0.1 Covariant and contravariant bases

In element form we write a vector as:

$v = e_i v^i$

The indices are raised and lowered to reflect whether the value is covariant or contravariant.

v^i is contravariant. If the basis moves one way, it moves the other.

e_i is covariant. If the basis moves, it moves with it.