

## 0.1 Cardinality of the natural numbers

Consider the infinite set, that is the set of all natural numbers which is defined in ZFC. Clearly there isn't a natural number cardinality of this – we instead write  $\aleph_0$ .

We call sets with this cardinality, countably infinite.

So:

$$|\mathbb{N}| = \aleph_0$$

### 0.1.1 Cardinality of natural numbers

We define:

$$|\emptyset| = 0$$

That, the empty set has a cardinality of 0.

As we define 0 as the empty set,  $|0| = 0$ .

What is 1? using the definition above we know  $|1| > |0|$ , so let's say  $|1| = 1$ , and more generally:

$$\forall n \in \mathbb{N} |n| = n$$