

## 0.1 Matrix additon and multiplication

### 0.1.1 Matrix multiplication

$$A = A^{mn}$$

$$B = B^{no}$$

$$C = C^{mo} = A.B$$

$$c_{ij} = \sum_{r=1}^n a_{ir}b_{rj}$$

Matrix multiplication depends on the order. Unlike for real numbers,

$$AB \neq BA$$

Matrix multiplication is not defined unless the condition above on dimensions is met.

A matrix multiplied by the identity matrix returns the original matrix.

For matrix  $M = M^{mn}$

$$M = MI^m = I^n M$$

### 0.1.2 Matrix addition

2 matrices of the same size, that is with identical dimensions, can be added together.

If we have 2 matrices  $A^{mn}$  and  $B^{mn}$

$$C = A + B$$

$$c_{ij} = a_{ij} + b_{ij}$$

An empty matrix with 0s of the same size as the other matrix is the identity matrix for addition.

### 0.1.3 Scalar multiplication

A matrix can be multiplied by a scalar. Every element in the matrix is multiplied by this.

$$B = cA$$

$$b_{ij} = ca_{ij}$$

The scalar 1 is the identity scalar.