0.1 Lie algebra of $O(n)$

0.1.1 $O(n)$ forms a Lie group

0.1.2 Lie algebra of $O(n)$

The Lie algebra of (n) is defined as:

$\mathfrak{o}(n) = \{X \in \mathbb{R}^{n \times n} | e^{tX} \in O(n) \forall t \in \mathbb{R}\}$

This is satisfied by the skew-symmetric matrices where $M = -M^T$. Note that this means the diagonals are all 0.