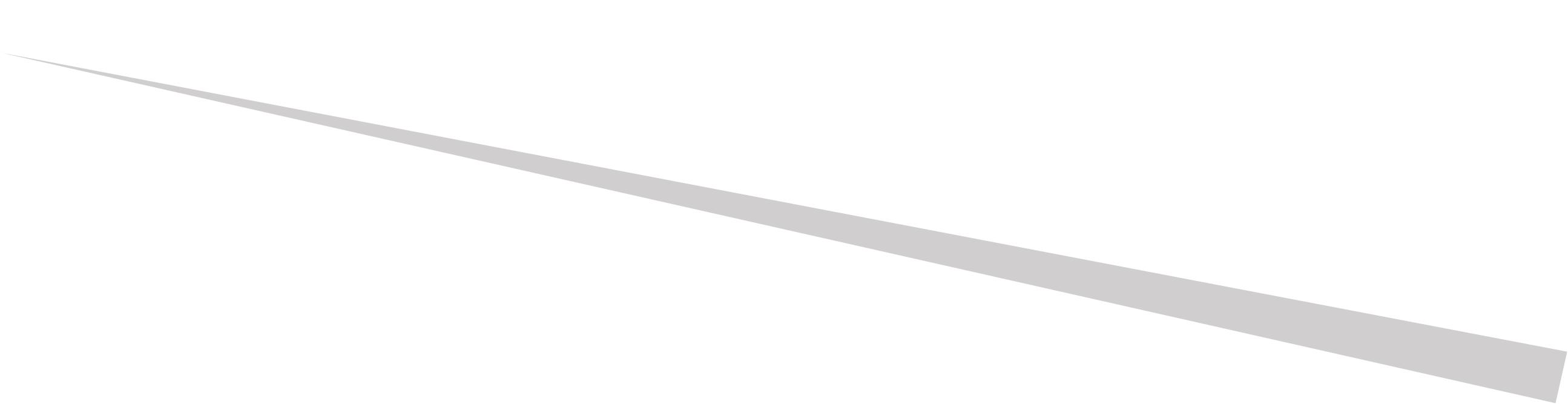
Nei and Kumar. 2000. pp. 33-50

Evolution of model complexity





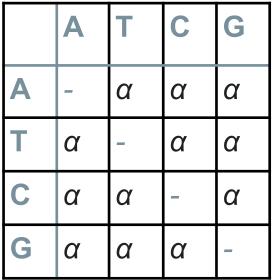


Observations

Count the number of different bases p-distance



All rates are equal One parameter





Kimura 2-parameter

Ts/Tv rate bias 2 parameters



Jukes-Cantor









Ts/Tv rate bias Base composition bias

Hasegawa-Kishino-Yano



Tamura-Nei

 Purine/Pyrimidine rates Ts/Tv rate bias 6 parameters





Time reversible Different rates 9 parameters

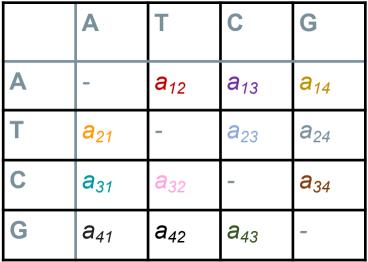


General-time-reversible

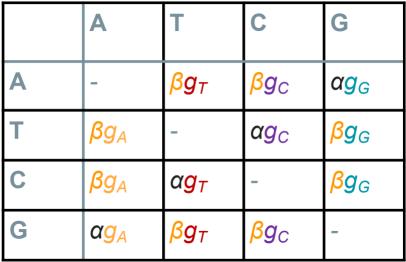
Unrestricted model

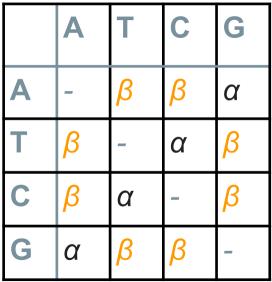
All different rates Not time reversible

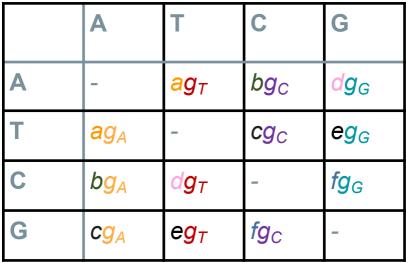


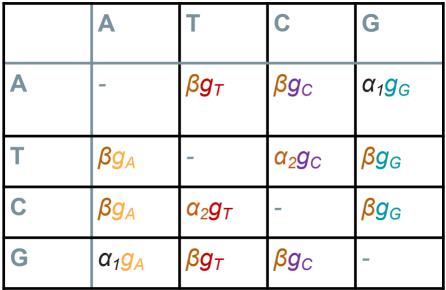








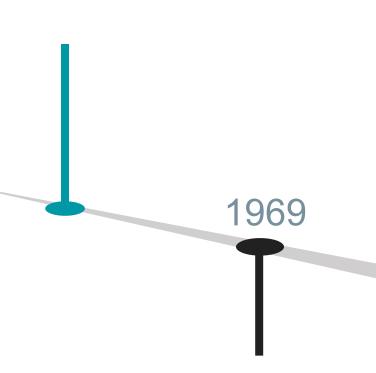




Slide courtesy of Dr. Qiqing Tao

Observations

- Count the number of different bases
- p-distance



Jukes-Cantor

- All rates are equal
- One parameter

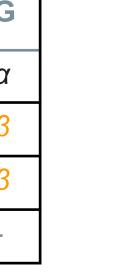
	A	Т	С	G
A	-	α	α	α
Т	α	ı	α	α
С	α	α	1	α
G	α	α	α	-

Evolution of model complexity

Kimura 2-parameter

- Ts/Tv rate bias
- 2 parameters

	Α	Т	C	G
Α	_	β	β	α
Т	β	1	α	β
С	β	α	1	β
G	α	β	β	ı



1985

1986

Tamura-Nei

- Purine/Pyrimidine rates
- Ts/Tv rate bias
- 6 parameters

	A	Т	С	G
A	-	$oldsymbol{eta}oldsymbol{g}_{ au}$	βg _C	a ₁ g _G
Т	βg_A	-	α ₂ g _C	βg_G
С	βg_A	α ₂ g _T	-	βg_G
G	α ₁ 9 _A	βg_{T}	βg_C	-

1993 1994

Unrestricted model

- All different rates
- Not time reversible

	Α	Т	С	G
A	-	a ₁₂	a ₁₃	a ₁₄
Т	a ₂₁	1	a ₂₃	a ₂₄
С	a ₃₁	a ₃₂	-	a ₃₄
G	a ₄₁	a ₄₂	a ₄₃	-

Hasegawa-Kishino-Yano

Ts/Tv rate bias

1980

Base composition bias

	A	Т	С	G
A	-	βg_T	βg_{C}	αg_G
Т	βg_A	1	ag_C	βg_G
C	βg_A	αg_T	1	βg _G
G	αg_A	βg_T	βg _C	-

General-time-reversible

- Time reversible
- Different rates
- 9 parameters

	A	Т	С	G
A	-	ag _⊤	bg _C	dg _G
Т	ag_A	-	cg _C	eg _G
С	bg _A	dg_T	_	fg_G
G	C _G A	eg _T	fg_C	-

Quantifying selection on coding sequences

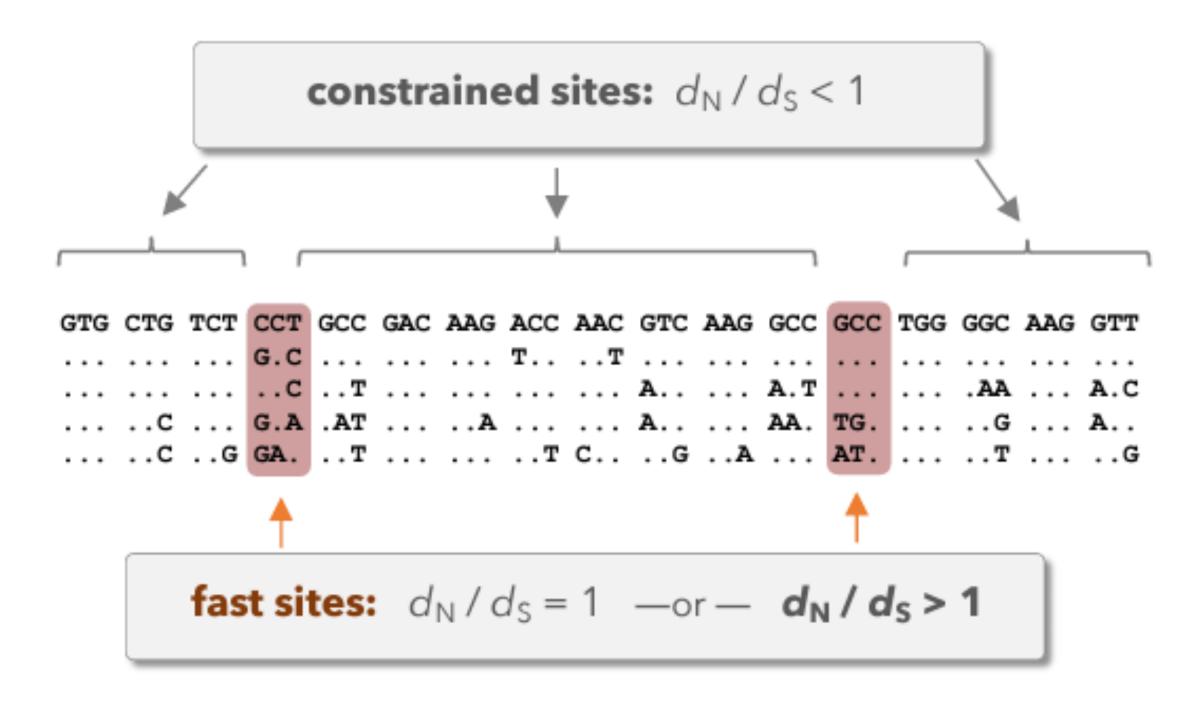
- 1.) selectively constrained:
 - $d_N/d_S < 1$

2.) strictly neutral:

$$d_N / d_S = 1$$

3.) adaptive evolution:

$$d_N/d_S > 1$$



Credit: Joe Bielawski