Package 'greeks'

February 25, 2024

Title Sensitivities of Prices of Financial Options and Implied Volatilities

```
Version 1.3.4
```

Description Methods to calculate sensitivities of financial option prices for European, geometric and arithmetic Asian, and American options, with various payoff functions in the Black Scholes model, and in more general jump diffusion models. A shiny app to interactively plot the results is included. Furthermore, methods to compute implied volatilities are provided for a wide range of option types and custom payoff functions. Classical formulas are implemented for European options in the Black Scholes Model, as is presented in Hull, J. C. (2017), Options, Futures, and Other Derivatives.

In the case of Asian options, Malliavin Monte Carlo Greeks are implemented, see Hudde, A. & Rüschendorf, L. (2023). European and Asian Greeks for exponential Lévy processes. <doi:10.1007/s11009-023-10014-5>. For American options, the Binomial Tree Method is implemented, as is presented in Hull, J. C. (2017).

```
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Encoding UTF-8
Roxygen list(markdown = TRUE)
RoxygenNote 7.2.3
Suggests knitr,
     rmarkdown.
     testthat (>= 3.0.0),
     R.rsp
Config/testthat/edition 3
Imports magrittr,
     dqrng,
     Rcpp,
     tibble,
     ggplot2,
     plotly,
     shiny,
     tidyr
LinkingTo Rcpp
URL https://github.com/ahudde/greeks
BugReports https://github.com/ahudde/greeks/issues
NeedsCompilation yes
```

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VignetteBuilder knitr

R topics documented:

Index		18
	Malliavin_Geometric_Asian_Greeks	16
	Malliavin_European_Greeks	
	Malliavin_Asian_Greeks	
	Implied_Volatility	11
	Greeks_UI	10
	Greeks	8
	BS_Malliavin_Asian_Greeks	6
	BS_Implied_Volatility	5
	BS_Geometric_Asian_Greeks	4
	BS_European_Greeks	3
	Binomial_American_Greeks	2

Binomial_American_Greeks

Computes the Greeks of an American call- or put-option with the Binomial options pricing model

Description

In contract to European Options, American options can be executed at any time until the expiration date. For more details on the definition of Greeks in general see Greeks. This functions computes Greeks of American put- and call options in the binomial option pricing model (see (Hull, 2022)).

Usage

```
Binomial_American_Greeks(
  initial_price = 100,
  exercise_price = 100,
  r = 0,
  time_to_maturity = 1,
  volatility = 0.3,
  dividend_yield = 0,
  payoff = "call",
  greek = c("fair_value", "delta", "vega", "theta", "rho", "epsilon", "gamma"),
  steps = 1000,
  eps = 1/1e+05
)
```

BS_European_Greeks

3

Arguments

initial_price • initial price of the underlying asset. exercise_price • strike price of the option. • risk-free interest rate. r time_to_maturity • time to maturity. volatility • volatility of the underlying asset. dividend_yield · dividend yield. • the payoff function, a string in ("call", "put"). payoff • the Greek to be calculated. greek • the number of integration steps. steps • the step size for the finite difference method to calculate theta, vega, rho eps and epsilon

Value

Named vector containing the values of the Greeks specified in the parameter greek.

References

Hull, J. C. (2022). Options, futures, and other derivatives (11th Edition). Pearson

See Also

Greeks_UI for an interactive visualization

Examples

```
Binomial_American_Greeks(initial_price = 100, exercise_price = 100, r = 0, time_to_maturity = 1, volatility = 0.3, dividend_yield = 0, payoff = "call", greek = c("fair_value", "delta", "vega", "theta", "rho", "epsilon", "gamma"), steps = 20)
```

BS_European_Greeks

Computes the Greeks of a European call- or put-option, or of digital options in the Black Scholes model.

Description

For details on the definition of Greeks see Greeks.

Usage

Arguments

```
initial_price
                     • initial price of the underlying asset
exercise_price
                     • strike price of the option
                     • risk-free interest rate
time_to_maturity
                     • time to maturity in years
volatility
                     • volatility of the underlying asset
{\tt dividend\_yield}
                     · dividend yield
                     • in c("call", "put", "cash_or_nothing_call", "cash_or_nothing_put", "asset_or_nothing_call",
payoff
                        "asset_or_nothing_put")
greek
                     • Greeks to be calculated in c("fair value", "delta", "vega", "theta", "rho",
                        "epsilon", "lambda", "gamma", "vanna", "charm", "vomma", "veta", "vera",
                        "speed", "zomma", "color", "ultima")
```

Value

Named vector containing the values of the Greeks specified in the parameter greek.

See Also

```
Malliavin_European_Greeks for the Monte Carlo implementation
Greeks_UI for an interactive visualization
```

```
BS_European_Greeks(initial_price = 120, exercise_price = 100, r = 0.02, time_to_maturity = 4.5, dividend_yield = 0.015, volatility = 0.22, greek = c("fair_value", "delta", "gamma"), payoff = "put")
```

```
BS_Geometric_Asian_Greeks
```

Computes the Greeks of a Geometric Asian Option with classical Calland Put-Payoff in the Black Scholes model

Description

In contrast to Asian options (see Malliavin_Asian_Greeks), geometric Asian options evaluate the geometric average $\exp\left(\frac{1}{T}\int_0^T \ln S_t dt\right)$, where S_t is the price of the underlying asset at time t and T is the time-to-maturity of the option. For more details on the definition of Greeks see Greeks.

Usage

```
BS_Geometric_Asian_Greeks(
  initial_price = 100,
  exercise_price = 100,
  r = 0,
  time_to_maturity = 1,
  volatility = 0.3,
  dividend_yield = 0,
  payoff = "call",
  greek = c("fair_value", "delta", "rho", "vega", "theta", "gamma")
)
```

Arguments

```
initial_price
                     • initial price of the underlying asset, can also be a vector
exercise_price
                     • strike price of the option
                     • risk-free interest rate
time_to_maturity
                     • time to maturity in years
volatility
                     · volatility of the underlying asset
                     · dividend yield
dividend_yield
payoff
                     • the payoff function, either a string in ("call", "put")
greek
                     • the Greeks to be calculated in c("fair_value", "delta", "vega", "theta", "rho",
                        "gamma", "vomma")
```

Value

Named vector containing the values of the Greeks specified in the parameter greek.

See Also

Malliavin_Geometric_Asian_Greeks for the Monte Carlo implementation which provides digital and custom payoff functions and also works for the jump diffusion model

Greeks_UI for an interactive visualization

Examples

```
BS_Geometric_Asian_Greeks(initial_price = 110, exercise_price = 100, r = 0.02, time_to_maturity = 4.5, dividend_yield = 0.015, volatility = 0.22, greek = c("fair_value", "delta", "rho", "vega", "theta", "gamma"), payoff = "put")
```

BS_Implied_Volatility Computes the implied volatility for European put- and call options in the Black Scholes model via Halley's method.

Description

For the definition of *implied volatility* see Implied_Volatility. BS_Implied_Volatility offers a very fast implementation for European put- and call options applying Halley's method (see en.wikipedia.org/wiki/Halley%27sg).

Usage

```
BS_Implied_Volatility(
  option_price,
  initial_price = 100,
  exercise_price = 100,
  r = 0,
  time_to_maturity = 1,
  dividend_yield = 0,
  payoff = "call",
  start_volatility = 0.3,
  precision = 1e-09
)
```

Arguments

```
option_price
                     • current price of the option
initial_price
                     • initial price of the underlying asset.
exercise_price
                     • strike price of the option.
                     • risk-free interest rate.
time_to_maturity
                     • time to maturity.
dividend_yield
                     · dividend yield.
payoff
                     • the payoff function, a string in ("call", "put").
start_volatility
                     • the volatility value to start the approximation
precision
                     • precision of the result
```

Value

Named vector containing the values of the Greeks specified in the parameter greek.

See Also

Implied_Volatility for American and Asian options, and for digital payoff functions

Examples

```
BS_Implied_Volatility(option_price = 27, initial_price = 100, exercise_price = 100, r = 0.03, time_to_maturity = 5, dividend_yield = 0.015, payoff = "call")
```

BS_Malliavin_Asian_Greeks

Computes the Greeks of an Asian option with the Malliavin Monte Carlo Method in the Black Scholes model

Description

For a description of Asian Greeks see Malliavin_Asian_Greeks. BS_Malliavin_Asian_Greeks offers a fast implementation in the Black Scholes model.

Usage

```
BS_Malliavin_Asian_Greeks(
   initial_price = 100,
   exercise_price = 100,
   r = 0,
   time_to_maturity = 1,
   volatility = 0.3,
   dividend_yield = 0,
   payoff = "call",
   greek = c("fair_value", "delta", "vega", "rho"),
   steps = round(time_to_maturity * 252),
   paths = 1000,
   seed = 1
)
```

Arguments

initial_price • initial price of the underlying asset, can also be a vector exercise_price • strike price of the option, can also be a vector · risk-free interest rate time_to_maturity • time to maturity in years volatility · volatility of the underlying asset · dividend yield dividend_yield • the payoff function, either a string in ("call", "put"), or a function payoff • Greeks to be calculated in c("fair_value", "delta", "rho", "vega") greek • the number of integration steps steps • the number of simulated paths paths • the seed of the random number generator seed

8 Greeks

Value

Named vector containing the values of the Greeks specified in the parameter greek.

See Also

Malliavin_Asian_Greeks for a greater set of Greeks and also in the jump diffusion model Greeks_UI for an interactive visualization

Examples

```
BS_Malliavin_Asian_Greeks(initial_price = 110, exercise_price = 100, r = 0.02, time_to_maturity = 4.5, dividend_yield = 0.015, volatility = 0.22, greek = c("fair_value", "delta", "rho"), payoff = "put")
```

Greeks

Computes the Greeks of various options in the Black Scholes model or both in the Black Scholes model or a Jump Diffusion model in the case of Asian Options, or in the Binomial options pricing model

Description

Greeks are derivatives of the option value with respect to underlying parameters. For instance, the Greek $\Delta = \frac{\partial fair_value}{\partial initial_price}$ (Delta) measures how the price of an option changes with a minor change in the underlying asset's price, while $\Gamma = \frac{\partial fair_value}{\partial initial_price}$ (Gamma) measures how Δ itself changes as the price of the underlying asset shifts. Greeks can be computed for different types of options: For

- European Greeks see also BS_European_Greeks and Malliavin_European_Greeks
- American Greeks see also Binomial_American_Greeks
- Asian Greeks see also BS_Malliavin_Asian_Greeks and Malliavin_Asian_Greeks
- Geometric Asian Greeks see also BS_Geometric_Asian_Greeks and Malliavin_Asian_Greeks

The Greeks are defined as the following partial derivatives of the option value:

- Delta = $\Delta = \frac{\partial fair_value}{\partial initial_price}$, the derivative with respect to the price of the underlying asset
- Vega = $\mathcal{V} = \frac{\partial fair_value}{\partial volatility}$, the derivative with respect to the volatility
- Theta = $\Theta = -\frac{\partial fair_value}{\partial time_to_maturity}$, the negative derivative with respect to the time until expiration of the option
- rho = $\rho = \frac{\partial \text{fair_value}}{\partial r}$, the derivative with respect to the risk-free interest rate
- Epsilon = $\epsilon = \frac{\partial fair_value}{\partial time_to_maturity}$, the derivative with respect to the dividend yield of the underlying asset
- Lambda = $\lambda = \Delta \times \frac{\text{initial_price}}{\text{exercise_price}}$
- Gamma = $\Gamma = \frac{\partial^2 fair_value}{\partial initial_price^2}$, the second derivative with respect to the price of the underlying asset
- Vanna = $\frac{\partial \Delta}{\partial \text{volatility}} = \frac{\partial^2 \text{fair_value}}{\partial \text{intial_price } \partial \text{volatility}}$, the derivative of Δ with respect to the volatility
- Vomma = $\frac{\partial^2 fair_value}{\partial volatility^2}$, the second derivative with respect to the volatility

Greeks 9

• Veta = $\frac{\partial \mathcal{V}}{\partial r} = \frac{\partial^2 \text{fair_value}}{\partial \text{volatility } \partial \text{time_to_maturity}}$, the derivative of \mathcal{V} with respect to the time until expiration of the option

- Vera = $\frac{\partial^2 \text{fair_value}}{\partial \text{volatiliy } \partial r}$, the derivative of $\mathcal V$ with respect to the risk-free interest rate
- Speed = $\frac{\partial \Gamma}{\partial \text{initial_price}} = \frac{\partial^3 \text{fair_value}}{\partial \text{initial_price}^3}$, the third derivative of the option value with respect to the price of the underlying asset
- Zomma = $\frac{\Gamma}{\text{volatility}} = \frac{\partial^3 \text{fair_value}}{\partial \text{volatility}^3}$, the derivative of Gamma with respect to the volatility
- Color = $\frac{\partial \Gamma}{\partial r} = \frac{\partial^3 fair_value}{\partial initial_price^2 \partial r}$, the derivative of Gamma with respect to the risk-free interest rate
- Ultima = $\frac{\partial Vomma}{\partial volatility} = \frac{\partial^3 fair_value}{\partial volatility^3}$, the third derivative with respect to the volatility

For the definitions of Greeks, and the different types of options see Hull (2022) or en.wikipedia.org/wiki/Greeks_(finance).

Usage

```
Greeks(
  initial_price,
  exercise_price,
  r,
  time_to_maturity,
  volatility,
  dividend_yield = 0,
  model = "Black_Scholes",
  option_type = "European",
  payoff = "call",
  greek = c("fair_value", "delta", "vega", "theta", "rho", "gamma"),
  antithetic = TRUE,
  ...
)
```

· ... Other arguments passed on to methods

Arguments

. . .

```
• initial price of the underlying asset
initial_price
exercise_price
                     • strike price of the option
                     • risk-free interest rate
time_to_maturity
                     · time to maturity in years
                     · volatility of the underlying asset
volatility
dividend_yield
                     · dividend yield
model
                     • the model to be chosen in ("black_scholes", "jump_diffusion")
                  in c("European", "American", "Asian", "Geometric Asian", "Digital", "Bino-
option_type
                  mial) - the type of option to be considered
                     • in c("call", "put", "cash_or_nothing_call", "cash_or_nothing_put", "asset_or_nothing_call",
payoff
                       "asset_or_nothing_put")
                     • Greeks to be calculated in c("fair_value", "delta", "vega", "theta", "rho",
greek
                       "epsilon", "lambda", "gamma", "vanna", "charm", "vomma", "veta", "vera",
                       "speed", "zomma", "color", "ultima")
antithetic
                     • if TRUE, antithetic random numbers will be chosen to decrease variance
```

10 Greeks_UI

Value

Named vector containing the values of the Greeks specified in the parameter greek.

References

```
Hull, J. C. (2022). Options, futures, and other derivatives (11th Edition). Pearson en.wikipedia.org/wiki/Greeks_(finance)
```

See Also

```
BS_European_Greeks for option_type = "European"

Binomial_American_Greeks for option_type = "American"

BS_Geometric_Asian_Greeks for option_type = "Geometric Asian" and model = "black_scholes"

BS_Malliavin_Asian_Greeks for option_type = = "Asian" and model = "black_scholes" and greek in c("fair_value", "delta", "rho", "vega")

Malliavin_Asian_Greeks for more general cases of Asian Greeks

Greeks_UI for an interactive visualization
```

Examples

```
Greeks(initial_price = 100, exercise_price = 120, r = 0.01,
time_to_maturity = 5, volatility = 0.30, payoff = "call")
Greeks(initial_price = 100, exercise_price = 100, r = -0.005,
time_to_maturity = 1, volatility = 0.30, payoff = "put",
option_type = "American")
```

Greeks_UI

Opens a shiny app to interactively visualize option prices and Greeks.

Description

Opens a shiny app to interactively visualize option prices and Greeks. This works for European Options (see BS_European_Greeks), American Options (see Binomial_American_Greeks), Geometric Asian Options (see BS_Geometric_Asian_Greeks), as well as Asian options (see BS_Malliavin_Asian_Greeks). For performance reasons, just the Black-Scholes model is possible, and for some cases, the set of Greeks is limited. On the y-Axis, the option value resp. the value of the greeks are displayed, for the x-axis, several parameters like initial_price or time_to_maturity are possible.

Implied_Volatility 11



Usage

Greeks_UI()

Implied_Volatility Computes the implied volatility for various options via Newton's method

Description

If the value of an option, and other (model)parameters like the risk-free interest rate, the time-to-maturity, and the dividend yield are known, the assumed volatility of the underlying asset, the *implied volatility* can be inferred. See Hull (2022).

Usage

```
Implied_Volatility(
  option_price,
  initial_price = 100,
  exercise_price = 100,
  r = 0,
  time_to_maturity = 1,
```

12 Implied_Volatility

```
dividend_yield = 0,
  model = "Black_Scholes",
  option_type = "European",
  payoff = "call",
  start_volatility = 0.3,
  precision = 1e-06,
  max_iter = 30
)
```

Arguments

option_price • current price of the option initial_price • initial price of the underlying asset • strike price of the option exercise_price • risk-free interest rate r time_to_maturity • time to maturity in years · dividend yield dividend_yield model • the model to be chosen in c("European", "American", "Geometric Asian", "Asian", "Digital") - the type option_type of option to be considered payoff • in c("call", "put") start_volatility initial guess precision of the computation precision maximal number of iterations of the approximation max_iter

Value

Named vector containing the values of the Greeks specified in the parameter greek.

References

```
Hull, J. C. (2022). Options, futures, and other derivatives (11th Edition). Pearson
```

See Also

```
BS_Implied_Volatility for the special case option_type = "European" and payoff in c("call", "put")
```

```
Implied_Volatility(15, r = 0.05, option_type = "Asian",
payoff = "call")
```

Malliavin_Asian_Greeks

Computes the Greeks of an Asian option with the Malliavin Monte Carlo Method in the Black Scholes model, or for Asian options, also in a Jump Diffusion model

Description

Asian options are path-dependent. If S_t is the price of the underlying asset at time t, the execution of an Asian option depends on the average price of option, $\frac{1}{T}\int_0^T S_t dt$, where T is the time-to-maturity of the option. For more details on the definition of Greeks in general see Greeks.

For a description of Malliavin Monte Carlo Methods for Greeks see for example (Hudde & Rüschendorf, 2023).

Usage

```
Malliavin_Asian_Greeks(
  initial_price = 100,
  exercise_price = 100,
  r = 0,
  time_to_maturity = 1,
  volatility = 0.3,
  dividend_yield = 0,
  payoff = "call",
  greek = c("fair_value", "delta", "rho", "vega", "theta", "gamma"),
  model = "black_scholes",
  lambda = 0.2,
  alpha = 0.3,
  jump_distribution = function(n) stats::rt(n, df = 3),
  steps = round(time_to_maturity * 252),
  paths = 10000,
  seed = 1,
  antithetic = FALSE
)
```

Arguments

```
initial_price
                     • initial price of the underlying asset, can also be a vector
                     • strike price of the option, can also be a vector
exercise_price
                     • risk-free interest rate
time_to_maturity
                     • time to maturity in years
                     • volatility of the underlying asset
volatility
                     · dividend yield
dividend_yield
payoff
                     • the payoff function, either a string in ("call", "put", "digital_call", "digi-
                        tal_put"), or a function
greek
                     • the Greek to be calculated
model
                     • the model to be chosen in ("black_scholes", "jump_diffusion")
```

the lambda of the Poisson process in the jump-diffusion model
 the alpha in the jump-diffusion model influences the jump size
 jump_distribution

 the distribution of the jumps, choose a function which generates random numbers with the desired distribution

 steps

 the number of integration steps

 the number of simulated paths
 the seed of the random number generator

• if TRUE, antithetic random numbers will be chosen to decrease variance

Value

Named vector containing the values of the Greeks specified in the parameter greek.

References

antithetic

Hudde, A., & Rüschendorf, L. (2023). European and Asian Greeks for Exponential Lévy Processes. Methodol Comput Appl Probab, 25 (39). https://doi.org/10.1007/s11009-023-10014-5

See Also

BS_Malliavin_Asian_Greeks for a faster computation, but only in the Black Scholes model and with a smaller set of Greeks

Examples

```
Malliavin_Asian_Greeks(initial_price = 110, exercise_price = 100, r = 0.02, time_to_maturity = 4.5, dividend_yield = 0.015, volatility = 0.22, greek = c("fair_value", "delta", "rho"), payoff = "put")
```

Malliavin_European_Greeks

Computes the Greeks of a European option with the Malliavin Monte Carlo Method in the Black Scholes model

Description

For details on the definition of Greeks see Greeks. For a description of Malliavin Monte Carlo Methods for Greeks see for example (Hudde & Rüschendorf, 2023).

Usage

```
Malliavin_European_Greeks(
  initial_price = 100,
  exercise_price = 100,
  r = 0,
  time_to_maturity = 1,
  volatility = 0.3,
  payoff = "call",
```

```
greek = c("fair_value", "delta", "vega", "theta", "rho", "gamma"),
model = "Black Scholes",
paths = 10000,
seed = 1,
antithetic = FALSE
)
```

Arguments

• initial price of the underlying asset initial_price • strike price of the option exercise_price • risk-free interest rate r time_to_maturity • time to maturity in years · volatility of the underlying asset volatility payoff • the payoff function, either a string in ("call", "put", "cash_or_nothing_call", "cash_or_nothing_call", "asset_or_nothing_call", "asset_or_nothing_put"), or a function greek • the Greeks to be calculated in ("fair_value", "delta", "vega", "theta", "rho", "gamma") model • the model to be chosen • the number of simulated paths paths seed • the seed of the random number generator antithetic • if TRUE, antithetic random numbers will be chosen to decrease variance

Value

Named vector containing the values of the Greeks specified in the parameter greek

References

Hudde, A., & Rüschendorf, L. (2023). European and Asian Greeks for Exponential Lévy Processes. Methodol Comput Appl Probab, 25 (39). https://doi.org/10.1007/s11009-023-10014-5

See Also

BS_European_Greeks for the exact and fast implementation for call-, put- and digital payoff functions

```
Malliavin_European_Greeks(initial_price = 110,
exercise_price = 100, r = 0.02, time_to_maturity = 4.5,
volatility = 0.22, greek = c("fair_value", "delta", "rho"), payoff = "put")
```

Malliavin_Geometric_Asian_Greeks

Computes the Greeks of a geometric Asian option with the Malliavin Monte Carlo Method in the Black Scholes- or Jump diffusion model

Description

For the definition of geometric Asian options see BS_Geometric_Asian_Greeks, and for a description of the Malliavin Monte Carlo Method for Greeks see for example (Hudde & Rüschendorf, 2023).

Usage

```
Malliavin_Geometric_Asian_Greeks(
  initial_price = 100,
  exercise_price = 100,
  r = 0,
  time_to_maturity = 1,
  volatility = 0.3,
  dividend_yield = 0,
  payoff = "call",
  greek = c("fair_value", "delta", "rho", "vega", "theta", "gamma"),
  model = "black_scholes",
  lambda = 0.2,
  alpha = 0.3,
  jump_distribution = function(n) stats::rt(n, df = 3),
  steps = round(time_to_maturity * 252),
  paths = 10000,
  seed = 1,
  antithetic = FALSE
```

Arguments

• initial price of the underlying asset, can also be a vector initial_price exercise_price • strike price of the option, can also be a vector • risk-free interest rate time_to_maturity • time to maturity in years volatility · volatility of the underlying asset dividend_yield · dividend yield payoff • the payoff function, either a string in ("call", "put", "digital_call", "digital_put"), or a function · the Greek to be calculated greek model • the model to be chosen in ("black_scholes", "jump_diffusion") • the lambda of the Poisson process in the jump-diffusion model lambda alpha • the alpha in the jump-diffusion model influences the jump size

jump_distribution

• the distribution of the jumps, choose a function which generates random numbers with the desired distribution

stepsthe number of integration stepsthe number of simulated paths

• the seed of the random number generator

antithetic • if TRUE, antithetic random numbers will be chosen to decrease variance

Value

Named vector containing the values of the Greeks specified in the parameter greek.

References

Hudde, A., & Rüschendorf, L. (2023). European and Asian Greeks for Exponential Lévy Processes. Methodol Comput Appl Probab, 25 (39). https://doi.org/10.1007/s11009-023-10014-5

See Also

BS_Geometric_Asian_Greeks for exact and fast computation in the Black Scholes model and for put- and call payoff functions

```
Malliavin_Asian_Greeks(initial_price = 110, exercise_price = 100, r = 0.02, time_to_maturity = 4.5, dividend_yield = 0.015, volatility = 0.22, greek = c("fair_value", "delta", "rho"), payoff = "put")
```

Index

```
Binomial_American_Greeks, 2, 8, 10

BS_European_Greeks, 3, 8, 10, 15

BS_Geometric_Asian_Greeks, 4, 8, 10, 16, 17

BS_Implied_Volatility, 5, 5, 12

BS_Malliavin_Asian_Greeks, 6, 8, 10, 14

Greeks, 2-4, 8, 13, 14

Greeks_UI, 3-5, 7, 10, 10

Implied_Volatility, 5, 6, 11

Malliavin_Asian_Greeks, 4, 6-8, 10, 13

Malliavin_European_Greeks, 4, 8, 14

Malliavin_Geometric_Asian_Greeks, 5, 16
```