CIS Software Manual

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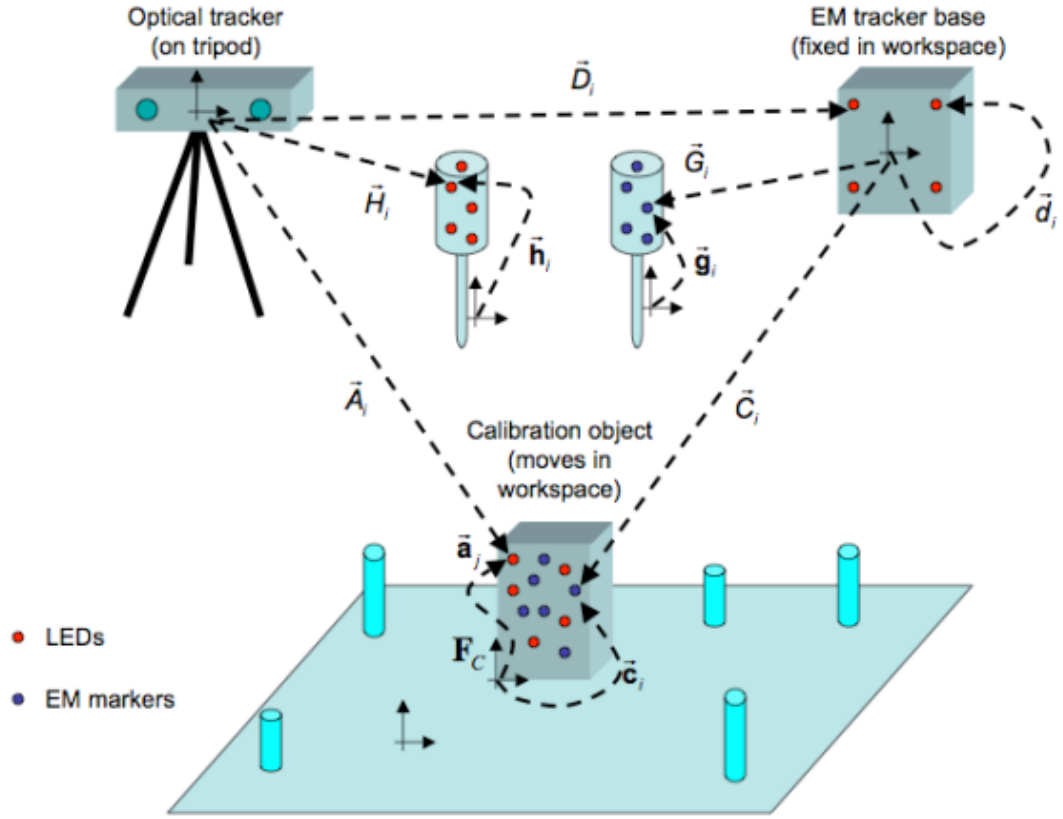
Contents

1 Introduction

1.1 PA1

The purpose of PA1 was to develop an algorithm for a 3D point set to 3D point set registration and a pivot calibration. The problem involved a stereotactic navigation system and an electromagnetic positional tracking device. Tracking markers were placed on objects so the optical tracking device and an electromagnetic tracking device could measure the 3D positions of objects in space relative to measuring base units. These objects were then registered so that they could be related in the same coordinate frames. Pivot calibration posts were placed in the system so pivot calibration could be performed and the 3D position of two different probes could be tracked throughout the system. The diagram below from the assignment document gives a visual description of the system.



1.2 PA2

In addition to all of the steps outlined in PA1, the core purpose of PA2 was to develop an algorithm for distortion correction and to implement it for use with the stereotactic navigation system of PA1. In addition to distortion correction, we performed registration of the device coordinate frames to prior CT coordinate frames.

2 Mathematical Approach

2.1 Distortion Correction

A number of distortion correction methods are available to correct for inaccuracies among various sensor coordinate systems and the real physical dimensions of the world. We seleced Bernstein polynomials for our implementation due to their numerical stability and accuracy for the specific electromagnetic distortion problem we encounter. The basic idea in this case is to construct a 3D polynomial representing the spatial flexing caused by distortions in measurements.

To reap the best of the numerical stability properties of the Bernstein polynomial we scale the input values to the range from 0 to 1. Therefore we scale the values to within the range [0,1] in each dimension, utilizing the minimum bounding rectangle (MBR) to determine the scale factor. Then, we construct a 5th degree Bernstein polynomial for each point using the polynomial function outlined in slide 18 of the InterpolationReview.pdf lecture notes pictured below.

$$B_{N,k}(v) = \binom{N}{k}(1-v)^{N-k}\, v^{k}$$

We then stack the polynomials to form the F Matrix, although this polynomial can be increased for higher precision or decreased for higher performance as needed. Once we have these polynomials stacked as a large matrix we solve the least squareds problem utilizing SVD against the ground truth data, as outlined on slide 43 of the lecture notes pictured below.

$$\begin{bmatrix} \vdots & & \vdots \\ F_{000}(\vec{\mathbf{u}}_s) & \cdots & F_{555}(\vec{\mathbf{u}}_s) \\ \vdots & & \vdots \end{bmatrix} \begin{bmatrix} c^x_{000} & c^y_{000} & c^z_{000} \\ \vdots & \vdots & \vdots \\ c^x_{555} & c^y_{555} & c^z_{555} \end{bmatrix} \cong \begin{bmatrix} \vdots & & \vdots \\ p^x_s & p^y_s & p^z_s \\ \vdots & & \vdots \end{bmatrix}$$

The output of that equation is the calibration coefficient matrix which can then be multiplied by the stacked F matrix of a distorted point set to generate the final corrected and undistorted point set. Multiplication of a stacked matrix is a more efficient alternative to the loop of sums from the slides.

Tradeoffs

One of the particular advantages of Bernstein polynomials is the ability to select the degree of the polynomial. The polynomial degree presents an interesting tradeoff, because a higher degree polynomial allows more precise representation of distortions and lower error. This benefit comes at the cost of an exponential increase in computation time for each additional polynomial degree.

2.2 Point Cloud Registration

A number of least squares methods could be used to determine a transformation matrix for a 3D point set registration. We selected Horn's method because a rotation matrix is always found and no iterative approximation is involved. The first step is to find the centroid of the point clouds in the two different coordinate systems. Then the centroid is subtracted from each point measurement of the separate point clouds so the points will be relative to the centroid. Next an H matrix is created which is the sum of the products of each corresponding point in the two frames. A real symmetric G matrix is then created from the sums and differences of the elements in the H matrix which was previously created. Next, the eigenvalues and corresponding eigenvectors of the G matrix were calculated. The eigenvector corresponding to the most positive eigenvalue represents the unit quaternion of the matrix. Once the quaternion is known, the rotation matrix can be found using Rodriguez's formula. The translation between the two coordinate systems is next found from the difference between the centroid of the known point cloud and the scaled centroid of the unknown point cloud. Finally a homogeneous transformation matrix could be made to know the frame transformation between the two point clouds.

2.3 Pivot Calibration

For the pivot calibration, singular value decomposition was used to estimate the orientation of the probe by finding the positions of the centroid of the tracked markers on the probe and the tip of the probe. First, a matrix was created which consisted of the rotation matrices calculated in each frame and the negative identity matrix found using Horn's method.[1] Next, a vector was created which consisted of the stack of the translation vectors in each frame also found using Horn's method. The singular value decomposition of the matrix was performed to split the matrix into the matrices containing the singular values, the left-singular vectors, and the right singular vectors. Once this was done, the vector between the centroid of the tracked markers on the probe and the probe tip could be approximated using the SVD matrices and the translation vectors of each frame.

- [1] Horn, Closed-form solution of absolute orientation using unit quaternions, Optical Society of America (1987)

3 Algorithmic Approach:

3.1 Parsing

We developed our algorithm using C++. The Eigen library was used as a Cartesian math package for 3D points, rotations, and frame transformations. The Boost library was also used to write a parser file and develop various aspects of our algorithms. The first step was to write parser code that could interpret the given data. The parser needed to interpret which data set was being entered, the number of frames in each data set, and which markers were being tracked in the data set. The parser would store the data as Eigen matrices to be easily used for our algorithms. A diagram below shows how the parser function interpreted and stored the data.

3.2 Transforms

Once the data was parsed, two matrices containing marker positions in different coordinate frames was put in the function hornRegistration to determine the corresponding transformation matrix between the two frames. The first step of the hornRegistration was to find the two centroids of two 3D marker positions and subtract it from each marker position using functions in the Eigen library. The next step was to put these values in a function that would create a 3x3 H matrix. Once this was done, the H matrix could be put in a separate function that would calculate the 4x4 G matrix. The eigenvalues and the corresponding eigenvectors of the G matrix were next calculated by using functions of the Eigen library. A vector of each eigenvalue and the corresponding eigenvector was then created so that the eigenvalues could be sorted to find the most positive eigenvalue and its corresponding eigenvector which represented the unit quaternion of the rotation. Next, the 3x3 rotation matrix was created by an Eigen function that converted a unit quaternion into the corresponding rotation matrix. Finally, the translation vector between the two centroids was

calculated and a 4x4 homogeneous transformation matrix was created by using another function that takes a rotation matrix and a translation vector and outputs the corresponding transformation matrix.

3.3 Pivot Calibration

Next a pivot calibration algorithm was created which used both the parser and hornRegistration algorithms mentioned above. First, the tracker data was parsed into separate matrices which corresponded to each frame of tracked data. Each matrix of frame data was compared to the base matrix frame using the hornRegistration function described above and the corresponding homogeneous transformation from the base frame to the current frame was found. The rotational component of each frame was put into an Eigen matrix and the translational component of each frame was put into an Eigen vector with the form described in the mathematical approach above. The function of JacobiSVD of the Eigen library was then used to solve the least squares vector between the rotational matrix and translation vectors. The least squares vector contained approximated orientation of the probe and the position of the probe tip.

3.4 Distortion Calibration

Next we create a distortion calibration algorithm, which followed the mathematical procedure outlined above. First, the data was parsed and stored in a large vector so the the maximum and minimum values could be obtained in the X, Y, and Z dimensions of the data set. This data is divided into three portions, the groundTruth and distorted points reflecting the same physical points with some error, and another set of points for which the first two distortion point clouds should be used to undistort this one. Then the values of the data set were scaled to between [0 1] to create a minimum bounding box. We calculate Bernstein polynomials for each point and stack them into the F matrix. The Eigen library is utilized to calculate the SVD of Fc=p, where F is the F matrix of Berrnstein Polynomials, c is the calibration coefficient matrix, and p is the undistorted points matrix that you compare the distorted points to. A separate set of points can be scaled according to the corresponding distortion parameters.

4 Structure of the Program

The software is structured as a set of header only libraries in the include folder, which are utilized by the unit tests, main, and any external libraries that choose to use these utilities.

The most important files include:

File name	Description
DistortionCalibration.hpp	Bernstein Polynomial method of distortion correction.
PA2.hpp	**fiducialPointInEMFrame()** and **probeTipPointinCTFrame()** PA2 #4,6
hornRegistration.hpp	Horn's method of Point Cloud to Point Cloud registration.
PivotCalibration.hpp	Pivot Calibration.
cisHW1test.cpp	An extensive set of unit tests for the library relevant to PA1.
cisHW2test.cpp	An extensive set of unit tests for the library relevant to PA2.
cisHW1-2.cpp	Main executable source, contains cmdline parsing code and produces output data.
parseCSV...	File parsing functions are in **parseCSV_CIS_pointCloud.hpp**.

4.1 Important Functions and Descriptions

Each function includes substantial doxygen documentation explaining its purpose and usage. This documentation can be viewed inline with the source code, or via a generated html sphinx + doxygen website generated using CMake. Here is a list of the most important functions used in the program is a brief description of each of them.

PA1

EigenMatrix()

Computes the eigenvalues and corresponding eigenvectors from a given G matrix. It outputs a rotation matrix corresponding to the unit quaternion of the largest positive eigenvalue

homogeneousmatrix()

Creates a 4x4 homogeneous matrix from a derived rotational matrix and translational vector

hornRegistration()

Computes the homogeneous transformation matrix F given a set of two cloud points. It is comprised of the various functions listed above

homogeneousInverse()

Computes the inverse of a given homogeneous matrix

registrationToFirstCloud()

Parses the data and runs the hornRegistration function for pivot calibration

transformToRandMinusIandPMatrices()

Creates the A and b components of the form Ax=b for singular value decomposition. A is of the form [Rl-I] while b is of the form [-p] where R is the stack of rotational matrices of the F transformation matrices, I is stack of 3x3 identity matrices, and p is the stack of the translational vectors of the F transformation matrices.

SVDSolve()

Computes the x of the least squares problem Ax=b using singular value decomposition when the stack of matrices in given

Hmatrix()

Computes a sum of the products H matrix given a set of two cloud points

Gmatrix()

Computes a sum of the differences of the given H matrix

pivotCalibration()

Computes the pivot point position from tracking data using the SVDSolve(), registrationToFirstCloud(), and transformToRandMinusIandPMatrices() functions

PA2

CorrectDistortion()

Correct distortions in one point cloud by utilizing distorted and undistorted versions of a second point cloud. Bernstein Polynomials are utilized to perform the correction.

BernsteinPolynomial()

Find the solution to the Berstein polynomial when at varying degrees and points depending on the input.

Fmatrix()

Multiplies the Bernstein polynomial into a matrix so that a function of every degree of i, j, and k are found and a distortion calibration can be done using the matrix.

ScaleToUnitBox()

Calculates maximum and minimum values in the X,Y, and z coordinates of a point cloud and then normalizes the value of every single opint.

probeTipPointinCTF()

Uses measured positions of EM tracker points on the EM probe in the EM frame when the tip is in a CT fiducial and returns the point of the fiducial dimple (solves problem 5).

fiducialPointInEMFrame()

Uses measured positions of EM tracker points on the EM probe in the EM frame when the tip is in a CT fiducial and returns points of the CT fiducial locations in EM frame.

5 Results and Discussion

5.1 Validation

We took several approaches to the validation of our software. These include manual and automatic execution of the supplied test data, the implementation of unit tests to verify the data, and initial integration of continuous integration software to catch errors early. We implemented a battery of unit tests to verify the basic functions and ensure they are running correctly.

5.2 Point Cloud Registration

We have been able to ensure that point cloud to point cloud registration is working correctly by finding the transformation of one point cloud to another and then the opposite. Multiplying these two transformation matrices together resulted in an identity matrix which would be expected. We tested the input data set as well, ensuring that we were within the given tolerance range. Our program produces nearly exact results when the data was run with no error. When error such as EM distortion, EM noise, and OT jiggle, were introduced in the data, our results were still very close to the expected results and were well within our tolerance range. This shows the strength of Horn's method and since it requires no special case exceptions for a solution, we concluded it was the best method of the one's taught in class.

5.3 Calibration

The position of the tip of the probe when calibrate by EM also gave us results well within our tolerance levels. Our results were less accurate when error was introduced, but not to an unreasonable degree.

6 Status of results

We have encountered errors in our software that we have narrowed down to points after the EM distortion calibration steps, because we have been able to verify our Bernstein functions using unit tests and debug data. However, a bug remains in either the steps for calculating Freg or finding each of the CT fiducials. Since the underlying components are largely well tested, we expect the bug to be in the transform or data flow steps of the generateOutputFile() function in cisHW1-2.cpp or the function definitions in PA2.hpp.

6.1 Error Propagation

Barring errors due to software bugs, error propagation can occur based on several sources. If there is systemic biased measurement in a single direction, this can offset error and cause it to propagate along transform chains and even amplify error.

Error sources and propagation can come from a variety of sources, including EM distortion, EM Noise, and OT jiggle. We were able to account for the EM distortion through our distortion calibration functions. It is expected that some amount of EM Noise, distortion, and jiggle will be propagated throughout the system that we are unable to account for.

One example of how error can propagate is if both the optical tracker and EM tracker are off with a common distortion component, it is possible for this information to cause the bernstein curve to misestimate the actual curve, and consequently cause the registration between the CT scan and the other sensors to have a higer error. In this way errors can propagate through the whole system. This particular example can be mitigated through the use of fixed physical structures that are known in advance that can be used to estimate and account for such systemic errors.

Additionally, inaccurate sensors due to large random variation are an example of error which cannot be removed through distortion calibration.

6.2 Results Metric

We know that our distortion is correct and we can measure its accuracy because we can compare the old values of EM pivot to the newly undistorted values that we encounter. By comparing to prior ground truth values we can assess the accuracy of our calibration.

Our metric for error is the distance difference between our calculations and the debug outputs. This can be measured as an average, or with other statistical tools. We can also detect certain sources of error by specifying our own test functions. We also utilize the **BOOST_VERIFY** macro and the checkWitinTolerances() function to verify that funcions are being called and returning values that or correct to within ceratain tolerances, considering the limits of the particular algorithms we are using.

Andrew and Alex spent approximately equal time on the assignment, with significant amounts of time spent pair programming. Both contributed equally to the implementation and debugging of functions.

7 Additional Information

7.1 Features

Horn Registration

- Point cloud to point cloud transformations .

Pivot calibrations

- Pivot calibrations allow a coordinate system to be established with respect to existing data and the world frame.

7.2 People

Software Development

- Andrew Hundt
- Alex Strickland

7.3 Quick Start

First Steps

The following steps will show you how to

- download and install CIS on your system.
- use the installation to create an example.
- build and test the example project.

You need to have a Unix-like operating system such as Linux or Mac OS X installed on your machine in order to follow these steps. At the moment, there is no separate tutorial available for Windows users, but you can install CygWin as an alternative. Note, however, that CIS can also be installed and used on Windows.

Install CIS

Get a copy of the source code Clone the Git repository from GitHub as follows:

```
mkdir -p ~/local/src
cd ~/local/src
git clone https://github.com/ahundt/cis
cd cis
```

or *Download* a pre-packaged `.tar.gz` of the latest release and unpack it using the following command:

```
mkdir -p ~/local/src
cd ~/local/src
tar xzf /path/to/downloaded/cis-$version.tar.gz
cd cis-$version
```

Configure the build Configure the build system using CMake 2.8.4 or a more recent version:

```
mkdir build && cd build
ccmake ..
```

- Press `c` to configure the project.
- Change `CMAKE_INSTALL_PREFIX` to `~/local`.
- Set option `BUILD_EXAMPLE` to `ON`.
- Make sure that option `BUILD_PROJECT_TOOL` is enabled.
- Press `g` to generate the Makefiles.

Build and install CIS CMake has generated Makefiles for GNU Make. The build is thus triggered by the make command:

```
make
```

To install BASIS after the successful build, run the following command:

```
make install
```

As a result, CMake copies the built files into the installation tree as specified by the `CMAKE_INSTALL_PREFIX` variable.

Set up the environment For the following tutorial steps, set up your environment as follows. In general, however, only the change of the `PATH` environment variable is recommended. The other environment variables are only needed for the tutorial sessions.

Using the C or TC shell (csh/tcsh):

```
setenv PATH "~/local/bin:${PATH}"
setenv CIS_EXAMPLE_DIR "~/local/share/cis/example"
```

Using the Bourne Again SHell (bash):

```
export PATH="~/local/bin:${PATH} "
export CIS_EXAMPLE_DIR="~/local/share/basis/example"
```

Test the Example Excepteur sint occaecat cupidatat non proident, sunt in culpa qui officia deserunt mollit anim id est laborum.

```
./cisHW1main --dataFilenamePrefix pa1-debug-a --dataFolderPath /path/to/cis/data/PA1-2/


PivotCalibration result for pa1-debug-a-empivot.txt:

197.115
192.677
192.437
197.113
192.677
192.434
```

Command Line Format The command line format follows standard conventions, plus the ability to store a response file, typically named *.rsp, which saves additional command line parameters for future use and convenience. The available command line parameters and descriptions for the primary cisHW1main executable file are below.

```
./cisHW1main

    General Options:
      --responseFile arg                    File containing additional command line
                                            parameters
      --help                                produce help message
      --debug                               enable debug output
      --debugParser                         display debug information for data file
                                            parser

    Algorithm Options:

    Data Options:
      --pa1                                 set automatic programming assignment 1
                                            source data parameters, overrides
                                            DataFilenamePrefix, exclusive of pa2
      --pa2                                 set automatic programming assignment 2
                                            source data parameters, overrides
                                            DataFilenamePrefix, exclusive of pa1
      --dataFolderPath arg (=/Users/athundt/source/cis/xcodebuild/bin/Debug)
                                            folder containing data files, defaults
                                            to current working directory
      --dataFilenamePrefix arg              constant prefix of data filename path.
                                            Specify this multiple times to run on
```

```
                                        many data sources at once
--dataFileNameSuffix_calbody arg (=-calbody.txt)
                                        suffix of data filename path
--dataFileNameSuffix_calreadings arg (=-calreadings.txt)
                                        suffix of data filename path
--dataFileNameSuffix_empivot arg (=-empivot.txt)
                                        suffix of data filename path
--dataFileNameSuffix_optpivot arg (=-optpivot.txt)
                                        suffix of data filename path
--dataFileNameSuffix_output1 arg (=-output1.txt)
                                        suffix of data filename path
--dataFileNameSuffix_ct_fiducials arg (=-ct-fiducials.txt)
                                        suffix of data filename path
--dataFileNameSuffix_em_fiducials arg (=-em-fiducialss.txt)
                                        suffix of data filename path
--dataFileNameSuffix_em_nav arg (=-EM-nav.txt)
                                        suffix of data filename path
--dataFileNameSuffix_output2 arg (=-output2.txt)
                                        suffix of data filename path
--calbodyPath arg                       full path to data txt file, optional
                                        alternative to prefix+suffix name
                                        combination
--calreadingsPath arg                   full path to data txt file, optional
                                        alternative to prefix+suffix name
                                        combination
--empivotPath arg                       full path to data txt file, optional
                                        alternative to prefix+suffix name
                                        combination
--optpivotPath arg                      full path to data txt file, optional
                                        alternative to prefix+suffix name
                                        combination
--output1Path arg                       full path to data txt file, optional
                                        alternative to prefix+suffix name
                                        combination
--ct_fiducialsPath arg                  full path to data txt file, optional
                                        alternative to prefix+suffix name
                                        combination
--em_fiducialsPath arg                  full path to data txt file, optional
                                        alternative to prefix+suffix name
                                        combination
--em_navPath arg                        full path to data txt file, optional
                                        alternative to prefix+suffix name
                                        combination
--output2Path arg                       full path to data txt file, optional
                                        alternative to prefix+suffix name
                                        combination
```

Unit Test The easiest way to run the unit test is to build the software, then symlink the data folder "PA1-2" from "data/PA1-2" into the same directory as the unit tests. In other words, the unit tests expect the directory "PA1-2" to be in the same directory as the unit test executable when it is run. The same should be done for the OUTPUT folder to PA1-2-OUTPUT for comparison of debug output files for identifying problems in the system.

```
ln -s /path/to/cis/data/PA1-2
ln -s /path/to/cis/OUTPUT PA1-2-OUTPUT
./cisHW1test
```

Next Steps

Congratulations! You just finished your first CIS tutorial.

Now check out the *Advanced Information* for more details regarding each of the above steps and in-depth information about the used commands if you like, or move on to the various `How-to Guides`.

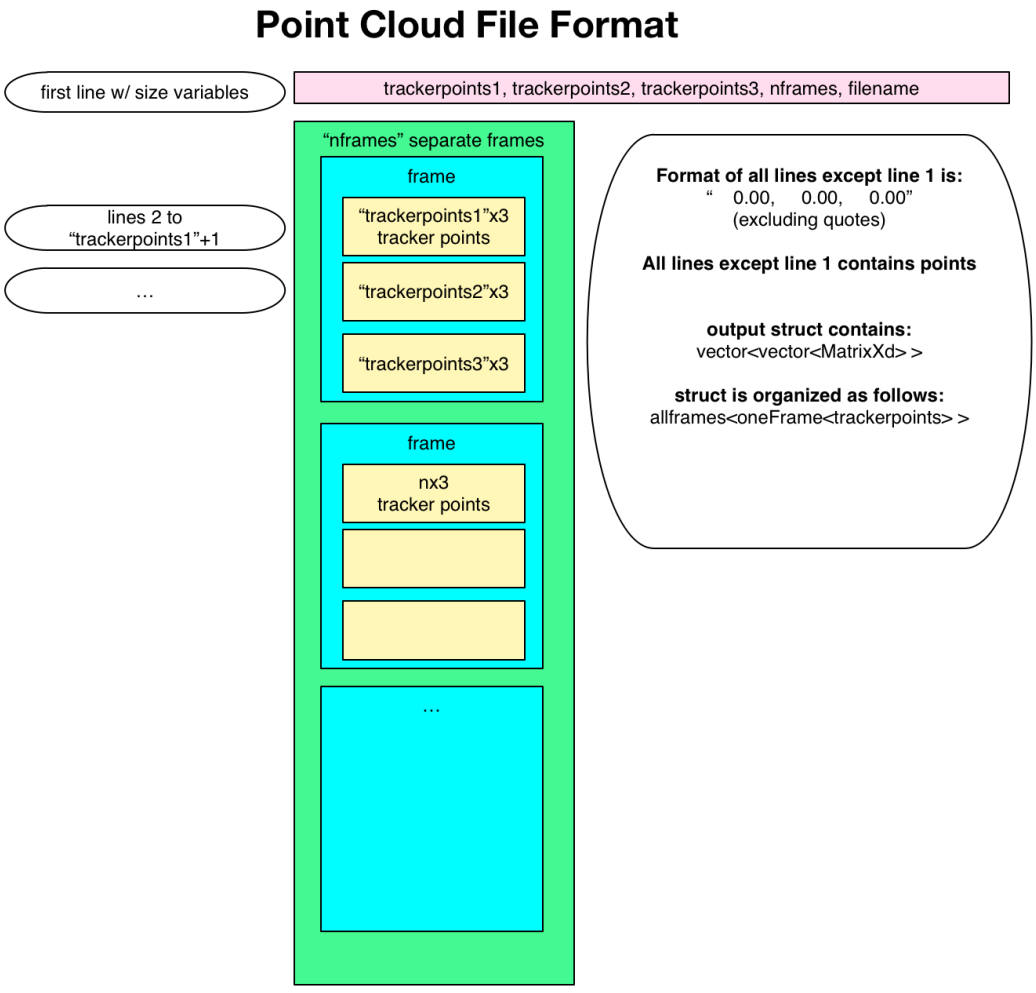
Advanced Information

For advanced documentation, please see the doxygen API documentation, unit tests, software manual. If you cannot view these files and documents, they are visible as inline source code documentation and and restructured text files found in the /doc folder.

For a less comprehensive tutorial-like introduction, please refer to the *First Steps* above.

7.4 Read the Data format

The following image illustrates the basics of the input testing data format.



7.5 Getting Help

Please report any issues with CIS, including bug reports, feature requests, or support questions, on GitHub.

7.6 Reference

Source Package

config/	Package configuration files.
data/	Data files required by the software.
doc/	Documentation source files.
example/	Example files for users to try out the software.
include/	Header files of the public API of libraries.
lib/	Module files for scripting languages.
modules/	Project modules (i.e., subprojects).
src/	Source code files.
test/	Implementations of unit and regression tests.
AUTHORS.md	A list of the people who contributed to this sofware.
BasisProject.cmake	Sets basic project information and lists external dependencies.
CMakeLists.txt	Root CMake configuration file.
COPYING.txt	The copyright and license notices.
INSTALL.md	Build and installation instructions.
README.md	Basic summary and references to the documentation.

7.7 Download

Source Code

The source code of the CMake BASIS package is hosted on GitHub from which all releases and latest development versions can be downloaded. See the `changelog` for a summary of changes in each release.

Either clone the Git repository:

```
git clone https://github.com/schuhschuh/cis.git
```

or download a pre-packaged `.tar.gz` of the latest BASIS release:

- Download CIS v1.0.0 as .tar.gz
- Download CIS v1.0.0 as .zip

See also:

The *Quick Start Guide* can help you get up and running.

System Requirements

Operating System: Linux, Mac OS X, Microsoft Windows

Software License

Documentation

BASIS Manual: Online version of this manual

7.8 Installation

See the BASIS guide on software installation for a complete list of build tools and detailed installation instructions.

Prerequisites

Dependency	Version	Description
BASIS	3.1.0	Utility to automate and standardize creating, documenting, and sharing software.
Boost	1.56.0+	C++ Library collection for general use
CMake	3.0.0	Build Tools.
Eigen	3.2.0	Linear Algebra Library.

Configure

1. Extract source files:

   ```
   tar -xzf cis-1.0.0-source.tar.gz
   ```

2. Create build directory:

   ```
   mkdir cis-1.0.0-build
   ```

3. Change to build directory:

   ```
   cd cis-1.0.0-build
   ```

4. Run CMake to configure the build tree:

   ```
   ccmake -DBASIS_DIR:PATH=/path/to/basis ../cis-1.0.0-source
   ```

   - Press `c` to configure the build system and `e` to ignore warnings.
   - Set `CMAKE_INSTALL_PREFIX` and other CMake variables and options.
   - Continue pressing `c` until the option `g` is available.
   - Then press `g` to generate the GNU Make configuration files.

Build

After the configuration of the build tree, the software can be build using GNU Make:

```
make
```

Test

After the build of the software, optionally run the tests using the command:

```
make test
```

In case of failing tests, re-run the tests, but this time by executing CTest directly with the `-V` option to enable verbose output and redirect the output to a text file:

```
ctest -V >& cis-test.log
```

and attach the file `cis-test.log` to the issue report.

Install

The final installation copies the built files and additional data and documentation files to the installation directory specified using the `CMAKE_INSTALL_PREFIX` option during the configuration of the build tree:

```
make install
```

After the successful installation, the build directory can be removed again.