

0.1 Extreme value theorem

We can expand the boundedness theorem such that m and M are functions of $f(x)$ in the bound $[a, b]$. That is:

$$\exists m \in \mathbb{R} \exists M \in \mathbb{R} \forall x \in [a, b] (m < f(x) < M)$$