

## Homework Lecture 4

3.1

Show the results of adding the following pairs of five-bit twos complement numbers and indicate whether or not overflow occurs for each case.

$$\begin{array}{r} 1\ 0\ 1\ 1\ 0 \\ +\ 1\ 0\ 1\ 1\ 1 \\ \hline \end{array}$$

$$\begin{array}{r} 1\ 1\ 1\ 1\ 0 \\ +\ 1\ 1\ 1\ 0\ 1 \\ \hline \end{array}$$

$$\begin{array}{r} 1\ 1\ 1\ 1\ 1 \\ +\ 0\ 1\ 1\ 1\ 1 \\ \hline \end{array}$$

3.3

Add the following twos complement and ones complement binary numbers as indicated. For each case, indicate if there is overflow.

Two's complement

$$\begin{array}{r} 1\ 0\ 1\ 1.1\ 0\ 1 \\ +\ 0\ 1\ 1\ 1.0\ 1\ 1 \\ \hline \end{array}$$

One's complement

$$\begin{array}{r} 1\ 0\ 1\ 1.1\ 0\ 1 \\ +\ 0\ 1\ 1\ 1.0\ 1\ 1 \\ \hline \end{array}$$

3.4

Show the process of serial unsigned multiplication for 1010 (multiplicand) and multiplied by 0101 (multiplier).

In the lecture hardware for a sequential unsigned multiplier is given. So for this example the intermediate steps (content of the registers after each step).

### Exercise 1

The IEEE FP standard 754 also defines a "double precision" floating point number system. Properties:

- total number of bits 64
- sign: single bit (left most bit)
- exponent: 11 bits, excess 1023 code, all zero and all one is used for special numbers.
- fraction field 52 bits. A hidden bit is used (not included in the 52 bits). Point is right of hidden bit.

For the normalized numbers:

- a) Max decimal value of the mantissa ( $M_{\max}$ )
- b) Min decimal value of the mantissa ( $M_{\min}$ )
- c) Max decimal value of the exponent ( $E_{\max}$ )
- d) Min decimal value of the exponent ( $E_{\min}$ )
- e) Largest positive decimal value that can be representend ( $V_{\max}$ )
- f) Smallest positive decimal value that can be represented ( $V_{\min}$ )