customer_segments

March 11, 2016

1 Creating Customer Segments

In this project you, will analyze a dataset containing annual spending amounts for internal structure, to understand the variation in the different types of customers that a wholesale distributor interacts with.

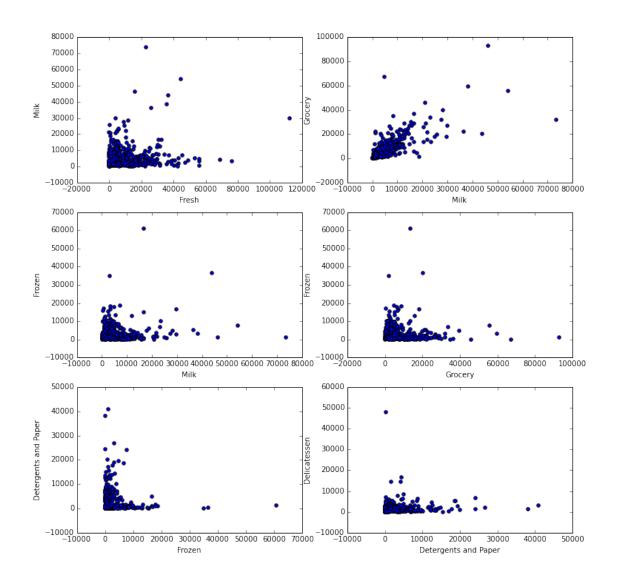
Instructions:

- Run each code block below by pressing **Shift+Enter**, making sure to implement any steps marked with a TODO
- Answer each question in the space provided by editing the blocks labeled "Answer:".
- When you are done, submit the completed notebook (.ipynb) with all code blocks executed, as well as a .pdf version (File > Download as).

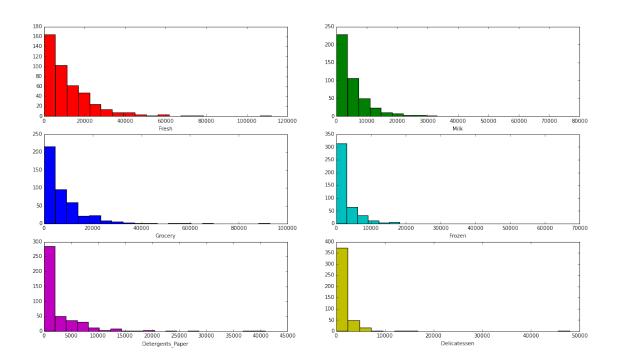
```
In [14]: # Import libraries: NumPy, pandas, matplotlib
         import numpy as np
         import pandas as pd
         import matplotlib.pyplot as plt
         # Tell iPython to include plots inline in the notebook
         %matplotlib inline
         import warnings
         warnings.filterwarnings('ignore')
         pd.options.display.float_format = '{:.5f}'.format
         pd.set_option('display.max_columns', 500)
         pd.set_option('display.width', 1000)
         # Read dataset
         data = pd.read_csv("wholesale-customers.csv")
         num_features=data.shape[1]
         num_data_points=data.shape[0]
         print "Dataset has {} rows, {} columns".format(num_data_points,num_features)
         print data.head() # print the first 5 rows
         print data.describe()
         ,,,
         TODOs:
         1. Create 3-D plot for pca vectors.
         2. Apply PCA on ICA-demixed-transformed data.
         3. Draw elbow graph to identify k in k-means.
Dataset has 440 rows, 6 columns
  Fresh Milk Grocery Frozen Detergents_Paper Delicatessen
```

```
12669 9656
                   7561
                            214
                                             2674
                                                           1338
   7057 9810
                   9568
1
                           1762
                                             3293
                                                           1776
2
   6353 8808
                   7684
                           2405
                                             3516
                                                           7844
3 13265 1196
                   4221
                           6404
                                              507
                                                            1788
 22615 5410
                   7198
                           3915
                                             1777
                                                           5185
                                                Frozen Detergents_Paper Delicatessen
             Fresh
                          Milk
                                   Grocery
count
         440.00000
                     440.00000
                                 440.00000
                                             440.00000
                                                               440.00000
                                                                              440.00000
       12000.29773 5796.26591 7951.27727 3071.93182
mean
                                                               2881.49318
                                                                             1524.87045
std
       12647.32887 7380.37717 9503.16283 4854.67333
                                                               4767.85445
                                                                             2820.10594
min
           3.00000
                      55.00000
                                   3.00000
                                              25.00000
                                                                  3.00000
                                                                                3.00000
25%
       3127.75000 1533.00000 2153.00000
                                             742.25000
                                                                256.75000
                                                                              408.25000
50%
       8504.00000 3627.00000 4755.50000 1526.00000
                                                                816.50000
                                                                              965.50000
75%
       16933.75000 7190.25000 10655.75000 3554.25000
                                                               3922.00000
                                                                             1820.25000
      112151.00000 73498.00000 92780.00000 60869.00000
                                                              40827.00000
                                                                            47943.00000
Out[14]: '\nTODOs:\n1. Create 3-D plot for pca vectors.\n2. Apply PCA on ICA-demixed-transformed data.\n
In [15]: ## Cleanup data, remove outliers.
         f, ((ax1, ax2), (ax3, ax4), (ax5, ax6)) = plt.subplots(3, 2)
         ax1.scatter(data.iloc[:,0],data.iloc[:,1])
         ax1.set_xlabel('Fresh')
         ax1.set_ylabel('Milk')
         ax2.scatter(data.iloc[:,1],data.iloc[:,2])
         ax2.set_xlabel('Milk')
         ax2.set_ylabel('Grocery')
         ax3.scatter(data.iloc[:,1],data.iloc[:,3])
         ax3.set_xlabel('Milk')
         ax3.set_ylabel('Frozen')
         ax4.scatter(data.iloc[:,2],data.iloc[:,3])
         ax4.set_xlabel('Grocery')
         ax4.set_ylabel('Frozen')
         ax5.scatter(data.iloc[:,3],data.iloc[:,4])
         ax5.set_xlabel('Frozen')
         ax5.set_ylabel('Detergents and Paper')
         ax6.scatter(data.iloc[:,4],data.iloc[:,5])
         ax6.set_xlabel('Detergents and Paper')
         ax6.set_ylabel('Delicatessen')
         fig = plt.gcf()
         fig.set_size_inches(12, 12)
         #fig.set_size_inches(18.5, 10.5, forward=True)
         plt.show()
         print "-"*100
```

```
print "Histogram of spending on specific product types."
print "-"*100
f, ((axis1, axis2), (axis3, axis4), (axis5, axis6)) = plt.subplots(3, 2)
### Visualize data spread.
colormap = np.array(['r', 'g', 'b','c','m','y'])
f.axes[0].hist(data.iloc[:,0],bins=20,color=colormap[0])
f.axes[0].set_xlabel(data.columns.values[0]);
f.axes[1].hist(data.iloc[:,1],bins=20,color=colormap[1])
f.axes[1].set_xlabel(data.columns.values[1]);
f.axes[2].hist(data.iloc[:,2],bins=20,color=colormap[2])
f.axes[2].set_xlabel(data.columns.values[2]);
f.axes[3].hist(data.iloc[:,3],bins=20,color=colormap[3])
f.axes[3].set_xlabel(data.columns.values[3]);
f.axes[4].hist(data.iloc[:,4],bins=20,color=colormap[4])
f.axes[4].set_xlabel(data.columns.values[4]);
f.axes[5].hist(data.iloc[:,5],bins=20,color=colormap[5])
f.axes[5].set_xlabel(data.columns.values[5]);
fig = plt.gcf()
fig.set_size_inches(12, 12)
fig.set_size_inches(18.5, 10.5, forward=True)
plt.show()
```



Histogram of spending on specific product types.



cleaned_data=cleaned_data[cleaned_data['Fresh']<60000]</pre>

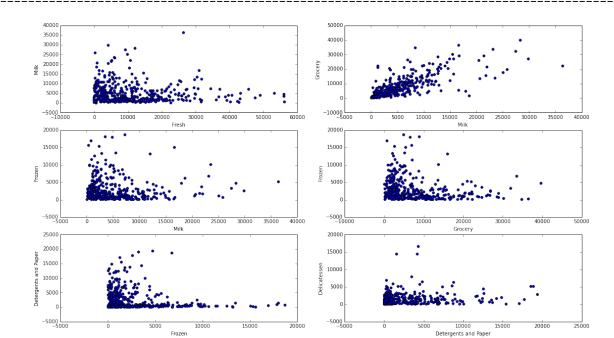
```
cleaned_data=cleaned_data[cleaned_data['Milk']<50000]</pre>
cleaned_data=cleaned_data[cleaned_data['Grocery']<50000]</pre>
cleaned_data=cleaned_data[cleaned_data['Frozen']<30000]</pre>
cleaned_data=cleaned_data[cleaned_data['Detergents_Paper']<20000]</pre>
cleaned_data=cleaned_data[cleaned_data['Delicatessen']<20000]</pre>
# Removed scaling since units are same, and feature-wise expenses are part of same expense, i.
#from sklearn import preprocessing
#cleaned_data[['Fresh','Milk','Grocery','Frozen','Detergents_Paper','Delicatessen']] = cleaned
print '-'*100
print " Cleaned, centered, and normalized data."
print '-'*100
f, ((ax1, ax2), (ax3, ax4), (ax5, ax6)) = plt.subplots(3, 2)
ax1.scatter(cleaned_data.iloc[:,0],cleaned_data.iloc[:,1])
ax1.set_xlabel('Fresh')
ax1.set_ylabel('Milk')
ax2.scatter(cleaned_data.iloc[:,1],cleaned_data.iloc[:,2])
ax2.set_xlabel('Milk')
ax2.set_ylabel('Grocery')
ax3.scatter(cleaned_data.iloc[:,1],cleaned_data.iloc[:,3])
ax3.set_xlabel('Milk')
```

```
ax3.set_ylabel('Frozen')
ax4.scatter(cleaned_data.iloc[:,2],cleaned_data.iloc[:,3])
ax4.set_xlabel('Grocery')
ax4.set_ylabel('Frozen')
ax5.scatter(cleaned_data.iloc[:,3],cleaned_data.iloc[:,4])
ax5.set_xlabel('Frozen')
ax5.set_ylabel('Detergents and Paper')
ax6.scatter(cleaned_data.iloc[:,4],cleaned_data.iloc[:,5])
ax6.set_xlabel('Detergents and Paper')
ax6.set_ylabel('Delicatessen')
fig = plt.gcf()
fig.set_size_inches(12, 12)
fig.set_size_inches(18.5, 10.5, forward=True)
plt.show()
print " -> Fresh vs Milk, Milk vs Frozen, Grocery vs Frozen, and Detergent_paper vs Frozen all
print "-"*100
print "Histogram of spending on specific product types."
print "-"*100
f, ((axis1, axis2), (axis3, axis4), (axis5, axis6)) = plt.subplots(3, 2)
### Visualize data spread.
colormap = np.array(['r', 'g', 'b','c','m','y'])
f.axes[0].hist(cleaned_data.iloc[:,0],bins=20,color=colormap[0])
f.axes[0].set_xlabel(cleaned_data.columns.values[0]);
f.axes[1].hist(cleaned_data.iloc[:,1],bins=20,color=colormap[1])
f.axes[1].set_xlabel(cleaned_data.columns.values[1]);
f.axes[2].hist(cleaned_data.iloc[:,2],bins=20,color=colormap[2])
f.axes[2].set_xlabel(cleaned_data.columns.values[2]);
f.axes[3].hist(cleaned_data.iloc[:,3],bins=20,color=colormap[3])
f.axes[3].set_xlabel(cleaned_data.columns.values[3]);
f.axes[4].hist(cleaned_data.iloc[:,4],bins=20,color=colormap[4])
f.axes[4].set_xlabel(cleaned_data.columns.values[4]);
f.axes[5].hist(cleaned_data.iloc[:,5],bins=20,color=colormap[5])
f.axes[5].set_xlabel(cleaned_data.columns.values[5]);
fig = plt.gcf()
fig.set_size_inches(12, 12)
fig.set_size_inches(18.5, 10.5, forward=True)
```

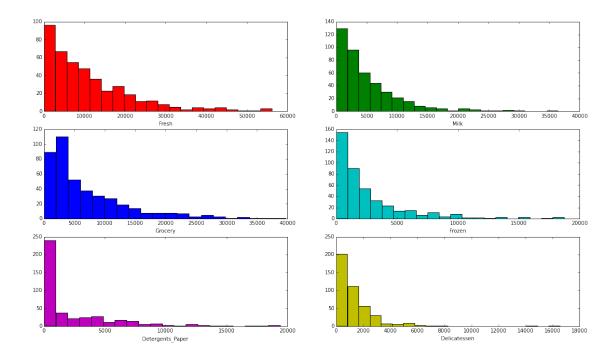
plt.show()

print "-> Plots of Fresh, Milk, Grocery, and Frozen seems to have some similarity in shape and

Cleaned, centered, and normalized data.



-> Fresh vs Milk, Milk vs Frozen, Grocery vs Frozen, and Detergent_paper vs Frozen all seem to have inverted to the seem of spending on specific product types.



-> Plots of Fresh, Milk, Grocery, and Frozen seems to have some similarity in shape and scale.

1.1 Feature Transformation

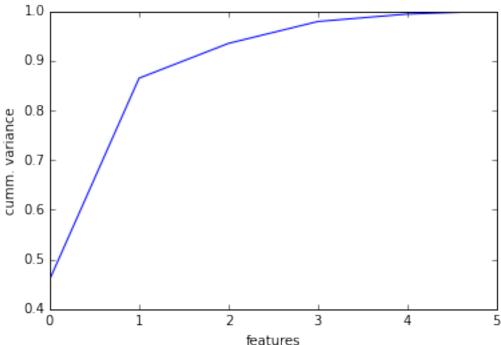
1) In this section you will be using PCA and ICA to start to understand the structure of the data. Before doing any computations, what do you think will show up in your computations? List one or two ideas for what might show up as the first PCA dimensions, or what type of vectors will show up as ICA dimensions. Answer:

Idea 1. Based on data spread, first PCA would be either fresh, or it could be combination of milk and groceries. Second PCA could include Frozen and Detergent_Paper, and Third PCA could be delicatessen.

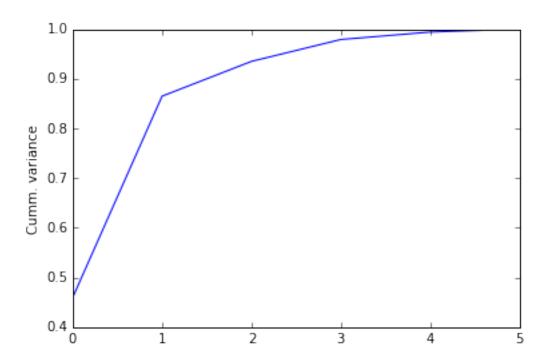
Idea 2. Perishability could be the differentiator in consumables / non-Delicatessen. ICA could identify the size or type of store, as this capability to manage perishables would depend on size or type of business.

1.1.1 PCA

```
print '*'*5," Cumm variance:",'*'*5,"\n",pc_cmf_df
          plt.plot(pc_cmf_df)
          plt.ylabel('cumm. variance')
          plt.xlabel('features')
          plt.show()
['Fresh' 'Milk' 'Grocery' 'Frozen' 'Detergents_Paper' 'Delicatessen']
 \begin{bmatrix} [-0.97653685 \ -0.12118407 \ -0.06154039 \ -0.15236462 \ 0.00705417 \ -0.06810471] \end{bmatrix} 
 [-0.11061386  0.51580216  0.76460638  -0.01872345  0.36535076  0.05707921]
 [-0.17855726  0.50988675  -0.27578088  0.71420037  -0.20440987  0.28321747]
  \begin{bmatrix} -0.04187648 & -0.64564047 & 0.37546049 & 0.64629232 & 0.14938013 & -0.02039579 \end{bmatrix} 
                0.20323566 -0.1602915
                                           0.22018612 0.20793016 -0.91707659]
 [-0.01576316 0.03349187 0.41093894 -0.01328898 -0.87128428 -0.26541687]]
[ \ 0.45961362 \ \ 0.40517227 \ \ 0.07003008 \ \ 0.04402344 \ \ 0.01502212 \ \ 0.00613848 ]
**** PCA on original data. ****
**** Cumm variance: ****
      pca
0 0.45961
1 0.86479
2 0.93482
3 0.97884
4 0.99386
5 1.00000
```

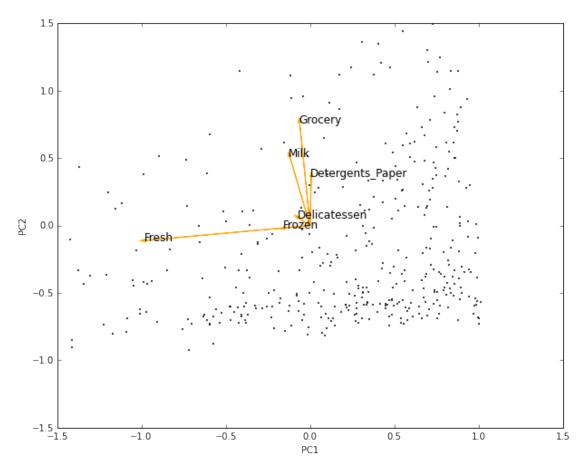


```
from sklearn.decomposition import PCA
          pca = PCA(n_components=num_features, whiten=True)
          pca.fit(data)
          # Print the components and the amount of variance in the data contained in each dimension
          print data.columns.values
          print pca.components_
          print pca.explained_variance_ratio_
          print "\n", '*'*5, "PCA on cleaned data.", '*'*5, "\n"
          pc_df=pd.DataFrame({"pca":pca.explained_variance_ratio_})
          pc_cmf_df=np.cumsum(pc_df)
          print '*'*5," Cumm variance:",'*'*5,"\n",pc_cmf_df
          plt.plot(pc_cmf_df)
          plt.ylabel('Cumm. variance')
['Fresh' 'Milk' 'Grocery' 'Frozen' 'Detergents_Paper' 'Delicatessen']
[[-0.97653685 -0.12118407 -0.06154039 -0.15236462 0.00705417 -0.06810471]
  \begin{bmatrix} -0.11061386 & 0.51580216 & 0.76460638 & -0.01872345 & 0.36535076 & 0.05707921 \end{bmatrix} 
  \begin{bmatrix} -0.17855726 & 0.50988675 & -0.27578088 & 0.71420037 & -0.20440987 & 0.28321747 \end{bmatrix} 
 [-0.04187648 \ -0.64564047 \ \ 0.37546049 \ \ 0.64629232 \ \ \ 0.14938013 \ \ -0.02039579]
 [ 0.015986
                0.20323566 - 0.1602915 \quad 0.22018612 \quad 0.20793016 - 0.91707659
  \begin{bmatrix} -0.01576316 & 0.03349187 & 0.41093894 & -0.01328898 & -0.87128428 & -0.26541687 \end{bmatrix} \end{bmatrix} 
[ 0.45961362  0.40517227  0.07003008  0.04402344  0.01502212  0.00613848]
**** PCA on cleaned data. ****
**** Cumm variance: ****
      pca
0 0.45961
1 0.86479
2 0.93482
3 0.97884
4 0.99386
5 1.00000
Out[18]: <matplotlib.text.Text at 0x108c08150>
```



```
In [19]: ''' Following function has been taken from Udacity Forum:
         https://discussions.udacity.com/t/
         having-trouble-with-pca-and-ica-specifically-with-explaining-what-the-dimensions-mean/41890/12. \\
         def biplot12(df):
             # Fit on 2 components
             pca = PCA(n_components=2, whiten=True).fit(df)
             # Plot transformed/projected data
             ax = pd.DataFrame(
                 pca.transform(df),
                 columns=['PC1', 'PC2']
             ).plot(kind='scatter', x='PC1', y='PC2', figsize=(10, 8), s=0.8)
             # Plot arrows and labels
             for i, (pc1, pc2) in enumerate(zip(pca.components_[0], pca.components_[1])):
                 ax.arrow(0, 0, pc1, pc2, width=0.001, fc='orange', ec='orange')
                 ax.annotate(df.columns[i], (pc1, pc2), size=12)
             return ax
         print '-'*100
         print "PC1 / PC2: Bi-plot of original data"
         print '-'*100
         ax = biplot12(data)
         # Play around with the ranges for scaling the plot
         ax.set_xlim([-1.5, 1.5])
         ax.set_ylim([-1.5, 1.5])
```

PC1 / PC2: Bi-plot of original data



In []:

2) How quickly does the variance drop off by dimension? If you were to use PCA on this dataset, how many dimensions would you choose for your analysis? Why?

Answer: Variance drops fast for first 2 dimentions, but then reduces slowly for remaining dimentions. Given the PCA variance graphs above, elbow is formed at 2nd PCA component, both for original data and scaled data. But since there are data points that have a some variance along multiple PCAs.

3) What do the dimensions seem to represent? How can you use this information?

Answer: PCA here can be used in 2 ways here: 1.) to identify similar customers. 2.)To find similar features. But target here is to find similar customers, and first 2 primary components seem to cover a most of variance.

Then, first PCA dimention corresponds to a segment that spends mostly on Fresh and Frozen products. Second PCA corresponds that spend mostly on Grocery, and significantly on Milk and Detergent_Paper in that order.

We can use this information in many ways: 1.) To transform the data along these 2 PCA, and then find cluster of users using transformed data. But this may not be good approach, since PCA-transformed data might loose some information which could impact be useful for un-biased clustering.

- 2.) To do clustering independently, and then compare the results with those from PCA, to see if both these results are convergent of divergent.
- 3.) We can use the results of PCA further components for supervised learning analysis regression or classification.
- 4.) We could also use K=2 and K=3 for k-mens clustering. Although value of K could depend on elbow in sum-of-square vs k plot.

1.1.2 ICA

```
In [20]: # TODO: Fit an ICA model to the data
        # Note: Adjust the data to have center at the origin first!
        from sklearn.decomposition import FastICA
        from sklearn import preprocessing
        scaled_data=data.copy(deep=True)
        #from sklearn import preprocessing
        scaled_data[['Fresh','Milk','Grocery','Frozen','Detergents_Paper','Delicatessen']] = scaled_da
        ica = FastICA(whiten=True,random_state=0)
        transformed_data=ica.fit_transform(scaled_data)
        # Print the independent components
        print "\n"
        print scaled_data.columns.values
        print ica.components_
        print "\n"
        print preprocessing.StandardScaler().fit_transform(ica.components_)
        #print "\n"
        #print ica.mixing_
['Fresh' 'Milk' 'Grocery' 'Frozen' 'Detergents_Paper' 'Delicatessen']
[[ 0.00259749 -0.01304261  0.06424104  0.00176503 -0.00789576 -0.00472804]
 [ \ 0.0036662 \ \ -0.01675528 \ \ -0.11301178 \ \ \ 0.00711535 \ \ \ 0.13424464 \ \ \ 0.01592772]
 [-0.00189529 \ -0.07279239 \ \ 0.05444162 \ \ \ 0.00183269 \ \ -0.01463357 \ \ \ 0.01719393]
 [-0.05024607 \quad 0.00639506 \quad 0.00647498 \quad 0.00325086 \quad -0.0104146 \quad \quad 0.00291214]
 [-0.00485887 \ -0.00161266 \ -0.00552872 \ -0.00242502 \ \ 0.0023066 \ \ \ 0.05090388]
 [ 0.51224275 -0.02365303 -1.95603618  0.67015972  2.21983183 -0.03356863]
 [ 0.23572202 -2.13321102  0.9452022  0.42088438 -0.6157666  0.03913673]
  \begin{bmatrix} -2.16830789 & 0.84785851 & 0.11414921 & 0.48780439 & -0.53541034 & -0.78091823 \end{bmatrix} 
 [ 0.08837092  0.54640212  -0.09382264  0.21997389  -0.29311692  1.97475038]
```

4) For each vector in the ICA decomposition, write a sentence or two explaining what sort of object or property it corresponds to. What could these components be used for?

Answer:

```
['Fresh' 'Milk' 'Grocery' 'Frozen' 'Detergents_Paper' 'Delicatessen']
```

A [0.45910575 0.11611315 1.11498351 0.41769164 -0.48743545 -1.21961489] - grc, frz, frs B [0.51224275 -0.02365303 -1.95603618 0.67015972 2.21983183 -0.03356863] - det, frz C [0.23572202 -2.13321102 0.9452022

 $\begin{array}{l} 0.42088438 - 0.6157666 \ 0.03913673] - \mathrm{grc}, \ \mathrm{frz} \ \mathrm{D} \ [-2.16830789 \ 0.84785851 \ 0.11414921 \ 0.48780439 \ -0.53541034 \ -0.78091823] - \mathrm{mlk}, \ \mathrm{frz} \ \mathrm{E} \ [\ 0.08837092 \ 0.54640212 \ -0.09382264 \ 0.21997389 \ -0.29311692 \ 1.97475038] - \mathrm{dlc}, \ \mathrm{F} \ [\ 0.87286647 \ 0.64649027 \ -0.12447609 \ -2.21651401 \ -0.28810251 \ 0.02021463]] - \mathrm{frsh}, \ \mathrm{milk} \end{array}$

-> Store of type A and C buy primarily Groceries, but also some Fresh and Frozen. -> Store B buys Detergent, Paper, and some Fresh and Frozen. -> D and F buy Fresh, Milk, and Frozen. -> E mostly buys Delicacies.

So there are 4 types of Stores:

1.) First that primarily buy Groceries, but also some Fresh and Frozen. 2.) Second that mainly buy Detergent, Paper, and some Fresh and Frozen. 3.) Third that primarily buy Fresh, Milk, and Frozen. 4.) Fourth that mainly buy Delicacies.

So some stores are specialized, while others are general stores. There could be further classification in general stores, by Groceries, Detergent_Paper, and Milk.

1.2 Clustering

In this section you will choose either K Means clustering or Gaussian Mixed Models clustering, which implements expectation-maximization. Then you will sample elements from the clusters to understand their significance.

1.2.1 Choose a Cluster Type

- 5) What are the advantages of using K Means clustering or Gaussian Mixture Models? Answer:
 - 1. k-means is intuitive, and fast.
 - 2. k-means can be computed and stored, for later application. This would allow quickly finding similarity.
 - 3. But k-means is strict.

[0.09602554 0.22619097]

- 4. GMM is more soft, and allows more realistic / fuzzy interpretation of distributions.
- 5. GMM is fast, but uses all available features. SO it is important to reduce features before applying GMM.
- 6) Below is some starter code to help you visualize some cluster data. The visualization is based on this demo from the sklearn documentation.

```
[ 0.20616164  0.40235345]
 [-0.08644358 0.17702881]
 [ 0.31808868  0.50532431]
[-0.9789537 0.56789831]]
 \begin{bmatrix} -0.15693572 & 1.71889528 & 1.9579227 & -0.17674166 & 2.33303464 & 0.52288549 \end{bmatrix} 
[ 0.64735159  0.89230964  0.68864929  0.7518027  0.52288549  1.33631608]]
In [23]: # TODO: Implement your clustering algorithm here, and fit it to the reduced data for visualiza
        # The visualizer below assumes your clustering object is named 'clusters'
        from scipy.spatial.distance import cdist
        clusters = KMeans(init='k-means++', n_clusters=3, n_init=5,max_iter=50).fit(reduced_data)
        print clusters
        # Plot the decision boundary by building a mesh grid to populate a graph.
        x_min, x_max = reduced_data[:, 0].min() - 1, reduced_data[:, 0].max() + 1
        y_min, y_max = reduced_data[:, 1].min() - 1, reduced_data[:, 1].max() + 1
       hx = (x_max - x_min)/1000.
       hy = (y_max-y_min)/1000.
        xx, yy = np.meshgrid(np.arange(x_min, x_max, hx), np.arange(y_min, y_max, hy))
        # Obtain labels for each point in mesh. Use last trained model.
        Z = clusters.predict(np.c_[xx.ravel(), yy.ravel()])
KMeans(copy_x=True, init='k-means++', max_iter=50, n_clusters=3, n_init=5,
   n_jobs=1, precompute_distances='auto', random_state=None, tol=0.0001,
   verbose=0)
In [24]: # TODO: Find the centroids for KMeans or the cluster means for GMM
        centroids = clusters.cluster_centers_
        print centroids
[[ 0.27639454  0.05157934]
 [-2.15260094 0.79297709]
 [-0.86805823 -3.58675495]]
In [25]: # Put the result into a color plot
       Z = Z.reshape(xx.shape)
        plt.figure(1)
        plt.clf()
        plt.imshow(Z, interpolation='nearest',
                 extent=(xx.min(), xx.max(), yy.min(), yy.max()),
                 cmap=plt.cm.Paired,
                 aspect='auto', origin='lower')
        plt.scatter(centroids[:, 0], centroids[:, 1],
                  marker='x', s=169, linewidths=3,
                  color='w', zorder=10)
        plt.title('Clustering on the wholesale grocery dataset (PCA-reduced data)\n'
```

```
'Centroids are marked with white cross')

plt.scatter(reduced_data[:,0],reduced_data[:,1])

plt.xlim(x_min, x_max)

plt.ylim(y_min, y_max)

plt.xticks(())

plt.yticks(())

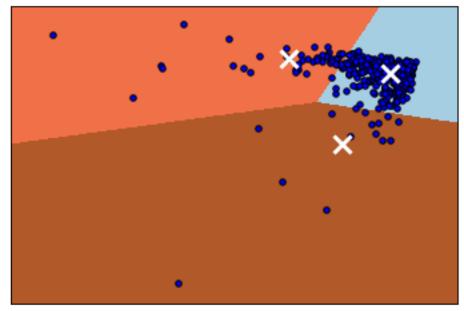
plt.show()

print scaled_data.columns.values

print centroids

print pca.inverse_transform(centroids)
```

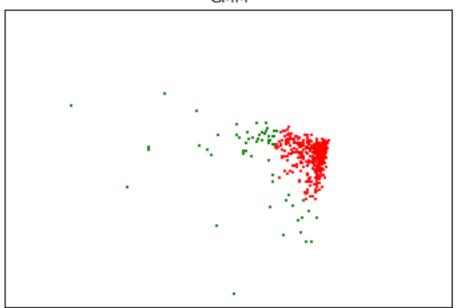
Clustering on the wholesale grocery dataset (PCA-reduced data) Centroids are marked with white cross



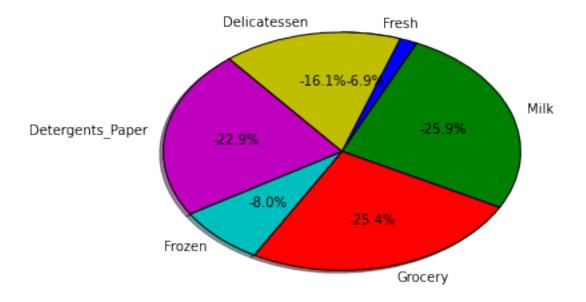
```
gmm=GMM(n_components=2).fit(reduced_data)
color_iter = ['r', 'g', 'b']
print gmm.covars_
Y_ = gmm.predict(reduced_data)
for i, (mean, covar, color) in enumerate(zip(gmm.means_, gmm._get_covars(), color_iter)):
        print "\ni=",i
        print "mean:", mean
        print "covar:", covar
        print "color:",color
        print "inverse of Mean", pca.inverse_transform(mean)
        v, w = linalg.eigh(covar)
        u = w[0] / linalg.norm(w[0])
        plt.scatter(reduced_data[Y_ == i, 0], reduced_data[Y_ == i, 1], 1.2, color=color)
print data.columns.values
inv_means=pca.inverse_transform(gmm.means_)
print inv_means
plt.xlim(-10, 5)
plt.ylim(-6, 6)
plt.xticks(())
plt.yticks(())
plt.title("GMM")
plt.show()
print "Composition for first type"
plt.pie(inv_means[0], labels=data.columns.values, autopct='%1.1f\%', shadow=True, startangle=9
plt.show()
print "Composition for second type"
plt.pie(inv_means[1], labels=data.columns.values, autopct='%1.1f%%', shadow=True, startangle=9
plt.show()
updated_data=data.copy(deep=True)
updated_data['total'] = updated_data.apply(np.sum, axis=1).tolist()
print "Data with total sales and cluster identifier."
updated_data['pred']=Y_.tolist()
print updated_data.tail(5)
summary_data_high = updated_data.copy(deep=True)
summary_data_high=summary_data_high[(summary_data_high.pred==0)].apply(np.sum,axis=0)
summary_data_all=pd.DataFrame(summary_data_high.iloc[:6],columns=['high'])
summary_data_low = updated_data.copy(deep=True)
summary_data_low=summary_data_low[(summary_data_low.pred==1)].apply(np.sum,axis=0)
summary_data_low=summary_data_low.iloc[:6].values
summary_data_all['low'] = summary_data_low
```

```
summary_data_all.T.plot(kind='bar', stacked=True,figsize=(10, 10))
[[ 0.19362965  0.29775726]
[ 2.58508355  4.60085312]]
i= 0
mean: [ 0.28365402  0.07109444]
covar: [[ 0.19362965 0.
                              1
              0.29775726]]
color: r
inverse of Mean [-0.06875738 -0.25918758 -0.25366884 -0.0803201 -0.22942012 -0.16149465]
mean: [-1.52160791 -0.38137257]
covar: [[ 2.58508355 0.
[ 0.
              4.60085312]]
color: g
inverse of Mean [ 0.36883584   1.39036239   1.36075817   0.43086185   1.23068049   0.86630727]
['Fresh' 'Milk' 'Grocery' 'Frozen' 'Detergents_Paper' 'Delicatessen']
 \begin{bmatrix} [-0.06875738 & -0.25918758 & -0.25366884 & -0.0803201 & -0.22942012 & -0.16149465] \end{bmatrix}
```

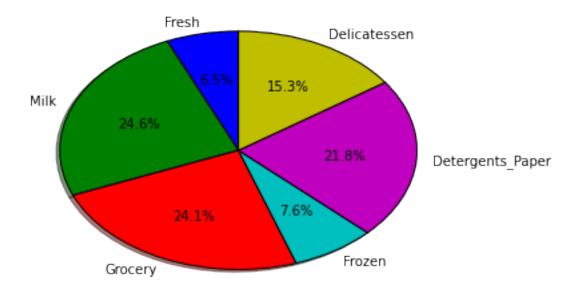
GMM



Composition for first type



Composition for second type

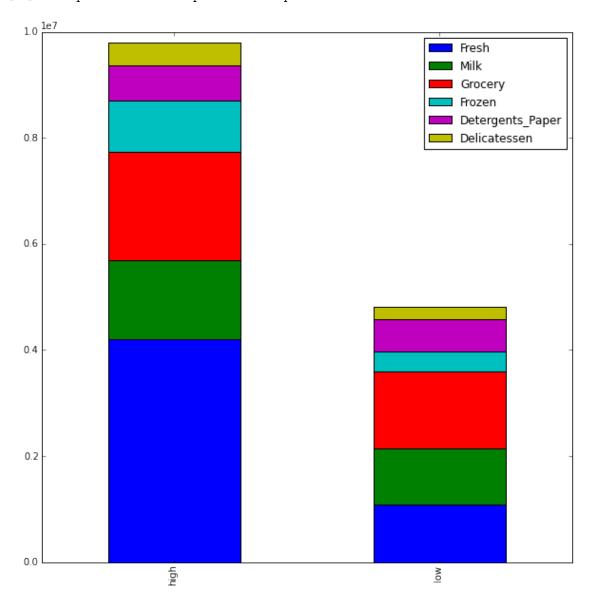


Data with total sales and cluster identified	er.
--	-----

	Fresh	Milk	Grocery	Frozen	Detergents_Paper	Delicatessen	total	pred
435	29703	12051	16027	13135	182	2204	73302	1
436	39228	1431	764	4510	93	2346	48372	0
437	14531	15488	30243	437	14841	1867	77407	1

438	10290	1981	2232	1038	168	2125	17834	0
439	2787	1698	2510	65	477	52	7589	0

Out[26]: <matplotlib.axes._subplots.AxesSubplot at 0x10d746c90>



7) What are the central objects in each cluster? Describe them as customers.

Answer: Centroids in K_Means are 1.) Small qty of everything, which means small stores. 2.) Mostly Milk, Grocery, and Detergent_Paper. 3.) Shops buying mostly Fresh, Frozen Milk, and Detergent Paper. Centroids in GMMs are: 1.) Lots of everything. 2.) Small qty of everything.

1.2.2 Conclusions

** 8)** Which of these techniques did you feel gave you the most insight into the data? Answer:

Tried multiple number of clusters for GMM and k-means, and 3 seemed best for k-means and 2 for GMMs.

k-Means groups data based on similarity, while GMM is bayesian and creates a model of mixtures and then assigns data to these models.

Also K-means is based on specific values and identifies centroids, while GMM is probabilistic and estimates the gaussians. K-Means assumes that variance of distribution is spherical, while GMM does not make such assumption.

k-means also assumes that observations are homogeneously distributes across clusters, which is not the case here.

K-Means creates hard boundaries, while GMM creates soft boundaries.

GMM identifies hidden factors, which is what we are trying to identify here.

All 3 techniques gave different information, and collating all 3 techniques gives confidence in solution. PCA gave more direct info on primary conponents, while ICA and Clustering gave insight into source and unlabeled similarity in data.

But GMMs seem to be best suited for such a problem, as observations are not equally distributed across clusters, and there is NO info that suggests that variance distribution is spherical.

Clusters created using K-means are not compact, and the bouldaries dont reflect the irregular distribution of points.

While GMM allows non-linear and soft boundaries, thus allowing more realistic explanation of clustering. So GMM and ICA provide most info about the latent factors.

9) How would you use that technique to help the company design new experiments?

A/B tests should give results in short time. So long running tests are not advisable.

Based on above analysis, we understand that there are 2 types of shops based on purchase units, and 4 types of shops based on product-type distribution.

Now there could be 2 types of tests: Type 1. That are visible to the users (shops, in this case). Type 2. Those that are not easily visible to the customers.

Lets take an example of 2 Tests that are visible to customers. Here we try to find out the best mechanizm to deliver products. Test 2 will follow results from Test 1.

Test 1: Divide the "Low" group further into 2 groups - "Control" and "Test" group. Each sub-group should have same proportion of each of the 4 types of shops. Control group will get the regular morning delivery (PUSH), while the Test group can choose the time of their choice for delivery (PULL).

Null hypothesis here is that morning delivery is best solution for "low" shops.

Results from this test will show either of these things: a.) If there is a common time during day or frequency that is more suitable for deliveries. b.) Do customers (shops) buy more products if they are given a choice in delivery schedule. c.) If there is a change in delivery costs.

Based on results of above test, we can run another A/B test to find if there are "HIGH" customers that are flexible with delivery times. Delivery trips for "PULL" deliveries for "LOW" shops can be used to delivery goods to "HIGH" shops at times other than normal morning and bulk evening deliveries.

Here, since "High" group was able to absorb the changes in original test, we run this 2nd A/B test to find out if their flexibility can be used to reduce delivery costs.

Null hypothesis here is that same delivery schedule suits all "HIGH" stores.

Here we divide the "High" group in 2 sub-groups, each having same proportion of the 4-types of shops. Control group "A" will receive the bulk delivery, and the Test group B will get delivery at the optimal time-of-day, say afternoon, as found in Test 1 above. This test would answer following questions: a.) If the on-demand time of Low stores is also suitable for "High" group stores. b.) Do stores buy more / less with change in delivery times. c.) Is there a change in delivery costs. d.) Is there an impact on wholeseller's inventory costs.

Based on results of Test 1 and Test 2, we would know: 1. What time(s) during day is most suitable for each type of store. 2. Can deliveries be combined for Low and High group stores. 3. Get more data points, like impact of distance, reason for flexibility, for further insight and better models.

Further A/B test could be to divide all shops into 2 sub-groups. Here the control group will receive all items in the regular morning delivery. Test group will receive one type of product in bulk evening delivery, but all other items in regular morning delivery. We then repeat this test for all 6 products. This will help identify time-sensitivity towards different products and of different store types.

Note: Run-time of these tests could be pre-decided to avoid any masses during execution period, FOr example, Test 1 could be run for 2 weeks, and results be analyzed for a week. And then Test 2 could be run

again for 2 weeks. This 5 week period should be such that it is not around any major shopping / festive season, to avoid reduce biases.

10) How would you use that data to help you predict future customer needs?

Answer: We have added a column 'Pred' to the original data, based on the cluster to which each data point belongs. 'Pred' can be used as a Label in supervised learning. Given the qty of various items of a future customer (store), its suitable label and hence other attributes, like best delivery mechanism can be predicted.

Based on ICA anlaysis, we found that there are 4 groups of stores.

For a new store, first step would be to identify what is the primary product that store buys. Using a classification model, we can use this info to map store to any of above 4 types of stores, and use that to predict other trends associated with the stores of that type.

We can then train supervised regression algorithms to predict the purchase units of milk, given the purchase units of all other products, and these would be 2 separate models, one for "Low" and another for "High" cluster.

Similarly we can train a classification model to classify a store as belonging to either of these 2 groups by using purchase unit of any 5 product types.

For example, if there is a new store that is only purchasing Grocery, Fresh, Frozen, Detergent_Paper, and Delicacies.

Using this data and our trained classification and regression models, we can prodect if the store belongs to "Low" or "High" group, and also predict its requirement of Milk.