1 Real functions as infinite-dimensional vectors