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### 0.1 Polar co-ordinates

#### 0.1.1 All complex numbers can be shown in polar form

Consider a complex number

$$z = a + bi$$

We can write this as:

$$z = r \cos(\theta) + ir \sin(\theta)$$

#### 0.1.2 Polar forms are not unique

Because the functions loop:

$$ae^{i\theta} = a(\cos(\theta) + i \sin(\theta))$$

$$ae^{i\theta} = a(\cos(\theta + n\tau) + i \sin(\theta + n\tau))$$

$$ae^{i\theta} = ae^{i\theta + n\tau}$$

Additionally:

$$ae^{i\theta} = a(\cos(\theta) + i \sin(\theta))$$

$$ae^{i\theta} = a(\cos(\theta) + i \sin(\theta))$$

$$ae^{i\theta} = -a(\cos(\theta) - i \sin(\theta))$$

$$ae^{i\theta} = -a(\cos(\theta + \frac{\pi}{2}) + i \sin(\theta + \frac{\pi}{2}))$$

#### 0.1.3 Real and imaginary parts of a complex number in polar form

We can extract the real and imaginary parts of this number.

$$Re(z) := r \cos(\theta)$$

$$Im(z) := r \sin(\theta)$$

Alternatively:

$$Re(z) = r \frac{e^{i\theta} + e^{-i\theta}}{2}$$

$$\operatorname{Im}(z) = r \frac{e^{i\theta} - e^{-i\theta}}{2i}$$