

week spent on Facebook with the average number per week spent preparing for class.

- (a) Provide an estimate of this difference.
- (b) Explain why it is incorrect to use the two-sample  $t$  test to see if the means differ.

**7.71 Sadness and spending.** The “misery is not miserly” phenomenon refers to a person’s spending judgment going haywire when the person is sad. In a study, 31 young adults were given \$10 and randomly assigned to either a sad or a neutral group. The participants in the sad group watched a video about the death of a boy’s mentor (from *The Champ*), and those in the neutral group watched a video on the Great Barrier Reef. After the video, each participant was offered the chance to

trade \$0.50 increments of the \$10 for an insulated water bottle.<sup>27</sup> Here are the data:



SADNESS

Group	Purchase price (\$)						
Neutral	0.00	2.00	0.00	1.00	0.50	0.00	0.50
	2.00	1.00	0.00	0.00	0.00	0.00	1.00
Sad	3.00	4.00	0.50	1.00	2.50	2.00	1.50
	1.50	1.50	2.50	4.00	3.00	3.50	1.00
							3.50

- Examine each group's prices graphically. Is use of the  $t$  procedures appropriate for these data? Carefully explain your answer.
- Make a table with the sample size, mean, and standard deviation for each of the two groups.
- State appropriate null and alternative hypotheses for comparing these two groups.
- Perform the significance test at the  $\alpha = 0.05$  level, making sure to report the test statistic, degrees of freedom, and  $P$ -value. What is your conclusion?
- Construct a 95% confidence interval for the mean difference in purchase price between the two groups.

sold at all retail stores.

- (b) Explain in language that the manager can understand why he cannot be certain that sales rose by 6%, and that in fact sales may even have dropped.

**7.88 An improper significance test.** A friend has performed a significance test of the null hypothesis that two means are equal. His report states that the null hypothesis is rejected in favor of the alternative that the first mean is larger than the second. In a presentation on his work, he notes that the first sample mean was larger than the second mean and this is why he chose this particular one-sided alternative.

- (a) Explain what is wrong with your friend's procedure and why.

- (b) Suppose that he reported  $t = 1.70$  with a  $P$ -value of 0.06. What is the correct  $P$ -value that he should report?

**7.89 Breast-feeding versus baby formula.** A study of iron deficiency among infants compared samples of infants following different feeding regimens. One group contained breast-fed infants, while the infants in another group were fed a standard baby formula without any iron supplements. Here are summary results on blood hemoglobin levels at 12 months of age:<sup>35</sup>

Group	<i>n</i>	$\bar{x}$	<i>s</i>
Breast-fed	23	13.3	1.7
Formula	19	12.4	1.8

- (a) Is there significant evidence that the mean hemoglobin level is higher among breast-fed babies? State  $H_0$  and  $H_a$  and carry out a *t* test. Give the *P*-value. What is your conclusion?
- (b) Give a 95% confidence interval for the mean difference in hemoglobin level between the two populations of infants.
- (c) State the assumptions that your procedures in parts (a) and (b) require in order to be valid.

for Exercise 7.99, see page 476; and for Exercises 7.100 and 7.101, see page 479.

In all exercises calling for use of the *F* test, assume that both population distributions are very close to Normal. The actual data are not always sufficiently Normal to justify use of the *F* test.

**7.102 Comparison of standard deviations.** Here are some summary statistics from two independent samples from Normal distributions:

Sample	$n$	$s^2$
1	11	3.5
2	16	9.1

You want to test the null hypothesis that the two population standard deviations are equal versus the two-sided alternative at the 5% significance level.

- Calculate the test statistic.
- Find the appropriate value from Table E that you need to perform the significance test.
- What do you conclude?

**7.103 Revisiting the eating-group comparison.** Compare the standard deviations of weight loss in Example 7.16 (page 456). Give the test statistic, the degrees of freedom, and the *P*-value. Write a short summary of your analysis, including comments on the assumptions for the test.

 **7.104 A fat intake comparison.** Compare the standard deviations of fat intake in Exercise 7.75 (page 460).

(c) You ask an SRS of customers their opinions on each of two new floor plans for your store.

**7.121 Number of critical food violations.** The results of a major city's restaurant inspections are available through its online newspaper.<sup>38</sup> Critical food violations are those that put patrons at risk of getting sick and must immediately be corrected by the restaurant. An SRS of  $n = 200$  inspections from the more than 16,000 inspections since January 2009 were collected, resulting in  $\bar{x} = 0.83$  violations and  $s = 0.95$  violations.

- (a) Test the hypothesis that the average number of critical violations is less than 1.5 using a significance level of 0.05. State the two hypotheses, the test statistic, and  $P$ -value.
- (b) Construct a 95% confidence interval for the average number of critical violations and summarize your result.
- (c) Which of the two summaries (significance test versus confidence interval) do you find more helpful in this case? Explain your answer.
- (d) These data are integers ranging from 0 to 9. The data are also skewed to the right, with 70% of the values either a 0 or a 1. Given this information, do you think use of the  $t$  procedures is appropriate? Explain your answer.

**7.122 Two-sample  $t$  test versus matched pairs  $t$  test.**

Consider the following data set. The data were actually collected in pairs, and each row represents a pair.



PAIRED

Group 1	Group 2
48.86	48.88
50.60	52.63
51.02	52.55
47.99	50.94
54.20	53.02
50.66	50.66
45.91	47.78
48.79	48.44
47.76	48.92
51.13	51.63

- (a) Suppose that we ignore the fact that the data were collected in pairs and mistakenly treat this as a two-sample problem. Compute the sample mean and variance for each group. Then compute the two-sample  $t$  statistic, degrees of freedom, and  $P$ -value for the two-sided alternative.
- (b) Now analyze the data in the proper way. Compute the sample mean and variance of the differences. Then compute the  $t$  statistic, degrees of freedom, and  $P$ -value.
- (c) Describe the differences in the two test results.

**7.123 Two-sample  $t$  test versus matched pairs  $t$  test, continued.** Refer to the previous exercise. Perhaps an easier way to see the major difference in the two analysis

**8.71 Gender bias in textbooks.** To what extent do syntax textbooks, which analyze the structure of sentences, illustrate gender bias? A study of this question sampled sentences from 10 texts.<sup>23</sup> One part of the study examined the use of the words “girl,” “boy,” “man,” and “woman.” We will call the first two words *juvenile* and the last two *adult*. Is the proportion of female references that are juvenile (girl) equal to the proportion of male references that are juvenile (boy)? Here are data from one of the texts:

Gender	<i>n</i>	$\bar{X}$ (juvenile)
Female	60	48
Male	132	52

- Find the proportion of juvenile references for females and its standard error. Do the same for the males.
- Give a 90% confidence interval for the difference and briefly summarize what the data show.
- Use a test of significance to examine whether the two proportions are equal.