

## A few notes on the sign pattern.

The sign pattern: Please work through the problems in your Study guide .  
The SG is under study material on myUnisa.

Very important:

1. Always put in your sign table those functions which **change signs** or are **always negative**.
2. Remember to include the values in your sign pattern where you have **division by zero**.
3. Always work with **positive powers of  $x$**  and put on a common denominator (to be able to do the problem) and find the correct sign pattern. For example for  $f(x) = x + 1/x$  ,

$$f'(x) = 1 - 1/x^2 = \frac{x^2 - 1}{x^2}$$

Then you have to follow the rules for the parabolas (see B below).  
Also, **never use the form  $f'(x) = 1 - x^{-2}$**  in your sign pattern since you cannot make any deductions from this.  
You will get a mark for the derivative but 0 for the sign pattern.

A. Now **straight lines** have the form  $y = mx + c$ .

If you have a straight line draw the line (rough work if you must).

The point where it cuts the  $x$  - *axis* (i.e. where  $y = 0$ ) is the point which must be included in your sign pattern.

If  $y = mx + c, m > 0$  then to right of this cutting point the  $y$  values are positive and to the left the  $y$  values are negative.

For example the line  $y = 3x + 3$  cuts the  $x$  - *axis* at  $-1$  so to the right of  $-1$  the  $y$  values are positive and to the left of  $-1$  the  $y$  values are negative.

For  $y = mx + c, m < 0$  for example  $y = -3x + 3$  we have that that this line cuts the  $x$  - *axis* at  $x = 1$  so to the right of 1 we have that the  $y$  values are negative and to the left the  $y$  values are positive (just the other way round as previous example).

B. Draw your **parabola** (rough work if you must):

Parabolas have a form  $y = ax^2 + bx + c$ . So you need to factorize them i.e.  $y = 2x^2 + 5x - 3 = (2x - 1)(x + 3)$ .

Then you work with these two straight lines separately in your sign pattern as in A.

For parabolas without real roots we have  $(b^2 - 4ac) < 0$ .

Thus the parabola cannot be factorize and never cuts the  $x$  - *axis*.

For example for  $y = x^2 + 4$  we have  $b = 0$  and  $b^2 - 4ac = -4 \cdot 1 \cdot 4 = -16 < 0$ .

So  $y = x^2 + 4$  cannot be factorize and never cuts the  $x - axis$ .  
 It is **always positive** (since  $a > 0$ ) and you **don't need to include** this parabola in your sign pattern.  
 For the parabola  $y = -2x^2 + 2x - 1$  we also have  
 $b^2 - 4ac = 4 - 4(-2)(-1) = -4 < 0$ , it cannot be factorized and  
 never cuts the  $x - axis$  but since  $a$  is **negative** we have a parabola  
 which is always negative and it **needs to be included in the sign pattern**.

C. You have also seen in the **example assignment 1** attached in additional resources how we had worked with  $\ln x$ .

D. What if we have the inverse of  $\ln x$  i.e  $e^x$  in your given function?  
 The first very important fact is that  $y = e^x$  is **ALWAYS positive** no matter what the values of  $x$  are.  
 For example the function  $f(x) = \frac{3x}{e^x}$  has a derivative

$$f'(x) = \frac{3e^x - 3xe^x}{e^{2x}} = \frac{3e^x(1 - x)}{e^{2x}} = \frac{3(1 - x)}{e^x}$$

after simplification. [Don't write for instance  $e^{-x}$  since we don't want negative powers. The derivative will still be correct with negative powers but the deductions cannot be made from such an equation.]

Here you **only** need to include  $y = 1 - x$  in the sign pattern.  
 Why? because both 3 and  $e^x$  are always positive and you may leave them out of the sign pattern.