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0.1 Addition of sine and cosine

0.1.1 Adding waves with same frequency

We know that:

$$a\sin(bx+c) = a\sin(bx)\cos(c) + a\sin(c)\cos(bx)$$

So:

$$a\sin(bx+c) + d\sin(bx+e) = a\sin(bx)\cos(c) + a\sin(c)\cos(bx) + d\sin(bx)\cos(e) + d\sin(e)\cos(bx)$$

We know that:

$$\sin(\theta) = \frac{e^{i\theta} - e^{-i\theta}}{2i}$$

So:

$$\begin{split} a\sin(bx+c) + d\sin(bx+f) &= a\frac{e^{i(bx+c)} - e^{-i(bx+c)}}{2i} + d\frac{e^{i(bx+f)} - e^{-i(bx+f)}}{2i} \\ a\sin(bx+c) + d\sin(bx+f) &= \frac{a(e^{i(bx+c)} - e^{-i(bx+c)}) + d(e^{i(bx+f)} - e^{-i(bx+f)})}{2i} \\ a\sin(bx+c) + d\sin(bx+f) &= \frac{a(e^{ibx}e^{ic} - e^{-ibx}e^{-ic}) + d(e^{ibx}e^{if} - e^{-ibx}e^{-if})}{2i} \\ a\sin(bx+c) + d\sin(bx+f) &= \frac{(e^{ibx}(ae^{ic} + de^{if}) - e^{-ibx}(ae^{-c} + d^{-if})}{2i} \\ a\sin(bx+c) + d\sin(bx+f) &= \frac{(e^{ibx}(ae^{ic} + de^{if}) - e^{-ibx}(ae^{-c} + d^{-if})}{2i} \\ a_i\sin(b_ix+c_i) + a_j\sin(b_jx+c_j) &= a_i\sin(b_ix+c_i) + a_j\sin(b_ix+c_j) \\ a_i\sin(b_ix+c_i) + a_j\sin(b_jx+c_j) &= a_i\sin(b_ix)\cos(c_i) + a_i\sin(c_i)\cos(b_ix) + a_j\sin(b_ix)\cos(c_j) + a_j\sin(c_j)\cos(b_ix) \end{split}$$