

## Contents

0.1	Cantors theorem . . . . .	1
0.1.1	Proof . . . . .	1

### 0.1 Cantors theorem

The cardinality of the powerset is strictly greater than the cardinality of the underlying set.

That is,  $|P(s)| < |s|$ .

This applies to finite sets and infinite sets. In particular, this means that the powerset of the natural numbers is bigger than the natural numbers.

#### 0.1.1 Proof

If one set is at least as big as another, then there is a surjection from that set to the other.

That is, if we can prove that there is no surjection from a set to its powerset, then we have proved the theorem.

We consider  $f(s)$ . If there is a surjection, then for every subset of  $s$  there should be a mapping from  $s$  to that subset.

We take set  $s$  and have the powerset of this,  $P(s)$ .

Consider the set:

$$A = \{x \in s | x \notin f(x)\}$$

That is, the set of all elements of  $s$  which do not map to the surjection.