

0.1 Euclidian division

Euclidian division is the theory for any pair of natural numbers, we can divide one by the other and have a remainder less than the divisor. Formally: $\forall a \in \mathbb{N}, \forall b \in \mathbb{N}^+, \exists q \in \mathbb{N}, \exists r \in \mathbb{N}[(a = bq + r) \wedge (0 \leq r < b)]$

Where \mathbb{N}^+ refers to natural numbers excluding 0.

That is, every natural number a is a multiple q of any other natural number b , plus another natural number r less than the other natural number b .

These are unique. For each jump in q , r falls by b . As the range of r is b there is only one solution.

$$17 = 2 \cdot 8 + 1$$

$$9 = 3 \cdot 3 + 0$$