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## 0.1 Lie algebra

Lie groups have symmetries. We can consider only the infintesimal symmetries.

For example the unit circle has many symmetries, but we can consider only those which rotate infintesimally.

#### 0.1.1 Example

Take a continous group, such as U(1). Its Lie algebra is all matrices such that their exponential is in the Lie group.

$$\mathfrak{u}(1) = \{ X \in \mathbb{C}^{1 \times 1} | e^{tX} \in U(1) \forall t \in \mathbb{R} \}$$

This is satisfied by the matrices where  $M=-M^*$ . Note that this means the diagonals are all 0.

### 0.1.2 Scale of specific Lie algebra matrices doesn't matter

Because of t.

#### 0.1.3 Commutation of Lie group algebra

Consider two members of the Lie algebra: A and B. The commutator is:

A.

The corresponding Lie group member is:

$$e^{t(A+B)} = e^{tA}e^{tB}$$

While the Lie group multiplication may not commute, the corresponding addition of the Lie algebra does.