1 Expanding functions of natural numbers