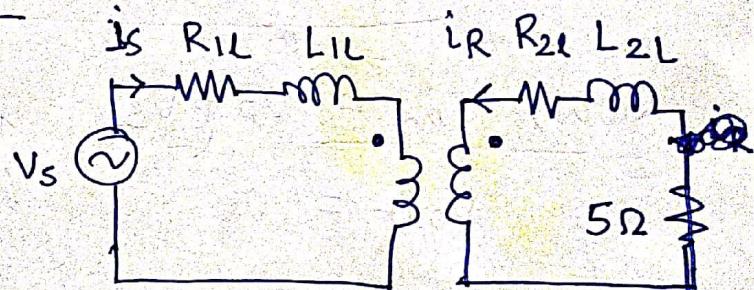
$$L_{11} = \frac{N_1}{N_2} M + L_{1e} \Rightarrow M = 396.3 \text{ mH.}$$

$$L_{22} = \frac{N_2}{N_1} M + L_{2e} \Rightarrow L_{22} = 198.85 \text{ mH.}$$

$$\text{Now, } \bar{V}_s = R_{1e} \bar{I}_S + j\omega L_{11} \bar{I}_S + j\omega M \bar{I}_R$$

$$0 = j\omega L_{22} \bar{I}_R + j\omega M \bar{I}_S + R \bar{I}_R$$

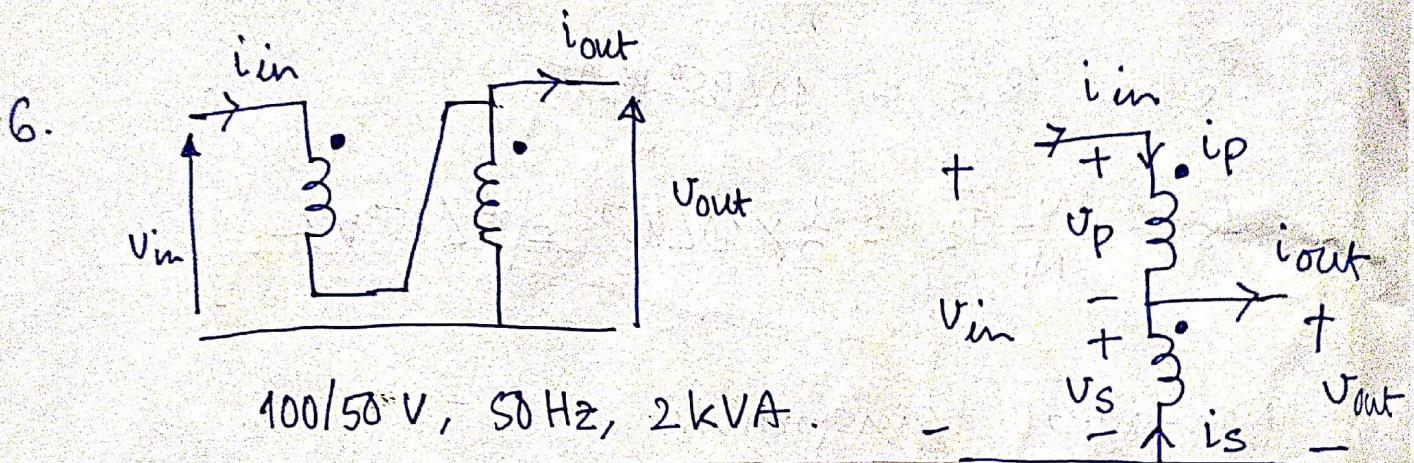
$$\text{Solving, } \bar{I}_S = 4.75 \angle 35.13^\circ \text{ A, } \bar{I}_R = 9.44 \angle -140.18^\circ \text{ A.}$$



$$\bar{V}_2 = -R \bar{I}_2 = 47.2 \angle 39.82^\circ A.$$

$$\left| \frac{\bar{V}_1}{\bar{V}_2} \right| = 2.118 \neq 2, \quad \left| \frac{\bar{I}_2}{\bar{I}_1} \right| = 1.987 \neq 2.$$

$$Re[\bar{V}_1 \bar{I}_1^*] = 468.68 W, \quad Re[\bar{V}_2 \bar{I}_2^*] = 446.22 W.$$



$$Now, V_{in} = V_p + V_s$$

$$V_{out} = V_s \quad \therefore \frac{V_{out}}{V_{in}} = \frac{V_s}{V_p + V_s} = \frac{1}{1 + V_p/V_s}$$

$$= \frac{1}{3}.$$

$$i_{in} = i_p \text{ and } i_{out} = i_p + i_s.$$

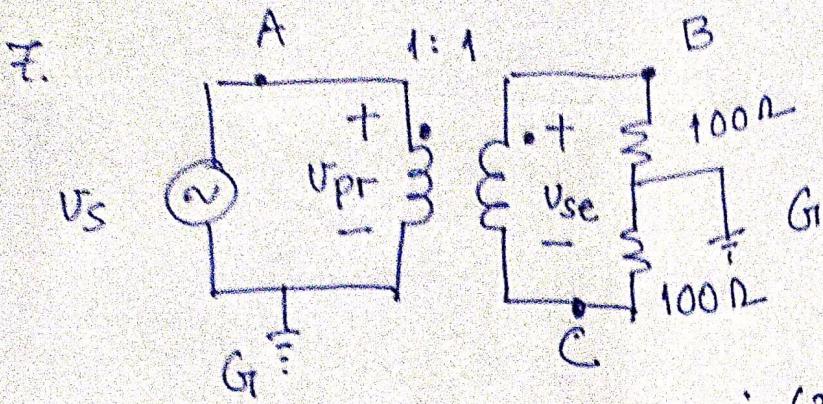
$$\therefore \frac{i_{in}}{i_{out}} = \frac{i_p}{i_p + i_s} = \frac{1}{1 + i_s/i_p} = \frac{1}{3}.$$

$$VA \text{ rated} = 2000 VA \quad V_p \text{ rated} = 100 V.$$

$$So, I_p \text{ rated} = 20 A.$$

$$\text{New rating} = V_{in} \cdot i_{in} = (V_p + V_s) i_p = 1.5 V_p^2$$

$$= 3 kVA$$



$$V_S = \sqrt{2} \times 100 \sin(2\pi \times 50t) \text{ V.}$$

$$\bar{V}_{Pr} = \bar{V}_S = 100 \angle 0 \text{ V.}$$

$$\bar{V}_{Se} = \bar{V}_{Pr} = 100 \angle 0 \text{ V.}$$

$$\therefore \bar{V}_{BC} = 100 \angle 0 \text{ V.}$$

$$\therefore \bar{V}_{BG_1} = \frac{100 \angle 0}{2} = 50 \angle 0 \text{ V.}$$

$$\bar{V}_{AG_1} = 100 \angle 0 \text{ V.}$$

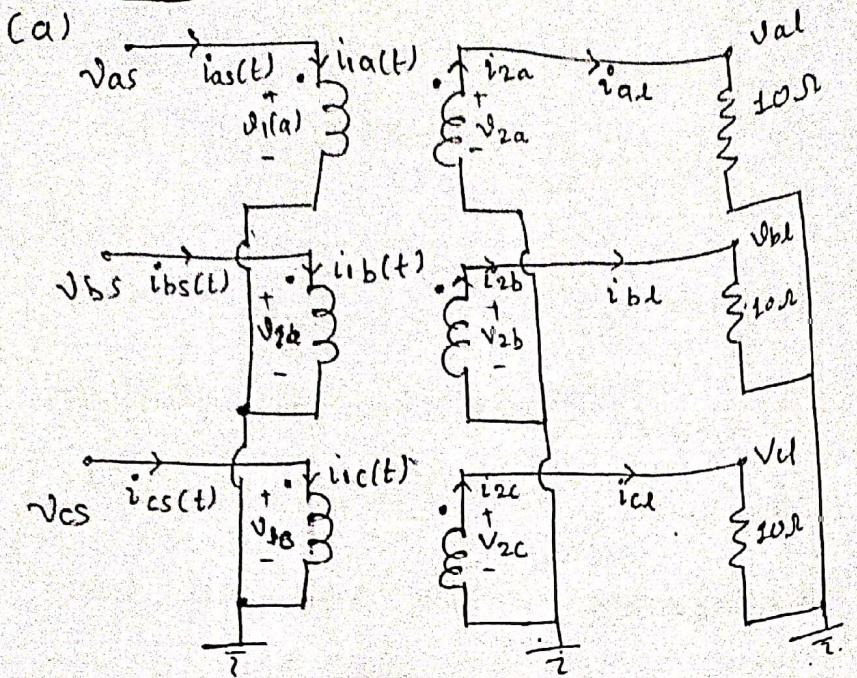
$$\therefore \bar{V}_{AB} = \bar{V}_{AG_1} - \bar{V}_{BG_1} = 50 \angle 0 \text{ V.}$$

$$\therefore V_{AB}(t) = \underline{\underline{\sqrt{2} \times 50 \sin(2\pi \times 50t)}} \text{ V.}$$

8.  $\frac{U_1}{N_1} = \frac{U_2}{N_2} = \frac{U_3}{N_3} .$

$$N_1 i_1 = N_2 i_2 + N_3 i_3 .$$

Problem: 9



Let the voltage across the three primary windings be  $v_{1a}, v_{1b}, v_{1c}$  and the corresponding secondary winding voltages be  $v_{2a}, v_{2b}, v_{2c}$ , respectively.

Let the current in the three primary windings be  $i_{1a}, i_{1b}, i_{1c}$  and the corresponding secondary winding currents be  $i_{2a}, i_{2b}, i_{2c}$  respectively.

Note: The current enters the dot in primary and leaves the dot in secondary.

The transformers are given to be ideal, so,

$$\frac{v_{1a}}{v_{2a}} = \frac{v_{1b}}{v_{2b}} = \frac{v_{1c}}{v_{2c}} = \frac{2}{1}$$

And assuming there is no open-circuit current, i.e.  $I_{oc} = 0$ ,

$$\frac{i_{1a}}{i_{2a}} = \frac{i_{1b}}{i_{2b}} = \frac{i_{1c}}{i_{2c}} = \frac{1}{2}$$

Since primary side windings are connected in star, we have,  
 $i_{as} = i_{1a}$ ,  $i_{bs} = i_{1b}$ ,  $i_{cs} = i_{1c}$ .

Since neutral point is grounded, we have

$$v_{as} = v_{1a}, v_{bs} = v_{1b}, v_{cs} = v_{1c}.$$

since secondary winding is star connected.

grounded, we have

$$i_{2a} = i_{2a}, i_{2b} = i_{2b}, i_{2c} = i_{2c},$$

$$v_{2a} = v_{2a}, v_{2b} = v_{2b}, v_{2c} = v_{2c}.$$

$$\therefore \frac{v_{al}}{v_{as}} = \frac{v_{2a}}{v_{1a}} = \frac{1}{2} \Rightarrow v_{al} = \frac{\sqrt{2} \cdot 25 \sin(2\pi \cdot 50t)}{2} = \sqrt{2} \cdot 25 \sin(2\pi \cdot 50t)$$

Similarly,  $v_{bl}$  and  $v_{cl}$  can be calculated.

$$v_{bl} = \sqrt{2} \cdot 25 \sin(2\pi \cdot 50t - 2\pi/3), v_{cl} = \sqrt{2} \cdot 25 \sin(2\pi \cdot 50t + 2\pi/3)$$

Since the impedances are star connected with neutral grounded,

$$i_{al} = v_{al}/z_0, i_{bl} = v_{bl}/z_0, i_{cl} = v_{cl}/z_0.$$

$$i_{al} = \sqrt{2} \cdot 2.5 \sin(2\pi \cdot 50t), i_{bl} = \sqrt{2} \cdot 2.5 \sin(2\pi \cdot 50t - 2\pi/3)$$

$$i_{cl} = \sqrt{2} \cdot 2.5 \sin(2\pi \cdot 50t + 2\pi/3)$$

$$\begin{aligned} \frac{i_{al}}{i_{as}} &= \frac{i_{2a}}{i_{1a}} = \frac{2}{1} \Rightarrow i_{as} = \frac{\sqrt{2} \cdot 2.5 \sin(2\pi \cdot 50t)}{2} \\ &= \sqrt{2} \cdot 1.25 \sin(2\pi \cdot 50t) \end{aligned}$$

Similarly  $i_{bs}, i_{cs}$  can be calculated.

(b) configuration II is same as configuration I except primary is delta connected.

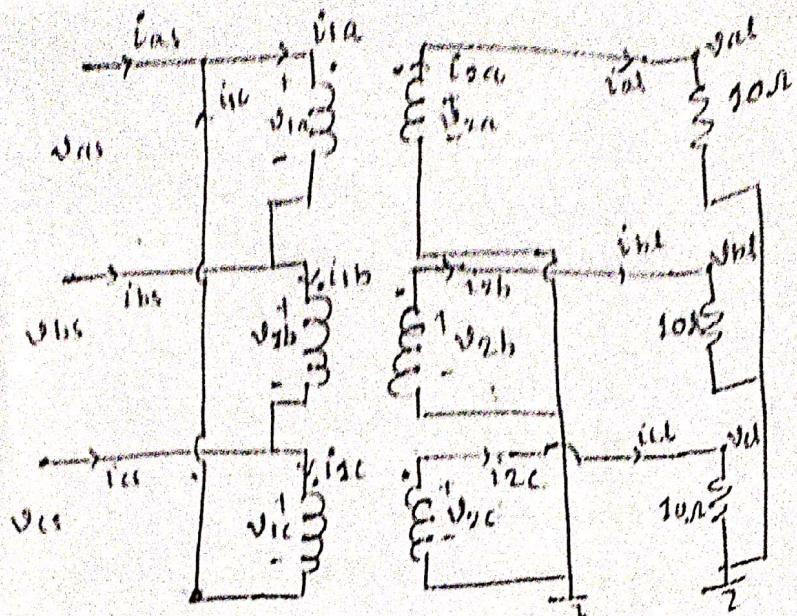
Since the secondary windings are connected in star, we have

$$i_{2a} = i_{al}, i_{2b} = i_{bl}, i_{2c} = i_{cl}$$

Since the secondary winding neutral and load neutral are grounded we have  $v_{2a} = v_{al}, v_{2b} = v_{bl}, v_{2c} = v_{cl}$ .

$$\frac{v_{1a}}{v_{2a}} = \frac{v_{1b}}{v_{2b}} = \frac{v_{1c}}{v_{2c}} = \frac{2}{1}$$

$$\frac{i_{1a}}{i_{2a}} = \frac{i_{2b}}{i_{2b}} = \frac{i_{2c}}{i_{2c}} = \frac{1}{2}$$



The primary windings are connected in delta, it can be seen from the circuit diagram given,

$$V_{1A} = V_{AS} - V_{BS}; \quad V_{1B} = V_{BS} - V_{CS}; \quad V_{1C} = V_{CS} - V_{AS}.$$

$$V_{1A} = \sqrt{2} \times \sqrt{3} \times 8 \sin(2\pi \times 50t + \pi/6) \times 50;$$

$$V_{1B} = \sqrt{2} \times \sqrt{3} \times 8 \sin(2\pi \times 50t - \pi/2) \times 50;$$

$$V_{1C} = \sqrt{2} \times \sqrt{3} \times 8 \sin(2\pi \times 50t + \frac{5\pi}{6}) \times 50;$$

$$V_{2A} = \frac{1}{2} V_{1A} = \sqrt{2} \times \sqrt{3} \times 25 \times \sin(2\pi \times 50t + \pi/6)$$

$$\therefore V_{AL} = V_{2A} \Rightarrow V_{AL} = \sqrt{2} \times \sqrt{3} \times 25 \sin(2\pi \times 50t + \pi/6)$$

As load is neutral connected, we can write,

$$i_{AL} = \frac{V_{AL}}{Z_L} = \sqrt{6} \times 2.5 \times 8 \sin(2\pi \times 50t + \pi/6)$$

Similarly  $i_{1B}$  and  $i_{1C}$  can be calculated.

$$\text{We know that, } i_{AL} = i_{1A} \text{ and } \frac{i_{1A}}{i_{2A}} = \frac{1}{2}$$

$$i_{1A} = \sqrt{6} \times 1.25 \sin(2\pi \times 50t + \pi/6)$$

$$i_{1B} = \sqrt{6} \times 1.25 \sin(2\pi \times 50t - \pi/2)$$

$$i_{1C} = \sqrt{6} \times 1.25 \sin(2\pi \times 50t + 5\pi/6)$$

looking at circuit diagram on primary side,

$$i_{bs} = i_{1b} - i_{1a}$$

$$i_{cs} = i_{1c} - i_{1b}$$

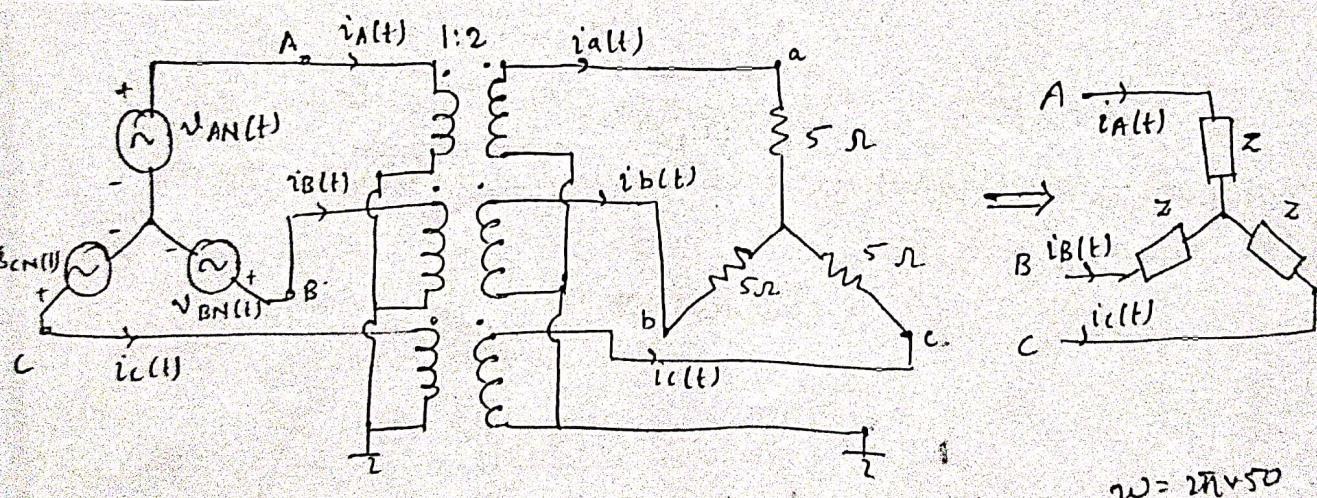
$$i_{as} = i_{1a} - i_{1c}$$

$$\begin{aligned} i_{as} &= \sqrt{6} + \sqrt{3} \times 1.25 \times \sin(2\pi \times 50t + \pi/6 - \pi/6) \\ &= \sqrt{2} + 3.75 \times \sin(2\pi \times 50t) \end{aligned}$$

$$i_{bs} = \sqrt{2} + 3.75 \times \sin(2\pi \times 50t - 2\pi/3)$$

$$i_{cs} = \sqrt{2} + 3.75 \times \sin(2\pi \times 50t + 2\pi/3)$$

Problem: ④ 10



$$\omega = 2\pi \times 50$$

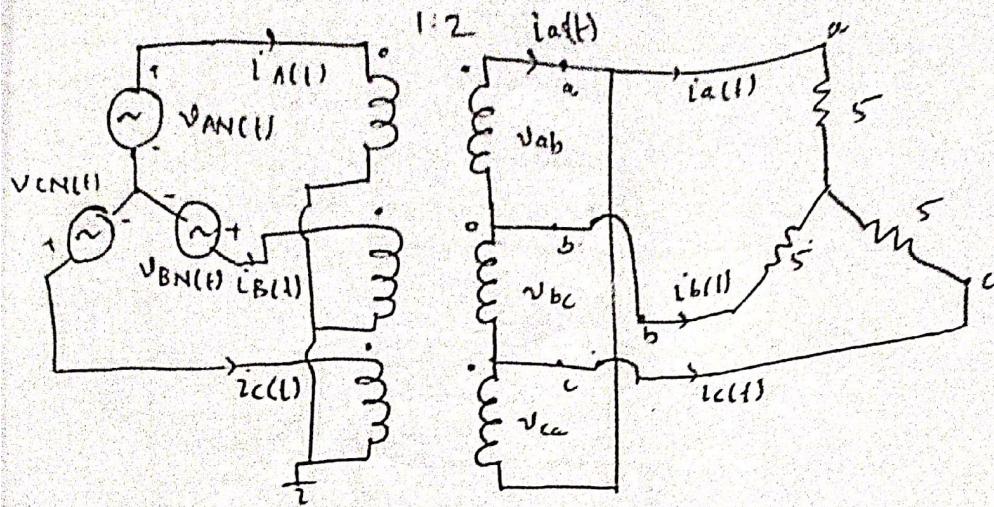
$$\frac{v_{AN}}{v_{AN}} = \frac{2}{1} \Rightarrow v_{AN} = 2 \times v_{AN} = \sqrt{2} \times 220 \times \sin(\omega t) V.$$

$$i_{al(t)} = \frac{v_{AN}}{\sqrt{3}} = \sqrt{2} \times \frac{220}{\sqrt{3}} \times \sin(\omega t) = \sqrt{2} \times 44 \sin(\omega t) A \Rightarrow i_{am} = 44 A$$

$$\frac{i_{al(t)}}{i_A(t)} = \frac{1}{2} \Rightarrow I_A(t) = 2 \times i_{al(t)} = \sqrt{2} \times 88 \sin(\omega t) A \Rightarrow i_{A,am} = 88 A$$

$$Z = \frac{\text{phasor } V_{AN}}{\text{phasor } i_A} = \frac{110 \angle 0^\circ}{88 \angle 0^\circ} = 1.25 \Omega$$

Y-Δ connection



$$V_{ab} = 2 \times V_{AN} = \sqrt{2} \times 220 \sin(\omega t)$$

phase voltage with respect to star point of load  $\alpha$ , (writing 5)

$$= \frac{\sqrt{2} \times 220 \sin(\omega t - 30^\circ)}{\sqrt{3}}$$

$$i_a(t) = \frac{\sqrt{2} \times 220 \sin(\omega t - 30^\circ)}{\sqrt{3} \times 5}$$

$$i_{a\text{rms}} = \frac{220}{5\sqrt{3}} = 25.4 \text{ A}$$

The current in secondary winding is,

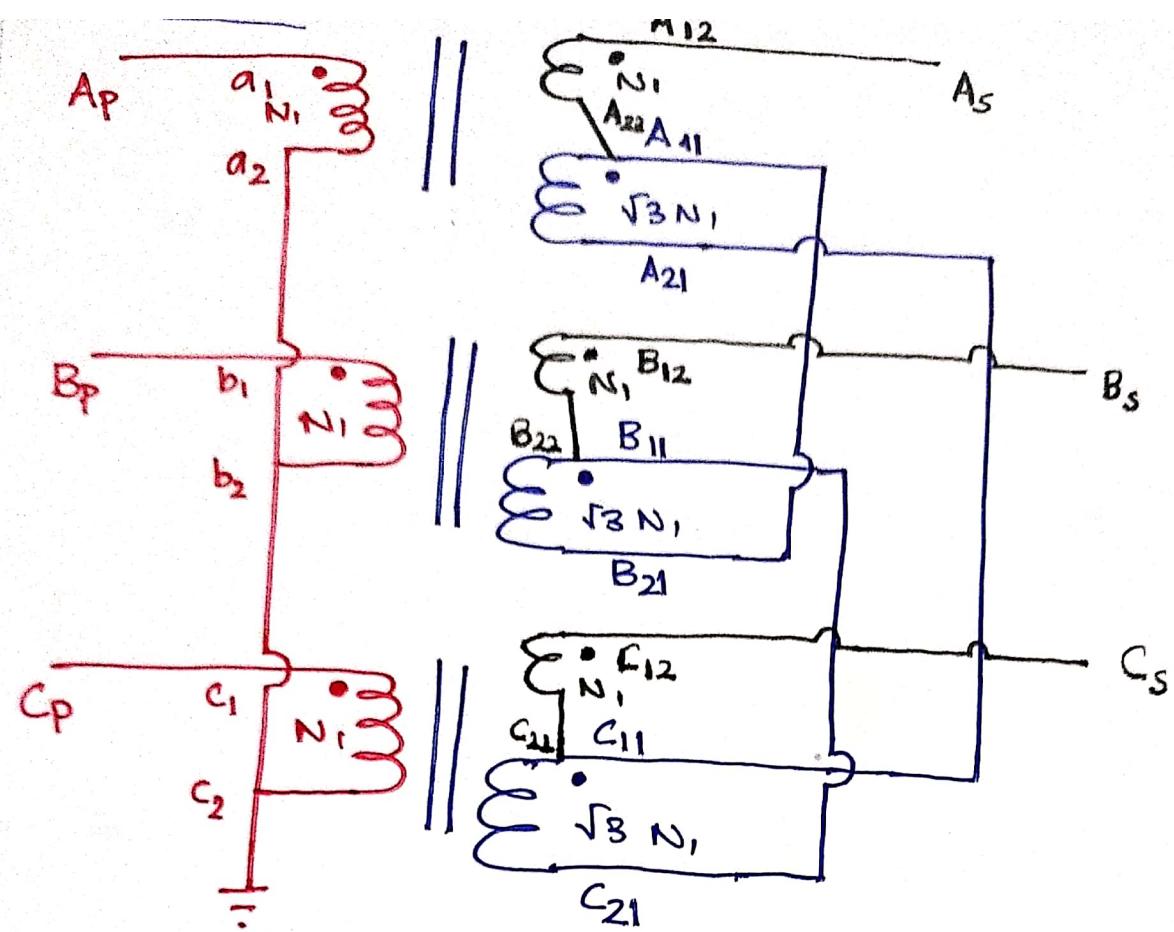
$$i_{as}(t) = i_a(t) + i_c(t)$$

$$= \frac{\sqrt{2} \times 220 \sin(\omega t - 30^\circ + 30^\circ)}{\sqrt{3} \times \sqrt{3} \times 5}$$

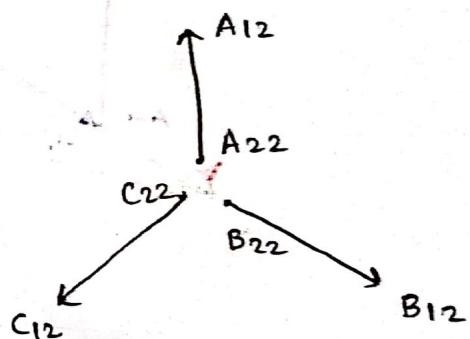
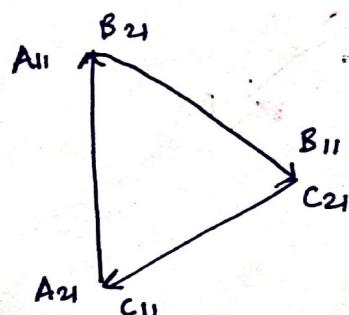
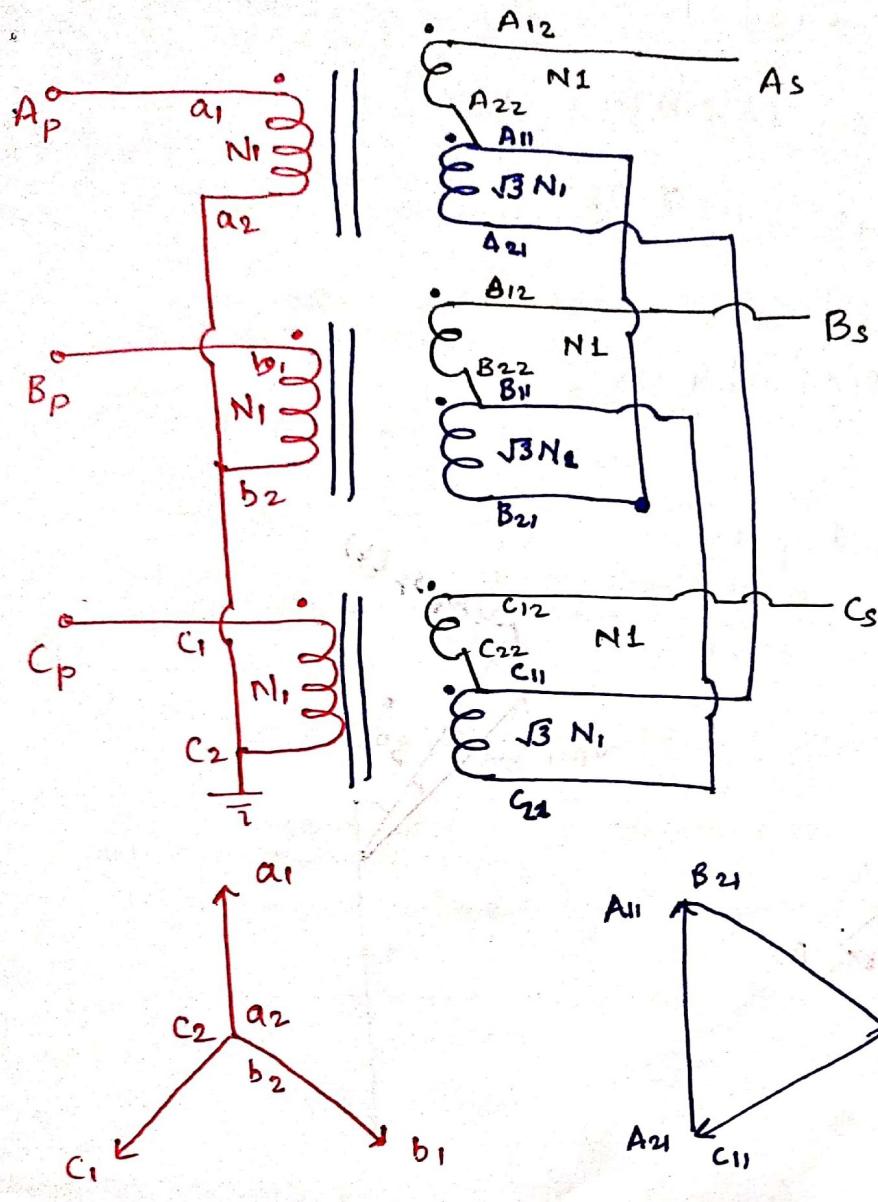
$$= \frac{\sqrt{2} \times 220 \sin(\omega t)}{15}$$

$$i_A(t) = \bar{i}_{as}(t) = \frac{\sqrt{2} \times 440}{15} \sin(\omega t) \text{ A} = 29.33 \text{ A}$$

$$Z = \frac{V_{AN}}{I_A} = 3.75 \Omega$$



Problem : 8



$$v_{a_1 a_2}(t) = V \sin \omega t$$

$$v_{b_1 b_2}(t) = V \sin(\omega t - 120^\circ)$$

$$v_{A_{11} A_{21}}(t) = \sqrt{3} V \sin \omega t$$

$$v_{B_{11} B_{21}}(t) = \sqrt{3} V \sin(\omega t - 120^\circ)$$

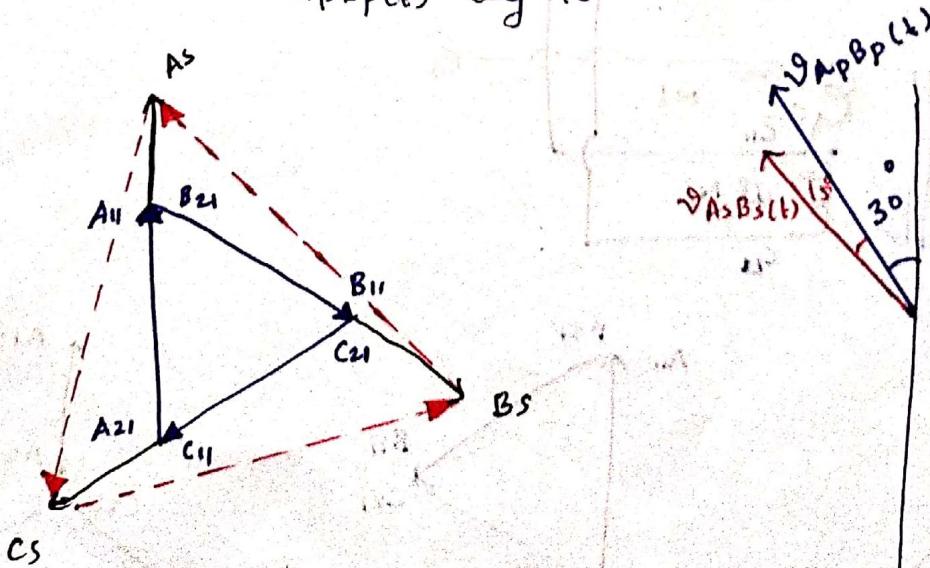
$$v_{A_{12} A_{22}}(t) = V \sin \omega t$$

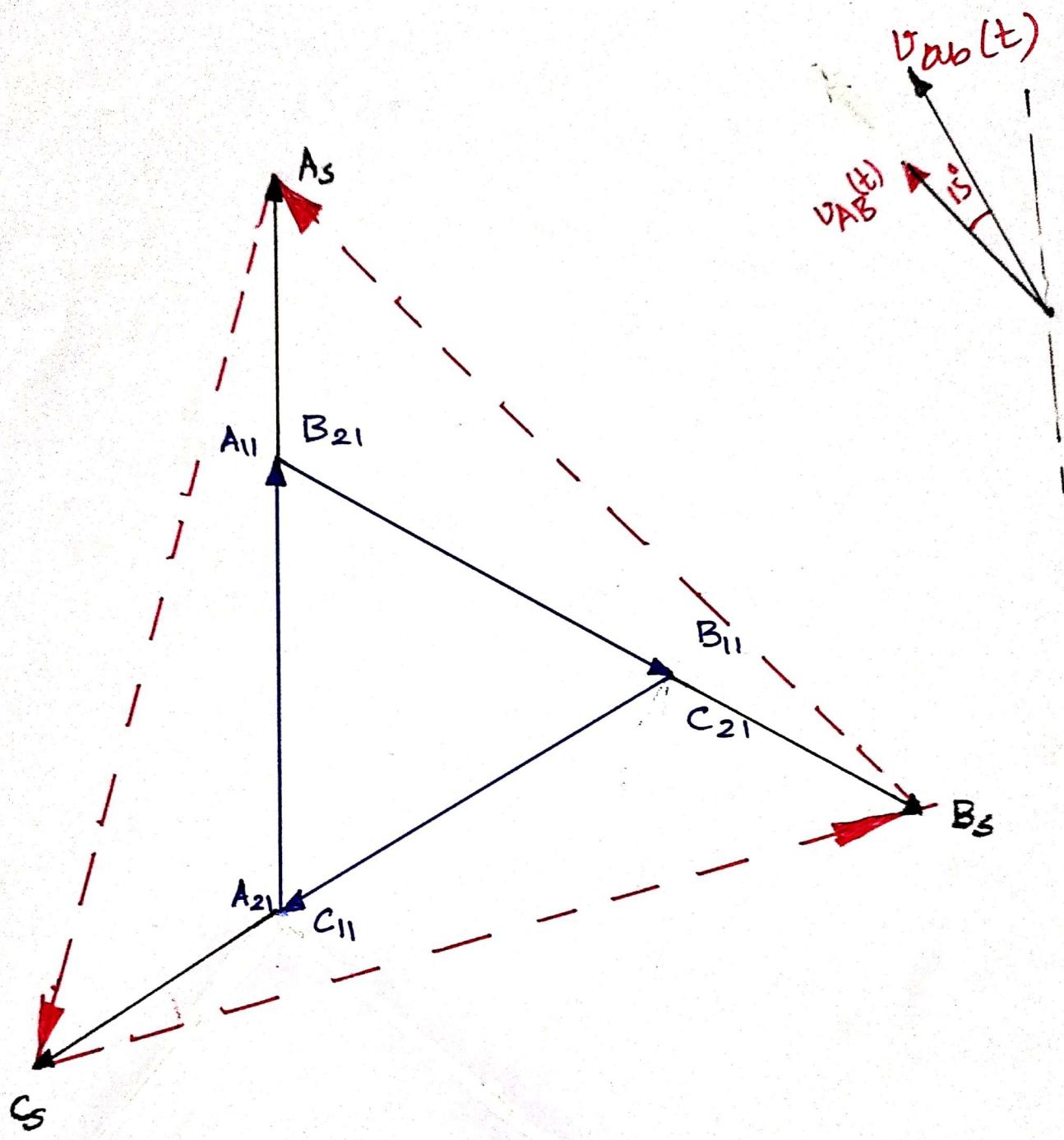
$$v_{B_{12} B_{22}}(t) = V \sin(\omega t - 120^\circ)$$

$$\begin{aligned} v_{A_P B_P}(t) &= v_{a_1 a_2}(t) - v_{b_1 b_2}(t) = V (\sin(\omega t) - \sin(\omega t - 120^\circ)) \\ &= \sqrt{3} V \sin(\omega t + 30^\circ) \end{aligned}$$

$$\begin{aligned} v_{A_S B_S}(t) &= v_{A_{12} A_{22}}(t) + v_{B_{21} B_{11}}(t) + v_{B_{22} B_{12}}(t) \\ &= V \sin(\omega t) - \sqrt{3} V \sin(\omega t - 120^\circ) - V \sin(\omega t - 120^\circ) \\ &= \sqrt{3} V \sin(\omega t + 30^\circ) - \sqrt{3} V \sin(\omega t - 120^\circ) \\ &= \frac{2\sqrt{3} V}{T} \cos(\omega t - 45^\circ) \sin(75^\circ) \\ &= \frac{2\sqrt{3} V}{T} \sin(75^\circ) \sin(\omega t + 45^\circ) \end{aligned}$$

Thus  $v_{A_S B_S}(t)$  leads  $v_{A_P B_P}(t)$  by  $15^\circ$ .





Problem 12 : (B).

Problem 13 : (A).

Problem 14 : (D) 4 mH.