ICPC Templates For Africamonkey

Africamonkey

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1 莫队算法

1.1 普通莫队

```
struct Q { int 1, r, sqrt1, id; } q[N];
    int n, m, v[N], ans[N], nowans;
 3
    bool cmp(const Q &a, const Q &b) {
 4
        if (a.sqrtl != b.sqrtl) return a.sqrtl < b.sqrtl;</pre>
 5
        return a.r < b.r;</pre>
 6
 7
   void change(int x) { if (!v[x]) checkin(); else checkout(); }
 8
    int main() {
 9
        . . . . . .
10
        for (int i=1;i<=m;i++) q[i].sqrtl = q[i].l / sqrt(n), q[i].id = i;</pre>
11
        sort(q+1, q+m+1, cmp);
        int L=1,R=0; nowans=0;
12
        memset(v, 0, sizeof(v));
13
14
        for (int i=1;i<=m;i++) {</pre>
15
             while (L<q[i].l) change(L++);
16
             while (L>q[i].l) change (--L);
17
             while (R<q[i].r) change(++R);</pre>
18
             while (R>q[i].r) change(R--);
19
            ans[q[i].id] = nowans;
20
21
         . . . . . .
22
```

1.2 树上莫队

```
1 | struct Query { int l, r, id, l_group; } query[N];
  struct EDGE { int adj, next; } edge[N*2];
3
   int n, m, top, gh[N], c[N], reorder[N], deep[N], father[N], size[N], son[N], Top[N];
   void addedge(int x, int y) {
4
5
        edge[++top].adj = y;
6
        edge[top].next = gh[x];
7
        gh[x] = top;
8
   void dfs(int x, int root=0) {
10
        reorder[x] = ++top; father[x] = root; deep[x] = deep[root] + 1;
11
        son[x] = 0; size[x] = 1; int dd = 0;
12
        for (int p=gh[x]; p; p=edge[p].next)
13
            if (edge[p].adj != root) {
14
                dfs(edge[p].adj, x);
15
                if (size[edge[p].adj] > dd) {
16
                    son[x] = edge[p].adj;
17
                    dd = size[edge[p].adj];
18
19
                size[x] += size[edge[p].adj];
20
21
22
   void split(int x, int tp) {
23
        Top[x] = tp;
24
        if (son[x]) split(son[x], tp);
25
        for (int p=gh[x]; p; p=edge[p].next)
26
            if (edge[p].adj != father[x] && edge[p].adj != son[x])
```

```
27
                split(edge[p].adj, edge[p].adj);
28
29
   int lca(int x, int y) {
30
        int tx = Top[x], ty = Top[y];
31
        while (tx != ty) {
32
            if (deep[tx] < deep[ty]) {</pre>
33
                swap(tx, ty);
34
                swap(x, y);
35
36
            x = father[tx];
37
            tx = Top[x];
38
        if (deep[x] < deep[y]) swap(x, y);</pre>
39
40
        return y;
41
42
   bool cmp(const Query &a, const Query &b) {
43
        if (a.l_group != b.l_group) return a.l_group < b.l_group;</pre>
44
        return reorder[a.r] < reorder[b.r];</pre>
45
46 | int v[N], ans[N];
  void upd(int x) { if (!v[x]) checkin(); else checkout(); }
47
   void go(int &u, int taru, int v) {
        int lca0 = lca(u, taru);
49
50
       int lca1 = lca(u, v); upd(lca1);
51
       int lca2 = lca(taru, v); upd(lca2);
52
        for (int x=u; x!=lca0; x=father[x]) upd(x);
        for (int x=taru; x!=lca0; x=father[x]) upd(x);
53
54
        u = taru;
55
56
   int main() {
57
        memset(gh, 0, sizeof(gh));
58
        scanf("%d%d", &n, &m); top = 0;
59
        for (int i=1;i<n;i++) {</pre>
60
            int x,y; scanf("%d%d", &x, &y);
61
            addedge(x, y); addedge(y, x);
62
63
        top = 0; dfs(1); split(1, 1);
64
        for (int i=1;i<=m;i++) {</pre>
65
            if (reorder[query[i].l] > reorder[query[i].r])
66
                swap(query[i].l, query[i].r);
67
            query[i].id = i;
68
            query[i].l_group = reorder[query[i].l] / sqrt(n);
69
70
        sort(query+1, query+m+1, cmp);
71
        int L=1,R=1; upd(1);
72
        for (int i=1;i<=m;i++) {</pre>
73
            go(L, query[i].1,R);
74
            go(R, query[i].r,L);
75
            ans[query[i].id] = answer();
76
77
78
```

2 字符串

2.1 哈希

```
const int P=31, D=1000173169;
1
2
   int n, pow[N], f[N]; char a[N];
3
   int hash(int 1, int r) { return (LL)(f[r]-(LL)f[l-1]*pow[r-l+1]%D+D)%D; }
4
   int main() {
5
       scanf("%d%s", &n, a+1);
6
       pow[0] = 1;
7
       for (int i=1;i<=n;i++) pow[i] = (LL)pow[i-1]*P%D;</pre>
8
       for (int i=1;i<=n;i++) f[i] = (LL)((LL)f[i-1]*P+a[i])%D;</pre>
```

2.2 KMP

接口: int find_substring(char *pattern, char *text, int *next, int *ret);

输入: 模式串, 匹配串

输出: 返回值表示模式串在匹配串中出现的次数

KMP的next[i]表示从0到i的字符串s,前缀和后缀的最长重叠长度。

```
1
    void find_next(char *pattern, int *next) {
 2
        int n = strlen(pattern);
 3
        for (int i=1;i<n;i++) {</pre>
 4
             int j = i;
 5
             while (j > 0) {
 6
                 j = next[j];
 7
                 if (pattern[j] == pattern[i]) {
 8
                     next[i+1] = j+1;
 9
                     break;
10
11
             }
12
13
14
    int find_substring(char *pattern, char *text, int *next, int *ret) {
15
        find_next(pattern, next);
16
        int n = strlen(pattern);
17
        int m = strlen(text);
18
        int k = 0:
19
        for (int i=0, j=0; i<m; i++) {</pre>
20
             if (j<n && text[i] == pattern[j]) {</pre>
21
                 j++;
22
             } else {
23
                 while (j>0) {
24
                     j = next[j];
                     if (text[i] == pattern[j]) {
25
26
                          j++;
27
                          break;
28
29
                 }
30
31
             if (j == n)
                 ret[k++] = i-n+1;
32
33
34
        return k;
```

2.3 扩展KMP

接口: void ExtendedKMP(char *a, char *b, int *next, int *ret); 输出:

next: a 关于自己每个后缀的最长公共前缀ret: a 关于 b 的每个后缀的最长公共前缀

EXKMP的next[i]表示: 从i到n-1的字符串st前缀和原串前缀的最长重叠长度。

```
1
    void get_next(char *a, int *next) {
2
        int i, j, k;
        int n = strlen(a);
3
        for (j = 0; j+1<n && a[j]==a[j+1];j++);</pre>
 4
5
        next[1] = j;
6
        k = 1;
7
        for (i=2;i<n;i++) {</pre>
8
            int len = k+next[k], l = next[i-k];
            if (1 < len-i) {
9
10
                 next[i] = 1;
11
             } else {
12
                 for (j = max(0, len-i); i+j < n && a[j] == a[i+j]; j++);
13
                 next[i] = j;
14
                 k = i;
15
16
17
18
    void ExtendedKMP(char *a, char *b, int *next, int *ret) {
19
        get_next(a, next);
        int n = strlen(a), m = strlen(b);
20
21
        int i, j, k;
22
        for (j=0;j<n && j<m && a[j]==b[j];j++);</pre>
        ret[0] = j;
23
24
        k = 0;
25
        for (i=1;i<m;i++) {</pre>
26
            int len = k+ret[k], l = next[i-k];
27
            if (1 < len-i) {
28
                 ret[i] = 1;
29
             } else {
                 for (j = max(0, len-i); j<n && i+j<m && a[j]==b[i+j]; j++);</pre>
30
31
                 ret[i] = j;
32
                 k = i;
33
34
35
```

2.4 Manacher

p[i] 表示以 i 为对称轴的最长回文串长度

```
1
  char st[N*2], s[N];
2
  int len, p[N*2];
3
   while (scanf("%s", s) != EOF) {
4
        len = strlen(s);
5
        st[0] = '$', st[1] = '#';
6
        for (int i=1;i<=len;i++)</pre>
7
           st[i*2] = s[i-1], st[i*2+1] = '#';
8
9
        len = len * 2 + 2;
10
        int mx = 0, id = 0, ans = 0;
        for (int i=1;i<=len;i++) {</pre>
11
            p[i] = (mx > i) ? min(p[id*2-i]+1, mx-i) : 1;
12
13
            for (; st[i+p[i]] == st[i-p[i]]; ++p[i]);
14
            if (p[i]+i > mx) mx = p[i]+i, id = i;
15
           p[i] --;
16
            if (p[i] > ans) ans = p[i];
17
18
        printf("%d\n", ans);
19
```

2.5 最小表示法

```
1
    string smallestRepresation(string s) {
2
       int i, j, k, l;
3
        int n = s.length();
        s += s;
4
5
        for (i=0, j=1; j<n;) {</pre>
6
             for (k=0; k<n && s[i+k] == s[j+k]; k++);</pre>
7
             if (k>=n) break;
            if (s[i+k] <s[j+k]) j+=k+1;
8
9
             else {
10
                 l=i+k;
                 i=j;
11
12
                 j=\max(1, j)+1;
13
14
15
        return s.substr(i, n);
16
```

2.6 AC自动机

```
struct Node {
2
        int next[**Size of Alphabet**];
3
        int terminal, fail;
4
   } node[**Number of Nodes**];
5
   int top;
    void add(char *st) {
6
7
        int len = strlen(st), x = 1;
        for (int i=0;i<len;i++) {</pre>
8
            int ind = trans(st[i]);
9
10
            if (!node[x].next[ind])
11
                node[x].next[ind] = ++top;
12
            x = node[x].next[ind];
13
14
        node[x].terminal = 1;
15
16
   int q[**Number of Nodes**], head, tail;
17
    void build() {
18
        head = 0, tail = 1; q[1] = 1;
19
        while (head != tail) {
20
            int x = q[++head];
21
            /*(when necessary) node[x].terminal |= node[node[x].fail].terminal; */
22
            for (int i=0;i<n;i++)</pre>
23
                if (node[x].next[i]) {
24
                    if (x == 1) node[node[x].next[i]].fail = 1;
25
                    else {
26
                         int y = node[x].fail;
27
                         while (y) {
28
                             if (node[y].next[i]) {
29
                                 node[node[x].next[i]].fail = node[y].next[i];
30
31
32
                             y = node[y].fail;
33
34
                         if (!node[node[x].next[i]].fail) node[node[x].next[i]].fail = 1;
35
                    q[++tail] = node[x].next[i];
36
37
38
39
```

2.7 后缀数组

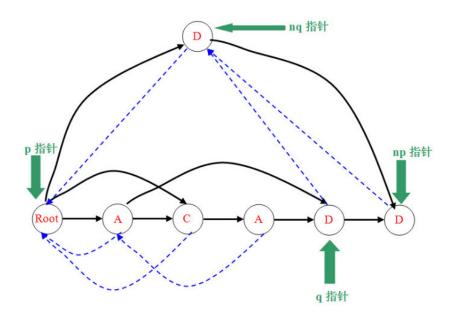
参数 m 表示字符集的大小, 即 $0 \le r_i < m$

```
1 #define rank rank2
2
   int n, r[N], wa[N], wb[N], ws[N], sa[N], rank[N], height[N];
   int cmp(int *r, int a, int b, int 1, int n)
4
5
        if (r[a]==r[b])
6
             if (a+l<n && b+l<n && r[a+l]==r[b+l])</pre>
7
8
                 return 1;
9
10
        return 0;
11
12
    void suffix_array(int m)
13
        int i, j, p, *x=wa, *y=wb, *t;
14
15
        for (i=0;i<m;i++) ws[i]=0;</pre>
16
        for (i=0;i<n;i++) ws[x[i]=r[i]]++;</pre>
17
        for (i=1;i<m;i++) ws[i]+=ws[i-1];</pre>
18
        for (i=n-1; i>=0; i--) sa[--ws[x[i]]]=i;
19
        for (j=1,p=1;p<n;m=p,j<<=1)</pre>
20
21
             for (p=0,i=n-j;i<n;i++) y[p++]=i;</pre>
22
             for (i=0;i<n;i++) if (sa[i]>=j) y[p++]=sa[i]-j;
23
             for (i=0;i<m;i++) ws[i]=0;</pre>
24
             for (i=0;i<n;i++) ws[x[y[i]]]++;</pre>
25
             for (i=1;i<m;i++) ws[i]+=ws[i-1];</pre>
26
             for (i=n-1;i>=0;i--) sa[--ws[x[y[i]]]]=y[i];
27
             for (t=x,x=y,y=t,x[sa[0]]=0,i=1,p=1;i<n;i++)</pre>
28
                 x[sa[i]] = cmp(y, sa[i-1], sa[i], j, n)?p-1:p++;
29
30
        for (i=0;i<n;i++) rank[sa[i]]=i;</pre>
31
32
    void calc_height()
33
34
        int j=0;
        for (int i=0;i<n;i++)</pre>
35
36
             if (rank[i])
37
38
                 while (r[i+j] == r[sa[rank[i]-1]+j]) j++;
39
                 height[rank[i]]=j;
40
                 if (j) j--;
41
42
```

2.8 后缀自动机

下面的代码是求两个串的LCS(最长公共子串)。

```
1 #include <cstdio>
2 #include <cstdlib>
3 #include <cstring>
4 #define N 500001
5 using namespace std;
6
   char st[N];
   int pre[N<<1], son[26][N<<1], step[N<<1], last, total;</pre>
7
   int apply(int x) { step[++total]=x; return total; }
9
   void Extend(char x) {
10
        int p = last, np = apply(step[last]+1);
11
        for (; p && !son[x][p]; p=pre[p]) son[x][p] = np;
12
        if (!p) pre[np] = 1;
13
        else {
14
           int q = son[x][p];
15
           if (step[p]+1 == step[q]) pre[np] = q;
16
17
                int nq = apply(step[p]+1);
18
                for (int i=0;i<26;i++) son[i][nq] = son[i][q];</pre>
19
                pre[nq] = pre[q];
20
               pre[q] = pre[np] = nq;
21
                for (; p && son[x][p]==q; p=pre[p]) son[x][p] = nq;
22
23
24
        last = np;
25
26
   void init() {
27
       last = total = 0;
28
       last = apply(0);
29
      scanf("%s",st);
30
       for (int i=0; st[i]; i++)
31
           Extend(st[i]-'a');
32
        scanf("%s",st);
33
34
   int main() {
35
       init();
36
        int p = 1, now = 0, ans = 0;
37
        for (int i=0; st[i]; i++) {
38
            int index = st[i]-'a';
39
            for (; p && !son[index][p]; p = pre[p], now = step[p]) ;
40
            if (!p) p = 1;
41
            if (son[index][p]) {
42
               p = son[index][p];
43
               now++;
44
                if (now > ans) ans = now;
45
46
        printf("%d\n",ans);
47
48
        return 0;
49
```



3 数据结构

3.1 ST表

```
int Log[N],f[17][N];
int ask(int x,int y) {
    int k=log[y-x+1];
    return max(f[k][x],f[k][y-(1<<k)+1]);
}
int main() {
    for(i=2;i<=n;i++)Log[i]=Log[i>>1]+1;
    for(j=1;j<K;j++)for(i=1;i+(1<<j-1)<=n;i++)f[j][i]=max(f[j-1][i],f[j-1][i+(1<<j-1)]);
}</pre>
```

3.2 线段树小技巧

给定一个序列 a , 寻找一个最大的 i 使得 $i \le y$ 且满足一些条件(如 $a[i] \ge w$, 那么需要在线段树维护 a 的区间最大值)

```
int queryl(int p, int left, int right, int y, int w) {
1
2
        if (right <= y) {
3
            if (! __condition__ ) return -1;
            else if (left == right) return left;
4
5
6
        int mid = (left + right) / 2;
        if (y <= mid) return queryl(p<<1|0, left, mid, y, w);</pre>
8
        int ret = queryl(p<<1|1, mid+1, right, y, w);</pre>
        if (ret != -1) return ret;
10
        return queryl(p<<1|0, left, mid, y, w);</pre>
11
```

给定一个序列 a , 寻找一个最小的 i 使得 $i \geq x$ 且满足一些条件(如 $a[i] \geq w$,那么需要在线段树维护 a 的区间最大值)

```
1
    int queryr(int p, int left, int right, int y, int w) {
2
        if (left >= x) {
3
            if (! __condition__ ) return -1;
            else if (left == right) return left;
4
5
6
        int mid = (left + right) / 2;
7
        if (x > mid) return queryr(p<<1|1, mid+1, right, y, w);
8
        int ret = queryr(p<<1|0, left, mid, y, w);</pre>
9
        if (ret != -1) return ret;
10
        return queryr(p<<1|1, mid+1, right, y, w);</pre>
11
```

3.3 Splay

接口:

ADD x y d: 将 [x,y] 的所有数加上 d

REVERSE x y : 将 [x,y] 翻转

INSERT x p: 将 p 插入到第 x 个数的后面

DEL x: 将第x个数删除

```
struct SPLAY {
1
2
         struct NODE {
3
              int w, min;
              int son[2], size, father, rev, lazy;
4
5
         } node[N];
 6
         int top, rt;
 7
         void pushdown(int x) {
              if (!x) return;
8
9
              if (node[x].rev) {
10
                   node[node[x].son[0]].rev ^= 1;
11
                   node[node[x].son[1]].rev ^= 1;
12
                   swap(node[x].son[0], node[x].son[1]);
13
                   node[x].rev = 0;
14
              if (node[x].lazy) {
15
16
                   node[node[x].son[0]].lazy += node[x].lazy;
17
                   node[node[x].son[1]].lazy += node[x].lazy;
18
                   node[x].w += node[x].lazy;
19
                   node[x].min += node[x].lazy;
20
                   node[x].lazy = 0;
21
22
23
         void pushup(int x) {
24
              if (!x) return;
25
              pushdown(node[x].son[0]);
26
              pushdown(node[x].son[1]);
27
              \verb|node[x].size = \verb|node[node[x].son[0]||.size + \verb|node[node[x].son[1]||.size + 1||;
28
              node[x].min = node[x].w;
29
              if (node[x].son[0]) node[x].min = min(node[x].min, node[node[x].son[0]].min);
30
               \textbf{if} \ (\texttt{node}[\texttt{x}].\texttt{son}[\texttt{1}]) \ \texttt{node}[\texttt{x}].\texttt{min} = \texttt{min}(\texttt{node}[\texttt{x}].\texttt{min}, \ \texttt{node}[\texttt{node}[\texttt{x}].\texttt{son}[\texttt{1}]].\texttt{min}); 
31
32
         void sc(int x, int y, int w) {
33
              node[x].son[w] = y;
              node[y].father = x;
34
```

```
35
            pushup(x);
36
37
        void _ins(int w) {
38
            top++;
39
            node[top].w = node[top].min = w;
40
            node[top].son[0] = node[top].son[1] = 0;
41
            node[top].size = 1; node[top].father = 0; node[top].rev = 0;
42
43
        void init() {
44
            top = 0;
45
            _{ins(0)}; _{ins(0)}; rt=1;
46
            sc(1, 2, 1);
47
48
        void rotate(int x) {
49
            if (!x) return;
50
            int y = node[x].father;
51
            int w = node[y].son[1] == x;
52
            sc(y, node[x].son[w^1], w);
53
            sc(node[y].father, x, node[node[y].father].son[1]==y);
54
            sc(x, y, w^1);
55
56
        int q[N];
57
        void flushdown(int x) {
            int t=0; for (; x; x=node[x].father) q[++t]=x;
58
59
            for (; t; t--) pushdown(q[t]);
60
        void Splay(int x, int root=0) {
61
62
            flushdown(x);
63
            while (node[x].father != root) {
64
                int y=node[x].father;
65
                int w=node[y].son[1]==x;
66
                if (node[y].father != root && node[node[y].father].son[w]==y) rotate(y);
67
                rotate(x);
68
69
70
        int find(int k) {
71
            Splay(rt);
72
            while (1) {
73
                pushdown(rt);
74
                if (node[node[rt].son[0]].size+1==k) {
75
                     Splay(rt);
76
                     return rt;
77
                 } else
                if (node[node[rt].son[0]].size+1<k) {</pre>
78
79
                     k-=node[node[rt].son[0]].size+1;
80
                     rt=node[rt].son[1];
81
                } else {
82
                    rt=node[rt].son[0];
83
84
            }
85
        int split(int x, int y) {
86
87
            int fx = find(x);
            int fy = find(y+2);
88
89
            Splay(fx);
90
            Splay(fy, fx);
91
            return node[fy].son[0];
```

```
92
 93
          void add(int x, int y, int d) { //add d to each number in a[x]...a[y]
94
              int t = split(x, y);
95
              node[t].lazy += d;
96
              Splay(t); rt=t;
97
          \textbf{void} \ \texttt{reverse}(\textbf{int} \ \texttt{x}, \ \textbf{int} \ \texttt{y}) \ \textit{\{ // reverse the x-th to y-th elements } \\
98
99
              int t = split(x, y);
100
              node[t].rev ^= 1;
101
              Splay(t); rt=t;
102
103
          void insert(int x, int p) { // insert p after the x-th element
104
              int fx = find(x+1);
105
              int fy = find(x+2);
106
              Splay(fx);
107
              Splay(fy, fx);
108
              _ins(p);
109
              sc(fy, top, 0);
110
              Splay(top); rt=top;
111
          void del(int x) { // delete the x-th element in Splay
112
113
              int fx = find(x), fy = find(x+2);
114
              Splay(fx); Splay(fy, fx);
115
              node[fy].son[0] = 0;
116
              Splay(fy); rt=fy;
117
118
     } tree;
```

3.4 可持久化Treap

接口:

```
void insert(int x, char c); 在当前第 x 个字符后插入 c void del(int x, int y); 删除第 x 个字符到第 y 个字符 void copy(int l, int r, int x); 复制第 l 个字符到第 r 个字符,然后粘贴到第 x 个字符后 void reverse(int x, int y); 翻转第 x 个到第 y 个字符 char query(int k); 表示询问当前第 x 个字符是什么
```

```
#define mod 1000000007
1
2
    struct Treap {
3
        struct Node {
4
            char key;
5
            bool reverse;
6
            int lc, rc, size;
7
        } node[N];
8
        int n, root, rd;
9
        int Rand() { rd = (rd * 20372052LL + 25022087LL) % mod; return rd; }
10
        void init() { n = root = 0; }
11
        inline int copy(int x) { node[++n] = node[x]; return n; }
12
        inline void pushdown(int x) {
13
            if (!node[x].reverse) return;
14
            if (node[x].lc) node[x].lc = copy(node[x].lc);
15
            if (node[x].rc) node[x].rc = copy(node[x].rc);
16
            swap(node[x].lc, node[x].rc);
17
            node[node[x].lc].reverse ^= 1;
18
            node[node[x].rc].reverse ^= 1;
19
            node[x].reverse = 0;
20
21
        inline void pushup(int x) { node[x].size = node[node[x].lc].size + node[node[x].rc].size
             + 1; }
22
        int merge(int u, int v) {
23
            if (!u || !v) return u+v;
24
            pushdown(u); pushdown(v);
25
            int t = Rand() % (node[u].size + node[v].size), r;
26
            if (t < node[u].size) {</pre>
27
                r = copy(u);
28
                node[r].rc = merge(node[u].rc, v);
29
            } else {
30
                r = copy(v);
                node[r].lc = merge(u, node[v].lc);
31
32
33
            pushup(r);
34
            return r;
35
36
        int split(int u, int x, int y) {
37
            if (x > y) return 0;
38
            pushdown(u);
39
            if (x == 1 && y == node[u].size) return u;
40
            if (y <= node[node[u].lc].size) return split(node[u].lc, x, y);</pre>
41
            int t = node[node[u].lc].size + 1;
42
            if (x > t) return split(node[u].rc, x-t, y-t);
43
            int num = copy(u);
44
            node[num].lc = split(node[u].lc, x, t-1);
45
            node[num].rc = split(node[u].rc, 1, y-t);
46
            pushup (num);
```

```
47
              return num;
48
49
         void insert(int x, char c) {
50
              int t1 = split(root, 1, x), t2 = split(root, x+1, node[root].size);
51
              node[++n].key = c; node[n].size = 1;
52
              root = merge(merge(t1, n), t2);
53
54
         void del(int x, int y) {
55
              int t1 = split(root, 1, x-1), t2 = split(root, y+1, node[root].size);
56
              root = merge(t1, t2);
57
         void copy(int 1, int r, int x) {
58
59
              \textbf{int} \ \texttt{t1} \ = \ \texttt{split}(\texttt{root}, \ \texttt{1}, \ \texttt{x}) \,, \ \texttt{t2} \ = \ \texttt{split}(\texttt{root}, \ \texttt{1}, \ \texttt{r}) \,, \ \texttt{t3} \ = \ \texttt{split}(\texttt{root}, \ \texttt{x+1}, \ \texttt{node}[\texttt{root}] \,.
60
              root = merge(merge(t1, t2), t3);
61
62
         void reverse(int x, int y) {
              int t1 = split(root, 1, x-1), t2 = split(root, x, y), t3 = split(root, y+1, node[root].
63
                   size);
              node[t2].reverse ^= 1;
64
              root = merge(merge(t1, t2), t3);
65
66
         char query(int k) {
67
68
              int x = root;
69
              while (1) {
70
                   pushdown(x);
                   if (k <= node[node[x].lc].size) x = node[x].lc;</pre>
71
72
                   else
73
                   if (k == node[node[x].lc].size + 1) return node[x].key;
74
75
                   k \rightarrow node[node[x].lc].size + 1, x = node[x].rc;
76
77
78
    } treap;
```

4 树

4.1 动态树

接口:

command(x, y): 将 x 到 y 路径的 Splay Tree 分离出来。 linkcut(u1, v1, u2, v2): 将树中原有的边 (u1, v1) 删除,加入一条新边 (u2, v2)

```
1
   struct DynamicTREE{
2
        struct NODE {
            int father, son[2], top, size, reverse;
3
4
        } splay[N];
5
        void init(int i, int fat) {
6
            splay[i].father = splay[i].son[0] = splay[i].son[1] = 0;
7
            splay[i].top = fat; splay[i].size = 1; splay[i].reverse = 0;
8
        void pushdown(int x) {
9
10
            if (!x) return;
11
            int s0 = splay[x].son[0], s1 = splay[x].son[1];
12
            if (splay[x].reverse) {
                splay[s0].reverse ^= 1;
13
                splay[s1].reverse ^= 1;
14
15
                swap(splay[x].son[0], splay[x].son[1]);
16
                splay[x].reverse = 0;
17
18
            s0 = splay[x].son[0], s1 = splay[x].son[1];
19
            splay[s0].top = splay[s1].top = splay[x].top;
20
21
        void pushup(int x) {
22
            if (!x) return;
23
            pushdown(splay[x].son[0]);
24
            pushdown(splay[x].son[1]);
25
            splay[x].size = splay[splay[x].son[0]].size + splay[splay[x].son[1]].size + 1;
26
27
        void sc(int x, int y, int w, bool Auto=true) {
28
            splay[x].son[w] = y;
29
            splay[y].father = x;
30
            if (Auto) {
31
                pushup(y);
32
                pushup(x);
33
34
35
        int top, tush[N];
36
        void flowdown(int x) {
37
            for (top=1; x; top++, x = splay[x].father) tush[top] = x;
38
            for (; top; top--) pushdown(tush[top]);
39
40
        void rotate(int x) {
41
            if (!x) return;
42
            int y = splay[x].father;
43
            int w = splay[y].son[1] == x;
44
            pushdown(y);
45
            pushdown(x);
46
            sc(splay[y].father, x, splay[splay[y].father].son[1]==y, false);
47
            sc(y, splay[x].son[w^1], w, false);
48
            sc(x, y, w^1, false);
49
            pushup(y);
```

```
50
             pushup(x);
51
52
         void Splay(int x, int rt=0) {
             if (!x) return;
53
54
             flowdown(x);
             while (splay[x].father != rt) {
55
56
                 int y = splay[x].father;
57
                 int w = splay[y].son[1]==x;
58
                 if (splay[y].father != rt && splay[splay[y].father].son[w] == y) rotate(y);
59
                 rotate(x);
60
61
62
         void split(int x) {
63
             int y = splay[x].son[1];
64
             if (!y) return;
65
             splay[y].father = 0;
66
             splay[x].son[1] = 0;
67
             splay[y].top = x;
68
             pushup(x);
69
70
         void access(int x) {
71
             int y = 0;
72
             while (x) {
73
                 Splay(x);
74
                 split(x);
75
                 sc(x, y, 1);
76
                 Splay(x);
77
                 y = x;
78
                 x = splay[x].top;
79
80
81
         void changeroot(int x) {
82
             access(x);
83
             Splay(x);
84
             splay[x].reverse = 1;
85
             Splay(x);
86
         void command(int x, int y, ...) {
87
88
            LL ans = 0;
89
             changeroot(x);
90
             access(y);
91
             Splay(x);
92
             //then you can modify the Splay Tree
93
94
         void linkcut(int u1, int v1, int u2, int v2) {
95
             changeroot (u1);
96
             access(v1);
97
             Splay(u1); split(u1);
98
             splay[v1].top = 0;
99
             access(u2); changeroot(u2);
100
             access(v2); changeroot(v2);
101
             Splay(u2); Splay(v2);
102
             splay[v2].top = u2;
103
104
    } lct;
```

5 图

5.1 欧拉回路

欧拉回路:

无向图:每个顶点的度数都是偶数,则存在欧拉回路。

有向图:每个顶点的入度 = 出度,则存在欧拉回路。

欧拉路径:

无向图: 当且仅当该图所有顶点的度数为偶数,或者除了两个度数为奇数外其余的全是偶数。

有向图: 当且仅当该图所有顶点出度 = 入度或者一个顶点出度 = 入度 + 1,另一个顶点入 度 = 出度 + 1,其他顶点出度 = 入度。 下面 O(n+m) 求欧拉回路的代码中, n 为点数, m 为边数,若有解则依次输出经过的边 的编号,若是无向图,则正数表示 x 到 y ,负数表示 y 到 x 。

```
1
    namespace UndirectedGraph{
 2
         int n,m,i,x,y,d[N],g[N],v[M<<1],w[M<<1],vis[M<<1],nxt[M<<1],ed;</pre>
 3
         int ans[M],cnt;
 4
         void add(int x,int y,int z) {
             d[x]++;
 5
 6
             v[++ed]=y;w[ed]=z;nxt[ed]=g[x];g[x]=ed;
 7
 8
         void dfs(int x) {
 9
             for (int&i=g[x];i;) {
10
                  if (vis[i]) {i=nxt[i];continue;}
11
                  vis[i]=vis[i^1]=1;
12
                  int j=w[i];
13
                  dfs(v[i]);
14
                  ans[++cnt]=j;
15
             }
16
17
         void solve(){
18
             scanf("%d%d",&n,&m);
19
             for (i=ed=1; i<=m; i++) scanf("%d%d", &x, &y), add(x, y, i), add(y, x, -i);</pre>
20
             for (i=1; i<=n; i++) if (d[i]&1) {puts("NO"); return; }</pre>
21
             for (i=1; i<=n; i++) if (q[i]) { dfs (i); break; }</pre>
22
             for (i=1; i<=n; i++) if (g[i]) {puts("NO"); return; }</pre>
23
             puts("YES");
24
             for(i=m;i;i--)printf("%d_",ans[i]);
25
26
27
    namespace DirectedGraph{
         int n, m, i, x, y, d[N], g[N], v[M], vis[M], nxt[M], ed;
28
29
         int ans[M],cnt;
30
         void add(int x,int y) {
31
             d[x]++;d[y]--;
32
             v[++ed] = y; nxt[ed] = g[x]; g[x] = ed;
33
         void dfs(int x) {
34
35
             for (int&i=g[x];i;) {
36
                  if(vis[i]){i=nxt[i];continue;}
37
                  vis[i]=1;
38
                  int j=i;
39
                  dfs(v[i]);
40
                  ans[++cnt]=j;
41
42
```

```
43
          void solve() {
44
               scanf("%d%d",&n,&m);
45
               for (i=1; i<=m; i++) scanf ("%d%d", &x, &y), add(x, y);</pre>
46
               for (i=1; i<=n; i++) if (d[i]) {puts("NO"); return; }</pre>
47
               for (i=1; i<=n; i++) if (q[i]) { dfs(i); break; }</pre>
48
               for (i=1; i<=n; i++) if (g[i]) {puts("NO"); return; }</pre>
49
               puts("YES");
50
               for (i=m; i; i--) printf("%d_", ans[i]);
51
52
```

5.2 最短路径

5.2.1 Dijkstra

```
1 #include <queue>
  using namespace std;
   struct EDGE { int adj, w, next; } edge[M*2];
   struct dat { int id, dist; dat(int id=0, int dist=0) : id(id), dist(dist) {} };
4
5
   struct cmp { bool operator () (const dat &a, const dat &b) { return a.dist > b.dist; } };
6
   priority_queue < dat, vector<dat>, cmp > q;
7
   int n, top, gh[N], v[N], dist[N];
8
   void addedge(int x, int y, int w) {
9
        edge[++top].adj = y;
10
        edge[top].w = w;
11
        edge[top].next = gh[x];
12
        gh[x] = top;
13
   int dijkstra(int s, int t) {
14
15
        memset(dist, 63, sizeof(dist));
        memset(v, 0, sizeof(v));
16
        dist[s] = 0;
17
18
        q.push(dat(s, 0));
19
        while (!q.empty()) {
            dat x = q.top(); q.pop();
20
21
            if (v[x.id]) continue; v[x.id] = 1;
22
            for (int p=gh[x.id]; p; p=edge[p].next) {
23
                if (x.dist + edge[p].w < dist[edge[p].adj]) {</pre>
24
                    dist[edge[p].adj] = x.dist + edge[p].w;
25
                    q.push(dat(edge[p].adj, dist[edge[p].adj]));
26
27
28
29
        return dist[t];
30
```

5.2.2 SPFA

```
struct EDGE { int adj, w, next; } edge[M*2];
int n,m,top,gh[N],v[N],cnt[N],q[N],dist[N],head,tail;

void addedge(int x, int y, int w) {
   edge[++top].adj = y;
   edge[top].w = w;
   edge[top].next = gh[x];
```

```
7
        gh[x] = top;
8
9
   int spfa(int S, int T) {
10
        memset(v, 0, sizeof(v));
11
        memset(cnt, 0, sizeof(cnt));
12
        memset(dist, 63, sizeof(dist));
        head = 0, tail = 1;
13
14
        dist[S] = 0; q[1] = S;
15
        while (head != tail) {
            (head += 1) %= N;
16
17
            int x = q[head]; v[x] = 0;
18
            ++cnt[x]; if (cnt[x] > n) return -1;
19
            for (int p=gh[x]; p; p=edge[p].next)
20
                if (dist[x] + edge[p].w < dist[edge[p].adj]) {</pre>
21
                     dist[edge[p].adj] = dist[x] + edge[p].w;
22
                     if (!v[edge[p].adj]) {
23
                         v[edge[p].adj] = 1;
24
                         (tail += 1) %= N;
25
                         q[tail] = edge[p].adj;
26
27
28
29
        return dist[T];
30
```

5.3 K 短路

接口:

kthsp::init(n): 初始化并设置节点个数为n kthsp::add(x, y, w): 添加一条x到y的有向边 kthsp::work(S, T, k): 求S到T的第k短路

```
1
    #include <queue>
2
   #define N 200020
3
4
   #define M 400020
   #define LOGM 20
5
   #define LL long long
6
7
   #define inf (1LL<<61)
9
   namespace pheap {
10
        struct Node {
11
            int next, son[2];
12
            LL val;
13
        } node[M*LOGM];
14
        int LOG[M];
15
        int root[M], size[M*LOGM], top;
16
        int add() {
17
            ++top; assert(top < M*LOGM);
            node[top].next = node[top].son[0] = node[top].son[1] = 0;
18
19
            node[top].val = inf;
20
            return top;
21
22
        int copy(int x) { int t = add(); node[t] = node[x]; return t; }
23
        void init() {
```

```
24
            top = -1; add();
25
            for (int i=2;i<M;i++) LOG[i] = LOG[i>>1] + 1;
26
27
        void upd(int x, int &next, LL &val) {
28
            if (val < node[x].val) {</pre>
29
                swap(val, node[x].val);
30
                swap(next, node[x].next);
31
32
33
        void insert(int x, int next, LL val) {
34
            int sz = size[root[x]] + 1;
35
            root[x] = copy(root[x]);
36
            size[root[x]] = sz; x = root[x];
37
            upd(x, next, val);
38
            for (int i=LOG[sz]-1;i>=0;i--) {
39
                int ind = (sz>>i)&1;
40
                node[x].son[ind] = copy(node[x].son[ind]);
41
                x = node[x].son[ind];
42
                upd(x, next, val);
43
44
45
    };
46
47
   namespace kthsp {
48
        using namespace pheap;
49
        struct EDGE {
            int adj, w, next;
50
51
        } edge[2][M];
52
        struct W {
53
            int x, y, w;
54
        } e[M];
55
        bool has_init = 0;
        int n, m, top[2], gh[2][N], v[N];
56
57
        LL dist[N];
58
        void init(int n1) {
59
           has_init = 1;
            n = n1; m = 0;
60
61
            memset(top, 0, sizeof(top));
62
            memset(qh, 0, sizeof(qh));
63
            for (int i=1;i<=n;i++) dist[i] = inf;</pre>
64
65
        void addedge(int id, int x, int y, int w) {
66
            edge[id][++top[id]].adj = y;
67
            edge[id][top[id]].w = w;
68
            edge[id][top[id]].next = gh[id][x];
69
            gh[id][x] = top[id];
70
71
        void add(int x, int y, int w) {
72
            assert(has_init);
73
            e[++m].x=x; e[m].y=y; e[m].w=w;
74
75
        int q[N], best[N], bestw[N];
76
        int deg[N];
77
        void spfa(int S) {
78
            for (int i=1;i<=n;i++) deg[i] = 0;</pre>
79
            for (int i=1;i<=m;i++) deg[e[i].x] ++;</pre>
80
            int head = 0, tail = 1;
```

```
81
             dist[S] = 0; q[1] = S;
82
             while (head != tail) {
83
                 (head += 1) %= N;
                 int x = q[head];
84
85
                 for (int p=gh[1][x]; p; p=edge[1][p].next) {
86
                      if (dist[x] + edge[1][p].w < dist[edge[1][p].adj]) {</pre>
87
                         dist[edge[1][p].adj] = dist[x] + edge[1][p].w;
                         best[edge[1][p].adj] = x;
88
89
                         bestw[edge[1][p].adj] = p;
90
91
                     if (!--deg[edge[1][p].adj]) {
92
                          (tail += 1) %= N;
93
                         q[tail] = edge[1][p].adj;
94
95
                 }
96
97
98
         void dfs(int x) {
99
             if (v[x]) return; v[x] = 1;
             if (best[x]) root[x] = root[best[x]];
100
101
             for (int p=gh[0][x]; p; p=edge[0][p].next)
102
                 if (dist[edge[0][p].adj] != inf && bestw[x] != p) {
                     insert(x, edge[0][p].adj, edge[0][p].w + dist[edge[0][p].adj] - dist[x]);
103
104
105
             for (int p=gh[1][x]; p; p=edge[1][p].next)
106
                 if (best[edge[1][p].adj] == x)
107
                     dfs(edge[1][p].adj);
108
109
         typedef pair<LL,int> pli;
110
         priority_queue <pli, vector<pli>, greater<pli> > pq;
111
         LL work(int S, int T, int k) {
112
             assert(has_init);
113
             n++; add(T, n, 0);
             if (S == T) k ++;
114
115
             T = n;
116
             for (int i=1;i<=m;i++) {</pre>
117
                 addedge(0, e[i].x, e[i].y, e[i].w);
118
                 addedge(1, e[i].y, e[i].x, e[i].w);
119
120
             spfa(T);
121
             root[T] = 0; pheap::init();
122
             memset(v, 0, sizeof(v));
123
             dfs(T);
124
             while (!pq.empty()) pq.pop();
125
             if (k == 1) return dist[S];
126
             if (root[S]) pq.push(make_pair(dist[S] + node[root[S]].val, root[S]));
127
             while (k--) {
128
                 if (pq.empty()) return inf;
                 pli now = pq.top(); pq.pop();
129
130
                 if (k == 1) return now.first;
131
                 int x = node[now.second].next, u = node[now.second].son[0], v = node[now.second].
                      son[1];
132
                 if (root[x]) pq.push(make_pair(now.first + node[root[x]].val, root[x]));
133
                 if (u) pq.push(make_pair(now.first - node[now.second].val + node[u].val, u));
134
                 if (v) pq.push(make_pair(now.first - node[now.second].val + node[v].val, v));
135
136
             return 0;
```

```
137 } 138 };
```

5.4 Tarjan

割点的判断:一个顶点 u 是割点,当且仅当满足 (1) 或 (2):

- (1) u 为树根,且 u 有多于一个子树
- (2) u 不为树根,且满足存在 (u,v) 为树枝边(u 为 v 的父亲),使得 $dfn[u] \leq low[v]$ 桥的判断: 一条无向边 (u,v) 是桥,当且仅当 (u,v) 为树枝边,满足 dfn[u] < low[v]

```
1
    struct EDGE { int adj, next; } edge[M];
2
    int n, m, top, gh[N];
    \textbf{int} \ dfn[N], \ low[N], \ cnt, \ ind, \ stop, \ instack[N], \ stack[N], \ belong[N];
3
 4
    void addedge(int x, int y) {
5
        edge[++top].adj = y;
        edge[top].next = gh[x];
6
7
        gh[x] = top;
8
9
    void tarjan(int x) {
10
        dfn[x] = low[x] = ++ind;
11
        instack[x] = 1; stack[++stop] = x;
12
        for (int p=gh[x]; p; p=edge[p].next)
            if (!dfn[edge[p].adj]) {
13
14
                 tarjan(edge[p].adj);
15
                 low[x] = min(low[x], low[edge[p].adj]);
16
             } else if (instack[edge[p].adj]) {
17
                 low[x] = min(low[x], dfn[edge[p].adj]);
18
19
        if (dfn[x] == low[x]) {
20
            ++cnt; int tmp=0;
21
            while (tmp!=x) {
22
                 tmp = stack[stop--];
23
                 belong[tmp] = cnt;
24
                 instack[tmp] = 0;
25
26
27
```

5.5 统治者树 (Dominator Tree)

Dominator Tree 可以解决判断一类有向图必经点的问题。

idom[x] 表示离 x 最近的必经点(重编号后)。将 idom[x] 作为 x 的父亲,构成一棵 Dominator Tree 接口:

void dominator::init(int n); 初始化,有向图节点数为 n void dominator::addedge(int u, int v); 添加一条有向边 (u, v) void dominator::work(int root); 以 root 为根,建立一棵 Dominator Tree 结果的返回:

在执行 dominator::work(int root); 后, 树边保存在 vector jint; tree[N] 中

```
namespace dominator {
    vector <int> g[N], rg[N], bucket[N], tree[N];
    int n, ind, idom[N], sdom[N], dfn[N], dsu[N], father[N], label[N], rev[N];
    void dfs(int x) {
```

```
5
            ++ind;
6
            dfn[x] = ind; rev[ind] = x;
7
            label[ind] = dsu[ind] = sdom[ind] = ind;
8
            for (auto p : g[x]) {
9
                if (!dfn[p]) dfs(p), father[dfn[p]] = dfn[x];
10
                rg[dfn[p]].push_back(dfn[x]);
11
12
13
        void init(int n1) {
            n = n1; ind = 0;
14
            for (int i = 1; i <= n; ++i) {</pre>
15
16
                g[i].clear();
17
                rg[i].clear();
18
                bucket[i].clear();
19
                tree[i].clear();
20
                dfn[i] = 0;
21
            }
22
23
        void addedge(int u, int v) {
24
            g[u].push_back(v);
25
26
        int find(int x, int step=0) {
27
            if (dsu[x] == x) return step ? -1 : x;
28
            int y = find(dsu[x], 1);
29
            if (y < 0) return x;
30
            if (sdom[label[dsu[x]]] < sdom[label[x]])</pre>
31
                label[x] = label[dsu[x]];
32
            dsu[x] = y;
33
            return step ? dsu[x] : label[x];
34
35
        void work(int root) {
36
            dfs(root); n = ind;
37
            for (int i = n; i; --i) {
                for (auto p : rg[i])
38
39
                    sdom[i] = min(sdom[i], sdom[find(p)]);
40
                if (i > 1) bucket[sdom[i]].push_back(i);
41
                for (auto p : bucket[i]) {
42
                    int u = find(p);
43
                    if (sdom[p] == sdom[u]) idom[p] = sdom[p];
44
                    else idom[p] = u;
45
46
                if (i > 1) dsu[i] = father[i];
47
            for (int i = 2; i <= n; ++i) {</pre>
48
49
                if (idom[i] != sdom[i])
                    idom[i] = idom[idom[i]];
50
51
                tree[rev[i]].push_back(rev[idom[i]]);
52
                tree[rev[idom[i]]].push_back(rev[i]);
53
54
```

5.6 网络流

5.6.1 最大流

```
1
   struct EDGE { int adj, w, next; } edge[M];
2
   int n, top, gh[N], nrl[N];
3
   void addedge(int x, int y, int w) {
4
        edge[++top].adj = y;
5
        edge[top].w = w;
6
       edge[top].next = gh[x];
7
        gh[x] = top;
8
        edge[++top].adj = x;
        edge[top].w = 0;
10
        edge[top].next = gh[y];
11
        gh[y] = top;
12
13
   int dist[N], q[N];
14
   int bfs() {
       memset(dist, 0, sizeof(dist));
16
        q[1] = S; int head = 0, tail = 1; dist[S] = 1;
17
        while (head != tail) {
18
            int x = q[++head];
19
            for (int p=gh[x]; p; p=edge[p].next)
20
                if (edge[p].w && !dist[edge[p].adj]) {
21
                    dist[edge[p].adj] = dist[x] + 1;
22
                    q[++tail] = edge[p].adj;
23
24
25
        return dist[T];
26
   int dinic(int x, int delta) {
27
28
        if (x==T) return delta;
29
        for (int& p=nrl[x]; p && delta; p=edge[p].next)
            if (edge[p].w \&\& dist[x]+1 == dist[edge[p].adj]) {
30
31
                int dd = dinic(edge[p].adj, min(delta, edge[p].w));
32
                if (!dd) continue;
33
                edge[p].w -= dd;
34
                edge[p^1].w += dd;
35
                return dd;
36
37
        return 0;
38
39
   int work() {
40
        int ans = 0;
41
        while (bfs()) {
42
           memcpy(nrl, qh, sizeof(qh));
            int t; while (t = dinic(S, inf)) ans += t;
43
44
45
        return ans;
46
```

5.6.2 上下界有源汇网络流

T 向 S 连容量为正无穷的边,将有源汇转化为无源汇。

每条边容量减去下界,设 in[i] 表示流入 i 的下界之和减去流出 i 的下界之和。

新建超级源汇 SS,TT ,对于 in[i]>0 的点, SS 向 i 连容量为 in[i] 的边。对于 in[i]<0 的点, i 向 TT 连容量为 -in[i] 的边。

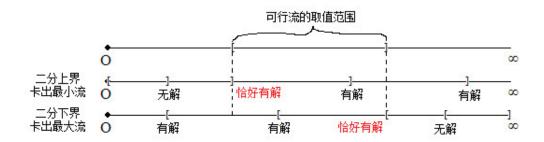
求出以 SS,TT 为源汇的最大流,如果等于 $\Sigma in[i](in[i]>0)$,则存在可行流。再求出 S,T 为源汇的最

大流即为最大流。

费用流: 建完图后等价于求以 SS,TT 为源汇的费用流。

5.6.3 上下界无源汇网络流

- 1. 怎样求无源汇有上下界网络的可行流?
- 由于有源汇的网络我们先要转化成无源汇,所以本来就无源汇的网络不用再作特殊处理。
- 2. 怎样求无源汇有上下界网络的最大流、最小流?
- 一种简易的方法是采用二分的思想,不断通过可行流的存在与否对 (t,s) 边的上下界 U,L 进行调整。求最大流时令 $U=\infty$ 并二分 L ; 求最小流时令 L=0 并二分 U 。道理很简单,因为可行流的取值范围是一段连续的区间,我们只要通过二分找到有解和无解的分界线即可。



5.6.4 费用流

```
1
    #define inf 0x3f3f3f3f
2
    struct NetWorkFlow {
3
        struct EDGE {
4
            int adj, w, cost, next;
5
        } edge[M*2];
6
        int gh[N], q[N], dist[N], v[N], pre[N], prev[N], top;
7
8
        void addedge(int x, int y, int w, int cost) {
9
            edge[++top].adj = y;
10
            edge[top].w = w;
11
            edge[top].cost = cost;
12
            edge[top].next = gh[x];
13
            gh[x] = top;
            edge[++top].adj = x;
14
15
            edge[top].w = 0;
16
            edge[top].cost = -cost;
17
            edge[top].next = gh[y];
18
            gh[y] = top;
19
20
        void clear() {
21
            top = 1;
22
            memset(gh, 0, sizeof(gh));
23
24
        int spfa() {
25
            memset(dist, 63, sizeof(dist));
26
            memset(v, 0, sizeof(v));
```

```
27
            int head = 0, tail = 1;
28
            q[1] = S; v[S] = 1; dist[S] = 0;
29
            while (head != tail) {
30
                 (head += 1) %= N;
31
                int x = q[head];
32
                v[x] = 0;
33
                for (int p=gh[x]; p; p=edge[p].next)
34
                     if (edge[p].w && dist[x] + edge[p].cost < dist[edge[p].adj]) {</pre>
35
                         dist[edge[p].adj] = dist[x] + edge[p].cost;
36
                         pre[edge[p].adj] = x;
37
                         prev[edge[p].adj] = p;
38
                         if (!v[edge[p].adj]) {
39
                             v[edge[p].adj] = 1;
                             (tail += 1) %= N;
40
41
                             q[tail] = edge[p].adj;
42
43
                     }
44
45
            return dist[T] != inf;
46
        int work() {
47
48
            int ans = 0;
            while (spfa()) {
49
50
                int mx = inf;
51
                for (int x=T; x!=S; x=pre[x])
52
                     mx = min(edge[prev[x]].w, mx);
53
                ans += dist[T] * mx;
54
                 for (int x=T;x!=S;x=pre[x]) {
55
                     edge[prev[x]].w -= mx;
56
                     edge[prev[x]^1].w += mx;
57
58
59
            return ans;
60
61
    } nwf;
```

5.6.5 zkw费用流

```
#define inf 0x3f3f3f3f
2
   struct NetWorkFlow {
3
        struct EDGE {
4
            int adj, w, cost, next;
5
        } edge[M*2];
6
        int gh[N], top;
7
        int S, T;
8
        void addedge(int x, int y, int w, int cost) {
9
            edge[++top].adj = y;
10
            edge[top].w = w;
11
            edge[top].cost = cost;
12
            edge[top].next = gh[x];
13
            gh[x] = top;
14
            edge[++top].adj = x;
15
            edge[top].w = 0;
16
            edge[top].cost = -cost;
17
            edge[top].next = gh[y];
18
            gh[y] = top;
```

```
19
20
        void clear() {
21
            top = 1;
22
            memset(gh, 0, sizeof(gh));
23
24
        int cost, d[N], slk[N], v[N];
25
        int aug(int x, int f) {
            int left = f;
26
27
            if (x == T) {
28
                cost += f * d[S];
29
                return f;
31
            v[x] = true;
32
            for (int p=gh[x]; p; p=edge[p].next)
33
                if (edge[p].w && !v[edge[p].adj]) {
34
                     int t = d[edge[p].adj] + edge[p].cost - d[x];
35
                     if (t == 0) {
36
                         int delt = aug(edge[p].adj, min(left, edge[p].w));
37
                         if (delt > 0) {
38
                             edge[p].w -= delt;
39
                             edge[p^1].w += delt;
40
                             left -= delt;
41
42
                         if (left == 0) return f;
43
                     } else {
44
                     if (t < slk[edge[p].adj])</pre>
45
                         slk[edge[p].adj] = t;
46
47
48
            return f-left;
49
50
        bool modlabel() {
51
            int delt = inf;
52
            for (int i=1;i<=T;i++)</pre>
53
                if (!v[i]) {
54
                    if (slk[i] < delt) delt = slk[i];</pre>
                    slk[i] = inf;
55
56
57
            if (delt == inf) return true;
            for (int i=1;i<=T;i++)</pre>
58
59
                if (v[i]) d[i] += delt;
60
            return false;
61
62
        int work() {
63
            cost = 0;
64
            memset(d, 0, sizeof(d));
            memset(slk, 63, sizeof(slk));
65
66
            do {
67
                do {
68
                    memset(v, 0, sizeof(v));
                 } while (aug(S, inf));
69
            } while (!modlabel());
71
            return cost;
72
    } nwf;
```

6 数学

6.1 扩展欧几里得解同余方程

ans[] 保存的是循环节内所有的解

```
1
    int exgcd(int a,int b,int&x,int&y) {
2
         if(!b)return x=1,y=0,a;
3
         int d=exgcd(b,a%b,x,y),t=x;
4
         return x=y,y=t-a/b*y,d;
5
 6
    void cal(ll a,ll b,ll n){//ax=b(mod n)
 7
        11 x, y, d=exgcd(a, n, x, y);
        if (b%d) return;
8
9
         x=(x%n+n)%n;
10
         ans [cnt=1]=x*(b/d)%(n/d);
11
         for (ll i=1; i < d; i++) ans [++cnt] = (ans [1] + i * n/d) %n;</pre>
12
```

6.2 同余方程组

```
1
    int n,flag,k,m,a,r,d,x,y;
2
    int main(){
3
        scanf("%d",&n);
 4
        flag=k=1, m=0;
        while (n--) {
5
 6
            scanf("%d%d",&a,&r);//ans%a=r
 7
            if(flag){
 8
                 d=exgcd(k,a,x,y);
9
                if((r-m)%d) {flag=0;continue;}
10
                 x = (x*(r-m)/d+a/d) % (a/d), y=k/d*a, m= ((x*k+m) %y) %y;
11
                 if (m<0) m+=y;
12
                 k=y;
13
            }
14
15
        printf("%d",flag?m:-1);//若flag说明有解解为=1,,ki+m,为任意整数i
16
```

6.3 卡特兰数

```
h_1=1, h_n=rac{h_{n-1}(4n-2)}{n+1}=rac{C(2n,n)}{n+1}=C(2n,n)-C(2n,n-1) 在一个格点阵列中,从 (0,0) 点走到 (n,m) 点且不经过对角线 x=y 的方案数 (x>y):C(n+m-1,m)-C(n+m-1,m-1) 在一个格点阵列中,从 (0,0) 点走到 (n,m) 点且不穿过对角线 x=y 的方案数 (x\geq y):C(n+m,m)-C(n+m,m-1)
```

6.4 Lucas定理

```
接口:
初始化: void lucas::init();
计算 C(n,m)\%mod 的值: LL lucas::Lucas(LL n, LL m);
```

```
1
    #define mod 110119
2
    #define LL long long
3
   namespace lucas {
        LL fac[mod+1], facv[mod+1];
4
5
        LL power(LL base, LL times) {
6
            LL ans = 1;
7
            while (times) {
8
                if (times&1) (ans *= base) %= mod;
9
                (base *= base) %= mod;
10
                times >>= 1;
11
12
            return ans;
13
        void init() {
14
15
            fac[0] = 1; for (int i=1; i < mod; i++) fac[i] = (fac[i-1] * i) % mod;
16
            facv[mod-1] = power(fac[mod-1], mod-2);
17
18
        LL C(unsigned LL n, unsigned LL m) {
19
            if (n < m) return 0;</pre>
20
            return (fac[n] * facv[m] % mod * facv[n-m] % mod) % mod;
21
22
        LL Lucas(unsigned LL n, unsigned LL m)
23
24
            if (m == 0) return 1;
25
            return (C(n%mod, m%mod) * Lucas(n/mod, m/mod)) %mod;
26
27
   };
```

6.5 高斯消元

6.5.1 行列式

```
1
   int ans = 1;
2
    for (int i=0;i<n;i++) {</pre>
3
         for (int j=i; j<n; j++)</pre>
4
             if (g[j][i]) {
5
                  for (int k=i; k<n; k++)</pre>
6
                       swap(g[i][k], g[j][k]);
7
                  if (j != i) ans \star = -1;
8
                  break;
9
10
         if (g[i][i] == 0) {
11
             ans = 0;
12
             break;
13
14
         for (int j=i+1; j<n; j++) {</pre>
15
             while (g[j][i]) {
16
                  int t = g[i][i] / g[j][i];
17
                  for (int k=i; k<n; k++)</pre>
18
                       g[i][k] = (g[i][k] + mod - ((LL)t * g[j][k] % mod)) % mod;
19
                  for (int k=i; k<n; k++)</pre>
20
                      swap(g[i][k], g[j][k]);
21
                  ans \star = -1;
22
23
```

```
24 }
25 for (int i=0; i < n; i++)
26 ans = ((LL) ans * g[i][i]) % mod;
27 ans = (ans % mod + mod) % mod;
28 printf("%d\n", ans);
```

6.5.2 Matrix-Tree定理

对于一张图,建立矩阵 C , C[i][i]=i 的度数,若 i,j 之间有边,那么 C[i][j]=-1 ,否则为 0 。这张图的生成树个数等于矩阵 C 的 n-1 阶行列式的值。

6.6 调和级数

 $\sum\limits_{i=1}^{n} \frac{1}{i}$ 在 n 较大时约等于 ln(n)+r , r 为欧拉常数,约等于 0.5772156649015328 。

6.7 曼哈顿距离的变换

```
|x_1 - x_2| + |y_1 - y_2| = max(|(x_1 + y_1) - (x_2 + y_2)|, |(x_1 - y_1) - (x_2 - y_2)|)
```

6.8 线性筛素数

```
mu[1]=phi[1]=1;top=0;
2
   for (int i=2;i<N;i++) {</pre>
3
        if (!v[i]) prime[++top]=i, mu[i] = -1, phi[i] = i-1;
4
        for (int j=1;i*prime[j] <N && j<=top; j++) {</pre>
5
            v[i*prime[j]] = 1;
6
            if (i%prime[j]) {
7
                mu[i*prime[j]] = -mu[i];
8
                phi[i*prime[j]] = phi[i] * (prime[j]-1);
9
            } else {
10
                mu[i*prime[j]] = 0;
11
                phi[i*prime[j]] = phi[i] * prime[j];
12
                break;
13
14
15
```

6.9 FFT

```
1
    typedef complex<double> comp;
2
    namespace FFT {
3
        comp A[N], B[N], omega[N];
4
        void transform(comp *x, int len) {
5
             for (int i=1, j=len/2; i<len-1; i++) {</pre>
6
                 if (i<j) swap(x[i], x[j]);</pre>
7
                 int k = len/2;
8
                 while (j>=k) {
9
                      j-=k;
10
                      k/=2;
11
                 if (j<k) j+=k;
12
```

```
13
14
15
         void fft(comp *x, int len, int reverse) {
16
            transform(x, len);
17
             for (int h=2;h<=len;h<<=1) {</pre>
18
                 for (int i=0;i<h/2;i++) omega[i] = polar(1.0, 2*pi*reverse/h*i);</pre>
19
                 for (int i=0;i<len;i+=h) {</pre>
20
                      for (int j=i; j<i+h/2; j++) {</pre>
21
                          comp w = omega[j-i];
22
                          comp u = x[j];
23
                          comp v = (w * x[j+h/2]);
24
                          x[j] = u + v;
25
                          x[j+h/2] = u - v;
26
27
                 }
28
29
             if (reverse == -1) {
                 for (int i=0;i<len;i++)</pre>
30
31
                     x[i] /= len;
32
33
34
        void work(int n, int *a, int *b) {
35
             int len = 1;
36
             while (len <= n*2) len *= 2;
37
             for (int i=0;i<len;i++) A[i] = B[i] = 0;</pre>
38
             for (int i=0;i<n;i++) A[i] = a[i], B[i] = b[i];</pre>
             fft(A, len, 1); fft(B, len, 1);
39
40
             for (int i=0;i<len;i++) A[i] = A[i] * B[i];</pre>
41
             fft(A, len, -1);
42
             for (int i=0;i<len;i++) {</pre>
43
                 LL r = round(A[i].real());
44
                 a[i] = r % mod;
45
46
47
    };
```

6.10 求原根

```
接口: LL p_root(LL p);
输入: 一个素数 p
输出: p 的原根
```

```
1 #include <bits/stdc++.h>
2
   #define LL long long
3
4
   using namespace std;
5
6
   vector <LL> a;
8
   LL pow_mod(LL base, LL times, LL mod) {
9
       LL ret = 1;
10
       while (times) {
11
           if (times&1) ret = ret * base % mod;
           base = base * base % mod;
12
13
           times>>=1;
14
       }
```

```
15
        return ret;
16
17
18
   bool g_test(LL g, LL p) {
19
        for (LL i = 0; i < a.size(); ++i)</pre>
20
            if (pow_mod(g, (p-1)/a[i], p) == 1) return 0;
21
        return 1;
22
23
24
   LL p_root(LL p) {
25
       LL tmp = p - 1;
        for (LL i = 2; i <= tmp / i; ++i)</pre>
27
            if (tmp % i == 0) {
28
                a.push_back(i);
29
                 while (tmp % i == 0)
30
                    tmp /= i;
31
            }
32
        if (tmp != 1) a.push_back(tmp);
        LL g = 1;
33
34
        while (1) {
35
            if (g_test(g, p)) return g;
36
            ++q;
37
38
   }
39
40
   int main() {
41
        LL p;
42
        cin >> p;
43
        cout << p_root(p) << endl;</pre>
44
```

6.11 NTT

998244353 原根为 3 , 1004535809 原根为 3 , 786433 原根为 10 , 880803841 原根为 26 。

```
1 #define mod 998244353
2 #define g 3
   LL wi[N], wiv[N];
4
   LL power(LL base, LL times) {
5
       LL ans = 1;
6
        while (times) {
7
            if (times&1) (ans *= base) %= mod;
8
            (base *= base) %= mod;
9
            times >>= 1;
10
11
        return ans;
12
    void transform(LL *x, int len) {
13
14
        for (int i=1, j=len/2; i<len-1; i++) {</pre>
15
            if (i<j) swap(x[i], x[j]);</pre>
16
            int k = len/2;
17
            while (\dot{j}>=k) {
                 j−=k;
18
19
                 k/=2;
20
21
            if (j<k) j+=k;
```

```
22
23
24
    void NTT(LL *x, int len, int reverse) {
25
        transform(x, len);
26
        for (int h=2;h<=len;h<<=1) {</pre>
27
             for (int i=0;i<len;i+=h) {</pre>
28
                 LL w = 1, wn;
29
                 if (reverse==1) wn = wi[h]; else wn = wiv[h];
30
                 for (int j=i; j<i+h/2; j++) {</pre>
                     LL u = x[j];
31
32
                     LL v = (w * x[j+h/2]) % mod;
33
                     x[j] = (u + v) % mod;
                     x[j+h/2] = (u - v + mod) % mod;
34
                     (w *= wn) %= mod;
35
36
37
38
39
        if (reverse == -1) {
40
            LL t = power(len, mod-2);
             for (int i=0;i<len;i++)</pre>
41
                 (x[i] *= t) %= mod;
42
43
44
45
    LL A[N], B[N];
46
    int main() {
47
        for (int i=1;i<N;i*=2) {</pre>
48
            wi[i] = power(g, (mod-1)/i);
49
            wiv[i] = power(wi[i], mod-2);
50
51
        memset(A, 0, sizeof(A));
        memset(B, 0, sizeof(B));
52
53
        NTT(A, len, 1); NTT(B, len, 1);
54
        for (int i=0;i<len;i++) (A[i] *= B[i]) %= mod;</pre>
        NTT(A, len, -1);
55
56
```

6.12 组合数 lcm

(n+1)lcm(C(n,0),C(n,1),...,C(n,k)) = lcm(n+1,n,n-1,...,n-k+1)

6.13 区间 lcm 的维护

对于一个数,将其分解质因数,若有因子 p^k ,那么拆分出 k 个数 $p,p^2,...,p^k$,权值都为 p ,那么查询区间 [l,r] 内所有数的 lcm 的答案 = 所有在该区间中出现过的数的权值之积,可持久化线段树维护即可。

7 几何

7.1 凸包

```
typedef complex<int> point;
   #define X real()
   #define Y imag()
  int n;
4
   long long cross(point a, point b) {
        return 111 * a.X * b.Y - 111 * a.Y * b.X;
6
7
8
   bool cmp(point a, point b) {
9
        return make_pair(a.X, a.Y) < make_pair(b.X, b.Y);</pre>
10
11
   int convexHull(point p[],int n,point ch[]) {
12
        sort(p, p + n, cmp);
13
        int m = 0;
14
        for(int i = 0; i < n; ++i) {</pre>
15
            while (m > 1 \&\& cross(ch[m-1] - ch[m-2], p[i] - ch[m-2]) <= 0) m--;
16
            ch[m++] = p[i];
17
18
        int k = m;
        for(int i = n - 2; i >= 0; --i) {
19
            while (m > k \&\& cross(ch[m-1] - ch[m-2], p[i] - ch[m-2]) <= 0) m--;
20
21
            ch[m++] = p[i];
22
23
        if(n > 1) m--;
24
        return m;
25
```

8 黑科技和杂项

8.1 高精度计算

```
#include<algorithm>
   using namespace std;
3
   const int N_huge=850,base=100000000;
4
   char s[N_huge*10];
   struct huge {
6
        typedef long long value;
7
        value a[N_huge];int len;
8
        void clear() {len=1;a[len]=0;}
9
        huge(){clear();}
10
        huge(value x) {*this=x;}
11
        huge operator = (huge b) {
12
            len=b.len;for (int i=1;i<=len;++i)a[i]=b.a[i]; return *this;</pre>
13
14
        huge operator +(huge b) {
15
            int L=len>b.len?len:b.len;huge tmp;
16
            for (int i=1;i<=L+1;++i)tmp.a[i]=0;</pre>
17
            for (int i=1;i<=L;++i) {</pre>
18
                if (i>len)tmp.a[i]+=b.a[i];
19
                else if (i>b.len)tmp.a[i]+=a[i];
20
                else {
```

```
21
                     tmp.a[i]+=a[i]+b.a[i];
22
                      if (tmp.a[i]>=base) {
23
                          tmp.a[i]-=base;++tmp.a[i+1];
24
25
                 }
26
27
             if (tmp.a[L+1])tmp.len=L+1;
28
                 else tmp.len=L;
29
            return tmp;
30
31
        huge operator - (huge b) {
32
            int L=len>b.len?len:b.len;huge tmp;
33
             for (int i=1;i<=L+1;++i)tmp.a[i]=0;</pre>
34
             for (int i=1;i<=L;++i) {</pre>
35
                 if (i>b.len)b.a[i]=0;
36
                 tmp.a[i]+=a[i]-b.a[i];
37
                 if (tmp.a[i]<0) {</pre>
38
                     tmp.a[i]+=base;--tmp.a[i+1];
39
40
             while (L>1&&!tmp.a[L])--L;
41
42
             tmp.len=L;
43
             return tmp;
44
45
        huge operator *(huge b) {
46
            int L=len+b.len;huge tmp;
47
             for (int i=1;i<=L;++i)tmp.a[i]=0;</pre>
48
             for (int i=1;i<=len;++i)</pre>
49
                 for (int j=1; j<=b.len; ++j) {</pre>
50
                     tmp.a[i+j-1]+=a[i]*b.a[j];
51
                     if (tmp.a[i+j-1] >= base) {
52
                          tmp.a[i+j] += tmp.a[i+j-1]/base;
53
                          tmp.a[i+j-1]%=base;
54
55
56
             tmp.len=len+b.len;
             while (tmp.len>1&&!tmp.a[tmp.len])--tmp.len;
57
58
             return tmp;
59
60
        pair<huge, huge> divide(huge a, huge b) {
61
             int L=a.len;huge c,d;
62
             for (int i=L;i;--i) {
63
            c.a[i]=0;d=d*base;d.a[1]=a.a[i];
64
                 int l=0,r=base-1,mid;
65
                 while (1<r) {
66
                     mid=(1+r+1)>>1;
67
                     if (b*mid<=d)l=mid;</pre>
68
                          else r=mid-1;
69
70
                 c.a[i]=1;d-=b*1;
71
72
             while (L>1&&!c.a[L])--L;c.len=L;
73
            return make_pair(c,d);
74
75
        huge operator / (value x) {
76
            value d=0;huge tmp;
77
            for (int i=len;i;--i) {
```

```
78
                  d=d*base+a[i];
 79
                  tmp.a[i]=d/x; d%=x;
 80
 81
              tmp.len=len;
 82
              while (tmp.len>1&&!tmp.a[tmp.len]) --tmp.len;
 83
              return tmp;
 84
 85
         value operator %(value x){
 86
              value d=0;
              for (int i=len;i;--i)d=(d*base+a[i])%x;
 87
              return d:
 88
 89
 90
         huge operator / (huge b) {return divide(*this,b).first;}
 91
          huge operator % (huge b) {return divide(*this,b).second;}
 92
          huge &operator += (huge b) { *this=*this+b; return *this; }
 93
          huge &operator -= (huge b) { *this=*this-b; return *this; }
 94
         huge &operator *=(huge b) {*this=*this*b;return *this;}
 95
          huge &operator ++() {huge T; T=1; *this=*this+T; return *this; }
 96
          huge & operator --() {huge T; T=1; *this=*this-T; return *this; }
 97
          huge operator ++(int) {huge T, tmp=*this; T=1; *this=*this+T; return tmp; }
          huge operator -- (int) {huge T, tmp=*this; T=1; *this=*this-T; return tmp; }
 98
          huge operator + (value x) {huge T; T=x; return *this+T; }
100
         huge operator -(value x) {huge T; T=x; return *this-T; }
101
         huge operator *(value x) {huge T; T=x; return *this*T;}
102
          huge operator *=(value x) {*this=*this*x;return *this;}
103
          huge operator += (value x) { *this=*this+x; return *this; }
104
          huge operator -= (value x) { *this=*this-x; return *this; }
105
          huge operator /=(value x) {*this=*this/x;return *this;}
106
         huge operator %=(value x) {*this=*this%x;return *this;}
107
         bool operator == (value x) {huge T; T=x; return *this==T; }
108
         bool operator !=(value x) {huge T; T=x; return *this!=T; }
109
         bool operator <=(value x) {huge T; T=x; return *this<=T; }</pre>
110
         bool operator >= (value x) {huge T; T=x; return *this>=T; }
111
         bool operator <(value x) {huge T; T=x; return *this<T; }</pre>
112
         bool operator > (value x) {huge T; T=x; return *this>T; }
113
         huge operator = (value x) {
114
              len=0:
115
              while (x)a[++len]=x%base,x/=base;
116
              if (!len)a[++len]=0;
117
              return *this;
118
119
         bool operator < (huge b) {</pre>
120
              if (len<b.len)return 1;</pre>
121
              if (len>b.len)return 0;
122
              for (int i=len;i;--i) {
123
                  if (a[i] <b.a[i]) return 1;</pre>
124
                  if (a[i]>b.a[i])return 0;
125
126
              return 0;
127
128
         bool operator == (huge b) {
129
              if (len!=b.len) return 0;
130
              for (int i=len;i;--i)
131
                  if (a[i]!=b.a[i])return 0;
132
              return 1:
133
134
         bool operator !=(huge b) {return !(*this==b);}
```

```
135
         bool operator > (huge b) {return ! (*this<b||*this==b);}</pre>
136
         bool operator <= (huge b) {return (*this<b) | | (*this==b);}</pre>
137
         bool operator >=(huge b) {return (*this>b) | | (*this==b);}
138
         void str(char s[]) {
139
              int l=strlen(s); value x=0, y=1; len=0;
140
              for (int i=1-1; i>=0; --i) {
141
                  x=x+(s[i'']-0)*y;y*=10;
142
                  if (y==base)a[++len]=x,x=0,y=1;
143
144
              if (!len||x)a[++len]=x;
145
146
         void read() {
147
              scanf("%s",s);this->str(s);
148
149
         void print(){
150
              printf("%d",(int)a[len]);
151
              for (int i=len-1;i;--i) {
152
                  for (int j=base/10; j>=10; j/=10) {
153
                       if (a[i]<j)printf("0");</pre>
154
                           else break;
155
156
                  printf("%d",(int)a[i]);
157
              printf("\n");
158
159
160
    }f[1005];
161
     int main(){
162
         f[1]=f[2]=1;
163
         for (int i=3;i<=1000;i++)f[i]=f[i-1]+f[i-2];</pre>
164
```