Reg. No.:
Name:



#### Continuous Assessment Test (CAT) – I – August 2018

Programme : **B. Tech** Semester : **Fall 2018-19**Course : **Calculus and Laplace Transforms** Code : **MAT1001** 

Faculty: Dr. Anant Kant Shukla Slot/Class No.: B2+LB2+TB2/1076

Time :  $1\frac{1}{2}$  hours Max. Marks : 50

### **Answer all the Questions**

Q.No. **Question Description** Marks Show that the function  $f(x,y) = \begin{cases} \frac{x^2y^2}{x^4+y^4}, & (x,y) \neq (0,0) \\ 0, & (x,y) = (0,0) \end{cases}$  is discontinuous at the origin 1. 7 and check if the partial derivatives with respect to x and y exist at the origin. 2. Let P = P(V, R, T) and is given by P = RT/V, where R = R(t), T = T(t), V = V(t)6 then find dP/dt if at some t > 0, R'(t) = 0.1, T'(t) = 0.1, V'(t) = 0.01, R = 2, T = 0.01V = 1 units. Find  $\partial w/\partial u$  and  $\partial w/\partial v$  where  $w = 0.5 (x^2 + y^2 + z^2)^{-1}$ ,  $x = u^2 + v^2$ ,  $y = u^2 - v^2$ 3. 7  $v^2$ , z = 2uv. Prove the formula grad(fg) = f grad(g) + g grad(f) for the functions  $f = e^{xyz}$ , 4. 10 g = x + y. 5. Find the local extreme values of the function  $f = \frac{y + x^2 y^2 + x}{ry}$  if exist. 10 Find quadratic and cubic approximations of  $f = \ln(2x + y + 1)$  near origin. 6. 10

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Time :  $1\frac{1}{2}$  hours Max. Marks : 50

### **Answer all the Questions**

**Question Description** Q.No. Marks Show that the function  $f(x,y) = \begin{cases} \frac{x^4 - y^2}{x^4 + y^2}, & (x,y) \neq (0,0) \\ 0, & (x,y) = (0,0) \end{cases}$  is not continuous at the origin. 1. 7 The plane y = 1 intersects the surface  $z = x^2 - xy + y^2$  in a parabola. Find the slope 2. 7 of the tangent to the parabola at point (1,1,1). 3. Let w = f(x, y) and  $x = r \cos \theta$ ,  $y = r \sin \theta$  then prove that 7  $(f_x)^2 + (f_y)^2 = (w_r)^2 + \frac{1}{r^2} (w_\theta)^2.$ Find the directions of maximum and minimum change of the function  $f = \frac{x}{y} - yz$  at 4. 7 the point (4,1,1). Find the maxima, minima and saddle points of f(x, y) if any, given that  $f_x = 9x^2 - 9$ 5. 7 and  $f_{y} = 2y + 4$ . 6. Find the level surface of  $f = \frac{1}{x^2 + y^2 + z^2}$  and then find normal to that level surface at 5 point (1,1,1). 7. Find the maximum and minimum values of f = x - 2y + 5z on the sphere 10  $x^2 + y^2 + z^2 = 30.$ 

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Time :  $1\frac{1}{2}$  hours Max. Marks : 50

# **Answer all the Questions**

| Q.No. | Question Description  | Marks |
|-------|---|-------|
| 1.    | Find the normal to the surface $2z^3 - 3(x^2 + y^2)z + \tan^{-1}(xz) = 5$ at the point (1,1,1).   | 7     |
| 2.    | Show that the function $f(x,y) = \begin{cases} \frac{x^2y^2}{x^4+y^4}, & (x,y) \neq (0,0) \\ 0, & (x,y) = (0,0) \end{cases}$ is discontinuous at the origin and check if the partial derivatives with respect to $x$ and $y$ exist at the origin. | 7     |
| 3.    | Find an equation for the tangent plane on the surface $cos(\pi x) - x^2y + e^{xz} + yz = 4$ at the point (0,1,2).   | 6     |
| 4.    | Find the directional derivative of $f = xy^2 + yz^3$ at the point (2,-1,1) in the direction of the normal to the surface $x \ln(z) - y^2 = -4$ at the point (-1,2,1).   | 10    |
| 5.    | Find the largest product the positive numbers $x$ , $y$ and $z$ can have if $x + y + z^2 = 16$ .  | 10    |
| 6.    | Let $w = xy + yz + zx$ , and $x = t, y = \cos t$ , $z = \sin t$ . Find $dw/dt$ by direct substitution and by chain rule. Verify the results obtained.   | 10    |