## 1 Neighbourhoods

## 1.1 Neighbourhood topology

We have a set X.

For each element  $x \in X$ , there is a non-empty set of neighbourhoods  $N \in \mathbf{N}(x)$  where  $x \in N \subseteq X$  such that:

- If N is a subset of M, M is a neighbourhood.
- The intersection of two neighbourhoods of x is a neighbourhood of x.
- N is a neighbourhood for each point in some  $M\subseteq N$