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0.1 Length of a curve

We have a curve from a to b in \mathbb{R}^n .

$$f:[a,b]\to {\bf R}^n$$

We divide this into n segments.

The ith cut is at:

$$t_i = a + \frac{i}{n}(b - a)$$

So the first cut is at:

$$t_0 = a$$

$$t_n = b$$

The distance between two sequential cuts is:

$$||f(t_i) - f(t_{i-1})||$$

The sum of all these differences is:

$$L = \sum_{i=1}^{n} ||f(t_i) - f(t_{i-1})||$$

The limit is:

$$L = \lim_{n \to \infty} \sum_{i=1}^{n} ||f(t_i) - f(t_{i-1})||$$

0.1.1 Method 1

$$L = \lim_{n \to \infty} \sum_{i=1}^{n} ||f(t_i) - f(t_{i-1})||$$

$$L = \lim_{n \to \infty} \sum_{i=1}^{n} || \frac{f(t_i) - f(t_{i-1})}{\Delta t} || \Delta t$$

$$L = \lim_{n \to \infty} \sum_{i=1}^{n} ||f'(t)|| \Delta t$$

$$L = \int_{a}^{b} ||f'(t)|| dt$$

0.1.2 Method 2

$$\begin{split} L &= \lim_{n \to \infty} \sum_{i=1}^{n} ||f(t_i) - f(t_{i-1})|| \\ L &= \lim_{n \to \infty} \sum_{i=1}^{n} \sqrt{(f(t_i) - f(t_{i-1}))^* M(f(t_i) - f(t_{i-1}))} \\ L &= \int_a^b \sqrt{(dt)^T M(dt)} \end{split}$$