

ASSIGNMENT 01
Graphs of functions, rates of change, optimization, L'Hôpital's rule
FIXED CLOSING DATE: 22 April 2022
Unique Number: 620664

1. Let f be the function defined by

$$f(x) = \frac{x^2}{(-2x+1)^2}.$$

- (a) Determine the vertical and horizontal asymptotes (show all limits).
(4)
- (b) Use the sign pattern for $f'(x)$ to determine
 - (i) the interval(s) over which f rises and where it falls; (4)
 - (ii) the local extrema. (2)
- (c) Use the sign pattern for $f''(x)$ to determine
 - (i) where the graph of f is concave up and where it is concave down.
(4)
 - (ii) the inflection points (if any) (2)

[16]

2. The volume of a cube is increasing at a rate of $1200 \text{ cm}^3/\text{min}$ at the moment the lengths of the sides are 20 cm . How fast are the lengths of the sides increasing at that moment?

[8]

3. Find the exact value of $\cos ec \left(\cos^{-1} \left(-\frac{\sqrt{3}}{2} \right) + \sin^{-1} \left(-\frac{\sqrt{3}}{2} \right) \right)$.

[6]

4. Use L'Hôpital's Rule to determine

(a) $\lim_{x \rightarrow 0^+} \left(\frac{1}{x} - \frac{2}{\ln(1+2x)} \right)$ (6)

(b) $\lim_{x \rightarrow \infty} \frac{\ln(\ln x)}{2x}$ (7)

(c) $\lim_{x \rightarrow \infty} \left(1 + \frac{1}{x} \right)^{2x}$ (7)

[20]

TOTAL: [50]